## Supplement of

## **Improve** *i***LOVECLIM** (version 1.1) with a multi-layer snow model: surface mass balance evolution during the Last Interglacial

Thi-Khanh-Dieu Hoang<sup>1</sup>, Aurélien Quiquet<sup>1</sup>, Christophe Dumas<sup>1</sup>, Andreas Born<sup>2</sup>, and Didier M. Roche<sup>1,3</sup>

<sup>1</sup>Laboratoire des Sciences du Climat et de l'Environnement, LSCE/IPSL, CEA-CNRS-UVSQ, Université Paris-Saclay, 91191 Gif-sur-Yvette, France

<sup>2</sup>Department of Earth Sciences, University of Bergen and Bjerknes Centre for Climate Research, Bergen, Norway <sup>3</sup>Department of Earth Sciences, Faculty of Science, Vrije Universiteit Amsterdam, Amsterdam, the Netherlands

Correspondence: Thi-Khanh-Dieu Hoang (dieu.hoang@lsce.ipsl.fr)



**Figure S1.** Annual mean SMB anomalies (in mWE yr<sup>-1</sup>) of BESSI with respect to MAR during the period 1979-2021 for (**a**) Greenland and (**b**) Antarctica.



**Figure S2.** Temporal variation of the annual mean total SMB and its elements integrated on the present-day ice sheet extent of ITM (in Gt  $yr^{-1}$ ) during LIG for (a) Greenland and (b) Antarctica.



**Figure S3.** Annual mean SMB (in Gt yr<sup>-1</sup>) of some LIG time slices (135, 128.5 and 115 kaBP) and the pre-industrial simulation of (**a**) ITM and (**b**) BESSI-*i*LOVECLIM for Greenland Ice Sheet. The total SMB (in Gt yr<sup>-1</sup>) integrated for the present-day ice sheet extent (red line) is also included.



**Figure S4.** Annual mean SMB (in Gt yr<sup>-1</sup>) of some LIG time slices (135, 128.5 and 115 kaBP) and the pre-industrial simulation of (**a**) ITM and (**b**) BESSI-*i*LOVECLIM for Antarctic Ice Sheet. The total SMB (in Gt yr<sup>-1</sup>) integrated for the present-day ice sheet extent is also included.



**Figure S5.** (a) Annual mean SMB (in Gt yr<sup>-1</sup>) of some LIG time slices (135, 128.5 and 115 kaBP) and the pre-industrial simulation of bias-corrected BESSI-*i*LOVECLIM, including the total SMB (in Gt yr<sup>-1</sup>) integrated for the present-day ice sheet extent (red line). (b) Annual mean SMB anomalies (in Gt yr<sup>-1</sup>) between several LIG time slices (135, 128.5 and 115 kaBP) and the pre-industrial of bias-corrected BESSI-*i*LOVECLIM for Greenland Ice Sheet.