

## Response to Community Comment 1

\*We added page numbers and line numbers to the reviewer's comments, which refer to the original document. The page and line numbers of manuscript changes in our responses refer to the "tracked changes" document.

**This manuscript represents a valuable contribution to N<sub>2</sub>O stable isotope science. It provides a suitable approach for including appropriate mass balance considerations in applying the Rayleigh model to position-specific N isotope effects, and points towards a more comprehensive framework for position-specific isotope effects in a broader array of molecules. The level of clarity and detail with which the assumptions of this model are explained, including how they extend and differ from those of the conventional Rayleigh model, is very welcome. Also, the creation and evaluation of the simulated datasets provides great value in showing the strengths and limitations of the Rayleigh model at fitting natural data with error and variations, even beyond the specific application to the Extended Rayleigh model.**

Response: Thank you for your thorough reading of our manuscript, and we are happy to hear that you found it to be a valuable contribution to the field.

**However, given its complexity it is hard to follow in places. Any way that the calculations described in the Methods could be better connected with their outcomes in the Results would be welcome, as would better integration between figures illustrating various datasets and the outcome of calculations based on them. Furthermore, perhaps details regarding plotting and calculations that apply throughout could be consolidated and mentioned only once. Sections of the methods, especially Section 2.8 (P14-15, L241-346) could also be streamlined without eliminating any information, which would improve readability.**

Response: We have revised the first two paragraphs of the Results section to highlight the connection between the data shown in Fig. 1 and the results of calculations with the Expanded Rayleigh model (see below). We also added references to the appropriate figure(s) in other parts of the Methods and Results sections (see below).

Manuscript changes (P23, L416-437, *new text italicized*): "To demonstrate that the standard Rayleigh model produces inaccurate results for the individual nitrogen atoms in N<sub>2</sub>O, idealized, error-free datasets were simulated representing different scenarios with varying combinations of KIEs for N<sup>α</sup> and N<sup>β</sup> (Fig. 1, Table 1). *Because these data were simulated assuming that the fractions of <sup>15</sup>N and <sup>14</sup>N apportioned to each position remain constant (i.e., constant ρ and τ), the distance between δ<sup>15</sup>N<sup>α</sup> and δ<sup>15</sup>N<sup>β</sup> over the course of each reaction is constant, and the rates of change of δ<sup>15</sup>N<sup>α</sup>, δ<sup>15</sup>N<sup>β</sup>, and δ<sup>15</sup>N<sup>bulk</sup> with respect to reaction progress (1-f) are essentially equal (Fig. 1). Thus, when the standard Rayleigh model (Eq. 2) is applied to each dataset, the slopes (ε) of δ<sup>15</sup>N<sup>α</sup>, δ<sup>15</sup>N<sup>β</sup>, and δ<sup>15</sup>N<sup>bulk</sup> against [-f ln f / (1-f)] for each dataset are all approximately equal, as are the corresponding KIE <sup>15</sup>N<sup>bulk</sup>, KIE <sup>15</sup>N<sup>α</sup>, and KIE <sup>15</sup>N<sup>β</sup> values (Table 3). While the standard Rayleigh KIE <sup>15</sup>N<sup>bulk</sup> values match the actual KIE <sup>15</sup>N<sup>bulk</sup> values, the KIE <sup>15</sup>N<sup>α</sup> and KIE <sup>15</sup>N<sup>β</sup> values determined using the standard Rayleigh approach differ significantly from the actual KIEs calculated from simulation input values (Table 3). In each of the five simulated reactions*

(Datasets 1-5), the isotopic preference for  $N^\alpha$  differs from that of  $N^\beta$ , which can be verified visually by noting that the  $\delta^{15}N^\alpha$  values are significantly different than the  $\delta^{15}N^\beta$  values throughout each reaction (Fig. 1). However, in all five cases, the standard Rayleigh model produces KIE values for  $N^\alpha$  and  $N^\beta$  that are approximately equal, highlighting the fact that the standard Rayleigh model inaccurately quantifies  $^{15}N$  apportionment between  $N^\alpha$  and  $N^\beta$ . (*If KIE  $^{15}N^\alpha$  were equal to KIE  $^{15}N^\beta$ , the curves for  $\delta^{15}N^\alpha$ ,  $\delta^{15}N^\beta$ , and  $\delta^{15}N^{bulk}$  shown in Fig. 1 would all be on top of each other.*)

... For example, Dataset 1 represents a scenario where there is no isotopic preference at the  $\alpha$  position, meaning instantaneous  $\delta^{15}N^\alpha$  ( $\delta^{15}N^{\alpha i}$ ) is always equal to  $\delta^{15}N^s$ , *which can be verified visually by noting that accumulated  $\delta^{15}N^\alpha \approx \delta^{15}N^s$  at the start of the reaction (Fig. 1).*”

Manuscript changes (P9, L234): “Idealized, error-free  $\delta^{15}N^\alpha$  and  $\delta^{15}N^\beta$  values (*shown in Fig. 1*) were simulated for the values of  $\rho$  listed in Table 1 by calculating  $\delta^{15}N^\alpha$  and  $\delta^{15}N^\beta$  using Eq. (27) and Eq. (28) (Tables S4-S8).”

Manuscript change (P24): “Table 3. KIE values for  $N^{bulk}$ ,  $N^\alpha$ , and  $N^\beta$  calculated directly from simulation input values (Actual) or from the standard Rayleigh model or Expanded Rayleigh model *applied to error-free simulated datasets.*”

Manuscript change (P25, L470-472): “To test the robustness of the Expanded Rayleigh model, we applied this model to simulated data with error at varying levels of size and skewness (Table 2, Fig. 3, and Figs. S1-S4) and averaged the results from 1000 simulations for each error category (Table 4, Tables S9-S13).”

We have also streamlined the Methods section (including Section 2.8) by consolidating descriptions of calculations and plotting (all done with R) into one new sub-section (Section 2.10). The rest of Section 2.8, however, describes the generation of datasets with simulated error. Our error simulations are designed for a unique system with a gaseous reactant and product (NO and  $N_2O$ ) and must include error calculations for  $\delta^{15}N^\alpha$  and  $\delta^{15}N^\beta$ , unlike the study our method is based on (Scott et al., 2004). Additionally, the simulations have to be described in sufficient detail for these calculations to be reproducible. For these reasons, we feel that the brief explanation of the error levels and skewness values in Section 2.8 is warranted.

Scott, K. M., Lu, X., Cavanaugh, C. M., and Liu, J. S.: Optimal methods for estimating kinetic isotope effects from different forms of the Rayleigh distillation equation, *Geochim Cosmochim Ac*, 68, 433-442, 10.1016/s0016-7037(03)00459-9, 2004.

Manuscript changes (P22, L405-413): “2.10 Modeling, statistical analysis, and figures

*Modeling and statistical analyses of simulated and experimental  $\delta$  values were performed with R statistical software (R Core Team, 2022), and figures were produced with ggplot2 (Wickham, 2016). To determine  $\rho$  for the Expanded Rayleigh model, nonlinear least squares regression was performed as previously described (Baty et al., 2015) using a starting  $\rho$  value of 0.5.*

For datasets with simulated error, random numbers representing simulated error were generated using the *rsn* function from the skew-normal distribution package (Azzalini, 2023), and skewness was calculated with the *moments* package (Komsta and Novomestky, 2022). In the *moments* package, skewness is defined as  $(1/n) \sum ((x - \bar{x})/s)^3$ , where  $n$  is the sample size,  $\bar{x}$  is the sample mean, and  $s$  is the sample standard deviation (Hippel, 2011).

For previously published experimental data, a linear model was used to determine if  $SP$ ,  $\rho$ , or  $\tau$  varied as a function of  $[-\ln f/(1-f)]$ .”

Azzalini, A.: The R package 'sn': The Skew-Normal and Related Distributions such as the Skew-t and the SUN (version 2.1.1). URL <http://azzalini.stat.unipd.it/SN/>, <https://cran.r-project.org/package=sn> [code], 2023.

Baty, F., Ritz, C., Charles, S., Brutsche, M., Flandrois, J.-P., and Delignette-Muller, M.-L.: A Toolbox for Nonlinear Regression in R: The Package *nlstools*, *J Stat Softw*, 66, 1 - 21, 10.18637/jss.v066.i05, 2015.

Hippel, P. v.: Skewness, in: *International Encyclopedia of Statistical Science*, edited by: Lovric, M., Springer Berlin Heidelberg, Berlin, Heidelberg, 1340-1342, 10.1007/978-3-642-04898-2\_525, 2011.

Komsta, L. and Novomestky, F.: *moments: Moments, Cumulants, Skewness, Kurtosis and Related Tests*. R package version 0.14.1, <https://CRAN.R-project.org/package=moments>. [code], 2022.

R Core Team: *R: A language and environment for statistical computing*, R Foundation for Statistical Computing, Vienna, Austria, <https://www.R-project.org/>. [code], 2022.

Wickham, H.: *ggplot2: Elegant Graphics for Data Analysis*, Springer-Verlag New York. [code], 2016.

**The inclusion of both KIE and  $\epsilon$  throughout the manuscript also introduces some potential for confusion. This is mitigated somewhat by inclusion of ‘normal’ and ‘inverse’ in reference to various isotope effects in the text, but perhaps it would be clearer to note the alternative definitions but choose a single parameter to report throughout the text. Relatedly, I think that the definition of a given at line 60 (P2, L60) would be better referenced to Mariotti et al. (1981) or another source, and the cited reference (Bigeleisen and Wolfsberg, 1958) would be more suitable for the definition of KIE (and the overall concept).**

Response: Throughout most of the manuscript, we focus on KIE values, which make it easier to distinguish between normal and inverse isotope effects. For example, Tables 3–6 exclusively list KIE values. However, the simulated datasets were calculated using pre-determined values of  $\epsilon_{N\text{-bulk}}$ , and  $\epsilon_{N\text{-bulk}}$  values are frequently reported in the literature on microbial  $N_2O$  production. Therefore, we have included some reference  $\epsilon_{N\text{-bulk}}$  values to help the reader compare our data to previously reported values. We have added the corresponding KIE values wherever  $\epsilon$  values are listed (e.g., by adding a new footnote for Table 1) so that all of the data within our manuscript can be readily compared.

Manuscript change (P10, L248, Table 1 footnote): “*a Note that an  $\epsilon$  value of -20‰ corresponds to a KIE of 1.0204 and an  $\epsilon$  value of +20‰ corresponds to a KIE of 0.9804.*”

Manuscript change (P7, L192-193): “*... $\epsilon_{N\text{-bulk}}$  was set at either -20‰ (normal KIE,  $KIE = 1.0204$ ) or +20‰ (inverse KIE,  $KIE = 0.9804$ ).*”

Manuscript change (P19, L356, Fig. 3 caption): “*... $\epsilon_{N\text{-bulk}} = -20‰$  ( $KIE^{15N^{bulk}} = 1.0204$ ),...*”

Manuscript change (P28, L514, Fig. 6 caption): “*... $\epsilon_{N\text{-bulk}} = -20‰$  ( $KIE^{15N^{bulk}} = 1.0204$ ),...*”

Manuscript change (P29, L539-541): “*Indeed, the  $\epsilon_{N\text{-bulk}}$  value for  $N_2O$  produced in this experiment ( $5.3‰ \pm 0.4$  for replicate B ( $KIE^{15N^{bulk}} = 0.9947 \pm 4e-04$ , see Table S15) (Sutka et al., 2006)) is similar to the  $\epsilon_{N\text{-bulk}}$  value of  $2.0‰$  ( $KIE^{15N^{bulk}} = 0.9980$ ) reported for purified HAO from *Nitrosomonas europaea* (Yamazaki et al., 2014).*”

We have also replaced the reference at line 60 (P2, L60) with the Mariotti et al. (1981) reference. Bigeleisen and Wolfsberg, 1958 is already cited for the general definition of KIE in section 2.2 (P5, L131).

**Regarding the fungal P450 NOR case study, it was not entirely clear to me why the variation in fractionation over the course of the experiment requires that the Expanded Rayleigh model was applied only to subsets of the dataset. Doing so also limits the comparability of these outcomes to the results of the Standard Rayleigh model. (P16-17, L361-376; P27, L545-575)**

Response: The value of  $\rho$  for the P450 data increased from 0.5039 to 0.5075 during the course of the reaction. Our nonlinear models (Eq. 29 or Eq. 30) for determining  $\rho$ , however, assume that  $\rho$  is constant. Using nonlinear regression to determine  $\rho$  when  $\rho$  changes linearly yields a value of  $\rho$  in between the more extreme values observed at the start and end of the reaction ( $0.5057 \pm 0.0004$ ) and therefore does not represent the data from the overall reaction very well. However,  $\rho$  can be calculated for each individual observation without nonlinear regression using Eq. (23) ( $\rho = {}^{15}N^{\alpha}/{}^{15}N^{bulk}$ ), giving us a way to estimate position-specific KIEs for each timepoint. We chose to list the average KIEs for the beginning and end of the observed extent of reaction to provide an estimate for the range of KIEs for  $N^{\alpha}$  and  $N^{\beta}$ . Even though the new model does not fit this dataset optimally, probably due to a complex combination of equilibrium isotope effects and kinetic isotope effects, as we discussed in the manuscript (P34-35, L665-671), the new model provides KIE estimates that are more accurate than those previously reported using the standard Rayleigh model, and we feel it is important to publish these improved estimates.

Manuscript changes (P20, L376-378): “*Using nonlinear regression to determine  $\rho$  in this case yields a value of  $\rho$  in between the more extreme values of  $\rho$  observed at the start and end of the reaction and does not represent the data from the overall reaction very well.*”

Manuscript changes (P31, L582-585): “*Therefore, using nonlinear regression (Eq. 29 or Eq. 30) to determine  $\rho$  is not appropriate in this case. Using a modified version of the Expanded Rayleigh model, however, we calculated  $\rho$  for each individual timepoint and estimated apparent*

*KIE  $^{15}\text{N}^\alpha$  and KIE  $^{15}\text{N}^\beta$  values for the beginning and end of the observed range of  $f$  values (see Methods section 2.9)."*

Response: You bring up an important point about comparing the results of the two models. To make it easier to compare the results of the standard and Expanded Rayleigh models for the P450 NOR data, we have added the results of using the same approach for the standard Rayleigh model to Table 6. That is,  $\epsilon_{\text{N-bulk}}$  was calculated for each observation without linear regression by solving Eq. (2) for  $\epsilon$ . This approach effectively determines the slope ( $\epsilon$ ) between the y-intercept of a Rayleigh plot and the  $\delta$  value from one individual timepoint. (Note that the y-intercept must still be determined by linear regression of the entire dataset because it is technically challenging to measure this value when the substrate is NO.) Because this approach still relies on determining the slope of a Rayleigh plot, the results are very similar to the normal application of the standard Rayleigh model: Average early KIE  $^{15}\text{N}^\alpha = 1.0130 \pm 0.0031$ ; average late KIE  $^{15}\text{N}^\alpha = 1.0121 \pm 0.0029$ ; average early KIE  $^{15}\text{N}^\beta = 0.9687 \pm 0.0030$ ; average late KIE  $^{15}\text{N}^\beta = 0.9698 \pm 0.0018$ . Thus, this method of applying the standard Rayleigh model also inaccurately predicts the types of isotope effects at  $\text{N}^\alpha$  and  $\text{N}^\beta$ .

Manuscript change (P32, L595-597): *“(Note that applying the standard Rayleigh model to individual observations and averaging KIEs for the early and later parts of the reaction yields similar results to applying the standard Rayleigh model to the entire reaction (Table 6, Table S17); see SI for details.)”*

Manuscript change (P33): Updated Table 6

“Table 6. Comparison of standard Rayleigh and Expanded Rayleigh KIE values  $\pm$  standard error for N<sub>2</sub>O production from NO by purified *Histoplasma capsulatum* (fungal) P450 NOR [calculated using previously published isotopic data (Yang et al., 2014)].

Model	Extent of reaction (range of f)		KIE <sup>15</sup> N <sup>bulk</sup> a	KIE <sup>15</sup> N <sup>α</sup> a	KIE <sup>15</sup> N <sup>β</sup> a
Standard Rayleigh <sup>b</sup>	All	0.42-0.87	0.9910 $\pm$ 0.0014	1.0127 $\pm$ 0.0030	0.9694 $\pm$ 0.0022
Standard Rayleigh <sup>c</sup>	Early	0.77-0.81	0.9908 $\pm$ 0.0013	1.0130 $\pm$ 0.0031	0.9687 $\pm$ 0.0030
Standard Rayleigh <sup>c</sup>	Late	0.47-0.52	0.9909 $\pm$ 0.0015	1.0121 $\pm$ 0.0029	0.9698 $\pm$ 0.0018
Expanded Rayleigh <sup>d</sup>	Early	0.77-0.81	0.9910 $\pm$ 0.0014	0.9823 $\pm$ 0.0016	0.9998 $\pm$ 0.0015
Expanded Rayleigh <sup>d</sup>	Late	0.47-0.52	0.9910 $\pm$ 0.0014	0.9781 $\pm$ 0.0016	1.0041 $\pm$ 0.0013

<sup>a</sup> Average value  $\pm$  standard deviation

<sup>b</sup> KIE values were calculated from  $\epsilon_{N\text{-bulk}}$ ,  $\epsilon_{N\text{-}\alpha}$ , or  $\epsilon_{N\text{-}\beta}$  values obtained via linear regression of  $\delta^{15}N^{\text{bulk}}$ ,  $\delta^{15}N^{\alpha}$ , or  $\delta^{15}N^{\beta}$  against  $[-\ln f/(1-f)]$ . The standard Rayleigh model values presented here differ slightly from the previously published values (Yang et al., 2014) due to our exclusion of the earliest observation(s) from each replicate (i.e., observations with the highest values of  $f$  were excluded).

<sup>c</sup> For the standard Rayleigh model applied to individual observations,  $\epsilon_{N\text{-bulk}}$ ,  $\epsilon_{N\text{-}\alpha}$ , or  $\epsilon_{N\text{-}\beta}$  values were determined using Eq. (S24); the  $y$ -intercept listed in that equation corresponds to the  $y$ -intercept of  $\delta^{15}N^{\text{bulk}}$ ,  $\delta^{15}N^{\alpha}$ , or  $\delta^{15}N^{\beta}$  against  $[-\ln f/(1-f)]$  (determined by linear regression of the data from each replicate). KIE values for six (early) or seven (late) individual observations were pooled and averaged.

<sup>d</sup> For the Expanded Rayleigh model applied to individual observations, bulk values ( $\alpha_{N\text{-bulk}}$ ,  $\epsilon_{N\text{-bulk}}$ , and KIE <sup>15</sup>N<sup>bulk</sup>) were determined with the standard Rayleigh approach.  $\rho$  was calculated for each observation using Eq. (23) ( $\rho = {}^{15}N^{\alpha}/{}^{15}N^{\text{bulk}}$ ), and  $\tau$  was determined for every step of the reaction using Eq. (24) ( $\tau = {}^{14}N^{\alpha}/{}^{14}N^{\text{bulk}}$ ). Then  $\alpha_{N\text{-}\alpha}$  and  $\alpha_{N\text{-}\beta}$  were calculated for each individual observation with Eq. (21) or Eq. (22) and converted to KIE values using Eq. (10). KIE <sup>15</sup>N<sup>α</sup> and KIE <sup>15</sup>N<sup>β</sup> values for six (early) or seven (late) individual observations were pooled and averaged.”

SI changes (PS4): “Calculation of  $\epsilon$  values for individual observations from previously published P450 NOR data

The data for N<sub>2</sub>O production by purified P450 NOR is unusual because plots of  $\delta^{15}N^{\alpha}$  and  $\delta^{15}N^{\beta}$  against  $[-\ln f/(1-f)]$  form divergent lines instead of being roughly parallel (Yang et al., 2014). Thus,  $\rho$  is not constant, and using nonlinear least squares regression to predict a “constant” value of  $\rho$  that fits the entire dataset (i.e., the normal application of the Expanded Rayleigh model), is not appropriate. Therefore, as outlined in the Section 2.9 of the main paper, we calculated  $\rho$  for each observation to determine KIE <sup>15</sup>N<sup>α</sup> and KIE <sup>15</sup>N<sup>β</sup> values for each timepoint. Applying the Expanded Rayleigh model to individual observations yielded KIE <sup>15</sup>N<sup>α</sup> and KIE <sup>15</sup>N<sup>β</sup> values that are more accurate than values calculated by applying the standard

Rayleigh model to the entire dataset, indicating that the Expanded Rayleigh model outperforms the standard Rayleigh model even when  $\rho$  is not constant. To verify that this improved performance was due to the difference between the two models and not due to application of the Expanded Rayleigh model to individual observations instead of the entire dataset, we also applied the standard Rayleigh model to individual observations.

To apply the standard Rayleigh model to individual observations,  $\varepsilon_{N\text{-bulk}}$ ,  $\varepsilon_{N\text{-}\alpha}$ , and  $\varepsilon_{N\text{-}\beta}$  were calculated for each timepoint without linear regression by solving Eq. (2) for  $\varepsilon$

$$\varepsilon_{p/s} = \frac{\delta^{15}N^p - (\text{y intercept})}{\frac{f \ln(f)}{1-f}} \quad (\text{S24})$$

where  $\delta^{15}N^p$  represents  $\delta^{15}N^\alpha$ ,  $\delta^{15}N^\beta$ , or  $\delta^{15}N^{\text{bulk}}$  and (y-intercept) is the intercept of  $\delta^{15}N^\alpha$ ,  $\delta^{15}N^\beta$ , or  $\delta^{15}N^{\text{bulk}}$  plotted against  $[-f \ln f / (1-f)]$ . For  $\delta^{15}N^{\text{bulk}}$ , the y-intercept is the initial  $\delta$  value of the substrate,  $\delta^{15}N^{s0}$ . While  $\delta^{15}N^{s0}$  could theoretically be measured, this value was not measured for this dataset. For  $\delta^{15}N^\alpha$  and  $\delta^{15}N^\beta$ , the y-intercept doesn't have an analogous physical interpretation and thus cannot be measured directly. Therefore, the value of each y-intercept was determined via linear regression of the appropriate  $\delta$  value against  $[-f \ln f / (1-f)]$ . Linear regression was performed separately for each replicate (13 observations/replicate). The appropriate y-intercept value was then used to calculate  $\varepsilon$  for each timepoint using the specific  $\delta$  value and  $f$  value from one observation. As shown in Table S17, the KIEs calculated by applying the standard Rayleigh model to each individual observation are very similar to the KIEs calculated by applying the standard Rayleigh model to all the observations from one replicate.”

**For the NH<sub>2</sub>OH oxidation case study, even after looking in the supporting information and the original Sutka et al. (2006) paper, it was not clear to me what the initial value of substrate was, or exactly how the extent of reaction  $f$  was calculated from the information provided.**

Response: The initial amount of substrate was 3  $\mu\text{mol}$  (0.3 mL of 0.01 M NH<sub>2</sub>OH was added to the culture) (Sutka et al., 2006). Values of  $f$  (fraction of substrate remaining) were calculated by dividing remaining  $\mu\text{mol}$  of substrate by initial  $\mu\text{mol}$  of substrate. Remaining  $\mu\text{mol}$  of substrate was calculated by converting N<sub>2</sub>O concentration ( $\mu\text{M}$ ) to  $\mu\text{mol}$  of N<sub>2</sub>O and subtracting twice this value from the initial  $\mu\text{mol}$  of substrate. We have rewritten the SI text to make this more clear.

SI changes (P S3): “In this experiment, 0.3 mL of 0.01 M NH<sub>2</sub>OH (i.e., 3  $\mu\text{mol}$  of NH<sub>2</sub>OH) was added to a 25 mL culture tube containing 2 mL of suspended cells (Sutka et al., 2006). Values of  $f$  were calculated by dividing  $\mu\text{mol}$  of NH<sub>2</sub>OH remaining ( $N^s$ ) by the initial amount of NH<sub>2</sub>OH ( $N^{s0}$ ) (Eq. (S20)).

$$f = \frac{N^s}{N^{s0}} \quad (\text{S20})$$

*As noted above,  $N^{s0} = 3 \mu\text{mol}$ .  $N^s$  was calculated by subtracting  $\mu\text{mol}$  of  $\text{NH}_2\text{OH}$  consumed (i.e., twice the number of  $\mu\text{mol}$  of  $\text{N}_2\text{O}$  produced) from  $N^{s0}$  (Eq. S21).*

$$N^s = N^{s0} - 2 * (c_{\text{N}_2\text{O}} * v_{\text{headspace}}) \quad (\text{S21})$$

*As shown in Eq. (21), to convert from  $\text{N}_2\text{O}$  concentration in  $\mu\text{M}$  ( $c_{\text{N}_2\text{O}}$ ) to  $\mu\text{mol N}_2\text{O}$ ,  $\text{N}_2\text{O}$  concentration was multiplied by headspace volume ( $v_{\text{headspace}} = 0.0227 \text{ L}$ ).*

Sutka, R. L., Ostrom, N. E., Ostrom, P. H., Breznak, J. A., Gandhi, H., Pitt, A. J., and Li, F.: Distinguishing nitrous oxide production from nitrification and denitrification on the basis of isotopomer abundances, *Appl Environ Microb*, 72, 638-644, 10.1128/aem.72.1.638-644.2006, 2006.



## Response to Reviewer 1 Comment

\*The line numbers and page numbers of the reviewer's comments refer to the original document. (Note that we added the page numbers.) The page and line numbers of manuscript changes in our responses refer to the "tracked changes" document.

**This manuscript presents the new Expanded Rayleigh model applicable for N<sub>2</sub>O synthesis for proper calculation of isotope effects regarding 2 different positions of N. This is very important development for enzymatic studies on N<sub>2</sub>O production in various pathways. It is very surprising that the differences while using classical Rayleigh model and the new developed Expanded Rayleigh model are so significant. It shows that it is highly necessary to apply this new calculation approach in such kind of studies.**

**The manuscript is clearly written and appropriate for publication in BG after minor edition.**

Response: Thank you for your time and careful reading of our manuscript. We are happy to know that you find the manuscript clearly written and appropriate for publication in *Biogeochemistry*.

**I have only a few minor comments.**

**P2, L46 s in a particular chemical compound – which chemical compound when you write about N<sub>2</sub>O, you mean any other? – info on compound-specific stable isotope analysis can be omitted in your introduction, since you do not need this afterwards**

Response: As suggested, we have deleted "compound-specific" and the corresponding definition from the introduction.

Manuscript changes (P2, L45-46, *new text italicized*): "*One useful technique for N<sub>2</sub>O source apportionment is stable isotope analysis.*"

**P4, L116 – please delete "\*1000" from the equation, it shouldn't be part of the  $\delta$  definition, is just the way of presenting in permil notation, see eg.**

**<https://analyticalsciencejournals.onlinelibrary.wiley.com/doi/pdf/10.1002/rcm.8890>**

Response: The expression for  $\delta$  can be written to define either the unitless form (without multiplying by 1000) or the per mil form (defined by multiplying the unitless form by 1000). Indeed, the original definition of  $\delta$  was written using the per mil notation (Mckinney et al., 1950), and this definition has also been used in a more recent review (Casciotti et al., 2011). As  $\delta$  values are commonly expressed in per mil, we have written many other equations in this manuscript to accommodate per mil  $\delta$  notation (*e.g.*, Eq. 1 and Eqs. 27-30). Thus, to make it clear which form of  $\delta$  we use throughout the manuscript, we included the multiplication by a factor of 1000 in our definition of  $\delta$  (Eq. 6). We have also changed the manuscript text to make it clear that the per mil  $\delta$  notation is used.

Casciotti, K. L., Buchwald, C., Santoro, A. E., and Frame, C.: Assessment of nitrogen and oxygen isotopic fractionation during nitrification and its expression in the marine environment, *Methods in enzymology*, 486, 253-280, 10.1016/b978-0-12-381294-0.00011-0, 2011.

McKinney, C. R., McCrea, J. M., Epstein, S., Allen, H. A., and Urey, H. C.: Improvements in mass spectrometers for the measurement of small differences in isotope abundance ratios, *Rev Sci Instrum*, 21, 724-730, 10.1063/1.1745698, 1950.

Manuscript changes (P4, L115-120): “Because there is naturally little variation in  $^{15}\text{N}$ ,  $R_{\text{sample}}/R_{\text{standard}}$  values are typically close to 1, and isotopic ratios are usually converted to the  $\delta$  notation, which is commonly expressed in the per mil form (‰) by multiplying the unitless form of  $\delta$  by 1000:

$$\delta = \left( \left( \frac{R_{\text{sample}}}{R_{\text{standard}}} \right) - 1 \right) * 1000 \quad (6)$$

where  $R_{\text{sample}}$  is the isotopic ratio of the sample, and  $R_{\text{standard}}$  is the isotopic ratio of the analytical standard (Mariotti et al., 1981). *The per mil form of  $\delta$  is used throughout this manuscript.*”

Mariotti, A., Germon, J. C., Hubert, P., Kaiser, P., Letolle, R., Tardieux, A., and Tardieux, P.: Experimental determination of nitrogen kinetic isotope fractionation: Some principles; illustration for the denitrification and nitrification processes, *Plant Soil*, 62, 413-430, 10.1007/BF02374138, 1981.

On a related note, while reading the paper the reviewer referenced above (Skrzypek and Dunn, 2020), we realized that it would be more accurate to use 0.0036765 as the value of  $R_{\text{standard}}$  instead of 0.003663 (atom percent for  $^{15}\text{N}$ ) (Mariotti et al., 1981). As the two values are very similar, using 0.0036765 had essentially no effect on the outcome of our calculations. We have, however, updated the manuscript text and corresponding calculations, figures, and SI tables to be as accurate as possible. (The values reported in the main text and tables did not change.)

Manuscript change (P4, L113): “(Atom percent of  $^{15}\text{N}$  in atmospheric  $\text{N}_2$  (air) is  $0.3663 \pm 0.0004\%$ , so  $R = 0.0036765$ ) (Junk and Svec, 1958; Mariotti et al., 1981; Skrzypek and Dunn, 2020).”

Junk, G. A. and Svec, H. J.: Nitrogen isotope abundance measurements, US atomic energy commission. Office of technical information., ISC 1138, 1958.

Mariotti, A., Germon, J. C., Hubert, P., Kaiser, P., Letolle, R., Tardieux, A., and Tardieux, P.: Experimental determination of nitrogen kinetic isotope fractionation: Some principles; illustration for the denitrification and nitrification processes, *Plant Soil*, 62, 413-430, 10.1007/BF02374138, 1981.

Skrzypek, G. and Dunn, P. J. H.: Absolute isotope ratios defining isotope scales used in isotope ratio mass spectrometers and optical isotope instruments, *Rapid Communications in Mass Spectrometry*, 34, e8890, <https://doi.org/10.1002/rcm.8890>, 2020.

Manuscript change (P11-12): Updated Figure 1.

Manuscript change (P18-19): Updated Figure 3.

Manuscript change (P27-28): Updated Figure 6.

SI changes: Updated Tables S3-13 and Table S17 (P S9-24, S29-30) and updated Figures S1-S8 (P S31-46).

**P4, L121 – the equation is mathematically not true, you define N<sub>bulk</sub> as total number of atoms and then this is equal mol N<sub>2</sub>O?! When mol represents 6.022\*10<sup>23</sup> atoms! You mix here up different units. This is not equal. -The same wrong statement you have later in P9, L 225**

Response: The main goal of equation 7 was to express the relationship between N<sup>bulk</sup> and N<sup>α</sup> and N<sup>β</sup> (*i.e.*,  $0.5 * N^{bulk} = N^{\alpha} = N^{\beta}$ ). This relationship remains the same whether N is quantified in terms of atoms or moles/equivalents. However, as the reviewer correctly points out, because N<sup>bulk</sup> is formally defined as 0.5\**mol* N<sub>2</sub>O in Eq. 7, we should avoid using “atoms” and “moles” interchangeably. Thus, we have changed the text to match Eq. 7 by defining N<sup>bulk</sup> as the total number of moles of N at the α and β positions. Note that adopting this definition means the text from L225 does not need to be changed.

Manuscript changes (P4-5, L122-127): “N<sup>α</sup> and N<sup>β</sup> are defined as the number of moles of N at the α (central) and β (outer) positions of N<sub>2</sub>O, respectively.

$$0.5 * N^{bulk} = N^{\alpha} = N^{\beta} = \text{mol } N_2O \quad (7)$$

Thus, <sup>15</sup>N<sup>bulk</sup> is defined as the total number of moles of <sup>15</sup>N at both the α and β positions:

$$^{15}N^{bulk} = ^{15}N^{\alpha} + ^{15}N^{\beta} \quad (8)$$

Similarly, <sup>14</sup>N<sup>bulk</sup> is defined as the total number of moles of <sup>14</sup>N at the α and β positions of N<sub>2</sub>O:

$$^{14}N^{bulk} = ^{14}N^{\alpha} + ^{14}N^{\beta} \quad (9)$$

**Fig 4 and 5 it would be interesting to see the comparison of values calculated with normal and expanded Rayleigh model**

Response: With the exception of the δ<sup>15</sup>N<sup>s0</sup> values shown in Fig. 5, all of the δ values shown in Figs. 4 and 5 were experimentally measured and are the same regardless of which model is applied. The δ<sup>15</sup>N<sup>s0</sup> values from Fig. 5 were back-calculated from δ<sup>15</sup>N<sup>bulk</sup> values using the standard Rayleigh model (Eq. 2), which can be accurately applied to relate δ<sup>15</sup>N<sup>bulk</sup> to δ<sup>15</sup>N<sup>s0</sup>.

Note that the Expanded Rayleigh model also uses Eq. 2 for bulk  $\delta^{15}\text{N}^{\text{s0}}$  values, so these  $\delta^{15}\text{N}^{\text{s0}}$  values are the same regardless of which model is used. Tables 5-6 present comparisons of values calculated by applying the standard and Expanded Rayleigh models to the data from Figs. 4-5, and the differences between the two models are described in section 3.3, “Application of the Expanded Rayleigh model to previously published isotopic data.”

**P20, L 410-418 You present here the extreme cases with strong differences in fractionation in alfa and beta position, of course, then the differences between both calculation models are large. However, I wonder if these cases are realistic in any way? Is there any possible process which shows that different isotope discrimination in both positions?**

Response: In addition to the simulated datasets, we evaluated two experimental datasets with fairly large differences in isotope discrimination between the  $\alpha$  and  $\beta$  positions. The differences between position-specific KIE values calculated for the standard and Expanded Rayleigh models are similar for the simulated datasets and the experimental datasets. (Absolute relative differences between standard KIE  $^{15}\text{N}^{\alpha}$  or KIE  $^{15}\text{N}^{\beta}$  values and Expanded Rayleigh model values range from 0.01-0.04 for simulated datasets and from 0.02-0.04 for the experimental datasets.) As with the simulated data, the differences between the values calculated for the two models are large enough to be of practical significance for the experimental datasets: Some of the experimental standard Rayleigh KIE values for  $\text{N}^{\alpha}$  and  $\text{N}^{\beta}$  are qualitatively inaccurate, causing incorrect determination of the type of isotope effect at either the  $\alpha$  position (Table 6) or  $\beta$  position (Table 5). In contrast, the Expanded Rayleigh KIE values correctly identify the type of position-specific isotope effect for both positions (as determined by qualitative comparison of  $\delta^{15}\text{N}^{\text{s0}}$  with  $\delta^{15}\text{N}^{\alpha}$  and  $\delta^{15}\text{N}^{\beta}$ ).

**P21, L432 – the sentence from “To address this issue, we have developed...” is a repetition of what you already said in methods section, not needed here. Please pay attention to omit unnecessary repetitions**

Response: The sentence in question briefly summarizes how the Expanded Rayleigh model differs from the original Rayleigh model (*i.e.*, by the addition of new parameters,  $\rho$  and  $\tau$ ). Because the remainder of the paragraph discusses the results for  $\rho$  and  $\tau$  calculations, we feel it is appropriate to include this statement to remind the reader what these newly defined terms mean. Nevertheless, to address the reviewer’s concern, we shortened this sentence to avoid unnecessary repetition.

Manuscript change (P24, L457): “*To address this issue, we developed the Expanded Rayleigh model that introduces two new parameters,  $\rho$  and  $\tau$ , to define how  $^{15}\text{N}^{\text{bulk}}$  and  $^{14}\text{N}^{\text{bulk}}$ , respectively, are apportioned between  $\text{N}^{\alpha}$  and  $\text{N}^{\beta}$ .*”

**Table 5 – what is Expanded 1 and 2? Please explain in Fig caption or footnotes**

Response: We have modified footnote e to highlight the difference between Expanded Rayleigh models 1 and 2. Please see the new sentence at the end of the footnote below. We have also changed the model descriptions in the first column of Tables 5 and 6 to clarify which model is being used (*i.e.*, “Standard Rayleigh” or “Expanded Rayleigh”).

Manuscript changes (P31, L571-572): Table 5 footnote e: “For the Expanded Rayleigh model, bulk values ( $\alpha_{N\text{-bulk}}$ ,  $\epsilon_{N\text{-bulk}}$ , and KIE  $^{15}\text{N}^{\text{bulk}}$ ) were determined with the standard Rayleigh approach,  $\rho$  was determined via nonlinear regression, and  $\tau$  was determined by averaging  $^{14}\text{N}^{\alpha}/^{14}\text{N}^{\text{bulk}}$  for every step of the reaction. Then  $\alpha_{N\text{-}\alpha}$  and  $\alpha_{N\text{-}\beta}$  were calculated with Eq. (21) or Eq. (22) and converted to KIE values using Eq. (10). *The only difference between Expanded Rayleigh models 1 (Eq. (29)) and 2 (Eq. (30)) is which  $\delta$  value ( $\delta^{15}\text{N}^{\alpha}$  or  $\delta^{15}\text{N}^{\beta}$ ) is substituted with a  $\rho$ -containing expression in the nonlinear model.*”