

Spatio-temporal pattern analysis of MOPITT total column CO using varimax rotation and singular spectrum analysis

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Abstract. In this paper, we apply varimax ~~empirical-orthogonal-function~~ Empirical Orthogonal Function (EOF) analysis to ~~MOPITT~~ Measurement of Pollution in the Troposphere (MOPITT) total column CO retrievals to answer the question of whether or not it is possible to disentangle the dominant CO sources associated with inferred modes of variability at regional to global scales. ~~Additionally, we write this manuscript with the intention~~ This study aims to highlight the strengths and weaknesses of EOF analysis, specifically their usage in the field of atmospheric chemistry. In particular, we highlight an instance where varimax rotation fails to reveal additional spatial structure of a dataset despite being a more advanced technique than standard EOF analysis. Additionally, we emphasize to the reader that the success of EOF analysis to determine linearly independent physical modes relies on both the statistical distribution of the dataset as well as its temporal covariance structure. We analyzed daily MOPITT Version 8 Level 3 joint (TIR-NIR) products from 2005 to 2018, aggregated every 8 days on a 1° by 1° grid. Our findings show that EOF patterns of MOPITT CO are consistent across various regional subdomains, demonstrating that these spatial patterns are independent of the chosen domain. A comparison of the eigenvalue spectrum reveals that unrotated EOF analysis yields three distinct modes, while varimax rotation reduces these to two. The power spectra of the principal components indicate that the first two unrotated modes are primarily driven by annual and semi-annual cycles, while the third mode reflects seasonal variations occurring over roughly three months. To further isolate these modes, we employed singular spectrum analysis (SSA) at each grid point to generate long-term, seasonal, and residual EOF patterns. The power spectrum analysis of the principal components shows that the long-term EOFs replicate the original two dominant modes, while the seasonal EOFs reveal significant variations over 2 to 3 months, and the residual modes exhibit time scales of 2 months or shorter. By plotting the mean skewness field, we show the dataset is non-Gaussian, leading us to conclude ~~each principal component is leading us to conclude its principal components are~~ time-dependent despite being uncorrelated. The periodic decay observed in the temporal auto-correlation function for each time series suggests a classification of wide-sense cyclostationary or wide-sense polycyclostationary behavior. We find the non-stationarity of each time series ~~together with and~~ the temporal dependence of modes leads us to conclude that EOF analysis alone cannot fully disentangle individual CO sources. Consequently, we recommend exploring cyclostationary EOF analysis in future studies. These limitations must be carefully considered when interpreting EOF patterns of other composition datasets with similar characteristics.

1.1 The Role of Carbon Monoxide in Atmospheric Composition

Carbon monoxide (CO) plays an important role in tropospheric chemistry and composition. Firstly, its reaction with the hydroxyl radical (OH) has a significant impact on the atmospheric oxidizing capacity. CO as well as non-methane volatile organic compounds (NMVOCs) are both responsible for positive climate forcing because they raise tropospheric ozone (O_3) and methane (CH_4) by creating a global sink for ~~the hydroxyl radical OH (Fiore et al. (2012))~~ OH (Fiore et al., 2012). The spatiotemporal variations in CO (and hence OH) can lead to changes in O_3 abundance depending on whether the concentration of nitrogen oxides (NO_x) is low or high (Sillman et al., 1990; Jin et al., 2017). Regions of high NO_x experience ~~ozone~~ O_3 production while clean areas with low NO_x experience the destruction of ~~ozone (Holloway et al. (2000))~~ O_3 (Holloway et al., 2000). Because OH is a photochemical sink of CO through oxidation, its global distribution determines the lifetime of CO and therefore, values of CO are lowest with the shortest lifetime in regions with the highest OH. Secondly, CO can also serve as a tracer of pollution transport given its ~~medium-length~~ medium-length lifetime (weeks to months) (Cicerone, 1988). Mainly a product of incomplete combustion of wood and fossil fuels, CO is co-emitted with nitrogen dioxide (NO_2), black carbon (BC), and carbon dioxide (CO_2). It is more concentrated in the atmospheric boundary layer (with less in the stratosphere) so observing CO can be useful as well to study the exchange of these gases and aerosols across the troposphere. ~~Thirdly, as discussed by Gaubert et al. (2020), because~~ Because CO is the main sink of OH (Gaubert et al., 2020), it is important for quantifying losses of ~~methane~~ CH_4 in the troposphere as well (Myhre and Shindell (2013); Gaubert et al. (2016) Gaubert et al. (2017) ; Nguyen et al. (2020)) (Myhre and Shindell, 2013; Gaubert et al., 2016, 2017; Nguyen et al., 2020). The lack of constraints on OH spatiotemporal variability as well as the interannual variability of ~~CH_4 budget (Saunois et al. (2016), Prather and Holmes (2017), Turner et al. (2019))~~ CH_4 budget (Saunois et al., 2016; Turner et al., 2019) . This means there is a need to reduce the uncertainty of primary drivers of OH, including CO, ~~ozone, water vapor, nitrogen oxides, and non-methane volatile organic compounds (Gaubert et al. (2020))~~ O_3 , H_2O , NO_x , and NMVOCs (Gaubert et al., 2020).

Determining the spatial and temporal distribution of CO, along with the distribution of co-emitted species including NO_2 , CO_2 , CH_4 and aerosols, helps us to understand trends of combustion, biomass burning, and other sources of air pollution. For example, Lin et al. (2020b) uses a combined mean and standard deviation approach for total column CO to classify local regions of Southeast and East Asia based on combustion activity into areas of intense urbanization, large-scale biomass burning, regions undergoing significant change from one type to another, and clean regions. Raman and Arellano (2017) utilized variations in enhancement ratios of elemental carbon (EC), CO, and NO_2 to investigate processes driving EC levels across the United States. Tang and Arellano Jr. (2017) demonstrated that local enhancement ratios of $\Delta CO / \Delta NO_2$ can distinguish different combustion types, identifying whether or not a fire was in a flaming phase or smoldering phase while Silva et al. (2013) used $\Delta CO / \Delta CO_2$ to identify combustion efficiency patterns in urban agglomeration. Building on this, Silva and Arellano (2017) combined $\Delta CO / \Delta CO_2$ and $\Delta CO / \Delta NO_2$ to better characterize regional-scale combustion process while Tang et al. (2019) used $\Delta CO / \Delta NO_2$ and $\Delta CO / \Delta SO_2$ to track the common combustion emission pathways across China. Recently, Mottungan

et al. (2024) demonstrated the value of multi-species enhancement ratios (CO , CH_4 , CO_2) along with multivariate regression methods to differentiate between regional and local influences, and identify the dominant processes driving these patterns.

However, determining accurate trends in air pollution is difficult in practice for many different reasons. While there has been an increasing availability of satellite measurements of trace gases and aerosols in the recent decade, most of these remote sensing retrievals cannot ~~in general~~, in general, tell us where their ~~original~~ source or sink was due to the diffusive nature of atmospheric transport (~~?~~)(Murayama et al., 2004). Another challenge is that space-based CO measurements often lack accuracy in areas with persistent cloud cover and near the surface, where thermal infrared sensors struggle due to interference from surface radiation and limited retrieval sensitivity (Clerbaux et al., 2008). These significant sources of uncertainty require us to cross-validate satellites across different instruments as well as with ground and aircraft measurements during field campaigns ~~and is~~, and are especially problematic over areas such as Sub-Saharan Africa, where there are very few air quality monitoring stations (Malings et al., 2020; Gualtieri et al., 2024). Determining the background value of constituents is especially difficult on a global scale because it changes across time and space based on the sources and sinks for a given region and chemical regime (Jones et al., 2003; Wang et al., 2018; Borsdorff et al., 2019). Because satellites measure the total amount of a constituent rather than the source of emission for a given region, it is difficult to tell whether local changes in the overall trend are due to anthropogenic or biogenic sources or the background or residual burden (Novelli, 1999; Tang et al., 2022). As discussed in Buchholz et al. (2021) there are no overall trends in either CO or aerosol optical depth (AOD) in Central/Southern Africa despite the increasing trend in anthropogenic combustion in Central Africa as determined by Zheng et al. (2019) which may be counteracting the global decrease in CO . Buchholz et al. (2021) have also noted that the increase in burning in the region as shown in Andela et al. (2017) may be potentially counteracting transport.

There are also ~~a number of~~ several complex challenges when determining emission inventories. As discussed by Gaubert et al. (2020), emission inventories in China are low in comparison to in situ observations in the case of both forward and inverse models, and in particular there is an underestimation of CO despite having revised inventories ~~(Kong et al. (2020); Feng et al. (2020); Li et al. (2017))~~ (Li et al., 2017; Feng et al., 2020; Kong et al., 2020) as explained by an underestimation of residential coal combustion from either heating or cooling ~~(Chen et al. (2017); Cheng et al. (2017); Zhi et al. (2017))~~ (Chen et al., 2017; Chen et al., 2017). Even though this underestimation of fossil fuel burning does explain the underestimation of Northern Hemisphere (NH) CO in global models ~~(Shindell et al. (2006))~~ (Shindell et al., 2006) this is confounded by the large difference in modeled variability of the regional distributions of OH in the NH, which could offer an alternative explanation ~~(Naik et al. (2013); Young (2013))~~ (Naik et al., 2013; Young, 2013). Gaubert et al. (2020) used observations from the Korea-United States Air Quality (KORUS-AQ) field campaign to investigate this underestimate over East Asia and found that assimilation of CO improves the representation of OH in global chemical transport models by correcting OH/HO_2 partitioning. This also implies that assimilation of CO should ~~be helpful in studying coupled~~ CH_4 help study coupled CH_4 - CO - OH reactions, which allow for chemical feedback. Effectively distinguishing the signature of secondary CO from the influence of surface emissions—whether anthropogenic, biogenic, or from fires—is crucial for enhancing the reliability of source attribution studies, including inverse modeling for air quality assessments and chemistry-climate simulations (Gaubert et al., 2016, 2017; Worden et al., 2019; Gaubert et al., 2020; Miyazaki et al., 2020). This separation also aids in the physical interpretation of observed air pollution patterns, with important implications for

understanding the distributions of both OH and CH₄ (Gaubert et al., 2017; Vimont et al., 2019; Hooghiem et al., 2025). The
95 primary questions ~~that we are interested~~ in this study ~~include~~ are the following:

1. How can we use the spatial and temporal distribution of CO to detect the difference between anthropogenic and natural variability of CO?
2. Can the global background of CO be disentangled from the local-to-regional influences ~~to~~ on observed CO abundance?

In this context, because our analysis is performed in EOF space, we use the term "global background" to refer to a
100 mathematical, non-physical quantity broadly represented as an average. This is different from terminology frequently used in
literature. For example, Menichini et al. (2007) defines a background concentration as the observed concentration at a site "not
affected by local sources of pollution". More recently, Han et al. (2015) described background concentration as the collective
contribution of sources from regional, anthropogenic, natural emissions, and long-range transport.

To attempt an answer to these questions, we ~~will use an empirical orthogonal function~~ use Empirical Orthogonal Function
105 (EOF) analysis, which is a method in pattern analysis to determine the dominant spatial and temporal patterns of a dataset
and is described in ~~full detail in the next section on Methods~~ the Methods section. It has been extensively utilized in cli-
matology, a historical use being from Wallace and Gutzler (1981) who used EOF analysis of geopotential height fields
to produce EOF patterns that we now refer to as teleconnections. It has had fewer applications to atmospheric chemistry,
but for instance Li et al. (2009) ~~use~~ uses varimax rotated EOF analysis of de-seasonalized aerosol index ~~in order~~ to iso-
110 late major dust and biomass burning regions and dust transport. Li et al. (2013) ~~performs~~ performed a similar analysis
on AOD data. Lin et al. (2020a) ~~verifies~~ verified the result of their classification of urban and biomass burning regions
using EOF analysis. Yin et al. (2019) used EOF analysis to analyze the dominant patterns in summer ~~ozone~~ O₃ pollu-
tion over Eastern China and their relationship to atmospheric circulations. ~~The EOF analysis has also seen applications~~
to air quality monitoring. For instance, Eder et al. (1993) uses the principal components corresponding to rotated modes to
115 analyze seasonality of surface ozone concentrations in the Eastern United States. Pires et al. (2008) used principal component
analysis together with cluster analysis to examine monitoring sites and identify emission sources as well as cities with
similar pollution behavior. They successfully applied this method to several species, including CO, O₃, and NO₂. The use
of EOFs in our paper is especially motivated by studies that investigate the global CO budget through source attribution, for
example, see e.g. Granier et al. (1999); Holloway et al. (2000); Duncan et al. (2007); Zheng et al. (2019); Lichtig et al. (2024)
120 . Holloway et al. (2000) used 3D-modeled CO to study the total CO budget by simulating the tagged contributions from fossil
fuel, biomass burning, methane oxidation, and biogenic sources. In doing so, Holloway et al. (2000) was able to reproduce
global patterns in the CO seasonal cycle, most importantly the interhemispheric gradient observed in total CO measurements.
The same gradient was also detected in the fossil fuel tag, which showed that the global CO seasonal cycle can be thought of as
a convolution of the seasonal cycles for individual source terms. Our idea is similar, however, we begin with total column CO
125 in hopes of separating it into patterns that represent the variability of its individual sources and sinks. This is precisely the class
of problem that EOF analysis was designed to solve. Our focus of this ~~current paper will be~~ paper is on the use of EOF analysis
on total column CO data ~~to attempt the separation of~~ in an attempt to separate anthropogenic and biogenic modes of variability

from ~~the background. While EOF a global background. We show that while EOFs~~ have proven useful in climatological studies, this approach has significant limitations that require careful consideration, as detailed in this study.

130 2 Methods

2.1 Data Description

We use total column CO data from the Measurements of Pollution in the Troposphere (MOPITT) instrument, which uses a correlation radiometer from the NASA Terra instrument. Terra flies at a normal altitude of 705 km in a Sun-synchronous polar orbit that passes over the equator at approximately 10:30 and 22:30 local time. The temporal resolution is daily, which has
135 been averaged into 8-day periods, and the spatial pixel resolution is 22 km x 22 km at nadir, resampled to 1° from L3 products. The cross-track scanning angle is ± 26 degrees and yields a swath of approximately 640 km with global coverage every 3 days.

The radiometer performs gas correlation spectrometry for broadband measurements in thermal infrared (TIR) at approximately 2140 cm^{-1} and near-infrared (NIR) around 4725 cm^{-1} (~~Buchholz et al. (2021), Drummond et al. (2010)~~)([Drummond et al., 2010](#); [F
. This is done by modulating either pressure or length of a correlation cell filled with the gas of the target to determine
140 spectral line differences. The TIR is measured using terrestrial thermal radiation, while the overtone band from NIR is measured from reflected solar radiation and enhances retrievals, especially near the surface. Products are available in thermal infrared only, near-infrared only, or joint TIR-NIR, although NIR signals are only available during the day and over land :
\(~~Buchholz et al. \(2017\)~~\)\(\[Buchholz et al., 2017\]\(#\)\). For this study, we use Level 3 data using the V8 retrieval algorithm for TIR-NIR. Level 2 and Level 3 products for MOPITT for the V8 retrieval algorithms \(and ~~its~~ \[their\]\(#\) most recent version, V9\) are
145 publicly available through repositories located at <https://terra.nasa.gov/data/mopitt-data>.](#)

The V8 product includes updates to MODIS cloud cover Collection version 6.1, spectral data for H₂O and N₂ as well as aircraft data from NOAA ~~Deeter et al. (2019)~~([Deeter et al., 2019](#)). This enables a radiance-based bias correction and accounts for both temporal bias drift and bias as a result of water vapor. Daytime retrievals of total column CO for V8 are stable and have a nominal drift of $-0.015 \pm 0.061\%$ relative to NOAA airborne flask sampling during the MOPITT mission. MOPITT
150 measurements have been verified extensively using cross-validation with other satellites, in-situ measurements at the ground, as well as via aircraft, and more recently through ground-based solar Fourier transform infrared spectrometer measurements
(~~Buchholz et al. (2017); ?; George et al. (2015)~~)([George et al., 2015](#); [Buchholz et al., 2017](#); [Martínez-Alonso et al., 2020](#)).

We note that satellite retrievals of tropospheric CO are also available using a multitude of other instruments, including the Atmospheric InfraRed Sounder (AIRS) onboard Aqua ([McMillan et al., 2011](#)), the Tropospheric Emission Spectrometer (TES) on Aura ([Rinsland et al., 2006](#)), the Infrared Atmospheric Sounder Interferometer (IASI) on the MetOp platform
155 ([Clerbaux et al., 2015](#)), the Tropospheric Monitoring Instrument (TROPOMI) ([Borsdorff et al., 2018](#)), and the Cross-track Infrared Sounder (CrIS) ([Nalli et al., 2020](#)). These instruments are all sun-synchronous, capable of measuring CO in the infrared region, and have been shown to have consistent hemispheric CO variability when compared to MOPITT CO records from 2002 to 2018 (in the case of CrIS, from 2015 onward) (~~Buchholz et al. (2021)~~)([Buchholz et al., 2021](#)). Because CrIS was launched
160 in October 2011, it does not have a long or consistent enough period of measurement to be suitable for the determination of

long-term trends of CO. The same applies ~~for TROPOMI~~ to TROPOMI, which was launched in 2017. While CO measurements for IASI-A are long enough to determine trends, they have potential discontinuities ~~due to the fact that since~~ CO retrievals are not done using consistent humidity, temperature, and cloud information (Barret et al., 2025). Measurements from TES ~~are~~ may be up to 2 orders of magnitude fewer than other instruments and are more difficult to verify due to not being collocated (Buchholz et al., 2021). Measurements from AIRS have a long and stable enough record for trend determination and have been shown to reproduce trends from MOPITT (Yurganov et al., 2008), however, AIRS uses a cloud-clearing algorithm that increases global coverage at the expense of increasing ground pixel sizes to 45 km x 45 km, resulting in coarser resolution (Cho and Staelin, 2006).

Our choice of using MOPITT retrievals is because it has the longest available CO record with a verified history of reliable and stable observations and relatively fine spatial resolution. We use daily data averaged to 8-day periods to give us a sufficient resolution to observe CO during its lifetime while also reducing computation time and giving a more consistent overpass time. We also emphasize that for our specific application, daily data would not be sufficient because MOPITT does not have daily coverage, and EOF analysis fails to produce patterns if there are any gaps in the data. Even in using 8-day coverage, we needed to fill a small number of gaps using the inpaintn function offered by MATLAB. We use measurements for the ~~14-year~~ 14-year duration of 2005-2018 ~~so that we to~~ have sufficient data to ~~be able to~~ study long-term patterns. Our data had long-term trends by taking the globally averaged time series and applying a Fourier fit to it. We note that because the trends in the total column data are a non-linear combination of the trends from individual sources, it is not immediately clear what sources may have had their long-term trends removed. Plots are shown below of the spatial (Fig. 1) and temporal (Fig. 2) ~~mean~~ means of de-trended CO for global data over our stated observation period. We will discuss the significance of the variability observed by MOPITT in Sect. 3, focusing on its relationship to the sources and sinks of CO.

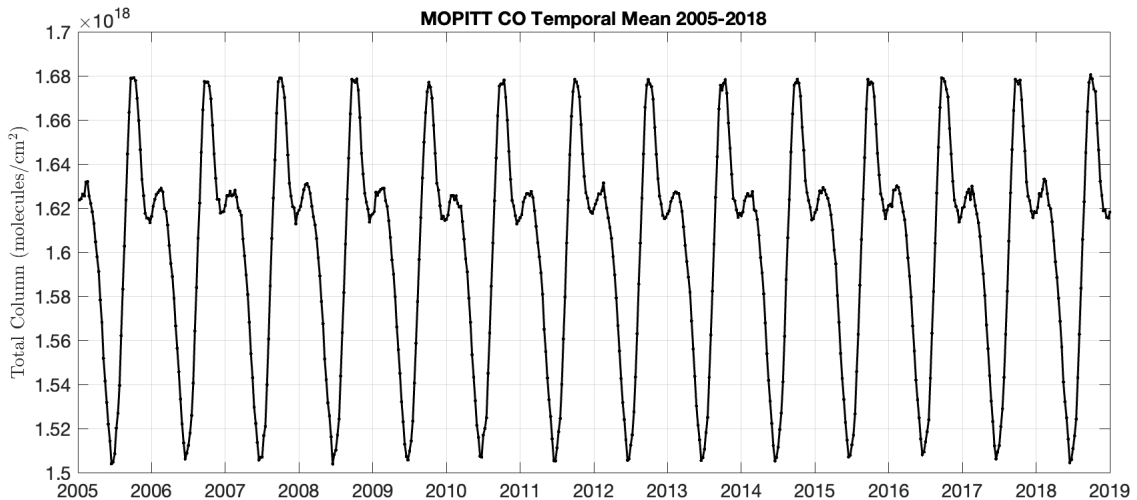


Figure 1. Spatially averaged time series of de-trended MOPITT CO over the period of 2005-2018 across the globe from 60°S to 60°N (in molecules cm⁻²).

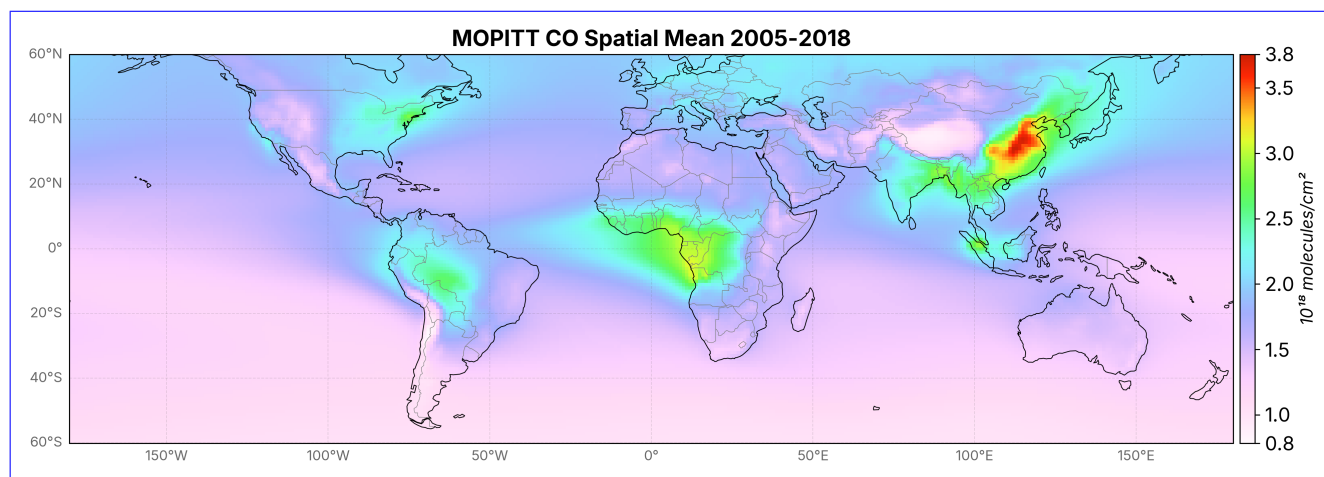


Figure 2. Temporally averaged global map of de-trended MOPITT CO over the period of 2005-2018 across the globe from 60°S to 60°N (in molecules cm^{-2}).

2.2 Source Signatures of CO

Here, we briefly describe the source categories of CO, which include fossil fuel/biofuel burning, biomass burning, biogenic, non-methane hydrocarbon oxidation, and methane- CH_4 oxidation as summarized in [Holloway et al. \(2000\)](#), [Edwards et al. \(2004\)](#), and [Edwards et al. \(2006\)](#). Describing these categories is useful because surface emissions of CO can display unique signatures that may be linked to specific spatial and temporal patterns in observed CO abundance.

CO from anthropogenic combustion (fossil fuel/biofuel burning) is much larger in the NH compared to the [SH-Southern Hemisphere \(SH\)](#), which is attributed to significantly more fossil fuel consumption in urban and industrial regions. We consider these areas of high emission to be mostly associated with eastern China, India, the eastern United States, and Western Europe. Historically, eastern China has contributed significantly to anthropogenic emissions [\(Jia et al., 2024\)](#) because of a distinct reliance on coal and biofuel burning [\(Du et al., 2023; Kao et al., 2024\)](#). ~~In recent years, however, recent regulations have shown to make progress toward slowing down emissions~~ [Buchholz et al. \(2021\)](#). ~~China has made significant progress in reducing emissions and improving air quality~~ [\(Greenstone et al., 2021; Li et al., 2024\)](#). This has been the case since 2014 when Premier Li Keqiang declared a "war on pollution", and implemented widespread changes in regulatory policy [\(Greenstone et al., 2021\)](#).

The lifetime of CO is much longer during the wintertime, and high pollution events may persist in the atmosphere for weeks at a time. It is found in general that CO loading tends to reach maximum values in April and minimum values in September [\(Edwards et al. \(2004\)\)](#).

[\(Edwards et al., 2004\)](#). Biomass burning is largest in the ~~Southern Hemisphere-SH~~ and a primary source of CO. Biomass burning consists of burning of savanna, forests, agricultural residue, fuelwood, and animal waste and is most concentrated in

tropical and sub-tropical forests and grasslands Holloway et al. (2000). The largest contributions of fire emissions come from Africa and South America, although fires also occur in Indonesia, the Boreal forests of Canada, Alaska, and Russia, as well as Australia. African NH fires occur in the savanna south of the Sahara Desert and in tropical rainforests north of the equator, while SH fires begin burning in the western portion of the continent near Angola and then spread southeast down the eastern coast. Fires in South America happen on the southern edge of the Amazon rain forest, the cerrado grasslands, and drought-deciduous forests in the south (Edwards et al., 2006). Another distinct feature of CO fire emissions is their timing (Wiedinmyer et al., 2023). While long-term drivers such as land-use and land cover changes, as well as drought conditions, heavily influence fire occurrences, seasonal variations are primarily driven by agricultural burning practices and prevailing weather conditions. The anomalously high CO levels from these fires, coupled with their distinct spatial and temporal variability inherent to biomass burning, provide a more reliable signature for distinguishing fire emissions from other CO sources.

The contribution of ~~methane-oxidation~~ CH₄ oxidation, as well as oxidation from non-methane hydrocarbons (NMHC) ~~represent NMHCs~~ represents secondary sources of CO that are most apparent in the ~~Southern Hemisphere~~. SH. Oxidation from CH₄ represents roughly 28% of the global budget (Folberth et al., 2006) while the biogenic component of NMHCs represents roughly 15% (Duncan et al., 2007). The oxidation of NMHCs includes a wide variety of constituents ~~which includes~~, which include isoprene, terpenes, acetone, as well as industrial and biomass NMHCs. Temperature-dependent (Sharkey and Yeh, 2001) biogenic emissions of isoprenes ~~account for about a third of hydrocarbon emissions. They are considered the most dominant hydrocarbon emissions due to their large annual contribution (400-600 TgC globally (Arneeth et al., 2008)) and their high reactivity with tropospheric oxidants (Atkinson, 2000).~~ Isoprenes are volatile organic compounds that are directly emitted by trees, ~~shrubs, and animals including humans (measurable in breath)~~ and shrubs through their leaves. They are also emitted by animals, including humans, and can be measured through various biological processes, including exhaled breath, perspiration, urine, feces, and tear production (Moura et al., 2023). Terpenes are produced ~~primarily~~ mostly from coniferous forests and are released in higher amounts with warmer weather (Holzke et al., 2006). The largest emissions of hydrocarbons occur in the tropics ~~which is~~, which are primarily from isoprene and ~~occurs because of~~ occur because of the large density of biomass and high temperature conditions. During the NH winter, there is a strong gradient resulting from biogenic emissions that are south of the equator, where the intertropical convergence zone is located, and includes emissions from South America, Southern Africa, and Australia. During the NH Summer biogenic sources contribute more in the NH, resulting in a weaker but still observable gradient. This gradient is significantly stronger for surface observations but is observable at all levels of the atmosphere (Holloway et al., 2000). CO production from ~~methane~~ CH₄ oxidation can be observed across the troposphere and tends to be spatially homogeneous given the longer lifetime of CH₄ (≈ 10 years). It does however, exhibit some seasonality due to chemical loss with its reaction to OH.

The dominant source of oceanic CO is due to sunlight-initiated photolysis of chromophoric dissolved organic matter (CDOM) in the open ocean (Stubbins et al., 2006). CDOM represents the portion of decaying plants and microbes that absorbs light, degrading into CO and other products in the process. The secondary sources of oceanic CO include dark production (the production of CO from CDOM without the presence of sunlight) and emission from phytoplankton (Zhang et al., 2008; Day and Faloona, 2007). While the physical processes that lead to dark production are not well understood, studies have observed it to be temperature

dependent (Von Hobe et al., 2001). The direct emission of phytoplankton is a similar source to CDOM in that CO is produced when exposed to photosynthetic radiation. The primary removal process for CO in the ocean is due to microbial consumption, and secondary removal comes from sea-air exchanges when the ocean releases CO into the atmosphere (Conte et al., 2019). A recent budget for oceanic CO in the Eastern Indian Ocean (Ji et al., 2025) found that CDOM, dark production, and phytoplankton emission accounted for roughly 67%, 30%, and 3% of oceanic emissions, respectively. Microbial consumption accounted for 94% of the removal of oceanic CO while sea-air exchanges only contributed 6%. Overall, the oceanic cycle of CO is not very well understood due to a general lack of observations and the fact that microbial consumption is difficult to predict due to its dynamically changing environmental conditions (Xie et al., 2005).

2.3 Mean Spatial and Temporal Distribution of CO

In this section, we describe the spatial and temporal variations in CO abundance, illustrated in Figs. 1 and 2 using MOPITT retrievals of total CO columns.

In addition to source signatures, the variability in CO (particularly its seasonality) is significantly influenced by its chemical loss with the OH radical. Notably, CO serves as the primary sink for OH, while CH₄ serving only as a secondary sink. A recent study by Bryant and Stevenson (2024) has shown that increased hydrogen can also increase the mixing ratio of CO in the troposphere through photolysis of formaldehyde (HCHO) and reactions and NMVOCs both serve as secondary sinks. Reactions between CO and CH₄ have highly complex non-linear chemical feedback (Prather, 1996, 2007; Prather and Holmes, 2017). This is due to the link between OH and CH₄ as well as the production of OH, which is tied to O₃. In addition to the primary production of OH through photolysis with OH and nitrate (NO₃)O₃, secondary production can also occur through photolysis with VOCs. These secondary reactions cause oxidation with either CO or VOCs to produce O₃ in the presence of NO_x, while also recycling OH in the process (Fiore et al., 2024).

Reports of the inter-annual variability of CO can be identified as fluctuations in the observed gradient of its abundance between the Northern and Southern Hemispheres NH and the SH. This gradient is driven by the significant differences in surface emissions between the hemispheres, along with the associated air mass exchange that occurs over a year, respectively, on timescales of a year or longer. To a first approximation, CO concentrations are lowest where OH abundance is highest, as CO's chemical lifetime is strongly dependent on reactions with OH. These areas are characterized by having high photochemical activity (solar radiation), as well as high concentrations of O₃ and NO_x, and correspond to continental regions during the summer. On the other hand, oceanic (remote) regions during the winter correspond to areas with the lowest OH and therefore the highest CO. However, the transport and mixing of surface emissions complicates this first-order relationship.

Seasonal differences in the distribution of OH and the imbalance of emission emissions in each hemisphere lead to a North-South gradient in CO that is clearly visible during the NH winter but is absent in the NH Summer. During the NH winter, low OH in the NH lead leads to high CO, while high OH in the SH lead leads to low CO. This in turn reinforces large NH anthropogenic emissions from Europe, North America, and Asia that peak during early spring time springtime which leads to a steep gradient during the NH winter. During the NH summer, we instead have low CO in the NH, but high CO in the SH, which balances a much lower budget of emissions of CO in the SH.

270 Significant changes in the annual cycle have been connected to fire emissions due to biomass burning, and limited studies have connected variability in the SH to climate indices where biomass burning is the primary driver. In the NH, fires from Boreal forests in North America and Eurasia have been shown to contribute to significant interannual variability. In the SH, while fires in southern Africa and South America generate overall high CO loadings, a primary driver of variability is due to fires in the Maritime Continent and Northern Australia. Buchholz et al. (2018) were able to use multilinear regression with four climate indices (~~ENSO, IOD, TSA, and AAO~~) to explain the variability of CO across the ~~Southern Hemisphere and tropics~~ SH and tropics, including Maritime SEA, two subregions in each of Australasia, Southern Africa, and South America. The indices used to explain variability included the El Niño Southern Oscillation (ENSO), the Indian Ocean Dipole (IOD), the Tropical South Atlantic Sea Surface Temperature Anomaly (TSA), and the Antarctic Oscillation (AAO) (Trenberth, 1997; Gong and Wang, 1999; Saji, 2003; Kucharski and Joshi, 2017). They found that more than 50% variability is explained over all regions, and more than 70% variability was explained across maritime ~~SEA~~ Southeast Asia and North Australasia. The fire intensity and burned area are connected to the amount, type, and dryness of fuel availability, which depend on climate-sensitive water availability and ecosystem responses. This indicates that SH interannual variability of CO loading has a clear but complex dependence on climate.

2.4 EOF Analysis

285 2.4.1 Overview of EOF Analysis

The following is a simplified description of EOF analysis. A more complete description can be found in ~~Hannaehi et al. (2007), Björnsson and Venegas (1997), Wilks (2011), Hannaehi (2021), and von Storch and Zwiers (2003)~~ Björnsson and Venegas (1997); von Storch and Zwiers (2003). The exposition presented here is ~~fairly involved because we wish to provide readers both practical and technical foundations that are detailed and specifically~~ tailored for the use of EOF analysis in atmospheric chemistry datasets, especially because most references approach the subject from the perspective of meteorological applications. We present key equations relevant to our main discussion, while derivations are provided in Appendix A. We do this to ~~simultaneously provide a tutorial for future atmospheric chemistry students, as well as to highlight both the strengths and the limitations of EOF analysis in our findings~~ emphasize the use of EOFs in atmospheric chemistry while keeping our discussion focused on their strengths and limitations rather than straying too far into technicalities.

295 Assume that we have a set of n observations in time of a gridded field with a total of m gridpoints. Let f_{ij} where $i = 1, 2, \dots, n$ and $j = 1, 2, \dots, m$ represent the value of the field observed at time i and location j , then the data is represented by the $n \times m$ matrix F :

$$F = (\mathbf{f}_1, \mathbf{f}_2, \dots, \mathbf{f}_n)^T = \begin{pmatrix} f_{11} & f_{12} & \cdots & f_{1m} \\ f_{21} & f_{22} & \cdots & f_{2m} \\ \vdots & \vdots & \ddots & \vdots \\ f_{n1} & f_{n2} & \cdots & f_{nm} \end{pmatrix}$$

$$300 \quad F = (\mathbf{f}_1, \mathbf{f}_2, \dots, \mathbf{f}_n)^T = \begin{pmatrix} f_{11} & f_{12} & \cdots & f_{1m} \\ f_{21} & f_{22} & \cdots & f_{2m} \\ \vdots & \vdots & \ddots & \vdots \\ f_{n1} & f_{n2} & \cdots & f_{nm} \end{pmatrix}. \quad (1)$$

~~so every~~ Every row of F represents a $1 \times m$ vector corresponding to a single observation in time across all grid points.

We now construct the anomaly matrix F' that represents the departure from normal climatology by removing from each grid point its corresponding mean across time. This is done by taking F and individually subtracting the mean for each of its m columns. Instead of constantly referring to F' as the anomaly matrix, we will simply refer to it as F from now on.

315 Our goal for EOF Analysis will be to decompose the anomaly matrix F into a matrix of orthogonal spatial patterns called the EOF modes C , and a set of uncorrelated time series Φ such that

$$F(x, t) = \lambda_1 \phi_1(t) c_1(x)^T + \lambda_2 \phi_2(t) c_2(x)^T + \cdots + \lambda_p \phi_p(t) c_p(x)^T = \sum_{k=1}^p \lambda_k \phi_k(t) c_k(x)^T$$

$$F(x, t) = \lambda_1 \phi_1(t) c_1(x)^T + \lambda_2 \phi_2(t) c_2(x)^T + \cdots + \lambda_p \phi_p(t) c_p(x)^T = \sum_{k=1}^p \lambda_k \phi_k(t) c_k(x)^T \quad (2)$$

310 where $p \leq r$, ~~with $r = \text{rank}(F) \leq \min(n, m)$~~ , and $r = \text{rank}(F)$ which satisfies:

$$\underline{r \leq \min(n, m)}. \quad (3)$$

The number of modes p to retain in the truncation is always chosen such that the maximum percent variance of the original dataset can be explained using the new set of basis functions. The data is compressed more when fewer modes of variability are kept in the expansion.

315 This decomposition can be accomplished by phrasing the question in the form of an optimization problem. ~~We will find uncorrelated linear combinations of the p spatial patterns $C = (c_1, \dots, c_p)^T$ such that the resulting projected time series $\Phi = FC$ have maximum variance and are uncorrelated. In terms of the $m \times m$ spatial covariance matrix $R = \frac{1}{n} F^T F$:~~

~~The maximization problem to be solved for C such that:~~

$$\underline{c_k^T R c_k = \frac{1}{n} \|F c_k\|^2 \text{ is maximized, with } c_k^T c_k = 1 \text{ for } k = 1, \dots, p.}$$

320 If we define $\lambda_k = \frac{1}{n} \|F c_k\|^2 \geq 0$ The maximization problem is equivalent to solving the eigenvalue problem given by:-

$$RC = C\Lambda$$

where $\Lambda = \text{diag}(\lambda_1, \lambda_2, \dots, \lambda_p)$, which is described in Appendix A1.

325 So From our discussion in Appendix A1, we see that the EOF spatial patterns C correspond to the eigenvectors of the spatial covariance matrix R , and of F . We can similarly show that the PC time series Φ correspond to the projections $\Phi = FC$ corresponds to the eigenvectors of the temporal covariance matrix of F . It is important to note that because the covariance matrix R is symmetric and positive semi-definite it has, they have non-negative eigenvalues with well-defined square roots as well as orthogonal eigenvectors. An equivalent formulation is to use singular value decomposition on F , so we expand it into unitary matrices Φ and C and a matrix $\Sigma = \Lambda^{1/2}$

$$\Sigma = \Lambda^{1/2} \tag{4}$$

330 of singular values such that:

$$F = \Phi \Sigma C^T.$$

$$F = \Phi \Sigma C^T. \tag{5}$$

335 Using this expression for F , we can verify using direct substitution that the EOF spatial patterns C are indeed the eigenvectors of the spatial covariance $R = \frac{1}{n} F^T F$, and additionally that the PC time series Φ are the eigenvectors of the temporal covariance $L = \frac{1}{n} F F^T$. Note that in the case that each column of F represents a different observed field, it should also be divided by its standard deviation so that the covariance matrix then becomes a correlation matrix. In our case, because F represents the total column concentration of CO, the units are consistent across columns. Therefore, the use of either covariance or correlation is acceptable. We note however, that our total column values are large in magnitude (they are measured in molecules cm^{-2}), so we choose to use correlation matrices to avoid potentially having large differences in the variance, skewing our interpretations.

345 In Appendix A2, we detail exactly how the EOF patterns and PC time series can be computed in Matlab either using SVD or MATLAB either using singular value decomposition (SVD) or by using eigendecomposition on R or L the spatial or temporal covariance matrices and then projecting the resulting eigenvectors onto the original matrix F . While using SVD is stable computationally, it In Appendix A3, we verify that these two methods are equivalent. Even though both methods are matrix factorizations for the original matrix F , SVD is generally preferred because it is more stable computationally

(Trefethen and Bau, 2022). This is because SVD uses a diagonal matrix of singular values (the square roots of the eigenvalues), which is always constructed to be non-negative. Unfortunately, SVD may require too much computing power in the case that F is very large because. This is because it requires us to compute eigenvectors of both the spatial covariance R and the temporal covariance L . When-Because the spatial grid is-in our problem was large, then $\dim(R) \gg \dim(L)$ and we-decompose-, so we decided to forego using SVD in favor of an eigendecomposition on L . On the other hand, if the number of observations is-had been large, then $\dim(L) \gg \dim(R)$ and we instead-will-decompose-would have instead used an eigendecomposition on R . An even better alternative that is considerably faster for large matrices with no loss of stability is to use Lanczos iteration to solve the eigenvalue problem as-detailed-in-Toumazou-and-Cretaux-(2001)- (Bennani and Braconnier, 1994; Toumazou and Cretaux, 2001) . Lanczos iteration is faster for larger matrices because it relies on Krylov subspaces to compute the largest eigenvalue first (Kuijlaars, 2006). While Lanczos iteration is more efficient, it is more complex to execute and therefore goes beyond the scope of our discussion.

2.4.2 Separation of Modes Using the North Test

Assuming that the p eigenvalues have been sorted in descending order of magnitude (this is done automatically in SVD algorithms but not necessarily in eigendecompositions), then the percent variance that is accounted for by the m th- m^{th} mode is given by Hannachi et al. (2007):

$$\% \text{ var} = \frac{\lambda_m}{\sum_{k=1}^p \lambda_k} \times 100\%.$$

$$\% \text{ var} = \frac{\lambda_m}{\sum_{k=1}^p \lambda_k} \times 100\%. \quad (6)$$

Because of correlations between variables (spatial autocorrelation in F), it-is-not-possible-for- F to-can't have truly independent samples. The sampling uncertainty for the eigenvalues can be estimated by using a variety of methods, including Asymptotic Approximation, Probabilistic PCA-Principal Component Analysis (PCA), Monte-Carlo Resampling Methods, or Bootstrapping (Hannachi-(2021))- (North et al., 1982; Kim and North, 1993; Tipping and Bishop, 2002; Hendrikse et al., 2009; Hannachi, 2021). In our paper, we only consider the use of asymptotic expansions because it is the only method out of the ones listed that does not rely on resampling. We take this approach not only because of simplicity, but because resampling would become computationally cumbersome given the large size of our data matrix.

To avoid confusion with language, we clarify that the term EOF analysis refers to the usage of PCA (a statistical technique used to reduce dimensionality) when it is applied to the fields of climate science and geophysics. While the two methods are virtually identical, the use of EOF analysis implies that the principal components being found are not just linearly uncorrelated, but they are also being used to explain the maximum amount of variance possible in the original dataset.

In this paper, we emphasize the asymptotic method as described by North et al. (1982) who established an estimate of the typical error $\Delta\lambda_k$ between two neighboring eigenvalues to be:

$$\Delta\lambda_k \approx \sqrt{\frac{2}{N^*}} \lambda_k$$

380 $\Delta\lambda_k \approx \sqrt{\frac{2}{N^*}} \lambda_k$ (7)

~~so we see that~~ We see that according to (7), the error in each eigenvalue in is proportional to its magnitude. ~~Because~~ Since this approximation relies on the central limit theorem and the law of large numbers, it is valid as long as the effective number of independent samples N^* is large.

According to Hartmann (2016), N^* ~~is~~ can be estimated in terms of a ~~red-noise~~ first-order stationary autoregressive Gaussian process (AR1) ~~time series defined by exponentially decaying autocorrelation. If $a = r_1(\Delta t)$ is the autocorrelation at one time step Δt , then~~ also known as red noise. By assuming N is large and that our process is AR1, we use the estimate for N^* ~~for first order processes is approximated in terms of the true sample size N as:-~~

$$N^* = N \left(\frac{1-a}{1+a} \right).$$

given by (Bartlett, 1935; Jones, 1975; Bretherton et al., 1999; Hartmann, 2016):

390 $N^* = N \left(\frac{1-a}{1+a} \right).$ (8)

~~This expression is not accurate for the case of non-Gaussian red noise. North~~ We derive (8) in Appendix A4, and clarify the reasoning for these assumptions. North et al. (1982) also gives an estimate for the error between eigenmodes (c_k is the EOF for λ_k) as:

$$\Delta c_k = \left(\frac{\Delta\lambda_k}{\lambda_j - \lambda_k} \right) c_k$$

395 $\Delta c_k = \left(\frac{\Delta\lambda_k}{\lambda_j - \lambda_k} \right) c_k,$ (9)

which shows that large errors in eigenvalues will also cause large errors in a neighboring EOF mode. When there is a significant overlap between the error bars of adjacent eigenvalues, it is a good indicator that these modes are either degenerate due to being contaminated by error, or potentially represent white noise. One downside of using this approach is that this estimation is inexact and inherently subjective. A more robust way to determine if the eigenvalues correspond to modes that have genuine spatial structure is to subject them to a stochastic null-hypothesis test (see e.g. Dommenget (2007); Montano and Jombart (2017)).

2.4.3 Weaknesses of EOF Analysis

While EOF analysis can be used as a very powerful tool to compress data and determine dominant modes of climate variability, the method suffers from numerous potential limitations. EOF modes have been extensively found to suffer from the following major drawbacks in comparison to Rotated EOFs (REOFs) (~~Hannachi (2021); Richman (1986)~~)(Richman, 1986; Hannachi, 2021) :

1. Domain Dependence
2. Subdomain Instability (Non-locality)
- 410 3. Sampling Error
4. Inaccurate Representation of Physical Phenomena

Domain dependence is a problem that was first reported by Kaiser (1958). Buell (1978) determined that the primary factor that determines the shape of an EOF was not its covariance structure, but rather the shape and size of the domain (also Lehr and Hohenbrink (2024)). This is ~~very immediately a~~ an immediate problem, as the covariance structure contains the features of our data and allows us to separate it into different modes of variability. Buell (1978) also showed that it is possible to find several different correlation functions that have a very similar structure over the same domain.

Sub-domain instability is closely related to the issue of domain dependence and references the lack of invariance when EOFs from a given domain are compared to those generated from localized subdomains (~~Richman (1986)~~). ~~In order for~~ (Richman, 1986). ~~For~~ for instance, for instance, an EOF to be physically insightful, it should be the case that EOF patterns over Africa and Asia should reproduce those generated globally. If this ~~was were~~ not the case, the modes generated would be impossible to reproduce with any semblance of consistency. This difficulty is caused by the orthogonality constraint of EOFs, which causes the variance criterion to become maximized globally rather than locally, and leads to the inability of EOF analysis to separate independent and localized features that share similar covariance structure ~~with each other (Horel (1981); Monahan et al. (2009))~~ (Horel, 1981; Monahan et al., 2009). This non-locality issue is also consistent with the mixing property for EOFs, which refers to their tendency to take a signal ~~which that~~ begins as a linear superposition of several different independent and potentially uncorrelated signals, and then combine them ~~together in order~~ to maximize variance (~~Hannachi (2021)~~) (Hannachi, 2021). Sampling error between neighboring eigenvalues is an issue that we have discussed in Sect. 2.4.2 of this document, so we will not examine it further here.

The difficulty EOF analysis suffers in expressing physical phenomena is a complex issue, and here we summarize the main points on this topic as discussed in Monahan et al. (2009). The first major issue is that statistical modes generated in EOF analysis do not ~~in general~~, in general, represent dynamical modes that correspond to true physical modes of variability, and in fact hold only under very strict circumstances. This is not unexpected, as the forced orthogonality of modes for EOFs is a mathematical constraint rather than a physical one. In particular, linearized climate models have conditionally orthogonal modes. The linearized barotropic model given in Simmons et al. (1983) does not have orthogonal processes. A more general climate model with conditional orthogonality is given in Monahan et al. (2009).

We should also not expect EOF analysis to produce principal component time series that are truly independent, because in the absence of autocorrelation, we could still have uncorrelated variables that may be related in a nonlinear way. Only in the case that ~~X has a joint Gaussian distribution~~ a probability distribution is jointly Gaussian will it have modes that are uncorrelated and independent. ~~To see this fact, we note that in the case of 2 random variables if X_1 and X_2 are uncorrelated and jointly Gaussian then the associated covariance matrix is diagonal and the joint PDF takes the form~~

$$f_X(x_1, x_2) = \frac{1}{\sqrt{(2\pi)^2 \sigma_1^2 \sigma_2^2}} \exp\left(-\frac{1}{2} \left(\frac{(x_1 - \mu_1)^2}{\sigma_1^2} + \frac{(x_2 - \mu_2)^2}{\sigma_2^2} \right)\right)$$

~~which can be written as:-~~

$$f_X(x_1, x_2) = \frac{1}{\sqrt{2\pi\sigma_1^2}} \exp\left(-\frac{1}{2} \left(\frac{(x_1 - \mu_1)^2}{\sigma_1^2} \right)\right) \times \frac{1}{\sqrt{2\pi\sigma_2^2}} \exp\left(-\frac{1}{2} \left(\frac{(x_2 - \mu_2)^2}{\sigma_2^2} \right)\right)$$

$$= f_X(x_1) \times f_X(x_2)$$

~~so therefore X_1 and X_2 are independent~~ This observation is verified in Appendix A5. Without this ~~joint~~ jointly Gaussian assumption, it does not follow in general that uncorrelated random variables are independent. A simple counterexample to this is given in ~~Hannachi 2021~~ where if Hannachi (2021). Suppose we take X to be standard normal, then X and $Y = X^2$ are uncorrelated, but are not independent. The degree to which a field F deviates from Gaussian behavior can be estimated by calculating the skewness:

$$\text{skew}(F) = \left\langle \left(\frac{F - \langle F \rangle}{\text{std}(F)} \right)^3 \right\rangle$$

$$\text{skew}(F) = \left\langle \left(\frac{F - \langle F \rangle}{\text{std}(F)} \right)^3 \right\rangle. \quad (10)$$

Climate data, which has a relatively low degree of skewness, can still be thought of as being Gaussian and therefore having independent principal components.

Some, but not all of these weaknesses in EOF analysis can be resolved using REOFs, but even they come with their own drawbacks, which will be discussed in the next section.

2.4.4 Varimax Rotation

We describe rotated EOFs (REOFs) using the varimax criterion, which are EOFs that have been rotated according to a maximization condition. REOFs are motivated by the need to make EOF patterns more localized, easier to interpret in physical space, and less dependent on the domain. This is accomplished by relaxing orthogonality constraints for the EOFs and/or the uncorrelated constraints of the PCs subject to a specified criterion. Rotations can either be oblique or orthogonal and include more than ten different possible criteria according to Richman (1986). We will only discuss are only concerned with the varimax criterion in detail, which has popularity due to the fact that because orthogonal rotation is less sensitive to changes in the number of variables, and it avoids some convergence issues that can happen during matrix inversion in oblique rotation.

Suppose we begin with an $m \times p$ matrix U_p of the first p leading EOF spatial modes:-

$$U_p = \{u_1, \dots, u_p\}$$

Then the new $m \times p$ matrix of REOF modes B is defined as:-

$$B = U_p Q$$

where Q is a $p \times p$ rotation matrix. In varimax rotation, the matrix Q is chosen to be orthogonal so that it satisfies-

$$Q^T Q = Q Q^T = I_p$$

where I_p is the $p \times p$ identity matrix. The varimax criterion requires maximizing the function $f(B)$ where:-

$$f(B) = \sum_{k=1}^p \left[m \sum_{j=1}^m b_{jk}^4 - \left(\sum_{j=1}^m b_{jk}^2 \right)^2 \right]$$

In plain English, the varimax criterion is named because it In simple terms, the varimax criterion attempts to maximize the sum of the spatial variances of the squared and rotated EOF patterns b_{ij} . Orthogonality is preserved while achieving simplicity by forcing patterns to have magnitude near either 0 or 1 so that each pattern can be easily represented by the linear combination of only a few basis vectors.

One potential drawback ~~from of~~ varimax rotation is that leading patterns produced by globally maximizing variance could potentially be destroyed. Suppose we can obtain the first p leading varimax modes. As p increases and we rotate a higher number of EOF patterns, the rotated EOFs become more localized at the expense of the leading patterns, which may no longer be invariant under the orthogonal transformation.

2.5 Seasonal Decomposition using Singular Spectrum Analysis

Singular spectrum analysis (SSA) is a very powerful tool in time series analysis with a wide variety of applications, some of the more notable ones including forecasting, change point detection, filtering, and detection of spatio-temporal patterns. SSA also has applications to meteorology and air quality monitoring, for instance, Macias et al. (2014) uses SSA on the global surface temperature to separate a multi-decadal oscillation from a secular trend, and Gruszczynska et al. (2019) uses multichannel SSA to perform spatiotemporal analysis for atmospheric, continental hydrology, and non-tidal ocean changes to determine an annual signal for 16 sections depending on the climate zone. Another application is from Espinosa et al. (2022), which uses the time derivative of a resulting SSA signal to detect air quality anomalies.

Broadly, our goal is to take a time series $x = [x_1, x_2, \dots, x_N]$ of length N and then decompose it into a sum of trends, periodic (or quasi-periodic) components, or noise, the sum of which will reconstruct the original series. ~~SSA is accomplished in two main stages: decomposition and reconstruction each of which has two different steps.~~ A detailed description of the method ~~can be found in Golyandina and Zhigljavsky (2013). Here we summarize the main points as discussed in Hassani (2007).~~

~~In stage 1 the decomposition is done by beginning with an embedding where the original 1-D time series is mapped into $K = N - L + 1$ different lagged vectors of length L where L is called the window length, a number that satisfies $2 \leq L \leq N$ and should be large enough to capture a key feature of the data. The L -trajectory matrix X is then a Hankel matrix of size (L, K) where each column is one of the lagged vectors and each element is constant along an anti-diagonal $i + j = \text{const}$.~~

$$X = [X_1, X_2, \dots, X_K] = \begin{bmatrix} x_1 & x_2 & x_3 & \dots & x_K \\ x_2 & x_3 & x_4 & \dots & x_{K+1} \\ x_3 & x_4 & x_5 & \dots & x_{K+2} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x_L & x_{L+1} & x_{L+2} & \dots & x_N \end{bmatrix}$$

is fairly technical, and we therefore refer the reader to summaries found in Hassani (2007) and Golyandina and Zhigljavsky (2013) for a more complete description. We perform a seasonal decomposition on the mean-centered and standardized time series for each grid point of our dataset A by using the `trenddecomp` function in Matlab with one mode of seasonal variability. This gives us

$$\underline{A = LT + S + R} \tag{11}$$

After completing the embedding, SVD is performed on the trajectory matrix by computing the eigenvalues $\lambda_1 \geq \lambda_2, \dots \geq \lambda_L$ and eigenvectors $U_1, U_2, \dots, U_L$ of $S = XX^T$ (since $L < N$). The eigenvectors of $X^T X$ are then computed as $V_i = X^T U_i / \sqrt{\lambda_i}$ ($i = 1, 2, \dots, d$) with $d = \text{rank}(A)$ and the decomposition for X is completed by writing it as a sum of d rank-1 elementary matrices:-

$$X = U \Sigma V^T = X_1 + \dots + X_d$$

where $\Sigma = \Lambda^{1/2}$ is the matrix of singular values.

Suppose that $I = 1, 2, \dots, d$ is the set of indices corresponding to our listing of elementary matrices. The reconstruction stage is begun by splitting the set I into m disjoint subsets so that:-

$$I = I_1 \cup I_2 \dots I_m.$$

The partitioning gives us d_1 elements in I_1 , d_2 elements in I_2 etc. and finally we have d_m elements in I_m so that $d = d_1 + d_2 + \dots + d_m$. This procedure of choosing the m subsets is called eigentriple grouping and allows us to write the reconstruction as m distinct sums:-

$$\begin{aligned} X &= X_{I_1} + X_{I_2} \dots + X_{I_m} \\ &= \sum_{i \in I_1} X_i + \sum_{i \in I_2} X_i + \dots + \sum_{i \in I_m} X_i. \end{aligned}$$

In the case that $m = d$ we reproduce the elementary grouping of rank-1 matrices. The percent variance that a specific group I_p contributes to the total variance is found by taking a ratio of their eigenvalues:-

$$\%var = \frac{\sum_{i \in I_p} \lambda_i}{\sum_{i=1}^d \lambda_i}.$$

After the eigentriple grouping is finished a diagonal averaging procedure called "Hankelization" is done to each matrix in the sum by averaging across the antidiagonal elements in the matrix where $i + j = k + 1$ for $k = 1, \dots, N$ in order to create m different time series of length N . We therefore obtain a reconstruction of the original time series:-

$$x = \tilde{x}_1 + \tilde{x}_2 + \dots + \tilde{x}_m$$

where $\tilde{x}_j$ corresponds to the resulting time series after X_{I_j} has been diagonally averaged.

In practice, there is a large amount of subtlety to the eigentriple grouping procedure, however, one important comment is the fact that the ability to extract cycles depends upon the chosen window length L . In general, structure in short-term time series is detected by choosing a smaller window length, and structure in longer-term series is detected by choosing a longer window length. LT is the long-term variation, S is the seasonal variation, and R is the remainder.

3 Results and Discussion

3.1 Domain Independence and Separation of Modes for MOPITT CO

As discussed in Methods (Sect. 2), one of the first potential issues that needs to be addressed ~~in-order~~ to produce physical EOF modes is whether or not the modes capture the local structure and if they are reproducible across differing subdomains. ~~Prior to~~ ~~Before~~ generating EOF modes, our data matrix of size $(longitude, latitude, time)$ is reshaped into size $(time, grid)$, and every grid point is ~~mean-centered~~ mean-centered across time and then standardized. In Fig. 3, we show the first leading EOF mode for the dataset across the entire globe (top left) and then recompute the first mode after subdividing the domain into North American (top right), African (bottom left), and Asian (bottom right). To verify that these spatial patterns did not change over time, we recomputed the EOFs after segmenting the time series by year and determined that the patterns remained unchanged (they only showed negligible differences in magnitude). The spatial structure of the original pattern has been preserved in each of the three subdomains, showing us that the local and global structure for the pattern is the same, and therefore our dataset is independent of its domain.

In some problems, it is often a good idea to attempt varimax rotation ~~in-order~~ to ensure that the resulting patterns are simple and easy to interpret (Kaiser, 1958; Horel, 1981; Richman, 1986), but in our case, there is not a real need to do so because our problem does not suffer from domain instability (Buell, 1975; Richman, 1986). To demonstrate that varimax does not improve our resulting modes, we show the eigenvalue spectrum of the first 6 unrotated EOF modes together with the spectrum of our varimax modes in Fig. 3. Each mode is plotted as a fraction of the percent variance, with the exact value shown at the top. We compute the error bars using the expression for $\Delta\lambda_k$ in Sect. 2.2.2 and plot the results in red. For our unrotated modes, the variance together with error bars (the length above/below each data value) are given by: $61.55 \pm 3.43\%$, $20.52 \pm 1.143\%$, $8.24 \pm 0.459\%$, $3.92 \pm 0.218\%$, $1.10 \pm 0.061\%$ and $0.69 \pm 0.038\%$. After using varimax rotation, the percent variance of each mode was: $86.02 \pm 4.793\%$, $11.56 \pm 0.644\%$, $1.87 \pm 0.104\%$, $0.49 \pm 0.027\%$, $0.03 \pm 0.002\%$ and $0.01 \pm 0.001\%$. While our plots of percent variance for the varimax modes show better representation for mode 1 of every dataset compared to our unrotated modes, all of the remaining modes showed significantly worse representation (except the residual modes). None of these eigenvalues represent degenerate modes because their error bars do not overlap with adjacent neighbors. We note however, that varimax modes 4, 5, and 6 have such a small percent variance that it is unlikely for them to rise above the level of noise and represent independent and important features. On the other hand, the higher modes of our unrotated EOFs have ~~higher-modes~~ ~~with~~ a much larger percent variance and are more likely to represent independent features, with modes 5 and 6 most likely representing noise. It is for this reason that we chose only to perform an SSA decomposition on our unrotated modes.

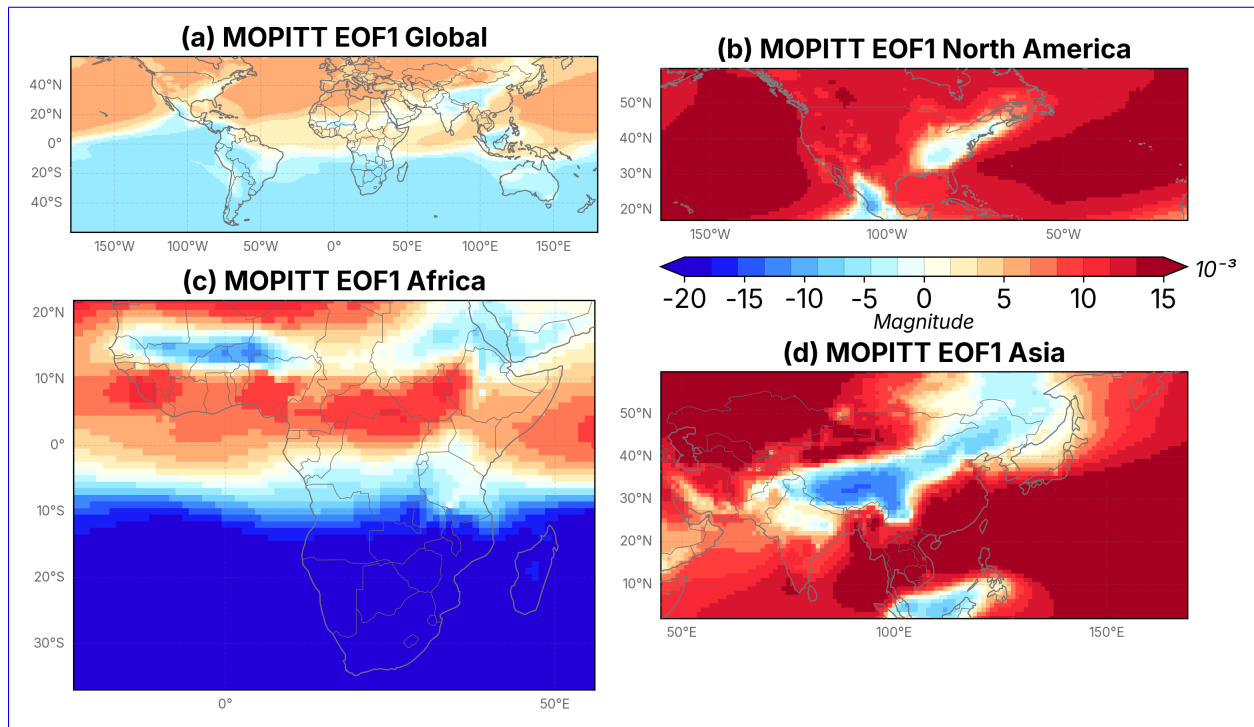


Figure 3. Spatial map showing the first EOF mode of MOPITT CO for (a) the globe, (Top-Left) North America (Top-Right), Africa (Bottom-Left), and Asia (Bottom-Right) Asia. All magnitudes are unitless, and all modes represented have unit norm.

3.2 Seasonal Decomposition for MOPITT CO

560 We perform a seasonal decomposition on the mean-centered and standardized time series A for each grid point of our dataset by using the *trenddecomp* function in Matlab with one mode of seasonal variability. This gives us $A = LT + S + R$ where LT is the long-term variation, S is the seasonal variation, and R is the remainder. To visualize this SSA decomposition, rather than choosing a single grid point as an example, we plot a decomposition for the temporal mean of the dataset in Fig. 5 to show the average overall effect. The result is that the long-term component (bluered) has a yearly periodicity that reproduces the peaks of the original MOPITT series (blackblue), the seasonal component (redgreen) has a shorter temporal periodicity (6 months), while the remainder (dashed, blackorange) shows the shortest periodicity, being on the order of 3 months. Note that in each case, the decomposition is phase shifted with reduced magnitude in comparison to MOPITT.

570 By implementing SSA on each grid point, we produce 3 matrices, each with the same size as our original dataset, which are again mean-centered and standardized. We then conduct EOF analysis on the resulting matrices, displaying the first 3 global modes for MOPITT in Fig. 6 together with the first 3 modes of the long-term, seasonal, and remainder datasets. While there are some differences in magnitude and percent variance, we note that the first two long-term EOF modes reproduce the spatial pattern of the first two modes for the original MOPITT CO patterns. Examination of the third long-term EOF mode shows

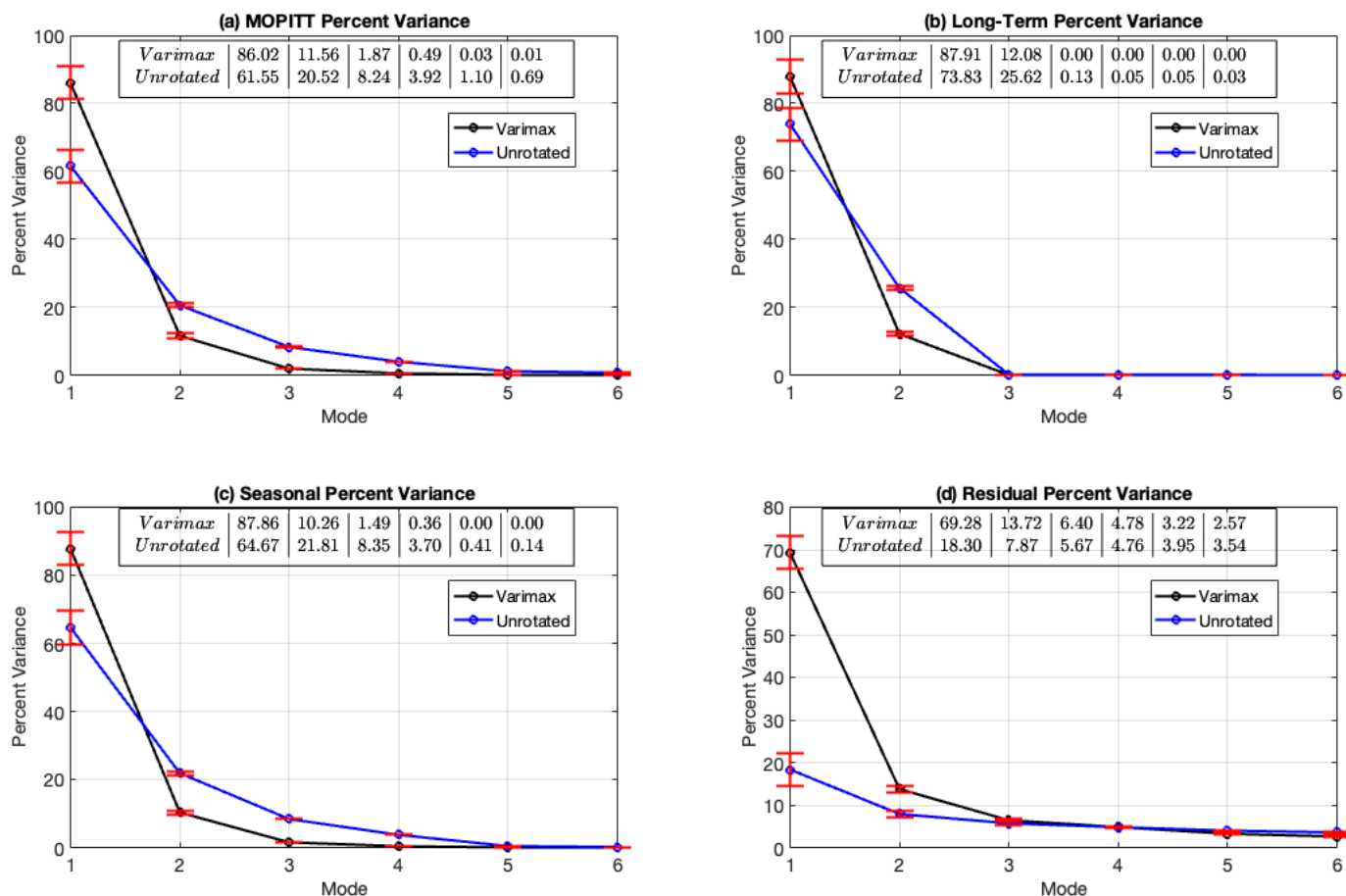


Figure 4. The percent variance that is explained by the first six normalized EOF modes for (a) the original-MOPITT Dataset-dataset and the long-(b) long- term, (c) seasonal, and (d) residual components after using an SSA decomposition. Results are shown globally for both for varimax EOFs (black) and unrotated EOFs (blue). Our error bars computed using the North test are shown in red.

that the pattern appears to be noise, as indicated by the low percent variance and the complete lack of any spatial structure.

575 We also note that there is a very similar structure between the third MOPITT EOF mode and the first Seasonal EOF mode, ; however, the first seasonal mode has a larger contrast between the positive and negative patterns which is especially noticeable in Northeastern Asia and the east coast of the United States. The structure for seasonal modes 2 and 3 as well as all three residual modes represent patterns distinct from our MOPITT EOF modes before we performed SSA on the data.

Our intention in performing EOF analysis was that each EOF mode would represent the variability from either a source or

580 sink in carbon-monoxide, CO; however, the patterns depicted in Fig. 6 do not correlate with physically separable sources. If each mode represented a source of CO, then we would expect to see modes that correlated with variability due to fossil fuel

burning, biomass burning, biogenic oxidation, or ~~methane-CH₄~~ oxidation. However, none of the modes depicted in Fig. 6 show patterns of variability that can be directly connected with source distributions, nor do they appear to directly correspond with synoptic weather patterns or transport pathways.

585 As an example, let us attempt to connect MOPITT EOF 2 with fossil fuel burning. If we attempt the interpretation that blue areas represent areas with high contributions of fuel burning, this would be inconsistent with our knowledge of fossil fuel burning as a source of CO. While we do see significant areas of blue highlighted on the east coast of the United States which is consistent with combustion, the pattern shows too little activity over Eastern China and India and higher activity over Russia than expected. Similarly, when we examine EOF 3, we see a pattern that has some consistency with biomass burning in
590 Africa and South America; however, the features are far too smeared to be a potential interpretation. For example, the pattern stretches too far across oceanic regions as well as the Sahara and ~~Saudia-~~Saudi Arabia to be classified as potential fire activity. For similar reasoning, it would not make sense for us to interpret this as a pattern of biogenic emission.

When examining EOF mode 1, we see a very clear boundary ~~in the Northern and Southern Hemisphere~~ between the NH and SH as indicative of the annual cycle in CO caused by the combination of larger combustion activity and lower hydroxide
595 radicals in the ~~Northern Hemisphere-NH~~ during the winter season. This interpretation is consistent with an observation we state in Sect. 3.3 on spectral analysis and time scales, which is that the time scale for EOF 1 is dominated by annual/semiannual variation.

The majority of the areas with the highest contrast in Residual EOF mode 1 are seen to be over oceanic regions, which ~~leads us to believe there may be~~ suggests the possibility of a connection between Residual mode 1 and oceanic variability. However,
600 these patterns do not match the variation of CO due to oceanic cycles, such as patterns as shown in Conte et al. (2019). This could be because we would expect oceanic variability to be strongest near the surface, and patterns due to surface variations would be obscured by the changes in CO throughout other areas of the atmosphere, which we are accounting for by using total column data. This could also be because budgets for oceanic cycles of CO vary widely both spatially and temporally due to changing environmental conditions (Ji et al., 2025).

605 Examining the remaining seasonal and residual patterns, we see patterns that could be indicative of regional-scale transport; however, verification and further discussion of these modes is beyond the scope of our analysis at this time.

3.3 Spectral Analysis and Time Scales

In Fig. 7, we display the principal component time series for the original MOPITT dataset as well as the long-term, seasonal, and residual components. We first note that the first two long-term principal components have very similar periodic patterns as
610 the original 2 MOPITT modes, while the third mode is ~~of course noise because as we already seen~~, of course, noise because, as we have already seen, the third long-term EOF pattern had no spatial structure. We also see that the first two seasonal components have a similar periodic pattern to the third MOPITT component, even though we saw from Fig. 6 that the second seasonal EOF has a very different spatial structure. The long-term modes have the largest period, while the seasonal components have shorter periodicity, and the residual modes have the shortest.

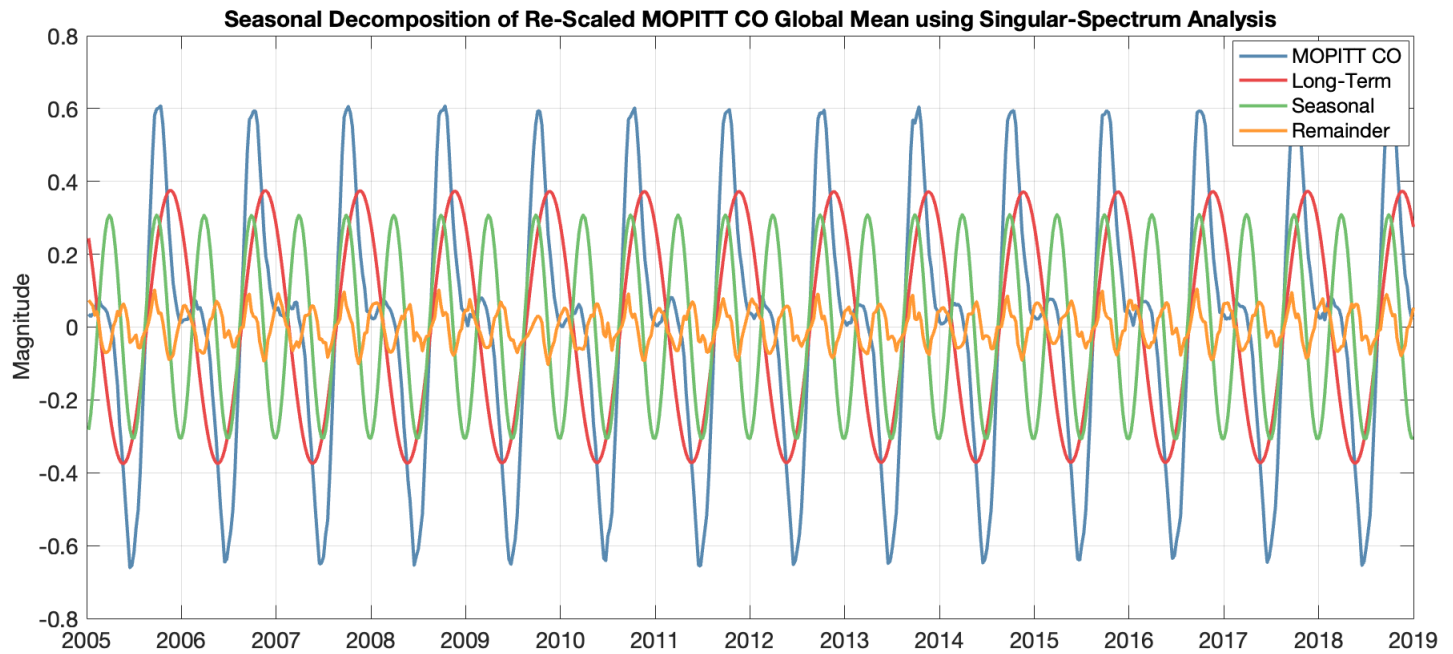


Figure 5. A time series plot of the spatially averaged MOPITT CO global mean (~~black~~blue) and the long-term (~~blue~~red), seasonal (~~red~~green) and remainder (~~black-dotted~~orange) components of the SSA decomposition.

615 ~~In-order-to~~To determine the most dominant time scale for a given mode, we used Fourier transforms to compute the power spectral density of each principal component and then used a numerical trapezoid rule to determine the total cumulative power as a percentage, which is then plotted in Fig. 8 on a logarithmic scale. The percent of total power is labeled for a period of oscillation for 100 days, 1 year, and 1000 days. We note that in this context, having time scales longer than the lifetime of CO still makes physical sense because some variability of CO is driven by large-scale weather patterns.

620 The intrahemispheric mixing time is about 6 months, while interhemispheric mass exchanges can happen across 1-2 years (Bowman and Cohen, 1997). Variability on this time scale could also be indicative of changes to climate drivers. For example, deforestation over several years may lead to long-term reduction of biogenic and fire emissions, while urbanization may lead to an increase of anthropogenic emissions. A dotted line and the value t_{max} ~~indicates~~indicate the period of oscillation ~~which has that~~ contributed the largest amount to the total power. For example, examining ~~Mopitt~~MOPITT Spectrum Mode 1, we see

625 that 1.3% of power is from periods of 100 days or smaller, 26.9% of power is from periods of 1 year or smaller, and 43.2% of power is from periods of 1000 days or smaller. We see that the first two ~~Mopitt~~MOPITT patterns correspond to variation dominated by an annual/semi-annual cycle, while the third mode is dominated by seasonal changes on the order of 3 months. Our long-term EOFs reproduce our original 2 modes, while our seasonal EOFs show dominant time scales on the order of 3 or 2 months, and our residual modes show dominant time scales on the order of 2 months or less.

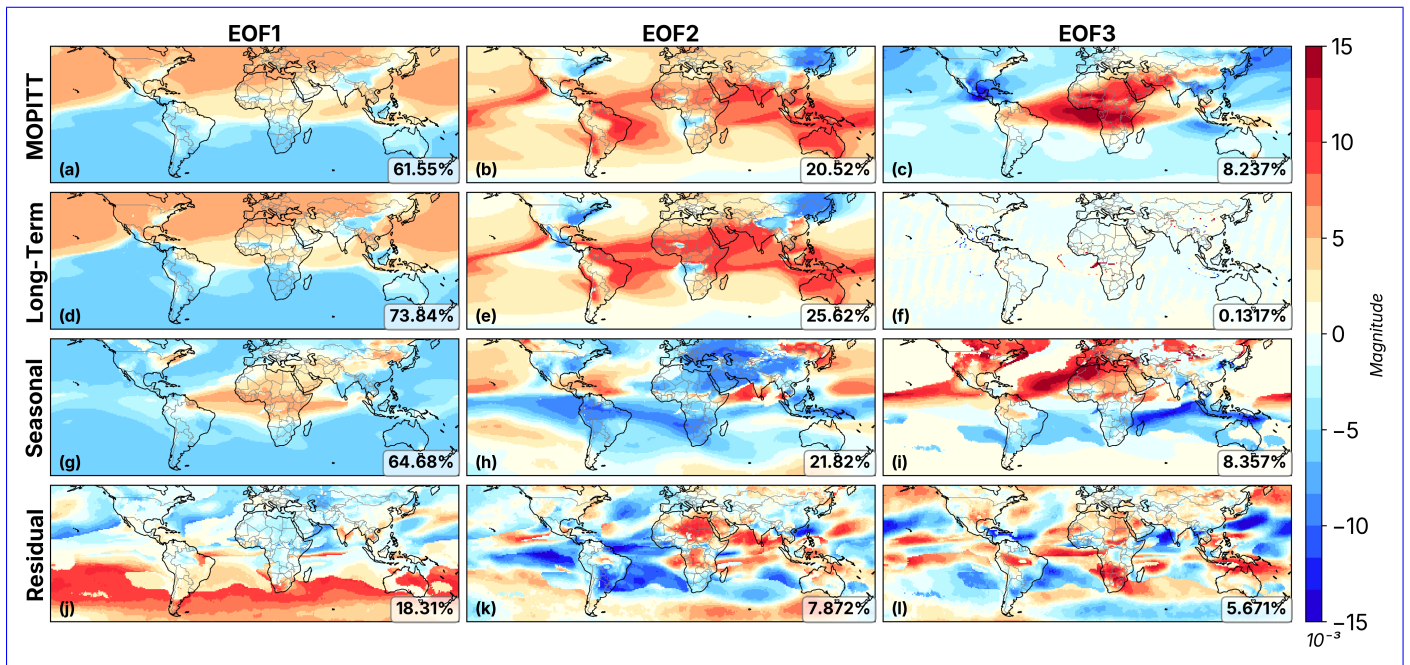


Figure 6. Spatial maps of the first 3 unrotated EOF modes of the (a)-(c) MOPITT dataset and the (d)-(f) long-term, (g)-(i) seasonal, and (j)-(l) residual components after using an SSA decomposition. The percent variance that is explained for each mode is displayed in the bottom right corner. All magnitudes are unitless, and all modes represented have unit norm.

3.4 Time Dependence and Non-Stationarity of Modes

As we have said discussed in Sect. 2.2.3, one weakness of EOF analysis is that even though the principal component time series are constructed to be uncorrelated, it is not necessarily appropriate to assume that they represent independent processes, which complicates the interpretation of assigning physical meaning to the modes. Only in the special case that the data is Gaussian does it follow that uncorrelated random variables are then deemed independent. In Fig. 9, we plot the mean skewness field for MOPITT CO over the period of interest from 2005-2018. It is standard to consider values of absolute skewness less than 0.5 to have negligible skewness corresponding to a relatively symmetric distribution, while values between 0.5 and 1.0 are moderately skewed, and values larger than 1.0 are highly skewed. Contour lines are shown for skewness values of -1, -0.5, +0.5, and +1.0 to highlight areas that have a notable degree of skewness. We see

We note that these sharp gradients in skewness in Fig. 9 are driven by long-term seasonal changes in sources and sinks depending on the region. Regions of low skewness generally indicate places where pollution levels are relatively constant throughout the year, with few extreme highs or lows. High positive skewness values indicate a larger number of extreme pollution events are occurring in the area, and may be interpreted as local enhancement from long-term transport. For example, we interpret the high skewness we see in central Africa as transport due to biomass burning plumes which frequently move westward (Krishnamurti et al., 1996; Fisher et al., 2015). Similarly, large skewness across South America may be indicative of the secondary contribution of isoprene oxidation near the equator. This observation is consistent with Fisher et al. (2015), who

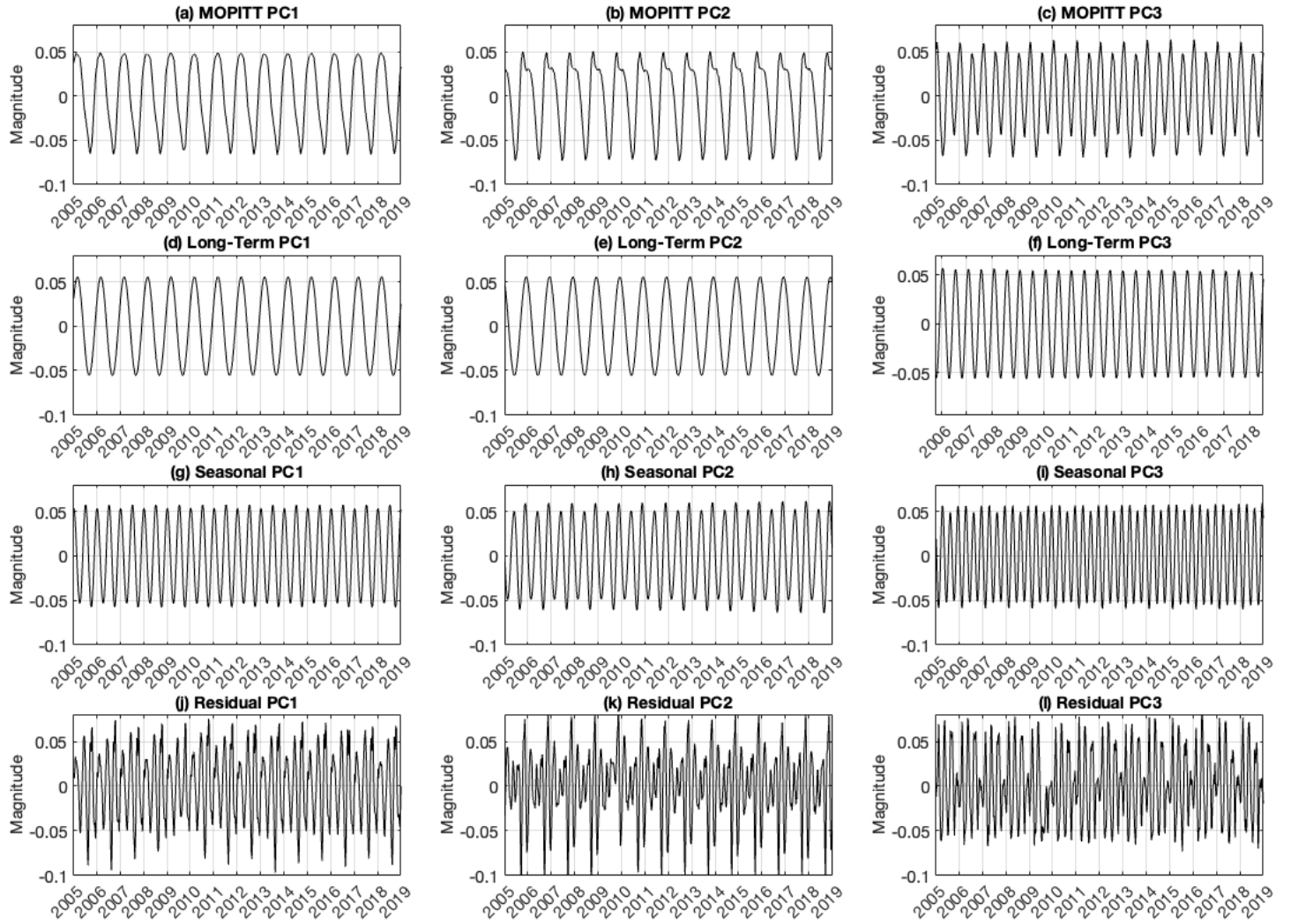


Figure 7. Time series for the first 3 principle-principal components of the (a)-(c) MOPITT dataset and the-its (d)-(f) long-term, (g)-(i) seasonal, and (j)-(l) residual components after using an-a SSA decomposition. All magnitudes are unitless, and all modes represented have unit norm

discuss how isoprene in South America is uplifted to sufficient levels to easily react with OH, where it is slowly transported far south and into the extratropics. The bands with high skewness across the SH are consistent with the north/south movement of the inter-tropical convergence zone due to exchange of CO through the Hadley circulation (Bowman and Cohen, 1997; Bowman, 2006)

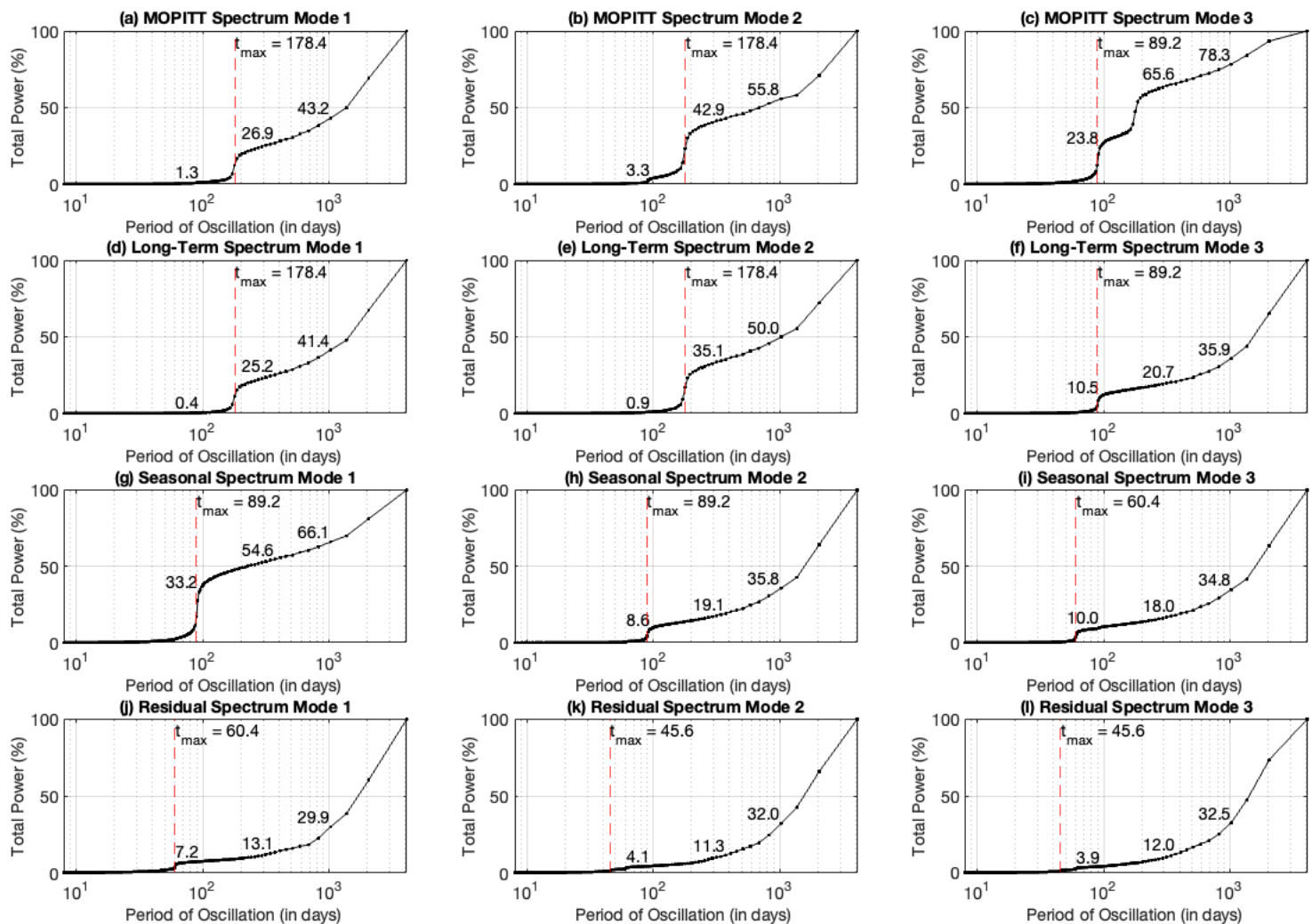


Figure 8. The cumulative percent total power for each principal component. Power values are labeled at 100 days, 1 year, and 1000 days. The dotted line and the value t_{max} indicates-indicate the period of oscillation which-that has contributed the largest amount to the total power.

. The skewness patterns we see in the NH are more diverse, and are indicative of the seasonal changes of fossil fuel usage, which vary by region and sector.

Overall, we see from Fig. 9 that our dataset has significant skewness in the Southern HemisphereSH, especially in South America, as well as over China, Indonesia, and East Asia. This indicates that we cannot consider our dataset to be approximately

Gaussian, and [this](#) is a potential explanation for why our principal components show significant dependence in the distributions of their spectral responses.

655 EOF analysis assumes that the dataset is stationary so that the mean and temporal covariance ~~remains~~[remain](#) constant in time, which is done ~~in-order-to-sure~~[to ensure](#) that the first and second moments (the mean and covariance) of random variables can be determined using a limit of simple summations (or integrals). In practice, this assumption is rarely realistic with physical data. An equivalent statement is that the temporal ~~autorelation~~[autocorrelation](#) is constant as a function of lag time τ . If we consider the mean and covariance of ~~carbon-monoxide~~[CO](#), it would be realistic to assume that these statistics *should* be a
660 function of time because their sources and sinks are correlated temporally. If we imagine a smokestack emitting CO at a fixed location, the CO measured in the future is highly correlated with the amount of CO in the present. This brings us to our next main point, which is that another reason why our modes cannot be interpreted in terms of individual sources and sinks lies in the non-stationarity of the MOPITT dataset, which remains unaccounted for in standard EOF analysis and is a fact we will now show.

665 As shown in Fig. 10, the autocorrelation for the original MOPITT time series as well as each component from the seasonal decomposition, do not decay to zero but instead ~~show~~[shows](#) periodic variation that persists across time. The MOPITT series has a positive correlation that peaks for every year exactly and shows two negative peaks, both of which also ~~reoccur~~[recur](#) at intervals of 1 year. We could therefore consider the MOPITT autocorrelation as being a sum of three periodic components. The long-term and seasonal autocorrelation are simpler functions and both have a single periodic component that ~~peak~~[peaks](#)
670 exactly once per year, and 6 months respectively. The residual autocorrelation~~like MOPITT~~[, like MOPITT](#), is a sum of periodic processes. It is important to note that we *cannot* force the dataset to become stationary by removing an annual cycle, because the autocorrelation represents a superposition of multiple periodic processes. We may therefore consider both the long-term and seasonal series to be wide-sense cyclostationary processes since they have [a](#) periodic temporal mean and a periodic temporal autocorrelation. Because the MOPITT series and residual series are composed of multiple periodic processes, we may consider
675 them to be wide-sense polycyclostationary. We conclude this discussion by recommending the use of cyclostationary EOF (CSEOF) analysis on either the original time series or on the seasonal modes, which is a method that is ~~well-suited~~[well-suited](#) for datasets that possess autocorrelation functions of this type ([Kim et al., 2015](#)).

4 Conclusions

In this study, we investigated the use of EOF analysis and its variants to assess whether source signatures of CO can be identified
680 from observed CO abundance. We hypothesize that the spatial and temporal differences are linked to surface emission patterns, which are intertwined with CO from ~~methane-and-non-methane-hydrocarbons~~[CH₄ and NMHCs](#), atmospheric transport, and reactions with OH. Our results highlight the dominant modes of variability in MOPITT CO columns from 2005 to 2018, with a focus on examining the methodological rationale (limitations) underlying these findings rather than ~~provide physical~~
~~interpretations-on~~[providing physical interpretations of](#) these patterns.

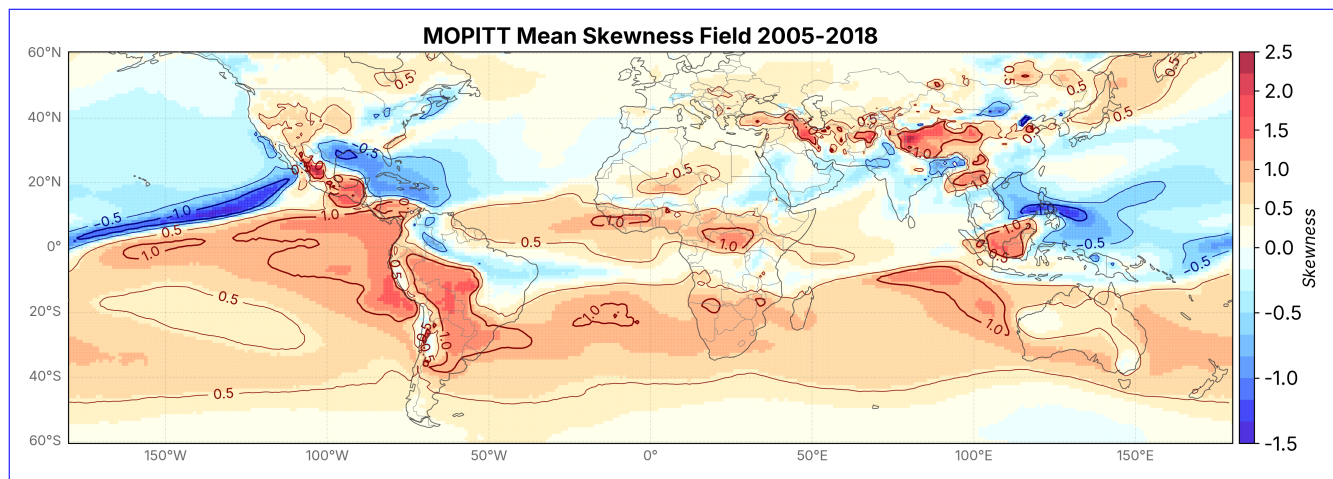


Figure 9. A spatial plot showing the mean skewness field of MOPITT CO from 2005-2018. Contour lines are shown to highlight skewness values of -1.0, -0.5, 0.5, and 1.0, indicating regions that are moderately or heavily skewed.

685 ~~First, our~~ Our results show that the EOF modes of MOPITT CO columns are not domain-dependent, as generating regional domains produced the same spatial patterns as those produced using a global domain. We have also shown that the resulting modes of variability are highly dependent on each other in time.

We used the North test to show that our unrotated modes had better representation than our varimax modes, and as such, we only performed a seasonal analysis with SSA using our unrotated modes. Our decision to only use our unrotated modes in
690 further analysis is due to their increased representation and domain-independence, which are features specific to our individual dataset. This decision is not something that we are recommending to be done in general for climate data, and must be treated on a case-by-case basis.

By examining the seasonal skewness, we verify that even though the principal component time series are constructed to be uncorrelated, they are not independent because the dataset is non-Gaussian, and therefore they do not correspond to potential
695 sources and sinks.

Spectral analysis for the principal components was used to compute the total accumulated power for each of the modes and to show the dominant time scale for each mode. This verifies that lower EOF modes correspond to the effects of long-term variability in the data, while higher modes correspond to the effects of ~~shorter-term variability. Because~~ shorter-term variability.
700 Since each spectrum is continuous with a significant spread of varying frequencies, we see that each mode is produced using a combination of many different time scales rather than an individual.

The first unrotated MOPITT pattern as well as the first long-term pattern are indicative of the annual/semiannual cycle for CO. Because each mode is highly dependent on time, it is very difficult for us to attribute the variability of higher modes for CO with the individual effects of a source or sink and we therefore cannot offer a complete physical interpretations beyond the understanding of what time scale contributed the most to its variability. Part of the reason for having dependent modes in time
705 ~~due to the fact that~~ since we chose to use total column CO data, which may be averaging the modes of variability

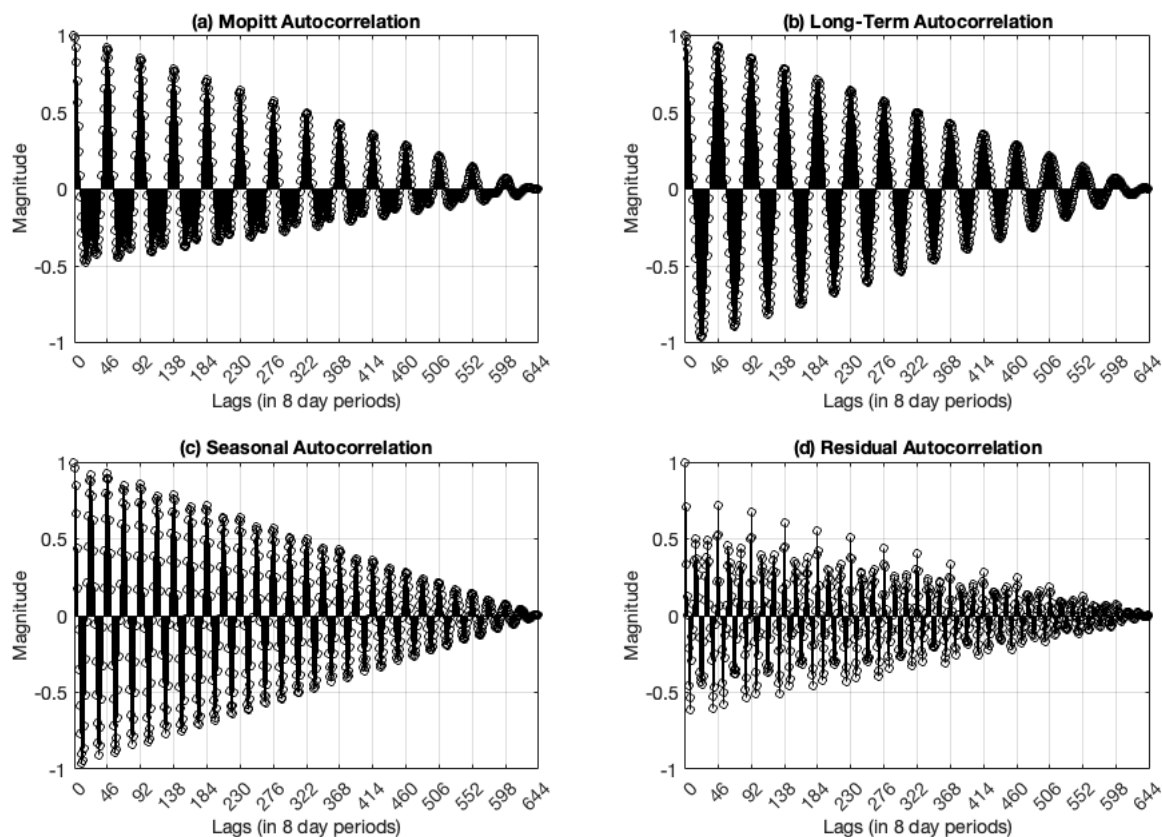


Figure 10. The autocorrelation for (a) MOPITT CO as well as the autocorrelation of the (b) long-term, (c) seasonal, and (d) residual modes after using an SSA decomposition, plotted as a function of lag time (measured in 8-day periods).

together. In future studies, it seems worthwhile to examine the statistics for CO throughout multiple levels of the atmosphere to see whether it is Gaussian or not and whether the spectrum shows ~~behavior that is more time-independent~~ behavior.

As we showed in the autocorrelation functions in Fig. 10, the MOPITT CO time series can be considered to be wide-sense polycyclostationary, and as such, we recommend using CSEOF analysis, which is a method that ~~is able to can~~ handle cyclostationary time series data by assuming that the covariance is a sum of periodic functions of time. This is unlike standard EOF analysis, which uses the major simplification to assume the covariance is stationary (constant in time). In practice, physical modes often have statistics that evolve in time and are an important feature that should be accounted for in the variability of time series data. The use of CSEOF analysis is therefore a more appropriate method to apply to the MOPITT time series data in future analysis, and may be able to separate modes of variability based on the individual sources and sinks of CO.

If this ~~was were~~ indeed possible, then this could have future implications ~~about for~~ the ability of EOF methods to identify biases in chemical transport models. For example, Covariance Discrimination Analysis (CDA) is a method that is able to tell

statistical differences between datasets based on the information content of their covariance matrices (or equivalently their principal components). If we were able to separate physical modes of variability for CO using CSEOFs, we may then be able to use CDA to identify statistical differences between model and satellite variability of CO and then connect differences in
720 each mode to biases in the attribution of individual sources, including fossil fuel and biomass burning, as well as methane-CH₄ and hydrocarbon oxidation. This would be very useful to identify which sources contribute the highest bias when attempting to model the chemical transport of CO.

Finally, we recognize that these limitations result from the convolution of atmospheric transport and mixing's highly diffusive nature with the reactive chemistry of CO and OH, compounded by the limited information content of columnar CO data.
725 These factors make it challenging to distinguish shorter-scale regional source signatures from the longer-scale background CO. Using a multi-species and multi-scale approach to leverage synergies between various data sources, combined with advanced algorithms—such as the previously mentioned pattern recognition techniques, dimensionality reduction, and machine learning—can greatly improve our ability to distinguish these signatures and attribute them to physical processes. This is especially true with the recent availability of higher-resolution atmospheric composition datasets.

730 *Data availability.* The MOPITT V8 joint TIR-NIR L3 datasets can be accessed at the following URLs : https://asdc.larc.nasa.gov/project/MOPITT/MOP03J_8.

Appendix A

A1 Eigenvectors of Temporal and Spatial Covariance Matrices EOF Analysis as an Optimization Problem

We will find uncorrelated linear combinations of the p spatial patterns given by:

$$735 \quad \underline{C} = (\underline{c}_1, \dots, \underline{c}_p)^T \quad (A1)$$

such that the resulting projected time series

$$\underline{\Phi} = \underline{F}\underline{C} \quad (A2)$$

have maximum variance and are uncorrelated. In terms of the $m \times m$ spatial covariance matrix given by

$$\underline{R} = \frac{1}{n} \underline{F}^T \underline{F}, \quad (A3)$$

740 The maximization problem to be solved for C such that:

$$\underline{c_k^T R c_k = \frac{1}{n} \|F c_k\|^2 \text{ is maximized, with } c_k^T c = 1 \text{ for } k = 1, \dots, p.} \quad (\text{A4})$$

If we define the k^{th} eigenvalue as:

$$\underline{\lambda_k = \frac{1}{n} \|F c_k\|^2 \geq 0} \quad (\text{A5})$$

then the maximization problem is equivalent to solving the eigenvalue problem given by:

745 $RC = C\Lambda$ (A6)

where $\Lambda = \text{diag}(\lambda_1, \lambda_2, \dots, \lambda_p)$. Using expression (5), we can verify using direct substitution that the EOF spatial patterns C are indeed the eigenvectors of the spatial covariance (A3), and additionally that the PC time series Φ are the eigenvectors of the temporal covariance

$$\underline{L = \frac{1}{n} F F^T.} \quad (\text{A7})$$

750 **A2 Eigenvectors of Temporal and Spatial Covariance Matrices**

Suppose F is an $n \times m$ matrix where measurements are taken over n points in time and over a spatial grid with m points. We define the $m \times m$ spatial covariance matrix as $R = F^T F$ and the $n \times n$ temporal covariance matrix as $L = F F^T$. Note that here we do not normalize our covariance matrices using the sample size purely to make the rest of this discussion (and the subsequent discussion in Appendix A3) easier to follow. In the case that the number of gridpoints is very large and $n \gg m$,

755 it becomes computationally infeasible to perform an eigendecomposition on R . It is instead desirable to decompose the much smaller covariance matrix L and project the resulting PC time series ~~in-order~~ to compute the EOF spatial patterns, which are eigenvectors of ~~R~~ .

R We begin by performing an eigendecomposition on the spatial covariance matrix R to yield the eigenvector matrix C , which corresponds to the EOF spatial patterns and satisfies:

760 $RC = C\Lambda$

$$\underline{RC = C\Lambda} \quad (\text{A8})$$

Multiplying on the LHS yields:

$$FRC = FF^T FC = LFC \quad (\text{A9})$$

765 and multiplication by F on the RHS then gives us:

$$L(FC) = (FC)\Lambda \quad (\text{A10})$$

And defining $A = FC$ we have:

$$LA = A\Lambda \quad (\text{A11})$$

770 which shows that A is the matrix of eigenvectors for L , while the eigenvalues Λ are the same as for R . We note that while the eigenvectors C of R are size $m \times m$ and represent a spatial pattern, the eigenvector matrix A of L is size $n \times n$ and represents the principal component (PC) time series constructed by projecting the original matrix F onto the EOF patterns C .

~~We are able to~~ We can reconstruct the original matrix F using the EOF spatial patterns and the un-normalized PC time series as:

$$F = AC^T \quad (\text{A12})$$

775 The fact that A is not normalized is apparent from the PCA property of R :

$$A^T A = (FC)^T FC = C^T F^T FC = C^T RC = C^T C \Lambda C C^T = \Lambda \quad (\text{A13})$$

which shows us that $\|A^T A\| = \|\Lambda\| \neq I$. We can therefore define a normalized PC time series Φ by dividing each term by $\lambda^{1/2}$:

$$\Phi = FC\Lambda^{-1/2} = A\Lambda^{-1/2} \quad (\text{A14})$$

780 then it follows that Φ is orthogonal:

$$\Phi^T \Phi = \left(A\Lambda^{-1/2}\right)^T A\Lambda^{-1/2} = (A^T A) \Lambda^{-1} = \Lambda \Lambda^{-1} = I \quad (\text{A15})$$

This expression of Φ is important, because it allows us to express the singular value decomposition of the matrix F as:

$$F = \Phi \Lambda^{1/2} C^T = \Phi \Sigma C^T \quad (\text{A16})$$

If we use the singular value decomposition for F in the covariance matrices, then we recover the eigendecompositions for both R and L :

$$R = F^T F = (\Phi \Sigma C^T)^T \Phi \Sigma C^T = C \Lambda C^T \quad (\text{A17})$$

$$L = F F^T = (\Phi \Sigma C^T)^T \Phi \Sigma C^T = \Phi \Lambda \Phi^T \quad (\text{A18})$$

so we see that orthogonal eigenvector matrices for R and L are the normalized EOF spatial patterns C and the PC time series Φ , respectively.

Therefore, when $n \gg m$ and we cannot easily compute C , our strategy is to perform eigendecomposition on L to find Φ , and then determine C by rearranging the SVD expression:

$$C = (F^T \Phi) \Lambda^{-1/2} = G \Lambda^{-1/2} \quad (\text{A19})$$

where $G = F^T \Phi$. The original matrix F can then be reconstructed using the full rank expression for the SVD. If we are using correlation matrices so that F has zero mean and has been scaled by its standard deviation, the original matrix in physical space F^* is given by:

$$F^* = F \text{std}(F) + \text{mean}(F) = (\Phi \Sigma C^T) \text{std}(F) + \text{mean}(F). \quad (\text{A20})$$

A3 Equivalence of Determining EOFs and PCs Using Eigenvector Decomposition and SVD

In the case of eigenvector decomposition, we will describe cases. When we have $n \gg m$, so the spatial grid is large, then $L = F F^T$ has size $m \times m$, and as described before, we compute the eigendecomposition of L to determine the PC time series, which are the column vectors of Φ . In **Matlab-MATLAB** we would simply use $[\Phi, \Lambda] = \text{eig}(L)$ to compute the normalized eigenvectors and the eigenvalues. We can then compute the matrix G and find the EOF spatial patterns, which are the column vectors of C (or the row vectors of C^T) as shown in (H1C^T).

In the case that $m \gg n$ so the time points are large, then $R = F^T F$ has size $n \times n$ and we first compute the EOF spatial patterns C which are the normalized eigenvectors of R , and are found in Matlab as $[C, \Lambda] = \text{eig}(R)$. We then determine the PC time series Φ using equation (6A2).

When $m \approx n$, then either method from above would be appropriate to compute the EOFs and PCs. It would also be appropriate (and equivalent) to compute the singular value decomposition of F using equation (85) which is determined in matlab as $[\Phi, \Sigma, C] = \text{svd}(F)$, where the singular values Σ are the square roots of the eigenvalues Λ . In this case, the left singular vectors are the normalized PC time series, and the right singular vectors are the normalized EOF spatial patterns.

	$R = F^T F$	$L = F F^T$	SVD
Matlab	$[C, \Lambda] = \text{eig}(R)$	$[\Phi, \Lambda] = \text{eig}(L)$	$[\Phi, \Sigma, C] = \text{svd}(F)$
PC (un-normalized)	FC	$\Phi \Lambda^{1/2}$	$\Phi \Sigma$
PC (normalized)	$FC \Lambda^{-1/2}$	Φ	Φ
EOF	C	$F^T \Phi \Lambda^{-1/2}$	C
F (un-normalized)	$(\text{PC})(\text{EOF})^T$	$(\text{PC})(\text{EOF})^T$	$(\text{PC})(\text{EOF})^T$
F (normalized)	$(\text{PC}) \Lambda^{1/2} (\text{EOF})^T$	$(\text{PC}) \Lambda^{1/2} (\text{EOF})^T$	$(\text{PC}) \Sigma (\text{EOF})^T$

A4 Estimate of N^* in Terms of an AR1 Process

The following is a derivation of N^* , which we use for the estimate for the effective sample size as discussed in Hartmann (2016). Red noise is characterized by the property that future observations are predicted using a linear combination of the previous observations plus a random noise term. Red noise has exponential autocorrelation, which decays according to:

$$r(\tau) = \exp(-\tau/T) \quad (\text{A21})$$

where τ is the lag time and T is the e-folding time (the time interval over which the autocorrelation drops to $1/e$). For a first-order process, note that if we define the autocorrelation at one time step Δt to be:

$$a = r(\Delta t) = \exp(-\Delta t/T) \quad (\text{A22})$$

then the autocorrelation evaluated n time steps in the future can be written as:

$$r_n = r(n\Delta t) = (\exp(-\Delta t/T))^n = a^n. \quad (\text{A23})$$

We can express N^* in terms of the true sample size N as follows (Thiébaux and Zwiers, 1984):

$$N^* = \frac{N}{\sum_{n=-N-1}^{N+1} \left(1 - \frac{|n|}{N}\right) r_n}. \quad (\text{A24})$$

If we further assume that N is very large and that our process is AR1, expression (A24) can be written as:

$$N^* = \frac{N}{\sum_{n=-\infty}^{\infty} r_n} = \frac{N}{1 + 2 \left(\sum_{n=1}^{\infty} a^n \right)} \quad (\text{A25})$$

825 and we see the sum in the denominator of (A25) is a geometric series with $|a| < 1$ which converges to the value:

$$\sum_{n=1}^{\infty} a^n = a + a^2 + \dots = \frac{a}{1 - a}. \quad (\text{A26})$$

Substituting (A26) into (A25) then yields our estimate for N^* given by equation (8) in our methods section. We reiterate that this estimation is only valid for a large number of independent samples and when we assume our time series is an AR1 stochastic process. This is because we rely on the property (A23) of AR1 processes and large N to both be true to guarantee that (A25) is valid. We also rely on N to be large for the sum in (A26) to be accurate.

A5 Jointly Gaussian Distributions Are Independent

In this section, we verify the fact that jointly Gaussian distributions have modes that are uncorrelated and independent. To see this fact, we note that in the case of 2 random variables, if X_1 and X_2 are uncorrelated and jointly Gaussian, then the associated covariance matrix is diagonal and the joint PDF takes the form:

$$835 \quad f_X(x_1, x_2) = \frac{1}{\sqrt{(2\pi)^2 \sigma_1^2 \sigma_2^2}} \exp \left(-\frac{1}{2} \left(\frac{(x_1 - \mu_1)^2}{\sigma_1^2} + \frac{(x_2 - \mu_2)^2}{\sigma_2^2} \right) \right) \quad (\text{A27})$$

which can be written as:

$$f_X(x_1, x_2) = \frac{1}{\sqrt{2\pi\sigma_1^2}} \exp \left(-\frac{1}{2} \left(\frac{(x_1 - \mu_1)^2}{\sigma_1^2} \right) \right) \times \frac{1}{\sqrt{2\pi\sigma_2^2}} \exp \left(-\frac{1}{2} \left(\frac{(x_2 - \mu_2)^2}{\sigma_2^2} \right) \right) \quad (\text{A28})$$

$$= f_X(x_1) \times f_X(x_2). \quad (\text{A29})$$

840 It follows that X_1 and X_2 are independent.

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