

Distribution characteristics of summer precipitation raindrop spectrum in Qinghai–Tibet Plateau

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Abstract: To enhance the precision of precipitation forecasting in the Qinghai–Tibet Plateau region, a comprehensive study of both macro– and micro–characteristics of local precipitation is imperative. In this study, we investigated the particle size distribution, droplet velocity, droplet number density, \( Z \) (Radar reflectivity) \( \sim I \) (Rainfall intensity) relationship, and Gamma distribution of precipitation droplet spectra with a single precipitation duration of at least 20 minutes and precipitation of 5 mm or more at four stations (Nyalam, Lhasa, Shigatse, and Naqu) in Tibet during the recent years from June to August. The results are as follows: (1) In the fitting relationship curve between precipitation raindrop spectral particle size and falling speed at the four stations in Tibet, when the particle size was less than 1.5 mm, the four lines essentially coincided. When the particle size exceeded 1.5 mm, the speed in Shigatse was the highest, followed by Lhasa, and the speed in Naqu was the lowest. The falling speed of particles correlated with altitude. (2) The diameter of the six microphysical features at the four stations increased with altitude. (3) The \( Z-I \) relationships at the four stations exhibited variations. Owing to the proximity in altitude between Lhasa and Shigatse, as well as between Nyalam and Naqu, the coefficients \( a \) and index \( b \) in the \( Z-I \) relationships of the two groups of sites were relatively similar. (4) The fitting curves of the M–P and Gamma distributions of the precipitation particle size at the aforementioned four stations are largely comparable. The M–P distribution fitting exhibits a slightly better effect. The parameter \( \mu \) in Gamma distribution decreases with the increase of altitude, while \( N_0 \) and \( \lambda \) in M–P distribution show a clear upward trend with altitude.
1. Introduction

The microphysical processes of cloud and precipitation over the Qinghai–Tibet Plateau significantly differ from those in low-altitude regions due to the high average altitude and complex, changeable terrain, resulting in a strong ground heating effect. Due to the terrain's influence, the plateau area has a limited number of observation stations, leading to a scarcity of precipitation records. Based on three atmospheric scientific experiments conducted over the Qinghai–Tibet Plateau, convective clouds exhibit high activity, although the precipitation intensity is moderate (Li et al., 2014; Jiang et al., 2002; Xu et al., 2006; Li et al., 2001). In the central part of the Plateau, severe convective clouds constitute 4% to 21%, with cumulonimbus clouds representing 21%. Additionally, the frequency of severe weather, such as thunderstorms and hail, surpasses that in other regions. In the majority of Qinghai–Tibet Plateau areas, convective cloud precipitation constitutes over 90% of the total (Chang and Guo, 2016). Particularly during the rainy season, convective processes are frequent with smaller horizontal scales, weaker intensities, and shorter durations. Due to observational constraints, short-term tests and satellite data (e.g., TRMM, CloudSat, and Aqua) are employed to investigate Tibetan Plateau precipitation, with a focus on liquid precipitation characteristics, including seasonal and diurnal variations and convective activity's liquid drop spectrum inversion (Ruan et al., 2015; Liu et al., 2015; Xiong et al., 2019; Zhang et al., 2018). The scarcity of observational data on cloud precipitation's physical processes in the Qinghai–Tibet Plateau results in limited studies on microscopic parameters' characteristics. The recent installation of a laser raindrop spectrometer enables a comprehensive understanding of the plateau's precipitation microphysical parameters through the study of raindrop spectral parameters and distribution characteristics in various regions.

Some studies have explored the spectral characteristics of raindrops over the Tibetan Plateau. Yu Jianyu et al. and Shu Lei et al. conducted analyses on the raindrop spectrum characteristics of various clouds in the Naqu and Yushu regions of the Qinghai–Tibet Plateau (Yu et al., 2020; Shu et al., 2021). Li Shanshan et al. investigated raindrop spectral characteristics at different elevations on the eastern slope of the Qinghai–Tibet Plateau. They discovered that the average spectrum of raindrop number concentration at various elevations conforms to the Gamma function distribution. Moreover, light precipitation and heavy precipitation exhibit distinct raindrop spectral characteristics (Li et al., 2020). The aforementioned research was conducted in Naqu and Yushu areas in the Qinghai–Tibet Plateau, as well as the west...
Sichuan Plateau area. However, there is a limited number of studies on the spectral characteristics and distribution rules of cloud precipitation raindrops in various regions of the Tibetan Plateau. The analysis of raindrop spectrum characteristics in the Naqu region, as mentioned earlier, was conducted only during the summer months from June to August 2014. In this study, we used raindrop spectrum data from the Naqu region spanning 2017 to 2020, building upon and extending previous research. We analyzed the temporal variation of the raindrop spectrum in convective cloud precipitation across various regions and examine differences in drop spectrum characteristics among these regions. We conducted a systematic analysis of raindrop spectrum data associated with moderate rain from four stations with varying altitudes, longitudes, and latitudes. We compared and analyzed the differences in drop spectrum characteristics among these four stations, which is of great significance for enhancing the scientific understanding of precipitation's influence in the plateau region.

The objective of this study is to enhance the understanding of raindrop spectrum characteristics at various elevations of the Tibetan Plateau. The findings of this study will establish a foundation for comprehending precipitation characteristics and improving precipitation forecasts at diverse elevations of the Tibetan Plateau. This study is structured as follows: Data sources and research methods are described in Section 2. The analysis results are presented in Section 3 while the conclusion and discussion are provided in Section 4.

2. Data and methods

2.1. Data collection

The data obtained for this study consist of raindrop spectrum data from four meteorological stations (i.e., Nyalam, Lhasa, Shigatse, and Naqu) in Tibet. Owing to its unique climate environment, snowfall occurs time to time from September to May. Data from June to August is selected to analyze the precipitation raindrop spectrum process in this study. The precipitation data selection criteria include a precipitation process duration exceeding 20 minutes and a single precipitation process with rainfall greater than 5mm. As the frequency of convective clouds in most areas of the Qinghai–Tibet Plateau exceeds 90%, all collected samples are categorized as convective clouds in this paper. Table 1 displays the longitude, latitude, altitude, and sample numbers of the four stations. Figure 1 illustrates the geographical distribution of the four sites. The four stations cover a broad area of central Tibet from south to north,
making the results representative.

Figure 1: Station distribution and the surrounding terrain

<table>
<thead>
<tr>
<th>Station</th>
<th>Longitude</th>
<th>Latitude</th>
<th>Elevation (m)</th>
<th>Sampling period</th>
<th>Sample size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nyalam</td>
<td>85.58° E</td>
<td>28.11° N</td>
<td>4519</td>
<td>2017–2019</td>
<td>11579</td>
</tr>
<tr>
<td>Lhasa</td>
<td>91.08° E</td>
<td>29.40° N</td>
<td>3653</td>
<td>2017–2018</td>
<td>8364</td>
</tr>
<tr>
<td>Shigatse</td>
<td>88.53° E</td>
<td>29.15° N</td>
<td>3910</td>
<td>2017–2018</td>
<td>14237</td>
</tr>
<tr>
<td>Naqu</td>
<td>92.04° E</td>
<td>31.29° N</td>
<td>4560</td>
<td>2017–2020</td>
<td>5630</td>
</tr>
</tbody>
</table>

2.2. Quality Control and Quality Assurance (QA/QC)

The Parsivel2 raindrop spectrometer features 32 particle size measurement channels and 32 particle velocity measurement channels. The particle size measurement range is 0.062–24.5 mm, and the particle velocity measurement range is 0.05–20.8 m s\(^{-1}\), with a sampling time of 60 s. In comparison to the previous Parsivel raindrop spectrometer model, the Parsivel2 raindrop spectrometer utilizes infrared light as its light source. This change reduces the interference of visible light, resulting in significant advancements in the measurement of raindrop size and rainfall. Following the sampling principle of the raindrop spectrometer, the instrument records the particle size and particle speed of all particles passing through the sampling surface. To mitigate the influence of sand and dust particles, it is imperative to control the quality of the fundamental data.

Atlas (Atlas et al., 1973) discovered a relationship between the final falling velocity of particles and the particle diameter. In an ideal windless environment, the formula for the final falling velocity of particles
is:

\[
\begin{align*}
    v &= 0, \quad x < 0.03 \\
    v &= 4.323 \times (x - 0.03), \quad 0.03 \leq x \leq 0.6 \\
    v &= 9.65 - 10.3 \times e^{-0.64x}, \quad x > 0.6
\end{align*}
\]  

(1)

where \( x \) represents the particle diameter in mm, and \( v \) represents the final falling velocity of the particle in m s\(^{-1}\).

Kruger and Krajewski (Kruger and Krajewski, 2002) proposed a method to mitigate the dispersion of velocity over large samples, building on the study by Atlas. Initially, the final falling velocity was calculated based on the particle diameter and final velocity formula, and subsequently, a threshold value was set for elimination. The formula is expressed in Equation 2:

\[
|v_{measured} - v_d| < 0.4v_d
\]

(2)

where \( v_{measured} \) represents the final velocity measured by the raindrop spectrometer, and \( v_d \) is the final velocity calculated using the final velocity formula. If the relative error falls within the specified threshold range, the data will be retained.

Previous studies have highlighted that the distribution of raindrop spectrum exhibits distinct characteristics influenced by geographical environment and topography. Hence, utilizing the same calculation formula across different areas for raindrop spectrum elimination is likely to introduce significant errors. Therefore, we utilized historical data from a raindrop spectrum site to localize the parameters identified in the study by Atlas and incorporates them into the formula for particle elimination.

Simultaneously, due to deformation occurring in raindrops during descent, the raindrop spectrum data undergoes deformation and correction after quality control. Battaglia() defined the axial ratio \( (ar) \) as the ratio of radial and transverse lengths of raindrop particles. Particles with a particle size less than 1 mm are defined as spherical. The axial ratio is defined as \( ar = 1.075 - 0.075Deq \) for particles with a particle size of 1–5 mm, where \( Deq \) is the equivalent precipitation particle diameter, and \( ar = 0.7 \) for particles with a particle size greater than 5 mm.

2.3. Raindrop spectrum parameters

The number density of the precipitation raindrop spectrum is defined as the total number of particles per unit volume (Shi et al., 2008).
where \( N(D) \) is the number density parameter, in units of \( \text{mm}^{-1} \text{ m}^{-3} \); \( n_{ij} \) represents the number of raindrops with the diameter of the \( i \)-th particle and the velocity of the \( j \)-th particle; \( A \) is the sampling base area of the raindrop spectrometer (5400 mm\(^2\)); \( \Delta T \) is the sampling time (60 s); \( V_j \) is the velocity value of the sampled particle, in units of \( \text{m s}^{-1} \).

The average diameter is calculated as the sum of the diameters of all raindrops per unit volume divided by the total number of raindrops, and the formula is given by equation 4.

\[
D_i = \frac{\sum_{i=1}^{32} N(D_i)D_i}{\sum_{i=1}^{32} N(D_i)}
\]  

(4)

The weighted average diameter represents the average diameter of the weighted mass of all particles per unit volume relative to the total mass of particles, measured in mm. The formula is expressed in equation 5.

\[
D_m = \frac{\sum_{i=1}^{32} N(D_i)D_i^4}{\sum_{i=1}^{32} N(D_i)D_i^3}
\]  

(5)

where \( D_i \) represents the diameter of the \( i \)-th particle, and \( N(D_i) \) represents the particle number density of the \( i \)-th particle diameter.

Precipitation intensity refers to precipitation per unit time (per hour), measured in mm h\(^{-1}\). The formula is given by equation 6.

\[
I = \frac{6\pi}{10^7} \sum_{i=1}^{32} D_i^3V(D_i)N(D_i)
\]  

(6)

The radar reflectivity factor is the sum of the backscattering area of all particles per unit volume, measured in mm\(^{-6} \text{ m}^{-3} \). The formula is expressed in equation 7.

\[
Z = \sum_{i=1}^{32} N(D_i)D_i^6
\]  

(7)

The observed raindrop spectrum is discrete, and the double–parameter index, namely M–P distribution, can be used to simulate the raindrop particle size distribution. The formula is given by equation 8.
where \( N_0 \) is a number density parameter, measured in mm\(^{-1}\) m\(^{-3}\). \( \lambda \) is a size parameter, measured in mm\(^{-1}\).

However, this distribution pattern has some errors compared with actual observation data when describing small and large raindrops. Therefore, Ulbrich and Atlas proposed a modified raindrop particle size distribution pattern. They treated the raindrop spectrum distribution as a Gamma distribution to correct the distribution pattern between small and large raindrops.

In this case, the raindrop particle size distribution follows the Gamma distribution with three parameters (Carlton and David, 1984). The formula is given by equation 9.

\[
N(D) = N_0 \times D^\mu \times \exp(-\lambda D) \tag{9}
\]

where \( \mu \) is a dimensionless parameter referred to as the shape factor. When \( \mu \) is greater than 0, the curve exhibits an upward curvature; when \( \mu \) is less than 0, the curve displays a downward curvature. When \( \mu=0 \), it corresponds to an M–P distribution.

Zhang (Zhang et al., 2003) pointed out a binomial relationship between \( \mu \) and \( \lambda \) when studying the \( \mu-\lambda \) relationship of precipitation in Florida:

\[
\lambda = a\mu^2 + b\mu + c \tag{10}
\]

Ulbrich (Ulbrich, 1983) pointed out in his study that the \( \mu-\lambda \) relation under Gamma distribution can be expressed as:

\[
D_n = \frac{4+\mu}{\lambda} \tag{11}
\]

Equation (11) shows that there is a relationship between the ratio of \( \mu \) and \( \lambda \) and the weighted average diameter of mass. The Gamma distribution fit is typically applied to the observed raindrops distribution \( N(D) \) using the least squares or order moments method. In this study, the least square method is employed to fit the M–P and Gamma distributions.

3. Result and discussion

The average altitude of the Qinghai–Tibet Plateau is over 4000 m, and the terrain is complex and changeable, resulting in varying microphysical characteristics of the raindrop spectrum. Therefore, considering the unique conditions of the Qinghai–Tibet Plateau, the rain intensity calculated based on
The raindrop spectrum was categorized into five grades for calculation and analysis, as presented in Table 2. The results indicated that the mean value and standard deviation of the rain intensity at the same station were generally proportional to the rain intensity, with slight fluctuations observed among individual stations. The samples from the four stations in the range of 0.5–5 mm·h⁻¹ were the largest, and the obtained standard deviation values were all very small. This indicates a high consistency in rain intensity distribution under weak rain intensity. In the interval of precipitation intensity greater than 20 mm·h⁻¹, only two stations have samples, and one of the stations exhibits a large standard deviation. This reflects a significant inversion error in raindrop spectrum for Nyalam during short-duration heavy precipitation.

<table>
<thead>
<tr>
<th>Range</th>
<th>Sample Size</th>
<th>Mean (mm·h⁻¹)</th>
<th>Standard Deviation (mm·h⁻¹)</th>
<th>Precipitation (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5–5</td>
<td>4047</td>
<td>2.16</td>
<td>1.21</td>
<td>146</td>
</tr>
<tr>
<td>5–10</td>
<td>1358</td>
<td>7.38</td>
<td>1.28</td>
<td>166.6</td>
</tr>
<tr>
<td>Nyalam</td>
<td>10–15</td>
<td>900</td>
<td>12.14</td>
<td>182.1</td>
</tr>
<tr>
<td></td>
<td>15–20</td>
<td>656</td>
<td>17.69</td>
<td>193.4</td>
</tr>
<tr>
<td></td>
<td>&gt;20</td>
<td>960</td>
<td>30.63</td>
<td>490</td>
</tr>
<tr>
<td>0.5–5</td>
<td>3245</td>
<td>1.8</td>
<td>0.94</td>
<td>97.4</td>
</tr>
<tr>
<td>5–10</td>
<td>180</td>
<td>5.87</td>
<td>0.77</td>
<td>17.6</td>
</tr>
<tr>
<td>Lhasa</td>
<td>10–15</td>
<td>50</td>
<td>12.1</td>
<td>12.1</td>
</tr>
<tr>
<td></td>
<td>15–20</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>&gt;20</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0.5–5</td>
<td>7094</td>
<td>1.78</td>
<td>1.06</td>
<td>210.7</td>
</tr>
<tr>
<td>5–10</td>
<td>584</td>
<td>6.37</td>
<td>1.11</td>
<td>62.02</td>
</tr>
<tr>
<td>Shigatse</td>
<td>10–15</td>
<td>60</td>
<td>10.01</td>
<td>10.01</td>
</tr>
<tr>
<td></td>
<td>15–20</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>&gt;20</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0.5–5</td>
<td>2389</td>
<td>3.27</td>
<td>1.5</td>
<td>130.1</td>
</tr>
<tr>
<td>Naqu</td>
<td>5–10</td>
<td>675</td>
<td>7.76</td>
<td>87.3</td>
</tr>
<tr>
<td></td>
<td>10–15</td>
<td>479</td>
<td>13.73</td>
<td>109.6</td>
</tr>
</tbody>
</table>
3.1. Precipitation particle size, speed and rainfall intensity contribution rate distribution

Figure 2 represent the mean precipitation values across the four stations. The canvas is divided into several rectangular areas defined by the coordinates of the horizontal and left axes, and the color code is applied to them. Each rectangular area represents a specific particle diameter and velocity. Figure 2 reveals that the fitting curves of particle diameter distribution and final falling velocity at the four stations are approximately identical, and the final falling velocity increases with the particle diameter. Regarding particle number density, it is concentrated in the area with particle size less than 1 mm, and it decreases with the increase of diameter. Concerning the contribution rate of precipitation intensity, the four stations exhibit a multi-peak distribution, with peak diameters at 0.812 mm and 1.375 mm. In comparison with the precipitation process of convective clouds at low-altitude stations, the particle size spectrum width at the four stations on the Tibetan Plateau in this analysis was notably reduced, and the particle number density at the four stations with particle sizes greater than 3 mm was very low.
Figure 2: The average spectrum of precipitation particle size, velocity, and contribution rate distribution of precipitation intensity. The color bar represents the number density in units per m³. (A. Nyalam, B. Lhasa, C. Shigatse, and D. Naqu).

Figure 3 displays the fitting relationship between the particle size of the raindrop spectrum and the falling speed at the four stations in Tibet. For particle sizes less than 1.5 mm, the particle size at the four stations essentially aligns with the final falling speed. For particle sizes greater than 1.5 mm, the speed is largest for Shigatse, followed by Lhasa, and Naqu has the smallest speed. However, under the same size, the final velocities of particles at the four stations are greater than those in Guizhou, exceeding 2 m/s. This may be attributed to the higher altitude of the four stations, which are over 3000 m above sea level. This indicates that the high altitude of Tibet, due to thin air and low air pressure, results in decreased fall speed of larger particles of the same size. However, particles at lower altitudes (Shigatse and Lhasa) exhibited slightly higher speeds than those at higher altitudes (Nyalam and Naqu). This difference may be attributed to the instruments at higher altitudes being closer to the clouds, leading to the detection of raindrops before they interacted with each other. The fitting formulas for the \( v-D \) relationships at the four sites (Nyalam, Lhasa, Shigatse, and Naqu) are given by Equations 12, 13, 14, and 15, respectively.

\[
\begin{align*}
\text{\( v=0, \) } & \quad x<0.03 \\
\text{\( v = 3.720 \times (x+0.456), 0.03 \leq x \leq 0.6 \) } & \quad \text{\( x \geq 0.6 \)} \\
\text{\( v = 10.325 - 9.252 \times e^{-0.6x}, x > 0.6 \)} \\
\end{align*}
\]

\( (12) \)

\[
\begin{align*}
\text{\( v=0, \) } & \quad x<0.03 \\
\text{\( v = 3.796 \times (x+0.468), 0.03 \leq x \leq 0.6 \) } & \quad \text{\( x \geq 0.6 \)} \\
\text{\( v = 10.375 - 9.118 \times e^{-0.6x}, x > 0.6 \)} \\
\end{align*}
\]

\( (13) \)

\[
\begin{align*}
\text{\( v=0, \) } & \quad x<0.03 \\
\text{\( v = 4.035 \times (x+0.401), 0.03 \leq x \leq 0.6 \) } & \quad \text{\( x \geq 0.6 \)} \\
\text{\( v = 10.614 - 9.568 \times e^{-0.6x}, x > 0.6 \)} \\
\end{align*}
\]

\( (14) \)

\[
\begin{align*}
\text{\( v=0, \) } & \quad x<0.03 \\
\text{\( v = 3.474 \times (x+0.524), 0.03 \leq x \leq 0.6 \) } & \quad \text{\( x \geq 0.6 \)} \\
\text{\( v = 10.162 - 9.018 \times e^{-0.6x}, x > 0.6 \)} \\
\end{align*}
\]

\( (15) \)
Figure 3: The relationship between particle size and speed at four stations.

The proportion of particle number density in raindrop spectrum and the contribution rate of precipitation are shown in Table 3 and Table 4, respectively.

Table 3: Percentage of particle number density.

<table>
<thead>
<tr>
<th>Particle diameter (mm)</th>
<th>0−1 mm</th>
<th>1−2 mm</th>
<th>2−3 mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nyalam</td>
<td>93.60</td>
<td>6.15</td>
<td>0.25</td>
</tr>
<tr>
<td>Lhasa</td>
<td>92.41</td>
<td>7.24</td>
<td>0.35</td>
</tr>
<tr>
<td>Shigatse</td>
<td>91.45</td>
<td>8.06</td>
<td>0.49</td>
</tr>
<tr>
<td>Naqu</td>
<td>91.89</td>
<td>7.52</td>
<td>0.59</td>
</tr>
</tbody>
</table>

Table 4: Percentage of precipitation contribution rate.

<table>
<thead>
<tr>
<th>Particle diameter (mm)</th>
<th>0−1 mm</th>
<th>1−2 mm</th>
<th>2−3 mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nyalam</td>
<td>55.63</td>
<td>37.32</td>
<td>7.05</td>
</tr>
<tr>
<td>Lhasa</td>
<td>54.60</td>
<td>38.16</td>
<td>7.24</td>
</tr>
<tr>
<td>Shigatse</td>
<td>51.12</td>
<td>40.49</td>
<td>8.39</td>
</tr>
<tr>
<td>Naqu</td>
<td>54.06</td>
<td>37.81</td>
<td>8.13</td>
</tr>
</tbody>
</table>

It can be observed from Table 3 that the number of precipitation particles with a distribution of 0−1 mm
constitutes the largest proportion, exceeding 91%, while the proportion of particles with a distribution of more than 3 mm is comparatively smaller, being less than 0.6%. The proportion of precipitation intensity below 1 mm constitutes over 51%, with other particles comprising less than 49%. The results indicate that the contribution of precipitation intensity on the Tibetan Plateau is primarily concentrated in small particles with a diameter less than 1 mm.

Simultaneously, it is observed that small particles below 1mm in Shigatse are smaller than those at other stations, and particles above 3 mm are larger than those at the other three stations. In contrast to the convective cloud precipitation in Zheng’an, Guizhou analyzed by Wang (Wang et al., 2020), where convective cloud particles less than 1 mm account for 64.4%, the contribution rate to precipitation is only 17%; Additionally, it significantly differs from the rainstorm in Hainan analyzed by Mao (Mao et al., 2020). Despite the proportion of less than 1 mm being 82.7%, the contribution rate is only 18.2%, and the rainstorm particle size spectrum in Hainan is remarkably wide. It is evident that the precipitation characteristics of convective clouds on the Qinghai–Tibet Plateau exhibit a particularity, wherein the diameter of precipitation particles is generally small, and the precipitation of small–diameter particles constitutes a substantial proportion of the total precipitation.

### 3.2. Microphysical characteristic parameters of precipitation

Calculation of characteristic parameters such as diameter (Dm), average volume diameter (Dv), mode diameter (Dd), dominant diameter (Dp), and medium diameter (Dnd) was conducted. Based on the comprehensive analysis of the characteristic parameters in Table 5, the Dm size at Lhasa station with the highest altitude (Naqu) is the largest, while the Dm size at the station with the lowest altitude (Lhasa) is the smallest. The values at the stations in Lhasa and Shigatse, with intermediate elevations, fall between the two extremes. The particle size at the Nyalam station, with a higher elevation, is also greater than that at the station in Shigatse, which is at a lower elevation. Simultaneously, the diameters of other features also increased with elevation, similar to Dm. Additionally, the differences in characteristic diameters among the stations in Nyalam (4519m), Naqu (4560m), Lhasa (3653m), and Shigatse (3910m) with similar altitudes are relatively small. The preceding analysis demonstrates a strong positive correlation between altitude and these six microphysical characteristic parameters.

<table>
<thead>
<tr>
<th>Station</th>
<th>Dm</th>
<th>Dv</th>
<th>Dd</th>
<th>Dp</th>
<th>Dnd</th>
</tr>
</thead>
</table>

Table 5: Microphysical parameters at the four stations.
3.3. Z−I relation distribution

Utilizing Formulae (6) and (7), the radar reflectivity (Z) and precipitation intensity (I) are calculated independently, and the data undergo fitting. The results are depicted in Figure 4.

Figure 4: The Z−I relationships at four stations. (A. Nyalam, B. Lhasa, C. Shigatse, and D. Naqu)

Figure 4 reveals that the suggested reference relation $Z=300 \times I^{1.4}$ inaccurately predicts precipitation, leading to an underestimation of precipitation intensity under identical radar reflectivity. With identical radar reflectance, the precipitation intensity is highest in Lhasa, followed by Shigatse, while the smallest precipitation intensity was observed in Naqu.

Table 6 shows the results of fitted Z−I relationships. Analyzing the altitude based differences in the Z−I relationship, the $a$ and $b$ coefficients are similar for the station at 3653 m (Lhasa) and the station at 3910 m (Shigatse), while $a$ and $b$ for the station at 4519 m (Nyalam) and the station at 4560 m (Naqu) are
close. This observation indicates that the fitting parameter $a$ is notably smaller, and the fitting parameter $b$ is larger for stations at higher altitudes.

Table 6: $Z$–$I$ relationship fitting results.

<table>
<thead>
<tr>
<th>Station</th>
<th>$Z = aI^b$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nyalam</td>
<td>$Z = 143.01 \times I^{1.41}$</td>
</tr>
<tr>
<td>Lhasa</td>
<td>$Z = 162.56 \times I^{1.31}$</td>
</tr>
<tr>
<td>Shigatse</td>
<td>$Z = 160.21 \times I^{1.33}$</td>
</tr>
<tr>
<td>Naqu</td>
<td>$Z = 143.81 \times I^{1.48}$</td>
</tr>
</tbody>
</table>

3.4. Precipitation particle distribution fitting

According to Formulas (8) and (9), the least squares method is applied to fit the $M$–$P$ and Gamma distributions of the mean raindrop spectrum of precipitation at the four stations. The results are presented in Figure 5 and Table 7.

As indicated in Table 7, $\mu$ decreases with increasing altitude in the Gamma distribution. A smaller $\mu$ corresponds to a wider raindrop spectrum, signifying a larger change in raindrop diameter with increasing
altitude. The raindrop diameter at higher altitudes is larger, corresponding to the precipitation microphysical characteristics calculated in Table 5. Conversely, the fitting results of the M−P distribution show that $N_0$ and $\lambda$ exhibit a clear increasing trend with height. In Figure 5, the abscissa represents particle diameter, and the ordinate represents particle number density. The curve trends at the four stations are relatively consistent. For Nyalam station, the M−P distribution is given by $N(D) = 218.78 \times e^{-3.53D}$, and the Gamma distribution is $N(D) = 282.14 \times D^{0.15} \times e^{-3.82D}$. For Lhasa station, the M−P distribution is $N(D) = 118.70 \times e^{-2.75D}$, and the Gamma distribution is $N(D) = 250.40 \times D^{0.43} \times e^{-3.56D}$. For Shigatse station, the M−P distribution is $N(D) = 130.35 \times e^{-2.79D}$, and the Gamma distribution is $N(D) = 216.08 \times D^{0.29} \times e^{-3.35D}$. Finally, for Naqu station, the M−P distribution is $N(D) = 177.22 \times e^{-3.10D}$, and the Gamma distribution is $N(D) = 238.95 \times D^{0.17} \times e^{-3.44D}$. In the Gamma distribution, two parameters, $\mu$ and $\lambda$, represent the curve shape factor and particle scale parameters, respectively, as shown in Equation (9). According to Equation (10), the two parameters $\mu$ and $\lambda$ for the four stations are fitted with an analytical binomial relationship, and the coefficients are presented in Table 8.

Table 7: Gamma fitting and M−P fitting results.

<table>
<thead>
<tr>
<th></th>
<th>Gamma</th>
<th>M−P</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$N_0$</td>
<td>$\mu$</td>
</tr>
<tr>
<td>Nyalam</td>
<td>284.90</td>
<td>0.15</td>
</tr>
<tr>
<td>Lhasa</td>
<td>253.26</td>
<td>0.44</td>
</tr>
<tr>
<td>Shigatse</td>
<td>217.69</td>
<td>0.30</td>
</tr>
<tr>
<td>Naqu</td>
<td>240.91</td>
<td>0.18</td>
</tr>
</tbody>
</table>

Table 8: $\mu$ and $\lambda$ binomial parameters

<table>
<thead>
<tr>
<th></th>
<th>$\lambda = a\mu^2 + b\mu + c$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$a$</td>
</tr>
<tr>
<td>Nyalam</td>
<td>0.2816</td>
</tr>
<tr>
<td>Lhasa</td>
<td>0.1717</td>
</tr>
<tr>
<td>Shigatse</td>
<td>0.0221</td>
</tr>
<tr>
<td>Naqu</td>
<td>0.0155</td>
</tr>
</tbody>
</table>

It can be observed from Figure 6 that, although the four curves bend towards the lambda axis, the degree of bending varies. The curves for Shigatse exhibit nearly straight curves, whereas the curves for Nyalam and Naqu are more pronounced in their curvature towards the lambda axis. The $\mu$−$\lambda$ relationship varies among the four stations, and this variation is associated with the mass−weighted diameter. Eq. (11) indicates that when $\lambda$ remains constant, a higher $\mu$ value corresponds to a greater mass−weighted average.
4. Conclusions

In this study, we conducted a statistical analysis of raindrop spectrum data above moderate rain at four sites in Tibet, considering different heights, latitudes, and longitudes. The analysis includes precipitation particle size distribution, particle landing speed, precipitation particle number density, and rainfall intensity at the end. Additionally, the relationship between Z–I distribution and rainfall rate, precipitation particle distribution fitting, and analysis of Gamma distribution μ–λ parameters for the precipitation raindrop spectrum characteristics at the four stations are examined. A comparison is made between the data from the four stations on the Qinghai–Tibet Plateau and some non–plateau areas. Simultaneously, the analysis of raindrop spectrum data at the Naqu station reveals certain similarities with previous studies (indicating convective cloud as the primary precipitation at Naqu station). However, some differences are noted, such as the mean spectral width of convective precipitation at the Naqu station being relatively narrow.

The relationship between precipitation particle size and particle landing velocity at the four stations
indicates that the falling velocity of the four stations essentially coincided when the particle size was less than 1.5 mm. For particle sizes greater than 1.5 mm, the final falling velocity of particles at the four stations is faster at medium and low altitudes than at high altitudes. This is attributed to instruments at high altitudes being closer to the clouds. At the four stations, the proportion of precipitation raindrop spectral particle size less than 1 mm exceeded 91%, and the contribution rate of precipitation was more than 51%. The characteristics of convective cloud precipitation over the Tibetan Plateau exhibit peculiarities that differ from the raindrop spectrum characteristics in the low-altitude areas of the mainland.

The six microphysical characteristic parameters at the four stations all increased with altitude, showing a positive correlation with altitude. Regarding the fitted Z–I relationship, the fitting parameter $a$ at the high-altitude station is significantly smaller, while the fitting parameter $b$ is larger. The particle spectrum of high-altitude stations is broader, with a larger equivalent diameter, and the reflectivity of high-altitude stations is significantly higher than that of low-altitude stations.

The concentration of small raindrops (less than 1 mm) in the raindrop spectrum of high-altitude stations on the Tibetan Plateau was higher. Both the M–P distribution and the Gamma distribution exhibit good fitting effects for low-altitude stations. Overall, the M–P fit performed better. In the relationship between the $\mu$ and $\lambda$ of the two parameters in the Gamma distribution, the larger the $\mu$, the larger the weighted average diameter of the mass when the $\lambda$ remains constant. In other words, the greater the $\mu$, the greater the precipitation intensity when $\lambda$ remains unchanged.

Data Availability Statement

The data used to support the findings of this study are available from the corresponding author upon request.

Author Contributions

Conceptualization, F.W. and G.C.; methodology, F.W. and Q.W.; software, Y.H. and Q.W.; writing—review and editing, F.W., Y.H. and Y.C.; resources, T.Z. and J.L.; supervision, T.Z. and G.C. All authors have read and agreed to the published version of the manuscript.
Competing interests

The contact author has declared that none of the authors has any competing interests.

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