

Volcano tsunamis and their effects on moored vessels safety: The 2022 Tonga event

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Abstract. The explosion of the Hunga Tonga-Hunga Ha’apai volcano on January 15, 2022 (Tonga22) was the origin of a volcano-meteorological tsunami (VMT) recorded worldwide. At a distance exceeding 10,000 kilometres from the volcano and 15 hours after its eruption, the moorings of a ship in the Port of La Pampilla, Callao (Peru), failed, releasing over 11,000 barrels of crude oil.

This study delves into the profound implications of the Tonga 22 event, investigating whether it could have led to the break of the mooring system. We conducted a comprehensive analysis of this significant event, examining the frequency content of the time series recorded at tide gauges, DART buoys, and barometers in the Southern Pacific Ocean. Our findings revealed that the maximum energy of the spectra corresponds to 120 minutes of wave period off the coast of Peru, with the arrival time of these waves coinciding with the time of the accident in the Port.

We used a Boussinesq model to simulate the propagation of the Volcano-Meteorological tsunami from the source to the Port in Peru to study the impact of those waves on the mooring system. We used the synthetic tsunami recorded in the Port as input for the model that simulates mooring line loads based on the ship's degrees of freedom. The results suggest that the 120-minute wave triggered by the VMT could significantly increase mooring stresses due to the resulting hydrodynamic effects, exceeding the Minimum Break Load (MBL).

We conclude that the propagation of the long wave period generated by the VMT caused overstresses in moored lines that triggered accidents in port environments. This event showed the need to prepare Tsunami Early Warning Systems and port authorities for detecting and managing VMTs induced by atmospheric acoustic waves. The work provides new insights into the far-reaching impacts of the Tonga 2022 tsunami.

31 **1. Introduction**

32 Volcanic activity can trigger tsunamis through underwater explosion, caldera collapse, pyroclastic flow,
33 flank collapse, or atmospheric gravity waves produced by large explosions (Paris, 2015). Throughout
34 history, tsunamis of volcanic origin have been poorly studied due to their scarcity, leading to a limited
35 understanding of their generation mechanisms and impacts at local, regional, and global scales (Hayward
36 et al., 2022). To better understand this type of tsunami geneses and, therefore, reduce the epistemic
37 uncertainties associated with it, several studies have been carried out (Antonopoulos, 1992; Pararas-
38 Carayannis, 1992, 2004), which also include aquatic environments other than oceans, such as great lakes
39 in Russia and the Philippines (Belousov et al., 2000; Falvard et al., 2018). In these studies, the 1883 eruption
40 of the Krakatau volcano in the Sunda Strait (Indonesia), is commonly accepted as a main reference and a
41 unique example (Kienle et al., 1987), as it was the first event of its kind recorded by different instruments
42 worldwide (Paris et al., 2014; Yokoyama, 1981).

43 The Hunga Tonga-Hunga Ha'apai volcano (HTHH) is a submarine volcano near an island with the same
44 name, and located 65 km NNW of the island of Tongatapu capital of Tonga, Nuku'alofa (20.55°S,
45 175.39°W, see location in Figure 1). It is one of several active volcanoes in the Kingdom of Tonga, an
46 archipelago nation in the South Pacific. The latest eruptive phase of the HTHH volcano began in mid-
47 December 2021 with vigorous shallow-water explosive activity (Vergoz et al., 2022). On January 15, 2022,
48 the volcano erupted at 4:00 a.m. UTC (Tonga Volcanic Eruption & Tsunami, 2022). The HTHH trigger a
49 volcano-meteorological tsunami (VMT) due to a violent volcanic explosion that generated atmospheric
50 gravity waves that propagated several times across the globe (Omira et al., 2022; Wright et al., 2022). These
51 waves resulted from particle agitation in the atmosphere, travelling both vertically and horizontally at sonic
52 and supersonic speeds (Kubota et al., 2022; Matoza et al., 2022; Wright et al., 2022; Dogan et al., 2023).
53 Following the volcano explosion, there were reports of flooding more than 1 m, causing damage to ports
54 and infrastructure in both near and far field (Ramírez-Herrera et al., 2022; Imamura et al., 2022). The
55 affected locations include Australia, New Zealand, the United States, Mexico, and Peru, resulting in
56 economic losses of approximately \$102 million due to damages to floating docks, vessels, and infrastructure
57 (Terry et al., 2022; World Bank, 2024).

58 The Tonga VMT was exceptional as it travelled at faster speeds than common tsunamis, had a global reach,
59 affected the far-field coasts, and caused noticeable damages, human fatalities, and coastal hydrodynamic
60 effects (Terry et al., 2022; Omira et al., 2022; Lynett et al., 2022). For instance in Kochi prefecture 5 boats
61 were sunk and capsized in the port of Sakihama in the city of Muroto ([https://oceancrew.org/news/more-
62 than-30-boats-sank-due-to-the-tsunami-in-japan-17-01-2022/](https://oceancrew.org/news/more-than-30-boats-sank-due-to-the-tsunami-in-japan-17-01-2022/)), two people died in Peru (INDECI, 2024)
63 and strong currents in ports of Mexico were reported as a direct effects of the tsunami (Ramírez-Herrera et
64 al., 2022). In their study, Omira et al. (2022) demonstrated that the primary source of the globally observed
65 Tonga tsunami was the acoustic gravity waves radiated from the volcanic explosion. Here, the sizeable
66 tsunami at some distant coasts (i.e., South America and Japan) was associated with the amplified ocean
67 waves under Proudman resonance (Proudman, 1929) when the atmospheric wave propagated over very
68 deep water (i.e., oceanic trenches). Other triggering mechanisms, including the submarine volcanic

69 explosion, likely contributed to the generation of the locally observed tsunami in the far-field (Lynett et al.,
70 2022; Omira et al., 2022).

71 The consequences of harbour-intruding long waves on moored vessels have been investigated by numerous
72 studies (Ayca and Lynett, 2016, 2018, 2021; Kirby et al., 2022; Wilson et al., 2017). Seismic tsunamis often
73 cause damage to port environments, such as broken moorings, collisions, or subsidence due to the large
74 amount of momentum flux travelling within the harbour (Lynett et al., 2022; Ohgaki et al., 2008; Inoue et
75 al., 2001). This also applies to tsunamis induced by atmospheric disturbances, **similarly, may** have caused
76 damage to ships, moored vessels, and small bays (Imamura et al., 2022; Thomson et al., 2009). It has been
77 observed in these studies that strong currents, often accompanying long-period waves, increase the
78 probability of generating large catastrophes in harbours (Shigeki and Masayoshi, 2009; Sakakibara et al.,
79 2010; Zheng et al., 2022; Lynett et al., 2012). **For instance Shigeki and Masayoshi (2009), studied**
80 **numerically the mooring loads due to large-scaled tsunamis in GNL-carriers vessels and found out that the**
81 **drag forces due to the currents induce large sway and surge motions are strongly important.** Likewise, based
82 on DOFs (Degrees Of Freedom), some authors such as López and Iglesias (2014) agree with the hypothesis
83 that the motions in the vessel's horizontal plane (named **sway, surge** and yaw) are strongly correlated with
84 the total tsunami wave energy, with the currents being quite significant in ship sway response (Inoue et al.,
85 2001). Furthermore, Ohgaki et al. (2008) and Zheng et al. (2022) mention that tsunamis are usually closer
86 to the natural period of a mooring system (>80 sec), which makes these waves more prone to **cause** damage.
87 Given the non-linearity of the **hydromechanical and** physical **processes that involve stress studies in**
88 **mooring systems, in which each ship has its own characteristics (geometric, inertial, among others),** it is
89 pertinent to perform specific studies focused on each situation, configuration, and need (Zheng et al., 2022).

90 In La Pampilla Port in Peru, 10,000 km away from the Tonga volcano, the Italian-flagged oil tanker Mare
91 Doricum reported the breakage of their mooring lines, 15 hours after the explosion of the HTHH volcano.
92 The ship captain associated the breaking of the vessel's moorings with the abnormal waves in the sea, for
93 which no warning was issued (SPDA Actualidad Ambiental, 2024). The Peruvian National Tsunami
94 Warning System (CNAT) stated that the Tonga tsunami did not generate a tsunami on the Peruvian coast
95 (CNAT, 2022). However, the tide gauge located in Callao Bay recorded a sudden change in sea level
96 coincident with the time of the accident (**UNESCO/IOC, 2021**). This article addresses the impact of the
97 Tonga 2022 tsunami on vessels moored on the Peruvian coast. It uses both sea-level data analysis and
98 numerical modelling to improve the understanding of the damage caused by far-field Tonga VMT, studying
99 its influence on the safety of moored vessels.

100 **2. Data and Methods**

101 Considering the complexity of the Tonga tsunami event, which likely involved multiple triggering volcanic
102 mechanisms, analysing waves measured by both oceanic and atmospheric instruments is highly important
103 (Wright et al., 2022). Firstly, we used the wavelet analysis to examine the composition of the signals
104 recorded by both tidal gauges and DART buoys **within the Pacific Ocean**. Secondly, we studied the
105 hydrodynamic effects of the Tonga tsunami in the far field, using tsunami numerical simulations

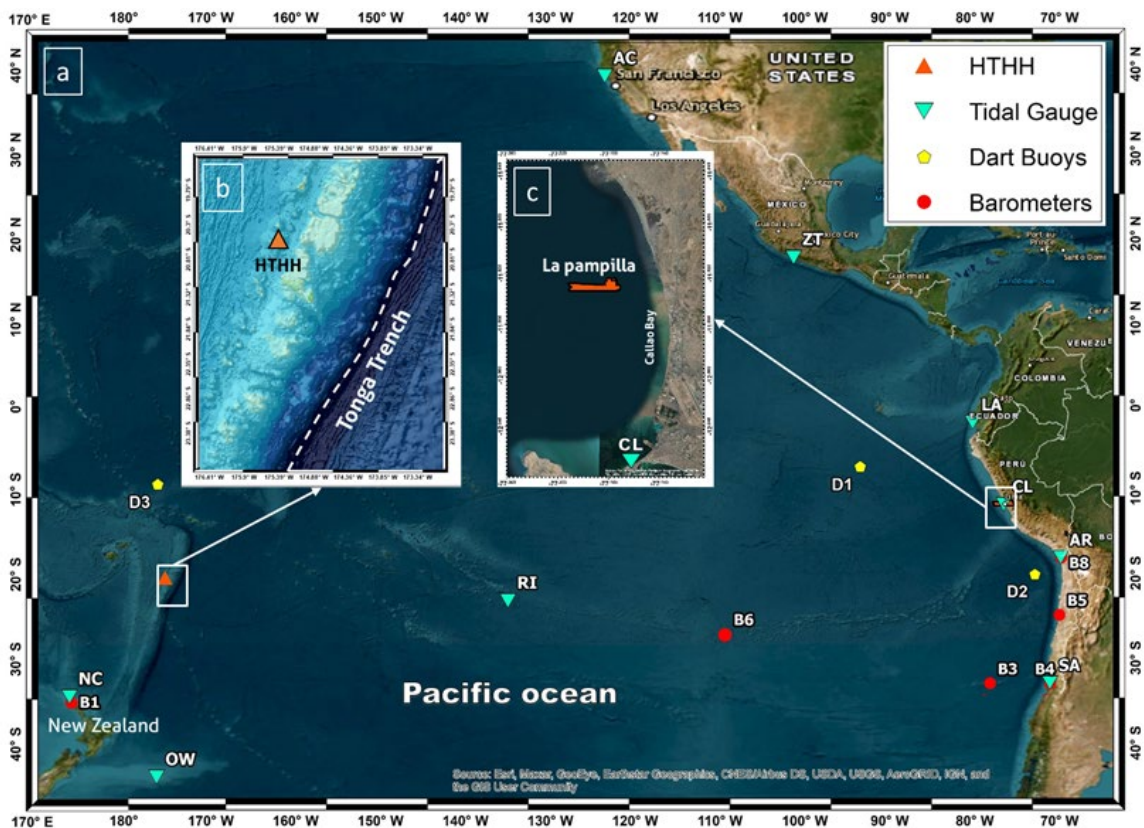
106 (Boussinesq-type model) over high-resolution bathymetric models. Thirdly, we developed a model to assess
 107 the loads on vessel's mooring lines based on the rigid body analytical equations with six degrees of freedom
 108 (DOFs), this model uses as input the ocean dynamics (ocean elevation and velocities) caused by the VTM.

109 **2.1. Air pressure and sea level data**

110 The data used in this study includes records from DART buoys, tide gauges, and weather stations in the
 111 Pacific Ocean. Figure 1 shows the location of the instruments considered in this study, with red circles
 112 representing the atmospheric pressure sensors, light blue triangles for the tide gauges, and yellow dots for
 113 the DART buoys.

114 The deep-water sea level time series (**D1**, **D2**, and **D3**) were obtained from the DART buoys, which in turn
 115 managed by the Center for Operational Oceanographic Products and Services of the National Oceanic and
 116 Atmospheric Administration (NOAA, <https://www.ndbc.noaa.gov/>). Coastal sea level data used in this
 117 study come from tidal stations connected in real-time to the Sea Level Station Monitoring Facility of
 118 UNESCO's Intergovernmental Oceanographic Commission (IOC, [http://www.ioc-](http://www.ioc-sealevelmonitoring.org/)
 119 [sealevelmonitoring.org/](http://www.ioc-sealevelmonitoring.org/)). The **B1** air pressure data have been obtained from local agents in New Zealand
 120 (NIWA, <https://niwa.co.nz/>) and those from stations **B3**, **B4**, **B5**, and **B8** came from the Dirección General
 121 De Aeronáutica Civil de Chile (DGAC, <https://climatologia.meteochile.gob.cl/>) through the Chilean
 122 Meteorological Office.

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124

125 **Figure 1. a, locations of the measuring instruments. Red circles show the atmospheric pressure sensors, the light**
 126 **blue triangles show the tide gauges, and the yellow circles refer to the Dart Buoys. b, shows the HTHH volcano**

127 (orange triangle) and Tonga trench location. c, is the Callao bay zoom, the orange vessel represents the location
 128 of terminal 2 of the port of La Pampilla, Peru.

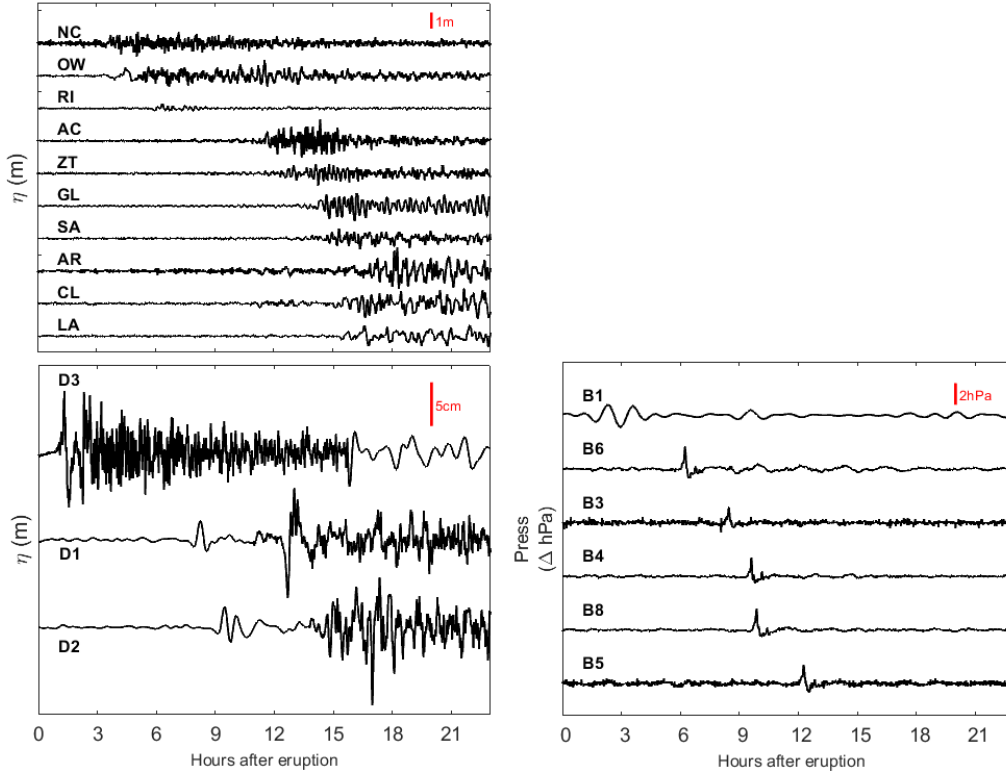
129 The sea level time series were de-tided using bandpass filters of 1.5 min-2.5 hours and 2 min - 3 hours for
 130 DART and tide gauge data, respectively, following Lynett et al. (2022). For atmospheric pressure data, a
 131 bandpass filter of 1.5 min - 2.5 hours was used (Table 1). Figure 2 shows the filtered time-series. The arrival
 132 time was less than 3 hours for the B1 sensor in the near field (shape differences are caused by the sample
 133 time), and between eight and twelve hours in the far field, about 10.000 km away. The air-pressure time-
 134 series shows a notable peak of approximately 2 hPa with the "N-wave" pulse shape associated with the
 135 leading Lamb wave (Lynett et al., 2022; Omira et al., 2022). The seawater elevation, in deep waters Dart
 136 sensors, shows tsunami arrival times in two different moments related with the inverse barometer effect
 137 due to the leading lamb wave and the acoustic gravity waves coupled in ocean (VMT) respectively whit
 138 values no more than 10 cm. On the other hand, the tidal gauge shows tsunami waves values higher than 1
 139 meter especially in the far field locations like Chilean and Peruvian coasts.

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Type	ID	Name	Source (country)	Latitude (deg)	Longitude (deg)	Distance from source (km)	Sample (min)
Barometric	B1	Nort Cape B.	New Zealand Gov	-35.134	173.263	1750	10
	B3	330031	Chilelan Gov.	-33.636	-78.833	9110	1
	B4	330030	Chilelan Gov.	-33.656	-71.613	9720	1
	B5	250005	Chilelan Gov.	-25.411	-70.484	10230	1
	B6	270001	Chilelan Gov	-35.134	173.263	6530	1
	B8	180042	Chilelan Gov.	-18.513	-70.266	10600	1
Tide Gauge	NC	North Cape T.G.	IOC (New Zealand)	-34.410	173.050	1715	1
	RI	Rikitea	IOC (France)	-23.118	-134.969	4025	1
	AC	Arena Cove	IOC (USA)	38.913	-123.705	8700	1
	ZT	Zihuatanejo	IOC (Mexico)	17.637	-101.558	9155	1
	GL	Galapagos	IOC (Ecuador)	-0.752	-90.307	9410	1
	SA	San Antonio	IOC (Chile)	-33.582	-71.618	9720	1
	OW	Owenga	IOC (New Zealand)	-44.025	-176.369	2290	1
	AR	Arica	IOC (Chile)	-18.476	-70.323	10595	1
	CL	Callao	IOC (Perú)	-12.069	-77.167	10240	1
	LA	La Libertad	IOC (Ecuador)	13.485	-89.319	10305	1
DART	D1	32413	NDBC (USA)	-7.421	-93.484	8800	15
	D2	32401	NDBC (USA)	-20.474	-73.421	10205	15
	D3	51425	NDBC (USA)	-9.511	-176.258	1530	15

141 **Table 1. Description of measuring instruments.**

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Figure 2. De-tided time series. Air pressure data (right panel), tide gauge, and Dart data (left panel). Vertical red lines used to scale the magnitude of the variations in each instrument.

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2.2. Spectral analysis

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Spectral analysis is a practical tool for identifying the characteristic frequencies and energy levels in a time-series, particularly when it is composed of the superposition of signals with different frequencies. This method has found extensive application in the study of tsunamis (Abe, 2011; Rabinovich, 1997; Shevchenko et al., 2011; Satake et al., 2013; Baptista et al., 2016; Xu et al., 2022). In the time domain, we use wavelets to perform spectral analysis, allowing the estimation of the evolution of the spectral energy and, consequently, the first instants of energy increase for a given specific period. **Wavelet methodology applies a function composed of a complex exponential equation modulated by a Gaussian function for its fitting procedure, which is generally known as a mother function. One of the famous wavelet mother functions is the Morlet function $[\psi(t)]$ which is given by Eq. 1 (Goupillaud et al., 1984):**

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$$\psi(t) = \pi^{-1/4} * e^{-\frac{1}{2}t^2} * \left(1 + e^{-f_0^2} - 2e^{-\frac{3}{4}f_0^2}\right)^{-1/2} * \left(e^{if_0t} - e^{-1/2f_0^2}\right) \quad (1)$$

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Where f_0 is the center frequency of the wavelet function and t is the time. For the present study, it has been discretized in n sub-octaves per octave with $n = 50$ for better scale resolution and a wavenumber (k_0) of 8. Where the spectral energy of the wavelet is defined as $ABS|\psi(t)|^2$. A logarithmic scaling has been performed to obtain an adequate highlighting of spectral energy information as follows:

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$$\psi(t)'' = \begin{cases} \log_{10}(\psi(t) + 1) & \psi(t) \ll 1 \\ \log_{10}(\psi(t)) & \psi(t) > 1 \end{cases} \quad (2)$$

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$$\psi(t)'' = eps * (\psi(\omega)'') \quad (3)$$

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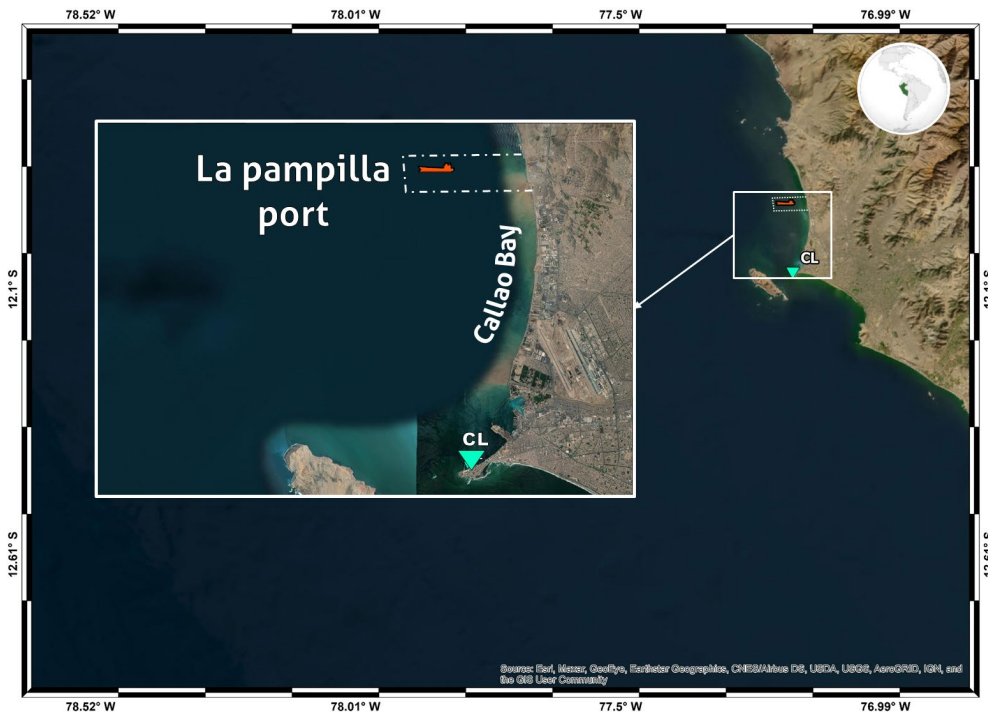
with $\log_2(eps) = -52$.

164 It means that eps returns the distance from 1.0 to the next larger double-precision number, that is 2^{-52} . In
 165 turn, the spectral energy in frequency is presented by performing the temporal integration of the wavelet as
 166 follows:

$$167 \quad G(f_o) = \int_{\omega_0}^{\omega_{end}} \psi(t)'' dt = \int_{-\infty}^{\infty} g(t) * e^{-i2\pi ft} dt \quad (4).$$

168 2.3. Tsunami propagation model

169 Although air-ocean interaction has been recognized as a primary mechanism for the global fast-travelling
 170 Tonga 2022 tsunami (Omira et al., 2022), volcano-ocean interaction provided valid explanations for the
 171 near-field observation (Lynett et al., 2022; Pakoksung et al., 2022). As our primary target is Callao Bay,
 172 located approximately 10,000 km away from the HTHH volcano (Figure 3), we only focused on the tsunami
 173 induced by the atmospheric disturbances that followed the volcano explosion. The hypothesis of a point-
 174 source tsunami reaching the South American coast was ruled out considering the modelling results of a
 175 tsunami generated by the underwater explosion of the HTHH volcano (Omira et al., 2022).
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 178 **Figure 3. Callao Bay and location of the vessel (Orange vessel) in the offshore port of La Pampilla, Peru at**
 179 **coordinates 11°56' S, 77°11' W.**

180 To simulate the VMT triggered by the explosion of the HTHH volcano, we used the finite volume GeoClaw
 181 code equipped with atmospheric pressure forcing terms that are handled using the flux-splitting method in
 182 momentum balance (Mandli and Dawson, 2014). This numerical code was validated in various
 183 meteotsunami studies (Kim and Omira, 2021; Kim et al., 2022; Omira et al., 2022). The determination of
 184 atmospheric source terms is based on barometric records from three distinct-selected observations in **B1**,
 185 **B6**, and **B8** (see Table 1 for details). To generate the atmospheric input for the tsunami propagation
 186 modeling, we adopted an approach where we assumed radial symmetry of atmospheric pressure emanating
 187 from HTHH with a constant speed. Specifically, we set the propagation speed at 310 m/s, and interpolated

188 the atmospheric pressure at each computational grid point using the values from the two closest observed
189 records. The selection of observed records at Kaitaia (New Zealand), 270001 (Chile), 200006 (Chile), and
190 Charlotte (US Virgin Islands) was made strategically to capture a diverse range of atmospheric conditions
191 and geographical locations relevant to our study area. These locations were chosen based on their proximity
192 to the region of interest and the availability of reliable barometric records. We acknowledge the importance
193 of validating our atmospheric input against barometric records. We have documented the details of this
194 validation process in our previous work (Omira et al., 2022), where we discuss the consistency between the
195 modeled atmospheric input and observed barometric data.

196 Our simulations covered an area from 170° E to 295° E longitude and from 40° S to 40° N latitude, as
197 obtained from GEBCO (<https://www.gebco.net/>). To effectively simulate sea level fluctuations induced by
198 atmospheric pressure, we used adaptive mesh refinements (AMR) based on both atmospheric pressure and
199 sea level variations. Six levels of AMR were utilized, beginning with a base resolution of 1° and employing
200 refinement ratios of 5, 6, 4, 4, and 5 at successive levels. We used resolutions as fine as $1''/40$ (~45 meters)
201 in the areas such as Pampilla, Callao, and La Libertad, while employing a coarser resolution of up to $1''/2$
202 (~900 meter) in other regions to balance computational efficiency with accuracy. To account for the bottom
203 friction, GeoClaw software uses Manning's formulation, and the Manning coefficient of 0.02 was
204 considered in this work. Our simulations were conducted using the Madsen's Boussinesq-type equations,
205 with a constant value of $B = 1/15$ (Kim et al., 2017; Madsen and Sørensen, 1992).

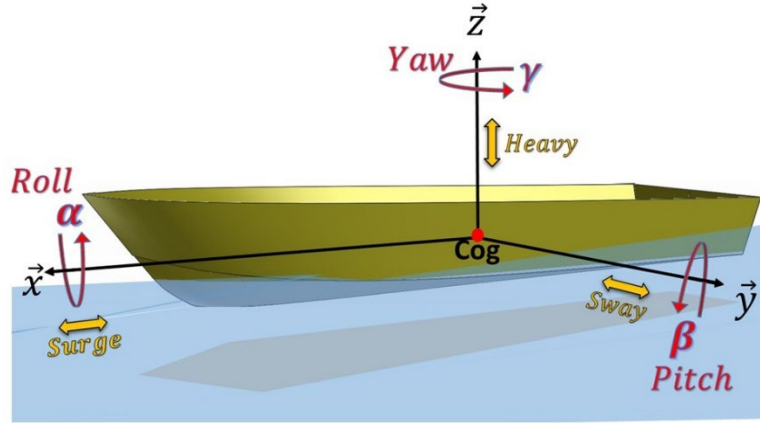
206 The computation was performed on Intel Core i7-8700 CPU 3.2GHz using 10 cores corresponding to 1161
207 hours of propagation time, and 119 hours of wall time.

208 **2.4. Stresses in moored ships model**

209 Here, we use an analytical model to estimate the loads on a vessel's mooring system under the
210 hydrodynamic effects of a tsunami (Tahar and Kim, 2003; OCIMF, 2010). The vessel is modelled as a rigid
211 body with six degrees of freedom (DOFs). The first three DOFs are the surge, sway, and heave (x , y , and z)
212 of the vessel's centre of gravity (C_{OG}), given in the global frame (Figure 4). The other three are the Euler
213 angles, roll, pitch, and yaw (α , β , and γ), which describe the local frame rotation status with respect to the
214 global frame.

215 We considered two reference frames, the first of which is a global orthogonal inertial frame (fixed) with its
216 origin located somewhere at the mean water level, where the X-axis points eastward and the Z-axis points
217 upward for the global frame. The second is an orthogonal non-inertial frame, moving with the vessel, with
218 its origin located at the C_{OG} . The X-axis points toward the bow, while the Z-axis points upward for the local
219 frame. The roll and pitch initial equilibrium positions are considered at zero degrees.

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Figure 4. Definition of Ship Motions in Six Degrees of Freedom, the yellow ones describe translation and the red ones rotation.

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The model contemplates the vessel's hydromechanics and physics characteristics such as hydrostatic stiffness (which considers both buoyancy and gravity forces), vessel mass (m), metacentric heights ($GM_{t,l}$), and inertial forces defined by the vessel's moments of inertia around the principal axes ($I_{x,y,z}$) as well as describing the vessel's stability (Journée and Massie, 2001). The vessel's dynamics are described with the equations of a forced and damped mass-spring system which allows the following initial value problem (Eq. 5):

230

$$\begin{cases} \dot{Y} = f(Y, t) = \begin{bmatrix} \dot{\xi} \\ \ddot{\xi} \end{bmatrix} = \begin{bmatrix} \xi \\ M^{-1} \cdot [B \cdot \dot{\xi} + G \cdot (\xi - \xi_0(t)) + F_m(\xi) + F_d(\xi, t)] \end{bmatrix} \\ Y(t = 0) = Y_0 \end{cases} \quad (5)$$

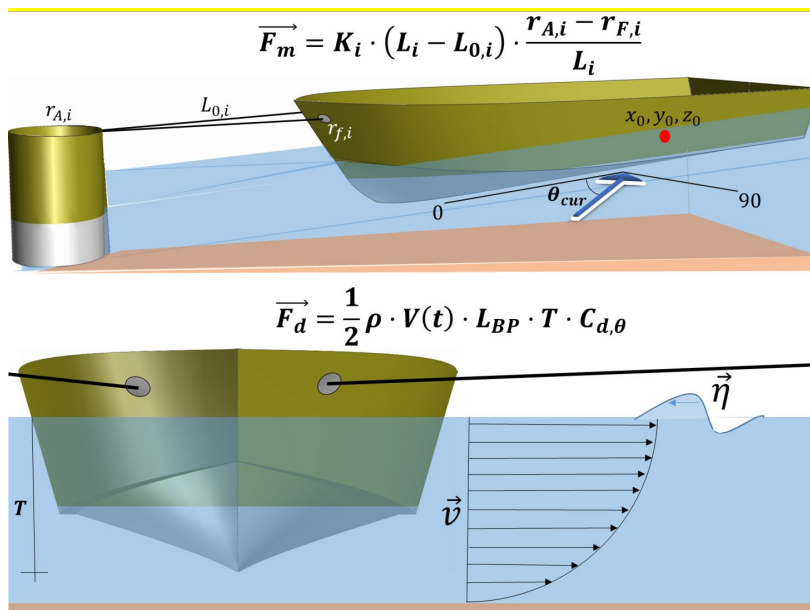
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where Y_0 is the initial vessel state vector, containing the initial position and the speed of the vessel, B is the damping matrix, G is the stiffness matrix, ξ is defined as the stacking of all the DOFs, ξ_0 is the initial equilibrium position, and F_m and F_d are the mooring system forces and the current drag forces (Figure 5).



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Figure 5. Schematic layout of Ship Mooring system forces F_m and Drag Forces F_d . The dynamics of the moored vessel are defined with a second-order ordinary differential equation (ODE)

238 The mooring system F_m is exclusively considered when the movement of the vessel results in a greater
 239 increase in the length of the line L_i compared to the previous position, as shown in the following Eq. (6):

$$240 \quad F_{m,i} = \begin{cases} K_i \cdot (L_i - L_{0,i}) \cdot \frac{r_{A,i} - r_{F,i}}{L_i}, & L_i > L_{0,i} \\ 0, & L_i \leq L_{0,i} \end{cases} \quad (6)$$

241 Where K_i includes Elastic properties for the i -th line, L_i is the line length, r_A and r_F are the pile and fairlead
 242 positions (where the line is tied to the hull). The Morison drag force model (Oh et al., 2020) is utilized to
 243 calculate the drag force F_d . The tsunami current at time t is defined by its speed. The current drag force
 244 changes depending on the angle of incidence, the $F_{d,x,y}$, calculated as Eq (7):

$$245 \quad F_{d,x,y}(\xi, t) = \frac{1}{2} \rho \cdot V(t) \cdot L_{BP} \cdot T \cdot \begin{pmatrix} \cos(\gamma) & -\sin(\gamma) \\ \sin(\gamma) & \cos(\gamma) \end{pmatrix} \cdot \begin{pmatrix} C_x(|\theta(t)|) \\ C_y(|\theta(t)|) \cdot \text{sgn}(\theta(t)) \end{pmatrix} \quad (7)$$

246 Where C_x and C_y are the drag forces in the x and y axes, ρ is the water density, $V(t)$ is the tsunami current
 247 velocity, L_{BP} is the length between the perpendicular, T is the vessel's draft, and γ is the Yaw DOF. We
 248 considers the tsunami current angle θ to be parallel to the vessel's centerline at zero degrees. Finally, this
 249 first-order ODE is integrated with a Runge-Kutta-4-5 method implemented in the SciPy Python library
 250 (Dormand and Prince, 1980; Shampine, 1986).

251 The model inputs consist of the vessel's dimensions, hydromechanical and mass properties, the ship's
 252 berthing scheme (including piles and fairleads coordinates), the line properties (such as young modulus and
 253 length), and the temporal tsunami dynamics (including waves and currents time-series) at the vessel's
 254 location. It should be noted that the tsunami dynamics time-series were obtained from the dispersive
 255 Boussinesq-type numerical model, explained in the previous section 2.3, who solve the equations known
 256 as Serre-Green-Naghdi (SGN) instead of the usual shallow water equations (SWE). The SGN equations are
 257 still depth-averaged equations, with the same conserved quantities (Berger and LeVeque, 2023). Their
 258 numerical results can be used to determine the estimation of current velocities due to tsunamis in harbor
 259 environments (Admiral et al., 2014; Lynett et al., 2014; Borrero et al., 2015; Ayca et al., 2014). The model
 260 outputs the movements in each DOF and the resulting stress, measured in tons, for each line throughout the
 261 time series.

262 3. Results

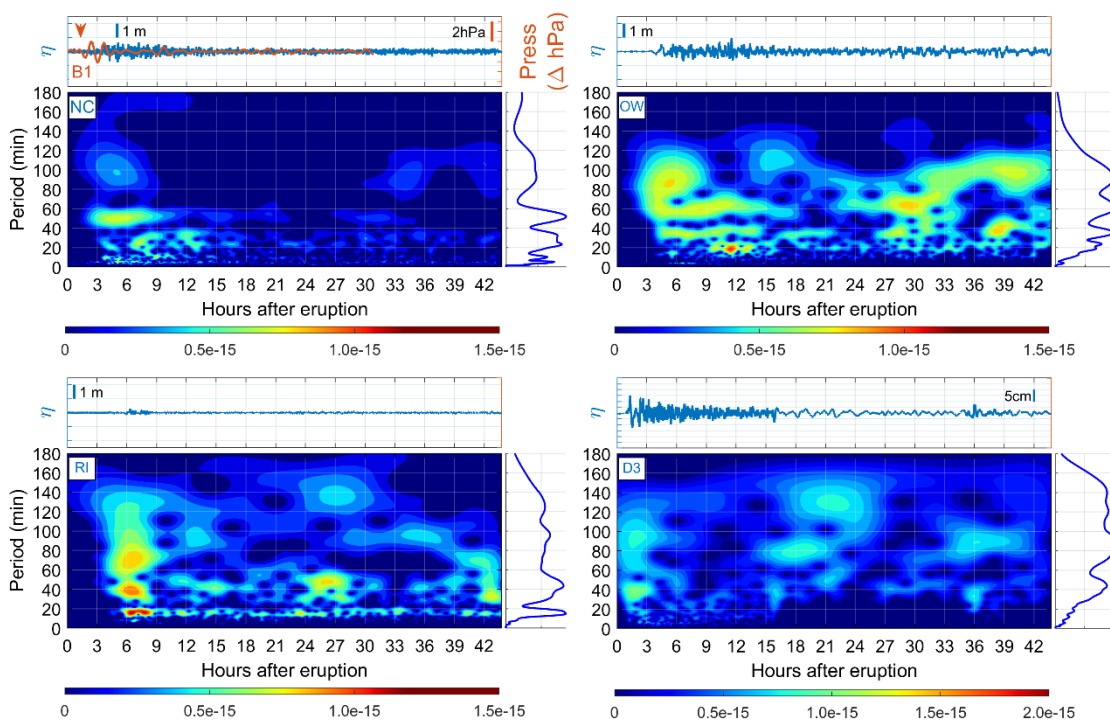
263 3.1. Atmospheric and oceanic data analysis

264 The analysis using wavelets is based on the hypothesis that the atmospheric waves' integral characteristics,
 265 such as the periods and propagation velocities, remain reciprocal when resonance is generated between
 266 atmospheric and oceanic waves. This allows the current knowledge extrapolation about atmospheric waves,
 267 which have been extensively studied in the literature, and their effect on oceanic tsunami waves.

268 The results in Figure 6, Figure 7, and Figure 8 show the analysis of the recorded atmospheric and sea-level
 269 signals, which are composed of three panels for each sensor. The top panel shows the filtered time-series

270 of both sea level and atmospheric pressure (blue and orange respectively). The orange arrow indicates the
 271 leading Lamb wave arrival time respectively. The lower panel shows the spectral results (wavelets) of the
 272 de-tided series of the ocean surface, the red-blue color scale marks the highest and lowest energy
 273 concentrations respectively; to the right is the Fourier spectrum obtained from integrating the wavelet over
 274 time.

275 Results in Figure 6 correspond to the tide gauges **NC**, **OW**, and **RI**, DART buoy **D3**, and pressure sensor
 276 **B1** (see Figure 1 for location). Wavelets consistently show four energy groups for sensors tide gauges **NC**,
 277 **OW**, **RI**, and DART buoy **D3**. These results allows for the identification of the initial characteristics of
 278 tsunami waves forced by atmospheric waves, i.e., the arrival times and wave periods.
 279

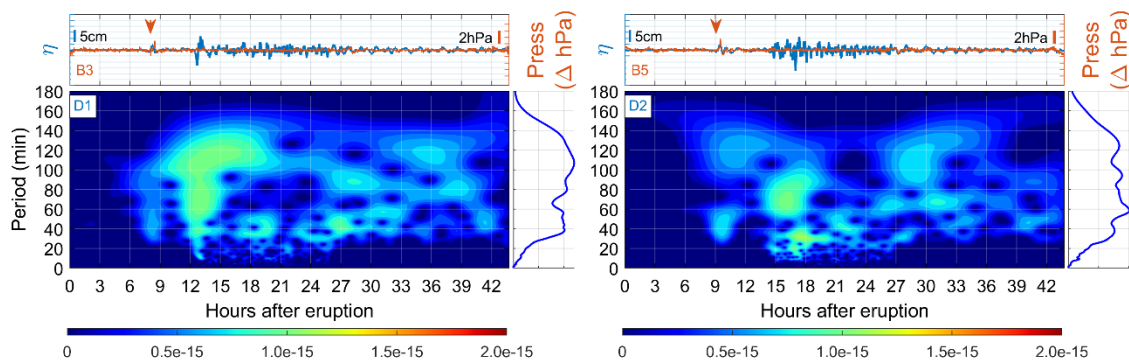


280
 281 **Figure 6. Analysis of air-pressure and sea-level records at tide gauges NC (North Cape, New Zealand), OW**
 282 **(Owenga, New Zealand) and RI (Rikitea, France), DART buoy D3 (51425, NDBC), and air-pressure sensor B1**
 283 **(North Cape, New Zealand). For each sensor, the time series of the air-pressure sensor (orange line) and tide**
 284 **gauge (blue line) are shown in the upper panel. The orange arrow refers to the arrival time of the leading**
 285 **pressure pulse. The panel to the right of the wavelet is the resulting frequency spectrum (FFT) of the time**
 286 **integration of the wavelet.**

287 The energy clusters fall within the 5-10 min, 20 to 40 min, 40 to 60 min, and 80-120 min periods, do the
 288 energy clusters suggest that there were multiple mechanisms that generated the Tonga tsunami waves.
 289 These results are consistent with the findings of previous studies (Hu et al., 2023; Kubota et al., 2022;
 290 Omira et al., 2022), where tsunami waves of 1-2 hr. period were also observed in different tidal gauges
 291 when analyzing the similar phenomenon that took place in 1883 during the eruption of the Krakatau
 292 volcano. (Choi et al., 2003; Pelinovsky et al., 2005).

293 Figure 7 shows far-field results (deep waters near the Peruvian coast) in sensors **D1-B3** and **D2-B5**. Air-
 294 pressure time-series shows the 2 hPa pulse associated with the leading Lamb wave arrived first, followed
 295 by second disturbances travelling at more than 200 m/s (Hu et al., 2022; Omira et al., 2022). DART buoy

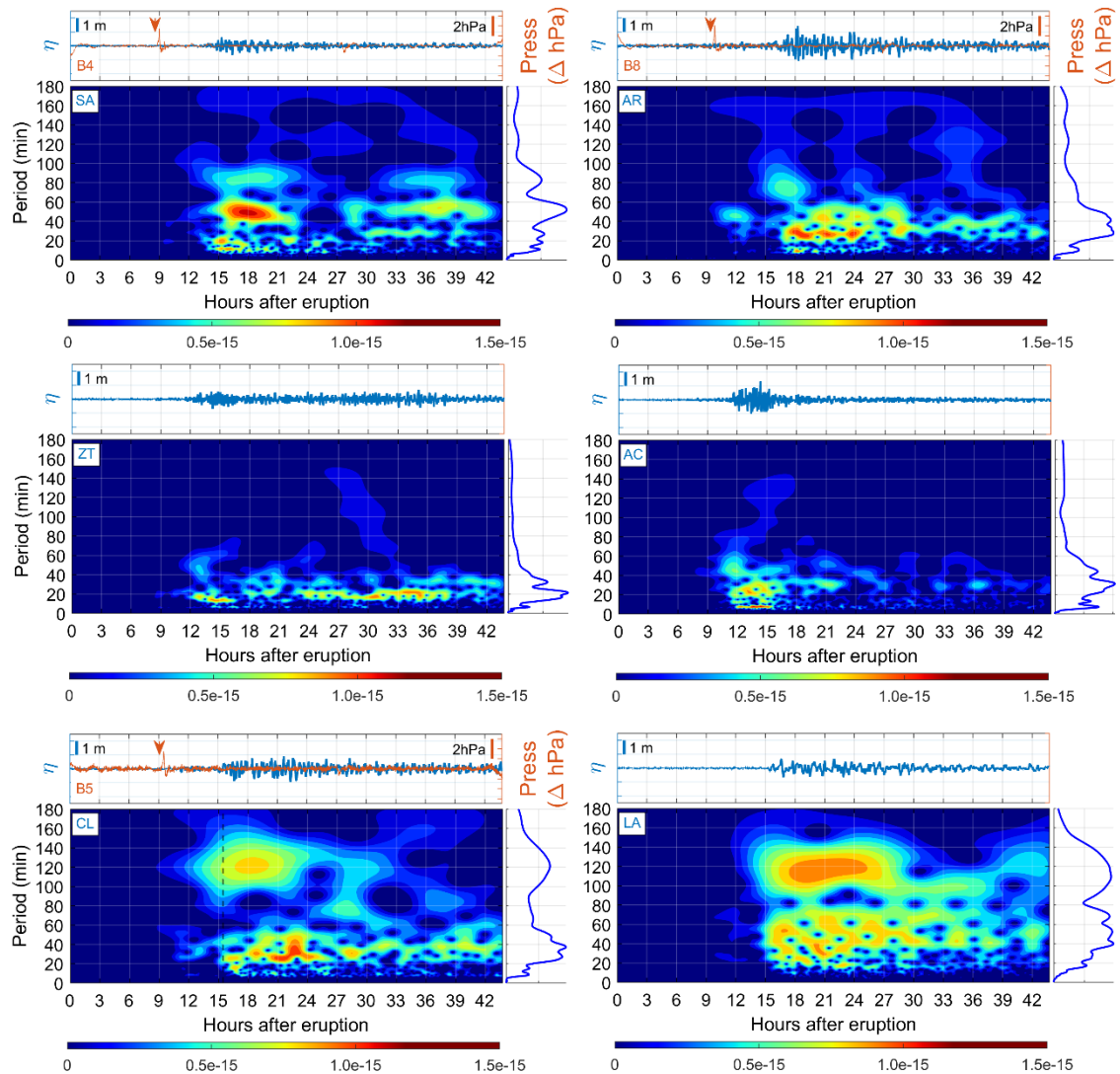
296 wavelets provide more spectral information related to the physical properties of these atmospheric waves
 297 coupled in the ocean. For example, DART Buoy **D2** shows that the first pulse coincides with the leading
 298 Lamb wave between 30- and 60- minute periods arriving 9 hours after the main eruption. Then, there is a
 299 group of energy contained in four ranges of periods: (i) about 10 min, (ii) between 20 and 40 min, (iii)
 300 between 60 and 90, and (iv) between 100 and 140 min. The latter is possibly associated with the air-ocean
 301 Proudman resonance that occurred on the Tonga Trench and propagated as common tsunami gravity waves
 302 towards the Southern American coast (Omira et al., 2022).
 303



304
 305 **Figure 7. Analysis of air-pressure and sea-level records at DART buoys D1 (32413, NDBC) and D2 (32401,**
 306 **NDBC) and atmospheric pressure sensors B3 (330031, Chile) and B5 (250005, Chile). For each sensor, the**
 307 **filtered time series of the atmospheric pressure sensor (orange line) and tide gauge (blue line) are shown in the**
 308 **upper panel. The orange arrow refers to the arrival of the leading pressure pulse. The right panel of the wavelet**
 309 **is the frequency spectrum resulting from the time integration of the wavelet.**

310 Figure 9 shows the spectral results for other locations along the Pacific American coasts. The South Pacific
 311 American instruments are **SA-B4** (Chile), **AR-B8** (Chile), **CL-B5** (Peru) and **AL** (Ecuador). The sensors
 312 in Central and North America are **ZT** (Mexico) and **AC** (USA). The wavelets' results in Chile, Mexico,
 313 and the USA show several energy groups: one in 40 - 60 min periods, another group between 20 - 40 min,
 314 and finally, energy in periods less than 10 min. Those wavelets exhibit a pattern similar to that observed in
 315 deep water sensors, with a notable difference regarding the absence of periods close to 120 min.

316 Subsequently, Figure 8 shows the analysis for sensors **LA** (Ecuador), and **CL-B5** (Peru), 15 km from the
 317 vessel accident. The black dotted vertical line on the **CL** wavelet refers to the moment when the ship's
 318 moorings break and the oil spill occurs, according to the captain of the ship, Mare Doricum. It can be
 319 observed in the **CL** wavelet that: (i) the Lamb wave coupled in the ocean (spectral energy between 30 - 60
 320 min periods), (ii) the mooring break moment coincides with the high period spectral energy (max between
 321 110-130 min period). Additionally, the energy within the 100 to 140 min period is present in deep water,
 322 (e.g., at DART buoy **D1** in Figure 7) and amplified exclusively in front of the Ecuador and Peru coasts (**LA**
 323 and **CL** tide gauges).
 324



325

326 **Figure 8.** Analysis of air-pressure and sea level records at the tide gauges of SA (San Antonio, Chile), AR (Arica,
 327 Chile), ZT (Zihuatanejo, Mexico), AC (California, USA), CL (Callao, Peru), and LA (La Libertad, Ecuador).
 328 The upper panel shows the time series of the atmospheric pressure sensor (orange line) and tide gauge (blue
 329 line). The orange arrow refers to the arrival of the leading Lamb wave. For the lower panel, we have the Wavelet.
 330 The vertical black dashed line in the CL wavelet refers to the instant when the vessel's moorings broke at La
 331 Pampilla port, Peru. The panel to the right of the wavelet is the frequency spectrum.

332 3.2. Numerical modelling of atmospheric pressure-induced tsunami waves

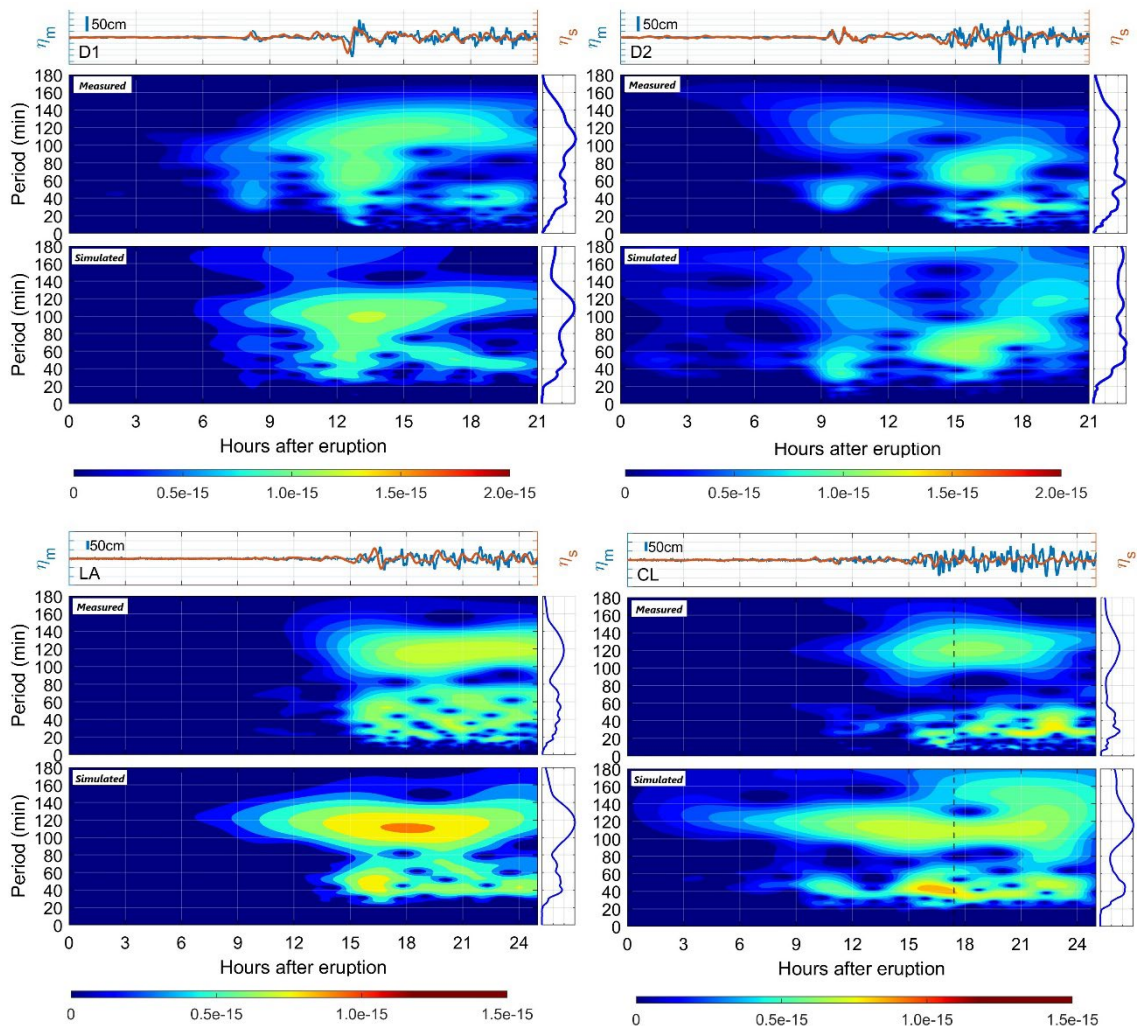
333 The numerical simulations have been calibrated/validated using both far- and near-field instrumental data.
 334 After validation, the significance of tsunami-like waves induced by atmospheric acoustic-gravity waves
 335 and tsunami-induced waves resulting from the submarine explosion were analyzed. We present the results
 336 in Figure 9, which shows the observed and simulated tsunami waveforms near the coast of Peru.

337 A comparison of observed and simulated tsunami waveforms at DART buoys (D1 and D2) shows that the
 338 Boussinesq numerical model correctly reproduces the first tsunami wave. It also fairly reproduces the
 339 second train of tsunami waves, likely associated with air-ocean resonance in deep ocean (near Tonga
 340 trench), and travelling at common tsunami speeds (Omira et al., 2022; Hu et al., 2023; Kubota et al., 2022).
 341 In shallow waters, the model correctly reproduces the tide gauges LA and CL (closest to the port of La
 342 Pampilla in Peru.), like in deep waters.

343 The correlation results obtained from the numerical validation near La Pampilla Port are mainly the
 344 consequence of detailed information such as bathymetry and atmospheric forcings. The low quantity/quality
 345 of the actual measured data nearby the port leads to the results:

- 346 • Do not accurately capture perturbations due to nonlinear interactions due to processes such as
 347 refraction, diffraction and reflection.
- 348 • Underestimation of the results in the ocean surface wave.
- 349 • Underestimation of current velocity.

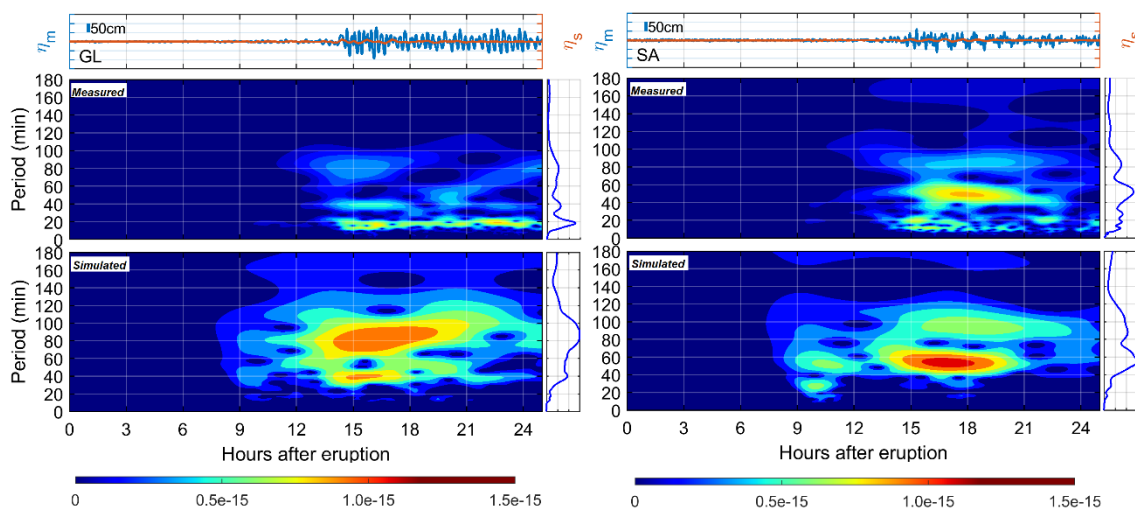
350 The wavelets and Fourier transform show a correct trend of the wave characteristics measured in each
 351 sensor, as shown in Figure 9. Wavelets corresponding to both deep and shallow waters present several
 352 groups of waves forced by acoustic waves between 20-40 minutes, periods 40-60 min, and long-period
 353 waves about 120 min (Hu et al., 2023; Kubota et al., 2022; Omira et al., 2022). Likewise, the Fourier spectra
 354 also show two distinguished groups of 40-60 min and 100-120 min in shallow water.
 355



356
 357 **Figure 9. Validation of numerical results at DART D1 and D2 buoys and tide gauges CL (Callao, Peru), and LA**
 358 **(La Libertad, Ecuador). For each buoy, the measured (blue line) and simulated (orange line) time series are**
 359 **shown in the upper panel. The lower panel shows the measured free sea surface wavelets (upper wavelet) and**
 360 **numerical simulation (lower wavelet). The vertical black dashed line in CL refers to the instant of the vessel**
 361 **mooring break in La Pampilla harbor, Peru. The panel to the right of each wavelet is the frequency spectrum.**

362 Compared to the DART buoys, the simulations exhibit similar behaviours because they are located at great
 363 depths, where the influence of the bathymetry and the land boundaries is negligible. The simulations
 364 demonstrate that tide gauges reveal variations such as earlier arrival times or more energy, possibly
 365 associated with local effects and limitations in resolution. **Despite these limitations, the model is sufficiently**
 366 **useful for the purpose of the study.**

367 Figure 10 displays simulation results for shallow water tide gauges **GL** and **SA** (located north and south of
 368 Peru, respectively), demonstrating that the 120-minute period wave is exclusive of the coast of Peru and is
 369 likely intensified by local effects. The wavelet analysis indicates that neither the simulated nor the measured
 370 waves show a significant amplification of high-period energy, as seen in the sensors situated off the coast
 371 of Peru.
 372



373
 374 **Figure 10. Comparisons of the numerical results at the GL (Galapagos, Ecuador) and SA (San Antonio, Chile)**
 375 **tide gauges are shown. For each tide gauge, the measured (blue line) and simulated (orange line) time series are**
 376 **shown in the upper panel. The lower panel has measured (upper wavelet) and simulated (lower wavelet) ocean**
 377 **results. The panel to the right of each wavelet is the frequency spectrum.**

378 3.3. Vessel response due to acoustic and tsunami waves

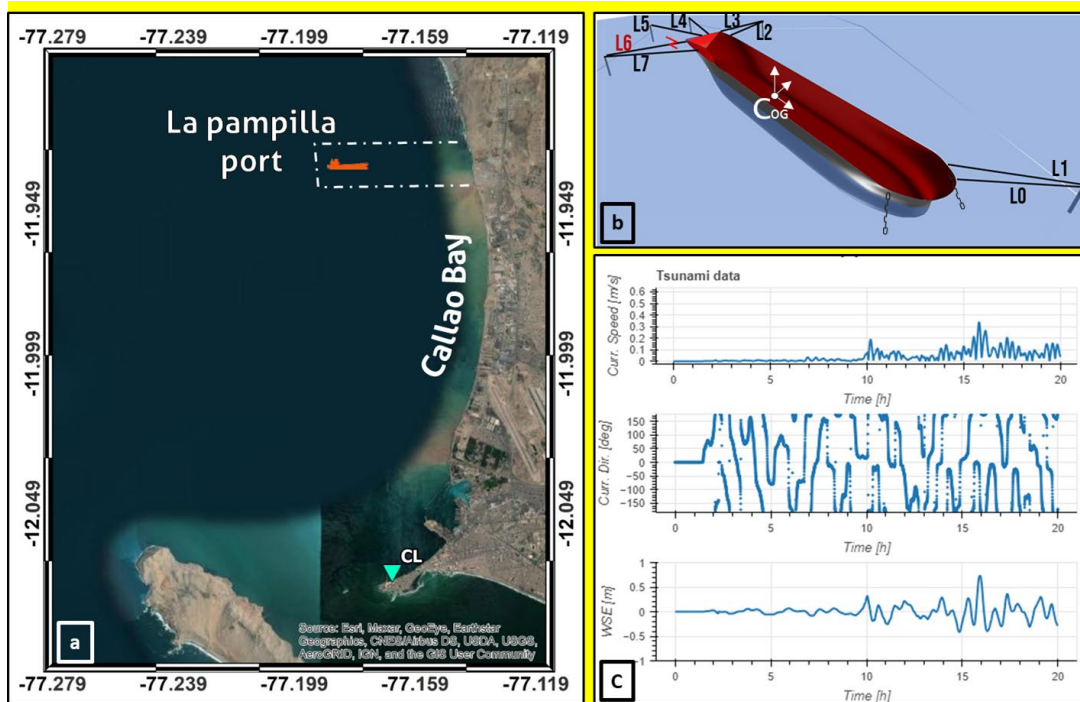
379 The model described in Section 2.4 was implemented to estimate the mooring stresses due to tsunami
 380 hydrodynamic effects produced during the Tonga event. The purpose is to demonstrate the variability in
 381 stress levels when exposed to tsunami waves of varying periods and, therefore, different hydrodynamic
 382 conditions.

383 The current velocity and water elevation time-series were extracted from the Boussinesq tsunami model,
 384 presented in Section 2.3 and validated in Section 3.2 at coordinates **-11.932 latitude, -77.181 longitude**
 385 **(Figure 11.a). The velocity of the current and Sea Water Elevation (SWE) input to the mooring line-loading**
 386 **model are presented in Figure 11.c. The numerical results suggest that the ocean dynamics over time begins**
 387 **to be noticeable after 10 hours after the eruption, which coincides with the arrival of the leading Lamb wave**
 388 **and with maximums at times close to the time of the rupture accident according to the port authority. The**
 389 **maxima of the current and SWE data values close to 40 cm/s and 0.7 m respectively. On the other hand,**

390 the direction of the current suggests a north-south tilting motion, a similar pattern observed during the entire
 391 simulation.

392 The mooring scheme (Figure 11.b) is similar to the one found in Terminal 2 of the Port of La Pampilla in
 393 Peru during the mooring-break accident. The vessel is moored to five buoys with eight moorings, one
 394 forward and four at the stern (in addition to two stern anchors anchored at a depth of 18 meters). The line
 395 number six (L6 in Figure 11.b) was the one that broke in the actual accident that occurred at the Port of La
 396 Pampilla 15 hours after the eruption of the THTT volcano.

397



398
 399 **Figure 11. a, shows the location of the tide gauge CL and the port of La Pampilla at Callao Bay – Peru. b, is the**
 400 **berthing scheme implemented in the mooring lines loads model, where L6 is the line that broke and caused the**
 401 **instability in the mooring system safety. CoG is the center of gravity of the tanker and origin of the model**
 402 **coordinate system. c, is the time series extracted from the numerical model at tanker location and inputted in**
 403 **the mooring line load model: upper panel is the current velocity, the middle panel is the current direction and**
 404 **the lower panel is the variation of the sea water elevation (SWE).**

405 In Tables 2 and 3 presents the vessel’s description and its hydromechanical characteristics. The entire
 406 mooring system schematic and the data used in the model are provided. The vessel used in this study is not
 407 the oil tanker Mare Doricum, but rather one with comparable physical characteristics. The ship is considered
 408 fully loaded throughout the simulation. (Figure 12).

409

LOA	274	m
Beam	48	m
draft	8	m
Mass	119.311	Ton
Xcg	118.3	m
Ycg	0	m

Zcg	-6.65	m
Ixx	21470000	Ton m ²
Iyy	515780000	Ton m ²
Izz	515780000	Ton m ²
MGt	20.042	m
MGl	471.824	m
Displacement	100,434	Ton
Waterplane area	9920.68	m ²
Gz	99949.56131	Ton m
Groll	2012895.542	Ton m
Gpitch	47387108.39	Ton m

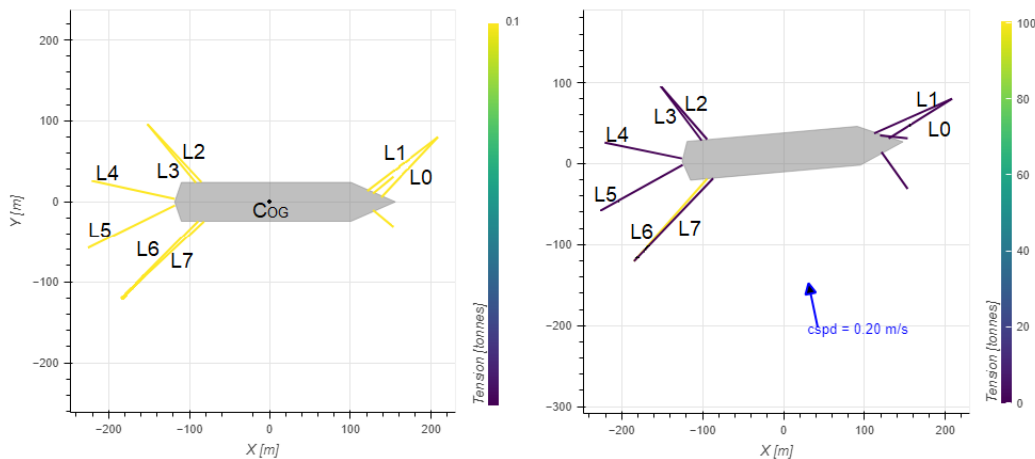
410 **Table 2. Description of the vessel used in the mooring stress simulation**

411

Line number	Pile position $r_{A,i}$ (m,m,m)	Fairlead position $r_{f,i}$ (m,m,m)	Length $L_{0,i}$ (m)
0	(208.27, 80.13, 3.00)	(138.34, 5.65, 6.00)	103.21
1	(208.27, 80.13, 3.00)	(121.00, 13.42, 6.00)	115.78
2	(-152.09, 96.13, 3.00)	(-85.20, 24.30, 6.00)	105.64
3	(-152.09, 96.13, 3.00)	(-92.13, 23.61, 6.00)	103.54
4	(-220.98, 25.94, 3.00)	(-118.19, 3.57, 6.00)	107.30
5	(-225.43, -57.61, 3.00)	(-117.98, -4.43, 6.00)	125.63
6	(-184.75, -120.44, 3.00)	(-89.22, -23.95, 6.00)	136.73
7	(-184.75, -120.44, 3.00)	(-82.04, -24.33, 6.00)	142.59

412 **Table 3. Description of the mooring system used in the stress simulation**

413



414

415 **Figure 12. On the left is the initial layout with the origin at the ship's COG and on the right is the layout at the**
416 **time of mooring breakage, where the yellow and purple colors mark the maximum and minimum stress values,**
417 **respectively. The cspd value is the current speed at the time of breaking of the mooring line.**

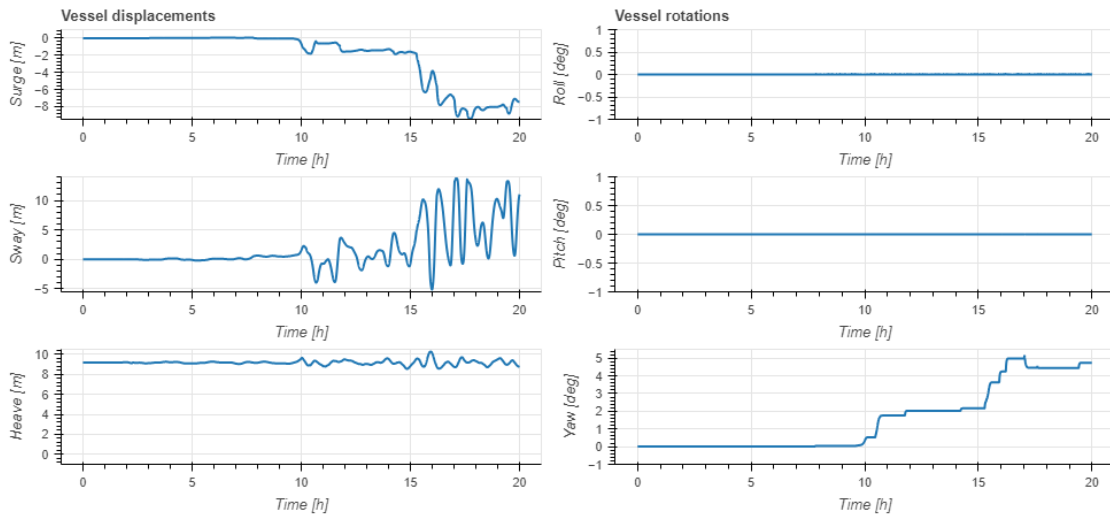
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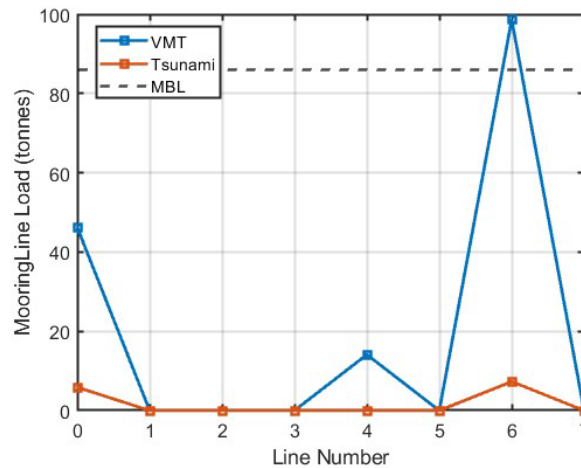
The results of the DOFs along the simulation are presented in Figure 13. The first instances of ship movement occur about 9 to 10 hours after the volcano erupts, coinciding with the arrival of atmospheric waves (VMT), with variations in the order of 2 m, 8 m, and 2 degrees for the DOFs Surge, Sway, and Yaw,

421 respectively, in the movements directly associated with tsunami hydrodynamic loads (López and Iglesias,
 422 2014). Then, 15 hours after the eruption, when the 120-minute period wave is present and the mooring
 423 breaks, further ship motion is generated, drastically increasing the vessel mentioned above DOFs values.
 424 The model results indicate that the movement was caused by the VMT. The anchored ship aligns with the
 425 surge, sway, and yaw; with a maximum deviation of 9 meters, 14 meters, and 5 degrees, respectively, which
 426 is more than enough to produce the breakage of the mooring system according to the port authority of La
 427 Pampilla (CPAAAAE, 2023).
 428



429
 430 **Figure 13. Time series of ship 6 degrees of freedom obtained from numerical simulation. Measured in hours**
 431 **after the eruption.**

432 To support the hypothesis that the 120-minute long-period wave along the Peruvian coast caused the
 433 mooring to break, a comparison was made between the stresses obtained by forcing with the VMT time-
 434 series and the tsunami caused only by the submarine explosion. The stress results for each line in both cases
 435 are shown in Figure 14. This illustration shows two things. Firstly, with the VMT, the lines that are primarily
 436 under stress are the starboard moorings lines number 0, 4, and 6, the latter having the maximum load (96
 437 tons), which exceeds the Minimum Breaking Load (MBL) by more than 10 tons. **The configuration of the**
 438 **mooring layout, tsunami wave direction, and hydrodynamic effects can be potential reasons for the increase**
 439 **in stresses, which could cause the mooring line to break.** Secondly, the findings suggest that the VMT
 440 results in a significant increase in mooring stresses, exceeding 10-times the levels observed during the
 441 tsunami-only event (where the VMT is not included in the simulation). These results **suggest** that the
 442 atmospheric waves generated during the volcanic eruption have **triggered a VMT**, generating tsunami-like
 443 waves that **may** have affected **mooring safety of vessels berthed in offshore ports in the** far field.
 444



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Figure 14. Maximum stresses obtained from the simulation at each mooring. Blue and orange lines represent the results of the simulations with and without atmospheric waves, respectively.

448

4. Conclusions

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The propagation of atmospheric waves and their coupling with the ocean were extensively studied following the Tonga event. Although epistemic uncertainties associated with the event are important, it was possible to understand the main drivers and effects of the volcano-meteorological tsunami (VMT) in the mooring safety of vessels moored in offshore ports in the far field. The air-ocean Proudman resonance in deep water was the driving mechanism that caused long period gravitational waves (which had very similar characteristics to those of a tectonic-source tsunami.) to travel along the Pacific Ocean and affect the offshore port La Pampilla in the far field.

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The potential of the explosion-induced atmospheric waves to magnify tsunamis once they pass over deep ocean regions has been evidenced. The second train of tsunami-like waves that arrived in the Peruvian coast and affected the mooring safety were generated due to Proudman resonance between acoustic-gravity waves with ocean-gravity waves, which produced an air-ocean energy transfer that led to an increase in tsunami energy in the far field instead of losing it. This happened near the Tonga trench in the propagation direction of South America (Figure 3-c in Omira et al., 2022).

462

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The presence of the high period waves exclusively in the tide gauges of Peru and Ecuador (CL and LA, respectively) could be explained by several processes associated with shoaling. These processes could include the width and slope of the continental shelf (which is wider on the Peruvian coast than on the Chilean coast, for example) and the effects associated with topographic boundaries and their geometry, such as the natural bay oscillation modes.

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The spectral analysis results establish the influence of the atmospheric waves generated by the HTHH volcano. Considering that, the 120-minutes long-period waves were associated with the air-ocean-resonance of the Tonga event and that numerical simulations additionally show the mooring line stress using the VMT time-series, it is possible to conclude that the Tonga tsunami caused the overstressing and subsequent accident in the port of La Pampilla, Peru.

472 Hydrodynamic loads on the vessel's hull due to tsunamigenic phenomena can threaten the stability of
473 moored vessels. These loads are mainly due to drag forces (driven by the tsunami kinetic energy) that affect
474 ship stability. Based on the ship DOF, the results suggest that VMT affect mainly the horizontal plane
475 motions, two associated with displacements (sway and surge) and the other with the angle of rotation about
476 its vertical axis (yaw). This is likely explained by the large amount of kinetic energy that tsunamis have in
477 their propagation, which travel at high speed, but with little wave elevation. The VMT produced during the
478 Tonga 2022 event was accompanied by long-period waves and currents, which could affect the stability of
479 the mooring system in the port of La Pampilla, Peru.

480 The hydrodynamic effects of very long period tsunami waves can generate damage similar to those of
481 tsunamis of tectonic origin, affecting elements such as infrastructure, vessels, merchandise and people in
482 port environments.

483 **4.1. Final Considerations**

484 Coastal and port infrastructure are not prepared to respond preventively to these Tonga-type tsunamis,
485 leaving them "unprotected", as tsunami warnings are not issued once a volcano eruption is known.
486 Furthermore, in the analyzed event, the initial ocean disturbance arrived earlier than anticipated because
487 the atmospheric waves produced a VMT that travelled at sonic velocity. This statement holds relevance as
488 state and international authorities are responsible for maritime safety and the creation of cautions-warnings
489 and suggestions to aid distinct users in coastal and offshore locations.

490 This event showed the need for Tsunami Early Warning Systems (TWS) to be prepared to include
491 atmospheric waves and detect them from existing monitoring sensors. In addition, Standard Operational
492 Procedures need to include protocols for these events to avoid damage to port facilities and ships, such as
493 the breaking of moorings and ship collisions. These events can also generate local flooding increasingly far
494 away from the origin and affect the population and coastal infrastructures (cities, nuclear reactors,
495 petrochemical industry, etc.). Therefore, efforts towards the incorporation of tsunamis caused by volcanic
496 acoustic waves in tsunami warning systems are needed.

497 **5. Author contribution**

498 Supervision and methodology (G.M and A-Q.I); Waves simulations (K.J and O.R); revision (B.M and O.R).
499 All authors have read and agreed to the published version of the manuscript.

500 **6. Competing interests**

501 At least one of the co-authors is a member of the editorial board of Natural Hazards and Earth System
502 Sciences.

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