

# Anticorrelation of Net Uptake of Atmospheric CO<sub>2</sub> by the World Ocean and Terrestrial Biosphere in Current Carbon Cycle Models

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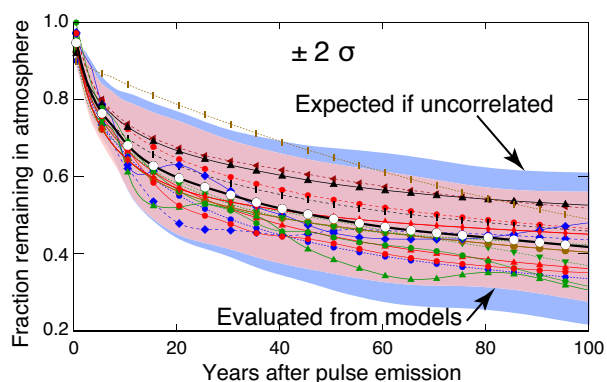
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**Abstract.** The rate at which atmospheric carbon dioxide (CO<sub>2</sub>) would decrease in response to decrease of anthropogenic emissions or cessation (net zero emissions) is of great scientific and societal interest. Such decrease in atmospheric CO<sub>2</sub> on the centennial scale would be due essentially entirely to transfer of carbon into the world ocean (WO) and the terrestrial biosphere (TB), which are sink compartments on this time scale. The rate of decrease of excess atmospheric CO<sub>2</sub> and the apportionment of this decrease into the two sink compartments has been examined in two prior model intercomparison studies, subsequent either to a pulse emission of CO<sub>2</sub> or to abrupt cessation of anthropogenic CO<sub>2</sub> emissions. The present study examines and quantifies inter-model anticorrelation in those studies in the net rate and extent of uptake of CO<sub>2</sub> into the two sink compartments. Specifically, in each study the time-dependent coefficients characterizing the net transfer rate into the two sink compartments, (evaluated as the net transfer rate normalized to excess atmospheric CO<sub>2</sub> above pre-pulse amount, for the pulse experiment; or as the net transfer rate divided by excess atmospheric CO<sub>2</sub> above preindustrial amount, for the abrupt cessation experiment) was found to exhibit strong anticorrelation across the participating models. That is, models for which the normalized rate of uptake into the WO was high exhibited low uptake rate into the TB, and vice versa. This anticorrelation in net transfer rate results in anticorrelation in net uptake extent into the two compartments that is substantially greater than would be expected simply from competition for excess CO<sub>2</sub> between the two sink compartments. This anticorrelation, which is manifested in diminished inter-model diversity, can lead to artificially enhanced confidence in current understanding of the consequences of potential future reductions of CO<sub>2</sub> emissions and in the global warming potentials of non-CO<sub>2</sub> greenhouse gases relative to that of CO<sub>2</sub>.

## 500 character summary

Anticorrelation in uptake of atmospheric CO<sub>2</sub> following pulse emission or abrupt cessation of emissions is examined in two key model intercomparison studies. In both studies net transfer coefficients from the atmosphere to the world ocean and the terrestrial biosphere are anticorrelated across models, reducing inter-model diversity in decrease of atmospheric CO<sub>2</sub> following the perturbation, increasing uncertainties of global warming potentials and consequences of prospective emissions reductions.

## Graphical Abstract



## 30 1 Introduction

Essentially the only means by which excess carbon dioxide (CO<sub>2</sub>), i.e., above preindustrial, is removed from the atmosphere on the centennial scale is net uptake by the world ocean (WO) and the terrestrial biosphere (TB). Here the term net uptake is used to emphasize that transfer of CO<sub>2</sub> from the atmosphere to these two compartments of Earth's biogeosphere is highly reversible; hence it is this net transfer that is pertinent to the disposition of excess atmospheric CO<sub>2</sub> due to anthropogenic emissions on this time scale. Historically, over the industrial era, the increase in atmospheric CO<sub>2</sub> has been about half of anthropogenic emissions (Bacastow and Keeling, 1973; Friedlingstein et al., 2022). Hence the processes governing this net uptake, and model-based representation of these processes, are of great scientific and societal interest. The need for confident understanding and model based representation of these processes has become increasingly acute because of the societal need to assess the consequences of prospective reduction or cessation (net zero emissions) of anthropogenic CO<sub>2</sub> emissions and to develop effective strategies to achieve specified targets, such as mixing ratio of atmospheric CO<sub>2</sub> or increase in global temperature.

Briefly, net drawdown of excess CO<sub>2</sub> (above preindustrial) from the atmosphere to the ocean consists of highly reversible exchange of CO<sub>2</sub> between the atmosphere and the upper ocean, resulting in increased concentration of dissolved inorganic carbon (DIC) in the upper ocean over time relative to its preindustrial value, followed by largely irreversible net transfer of DIC from the upper ocean to the deep ocean associated with water mass exchange from the upper ocean to the deep ocean. Similarly uptake of excess CO<sub>2</sub> from the atmosphere to the terrestrial biosphere consists of rapid exchange of carbon between the atmosphere and the TB in association with increased photosynthesis and respiration due to increased atmospheric CO<sub>2</sub>, with a small fraction of the increased carbon stock in the TB being taken up by long-lived woody and soil components of the TB. It is accurate representation of these processes is the objective and requirement of models of varying degrees of complexity that are to be used in assessment of the response of atmospheric CO<sub>2</sub> to potential future changes in CO<sub>2</sub> emissions.

A key means of assessing current understanding and model-based representation of processes governing the drawdown of atmospheric CO<sub>2</sub> in carbon-cycle models is model intercomparison studies, more specifically comparison of the modeled response of the change of the amount of carbon in the atmosphere, the WO, and the TB in response to a perturbation in emissions. (A perturbation in emissions is required because in the absence of such a perturbation the carbon stocks in the three

55 compartments would be in steady state, i.e., not changing.) Such intercomparison studies are intended to reveal, through inter-  
model diversity in model response, the extent to which model-based representations of the processes governing net uptake of  
CO<sub>2</sub> differ among the participating models, and thus to serve as a measure of uncertainty in understanding. In principle as well  
such intercomparisons might reveal reasons for differences among the models and lead to improvement in areas of disagreement.

60 In this study attention is directed to two key model intercomparison studies that examined changes in carbon stocks in the three  
compartments (atmosphere, WO, and TB) following abrupt changes in CO<sub>2</sub> emissions. The three compartments are considered a  
closed system; consequently the net change in atmospheric CO<sub>2</sub> subsequent to the pulse (or cessation) is the complement of the  
net changes in carbon stocks of the other two compartments. Joos et al. (2013; hereinafter J13) reported the disposition of a pulse  
emission of CO<sub>2</sub> of magnitude 100 Pg C emitted into the atmosphere as amount of increase of carbon in each of the three  
compartments as a function of time subsequent to the emission pulse, thereby obtaining impulse response functions (IRFs;  
fraction of emitted pulse in each compartment as a function of time subsequent to the pulse) for each of the three compartments.  
65 MacDougall et al. (2020; hereinafter M20), examined the decrease in atmospheric CO<sub>2</sub>, and the net uptake into the WO and the  
TB, subsequent to abrupt cessation of anthropogenic CO<sub>2</sub> emissions (ZECMIP study, Zero Emissions Commitment Model  
Intercomparison Project). The two studies are not wholly independent in that several models or modeling groups participated in  
both intercomparisons.

70 Because these two studies reported not just the decrease in atmospheric CO<sub>2</sub> but also net uptake of carbon by the WO and the  
TB, it is possible to assess inter-model diversity not just in the decrease in atmospheric CO<sub>2</sub> but also in the net changes in the  
carbon stocks in other two compartments in response to the perturbation in emissions, as governed by the process represented in  
the models. Here it should be noted that some inherent anticorrelation across the models is expected in the extent of uptake into  
the WO and the TB; because the WO and the TB are the only sinks of atmospheric CO<sub>2</sub>, a greater uptake into one compartment  
would necessarily result in a lesser uptake into the other. In contrast, the transfer coefficients characterizing the net uptake of  
75 atmospheric CO<sub>2</sub> into the WO and the TB, defined as the time-dependent net rate of uptake into the compartment divided by the  
time-dependent amount of excess atmospheric CO<sub>2</sub>, would be expected to be uncorrelated if treatment of the processes governing  
the net uptake rate into one compartment were independent from that governing the net uptake rate into the other compartment  
across the set of models participating in the studies. Here the inter-model correlations in extent and rate of uptake of atmospheric  
CO<sub>2</sub> are examined to assess the independence of the representation of uptake of atmospheric CO<sub>2</sub> into the WO and the TB in the  
80 models participating in each of the two intercomparison studies. Any substantial negative correlation transfer coefficients  
representing uptake of atmospheric CO<sub>2</sub> into the two compartments would be indicative of compensating effects, whereby  
models having net uptake rate into one compartment have higher net uptake rate into the other, thereby resulting in a reduced  
inter-model diversity in the rate and extent of decrease of atmospheric CO<sub>2</sub>. As inter-model diversity is commonly taken as a  
measure of uncertainty, any such negative correlation would artificially reduce the perceived uncertainty in the rate of drawdown  
85 of excess atmospheric CO<sub>2</sub> subsequent to a perturbation.

## 2 Analysis and findings

### 2.1 Joos et al. (2013)

J13 examined and reported the extent of decrease of atmospheric CO<sub>2</sub> and the integrated net flux from the atmosphere into the ocean and into the TB subsequent to a 100 Pg-C emission pulse added to an atmosphere having prior CO<sub>2</sub> mixing ratio of 389 ppm as the difference between the run with the 100 Pg pulse and a reference run with mixing ratio held constant at 389 ppm. Participating models were three comprehensive Earth System Models (ESMs), seven Earth System Models of Intermediate Complexity (EMICs), and four box-type models. The disposition of excess atmospheric carbon was presented graphically as IRFs, the fractions of the emitted pulse in the atmosphere, the ocean and the TB, over two time periods, 0.5 to 100.5 years subsequent to the pulse and 100.5 to 1000.5 years. In this analysis results are examined only for the first 100 years, over which time the excess atmospheric stock resulting from the pulse decreased by about 60 %. The J13 study has assumed considerable importance because its multimodel mean is widely used for evaluation of the consequences of prospective future profiles of CO<sub>2</sub> emissions and for comparison of integrated radiative forcing of non-CO<sub>2</sub> greenhouse gases with that of CO<sub>2</sub> (so-called greenhouse warming potentials; e.g., Myhre et al., 2013, IPCC Fifth Assessment Report). The results of the J13 study have also been used to represent the response to pulse emission of CO<sub>2</sub> in simple climate emulators such as the widely used FAIR (Finite Amplitude Impulse-Response) climate emulator (Millar et al., e.g. Smith et al. 2018).

The time dependence of the IRFs for the several compartments over the 100-year time period following pulse emission, Fig. 1(a), shows that all models exhibited monotonic or nearly monotonic net increase in ocean IRF over this period, with the IRFs of the several models relatively smooth over the time period. In contrast several of the models exhibited substantial fluctuations in extent of net uptake into the TB, Fig. 1(b); a negative derivative denotes a temporary negative net flux, i.e., net flux from TB to atmosphere. The atmospheric IRFs, nominally the complements of the sum of ocean and TB IRFs, exhibited fluctuations more or less comparable to those of TB IRF for the several models; here a positive slope denotes a temporary increase in atmospheric stock. Comparison of the inter-model diversity of the IRFs (as shown by the ranges of pink shading denoting  $\pm 2$  s.d.) on the same vertical scale for the several IRFs demonstrates that the inter-model diversity of the atmospheric IRFs, Fig. 1(c), to be systematically and substantially lower than that for the TB. As the decrease of the atmospheric stock is the sum of the uptakes into the ocean and TB compartments, the variance across the models of the atmosphere IRFs would, if uptake into the ocean and TB were uncorrelated across the model, be expected to exceed the variance for both the ocean and TB IRFs. The contravention of that expectation must therefore be due to anticorrelation of the IRFs across the models. This anticorrelation is examined further in Fig. 1(d), by means of the regression slope of IRF(WO) vs IRF(TB), which is negative throughout essentially the entire 100-year time period, approaching -0.4 by the end of the time period, with the difference from the value 0, which would be expected in the absence of anticorrelation of the regression slope up to several fold greater than the s.d. of that slope obtained from the linear least-squares regression. (Throughout this study correlation coefficients, regression coefficients, and their uncertainties are calculated by the linear regression model, as described, e.g., by Press et al., 1997.) The anticorrelation is examined further in Fig. 1(e), which shows the Pearson *r* correlation coefficient to be negative throughout the time period, approaching -0.9 at the end of the time period, again indicative of strong anticorrelation of IRF(WO) and IRF(TB) across the set of models that participated in this intercomparison study.

25 What are the causes of the anticorrelation? It would seem that there are two potential contributions to this. First would be competition between the two sinks for the excess atmospheric CO<sub>2</sub> remaining from the pulse at a given time subsequent to the pulse; if, at a given time, more of this excess CO<sub>2</sub> has previously been drawn down into one compartment, there would be less CO<sub>2</sub> available to be drawn down into other compartment, resulting in anticorrelation in the amounts in the two compartments, simply because of this competition effect. A second, more intrinsic and concerning source of anticorrelation would be compensating treatments in the several models of the processes that govern the uptake of the excess CO<sub>2</sub> from the pulse emission by the WO and the TB, such that if the rate of uptake into the WO in a given model were high relative to the other models, the rate of uptake into the TB would be low, and vice versa.

30 An example of the anticorrelation across the suite of models between the IRFs for uptake into the ocean and the TB is shown in Fig. 2(a) for time subsequent to pulse injection, time  $t = 99.5$  years. This example likewise shows strong anticorrelation, with models exhibiting high uptake into the ocean exhibiting low uptake into the TB, and vice versa. The Pearson  $r$  coefficient is negative, with value -0.85, and  $r^2$ , the fraction of the variance in the relation between IRF(WO) and IRF(TB) accounted for by the regression is 0.72. The standard deviations of the IRFs obtained with the several models at  $t = 99.5$  yr, are 0.061 and 0.118, respectively, much greater for the TB than for the ocean, as shown also in Fig. 1(a) and (b). Using these values for  $\sigma_O$  and  $\sigma_T$   
35 yields an unbiased estimate of  $\sigma_A$  at  $t = 99.5$  yr, evaluated as the quadrature sum,  $\sigma_A = (\sigma_O^2 + \sigma_T^2)^{1/2} = 0.132$ , nearly twice the value obtained from the modeled atmospheric IRFs themselves, 0.071.

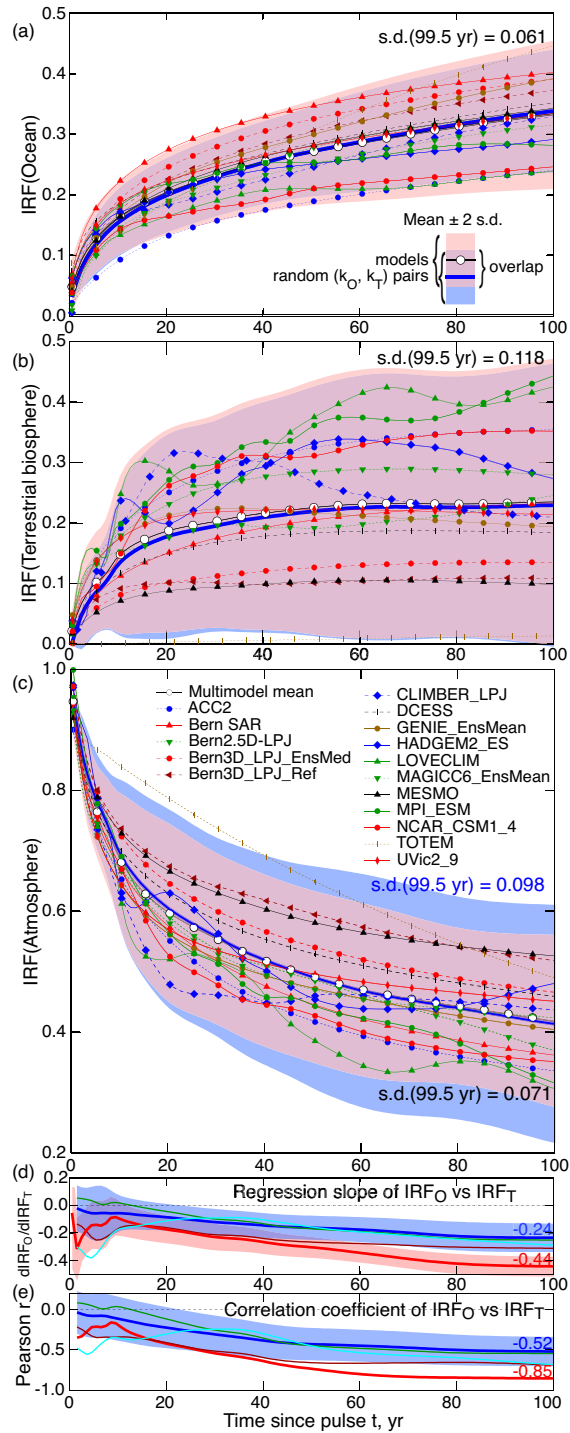
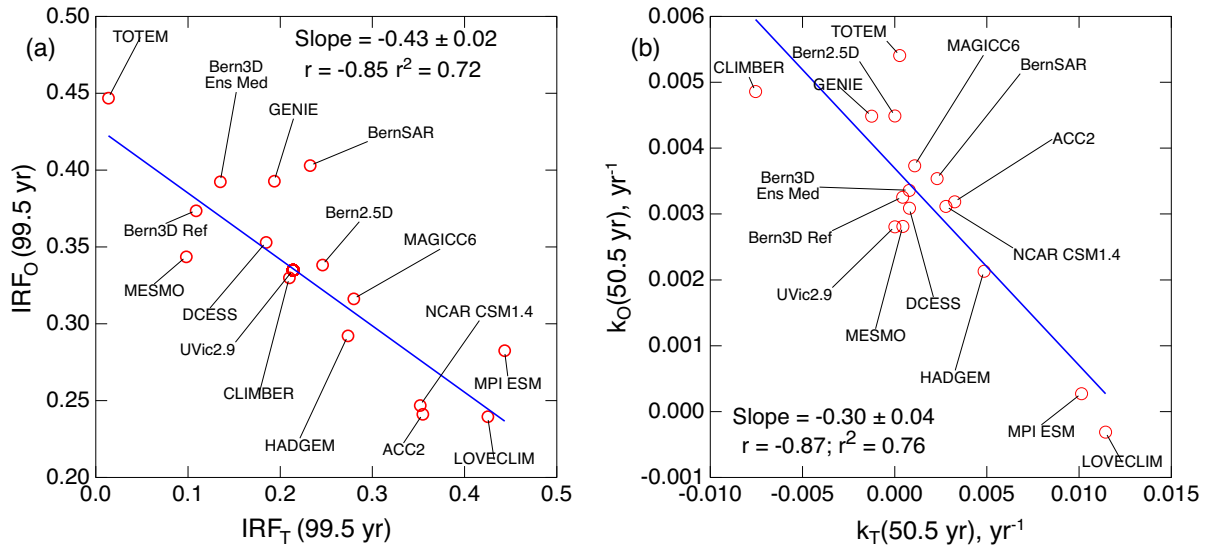


Figure 1. Time dependent impulse response functions (IRF's,  $f$ ) for the perturbations in stocks in (a), the world ocean  $f_O$ ; (b), the terrestrial biosphere  $f_T$ ; and (c), the global atmosphere  $f_A$ , as a function of time  $t$  subsequent to emission of

40 a 100-Pg(C) pulse of CO<sub>2</sub> into the atmosphere, in excess of the amount of carbon that would be present in each  
 compartment for atmospheric CO<sub>2</sub> held constant at the value at the time of emission of the pulse, as calculated by the  
 models that participated in the model intercomparison study of Joos et al. (2013); for details of the intercomparison and  
 identification of the models see J13; the three panels are to the same scales. Adapted from Joos et al. (2013); line codes  
 and symbol shapes are as in J13. Pink shading denotes  $\pm 2$  s.d. about the multimodel mean; s.d.'s at  $t = 99.5$  years after  
 45 pulse are in black text; thick blue curve and blue shading denote the mean and  $\pm 2$  times the mean s.d. of 120 instances  
 of IRFs calculated with randomly sorted pairs of net transfer coefficients ( $k_O, k_T$ ) taken from the sets of net transfer  
 coefficients evaluated from the data presented by J13; mean s.d. for  $f_A$  at  $t = 99.5$  yr in blue text in (c). Key at lower  
 right of  $a$  shows mean (black, white markers)  $\pm 2$  s.d. for models (pink shading), mean (thick dark blue)  $\pm 2$  s.d. (light  
 blue shading) for randomly sorted ( $k_O, k_{T,i}$ ) pairs, and region of overlap (violet shading). Attention is called to slight  
 50 non-overlapped regions in  $a$  and  $b$  and large non-overlapped region in (c). (d), Thick red, regression slope of linear fit  
 of  $f_O$  vs  $f_T$  among the models for each year over the 100-year period subsequent to pulse emission (example shown in  
 Fig. 2); pink shading denotes estimated error in slope as obtained from the regression ( $\pm 1$  s.d.); thick blue, mean of  
 regression slope of linear fit of  $f_O$  vs  $f_T$  evaluated for 120 instances of randomly sorted ( $k_O, k_{T,i}$ ) pairs; blue shading  
 denotes  $\pm 1$  s.d. of these 120 instances; thin curves denote time series of regression slopes for three instances of such  
 55 random pairings. (e), Pearson correlation coefficient  $r$  of regression of  $f_O$  vs  $f_T$  for the several models, thick red; thick  
 blue and blue shading, mean and s.d. of  $r$  for 120 instances of IRFs, as in  $d$ ; thin curves denote correlation coefficients  
 for three instances of those regressions.



60 Figure 2. (a). IRF for uptake of excess CO<sub>2</sub> by the world ocean versus that by the terrestrial biosphere, both given as  
 fraction relative to the magnitude of the pulse, at time  $t = 99.5$  years subsequent to pulse injection, as represented by  
 the models that participated in the model intercomparison study of Joos et al. (2013, J13). Blue line denotes linear  
 regression; also shown are the regression slope; the Pearson correlation coefficient  $r$ , the negative value of which  
 denotes anticorrelation; and  $r^2$ , the fraction of the variance that is accounted for by the regression. For identification

of models see J13. (b). As in (a), but for transfer coefficient for net uptake of excess CO<sub>2</sub> from the atmosphere to the  
65 WO  $k_O$  versus that from the atmosphere to the terrestrial biosphere  $k_T$  at time  $t = 50.5$  yr; negative values denote net  
transfer from the ocean or the TB to the atmosphere at that time.

Assessment of whether, and to what extent, the anticorrelation is due to the treatment of the processes versus due simply to  
competition requires examination of the rates of transfer of excess CO<sub>2</sub> as a function of time subsequent to the pulse, rather than  
of the IRFs themselves, which are the integrals of the transfer rates. The IRFs would be subject to the competition effect,  
70 whereas the time-dependent transfer rates would not. Hence, to assess the extent to which the anticorrelation is due to the  
competition effect a similar analysis was conducted of the coefficients characterizing the rate of net transfer of excess CO<sub>2</sub> from  
the atmosphere into each of the sink compartments. To this end the net transfer coefficients into the ocean and the terrestrial  
biosphere were evaluated as the rate of net uptake of CO<sub>2</sub> (reckoned as C) into the specific compartment (WO or TB) per excess  
stock remaining in the atmospheric compartment at a given time:

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$$k_O = \frac{df_O/dt}{f_A} \text{ and } k_T = \frac{df_T/dt}{f_A} \quad (1)$$

respectively, where  $f_O$  and  $f_T$  denote the time-dependent impulse response functions (IRFs) of the two compartments and  $f_A$   
similarly denotes the time dependent IRF of the atmospheric stock, all expressed as fractions  $f$  of the carbon mass of the emitted  
pulse. Dividing the time-dependent net transfer rates ( $df_O/dt$ ,  $df_T/dt$ ) by the time-dependent atmospheric IRF ( $f_A$ ) to obtain the  
80 time-dependent net transfer coefficients ( $k_O$ ,  $k_T$ ) results in quantities that would be constant if the net fractional uptake rate of  
excess CO<sub>2</sub> exhibited a constant proportionality to the amount of excess CO<sub>2</sub>, much like a rate constant for a first-order reaction  
in chemical kinetics. The departures from constancy in  $k_O$ , Fig. 3(a), and to much greater extent in  $k_T$ , Fig. 3(b), are  
manifestations of the effects of the history of prior uptake of CO<sub>2</sub> by the two compartments and of the time-dependent states of  
these compartments affecting this net uptake.

85 Similarly the coefficient denoting the net rate of decrease of the IRF for stock in the global atmosphere is given by

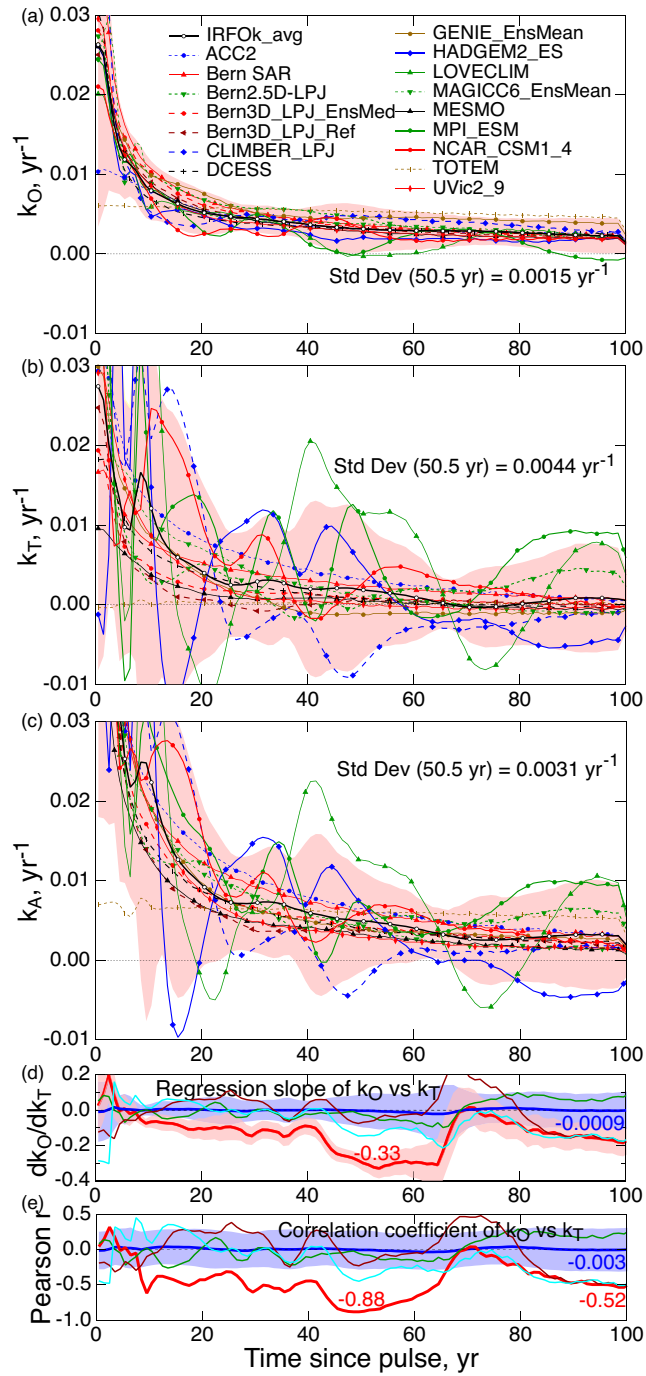
$$k_A = -\frac{df_A/dt}{f_A}; \quad (2)$$

the derivatives were calculated numerically from the IRFs presented by J13. (As the figures of J13 were published  
as vector graphics, it was possible to digitize the data quite precisely; the data are also tabulated at  
[https://climatehomes.unibe.ch/~joos/IRF\\_Intercomparison/](https://climatehomes.unibe.ch/~joos/IRF_Intercomparison/)). The results of this examination are presented in Fig. 3 as a function  
90 of time subsequent to the pulse and in Fig. 2(b) for a single value of time. At first look, the transfer coefficients plotted similarly  
to the IRFs are similar to the IRFs themselves. However the values of the  $k$ 's, being proportional to the derivatives of the IRFs,  
exhibit much greater fluctuations than the IRFs themselves (especially  $k_T$ ), some being rather smooth, others exhibiting rather  
large, high frequency fluctuations. A local maximum in the IRF results in a change in sign (from positive to negative) in the net  
transfer coefficient; that is net transfer of excess CO<sub>2</sub> resulting from the emission pulse being transferred thereafter from the WO  
95 or the TB back to the atmosphere; and correspondingly a local minimum in the IRF resulting in a change in sign in the transfer



00 coefficient from negative to positive. Essentially no such return transfer from the ocean to the atmosphere is exhibited by the any  
of the models (very slight return transfer for two of the models); in contrast, all but three of the models exhibited return flux from  
the TB to the atmosphere at one or more times in the 100-yr period examined, Fig. 3(b), with two of the models exhibiting  
instances of return flux of greater than 1 % yr<sup>-1</sup> relative to the amount of remaining excess atmospheric stock. As with the IRFs  
05 themselves, the anticorrelation between the transfer coefficients  $k_O$  and  $k_T$  is demonstrated graphically by the narrower spread of  
 $k_A$  than  $k_T$ ; Figs. 3(a)-(c) are drawn to the same scale. Quantitatively, as manifested by the traces for regression slope and  
correlation coefficient, throughout the time over which the two compartments were drawing down the major fraction of the  
pulse-emitted CO<sub>2</sub>, roughly the first 60 years or so subsequent to the pulse, Fig. 1(c), there is again systematic anticorrelation,  
here between  $k_O$  and  $k_T$  (negative of Pearson  $r$  as great as 0.88). An example, for time  $t = 50.5$  yr subsequent to the pulse, Fig.  
15 2(b), shows quite strong anticorrelation in the transfer coefficients into the WO and the TB across the models,  $r^2 = 0.72$ . This  
anticorrelation in the transfer coefficients themselves rules out the anticorrelation in the IRFs as being due solely to the  
competition effect and demonstrates that for models for which the transfer rate into the ocean was high relative to the multimodel  
mean, the transfer rate into the TB was low relative to the multimodel mean, and vice versa.

10 The cause of the anticorrelation of the IRFs was further assessed by calculations of the IRFs in which the  $k_T$ 's of the several  
models were randomly paired with the  $k_O$ 's, with examination of the resultant correlations between IRFs for uptake by the WO  
and the TB. First, the possibility of any correlation among the random pairs of the time dependent transfer coefficients was  
assessed; as anticipated, these random pairings exhibited essentially no correlation. The mean regression slope over the 120  
instances was essentially zero over the 100 yr period; mean at  $t = 100$  yr -0.0009 (Fig. 3(d)), and the mean Pearson  $r$  was  
likewise essentially zero, with standard deviation about 0.25 over the time range, with mean at  $t = 100$  yr -0.003 (Fig. 3(e)). To  
15 be sure there was meandering of both quantities for individual instances of pairing, three of which are shown in the figures, with  
some of these individual curves meandering considerably outside  $\pm 1$  s.d., but that is of course to be expected, and none  
exhibited the systematic strong anticorrelation exhibited by IRFs of the models, as shown by the thick red curve, with  $-r$  as great  
as 0.88, or 3.5 times the s.d. obtained with the randomly paired  $k_O$  and  $k_T$ .



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Figure 3. Net transfer coefficients from the atmosphere into (a), the world ocean  $k_O$  and (b), the terrestrial biosphere  $k_T$  as a function of time  $t$  subsequent to emission of a 100-Pg (C) pulse of  $CO_2$  into the atmosphere, evaluated from the

25 results from the model intercomparison of Joos et al., 2013; similarly, (c), the fractional rate of net decrease of excess CO<sub>2</sub> stock in the atmosphere; negative value denotes temporary net increase. Pink shading denotes  $\pm 2$  s.d. about the multimodel mean; s.d.'s at  $t = 50.5$  yr are indicated; the three panels are to the same scale. For identification of the models see J13; line codes and symbol shapes are as in J13. (d), Regression slope, thick red, of linear fit of  $k_O$  vs  $k_T$  for the several models for each year over the 100-year period subsequent to pulse emission (see Fig. 2(b) for example), with value at  $t = 53.5$  yr indicated, red text; pink shading denotes  $\pm 1$  s.d.; mean regression slope, thick blue, and  $\pm 1$  s.d., blue shading, for 120 instances of  $k_O$  and  $k_T$  of different models being randomly paired, with mean value at  $t = 100$  yr indicated, blue text; thin curves denote time series of three instances of those regression coefficients. (e),

30 Pearson correlation coefficient  $r$  of linear regression of  $k_O$  vs  $k_T$  for the several models, thick red, with values at  $t = 49.5$  and  $99.5$  yr indicated, red text; blue and blue shading, mean and  $\pm 1$  s.d. of  $r$ , for 120 instances of  $k_O$  and  $k_T$  of different models being randomly paired, with mean value at  $t = 100$  yr indicated, blue text; thin curves denote time series of three instances of those correlation coefficients.

35 To assess the contribution of the competition effect to the anticorrelation in the IRFs themselves, the randomized pairs of time-dependent  $k_O$  and  $k_T$  were used to calculate time-dependent IRFs corresponding to those randomized  $(k_O, k_T)$  pairs. To do this, first the time-dependent IRF of the atmospheric stock was evaluated for each  $(k_O, k_T)$  pair as the integral

$$f_A(t) = \exp\left(-\int (k_O(t) + k_T(t)) dt\right). \quad (3)$$

Then the IRFs of the WO and the TB were evaluated for each  $(k_O, k_T)$  pair as the integrals of the transfer rates.

$$f_O(t) = \int k_O(t) f_A(t) dt \quad \text{and} \quad f_T(t) = \int k_T(t) f_A(t) dt \quad (4)$$

40 The accuracy of this approach was demonstrated by examination of the IRFs calculated in this way for the original  $(k_O, k_T)$  pairs, which closely reproduced the original IRFs. The results of this examination are shown in Fig. 3(d) for the regression slope and Fig. 3(e) for the correlation coefficient of  $f_O$  vs  $f_T$  over the 100 yr period. In each panel the thick red curve denotes the time-dependent quantity evaluated for the  $(k_O, k_T)$  pairs of the 16 models of the Joos et al., study, as described above. The same analysis was then conducted for 120 instances in which a randomly sorted set of transfer coefficients  $k_{T,i}$  was paired with the set

45 of transfer coefficients in the Joos et al., study  $k_O$ , and the model was run out for 100 years for each randomized pair of transfer coefficients  $(k_O, k_{T,i})$ ; that process was then carried out for a total of 120 runs with randomized pairs  $(k_O, k_{T,i})$ ,  $0 \leq i \leq 119$ . The thick blue curve denotes the mean of the respective quantity for the 120 randomized pairs  $(k_O, k_{T,i})$  and the blue shading denotes the s.d. of the respective quantity. (As with the transfer coefficients, the curves for individual  $(k_O, k_{T,i})$  pairs meandered about the mean.) The non-zero values of the mean regression slope and the mean correlation coefficient of the IRFs

50 evaluated with the randomized pairs of transfer coefficients are measures of the competition effect, the negative regression coefficient  $-r$  increasing over the 100 year period, to 0.52 by the end of that period, a substantial fraction of the value for the models themselves, 0.85. The enhancement of the anticorrelation in IRFs due to anticorrelation of the transfer coefficients may be inferred from the increase in the regression slope of  $f_O$  vs  $f_T$  for the original models compared to that for the randomized  $(k_O, k_T)$  pairs, a factor of about 1.8.

55 The effect of anticorrelation between the net transfer coefficients in the models is examined also in Fig. 1 (a)-(c), by comparison of the standard deviations of the IRFs of the several compartments for each year up to 100 years following the pulse as calculated

in model runs with 120 instances of the randomized pairs  $(k_O, k_T, i)$  with those of the models themselves. (Here the mean of the IRFs obtained from the integration, which was initiated at time subsequent to the pulse  $t = 0$ , was set to match the mean of the IRFs presented by J13 at  $t = 0.5$  yr, the earliest time presented by J13.) The s.d.'s of the IRFs for the WO and the TB for the randomized pairs, shown by the blue shading denoting  $\pm 2$  s.d. about the mean are essentially identical over the entire 100-year period to the s.d.'s for the models, shown by the pink shading, with nearly complete overlap (purple) between the blue and pink shading and only slight regions of non-overlap – pink toward the tops of the shaded areas in Figs. 1(a) and (b), and a slight region of non-overlapped blue toward the bottom of the shaded area in Fig. 3(b). However the s.d. for the IRF of the atmosphere calculated with the randomized pairs  $(k_O, k_T, i)$  is substantially greater than that for the models, Fig. 1(c) as manifested by the substantial region of non-overlapped blue extending well above and below the overlap region. The decrease in inter-model spread of the atmospheric IRF of the models participating in the intercomparison relative to that calculated for random pairing of the transfer coefficients is thus confidently attributed to anticorrelation of the sets of transfer coefficients across the models.

By the several measures presented here the inter-model spread of the IRFs denoting the decrease of atmospheric  $\text{CO}_2$  subsequent to injection of a pulse of  $\text{CO}_2$  presented in by J13 would seem to be well less than would be expected in the absence of inter-model anticorrelation of the normalized net transfer rates of atmospheric  $\text{CO}_2$  to the WO and the TB. This reduction would seem to be due to compensating treatments of the underlying processes that control this transfer, such that for models for which  $k_O$  was high relative to the multimodel mean, the average value of  $k_T$  was low relative to the multimodel mean, and vice versa.

## 2.2 MacDougall et al. (2020)

The ZECMIP model intercomparison study (MacDougall et al., 2020; M20) was similar to that of Joos et al. (2013), except that it examined the drawdown of atmospheric  $\text{CO}_2$  (and uptake of this atmospheric  $\text{CO}_2$  by the world ocean and terrestrial biosphere) subsequent to an abrupt cessation of emissions, rather than in response to a pulse emission. The protocol of the M20 study was that atmospheric  $\text{CO}_2$  was forced, in each of the models, to increase from its preindustrial value at 1 % per year until cumulative emissions reached 1000 PgC (by coincidence, atmospheric  $\text{CO}_2$  approximately double preindustrial in most models), at which point anthropogenic emission was abruptly ceased. Participating models were nine ESMs, and nine EMICs. The paper itself and supplementary material reported stocks of excess carbon in the atmosphere, the WO, and the TB and net transfer rates from the atmosphere to the WO and the TB subsequent to the cessation. Results from that study are examined here similarly to the examination of the results from the study of J13. Data were obtained from the supplementary material of M20 and at <http://terra.seos.uvic.ca/ZEC/> (kindly provided as a single zip file by Andrew MacDougall).

The decrease of excess  $\text{CO}_2$  in the atmosphere and increases in the carbon stocks of the WO and the TB, subsequent to cessation of anthropogenic emissions, are all shown in Fig. 4 (a)-(c) as a fraction  $f$  relative to the amount of excess  $\text{CO}_2$  in the atmosphere at the time of cessation; all figures are at the same scale. The normalization to initial excess atmospheric  $\text{CO}_2$ , which accounts for differences among the models in the amount of excess atmospheric  $\text{CO}_2$  at the time of cessation, permits comparison across the set of models of the apportionment of net transfer from the atmosphere, i.e., the decrease in  $f_A$ , from its initial value of unity, into the WO,  $f_O$ , and the TB,  $f_T$ . The differences in the stocks in the WO and the TB relative to their values at the time of cessation, initially zero, increase as a function of time subsequent to cessation, as excess atmospheric  $\text{CO}_2$  present at the time of cessation is taken up by each of those compartments in the absence of further anthropogenic emissions (i.e., net-zero

95 anthropogenic emissions). This intercomparison is thus highly pertinent to a prospective transition to net-zero emissions, in contrast to the J13 study, which is pertinent to the disposition of an amount of CO<sub>2</sub> emitted at a given time. Because of these different protocols the results of the two studies cannot not be directly compared. Importantly the initial changes in the stocks following the pulse emission, relative to the magnitude of the pulse (J13) are much greater than those following abrupt cessation of emissions, relative to the amount of excess atmospheric CO<sub>2</sub> at the time of cessation (M20).

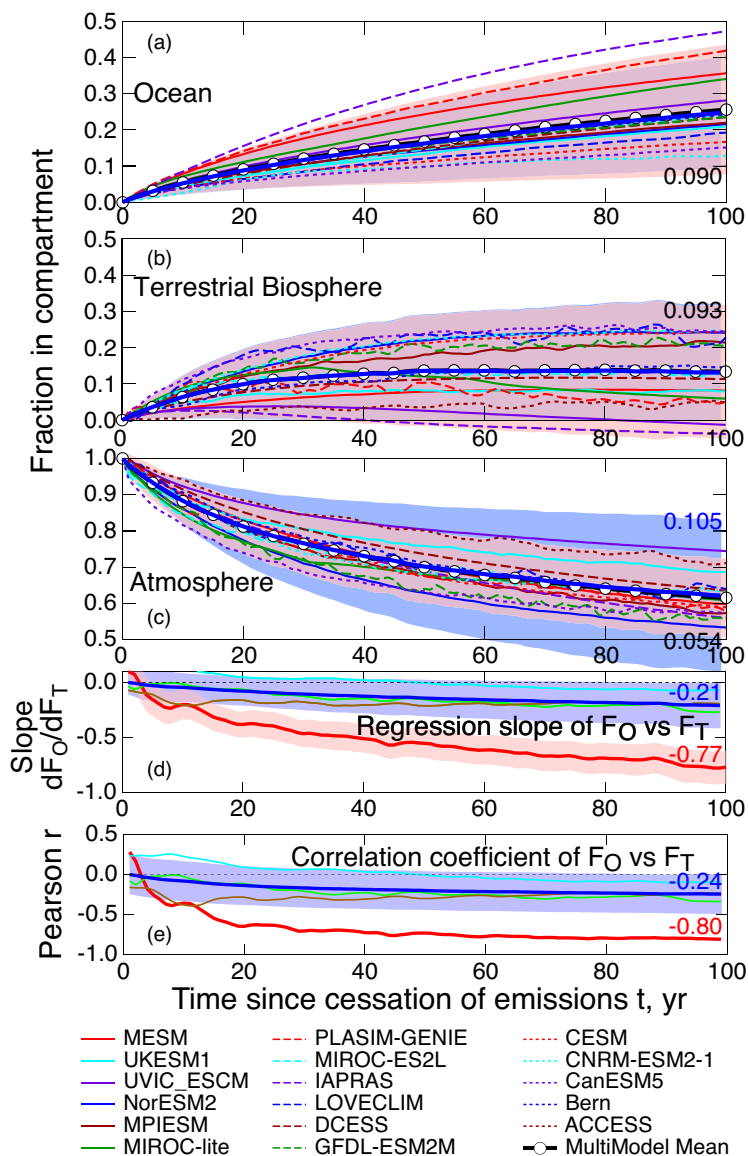


Figure 4. Time dependence of the fraction of excess atmospheric CO<sub>2</sub> (above preindustrial) at the time of cessation of anthropogenic emissions taken up by (a), the world ocean, and (b), the terrestrial biosphere, and (c), remaining in the atmosphere, subsequent to abrupt cessation of emissions,  $f_O$ ,  $f_T$ , and  $f_A$ , respectively, as calculated by the

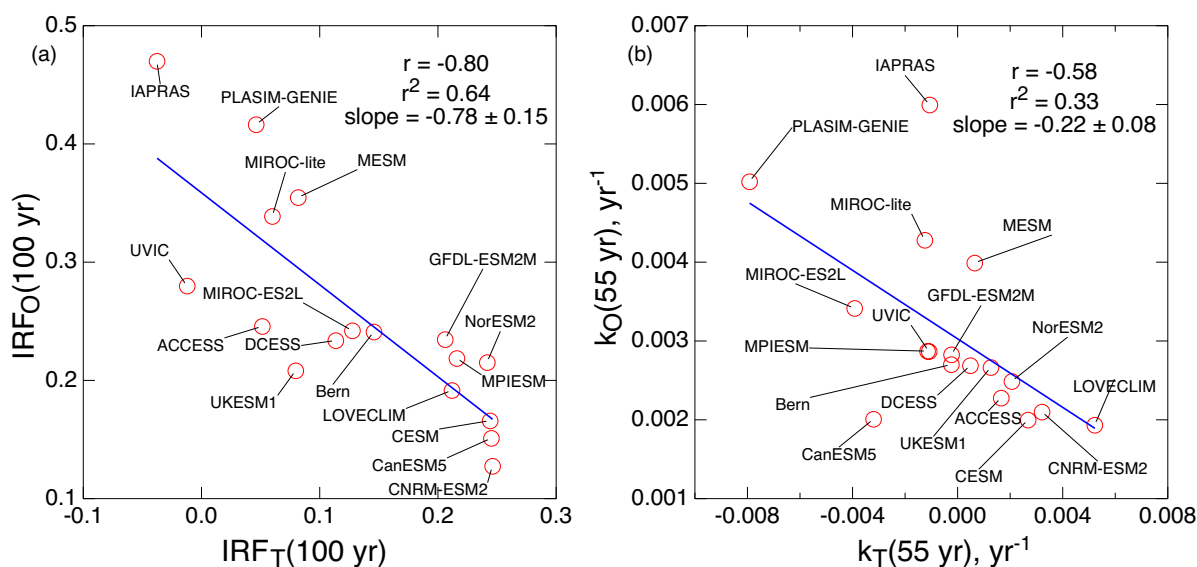
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models that participated in the ZECMIP intercomparison (MacDougall et al. 2020, M20). For details of the intercomparison and identification of the participating models see M20. Pink shading denotes  $\pm 2$  s.d. about the multimodel mean; s.d.'s at  $t = 100$  yr after cessation in black text. Thick blue curve and blue shading denote mean and  $\pm 2$  times the mean s.d. of 120 instances of IRFs calculated with randomly sorted pairs of net transfer coefficients ( $k_O, k_T$ ) taken from the set of net transfer coefficients evaluated from the data presented by M20; violet shading denotes overlap of blue and pink shading as in Fig. 1. Mean s.d. for  $f_A$  at  $t = 100$  years is in blue text. The three panels are to the same scale. (d), Regression slope of linear fit of time-dependent fraction of uptake into WO,  $f_O$ , vs into TB,  $f_T$ ; pink shading denotes  $\pm 1$  s.d.; value at 100 yr in red text; thick blue, mean of regression slope of linear fit of  $f_O$  vs  $f_T$  evaluated for 120 instances of randomly sorted pairs of net transfer coefficients ( $k_O, k_{T,i}$ ) taken from the set of net transfer coefficients evaluated from the data presented by M20; blue shading denotes  $\pm 1$  s.d.; value at  $t = 100$  yr in blue text; thin curves denote time series of regression slopes for three instances of such random pairings. (e). Pearson correlation coefficient  $r$  of linear regression of  $f_O$  vs  $f_T$  for the several models, thick red; mean and  $\pm 1$  s.d. of  $r$ , for 120 instances of  $k_O$  and  $k_T$ , thick blue, as in (d); values at  $t = 100$  yr as in (d); thin curves denote correlation coefficients for three instances of those regressions.

For all the models excess atmospheric CO<sub>2</sub> began to decrease immediately upon cessation as excess atmospheric CO<sub>2</sub> was being drawn into the WO and the TB. All models showed more or less monotonic decrease of atmospheric CO<sub>2</sub> throughout the initial 100 years subsequent to cessation; a few instances of temporary positive slope are indicative of slight, short-term net increase in atmospheric CO<sub>2</sub>. The fractional removal of excess atmospheric CO<sub>2</sub> at time subsequent to cessation  $t = 100$  yr ranged across the models from 26 % to 47 % (i.e., fraction of excess CO<sub>2</sub> remaining 53 % to 74 %). All but one of the models showed the net amount of CO<sub>2</sub> taken up by the WO increasing monotonically throughout the initial 100 years. All models also showed net uptake by the TB in the initial years subsequent to cessation, but with larger inter-model variation than for net uptake by the WO. In contrast to ocean uptake, the increase in TB amount exhibited substantial fluctuations for almost all the models. For all the models, toward the end of the 100 year period, the amount of uptake by the TB either leveled off, or decreased, or, in some models actually became negative (cumulative transfer from the TB back into the atmosphere over the initial 100 years exceeding cumulative transfer from the atmosphere into the TB). The spread of the extent of transfer into the two individual compartments (0.090, 0.093 at  $t = 100$  yr, 1 s.d.) was much greater than the spread in  $f_A$  (0.054). The fraction of the excess atmospheric CO<sub>2</sub> at the time of cessation taken up by the ocean at 100 years  $f_O(100 \text{ yr})$  ranged across the models from 13 % to 47 %. The fractional uptake by the TB  $f_T(100 \text{ yr})$  ranged from as great as about 25 % in three models to negative values in two models (i.e., stock in the TB actually decreasing over the time period, by 1 % or 4 % relative to the initial excess atmospheric CO<sub>2</sub>).

As in the results from the J13 intercomparison, there is indication of substantial anticorrelation across the suite of ZECMIP models between the extent of uptake into the WO and the TB. This is manifested in the first instance in the much narrower inter-model spread of the extent of decrease in the fraction of initial excess CO<sub>2</sub> remaining in the atmosphere than in the fractional uptake, again relative to the amount of excess atmospheric CO<sub>2</sub> at the time of cessation of anthropogenic emissions, by the ocean  $f_O$  and the terrestrial biosphere  $f_T$ . This anticorrelation is manifested also in the Pearson correlation coefficient,  $r$ , which is negative throughout almost the entire 100-year time period examined. The regression slope, initially rather small, increases (in magnitude) throughout the time period, almost to -0.8; a slope of -1 would indicate a one-to-one compensation between net uptake into the two compartments. This anticorrelation is manifested also in graphs of the net fractional uptake into the ocean versus that into the terrestrial biosphere, shown in Fig. 5(a), at the end of the time period examined by M20,  $t = 100$  yr after cessation of anthropogenic emissions.

40 Again, as with the results from J13, the question arises of the contribution to the anticorrelation across the models in extent of  
uptake of excess atmospheric CO<sub>2</sub> by the WO and the TB to competition between excess CO<sub>2</sub> taken up previously by one  
compartment reducing the amount available to be taken up by the other compartment. The contribution of this competition effect  
to the anticorrelation was first assessed by examining the net transfer coefficients, evaluated as the time-dependent rate of net  
45 increase in the fractional uptake into each of the two compartments divided by the time-dependent fraction of excess atmospheric  
CO<sub>2</sub>,  $k_O$  and  $k_T$ , Fig. 6. As the transfer rates and stocks were available from the supplementary materials and project website, it  
was not necessary to numerically differentiate the time dependent stocks, as was done in the analysis of J13. In several models  
the transfer coefficients were highly variable over time, with especially large fluctuations in the net transfer coefficients into the  
TB, panel (b), and in the fractional rate of decrease of excess atmospheric CO<sub>2</sub>, panel (c), which is nominally the sum of the net  
50 transfer coefficients into the WO and the TB. Despite these large fluctuations, it was found that the regression slope and  $r$  value,  
evaluated for each year over the 100-year period following cessation, were both consistently negative, for almost every year in  
this time period. Importantly also, the correlation slope between  $k_O$  and  $k_T$  was negative throughout almost the entire time  
period. An example plot of  $k_O$  vs  $k_T$  is shown in Fig. 5(b), for time  $t = 55$  years subsequent to cessation, a time period during  
which fairly consistent negative correlation was exhibited, Figs. 6(d) and 6(e). While a single plot with correlation  
65 coefficient -0.58 might not by itself be convincing, the consistent negative correlation between  $k_O$  and  $k_T$  would seem to make a  
fairly convincing case for negative correlation between these net transfer coefficients. Again, as was concluded for the models  
participating in the J13 intercomparison, such an anticorrelation would imply that models for which the terrestrial module  
resulted in relatively high uptake rate into the TB had ocean module that resulted in relatively low uptake rate into the WO,  
and vice versa. This anticorrelation between the transfer coefficients  $k_O$  and  $k_T$  resulted in substantial enhancement, by a factor of 3  
or so, of anticorrelation of the net uptake extent into the two compartments beyond that which would result only from the  
compensation effect as evaluated for random pairings of  $k_O$  and  $k_T$ , Figs. 4(d) and 4(e).



65 Figure 5. (a). Net uptake of CO<sub>2</sub> in the world ocean IRF<sub>O</sub> versus that in the terrestrial biosphere IRF<sub>T</sub>, both expressed as  
fraction of excess atmospheric CO<sub>2</sub> (i.e., above preindustrial) at the time of cessation of emissions, at time  $t = 100$  years  
subsequent to cessation of anthropogenic emissions, as represented by the models that participated in the ZECMIP

intercomparison study of MacDougall et al. (2020, M20); negative values for  $IRF_T$  denote net cumulative decrease in carbon stock in the TB over the 100-year time period. Blue line denotes linear regression; also shown are the regression slope, the Pearson correlation coefficient  $r$ , and  $r^2$ . For identification of models see M20. (b). As in (a), but for transfer coefficient for net uptake of excess atmospheric  $CO_2$  from the atmosphere to the WO  $k_O$  versus that from the atmosphere to the TB  $k_T$  at time  $t = 55$  yr; negative values of  $k_T$  denote net transfer from the TB to the atmosphere at that time .

As with the analysis of J13, the cause of the anticorrelation extent of uptake into the WO and the TB was further assessed by calculations in which the transfer coefficients  $k_T$  of the several models were randomly paired with the  $k_O$ 's with examination of the resultant correlations between uptake by the WO and the TB and the corresponding transfer coefficients, 120 such random pairings. Again these random pairings exhibited essentially no correlation in the transfer coefficients themselves. The mean correlation slope  $b$  at 55 years after cessation was  $-0.01 \pm 0.11$  (1 s.d.), (Fig. 6(d)), well less than the regression slope for the  $(k_O, k_T)$  pairs for the models,  $-0.22 \pm 0.14$ . A similar situation was found for the correlation coefficient, Fig. 6(e),  $r(55 \text{ yr}) = 0.03 \pm 0.30$  vs  $-0.58$  for the  $(k_O, k_T)$  pairs for the models. Again there was meandering of the correlation coefficient of individual instances of pairing, three of which are shown in the figure. Some of the individual curves meandered considerably outside  $\pm 1$  s.d., which is of course to be expected, but none exhibited the systematic strong anticorrelation exhibited by IRFs of the models, as shown by the thick red curve.

The anticorrelation of the transfer coefficients was found to exert quite a substantial influence on the anticorrelation of the extent of transfer, Fig. 4. Here, in panels (a)-(c), the curves for the original models and the associated spread, the pink shaded region representing  $\pm 2$  s.d. of the fraction of the excess atmospheric  $CO_2$  at the time of cessation of anthropogenic emissions that is transferred into the WO or the TB, and the fraction remaining in the atmosphere are superimposed on the averages taken over 120 random pairings of  $k_O$  and  $k_T$ , thick blue line (and averages of 2 s.d., blue shading). For transfer extents  $f_O$  and  $f_T$  the range of the blue shading (randomized pairs  $(k_O, k_{T,i})$ ) is essentially the same as that of the pink shading (models). However for the fractional extent of removal from the atmosphere  $f_A$ , while the curve representing the mean of the 120 instances of random  $k_O, k_T$  pairs (dark blue; no vertical adjustment, because time series started at  $t = 0$ ) is virtually identical to the mean of the models themselves (black with open circles), the spread of  $f_A$  for the randomly paired  $k_O$  and  $k_T$  (blue shading) substantially exceeds that for the models themselves, by nearly a factor of 2 by the end of the model runs. The difference between the blue shaded area (spread of the randomized pairs  $(k_O, k_{T,i})$ ) and the pink shaded area (spread of the models themselves) is a measure of the decrease in  $f_A$  that is due to anticorrelation of the transfer coefficients in the models. The effect of anticorrelation in the transfer coefficients is seen also in the regression slope  $b$  of  $f_O$  vs.  $f_T$ ,  $-0.77 \pm 0.15$  for the models themselves vs.  $-0.21 \pm 0.21$  for the randomized pairs  $(k_O, k_{T,i})$  and in the correlation coefficient  $r$ ,  $-0.80$  for the models vs.  $-0.24$  for the randomized pairs (all at 100 years after cessation of anthropogenic emissions). Again, values of  $b$  and  $r$  for individual random  $(k_O, k_T)$  pairs meander more or less within the space of  $\pm 1$  s.d., but this meandering is well less than the separation between the mean quantities for the randomized pairs and the values for the models.



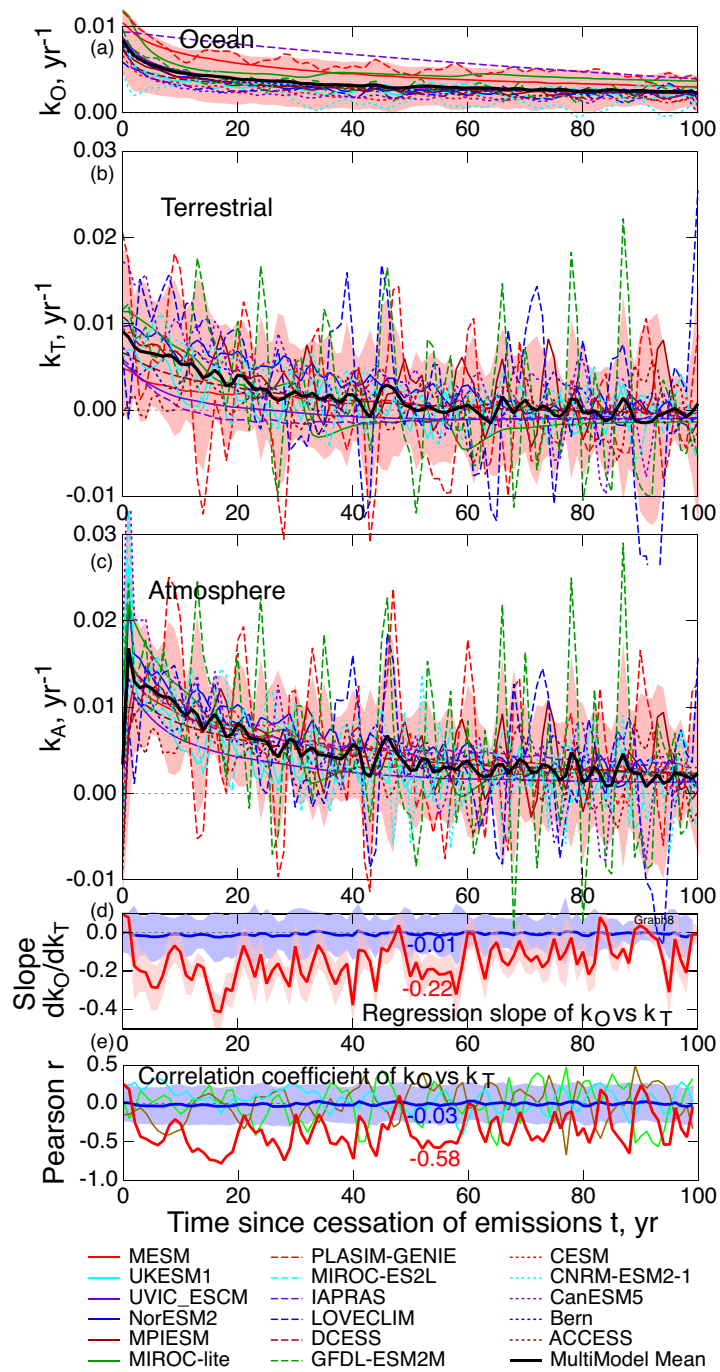


Figure 6. Net transfer coefficients from the atmosphere into (a) the world ocean  $k_O$  and (b) the terrestrial biosphere  $k_T$  as a function of time subsequent to cessation of emission of anthropogenic  $\text{CO}_2$  into the atmosphere, evaluated from the results presented by MacDougall et al. (2020; M20); similarly, (c), the fractional rate of decrease of excess  $\text{CO}_2$  stock in the atmosphere. Pink shading denotes  $\pm 2$  s.d. about the multimodel

405 mean; the three panels are to the same scale. For identification of the participating models see M20. (d),  
Regression slope, thick red, of linear fit of  $k_O$  vs  $k_T$  for the several models for each year over the 100-year period  
subsequent to cessation of emissions (see Fig. 5(b) for example), with value at 55 yr indicated; shading denotes  $\pm$   
1 s.d.; mean regression slope, thick blue, and  $\pm$  1 s.d., blue shading, for 120 instances of  $k_O$  and  $k_T$  of different  
410 models being randomly paired, with mean value at 55 yr indicated; thin curves denote time series of three  
instances of those regression coefficients. (e), Pearson correlation coefficient  $r$  of linear regression of  $k_O$  vs  $k_T$   
for the several models, thick red, with value at 55 yr indicated; blue and blue shading, mean and  $\pm$  1 s.d. of  $r$ , for  
the 120 instances of random pairing, with mean value at 55 yr indicated; thin curves denote time series of three  
instances of those correlation coefficients.

### 3 Discussion

415 The intent of this study has been to determine, for the two model intercomparison studies under examination, J13 and M20, the  
extent and causes of anticorrelation across the models participating in each study in the net uptake of excess  $\text{CO}_2$  by the WO and  
the TB under the experimental protocols of the two studies. The present analysis has demonstrated and quantified anticorrelation  
across the models that participated in each of the two intercomparison studies between the transfer coefficients characterizing the  
net rate of transport of excess atmospheric  $\text{CO}_2$  into the two receiving compartments, the WO and the TB, subsequent to the  
420 pulse emission (J13) or to cessation of anthropogenic emissions (M20). This study has also, for each of the two studies  
examined, quantified the enhancement in anticorrelation in the extent of uptake in the two receiving compartments beyond that  
which would be expected inevitably from the competition effect alone and the resultant decrease in inter-model diversity.

This study assessed not just anticorrelation across each of the model sets in the net uptake extent but also in the net transfer  
coefficients, the latter defined as the time-dependent rate of transfer into the WO and TB divided by the time-dependent amount  
425 of atmospheric  $\text{CO}_2$ , for J13, in excess of the amount atmospheric  $\text{CO}_2$ , subsequent to the pulse, that would have been present in  
the absence of the pulse, and for M20, in excess of preindustrial  $\text{CO}_2$  subsequent to cessation of anthropogenic emissions. As  
these net transfer coefficients are not dependent on prior uptake, they are not subject to what is denoted here as the competition  
effect, such that if more  $\text{CO}_2$  has previously been taken up by one sink compartment there is inevitably less available to be taken  
up by the other. In both studies significant anticorrelation was found between the transfer coefficients across the sets of  
430 participating models and that, as a consequence, diminished inter-model variance in the time-dependent extent of drawdown of  
excess atmospheric  $\text{CO}_2$  relative to that which would be expected in the absence of anticorrelation in the transfer coefficients.

The transfer coefficients  $k_O$  and  $k_T$ , being based on the net transfer rates, and the extents of transfer, being the integrals of the  
transfer rates, are net quantities, the difference between fluxes in the opposing directions. (As  $k_A$  is not a transfer coefficient *per*  
*se*, but represents the total net flux, from the atmosphere to the WO and the TB, again normalized to excess atmospheric  $\text{CO}_2$ ,  
435 fluctuations in  $k_A$  simply represent the sum of fluctuations in  $k_O$  and  $k_T$ , which must be considered more fundamental than  
those in  $k_A$ .) In both studies examined here fluctuations in  $k_T$  greatly exceeded those in  $k_O$  (and thus dominated fluctuation in  
 $k_A$ ). It would seem almost certain that the large interannual fluctuations in  $k_T$  in several of the models arise from externally  
imposed influences in processes controlling this net uptake such as temperature, cloudiness, precipitation, and fire, which  
seemingly are built into the models, or into the parent climate models, to represent variability in these processes and to examine

440 the consequences of this variability, as opposed to processes that would actually occur in a given hypothetical future year subsequent to the pulse emission or cessation of emissions. From an observational perspective, some sense of the temporal variability of the global rate of net drawdown of atmospheric CO<sub>2</sub> is gained from the historical time series of fractional annual removal rate of excess CO<sub>2</sub>, corresponding to  $k_A$ , which has ranged, over the time period 1959-2012 from as great as 4.3 % yr<sup>-1</sup> to as low as 0.8 % yr<sup>-1</sup>, but never negative (Raupach et al., 2014). It would thus seem that some of the models may be  
445 overestimating the effects of climate variables on the rate of drawdown of excess CO<sub>2</sub> in future climate, perhaps substantially so. In any event, given the large intra-model and inter-model fluctuations in  $k_T$ , it came as rather a surprise in this analysis to be able to demonstrate and quantify consistently negative inter-model anticorrelation between  $k_O$  and  $k_T$  across the models that participated in each of the studies.

The finding of inter-model anticorrelation between  $k_O$  and  $k_T$  led to determination of effect of this anticorrelation on  
450 enhancement of anticorrelation in the time-dependent extent of transfer of excess CO<sub>2</sub> into the two receiving compartments. Here the term "enhancement" is introduced to account for anticorrelation greater than that which would inevitably arise from the competition effect. A method was introduced to estimate the competition effect by randomizing the time-dependent pairs of net transfer coefficients. From comparison of the results from the model intercomparisons with those for the randomized ( $k_O$ ,  $k_T$ ) pairs it was shown by the several measures of anticorrelation examined here that in the each of the two studies the anticorrelation  
455 between the amount of excess atmospheric taken up by the WO and the TB, well exceeds that due to the competition effect, leading to substantial underestimation of the inter-model diversity that had previously been inferred from these studies.

Inter-model diversity of a quantity of interest may confidently be taken as a measure of the minimum uncertainty that would attach to knowledge of that quantity, at least as represented by the set of models examined. Not uncommonly, however, inter-model diversity is *equated* with uncertainty, e.g., in the present context, by Joos et al., (2013) and by the IPCC Fifth Assessment  
460 Report (Myhre et al., 2013). The finding here of substantial underestimation of inter-model diversity in the time-dependent extent of drawdown of excess atmospheric CO<sub>2</sub> implies a greater uncertainty in key measures of drawdown than has previously been recognized and ascribed to this quantity.

From a cumulative forcing perspective, the pertinent quantity is not the atmospheric IRF, but its integral over the time horizon of interest. This integrated IRF, shown for the pulse emission study of J13 in their Figure 1(b) is equal to 52.4 years for the J13  
465 multimodel mean, with standard deviation 5.5 years (10 %). The difference between the violet and blue regions of Fig. 1(c) is the reduction in inter-model diversity (expressed as  $\pm 2$  s.d.) due to anticorrelation of the transfer coefficients across the models. From integration of the upper and lower bounds of the blue shaded region in Fig. 1(c), which give the  $\pm 2$ -s.d. range of the spread in IRF that would result only from the competition effect, that is in the absence of anticorrelation of the transfer coefficients across the models, the standard deviation of the integrated IRF increases to 8.1 years (15 %), an increase of about 50 %. This  
470 increase in inter-model diversity would attach also to the absolute global warming potential (AGWP) of CO<sub>2</sub>, defined as the cumulative atmospheric IRF of CO<sub>2</sub> times its forcing efficiency, a quantity widely used in assessments, such as the IPCC Fifth Assessment Report (Myhre et al., 2013, p. 712), of the cumulative effects of prospective changes in emissions of CO<sub>2</sub>.

The AGWP of CO<sub>2</sub> is also widely used to compare the integrated radiative forcings of non-CO<sub>2</sub> greenhouse gases (ncghgs) to that of CO<sub>2</sub> via the global warming potential, GWP, the ratio of AGWP of ncghgs to that of CO<sub>2</sub>. In the IPCC Fifth Assessment  
475 Report Myhre et al. (2013) state that the GWP has become the "default metric" for transferring emissions of different gases to a

common scale, CO<sub>2</sub>-equivalent emissions, observing also that the GWP for a time horizon of 100 years has been adopted as a metric to implement a multi-gas approach to achieve specific targets. The increase in inter-model spread of the cumulative atmospheric IRF resulting from the present analysis attaches also to the GWPs and to equivalent emissions of n<sub>o</sub>ghgs, affecting the confidence that can be placed in strategies to achieve specific targets and the confidence that can be placed in replacing emissions of one ghg with another in achieving target ghg emissions. For all these reasons it seems essential that the minimum uncertainty in rate of drawdown of excess CO<sub>2</sub>, as represented by inter-model diversity, be accurately known and stated. If the inter-model diversity in integrated IRF obtained here is an accurate characterization of the uncertainty in that quantity, then the uncertainties in the AGWP of CO<sub>2</sub> and in the GWPs of n<sub>o</sub>ghgs would increase by like amount.

A question that naturally arises is the reason for the anticorrelation in drawdown rates across the sets of models participating in the two studies. A similar situation of anticorrelation across nominally independent models was found to exist between modeled climate sensitivity, forcing, and temperature change over the industrial era, as reported in a suite of climate model studies. This situation was initially identified (Schwartz et al., 2007) from the inter-model diversity in temperature change in climate model studies being much less than the uncertainty in forcing. Shortly afterwards Kiehl (2007) showed that this was due to inverse correlation across the set of models between forcing and climate sensitivity. Reflecting on such anticorrelation across nominally independent models, Sherwood et al. (2020) underscore the need to identify model co-dependencies that might have the effect of diminishing uncertainty in estimates of climate sensitivity. They observe that “Modelers and process experts are aware of the historical climate record. GCM aerosol forcings might have been selected in order to match the observed warming rate over the twentieth century (e.g., Kiehl, 2007).” Sherwood et al. go on to suggest that “otherwise plausible models or feedbacks might have been discarded because of perceived conflict with this warming rate, or aversion to a model's climate sensitivity being outside an accepted range.”

It would seem that considerations such as these might apply similarly to the anticorrelation in the modeled rate of drawdown of excess CO<sub>2</sub> subsequent to pulse emission (J13) or following abrupt cessation of anthropogenic emissions (M20). A *sine qua non* in modeling atmospheric CO<sub>2</sub> over the industrial period is that the model accurately represent the observed increase in atmospheric CO<sub>2</sub> over this period. This requirement, together with historical emissions, fixes the total time-dependent rate of net drawdown of excess atmospheric CO<sub>2</sub>, which is the sum of the net drawdown rates into the ocean and the TB. Thus to meet this observational constraint, if the net transfer rate from the atmosphere into one compartment is high, the net transfer rate into the other must be low. This requirement, built into CO<sub>2</sub> models because of the requirement that they accurately represent atmospheric CO<sub>2</sub> in historical runs, might plausibly lead to the anticorrelation of net uptake rates into the two compartments that is revealed in the present analysis of model responses to artificial emissions scenarios in the two studies under examination. I thank Andrew MacDougall in his capacity as reviewer of this paper (MacDougall, 2024) for stimulating my thoughts along these lines.

At the end of the day this study has done little to identify the underlying causes of the observed anticorrelations. Identifying these causes would, it would seem, require a much more thorough examination of the representations of the processes governing net uptake of excess atmospheric CO<sub>2</sub> into the two receiving compartments than can be achieved simply by intercomparisons of rate and extent of drawdown such as in the two studies examined here. Nonetheless it would seem that if progress is to be made in representing these processes and in enhancing confidence in these representations, such thorough inter-model comparison at the process level is required.

For the present, at minimum, it would seem incumbent upon the communities using the results of these intercomparison studies to assess the consequences of prospective changes in emissions or to compare integrated forcings of CO<sub>2</sub> and other greenhouse gases to take cognizance of the implications of anticorrelations across the models participating in the two intercomparison studies examined here and resultant artificial decrease in inter-model diversity in these two studies.

### Competing Interests

The author declares no competing interest.

### Acknowledgments

I thank Andrew MacDougall for providing the M20 data, for discussion, and for valuable suggestions in his capacity as Reviewer of this manuscript. I also thank L. Kleinman and E. Lewis and one anonymous reviewer for valuable suggestions. Much of this work was conducted while the author was at Brookhaven National Laboratory, with support in part from US Department of Energy (Contract No. DE-SC0012704); views expressed here are those of the author and do not necessarily reflect the views of BNL or DOE. This article and corresponding preprints are distributed under the Creative Commons Attribution 4.0 License.

### Data

Data from the ZECMIP project (MacDougall et al., 2020) are available from <http://terra.seos.uvic.ca/ZEC/>. Data from the Joos et. al. (2013) intercomparison were obtained by digitization of the figures in the published paper. Data displayed in the several figures are presented in SI.

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