

1 **Measurements of frazil ice flocs in rivers**

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5 **Abstract.** Frazil floc sizes and concentrations have been investigated in a small number of laboratory studies but no detailed
6 field measurements have been reported previously. In this study, a submersible camera system was deployed a total of eleven
7 times during the principal and residual supercooling phases in the North Saskatchewan, Peace, and Kananaskis Rivers to
8 capture time-series images of frazil ice particles and flocs. Images were processed to accurately identify flocs and to calculate
9 their sizes and concentrations. Key hydraulic and meteorological measurements were collected and air-water heat fluxes were
10 estimated to investigate their influence on floc properties. A lognormal distribution was found to be a good fit for the floc size
11 distribution. The mean floc size ranged from 1.19 to 5.64 mm and the overall mean floc size was 3.80 mm. The mean floc size
12 decreased linearly as the local Reynolds number increased. The average floc number concentration ranged from 1.80×10^{-4} to
13 $1.15 \times 10^{-1} \text{ cm}^{-3}$. The average floc volumetric concentration ranged from 2.05×10^{-7} to 4.56×10^{-3} and was found to correlate
14 strongly with the fractional height above the river bed. No significant correlations were found between the air-water heat flux
15 and floc properties. Time series analysis showed that during the principal supercooling phase, floc number concentration and
16 mean size increased significantly just prior to peak supercooling and reached a maximum near the end of principal
17 supercooling. During the residual supercooling phase, the mean floc size did not typically vary significantly even 2.5 hours
18 after the residual phase ended and the water temperature increased above zero degrees.

19 **1 Introduction**

20 In northern rivers, individual frazil ice particles form when the water is turbulent and supercooled below its freezing point due
21 to heat loss to the atmosphere. These suspended particles are ice crystals that are inherently adhesive in the supercooled water.
22 As they are transported by the turbulent flow, they may collide with each other due to spatially varying particle velocities
23 resulting from differential rising or due to spatially varying flow velocities created by turbulent eddies and boundary shear
24 (Mercier, 1985). Colliding particles may freeze together forming clusters of particles known as frazil flocs in a process called
25 flocculation (Clark and Doering, 2009). Frazil flocs increase in size either by the thermal growth of the crystals and/or by
26 further aggregation of individual frazil ice particles or flocs. Once frazil flocs gain sufficient buoyancy they rise to the water
27 surface forming surface ice pans or are deposited under existing surface ice contributing to their mass increase (Hicks, 2016).
28 In addition, turbulent flow may transport flocs to the river bed where they may adhere to the bed forming anchor ice (Kempema
29 et al., 1993). Once the surface ice pan concentration is high enough, congestion of incoming ice pans will occur at certain

30 locations where there is a flow constriction and a solid ice cover will form and propagate upstream (Beltaos, 2013). The
31 formation of a continuous solid ice cover insulates the flowing water from further heat loss to the atmosphere, thus preventing
32 the occurrence of supercooling and the production of frazil ice until the ice cover thaws or breaks up (Beltaos, 2013). Frazil
33 flocs may cause serious problems at hydroelectric facilities and water treatment plants by adhering to water intake, trash racks
34 and partially or fully blocking the flow (Ettema and Zabilansky, 2004; Barrette, 2021, Ghobrial et al., 2024). Therefore, it is
35 important to obtain a better understanding of the properties of frazil flocs as well as their evolution to better model and predict
36 their behavior.

37

38 As the constructing unit of frazil flocs, individual frazil ice particles have been investigated both in laboratory settings and
39 field. These particles exhibit various forms including dendritic, needle, and irregular but are predominately disc-shaped with
40 diameters ranging from 0.022 to 6 mm (McFarlane et al., 2017) and diameter-to-thickness ratios of 11 to 71 (McFarlane et al.,
41 2014). A lognormal distribution can be used to describe the particle size distribution (Daly and Colbeck, 1986; Clark and
42 Doering, 2006; McFarlane et al., 2015). During the principal supercooling period when the water temperature varies
43 transiently, the time from the start of supercooling to when a steady residual supercooling water temperature is reached, the
44 mean diameter of particles was found to first increase before reaching an approximately constant value (Clark and Doering,
45 2006; McFarlane et al., 2015). At the same time the number concentration of suspended particles first increased slowly then
46 more rapidly, peaking just after peak supercooling occurred (i.e., the minimum water temperature) (McFarlane et al., 2015;
47 Ye, 2002; Clark and Doering, 2006). The rapid increase in particle concentration was attributed to secondary nucleation which
48 refers to the formation of new crystals due to the presence of stable parent crystals (Evans, et al., 1974). After peaking the
49 particle concentration decreased as particles were removed via flocculation.

50

51 There have been a small number of laboratory studies that investigated the properties of frazil flocs as well as the flocculation
52 process. Park and Gerard (1984) used artificial flocs fabricated from plastic discs to investigate the hydraulic characteristics
53 of frazil flocs. They found that the sharp-edged floc surface resulted in a significantly higher drag coefficient compared to a
54 solid smooth sphere of the same size and density. Kempema et al. (1993) conducted racetrack flume experiments to investigate
55 interactions of frazil and anchor ice with sediments. They observed that in freshwater frazil easily agglomerated into roughly
56 spherical flocs up to 8 cm in diameter. Flocs that struck the bed tended to entrain sediments into their voids and become heavy
57 and settle to the bottom in the shelter of ripples forming anchor ice. Reimnitz et al. (1993) observed the characteristics and
58 behaviour of rising frazil in seawater using a stirred vertical tube or tank. They found that individual frazil crystals combine
59 rapidly into flocs with diameters as large as 5 cm. The rise velocities of flocs ranged from 1 to 5 cm s⁻¹ and rapidly rising large
60 flocs induced small-scale turbulence. The porosities of the resulting surface slush accumulations ranged from 0.68 to 0.85,
61 with an average of 0.77. Clark and Doering (2009) investigated frazil flocculation under different turbulence intensities using
62 a counter-rotating flume. Results showed that higher levels of turbulence increased the rate of secondary nucleation, inhibited
63 the formation of large flocs, and produced more dense flocs.

64

65 Schneck et al. (2019) measured the size and number concentration of frazil ice particles and flocs in water of varying salinity
66 using a stirred frazil ice tank. Results showed that the mean floc size was 2.57 mm in freshwater and 1.47 mm in saline water
67 and a lognormal distribution fit the floc size distributions closely. The floc porosity was estimated to vary from 0.75 to 0.86.
68 Time series measurements of floc properties indicated that, in freshwater, the floc number concentration and mean size started
69 to increase significantly just prior to peak supercooling, reached a maximum shortly afterwards. After that floc number
70 concentration decreased slowly while the mean floc size continually increased very slowly during the principal supercooling
71 period.

72

73 The above studies were all conducted in laboratory facilities that do not replicate the complex natural environment.
74 Measurements of frazil flocs in supercooled rivers are needed to verify the laboratory results and improve numerical river ice
75 process models. However, no detailed quantitative field measurements of the properties or evolution of frazil flocs have been
76 reported in the literature. The objective of this study was to determine the statistical characteristics and temporal evolution of
77 floc sizes and concentrations, as well as to investigate the key factors affecting the properties of frazil flocs in rivers. A
78 submersible high-resolution camera system was used to capture time-series images of frazil flocs. Images were analyzed to
79 accurately determine floc sizes and concentrations. Key hydraulic and meteorological measurements were collected and air-
80 water heat fluxes were estimated to investigate their influence on floc properties. Time series of floc size, number concentration
81 and volumetric concentrations as well as size distributions measured in rivers during the principal and residual supercooling
82 phase are presented for the first time.

83 **2 Study Reaches**

84 Measurements were conducted in three regulated Alberta rivers, the North Saskatchewan River (NSR) at Edmonton, the Peace
85 River (PR) near Fairview, and the Kananaskis River (KR). Figure 1 shows the geographical locations of the study reaches,
86 deployment sites and weather stations. The characteristics of the study reaches are summarized in Table 1. The turbulent
87 dissipation rate in Table 1 was estimated using the listed slope as well as the average depth and width following Clark and
88 Doering (2008). The three rivers are significantly different in terms of their size and hydraulic characteristics. The flow of the
89 NSR is regulated by the Brazeau and Bighorn Dams which are ~233 km and ~423 km upstream of the Laurier Park site,
90 respectively. A daily water level fluctuation of 0.3 to 0.4 m occurred in the study reach due to hydropeaking (McFarlane et al.,
91 2017). The estimated turbulence dissipation rate is $0.0058 \text{ m}^2 \text{ s}^{-3}$. Freeze-up typically starts in early November and ends in
92 early to late December with the formation of a static ice cover. However, the 2022 winter freeze-up progressed in a surprisingly
93 rapid manner, starting on Nov 5, 2022, and ending just three days later on Nov 8, 2022.

94

95 PR has the largest average discharge, depth, and width of the three rivers (Table 1). The estimated turbulence dissipation rate
 96 is $0.0051 \text{ m}^2 \text{ s}^{-3}$ which is slightly smaller than NSR. The flow of PR is regulated by the W.A.C Bennett Dam and the Peace
 97 Canyon Dam which are $\sim 309 \text{ km}$ and $\sim 288 \text{ km}$ upstream of the Fairview water intake deployment site, respectively. These
 98 outflows at the dams are relatively warm water ($\sim 6 \text{ }^\circ\text{C}$) during the winter, affecting the river thermal regime for up to 550 km
 99 downstream of the dams (Jasek and Pryse-Phillips, 2015) which is $\sim 250 \text{ km}$ downstream of the deployment site. Therefore,
 100 supercooling and frazil ice generation only occurs at the deployment site when the zero-degree isotherm is located upstream
 101 and ceases when it retreats downstream. This unique condition allows freeze-up to persist until the ice front reaches the
 102 Fairview intake site typically in mid-January.

103

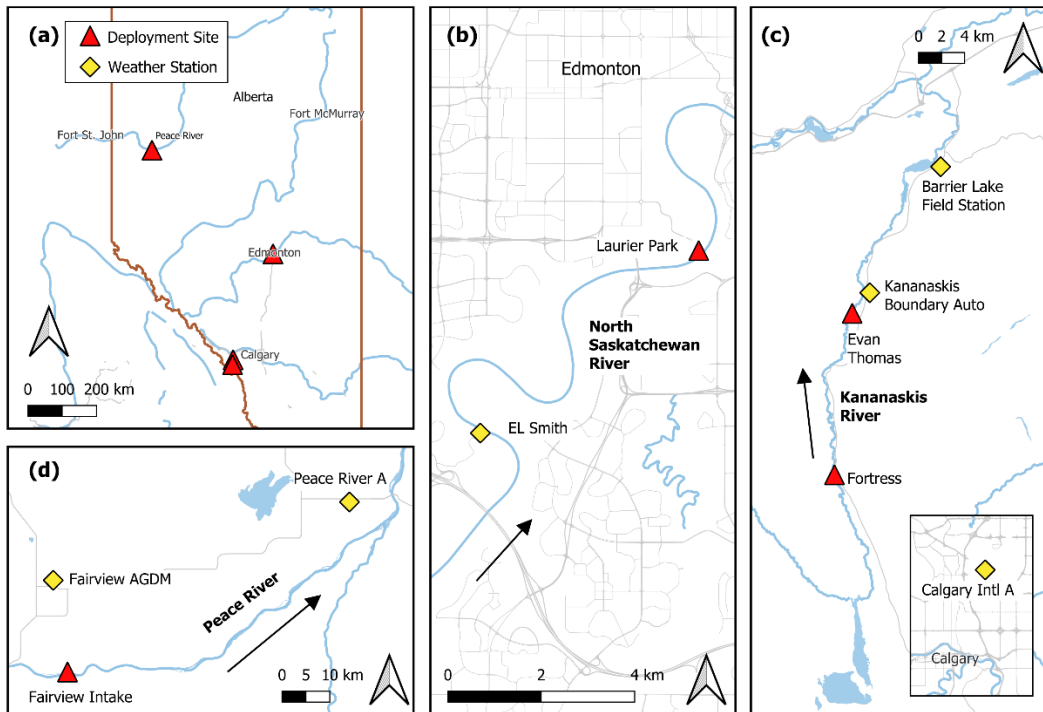
104 KR is the smallest of the three rivers in terms of average discharge, depth, and width (Table 1). It has the largest turbulence
 105 dissipation rate with a value of $0.2066 \text{ m}^2 \text{ s}^{-3}$, which is not unexpected since KR is a small-steep river in the mountains. The
 106 flow is regulated by the Pocaterra Dam which is 12 and 31 km upstream of the Fortress and Evan Thomas deployment sites,
 107 respectively. In winter, a dramatic discharge fluctuation from $\sim 1 \text{ m}^3 \text{ s}^{-1}$ to $21 \text{ m}^3 \text{ s}^{-1}$ occurred daily in the study reach due to
 108 hydropeaking (Government of Alberta, 2023). Low flows promote border ice formation reducing channel width, while high
 109 flows cause overtopping of existing ice and/or banks and prevent the formation of a complete ice cover. Without an ice cover
 110 to insulate the water, supercooling events and frazil generation occur when the air temperature is sufficiently cold.

111

112 **Table 1: Summary of the study reach characteristics.**

River	Slope	Average discharge ($\text{m}^3 \text{ s}^{-1}$)	Average depth (m)	Average width (m)	Average D_{100} of suspended sediment (mm)	Estimated turbulence dissipation rate ($\text{m}^2 \text{ s}^{-3}$)
NSR	0.00035	220	1.40	136	0.50	0.0058
PR	0.00025	1586	2.56	227	0.68	0.0051
KR	0.005	15	0.61	32	N/A	0.2066

113 *Note:* Slope, average discharge, average depth, and average width were obtained from Kellerhals et al. (1972); Average D_{100}
 114 of suspended sediments were computed from Water Survey of Canada historic size distribution data measured at North
 115 Saskatchewan River at Edmonton (05DF001) and Peace River at Dunvegan Bridge (07FD003) (Water Survey of Canada,
 116 2023).



117

118 **Figure 1: Maps showing (a) the locations of the deployment sites in Alberta, enlarged views of the locations on (b) the North**
 119 **Saskatchewan, (c) Kananaskis, and (d) Peace rivers.**

120 **3 Instrumentation, Methodology and Deployments**

121 A submersible camera system initially designed for imaging suspended frazil ice particles named “FrazilCam” (McFarlane et
 122 al., 2017) was modified in this study to image frazil flocs in the water column. Figure 2 shows the modified configuration of
 123 the FrazilCam system. A 36-megapixel Nikon D800 DSLR camera equipped with a Micro-Nikkor 60 mm f/2.8D lens was
 124 used to image underwater frazil ice particles and flocs. The camera was enclosed in an Ikelite waterproof housing. Two 16 cm
 125 × 16 cm Cavisson linear glass cross-polarizing filters were mounted 3.6 cm apart, which is 1.6 times larger than the original
 126 configuration. A PVC enclosure with a brass fitting on the top was installed in between the camera lens and polarizing filters
 127 to prevent ice or debris from flowing through this region blocking the camera field-of-view (FOV). The brass fitting was used
 128 for hot water injection to melt any ice that was initially trapped inside the enclosure. A Nikon SB-910 Speedlight flash in a
 129 Subal SN-910 waterproof housing was used as the light source, and a 5 mm thick white acrylic board was placed in between
 130 the polarizers and flash to diffuse the light. The camera settings were determined by submerging the system in a laboratory
 131 tank filled with tap water and capturing images of a transparent plastic ruler placed inside the camera FOV. This yielded an
 132 ISO of 6400, aperture f/25, and a shutter speed of 1/320. The configuration resulted in an image scale of 25.6 μm per pixel

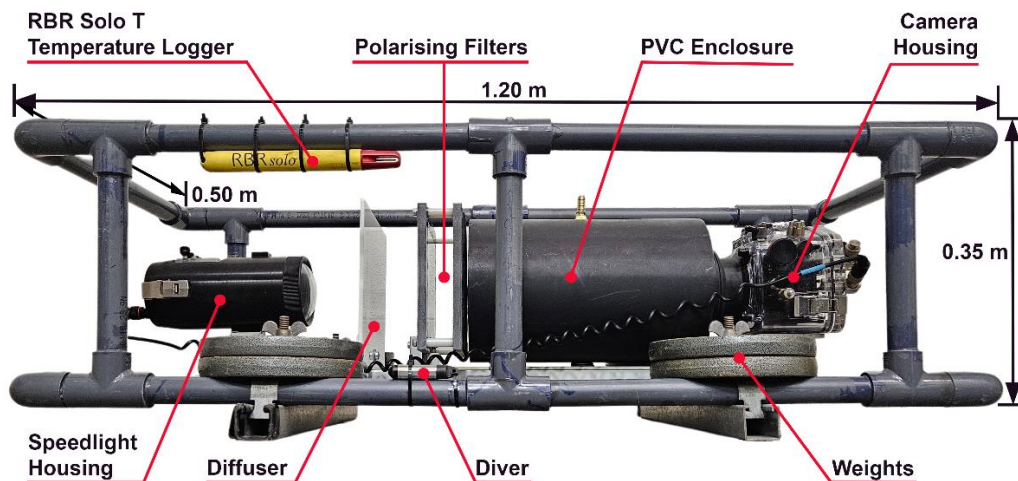
133 and an average FOV of 11.6 cm by 15.6 cm which is 6 times larger than the original configuration. The reason for enlarging
134 the FOV and increasing the gap between the polarizers was to enable larger flocs to pass through and fit within the FOV.

135

136 At the start of each deployment, the camera was programmed to acquire 5 images at 1 Hz every 9 s, 15 s, or 18 s depending
137 on the field conditions until the battery was depleted. A longer sampling interval (e.g. 18 s) was chosen for some deployments
138 to prolong the deployment duration with the goal of capturing a complete supercooling event. Just prior to deployment of the
139 FrazilCam in the river, the polarizers were rinsed with hot saline water to prevent ice crystals from forming on them once
140 submerged. The system was then quickly deployed in the river and the PVC enclosure was filled with hot fresh water from an
141 elevated container. During deployments, anchor ice often formed on system components as shown in Fig. 3 and ice that formed
142 on the polarizers could obstruct the FOV of the camera. To prevent or mitigate this problem, the polarizers were inspected
143 every 30 to 60 minutes and hot saline water was injected onto the polarizers to melt any ice crystals.

144

145 During each deployment, an RBR Solo T (accuracy $\pm 0.002^{\circ}\text{C}$) temperature logger sampling every second was attached to the
146 top of the frame to measure water temperature, and a Van Essen Diver (accuracy $\pm 1 \text{ cmH}_2\text{O}$) water level logger sampling
147 every 10 minutes was attached to the bottom of the frame to measure the water depth (Fig. 2). The water depth during the PR
148 deployments was measured using a wading rod since the Diver stopped working at that time. For all deployments the depth-
149 averaged water velocity was estimated using velocities measured adjacent to FrazilCam at 60% of the water depth. During the
150 2021 winter, the water velocity was measured using a 2-MHz Nortek AquaDopp High Resolution Acoustic Doppler Current
151 Profiler sampling every second with a blanking distance of 0.1 m and averaging every two minutes. For the rest of the
152 deployments, the water velocity was measured using a SonTek Flow Tracker Handheld Acoustic Doppler Velocimeter (ADV)
153 sampling every second for a total duration of 50 seconds.



154

155 **Figure 2: An image showing the configuration of the FrazilCam system.**



156

157 **Figure 3: An image showing the ice accumulation on the FrazilCam system.**

158 Meteorological conditions for the NSR reach were measured by a weather station installed at the E.L. Smith water treatment
 159 plant, which is located ~90 m from the river bank and ~6 km upstream of Laurier Park site (Fig. 1b). The weather station
 160 measures the air temperature, solar radiation, relative humidity, atmospheric pressure, wind speed and direction every minute
 161 and logs data every 10 minutes. An Apogee SN-500-SS net radiometer was deployed on the river bank at this location,
 162 measuring incoming and outgoing shortwave/longwave radiation every minute and logging data every 10 minutes. For the PR,
 163 1-hour interval meteorological data were obtained from ECCC station Fairview AGDM (ID: 3072525) and 3-hour interval
 164 cloud coverage data was obtained from the closest ECCC station Peace River A (ID: 3075041) as shown in Fig. 1d. For the
 165 KR, the Kananaskis Boundary Auto weather station operated by Alberta Forestry, Parks and Tourism (ACIS, 2023) was used
 166 to obtain 1-hour interval air temperature, humidity, wind speed, and wind direction data. In addition, 1-hour solar radiation
 167 data was obtained from the University of Calgary Barrier Lake Field Station weather station (University of Calgary, 2023),
 168 and 3-hour cloud coverage data was obtained from the closest ECCC station Calgary Intl A (ID: 3031092) as shown in Fig.
 169 1c. Table 2 summarizes the distance between weather stations and deployment sites. All weather stations are located within
 170 30 km of their nearby deployment sites, except for those providing cloud coverage data for PR and KR.

171

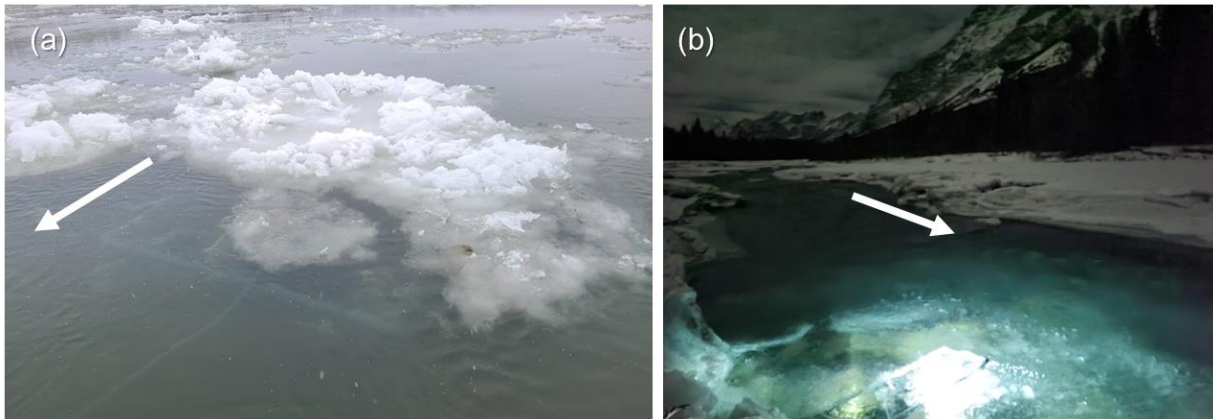
172 **Table 2: The distances between weather stations and deployment sites.**

River	Deployment site	Distance - weather station
NSR	Laurier Park	6 km - E.L. Smith
PR	Fairview Intake	18 km - Fairview AGDM; 68 km - Peace River A
KR	Evan Thomas	2 km - Kananaskis Boundary Auto; 15 km - Barrier Lake Field Station; 82 km - Calgary Intl A
	Fortress	16 km - Kananaskis Boundary Auto; 28 km - Barrier Lake Field Station; 88 km - Calgary Intl A

174 The FrazilCam system was deployed a total of eleven times during the 2021 and 2022 freeze-up periods, images of the
 175 FrazilCam during two of the deployments are shown in Fig. 4. The image sampling protocols were 5 images at 1 Hz every 9 s
 176 for all NSR and KR-E1 deployments, for KR-F1 and KR-F2 5 images at 1 Hz every 15 s, and for all PR deployments 5 images
 177 at 1 Hz every 18 s. Table 3 lists the detailed location, date, time, number of images processed, and deployment number for
 178 each deployment. The mean air temperature \overline{T}_a , mean water depth \overline{d} , depth-averaged flow velocity \overline{U} , and the local Reynolds
 179 number Re computed from \overline{d} and \overline{U} are also presented in Table 3. Eight of eleven deployments started in the afternoon around
 180 2 PM ~ 7 PM when the effect of solar radiation reduced decreasing heat gain of the water body, the time duration of
 181 deployments ranged from 1:48 to 3:21. As can be seen from Table 3, during these deployments \overline{T}_a ranged from -3.5 °C to -
 182 20.6 °C, \overline{d} ranged from 0.41 m to 1.24 m, \overline{U} ranged from 0.12 m s⁻¹ to 0.36 m s⁻¹, and Re ranged from 44866 to 160714,
 183 respectively, indicating that frazil floc properties and concentrations were measured and analyzed over a wide range of
 184 meteorological and hydraulic conditions. The eleven deployments captured various phases of supercooling but NSR-L4 was
 185 the only deployment that captured a complete principal supercooling phase (i.e., from when the water temperature first dropped
 186 below zero to when an approximately stable residual temperature was reached).
 187

188 **Table 3: Summary of the FrazilCam deployments and site conditions including the number (#) of images captured, mean air**
 189 **temperature \overline{T}_a , mean water depth \overline{d} , depth averaged water velocity \overline{U} , and local Reynolds number Re .**

River	Date (yyyy.mm. dd)	Time period (hh:mm~hh: mm)	# of processed images	Site	Deployment No.	\overline{T}_a (°C)	\overline{d} (m)	\overline{U} (m s ⁻¹)	Re
NSR	2021.12.3	16:41~18:49	4,099	Laurier Park	NSR-L1	-7.2	0.89	0.21	104,297
		19:05~21:34	4,797	Laurier Park	NSR-L2	-10.5	0.84	0.17	79,688
	2021.12.9	14:46~17:09	4,688	Laurier Park	NSR-L3	-3.5	1.24	0.19	131,473
	2021.12.12	15:02~16:50	3,495	Laurier Park	NSR-L4	-4.6	0.87	0.22	106,808
		17:08~19:31	4,091	Laurier Park	NSR-L5	-9.2	0.86	0.20	95,982
	2022.11.7	14:31~16:22	3,596	Laurier Park	NSR-L6	-12.1	0.80	0.36	160,714
PR	2022.12.12	10:40~13:57	3,155	Fairview Intake	PR-F1	-20.6	0.82	0.30	137,277
				Fairview Intake	PR-F2	-6.0	0.74	0.23	94,978
KR	2023.1.29	18:00~20:02	3,728	Evan Thomas	KR-E1	-15.8	0.41	0.22	50,335
	2023.1.30	14:46~17:59	3,379	Fortress	KR-F1	-11.1	0.55	0.30	92,076
	2023.1.31	7:28~10:39	3,610	Fortress	KR-F2	-13.3	0.67	0.12	44,866



191

192 **Figure 4: Image of the FrazilCam deployed during (a) NSR-L6, and (b) KR-E1. The arrow indicates the flow direction.**

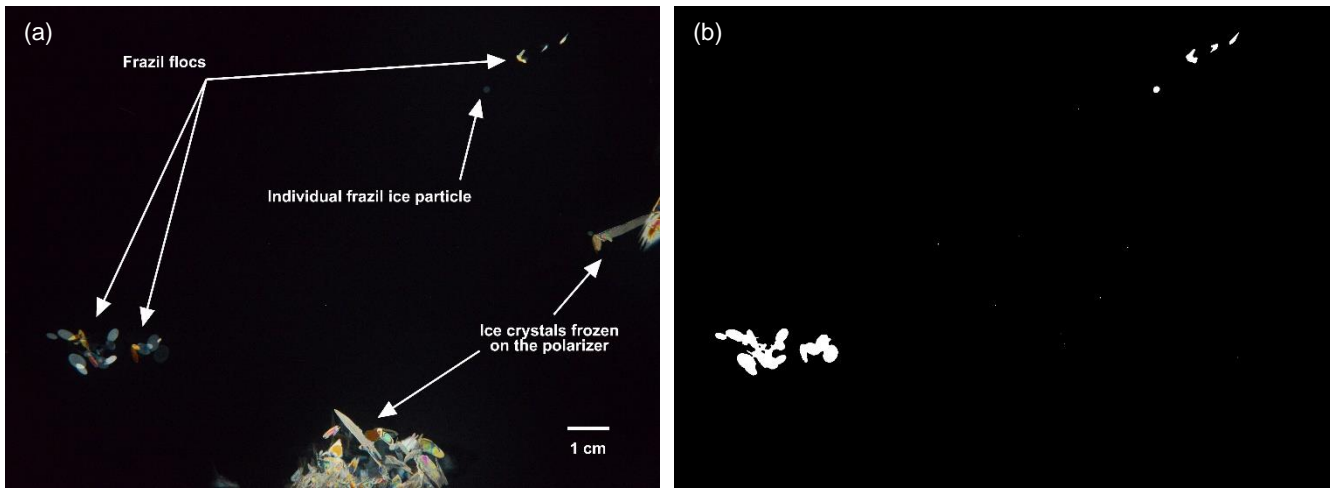
193 **4 Data processing**

194 **4.1 Image processing**

195 Figure 5a shows an example of a raw FrazilCam image with individual frazil ice particles, flocs, and ice crystals frozen on the
196 polarizer. Frazil ice particles are predominantly disk-shaped (McFarlane et al., 2017) and therefore depending on their
197 orientation appear in the images as shapes that vary from a line to a circle with the majority being ellipses. Flocs form through
198 the aggregation of frazil ice particles, resulting in varying shapes depending on the number, shape, and size of attached
199 particles. Ice crystals sometimes attached and froze to the surface of the polarizers despite the periodic hot saline water rinsing.
200 These crystals may appear anywhere in the image, blocking certain regions of the FOV.

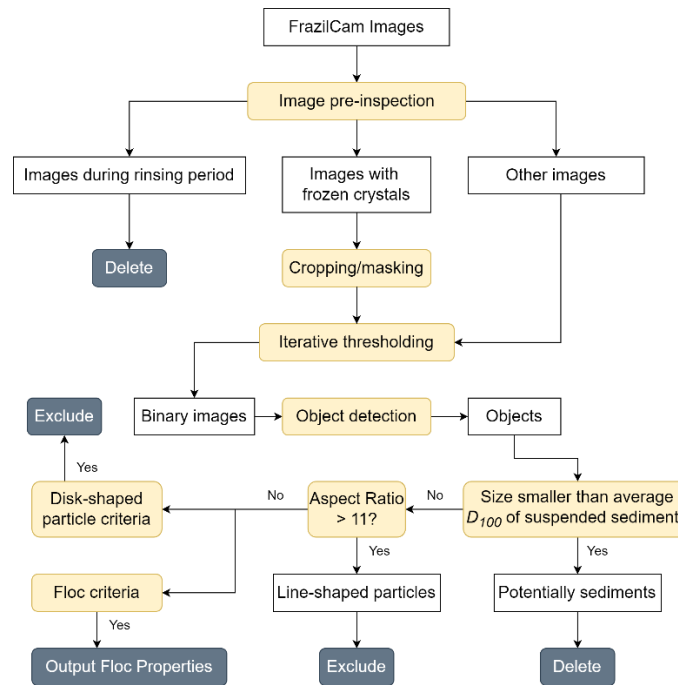
201

202 Figure 6 shows a flow chart of the image processing procedure used for extracting frazil floc properties. For each deployment,
203 images were first manually inspected to exclude those taken when the polarizers were being rinsed, which constitutes 2 ~ 14%
204 of the total images captured. Each image was then processed using an iterative thresholding algorithm developed by McFarlane
205 et al. (2014) to determine the location and extent of each object. Objects intersecting with the image boundary were eliminated,
206 which also removed the ice crystals that were frozen near polarizer edges. For frozen ice crystals that did not intersect with the
207 image boundary, the affected image area was removed either by cropping or masking, or a combination of both (Fig. 6). The
208 corresponding processed binary image is shown in Fig. 5b.



209

210 **Figure 5: An example of (a) a raw FrazilCam image captured on Dec 3, 2021, and (b) the corresponding processed binary image.**



211

212 **Figure 6: A flow chart showing the image processing procedure.**

213

214 The processed binary images were analyzed to compute each object's basic geometric characteristics such as area, perimeter,
 215 centroid, as well as the major and minor axis length of its fitted ellipse. The size S of both frazil particles and flocs was defined
 216 as the major axis length of its fitted ellipse (Clark and Doering, 2009). The objects in the processed images may include small-
 217 suspended sediments that were thin enough to refract light, which may significantly distort the size distribution of frazil ice
 218 particles and flocs (McFarlane et al., 2017; Pei et al., 2022). McFarlane et al. (2019a) used a support vector machine (SVM)

219 to distinguish between ice particles and sediments and compute accurate particle size distributions. However, this method
 220 requires ice-free sediment images at each site for site-specific SVM training, which is not possible for this study due to the
 221 lack of ice-free images at the PR and KR sites. Since this study focuses on flocs, which are considerably larger than particles,
 222 a simple cut-off criterion was used to minimize the effect of sediment particles in the images. Objects smaller than the average
 223 D_{100} of suspended sediment (see Table 1) in a given study reach were removed from the dataset (Fig. 6). For the KR, since no
 224 suspended sediment size distribution measurements were available in the literature, the cut-off size was determined to be 0.27
 225 mm, which is twice the average of seven mean sediment size measurements estimated from FrazilCam images by McFarlane
 226 et al. (2019b).

227

228 For each object, the following geometric parameters were used to classify the objects into either flocs or particles: the ratio of
 229 the object area to that of the fitted ellipse a/a_e , the absolute percentage difference between the object perimeter and its fitted
 230 ellipse perimeter $P_{diff\%}$, the ratio of an object's fitted ellipse area to its ellipse perimeter divided by the ratio of the object's
 231 actual area to its perimeter $(\frac{a_e}{P_e})/(\frac{a}{P})$ (McFarlane et al., 2014; Schneck, 2018). Preliminary experiments found that flocs formed
 232 by a very small particle attaching to a significantly larger particle remain approximately elliptical since the boundary does not
 233 change significantly. As a result, comparing changes in overall area/perimeter with the fitted ellipse did not help with
 234 classification. Therefore, the form index was introduced to assess minor changes in object shape (Masad et al., 2001; Al-
 235 Rousan et al., 2007). The form index is calculated using the following equation:

$$236 \quad FI = \sum_{\theta=0}^{\theta=360-\Delta\theta} \frac{|R_{\theta+\Delta\theta}-R_{\theta}|}{R_{\theta}}, \quad (1)$$

237 where θ is the directional angle and R is the radial length between the centroid of the particle and the boundary of the particle.
 238 The incremental change in angle $\Delta\theta$ is set to 2.81 °, dividing the particle boundary into 128 segments to factor in minor
 239 boundary changes. A perfectly circular object has an FI of 0, and FI will increase as an object's boundary becomes more
 240 irregular.

241

242 A total of 568 objects were manually labelled as either flocs (109) or disk-shaped frazil particles (459) to construct a test
 243 dataset to determine the optimal classification criteria of the aforementioned parameters. Results showed that
 244 $\{a/a_e \geq 0.9 \text{ and } P_{diff\%} \leq 0.1 \text{ and } S \leq 6\}$ for disk-shaped particles, and $\{(a/a_e < 0.9 \text{ or } P_{diff\%} > 0.15) \text{ and } (\frac{a_e}{P_e})/(\frac{a}{P}) >$
 245 $1.1 \text{ and } FI \geq 6\}$ for flocs provided the optimum classification accuracy of 97.0% and 92.7% for particles and flocs,
 246 respectively. In NSR-L4 the camera lens was slightly out of focus due to an accidental jarring of the camera during deployment.
 247 However, because this was the only deployment that captured a complete principal supercooling event, additional processing
 248 was performed on these images to allow for their inclusion in the dataset. Visual examination and analysis of these images
 249 indicated that the blurriness predominantly affected the boundary clarity of dim objects with a mean pixel intensity less than

250 24 and did not significantly affect brighter objects. Therefore, an additional criterion was introduced for NSR-L4 eliminating
 251 flocs with a mean pixel intensity less than 24. The rate of floc detection in the blurry images from deployment NSR-L4 was
 252 4.1 flocs per minute and it was 4.4 flocs per minute in NSR-L5 which occurred immediately afterwards. Therefore, the
 253 additional criterion, applied to the blurry images, only slightly reduced the number of flocs detected.

254

255 In order to prevent line-shaped frazil ice particles from being misidentified as flocs, frazil particles in the shape of a line were
 256 first identified if the aspect ratio of the object (i.e., the ratio between the major and minor axis length) was greater than 11
 257 based on minimum frazil ice particle aspect ratio measurements made by McFarlane et al. (2014) as shown in Fig. 6. Then the
 258 classification criteria mentioned above were applied to the remaining objects to identify disk-shaped particles and flocs (Fig.
 259 6). After classification, the number of flocs N_f , mean floc size $\overline{\mu_f}$, standard deviation σ_f , 95th percentile of floc size S_{95} ,
 260 maximum floc size S_{fmax} , average floc number concentration $\overline{C_{fn}}$, and average volumetric concentration $\overline{C_{fv}}$ for each
 261 deployment were computed. It is worth noting that the properties of frazil ice particles were not included in this study since
 262 the cut-off size likely eliminated up to 50% of the particle population which would significantly skew the data. In addition, the
 263 mean floc size μ_f , floc number concentration C_{fn} , floc volumetric concentration C_{fv} were computed for each image throughout
 264 a deployment, and a moving average over a period of 35 images was applied to the resulting time series to smooth the data.
 265 Note that the 35-image moving average was computed only if two or more non-zero values occurred in the window, if there
 266 were less than two non-zero values no average value was recorded. This created gaps in the moving average time series and
 267 the rationale for this is that two or more samples are required to compute a valid average value. The measuring volume used
 268 for the concentration calculations was the image FOV times the gap distance between the two polarizers. The volume of a
 269 frazil floc was assumed to be the volume of an ellipsoid with semi-axis lengths a , b , and c where a and b were equal to the
 270 semi-major and semi-minor axis lengths of the floc's fitted ellipse, and c was equal to the average of a and b but no larger than
 271 the gap between the two polarizing filters. The volume of ice in a frazil floc V_f was estimated as:

$$272 \quad V_f = \frac{4}{3} \pi abc(1 - \eta), \quad (2)$$

273 where η is the porosity of floc taken to be 0.8 (Schneck et al., 2019).

274 **4.2 Heat flux analysis at the water surface**

275 The net heat flux Q_n at the river surface is given by:

$$276 \quad Q_n = Q_{sw} + Q_{lw} + Q_E + Q_H, \quad (3)$$

277 where Q_{sw} is the net shortwave radiation; Q_{lw} is the net longwave radiation; Q_E is the latent heat flux; Q_H is the sensible heat
 278 flux. A positive sign denotes heat loss from the surface. Q_{sw} was calculated as:

$$279 \quad Q_{sw} = -(1 - \alpha_{ws})Q_s, \quad (4)$$

280 where Q_s is the measured incoming solar radiation; α_{ws} is the albedo of water surface to solar radiation, taken to be 0.15 for
 281 this study following Howley (2021). The net longwave radiation Q_{lw} was calculated as:

$$282 \quad Q_{lw} = Q_{lw}^{out} - (1 - \alpha_{wl})Q_{lw}^{in}, \quad (5)$$

$$283 \quad Q_{lw}^{out} = \varepsilon_w \sigma_{sb} T_{wk}^4, \quad (6)$$

284 where Q_{lw}^{out} is the outgoing longwave radiation emitted from the water; α_{wl} is the albedo of water surface to longwave
 285 radiation, taken as 0.03 (Raphael, 1962); ε_w is the emissivity of water taken as 0.97 (Ashton, 2013); σ_{sb} is the Stefan-
 286 Boltzmann constant ($5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$); T_{wk} is the water surface temperature in K. Note that it was assumed that the water
 287 column was completely mixed and therefore the water temperatures that were measured at the top of the FrazilCam frame (i.e.,
 288 not at the water surface) were used in Eq. (6). Q_{lw}^{in} is the incoming longwave radiation which was measured by a net radiometer
 289 for the NSR. For KR and PR, Q_{lw}^{in} is estimated using the following equations:

$$290 \quad Q_{lw_c}^{in} = \varepsilon_{ac} \sigma_{sb} T_{ak}^4, \quad (7)$$

$$291 \quad \varepsilon_{ac} = 1.08[1 - \exp(-e_a^{T_{ak}/2016})], \quad (8)$$

$$292 \quad e_s = 6.11 \exp\left(\frac{17.62T_a}{243.12 + T_a}\right), \quad (9)$$

$$293 \quad e_a = RH \times e_s, \quad (10)$$

$$294 \quad Q_{lw}^{in} = Q_{lw_c}^{in}(1 - N^4) + 0.952N^4 \sigma_{sb} T_{ak}^4, \quad (11)$$

295 where $Q_{lw_c}^{in}$ is the incoming longwave radiation under the clear sky; ε_{ac} is the clear sky atmospheric emissivity calculated
 296 using Eq. (8) by Satterlund (1979); T_{ak} is the air temperature in K; e_s and e_a are the saturated and actual vapour pressure of
 297 water, respectively; RH is the relative humidity; T_a is the air temperature in degree Celsius; N is the fractional cloud cover.
 298 Note that Eq. (11) was developed by Konzelmann et al. (1994).

299

300 Q_E was calculated using the equation suggested by Ryan et al. (1974) following Yang et al. (2023):

$$301 \quad Q_E = \left[2.70 \left(\frac{T_{wk}}{1 - 0.378(e_s/P)} - \frac{T_{ak}}{1 - 0.378(e_a/P)} \right)^{\frac{1}{3}} + 3.2V \right] (e_s - e_a), \quad (12)$$

302 where P is the atmospheric pressure; V is the wind speed. Q_H was calculated from Q_E using Bowen's ratio B as follows:

$$303 \quad B = \frac{c_a P}{0.622 t_v} \times \frac{T_s - T_a}{e_s - e_a}, \quad (13)$$

$$304 \quad Q_H = B Q_E, \quad (14)$$

305 where C_a is the specific heat of air; l_v is the latent heat of vaporization; T_s is the surface water temperature. In a previous study,
306 Yang et al. (2023) investigated various formulas used to calculate incoming longwave radiation and the latent and sensible
307 heat fluxes during freeze-up on the North Saskatchewan River in Alberta, and the combination of formulas (Eqs. 7~14) used
308 in this study were the ones that provided the most accurate results in Yang et al (2023). It is also worth noting that only hourly
309 meteorological data were available for the KR and PR regions as described in Sec. 3. As a result, the heat fluxes were calculated
310 on a 1-hour time interval for the KR and PR deployments, and for all the NSR deployments the heat fluxes were calculated on
311 a 10-min time interval.

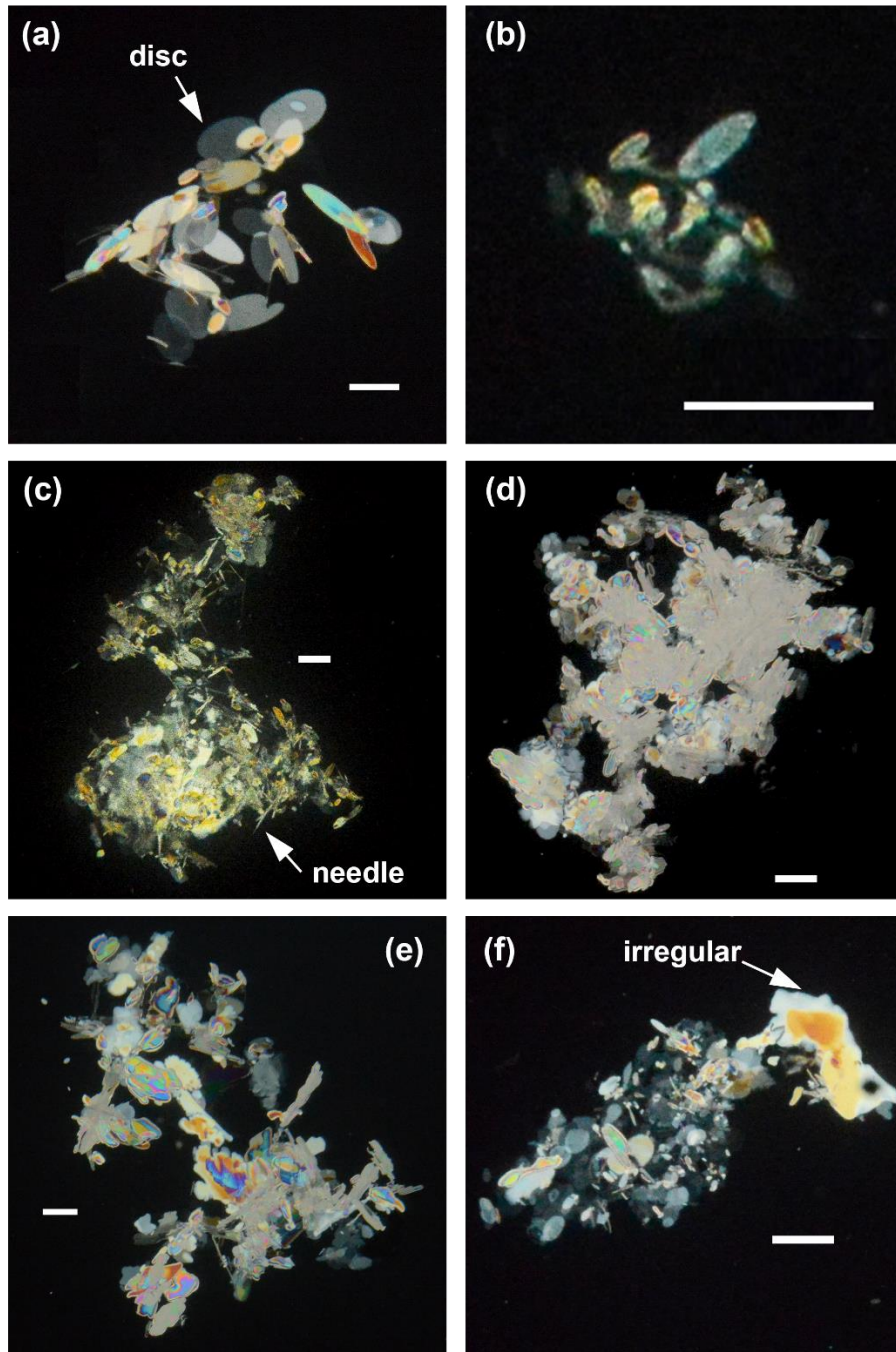
312 **5 Results**

313 **5.1 Floc shape, size and concentration**

314 In Fig. 7 images of typical shapes of frazil flocs observed during the different field deployments are presented. Flocs from
315 NSR deployments (Figs. 7a~b) were comprised predominantly of disc-shaped frazil ice particles of varying sizes frozen
316 together. The floc shown in Fig. 7b is representative of flocs observed during deployments NSR-L3 and NSR-L6. As can be
317 seen, it was comprised of much smaller individual particles than the flocs observed during the rest of the NSR deployments
318 (Fig. 7a). Flocs from deployment PR-F1 (Fig. 7c) were comprised of disc-shaped particles, irregular particles, and some needle-
319 shaped particles. Flocs from deployment KR-E1 (Fig. 7d) were formed primarily by densely aggregated irregular particles and
320 some small disc-shaped particles. Flocs from deployments PR-F2, KR-F1 (Fig. 7e), and KR-F2 (Fig. 7f) were mostly
321 comprised of disc-shaped and irregular particles, images of flocs from PR-F2 were not shown since they are similar to those
322 shown in Figs. 7e-f.

323

324 Table 4 presents the number of flocs N_T , mean size $\overline{\mu}_f$, standard deviation σ_f , 95th percentile and maximum of the floc size S_f ,
325 average floc number concentration \overline{C}_{fn} , and average volumetric concentration \overline{C}_{fv} for each deployment. The supercooling
326 phase, the minimum water temperature T_p , and average net surface heat flux \overline{Q}_n are also presented. Deployments NSR-L1,
327 NSR-L3, and NSR-L4 captured the principal supercooling phase (Principal), while the rest captured only the residual
328 supercooling phase (Residual). T_p ranged from -0.021 °C to -0.031 °C for Principal deployments, and from -0.007 °C to -
329 0.017 °C for Residual deployments. In all deployments \overline{Q}_n was positive indicating an overall heat loss. N_T varied significantly
330 ranging from 442 to 187,288 with the largest N_T of 187,288 occurring during deployment KR-E1. The mean floc size $\overline{\mu}_f$
331 ranged from 1.19 to 5.64 mm with an overall average of 3.8 mm and σ_f ranged from 0.88 to 5.03 mm. S_{f95} was greater than
332 ~8 mm except for deployments NSR-L3 and NSR-L6 with values of 4.44 mm and 2.47 mm, respectively. The largest value of
333 S_{fmax} , 99.69 mm, was observed during KR-E1 which also had the largest number of flocs. The average floc number
334 concentration \overline{C}_{fn} varied by three orders of magnitude from 1.80×10^{-4} to $1.15 \times 10^{-1} \text{ cm}^{-3}$, and the average floc volumetric
335 concentration \overline{C}_{fv} over four orders of magnitude from 2.05×10^{-7} to 4.56×10^{-3} .



336

337 **Figure 7: Images of frazil flocs of different sizes and shapes from the following deployments: (a) NSR-L1, (b) NSR-L6, (c) PR-F1,**
 338 **(d) KR-E1, (e) KR-F1, and (f) KR-F2. The white scale bar in each image represents a length of 3 mm. Note that in some images the**
 339 **surrounding ice particles were masked out to highlight the floc at the centre of the image.**

340 **Table 4: Supercooling phase, minimum water temperature T_p , mean net surface heat flux $\overline{Q_n}$, number of flocs N_T , mean floc size**
341 **$\overline{\mu_f}$, standard deviation σ_f , 95th percentile of floc size S_{f95} , maximum floc size S_{fmax} , average floc number concentration $\overline{C_{fn}}$, and**
342 **average volumetric concentration $\overline{C_{fv}}$ for each deployment.**

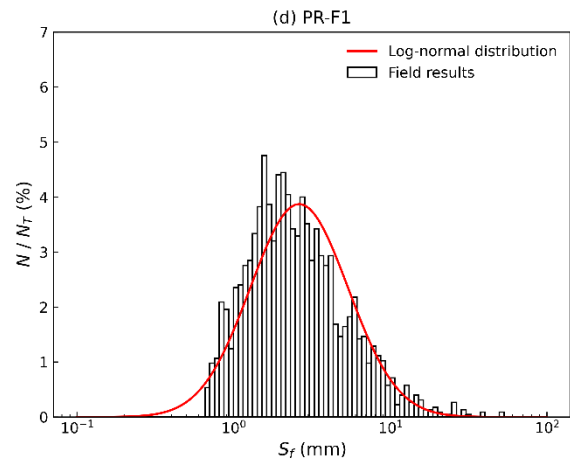
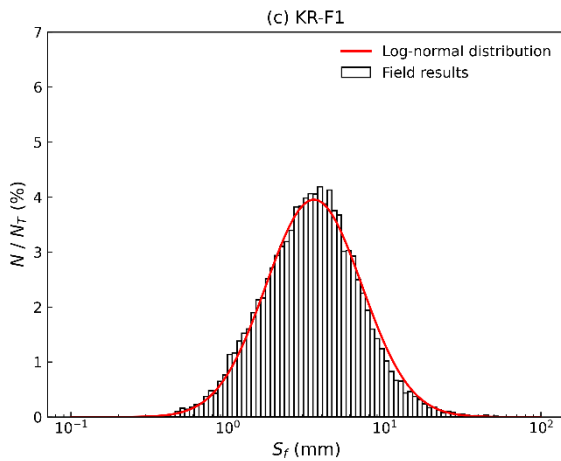
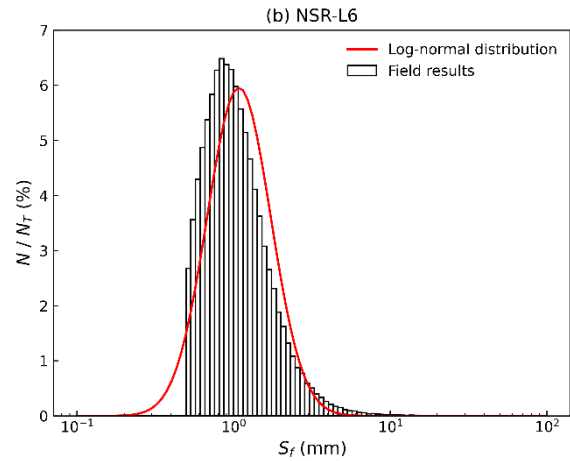
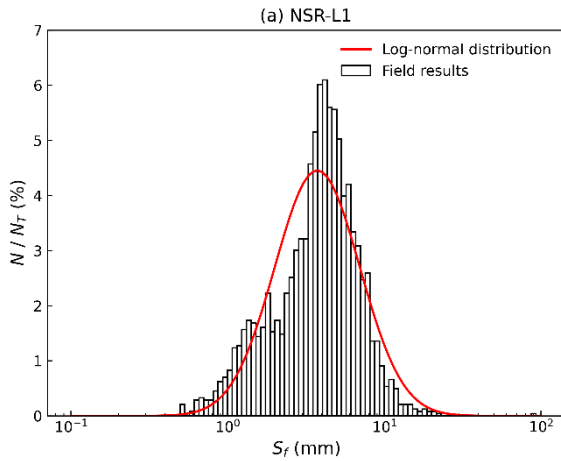
Deployment No.	Supercooling phase	T_p (°C)	$\overline{Q_n}$ (W m ⁻²)	N_T	$\overline{\mu_f}$ (mm)	σ_f (mm)	S_{f95} (mm)	S_{fmax} (mm)	$\overline{C_{fn}}$ (cm ⁻³)	$\overline{C_{fv}}$ (cm ³ cm ⁻³)
NSR-L1	Principal	-0.021	183.3	2,428	4.33	3.08	8.73	89.58	9.65×10 ⁻⁴	1.39×10 ⁻⁵
NSR-L2	Residual	-0.009	199.5	879	3.70	2.31	7.54	24.05	2.72×10 ⁻⁴	1.39×10 ⁻⁶
NSR-L3	Principal	-0.023	95.4	839	1.87	1.31	4.44	9.02	3.06×10 ⁻⁴	2.05×10 ⁻⁷
NSR-L4	Principal	-0.031	110.3	442	4.50	2.45	8.37	18.53	1.80×10 ⁻⁴	1.21×10 ⁻⁶
NSR-L5	Residual	-0.016	121.8	631	3.50	2.57	8.40	14.31	2.60×10 ⁻⁴	1.19×10 ⁻⁶
NSR-L6	Residual	-0.017	157.5	143,097	1.19	0.88	2.47	47.16	6.75×10 ⁻²	2.99×10 ⁻⁵
PR-F1	Residual	-0.009	318.8	2,250	3.43	3.72	9.16	53.35	1.11×10 ⁻³	1.84×10 ⁻⁵
PR-F2	Residual	-0.007	107.4	1,247	4.25	5.03	13.60	53.81	5.63×10 ⁻⁴	1.68×10 ⁻⁵
KR-E1	Residual	-0.008	243.3	187,288	5.64	4.79	14.28	99.69	1.15×10 ⁻¹	4.56×10 ⁻³
KR-F1	Residual	-0.010	122.4	23,670	4.43	3.86	10.69	81.38	1.05×10 ⁻²	2.32×10 ⁻⁴
KR-F2	Residual	-0.011	275.2	15,151	4.69	4.08	11.89	68.37	6.62×10 ⁻³	1.59×10 ⁻⁴

343

344 5.2 Floc size distribution

345 In Fig. 8, plots of the frazil floc size distribution as well as fitted lognormal distribution curves for four deployments are
346 presented. All of the size distributions obtained from NSR deployments closely resemble deployment NSR-L1 shown in Fig.
347 8a, except for deployment NSR-L6 shown in Fig. 8b. Size distributions from the KR and PR are well represented by
348 deployments KR-F1 and PR-F1 which are shown in Fig. 8c and Fig. 8d, respectively. It can be seen from Fig. 8 that a theoretical
349 lognormal distribution is a reasonable fit to all of the size distributions but a particularly good fit for deployment KR-F1. This
350 may be attributed to the order-of-magnitude larger sample size for KR-F1 (23,670) compared to NSR-L1 (2,428) and PR-F1
351 (2,250). The size distribution for NSR-L6 shown in Fig. 8b has the most flocs of the four deployments plotted with a sample
352 size of 143, 097 but it does not fit a lognormal distribution as closely as the others. This is because the distribution was cut off
353 at 0.5 mm to eliminate sediment particles. A similar condition can also be observed for PR-F1 shown in Fig. 8d where the cut-
354 off was 0.68 mm. Note that the cut-offs were applied to all size distributions but only impacted the distribution significantly if
355 there were a significant number of smaller flocs detected.

356



357

358

359 **Figure 8. Distributions of floc size S_f for deployments (a) NSR-L1, (b) NSR-L6, (c) KR-F1, and (d) PR-F1. The red line denotes a**
 360 **fitted lognormal distribution, N is the number of flocs in each bin, and N_T is the total number of flocs.**

361 **5.3 Time series**

362 Time series plots of water and air temperatures T_w and T_a , heat flux Q , floc mean size μ_f , floc number concentration C_{fn} , and
 363 floc volumetric concentration C_{fv} for deployments NSR-L4, KR-F1, and PR-F2 are presented in Figs. 9, 10 and 11,
 364 respectively (Note that similar time series plots for the other eight deployments are presented as Figs. S1-S8 in the Supplement).
 365 Deployment NSR-L4 occurred during the principal supercooling phase and is the only deployment that captured the entire
 366 principal supercooling phase, while KR-F1 and PR-F2 captured the middle and end of the residual supercooling phase,
 367 respectively.

368

369 During NSR-L4 (Fig. 9a) supercooling started at 15:25 and after that T_w decreased almost linearly at a cooling rate of -0.0009
370 $^{\circ}\text{C min}^{-1}$, reached a T_p of -0.031 $^{\circ}\text{C}$ (i.e., peak supercooling) at 16:02 and then started to increase and reached a stable residual
371 temperature of -0.010 $^{\circ}\text{C}$ at 16:37. T_a decreased from -1.7 to -7.2 $^{\circ}\text{C}$ with an average of -4.6 $^{\circ}\text{C}$. Figure 9b shows that the net
372 heat flux Q_n increased from 26 W m^{-2} to 150 W m^{-2} primarily due to the decrease in the magnitude of shortwave radiation
373 Q_{sw} . The rest of the heat flux components remained positive (heat loss) and relatively stable throughout the deployment, with
374 Q_{lw} being the dominant component. In Fig. 9c μ_f began increasing significantly ~ 7 minutes before the peak supercooling
375 temperature was reached, reaching a maximum of 7.8 mm ~ 37 minutes after peak supercooling, then it decreased to ~ 6 mm
376 and remained approximately constant afterwards. Figure 9d shows that significant numbers of frazil particles were detected
377 ~ 15 minutes before peak supercooling with C_{fn} values below 2×10^{-4} cm^{-3} . At ~ 2 minutes before peak supercooling C_{fn}
378 increased rapidly and peaked ~ 30 minutes after peak supercooling at a value of 9.3×10^{-4} cm^{-3} and then decreased to 2×10^{-4}
379 cm^{-3} at the end of the deployment. Figure 9e shows that C_{fv} only increased notably after peak supercooling and reached a value
380 of 8.8×10^{-6} ~ 30 minutes after the peak supercooling. After that it decreased before spiking to 1.6×10^{-5} ~ 38 minutes after the
381 peak supercooling and then decreased to 1.7×10^{-6} at the end. An examination of the images showed that the spike was caused
382 by several large flocs up to 18.5 mm in size.

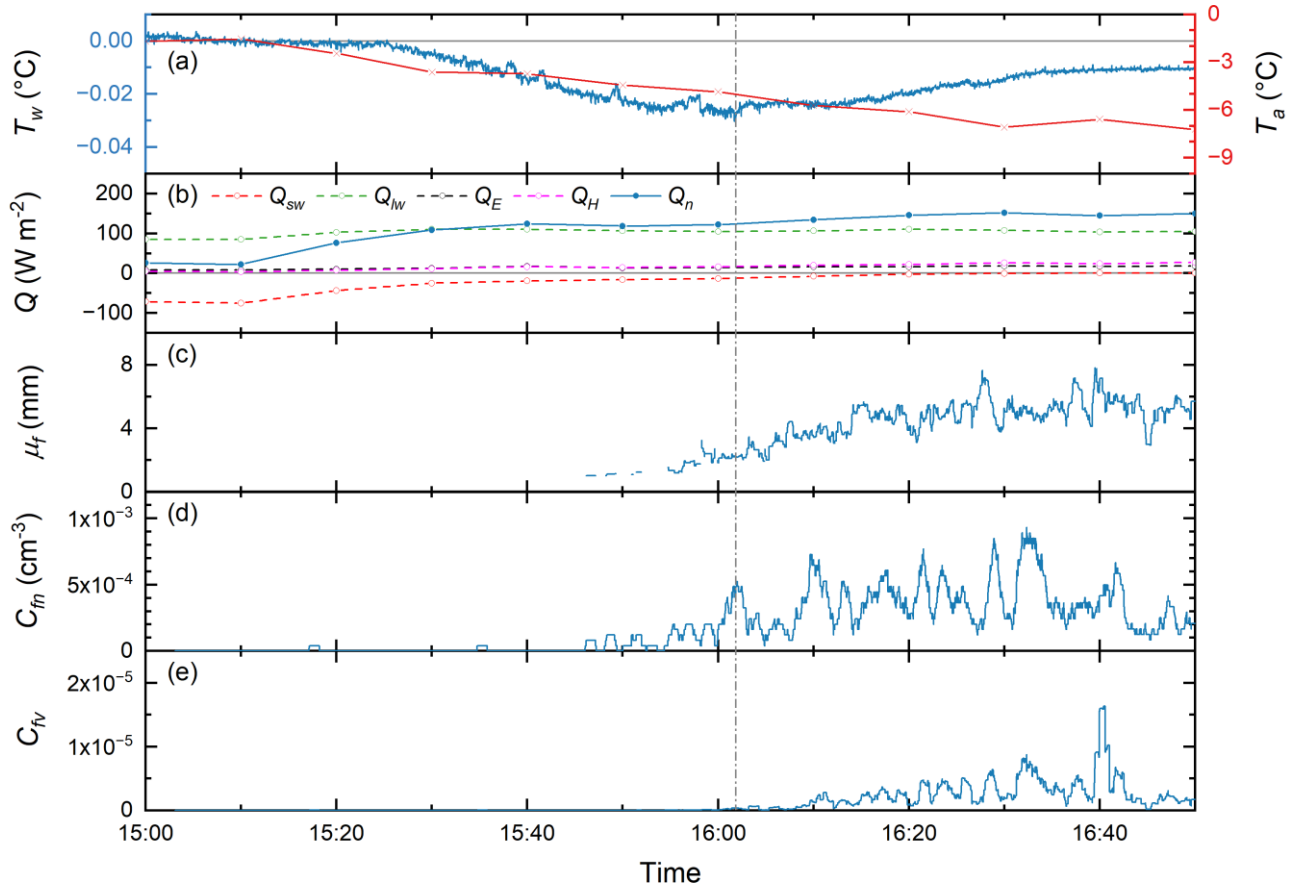
383

384 During KR-F1, T_w fluctuating continuously around -0.008 $^{\circ}\text{C}$, except for one anomalous spike that occurred at 17:03 (Fig.
385 10a), which was caused by ice contacting the sensor when the polarizers were being rinsed. Additionally, periodic upward
386 spikes with a period of 1 minute and magnitude of ~ 0.001 $^{\circ}\text{C}$ were visible on the plot. While the cause of these spikes remains
387 uncertain, it is worth noting that their magnitude falls within the range of accuracy of the sensor. The air temperature was
388 relatively stable with T_a varying between -10 to -12 $^{\circ}\text{C}$. In Fig. 10b, Q_n rose during the deployment from -2 W m^{-2} to 261 W
389 m^{-2} largely due to the decrease in the magnitude of Q_{sw} . Note that the heat flux components here were computed on a 1-hour
390 time interval. In Figs. 10c-e, there are gaps in the data during these time periods 15:33 \sim 15:38, 16:17 \sim 16:23, 16:58 \sim 17:04,
391 and 17:34 \sim 17:39, that are visible as short time series segments with zero slope. These were created when the images collected
392 during the time periods when the polarizers were being rinsed were removed from the dataset. In Fig. 10c, μ_f fluctuated around
393 ~ 4 mm before significantly increasing at 17:40, eventually reaching 5.9 mm by the end of the deployment. Similar trends are
394 evident in Figs. 10d-e for C_{fn} and C_{fv} , respectively. At 17:41 C_{fn} started to increase significantly and reached a peak value of
395 4.5×10^{-2} cm^{-3} at 17:53 while C_{fv} started to increase significantly at 17:50 and eventually peaked at a value of 2.8×10^{-3} . A
396 hydropeaking wave arrived at the Fortress site at 17:25 increasing the depth by 19% by the end of the deployment and causing
397 rapid increases in floc size and concentration.

398

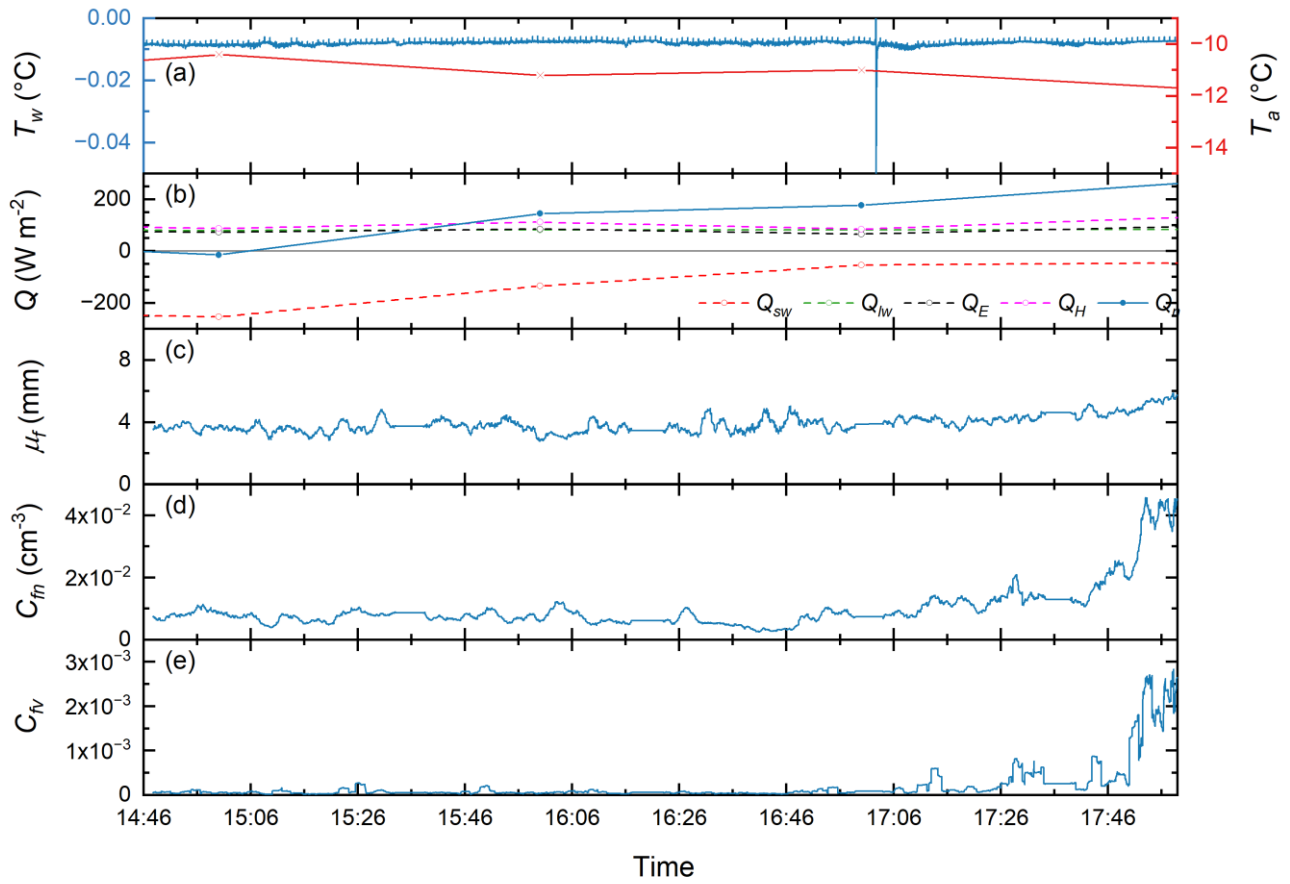
399 During deployment PR-F2, T_w was initially at -0.006 $^{\circ}\text{C}$ but then increased above zero at 10:21, and eventually reached 0.033
400 $^{\circ}\text{C}$ at the end of the deployment (Fig. 11a). T_a followed a similar trend to T_w rising from -7.6 to -4.1 $^{\circ}\text{C}$. The net heat loss Q_n
401 steadily decreased from 165 W m^{-2} to 12 W m^{-2} (Fig. 11b) due to an increase in the magnitude of Q_{sw} . In Fig. 11c μ_f fluctuated

402 between 1 mm and 10 mm during the deployment with an average of 4 mm. In Figs. 11d-e the time series of number and
 403 volume concentrations did not exhibit significant trends. C_{fn} ranged from $4.1 \times 10^{-5} \text{ cm}^{-3}$ to $2.4 \times 10^{-3} \text{ cm}^{-3}$ with an average of
 404 $5.6 \times 10^{-4} \text{ cm}^{-3}$ while C_{fv} was negligible most of the time with occasional spikes up to 4.2×10^{-4} . One spike that occurred at
 405 10:39 caused both C_{fn} and C_{fv} to reach their peak values. Visual examination of the images shows that at this time the number
 406 of flocs increased significantly for three consecutive images and this was possibly caused by a large floc colliding with the
 407 camera frame and fracturing.



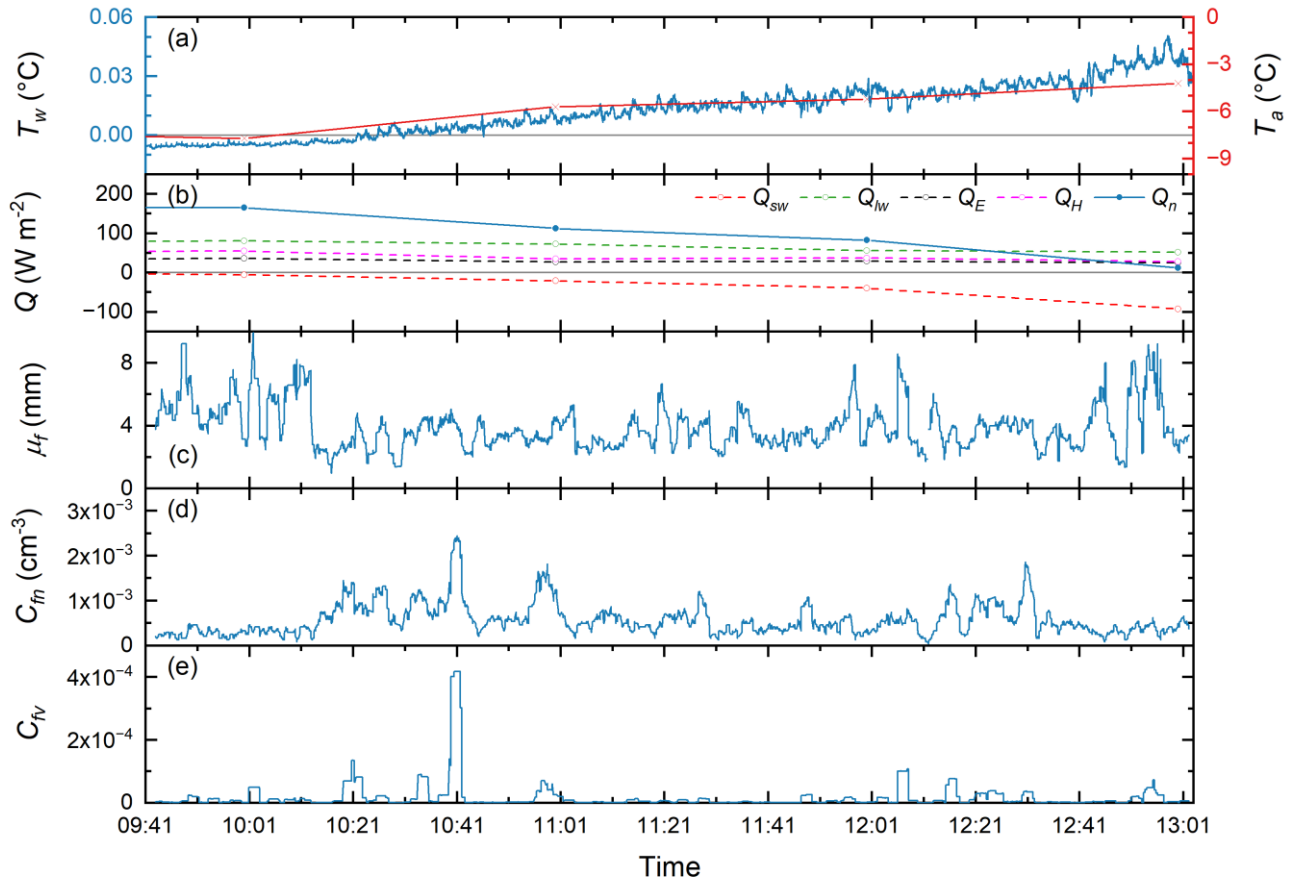
408
 409 **Figure 9.** Time series of (a) water and air temperatures T_w and T_a , (b) heat flux Q , (c) floc mean size μ_f , (d) floc number
 410 concentration C_{fn} and (e) floc volumetric concentration C_{fv} for deployment NSR-L4 on December 12, 2021. The vertical dashed
 411 grey line indicates the time when the peak supercooling temperature is achieved.

412



413

414 **Figure 10. Time series of (a) water and air temperatures T_w and T_a , (b) heat flux Q , (c) floc mean size μ_f , (d) floc number**
 415 **concentration C_{fn} and (e) floc volumetric concentration C_{fv} for deployment KR-F1 on January 30, 2023.**



416

417 **Figure 11. Time series of (a) water and air temperatures T_w and T_a , (b) heat flux Q , (c) floc mean size μ_f , (d) floc number**
 418 **concentration C_{fn} and (e) floc volumetric concentration C_{fv} for deployment PR-F2 on December 13, 2022.**

419 **6 Discussion**

420 Images of typical frazil flocs shown in Fig. 7 illustrate the complexity of their morphology, which encompasses various ice
 421 crystal shapes, including disc-shaped, needle-shaped, and irregular particles. Disc-shaped ice particles were observed in flocs
 422 from all three rivers but were most pronounced in the NSR where flocs were almost all formed by disc-shaped particles of
 423 different sizes (Figs. 7a–b). The growth of frazil ice in supercooled water is limited by the diffusive removal of the latent heat
 424 of solidification from the ice-water interface and by the slow attachment kinetics in the perpendicular direction, which leads
 425 to the formation of disc-shaped particles (Mullins and Serkerka, 1964; Rees Jones and Wells, 2015). Flocs containing needle-
 426 shaped crystals as shown in Fig. 7c were observed during deployment PR-F1 which had a very low mean air temperature of -
 427 20.64 °C. These types of crystals have been found to form primarily at the surface of supercooled water (Hallett, 1959; Clark
 428 and Doering, 2002). The cold air temperature during deployment PR-F1 may have promoted the growth of these needle-shaped

429 particles at the water surface before they were entrained in the water column and subsequently attached to flocs. Irregular
430 particles were observed in flocs from both the KR and PR, most pronouncedly in deployment KR-E1 as shown in Fig. 7d.
431 Irregularly shaped particles are formed by unstable disk growth which is known to be caused by the formation of temperature
432 gradients in the water surrounding the particles (Kallungal and Barduhn, 1977). This suggests that during the KR and PR
433 deployments, frazil ice particles probably spent some time in relatively quiescent water where the turbulence intensity was so
434 low that temperature gradients could form in the water surrounding the particles. Another possibility is that the particles were
435 temporarily transported to the river surface exposing them to cold air, which may also lead to unstable disk growth. In addition,
436 broken fragments of skim ice or border ice that were entrained into the water column are another possible source of irregular
437 particles in flocs. Clark and Doering (2009) observed in the laboratory that flocs could become denser over time when the
438 turbulence intensity was higher. During deployment KR-E1, although the locally measured depth-averaged velocity near the
439 FrazilCam was relatively low at 0.22 m s^{-1} , the water velocity $\sim 70 \text{ m}$ upstream of the deployment site was visually observed
440 to be very turbulent due to the presence of four groins and a narrow channel width. Therefore, this may have contributed to
441 the denser flocs that were observed during this deployment.

442

443 The data presented in Table 4 and Fig. 8 are the first quantitative measurements of frazil floc sizes and concentrations in rivers.
444 The mean floc size averaged over all deployments was 3.80 mm, which was close to the mean values observed for most of the
445 individual deployments except for deployments NSR-L3, NSR-L6, and KR-E1 which had mean floc sizes of 1.87, 1.19, and
446 5.64 mm, respectively. As noted in Sec. 5.1, flocs observed during deployments NSR-L3 and NSR-L6 were comprised of
447 much smaller disc-shaped individual particles (Fig. 7b) than the rest of the deployments (Fig. 7a). Deployment NSR-L3 took
448 place during a principal supercooling event in which the observed small frazil ice particles were likely newly formed and still
449 growing, which could be the reason why the flocs were smaller and comprised of significantly smaller particles. In addition,
450 deployment NSR-L3 took place as the crest of a hydropeaking wave was passing the site that resulted in a mean water depth
451 of 1.24 m which is 37% to 55% larger than the depths during the other NSR deployments (Table 3). The significantly higher
452 water depth reduced the fractional height where the images were collected, which could also result in smaller floc sizes. This
453 would be consistent with measurements by Reimnitz et al. (1993) that showed that larger flocs have higher rise velocities.
454 Deployment NSR-L6 occurred during the 2022 freeze-up season, which was the shortest freeze-up in ~ 10 years lasting only
455 three days. Significantly smaller flocs were observed during this deployment (see Fig. 7b) and this may be because smaller
456 relatively young flocs were generated during this rapid freeze-up process. The largest mean floc size, maximum floc size and
457 largest concentration (see Table 4) were observed during deployment KR-E1 (Fig. 7d). As discussed previously the particles
458 that formed flocs during KR-E1 included irregularly shaped particles and this could have resulted in larger flocs compared to
459 flocs formed entirely by disc-shaped particles.

460

461 The mean floc size and standard deviation ranged from 1.19 to 5.64 mm, and 0.88 to 5.03 mm, respectively as shown in Table
462 4. The 95th percentile of floc size ranged from 2.47 to 14.28 mm, and the largest flocs found was 99.69 mm in size. Schneck

463 et al. (2019) conducted laboratory experiments in a frazil ice tank with an average turbulent dissipation rate of $0.034 \text{ m}^2 \text{ s}^{-3}$
464 which falls within the range of the values estimated in the three rivers in this study ($0.005 \sim 0.207 \text{ m}^2 \text{ s}^{-3}$). They found that in
465 freshwater the size distribution of flocs followed a lognormal distribution and the mean size, 95th percentile of floc size, and
466 maximum size were 2.57 mm, 6.91 mm, and 95.1 mm, respectively. The mean and 95th percentile sizes fall within the range
467 of the values observed in this study. However, the overall mean floc size observed in the field was 3.80 mm, which is 48%
468 larger than the mean measured in the laboratory. The maximum floc sizes observed in the laboratory and field are comparable.
469 It is worth noting that the largest floc size of 99.69 mm was just slightly smaller than the FOV dimensions and considerably
470 larger than the 3.6 cm gap, indicating that the floc size measurements may have been physically limited by the FOV and the
471 gap between the polarizers. Therefore, further increases in both the FOV and the gap between the polarizers may be needed in
472 future studies to allow even larger flocs to be imaged and measured.

473

474 The size distributions obtained from different rivers are all a reasonable visual fit to a lognormal distribution as shown in Fig.
475 8, which is consistent with the laboratory measurements (Schneck et al., 2019). However, when the Chi-square test for
476 goodness-of-fit was applied none of the size distributions were quantitatively confirmed to fit a lognormal distribution at the
477 5% significance level. This could be primarily due to the use of the cut-off size to eliminate sediment particles which produced
478 a sharp cut-off in the distributions. In addition, the small number of samples in some deployments resulted in noisy size
479 distributions making it unlikely that they would be a good quantitative fit to a smooth lognormal distribution. Nonetheless, the
480 good qualitative comparison of the floc size distributions measured in the field with theoretical lognormal distributions in Fig.
481 8 does suggest that if the sample size was larger and sediment particles could be filtered out that floc size distributions in rivers
482 would also closely follow a lognormal distribution.

483

484 The average floc number concentration $\overline{C_{fn}}$ ranged from 1.80×10^{-4} to $1.15 \times 10^{-1} \text{ cm}^{-3}$ (Table 4), Schneck et al. (2019)
485 measured a peak floc number concentration of $2.5 \times 10^{-1} \text{ cm}^{-3}$ in freshwater laboratory experiments, which is similar in
486 magnitude to the upper limit of values measured in the field. The average floc volumetric concentration $\overline{C_{fv}}$ ranged from 2.05
487 $\times 10^{-7}$ to 4.56×10^{-3} (Table 4). Previous studies reported suspended ice volumetric concentrations ranged from 2×10^{-6} to $6 \times$
488 10^{-3} (Tsang, 1984; Marko and Jasek, 2010; Richard et al., 2011). These measurements were made using comparative resistance
489 probes and acoustic devices which in theory detect all of the ice suspended in the water. The upper range of previous
490 concentration measurements is comparable to that reported in this study. However, the lower range is one order of magnitude
491 larger than this study, which may be due to the fact that the previous studies reported the total volume of frazil flocs and
492 particles.

493

494 The time series of frazil floc properties in Fig. 9 indicate that during the principal supercooling phase, floc number and mean
495 size started to increase significantly just prior to peak supercooling and reached a maximum near the end of principal
496 supercooling, the floc volumetric concentration only started to increase significantly after peak supercooling occurred.

497 Deployment NSR-L3 that captured almost the entire principal supercooling phase also showed a similar trend (see Fig. S3 in
498 the Supplement). The increasing trend of floc mean size and number concentration generally agrees with previous laboratory
499 measurements (Schneck et al., 2019; Pei et al., 2023). However, laboratory measured mean floc size and number concentration
500 stopped increasing significantly shortly after peak supercooling, while in the field they stopped increasing later, near the end
501 of the principal supercooling period. For example, Schneck et al. (2019) observed that the mean floc size and number
502 concentration in freshwater stopped increasing significantly at dimensionless times of $t / t_c = 1.13$ and 1.27 , respectively
503 compared to $t / t_c = 2.00$ and 1.81 for NSR-L4 (t_c is the time interval between the start of supercooling and peak supercooling
504 and t is the time). The peak floc number concentration measured during the three Principal deployments in this study ranged
505 from $9.3 \times 10^{-4} \text{ cm}^{-3}$ to $3.1 \times 10^{-3} \text{ cm}^{-3}$, which was more than two orders of magnitude lower than the $2.5 \times 10^{-1} \text{ cm}^{-3}$ measured
506 in the laboratory tank by Schneck et al. (2019). These significantly lower floc concentrations suggest that particle
507 concentrations in the field were also much lower compared to laboratory measurements. At lower suspended frazil
508 concentrations the collision frequency of frazil particles would be reduced, increasing the time for flocs to gain mass via
509 collision-induced particle-floc aggregation, which might explain the longer time period that mean floc size and number
510 concentration was observed to increase in the field.

511

512 Figure 10 shows that during KR-F1 the mean floc size was approximately constant prior to the arrival of the hydropeaking
513 wave during the residual supercooling phase. Similarly, there were no trends observed in floc size in five other Residual
514 deployments, NSR-L2, NSR-L5, KR-E1, PR-F1 (see Figs. S2, S4, S7 and S6 in the Supplement) and PR-F2 (Fig. 11).
515 McFarlane et al. (2019b) found that in rivers the mean particle size remained approximately constant during the residual
516 supercooling phase if the environmental conditions were relatively stable. Therefore, it follows that flocs observed during the
517 residual supercooling phase would also have a stable mean size unless hydraulic and/or meteorological conditions changed
518 significantly. The mean floc size is the most stable during deployment KR-E1 (Fig. S7 in the Supplement) with a fluctuation
519 range of only 1.5 mm, which could be in part due to the significantly larger sample size of 187,288. The only two Residual
520 deployments that did not have a stable mean floc size were NSR-L6 and KR-F2 (Figs. S5 and S8 in the Supplement), and in
521 both cases, the size decreased and this coincided with minor increases in T_w (~ 0.005 °C). These results indicate that during the
522 residual phase the mean floc size does not typically vary significantly even at the end of the supercooling event when T_w rises
523 above zero, as was the case in PR-F1 and PR-F2. During the two PR deployments the floc properties did not change
524 significantly during the 1.3- and 2.5-hour time periods between when supercooling ended, and the measurements stopped. This
525 is likely because the zero degree isotherm had moved upstream of the deployment site but the frazil being generated upstream
526 of it was still advecting past the FrazilCam (i.e., the zero degree isotherm was not so far upstream that the advecting frazil had
527 time to melt.)

528

529 As shown in Fig. 10, during KR-F1 the residual supercooling water temperature remained mostly approximately constant at a
530 temperature of approximately -0.01 °C. An approximately constant residual supercooling temperature was also observed in

531 NSR-L2, KR-E1 and NSR-L5 (see Figs. S2, S7, and S4 in the Supplement). This means that during the residual supercooling
532 phase ice was still growing and releasing latent heat that balanced the heat loss from the water surface in order to maintain the
533 approximately constant water temperature. In this study, although the mean floc size did not vary significantly during most of
534 the measured residual supercooling deployments, fluctuations and trends in the floc number and volume concentration time
535 series were observed. This indicates that there may have been frazil ice particles still forming and growing, releasing latent
536 heat to help balance the surface heat loss. In addition, during the residual phase anchor ice, border ice, and surface ice pans
537 were likely growing as well and releasing latent heat, helping to maintain the stable residual supercooling temperature.

538

539 The time series of water temperature T_w and net heat flux Q_n provided an opportunity to theoretically estimate the total ice
540 growth in the water column, which could be compared to the measured floc volumetric concentration C_{fv} to estimate the
541 fraction of ice sampled by the FrazilCam. Assuming there were no significant water temperature gradients in any direction
542 (i.e. the river had a uniform temperature) and that the water depth was constant, the thermal balance of the water-ice mixture
543 is given by:

$$544 \rho C_p \frac{dT_w}{dt} = -\frac{Q_n}{\bar{d}} + \rho_i L_i \frac{dC_i}{dt}, \quad (15)$$

545 where ρ is the water density, C_p is the specific heat of water, ρ_i is the ice density, L_i is the latent heat of fusion of ice, and C_i
546 is the total ice concentration due to thermal growth (Souillé et al., 2023). Eq. (15) was then used to estimate, C_i for deployment
547 NSR-L4, which captured the entire principal supercooling period. The result showed that the FrazilCam was only sampling at
548 most 2% of the total ice that was forming in the water. It should be noted that Q_n used in the calculation does not account for
549 the effect of surface ice due to a lack of accurate surface ice data. In addition, mean water depth \bar{d} was used while in reality
550 water depth varied spatially and temporally. These approximations create considerable uncertainty in the calculations of the
551 total heat loss from the surface, and the volume of the water being cooled. Given all the simplifying assumptions that were
552 made the uncertainty in the calculated C_i is potentially quite large, but is likely not greater than a factor of two or three.
553 Therefore, despite this potential large uncertainty, the calculations suggest that the FrazilCam was only sampling less than
554 ~5% of the total ice being formed in the river. Similar calculations were also performed using data collected in a laboratory
555 frazil ice tank experiment using the laboratory version of the FrazilCam. In the laboratory environment the water depth is a
556 constant, the tank has been shown to be well mixed and the surface heat loss can be quantified from the water cooling rate
557 with reasonable accuracy. These results showed that C_i calculated using Eq. (15) was comparable to the volumetric
558 concentration of suspended ice calculated from the FrazilCam images prior to when flocs began rising to the surface. This
559 demonstrates that the FrazilCam does provide accurate measurements of the suspended ice concentrations. However, the only
560 time the FrazilCam would be sampling a significant fraction of the total ice being formed in a river would be when suspended
561 frazil is the only ice that is actively growing.

562

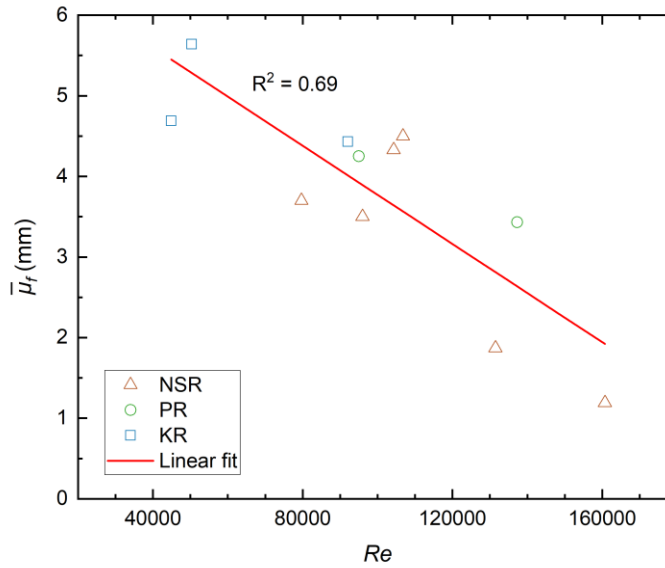
563 The effect of surface heat flux on floc properties was investigated. A positive mean net heat flux $\overline{Q_n}$ was observed for all
564 deployments indicating a net heat loss from the surface. The magnitude of $\overline{Q_n}$ ranged from 95.4 to 318.8 W m⁻² as shown in
565 Table 4. The dominant positive heat flux was Q_{lw} and Q_H for six and five deployments, respectively, while the dominant
566 negative heat flux in all deployments was Q_{sw} which is consistent with previous studies (McFarlane and Clark, 2021; Boyd et
567 al., 2023). Efforts were made to correlate the mean net heat flux $\overline{Q_n}$ with the measured floc properties listed in Table 4 (i.e.,
568 columns 5~11). No significant correlations were found when using data from all deployments or when only the data from the
569 six NSR deployments that have 10-min heat flux data were used. It is worth noting that the heat flux analysis in this study did
570 not account for varying surface ice concentrations and neglected several heat fluxes (e.g. sediment-water). Clearly, more
571 comprehensive and frequent measurements of heat fluxes and surface ice properties are needed in future studies to more fully
572 understand the impact of varying heat fluxes on frazil floc properties.

573

574 To investigate the effect of hydraulic conditions on the mean floc size μ_f , the local Reynolds number Re is plotted versus $\overline{\mu_f}$
575 in Fig. 12 along with the following linear regression equation:

$$576 \quad \overline{\mu_f} = 6.82 - 3.05 \times 10^{-5} Re, \quad (16)$$

577 As Re increases from ~40,000 to ~160,000, $\overline{\mu_f}$ decreases from approximately 5.5 mm to 2 mm and the coefficient of
578 determination (R^2) is 0.69, indicating that the two are moderately correlated. Clark and Doering (2009) found that higher
579 turbulence intensity inhibited the formation of large flocs. This finding is consistent with the correlation presented in Fig. 12
580 if it is assumed that turbulence intensity increased with Re in the three study rivers. However, this is not necessarily the case.
581 An alternate explanation for the observed correlation is that as Re increased flocs experienced higher shear strain rates (i.e.,
582 larger velocity gradients) and more violent floc-floc collisions which would tend to rupture larger flocs and reduce their mean
583 size.

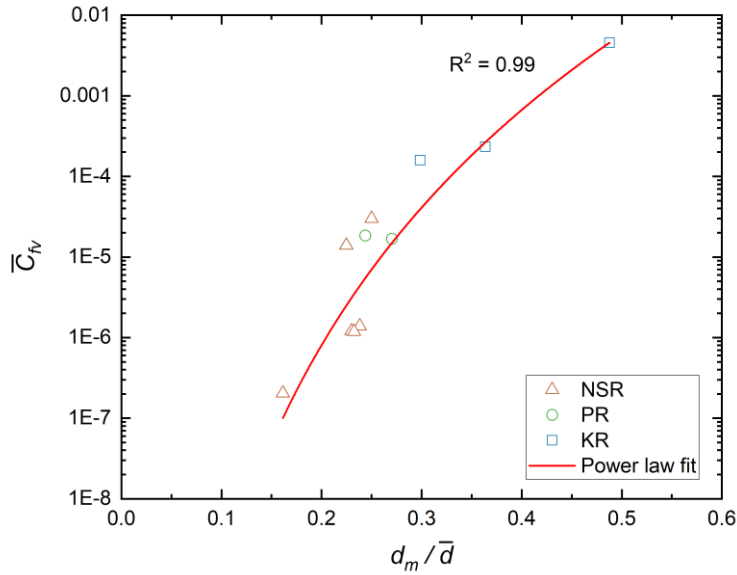


584
 585 **Figure 12. Relationship between local Reynolds number Re and mean floc size $\bar{\mu}_f$ in mm.**

586
 587 The effect of water depth on the floc volumetric concentration was investigated by correlating the average volumetric
 588 concentration with the fractional height d_m/\bar{d} where $d_m = 0.198\text{ m}$ is the height above the bed at the centre of FrazilCam
 589 FOV and \bar{d} is the mean water depth. Figure 13 presents a scatter plot of the fractional height d_m/\bar{d} versus the average floc
 590 volumetric concentration \bar{C}_{fv} . Results show that there is a strong nonlinear correlation given by the following power law
 591 equation:

592
$$\bar{C}_{fv} = 4.80 \left(\frac{d_m}{\bar{d}} \right)^{9.69}, \quad (17)$$

593 where the R^2 value equals 0.99. Ye (2002) and Morse and Richard (2009) reported measurements of vertical frazil
 594 concentration profiles and found that the Rouse equation (Rouse, 1937), previously used to characterize suspended sediment
 595 concentration profiles, could be used to describe the frazil ice concentration profile. Equation (17) is similar in format to the
 596 Rouse equation, indicating that the vertical concentration of both frazil particles and flocs may be accurately described by
 597 power law equations.



598

599 **Figure 13. Relationship between the fractional height d_m/\bar{d} and the average floc volumetric concentration \bar{C}_{fv}**

600 7 Conclusions

601 A submersible high-resolution camera system was deployed during supercooling in three rivers from 2021 ~ 2023. Images
 602 from the eleven deployments were analyzed to investigate frazil floc properties and their evolution. Images showed that frazil
 603 flocs observed in the North Saskatchewan River were predominately formed by disc-shaped particles, while flocs in the Peace
 604 River and Kananaskis River were comprised of various ice crystal shapes, including disc-shaped, needle-shaped, and irregular
 605 particles. A lognormal distribution is a reasonable description of floc size distributions in rivers. The mean floc size ranged
 606 from 1.19 to 5.64 mm and the overall mean floc size was 3.80 mm. The mean floc size in rivers was found to 48% larger than
 607 was previously observed in the laboratory by Schneck et al. (2019) while the maximum floc size was comparable in the
 608 laboratory and field. The average floc number concentration ranged from 1.80×10^{-4} to $1.15 \times 10^{-1} \text{ cm}^{-3}$ and previous laboratory
 609 measurements fall within the range of the values observed in this study. The estimated average floc volumetric concentration
 610 ranged from 2.05×10^{-7} to 4.56×10^{-3} , with the upper bound being comparable to previous total ice volume concentration
 611 measurements while the lower bound is an order of magnitude smaller.

612

613 Time series analysis indicated that during the principal supercooling phase, floc number concentration and mean size increased
 614 significantly just before peak supercooling and reached a maximum near the end of principal supercooling. This increasing
 615 trend was also observed in previous laboratory measurements (Schneck et al., 2019; Pei et al., 2023) but the duration of the

616 increasing trend was longer in the field. During the residual supercooling phase, the mean floc size did not typically vary
617 significantly even 2.5 hours after the water temperature rises above zero degrees. The effect of the air-water heat flux on floc
618 properties was investigated by conducting a linear regression analysis. However, no significant correlations were found, and
619 this may be due to the limited dataset or the complexity of the field environment where heat fluxes can vary temporally and
620 spatially. Future field measurements of floc properties, especially made during the principal supercooling phase and made
621 continuously along multiple sites along a study reach, are needed to more fully understand the factors that govern their size
622 and concentration.

623

624 Analysis of the influence of local hydraulic conditions on frazil floc properties showed that as the local Reynolds number
625 increases, the mean floc size decreases linearly. The resulting equation can be used to estimate mean floc sizes in rivers using
626 estimates of the mean velocity and depth. It was also shown that the averaged floc volumetric concentration can be related to
627 the fractional height above the bed through a power law equation. This relationship may be useful for describing the vertical
628 concentration profiles of frazil flocs.

629

630 The detailed measurements of frazil floc properties and their evolution in rivers presented in this study could be used in several
631 ways to enhance numerical modelling of river ice processes in order to improve predictions of river freeze-up. At the present
632 time the frazil rise velocity is treated as a calibration parameter in comprehensive river ice process models (e.g. Shen, 2010;
633 Blackburn and She, 2019). However, it could now be directly estimated by first using Eq. (16) to predict the mean floc size
634 using the local Reynolds number and then the rise velocity could be predicted using Reimnitz et al. (1993) measurements. In
635 addition, the reported lognormal size distributions of flocs, as well as time series evolution of mean floc size and
636 concentrations, measured in rivers for the first time, could provide opportunities to incorporate floc dynamics into numerical
637 models with the goal of improving how realistically they simulate frazil ice evolution and surface ice progression.

638

639 In the future, it would be of interest to deploy the FrazilCam in lakes and oceans, where the flow regime and salinity may be
640 considerably different, to investigate frazil particle and floc properties in these different environments. The FrazilCam system
641 in principle can be deployed in any sufficiently transparent waters, however, the system would need to be modified to automate
642 the polarizer rinsing process. This would be challenging but might be possible using a mechanical wiper which would allow
643 deployments on the bottom of deeper water bodies. In addition, the system could be attached to an unmanned or autonomous
644 underwater vehicle to allow observations to be made at various depths in the water column in lakes and oceans.

645

646 **Code and data availability**

647 Part of the meteorological data used to carry out heat flux analysis were obtained from Alberta Climate Information Service
648 (ACIS) <http://agriculture.alberta.ca/acis/weather-data-viewer.jsp>, Environmental and Climate Change Canada (ECCC)
649 https://climate.weather.gc.ca/historical_data/search_historic_data_e.html, and University of Calgary Biogeoscience Institute
650 <https://research.ucalgary.ca/biogeoscience-institute/research/environmental-data>. Historic sediment data for the North
651 Saskatchewan River at Edmonton and Peace River at Dunvegan Bridge can be accessed from Water Survey of Canada
652 Historical Hydrometric Data https://wateroffice.ec.gc.ca/mainmenu/historical_data_index_e.html. All other data and code
653 used in this study are available from the authors upon request.

654 **Author contribution**

655 CP and JY prepared the apparatus and performed the field work together with advice from YS and ML. CP carried out the
656 analysis and processing of the data, prepared the figures, and wrote the manuscript with review and contributions from JY,
657 YS, and ML.

658 **Competing interests**

659 The authors declare that they have no conflict of interest.

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666 (<https://qgis.org/en/site/>) using the data provided by © OpenStreetMap contributors
667 (<https://www.openstreetmap.org/copyright>) and MapTiler (<http://openmaptiles.org/>).

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