



1 Structured exploration of machine learning model

- 2 complexity for spatio-temporal forecasting of urban
- **3** flooding
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10 Abstract

Urban flooding may lead to significant socio-economic impacts and loss of life. To afford 11 preventative actions, researchers have implemented various modeling techniques to gain insight 12 into urban flood occurrences. Using New York City (NYC) as the study area, data-driven 13 techniques, specifically statistical and neural network models with increasing spatio-temporal 14 15 complexity, are formulated and tested, assessing the potential relative contribution of different modeling constructs. Zones, based on flood characteristics, are first delineated using the 16 unsupervised machine learning technique of spectral clustering. Then, the models are applied to 17 each cluster, with comprehensive performance evaluation, as to understand which algorithmic, 18 structural aspects contribute to the reduction of prediction errors. A chief discovery of this study 19 is the emergence of the Graph Wavenet (GWN) as the most effective model due to its proficiency 20 21 in capturing spatio-temporal aspects and implementing dynamic graph creation. Furthermore, it 22 is seen that the enhancement of specific temporal and spatial components within a modeling technique proves beneficial, and a novel adoption of graph-based architectures is additive. 23 Offering a unique exploration of spatio-temporal aspects, emphasizing the benefits of component 24 25 enhancement and the adoption of graph-based architectures, this paper identifies modification techniques, which would allow for insights to prevail in urban flood modeling despite being 26 27 confronted with limited data availability.

28 1. Introduction

Urban flooding, a natural disaster with dynamic ramifications, requires circumspect 29 30 consideration. At the onset of rainfall, as runoff traverses through an urban setting, numerous obstacles, including an inability to permeate structures, sidewalks, and streets, and restricted 31 entry into drainage systems due to debris blockages, are experienced. Compounding the issue, 32 additional rainfall in a brief timeframe overwhelms even the unobstructed drains, preventing 33 water admission and exacerbating overflow departure attempts. Consequently, runoff either 34 35 persists on the streets or seeps through gaps in homes and buildings. In the resulting 36 circumstance of urban flooding, the community is harmed. Most egregiously, deaths may occur,





37 as without adequate warning, individuals are not able to implement precautionary measures, such as avoiding outdoor travel or relocating to higher elevated areas when indoors. Veritably, this 38 tragic outcome was demonstrated during the post-tropical depression Ida event, where many of 39 44 deaths within the New York City (NYC) metropolitan region were caused either by exposure 40 to outdoor hazards, such as vehicular drownings or being swept away by the waters, or indoor 41 below-ground dangers, such as drownings in flooded basements (Falconer, 2021; Plumer, 2021). 42 Furthermore, in addition to fatalities, urban flooding exacts economic strain, as there may be 43 44 destruction to the infrastructure, interruption to transportation services, and structural damage to the buildings and vehicles. Indeed, in the event of a large flooding disaster, direct costs may be 45 incurred at the extent of billions of dollars; additionally, when examining smaller, frequent 46 floods, long-term costs collect over the years by the chronic strains to the structural, plumbing 47 and electrical systems (Agonafir et al., 2023). Hence, prioritizing the analysis of the diverse 48 elements and influences on water behavior in an urban environment proves essential. 49

Now, as accurate flood forecasting models, allowing for the implementation of disaster 50 deterrent measures, would offer significant health and financial relief, there is continuous 51 progression in model development. Traditionally, hydrodynamic models have been widely used 52 for flood prediction and risk assessment; however, the employment of these physics-based 53 54 models is limited in certain metropolitans (Agonafir et al., 2023). Specifically, hydrodynamic models rely on extensive calculations to determine water flow, requiring detailed drainage 55 network plans; as thus, in certain urban cities, such as NYC, where drainage details are 56 57 unobtainable to researchers (Al-Suhili et al., 2019), the implementation of physics-based models becomes infeasible. Therefore, there has been a turn towards data-driven techniques to provide 58 59 insight into water behavior when existing physical information is limited. With the provision of 60 influencing variables, via statistical calculations and artificial intelligence (AI) capabilities, the 61 models possess the ability to assess an occurrence and then create forecasts or ascertain vulnerabilities. Hence, the objective of understanding urban flooding is met without the need to 62 simulate the exact water path. Ultimately, due to the convenience of use, data-driven techniques, 63 particularly AI methods, have risen drastically in flood literature (Mosavi et al., 2018). 64 Accordingly, an in-depth study into the efficiency of emerging AI techniques, within the field of 65 66 urban flooding, affords complementation to the trend.

The mission of this study is formulated in consideration of the dire human and economic 67 devastations of urban flooding, the modeling limitations due to data availability, and the recent 68 advances in data-driven models to remedy the issues. Accurately assessing the intricacies of 69 urban flood occurrence in NYC, by the employment of physical and crowdsourced data, this 70 research provides a unique analysis of added components by presenting a cascade of statistical 71 72 and neural network models, each with ascending complexities. In the exploration, a preliminary step involves the delineation of zones based on urban flood characteristics, using the 73 74 unsupervised machine learning technique, spectral clustering. Then, a particular set of models, the Poisson Generalized Linear Regression (GLM), Feed Forward Neural Network (FFN), 75 76 Recurrent Neural Network (RNN), Convolutional Neural Network (CNN), Graph Convolutional Network (GCN) and the Graph Wavenet (GWN), is selected as to assess the benefits of auxiliary, 77 advanced spatio-temporal aspects, dynamic graph creation and convolutional node-messaging 78





capabilities. The conduction of the experiment follows such that every model, receiving identical time-series input data and undergoing training (8 years) and testing (2 years) using the same set of dates, is tasked with the production of daily predicted street flooding counts for the testing period. By goodness-of-fit determinations, model comparisons are performed and dissected to discover the impacts of additional complexities. Therefore, the comprehensive examination of diverse models imparts invaluable modeling guidance towards urban flood research in the datadriven era.

86 Regarding existing urban flood literature, there is limited utilization of graph-structured artificial neural network (ANN) models. Moreover, of the few existing studies, an inclusion of 87 pluvial, urban flooding is notably absent. For instance, in Farahmand et al., a spatial-temporal 88 graph-based model (ASTGCN) for nowcasting in Harris County, Texas is developed (Farahmand 89 90 et al., 2023). However, the examination is conducted on the singular flooding incident of Hurricane Harvey and its direct landfall onto the county, thereby effectively assessing the 91 model's accuracy only in regards to coastal flooding. In contrast, the research of this paper 92 93 delves into urban flooding over a 10-year duration, encompassing both large-scale events and persistent, frequent flash flood and pluvial occurrences. Furthermore, the primary objective of 94 Farahmand et al is to highlight the proficiencies of the new model, rather than to conduct an in-95 96 depth exploration of the specific advantages of its added elements. In contrast, this research traverses a range of models, inspecting the benefits of each advancement. In another existing 97 study, Wang et al, a graph-structed model is also created to benefit urban flood insights (Z. Wang 98 99 et al., 2023). Nonetheless, the paper does not serve as a comparative analysis of varying models; also, the model developed identifies flood susceptibility, as opposed to producing forecasts. 100 101 Finally, it is worth noting that Santos et al develops a graph-based, deep learning model for flood 102 prediction (Oliveira Santos et al., 2023). Yet, the forecasts are for riverine flooding instead of 103 urban flooding. As urban flooding involves multiple factors distinct from riverine flood variables (i.e., lack of infiltration and complex drainage networks), a model analysis specifically tailored 104 towards urban concerns has more utility to metropolitan stakeholders. Therefore, this paper is the 105 first of its kind to pioneer the adaptation of graph-based neural networks for urban, pluvial 106 107 flooding, while conducting an expansive exploration of the spatio-temporal aspects within the 108 domain.

This paper follows a structured sequence. In Section 2, the study initiates by discussing the 109 study area of NYC and the urban characteristics which make it ideal for experimentation. Also, 110 Section 2 demonstrates the data collection and pre-processing steps. Next, Section 3 delves, with 111 extensive detail, into the methodology employed for each machine learning and statistical 112 technique, laving a solid foundation for the thorough analysis presented in Section 4. Then, in 113 Section 4, a detailed presentation and discussion of results unfold, exploring risk zones and 114 model performances across diverse flood attributes and model features. Finally, in Section 5, 115 conclusions are drawn, as the findings from the study are synthesized, offering a comprehensive 116 overview of the outcomes and their implications for urban flood research. 117





118 2. Data pre-processing

119 2.1 Study area

Situated along the northeastern coast of the United States, NYC emerges as the metropolitan 120 landscape—distinctly impervious and densely populated. Lacking efficient infiltration with 121 approximately 72% impervious cover, and encompassing a mere 800 square kilometers, while 122 boasting roughly 8 million residents (City of New York, 2022; U.S. Census Bureau QuickFacts, 123 124 2012.), NYC embodies urbanization. Moreover, crucial details, such as the locations and widths of stormwater inlet drains and digitized maps of the sewer network are notably absent from 125 public records. This lack of drainage data poses a challenge to hydro-hydraulic flood modeling 126 and emphasizes the need for alternative methods to mitigate flooding issues within the city. 127 Moreover, NYC holds economical influence, contributing approximately \$1.8 trillion annually to 128 129 the U.S. gross domestic product (Bureau of Economic Analysis, 2021). Therefore, the intricate urban fabric, intertwined with the economic significance and challenges of minimally accessible 130 131 data, poses NYC as the ideal study area for the application of data-driven techniques in urban flooding. 132

133 NYC has 59 localized, politically based districts, called Community Boards (DISs). DISs manage zoning and land-use policies and address general municipal concerns (City of New York, 134 2023a). By borough, the breakdown of DISs is the following: 12 in Manhattan, 12 in the Bronx, 135 18 in Brooklyn, 14 in Queens, three in Staten Island. Due to the quantity and extent of the 136 137 districts, they serve as an ideal starting point for variable aggregation and clustering analysis. In this study, shapefiles were downloaded from NYC Open Data (City of New York, 2023b), and 138 139 the processing of data was conducted by ArcGIS and Python. In the proceeding sections, the methods of aggregation are further detailed. 140

141 2.2 Dynamic Variables

142 2.2.1 NYC 311 Platform

NYC311, a crowdsourcing platform, provides gainful insights into sewer related conditions in 143 NYC. Observations of city issues are reported by residents of the city, where the date, time, and 144 145 longitude and latitude coordinates of the incident are listed. Hence, the detailed temporal and 146 locational information affords researchers the opportunity to employ data-driven techniques for analyses. For this study, NYC311 street flooding (SF), sewer backups (SB), and catch basin 147 blockages (CB) reports, ranging from January 1, 2010 through December 31, 2019, were 148 149 downloaded from the NYC Open Data website: http://data.cityofnewyork.us (Dates after 2019 were excluded, as the COVID pandemic is assumed to have an impact on reporting behavior, 150 151 particularly in NYC, where residents and visitors relocated and returned at various intervals). For each report type, daily counts were aggregated to the DIS level. SF complaints, witnessed 152 incidents of street flooding, served as the response variable. SB and CB reports were chosen for 153 inclusion, as they are known influences towards SF (Agonafir et al., 2021; City of New York, 154 2022a). Specifically, SB indicate an internal issue within the drainage network, where it is 155 overtaxed (Schmitt et al., 2004).); moreover, Agonafir et al has shown that SB reports are a 156 significant predictor towards SF reports in almost half of NYC zip codes (Agonafir et al., 2021). 157





Thus, the addition of SB may strengthen a model's ability to make predictions. Also, in the Agonafir et al study, CB was found to have consequence on SF in roughly half the NYC zip codes (Agonafir et al., 2021). When a catch basin is blocked or clogged, runoff is not efficiently extracted into the stormwater drains, thereby allowing for ponding. In brief, from the NYC311 platform, the dynamic (values varying with time) infrastructural predictors, SB and CB, and the predictand, SF, were obtained. SF, SB, and CB counts were totaled per day per DIS by using the timestamps and longitude and latitude coordinates.

165 2.2.2 Radar and Gauge Data

Precipitation, rain and snow, drive urban flooding occurrence. While it is apparent that rainfall 166 is the primary contributor (Agonafir et al., 2023; Qin et al., 2013; Schmitt et al., 2004; Sharif et al., 167 168 2006; Valeo & Ho, 2004), snowmelt also has influence, as when large amounts of snow liquifies, 169 streets may be flooded (Semádeni-Davies & Bengtsson, 1998; Valeo & Ho, 2004). Concerning 170 rainfall, there are intense rainstorms (large amounts of rain in a brief time interval), which contribute to flash floods, and there are prolonged rainy days, where the rainfall may not be 171 172 intense, yet there is sufficient amount of water over a longer duration. In both cases, the capacity of the stormwater drains may become exceeded (Agonafir et al., 2023). Therefore, this study 173 used three predictor variables representing precipitation: Max Hourly Rainfall (MR), Total Daily 174 175 Rainfall (TR), and Snowfall (SN). Now, there are also varied methods of rainfall collection: insitu (gauge) and remote sensing (radar and satellite). Some benefits of in-situ measurements 176 177 include not being encumbered with cloud top reflectance, thermal radiance, retrieval algorithm and overpass frequency issues (AghaKouchak et al., 2009); whereas radar data is advantageous 178 in terms of spatial distribution (Thorndahl et al., 2017), capturing precipitation amounts at more 179 locations within an area. As both techniques are considered standard measurement methods, this 180 study employed radar data for the MR and gauge data for the TR and SN variables. Each of the 181 precipitation variables were determined at the DIS level. 182

183 The radar rain data was taken from the National Center for Atmospheric Research (NCAR)/Earth Observing Laboratory (EOL) website, and the gauge rain and snow data were 184 retrieved from NOAA's Climate Data Online. For the radar, the resolution is 4 km by 4 km, and 185 the gridded data is Stage IV, benefiting from manual quality control (EOL, 2022). Hourly totals 186 were gathered for the dates ranging from January 1, 2010 through December 31, 2019. Then, the 187 maximum hourly value (MR) was taken for each radar point for each day. Ultimately, the MR 188 values were assigned to each DIS based on the radar point's proximity to its centroid. Now, 189 190 regarding the gauge data, the Global Historical Climatology Network (GHCN) by NOAA's National Centers for Environmental Information (NCEI) provides daily climatology details from 191 192 land surface stations globally (National Centers for Environmental Information, 2023). With respect to the daily rain totals (TR) and snow totals (SN), data was collected from the GHCN 193 station, NY CITY CENTRAL PARK, NY US, for the dates ranging from January 1, 2010 194 through December 31, 2019. These are direct measurements provided by the station. The TR and 195 SN 24-hour amounts were assigned to each DIS. Therefore, by a combination of radar and gauge 196 197 determinations, precipitation, representing rainfall intensity, total rainfall, and total snowfall, were assigned to each DIS at the daily level as predictors for the models. 198





199 2.3 Static Features

There are multiple factors driving the occurrence of urban flooding. First, there are 200 topographical variables, such as slope (SLP) and elevation (ELV). Regarding slope, the greater 201 the incline of a surface, the greater the velocity and discharge of water; hence, at the bottom of 202 the slope, the water will pond quickly (Bruwier et al., 2020). Concerning elevation, studies have 203 204 also shown lower elevated areas to be at a higher risk of flooding. For one, lower elevated areas are more vulnerable to storm surges from coasts and rivers, and secondly, as mentioned prior, 205 lower elevated areas may be located at the edge of a sloped surface (Ouma & Tateishi, 2014; 206 207 Woodruff et al., 2013). In addition to the topographical, there are urban features, specifically the quantity of buildings (BLD) and the extent of building footprint (FTP), which affect flooding. 208 209 Buildings are an impervious surface, such that water is unable to infiltrate through the ground. Moreover, multiple studies have found buildings to have a dominating influence on urban 210 flooding, compared to other common flood factors (Agonafir et al., 2022; Bruwier et al., 2020; J. 211 Lin et al., 2021). Another variable included represents percent impervious (IMP); it depicts the 212 213 percentage of all impervious surfaces, such as buildings, sidewalks, and streets, within a neighborhood. Next, a variable representing the area (SIZ) of the DIS was included in the study. 214 The size of a region does not increase flooding occurrence, yet, larger areas have more 215 216 opportunity for flooding occurrences, leading to higher flood counts; thus, the machine learning model will benefit from the information. Lastly, concerning locational, latitude (LAT) and 217 longitude (LNG) coordinates, the variables allow for a directionality indication of flood 218 219 occurrence. For instance, Agonafir et al found that street flooding in NYC had a southern and eastern locationality of increased flood incidents (Agonafir et al., 2022). While the exact cause of 220 221 flooding is not given by the location, the variable allows for a geographical pattern to be learned within machine learning models. Overall, physical features including slope, elevation, building 222 extent, area and geographical coordinates are useful variables in understanding urban flooding 223 via modeling. 224

For the physical features, shapefiles were downloaded from NYC Open Data and processed 225 226 via ArcGIS analysis tools. For the SLP and ELV variables, a shapefile of elevation points was downloaded, and the mean elevation in meters (m) and mean degree of slope were determined 227 per DIS. Also, a shapefile, providing the number of buildings, was retrieved, and the total 228 number of buildings per square kilometer (km²) area of each DIS was tallied to represent the 229 BLD variable. Regarding the FTP variable, a shapefile of building footprints was used, and via 230 ArcGIS, for each building footprint, the area in km² was calculated. In each DIS, the sum of the 231 footprint areas was determined. For the SIZ, LAT, and LNG variables, with the DIS shapefile, 232 the values were determined via geometry processing tools of each DIS polygon, where SIZ was 233 calculated in km², and the LAT and LNG represent the centroid points of each polygon. 234 Therefore, by geoprocessing, the static features for the analysis were collected. 235

236 3. Methodology

With the overarching goal being the achievement of a model, which produces profound
insights on urban flooding despite limited data, this study investigates the value of added
components, ascending in complexity. The methodology is outlined as a flowchart in Fig. 1. The





- 240 preliminary step for this analysis was the delineation of meaningful zones. Borders of zip codes,
- 241 DISs, or boroughs are not based on topographical or urban flood characteristics. Therefore, while
- the DIS serves as a sufficient starting point for data aggregation, a further outlining of risk zones
- based on flood factors, as opposed to political or postal bordering, has more utility in modeling
- 244 endeavors. Accordingly, a spectral clustering technique was applied to identify areas of similar
- flood vulnerability characteristics. Specifically, the features used as inputs to the clustering
- algorithm were SLP, ELV, BLD, FTP and IMP. Then, six clusters (zones) based on likeness were
- 247 created (Fig. 2), and the dynamic and static variables were aggregated from the DIS to the cluster
- 248 level. Thus, with zones of NYC regions aligned on related flood factors, predictive modeling was
- able to be performed.



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- 251
- 252 Fig. 1 A flow chart outlining key processes.

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Fig. 2 The six zones delineated by urban flood risk characteristics. Fig. 2a depicts the mapping of the zonal spreads per DIS. Fig. 2b-f are box plots depicting the range of flood characteristics of DISs within each zone. For each zone, the extent of the mean slope, mean elevation, number of buildings per DIS area, the sum of total building footprint area per DIS area, and mean percent of impervious cover of each DIS are shown in Fig. 2b, 2c, 2d, 2e, and 2f, respectively. Fig. 2g are the bar plots illustrating the sum of the total SF reports in each zone over a 10-year period.

The first set of models were created to predict street flooding occurrence (SF) based on daily 260 values of climatic (MR, TR, SN) and infrastructural influences (SB and CB) over a 10-year time 261 262 span. The research begins with a classical model - the GLM. Features of GLMs include the provision of a link function and likelihood function; in addition, GLMs possess the ability to 263 264 work with count data and nonlinearities (Hardin & Hilbe, 2007). Next, the research moves to a more complex, yet classical AI-based model - the FFN. FFNs introduce a layered architecture 265 (input, hidden and output layers) of neurons, which gives the models the ability to sense an 266 environment for subtle patterns (Fine, 2006; Setiono, 2001). Also, FFNs have the benefit for 267 adaptability, where elements may be added, allowing for varying capabilities. Particularly, the 268 269 architecture of FFNs provides the basis for the RNN and CNN. For instance, with the RNN, there is the feed forward mechanism as found in the FFN; however, the RNN is also equipped 270 271 with a feedback loop, thereby enhancing short term memory and temporal dependency learning (Fei & Lu, 2018; Schmidt, 2019). Regarding the CNN, the feed forward process comprises of 272 convolutional and pooling layers, where spatial (patterns across neighboring time steps) aptitude 273 274 is achieved via filtering kernels (Albawi et al., 2017; Durairaj & Mohan, 2022; Koprinska et al., 2018; M. Sun et al., 2017). When working with time-series data, coordinates of observation values are 275 created, and the spatial capability refers to the comprehension these numerical relationships in 276 277 time, which is processed in parallel, as opposed to in sequence as with the RNN (K. Wang et al., 2019). Hence, the RNN and CNN are both capturing temporal dependencies; however, the 278 mechanism of temporal incorporation differs. This study investigates the RNN and CNN to 279 explore the effects of each added component towards the forecasting of SF within this specific 280 281 data set. Overall, the beginning models, varying in architecture, temporal capabilities, utilize the time-series predictors to make predictions on the response variable representing street flooding in 282 the urban setting. 283

Graph-based neural networks consider locational aspects. Since there is a geographical
 component to urban flooding, as localized areas of susceptibility are to be discovered, this model





286 study further explores the benefits of the graph neural network architecture. For the GCN, the predictors remain as MR, TR, SN, SB, and CB, with the response variable as SF. As there are 287 only 6 nodes in this study, all within a reasonably close geographical proximity, the model was 288 created so that each cluster is connected to all other clusters. Each cluster represents a node, and 289 290 via edges, external information is communicated among the nodes, thereby bridging potential gaps within each node's incomplete internal data (Jiang et al., 2023; Piao et al., 2022; Scarselli et 291 al., 2009; Y. Wang et al., 2023). Ensuingly, this study explores the GCN and the GWN. For the 292 293 GCN, the inputs are as described above. A tensor creates a fully-connected graph, where features from neighboring nodes are aggregated to assess how conditions in one zone may have affect 294 295 another zone. The process is achieved via two graph convolutional layers. Lastly, the graph neural network architecture is transfigured to the GWN. Here, the GWN had been adapted from 296 Sun et al (A. Y. Sun et al., 2021). Considered the most complex model of this study, the GWN 297 incorporates all the aspects of the previous neural network models - locational, spatial, and 298 recurrent elements - while also introducing novel features of its own, such as gated layers and the 299 self-adaptive adjacency (SAA) matrix. Moreover, due to the SAA, the GWN is able to 300 301 incorporate static features. For this study, the following static characteristics were fed into the GWN: SIZ, SLP, ELV, LAT, LNG, BLD, FTP, and IMP. 302

For every model in the exploration, the coefficient of determination (R²) was used as a validation measure. The dataset of variables was partitioned into training and testing sets. The training data ranged from January 1, 2010 through January 1, 2018; the testing data ranged from January 2, 2018 through December 31, 2019. Each model made predictions spanning the testing date range; the predictions were compared to the observed, and the R² was ultimately computed. Hence by evaluating the goodness of fit, model comparisons were conducted.

309 3.1 Spectral Clustering

Spectral clustering, an unsupervised machine learning technique, partitions groups based on 310 similarities. For this study, the SpectralClustering tool from the sklearn module is utilized in 311 Python (Scikit-learn, 2023). The data points of each DIS are SLP, ELV, BLD, FTP and IMP. Each 312 feature was transformed independently via Standard Scaler, processing for a mean of zero and 313 standard deviation of one, as to prevent disproportional influence on the algorithm's 314 computation. Here, the features were represented as x1, ..., xn. For each vertex (DIS), edges were 315 constructed from x_i to its k-nearest neighbor, x_{ij} . The Euclidean distance $[t(x_i, x_j)]$ between each 316 317 unique pair of x_i and x_j was calculated (Scikit-learn, 2023). Then, a measure of similarity (s_{ij}) was determined as follows (Scikit-learn, 2023): 318

319
$$s_{ii} = e^{-10 \times t(x_i, x_j)^2} \dots (1)$$

Edges were created between each pair, and similarity is used as the edge weight. The purpose of
similarity weights is for the edges between a pair of points in the same group to have greater
weights than the edges between a pair of points that lie in separate groups (von Luxburg, 2007).
An unnormalized Laplacian graph was formed, with the matrix defined by Luxburg as follows
(von Luxburg et al., 2008):

325
$$L = D - S \dots (2)$$





S was the similarity matrix: $S := (s_{ij})_{i,j=1,...,n}$ and D was the diagonal matrix with passes: d_{ij} : $= s_{ij} \sum_{j=1}^{n} s_{ij}$. With the computation of L, eigenvalue decomposition was initialized. The solver used was ARPACK, which computes k eigenvectors of L: $v_1, ..., v_k$ (von Luxburg, 2007). Here, k is six (the number of desired flood zones). Let V be the matrix, where the eigenvectors were columns, and q_i represented the vector in the i-th row of V, then via the k-means algorithm, the points, $(q_i)_{i=1,...,n}$ were grouped into clusters (von Luxburg, 2007). Hence, with the preceding machine learning technique, each of 59 DISs were grouped into six zones (labeled 0, 1, 2, 3, 4, and 5), based on the physical and urban traits.

334 There are physical characteristics which influence a region's susceptibility to SF complaints. 335 The primary intent of the spectral clustering application is informed delineation. Nevertheless, a further advantage is the depiction of regions sharing similar extents of known, physical, flood 336 factors, as detected in the Random Forest model by Agonafir et al. (Agonafir et al., 2022) and 337 discussed in previous urban flood literature. The Standard Scaler function was employed so that 338 each attribute holds comparable influence. Hence, for this study, the purpose of spectral 339 340 clustering model is not to serve as a discovery or predictive model, as it is preparing the data for the statistical model and supervised machine learning explorations. 341

By spectral clustering, six zones were designated based on the flood factors. The quantity of 342 six was chosen, as to provide a higher degree of localization compared to county or borough 343 levels. To illustrate the prevalence of each trait within a zone, box plots were created (Fig. 2b-f). 344 345 Each box plot is comprised of the values of the DISs within the specified zone. The plots 346 illustrate the range of SLP, ELV, BLD, FTP and IMP. Also, the total SF complaints, over the 10year timespan, for each zone is depicted in Fig. 2g. Since each DIS now belongs to a zone, the 347 data must also be aggregated to the zonal level. For the dynamic variables, SF, SB, and CB, the 348 349 totals of each DIS with a zone were taken, and for MR, the mean of the DIS values within a zone 350 were calculated. For TR and SN, the measurements were previously taken from a single source; hence, no aggregation was needed. For the static attributes [only used as an input to the GWN], 351 352 SLP, ELV, LAT, LNG, BLD, FTP, and IMP, mean values for each DIS within a zone were determined, and for SIZ, the sum of the areas of each DIS in a zone was calculated. Therefore, 353 354 the dynamic predictors and response variables and the static characteristics for each zone were prepared for the performance of predictive modeling. 355

356 3.2 Poisson Generalized Linear Regression Model

The GLM used in this study is the Poisson GLM (hereafter referred to as GLM). Here, the GLM uses a log link function and a Poisson distribution of the exponential family. For each zone, the target variable and the explanatory variables were expressed at i-th observations as follows:

361 $SF_i \sim Poisson(\lambda_i) \dots (3)$

362 where,

363 $\lambda_{i} = e^{\beta_{i}^{0} + \beta_{i}^{1}SB_{i} + \beta_{i}^{2}CB_{i} + \beta_{i}^{3}MR_{i} + \beta_{i}^{4}TR_{i} + \beta_{i}^{5}SN_{i}} \dots (4)$





The β^k coefficients represent the strength of change in the log-relative rate of the SF for a oneunit change in the associated predictor variable, and β^0 is the intercept, which is the baseline rate when the predictors are zero.

367 3.3 Feed Forward Neural Network

The FFN, applied to each zone independently, is composed of three layers: input, hidden, and 368 output. Fig. 3 depicts the architecture. The input layer has the two infrastructural and the three 369 climatic predictors; each predictor is normalized using the Python sklearn's Standard Scaler 370 function. For this model, at each time step, there are 32 neurons within the hidden layer, and each 371 372 predictor feeds forward to all neurons. For each connection, via the Adam optimizer gradient 373 descent method, weights, ω , are initialized; moreover, for all neurons, a distinctive bias, b, is 374 computed by random initialization. Then, for every neuron, i, there is a weighted sum calculation, as follows: 375

376
$$S_i = SB\omega_{SBi} + CB\omega_{CBi} + MR\omega_{MRi} + TR\omega_{TRi} + SN\omega_{SNi} + b_i \dots (5)$$

The sum then enters into the ReLU activation function, σ^R . Activation functions aid in understanding nonlinear relationships. The ReLU was chosen, as it is known for its accuracy and is widely used in deep learning modeling (Dubey & Jain, 2019). The next step in the FFN is the forward movement of information from the last hidden layer to the output layer. Similar to the last weighted sum calculation, the weighted sum at the output neuron is computed:

$$S_{output} = \left(\sum \omega_i \sigma_i^R\right) + b \dots (6)$$

From the output layer, the data enters a linear function and produces the predicted counts of SF.
The model was constructed via the Pytorch NN module (PyTorch, 2023c). The model was run
with a learning rate of 0.001, batch size of 32 and 100 epochs.

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387

388 Fig. 3 The FFN architecture.

389 3.4 Recurrent Neural Network

The RNN architecture, built upon a network of neurons, is similar to the FFN structure. 390 391 However, there is a difference within the hidden layer composition, where, as opposed to possessing only feed forward (FF) layers, the RNN includes a preceding Long Short-Term 392 393 Memory (LSTM) layer (Fig. 4). First, a concatenated input vector of the predictors, X at each time step enters each neuron. X is then concatenated with the hidden state vector, H, at the 394 previous time step. Then, via gradient descent optimization, unique (per neuron) input weight 395 396 and bias are calculated. The input gate, i, controls the extent of input information entering the cell state (Schmidt, 2019; Tsantekidis et al., 2022), and the computations for each neuron, n, of 397 the 16 neurons of the RNN layer are as follows: 398

399
$$i_{n,t} = \omega_{i,n} [H_{t-1,n}, X_t] + b_{i,n} \dots (7)$$

400 After the initial computation, the input enteres the sigmoid activation, σ^{s} function:

401
$$I_{n,t} = \sigma_n^S(i_{n,t})\dots(8)$$

402 Now, the forget gate, f, also receives the input vector of predictors; yet, it's function is to filter

403 out irrelevant information from the previous cell state (Schmidt, 2019) .The calculations for f are404 as follows:





$$f_{n,t} = \omega_{f,n} [H_{t-1,n}, X_t] + b_{f,n} \dots (9)$$

406 Then, the sigmoid function is applied:

407
$$F_{n,t} = \sigma_n^S(f_{n,t}) \dots (10)$$

With the productions of the input gate and the forget gate, the cell state, C, is computed. In the cell state computations, the tanh activation function, σ^T are applied:

410
$$C_{n,t} = F_{n,t}C_{n,t-1} + I_{n,t}\sigma_n^T \omega_{c,n} [H_{t-1,n}, X_t] + b_{c,n} \dots (11)$$

411 Additionally, the input vector of predictors also pass through the output gate. The role of the

412 output gate is to control the flow from the cell state to the hidden state and ultimately producing

the output of the LSTM neuron (Chung et al., 2014). The output gate calculations are shownhere:

415 $o_{n,t} = \omega_{o,n} [H_{t-1,n}, X_t] + b_{o,n} \dots (12)$

416
$$O_{n,t} = \sigma_n^S(O_{n,t}) \dots (13)$$

417 Finally, with the product of the output gate, the hidden state, the information that passes to the

418 next layer (the FF layer), is computed. The figuration was as follows:

419
$$H_{n,t} = O_{n,t} \sigma_n^T C_{n,t} \dots (14)$$

420 The process continues through the FF layer to predict SF counts. Here, the FF had 16 neurons.

421 The RNN model underwent 1000 epochs, with a batch size of 32, a learning rate of 0.007, and a

422 sequence length of 6 days. The model was constructed via the Pytorch LSTM module (PyTorch,423 2023b).







424

425 Fig. 4 The hidden layer structure of the RNN.

426 3.4 Convolutional Neural Network

The CNN is also comprised of an input, hidden and output layer. The input layer and the 427 output product are the same as the FFN; hence, the main difference from the FFN is the 428 composition of the hidden layers. Particularly, the CNN has two convolutional layers, a global 429 average pooling layer and a FF layer. For the first convolutional layer, there are 16 kernels (or 430 filters), f, of size one (Each kernel is applied independently to each predictor at each time step). 431 Each filter produces an output, c, by generating a unique bias and weight at each time step, t, and 432 for each predictor. Therefore, in the CNN, the convolutional layers involve the weighted sum of 433 434 predictors over time for each filter; this differs from the FNN, as in the FNN, the predictions are based on the weighted sum of predictors without considering the time dimension. Fig. 5 435 436 illustrates the hidden layers of the CNN. The overview of computations are depicted here:

437
$$c_{f,t} = \omega_{f,t,SB}SB + \omega_{f,t,CB}CB + \omega_{f,t,MR}MR + \omega_{f,t,TR}TR + \omega_{f,t,SN}SN + b_{f,t} \dots (15)$$

The output of the first convolutional layer enters the second convolutional layer, c^{*}, via the
ReLU activation function and computes the following:

440 $C_{f,t} = \sigma(c_{f,t}) \dots (16)$

441 The second convolutional layer has 32 kernels, f^* . For each filter output, c^* , at a time step, the 442 calculation is shown:





443

$$c_{f^*,t}^* = \sum_{f=1}^{16} \omega_{f^*,t,C_{f,t}} C_{f,t} + b_{f^*,t} \dots (17)$$

The output of each kernel in the second convolutional also enters the ReLU function to gainenhanced pattern recognition:

446
$$C_{f^*,t}^* = \sigma(c_{f^*,t}^*) \dots (18)$$

- 447 After exiting the second convolutional process, there is input into the global average pooling
- 448 layer. For each of the 32 channels, p, an average, g, is taken across all time steps (3,652 days):

449
$$g_p = \frac{1}{3652} \sum_{t=1}^{3652} C_{f^*,t}^* \quad for \ f^* = p \ \dots (19)$$

- 450 Now, the pooling output units are then processed by a feed forward layer of 32 neurons,
- 451 producing predicted SF counts. The model was run with a learning rate of 0.001, batch size of 32
- 452 and 100 epochs. The model was constructed via the Pytorch CONV1D module (PyTorch,
- 453 2023a).



454

455 Fig. 5 The hidden layer structure of the CNN.





456 3.5 Graph Convolutional Neural Network

The main contribution of graph-based methods is the sharing of information via neighbors. 457 The input predictors are the same as the previous models; however, as opposed to assessing each 458 node's predictors singularly and running separate models for each, the input vector includes all 459 the nodes and their respective predictor values at each time step. Within the model, individual 460 461 assessments occur, and SF counts are produced for each node. At the hidden layer, the GCN begins the process by the creation of edges, the advanced communication channels between 462 nodes of locational proximity. In this study, each cluster represents a node, and the edges are 463 constructed such that each node is fully connected to every other node. Fig 6 illustrates the edges 464 connecting the clusters (nodes) of this study. An input vector of the dynamic predictors, X at 465 466 each time step is entered into each node, c. Additionally, X is also messaged into neighboring 467 nodes, N (those nodes connected to the node by edges), via aggregation by edge weights. The messaging, m, calculation, for a node is as follows: 468

$$m_c = \sum_{i \in N_c} \omega_{c,i} X_i \dots (20)$$

470 After messages are aggregated, feature representation is updated at the next time step:

471
$$X_{c,t+1} = f(X_{c,t}m_c) \dots (21)$$

The aggregated updated node representations occur within the graph convolutional layers. The

473 model is constructed via the Pytorch Geometric GCN module (PyTorch Geometric, 2023). There

are two convolutional layers, of which the model acquires knowledge of the effect each

475 neighbor's feature may have on another. The ReLU activation function was employed. The

476 learning rate was 0.001, and the GCN underwent 100 epochs.



478 Fig. 6 The graph structure of the GCN.





479 3.6 Graph Wavenet

The GWN is graph-based, with sophisticated recurrent and convolutional aspects. The key 480 advances from the GCN, RNN, and CNN are the additions of the adjacency matrix, A, dilation 481 factors, l, and skip connections. The input set of dynamic predictors and the output of predicted 482 SF counts are similar to the other graph-based models. Although, for the GWN, the arrangement 483 484 of the input differs. The input is a vector, D, which includes the nodes and the dynamic predictors per node for each sequence, q. Here, the sequence is 6; thus, the vector includes 485 information from t, t-1, and so forth until t-5. D then enters the A, along with the static attributes 486 (SIZ, SLP, ELV, LAT, LNG, and BLD), T. With the data, A makes informed decisions towards 487 graph construction and the determination of node neighbors, via edges. Moreover, for each 488 489 unique filter, A creates a unique transformed input vector for a particular node. Now, for each 490 node, n, there is a transformed input vector, described as follows:

491
$$X_{n,f} = f(D, T, q) \dots (22)$$

The transformed vectors for each node then enter convolutions. Recall from the CNN section,
that the convolution operation, c, is a function of the predictors, weights and biases, where the
weights and biases are unique for each time step and filter. It is similar here; however, for the
GWN, it is also a function of the dilation factor. For the GWN, the output of the convolution

496 operation will be referred to g:

497
$$g_{n,f} = f(X_{n,f}, \omega_f, b_f, l) \dots (23)$$

Next, g is split, where one enters into the tanh activation function, and the other is processed by
the sigmoid activation function. While information passes through the sigmoid and tanh
activation functions in the RNN, this occurs at sequential steps. Whereas, for the GWN, the
transformations by the sigmoid and tanh activation functions are brought together in elementwise multiplication. The determinations of the output tensors of the sigmoid activation function,
G^S, and the output of the tanh activation function, G^T, are shown here:

504
$$G_{n,f}^{S} = \sigma_{f}^{S}(g_{n,f})...(24)$$

505
$$G_{n,f}^{T} = \sigma_{f}^{T}(g_{n,f}) \dots (25)$$

506 An element-wise multiplication, M is then performed on both tensors.

507
$$M_{n,f} = G_n^S \odot G_n^T \dots (26)$$

The input tensor, M, then passes through a 1X1 convolution, where a point-wise convolution
operation takes place, reducing the hidden dimensions from 11 to one. The output, P, is described
here:

511
$$P_{n,f} = f(M_{n,f}, \omega_{n,f}, b_{n,f}) \dots (27)$$

512 Now, during this process, the original input tensor X is also preserved. It is added, elementwise,

513 to P, as to produce a residual connection, r. In this way, the output not only learns from the





transformed input, via convolutions and gating mechanisms, but it also learns from its originalinput.

$$r_{n,f} = P_{n,f} \oplus X_{n,f} \dots (28)$$

517 Meanwhile, there is another part of the output of the 1x1 convolution with a different utility. This518 output, known as a skip connection, will be designated as s:

519
$$s_{n,f} = f(M_{n,f}, \omega_{n,f}, b_{n,f}) \dots (29)$$

At this point, the calculations have been shown at the filter level. As explained in the CNN section, the calculations of each filter are aggregated to the layer level. Hence, describing the calculations at the layer level, the residual connection exiting the layer, y, will be denoted as R, and the skip connection exiting y will be denoted as S. For this model, R exits the filter and is utilized in subsequent skip connections, and S exits the filter, and residual connections from previous layers are incorporated to form a feedforward output, K. Let z represent the quantity of layer skips, then the calculation of K is as follows:

527
$$K_{y} = s_{n,f,y} \bigoplus \sum_{z=0}^{Z} R_{n,f,y-z} \dots (30)$$

528 The final output then undergoes a ReLU activation function, and the model prepares predictions

529 for SF counts on the testing dates. The process is shown in Fig. 7. For this study, the

530 hyperparameters for the GWN included a 0.01 learning rate, batch size of 15, and 50 epochs.



531

532 Fig. 7 A diagram depicting GWN configuration.





⁵³³ 4 Results and discussion

534 4.1 Risk Zones

535 Spectral clustering, an unsupervised machine learning technique, created six zones based on the flood attributes of each DIS. Fig 2 shows the predominance of each of the five characteristics 536 537 within a zone and plots total SF occurrence in each zone. By a visual analysis of the plots, elements of risk are conveyed. For instance, zone 2 is shown to have the highest mean incline 538 539 (Fig. 2b), allowing for water to flow, as opposed to ponding. Moreover, zone 2 has the greatest elevation (Fig. 2c) and the least number of buildings per unit area (Fig. 2d). A higher elevation 540 and lower quantity of buildings are known to reduce urban flood susceptibility. Subsequently, the 541 542 physical qualities of zone 2 may serve as a plausible explanation for the zone having the lowest total SF complaints (Fig. 2g). Similarly, zonal characteristics may also explain SF occurrence in 543 zone 1. When viewing Figs. 2b-d and Fig 2g, it is shown that zone 1 has the opposite extent, with 544 the flattest surface (low slope), lowest elevation, and the second highest number of buildings per 545 square unit; notwithstanding, zone 1 has the most SF reports. Thus, the extensive flood risk 546 547 characteristics of zone 1 may be the antecedent for its high complaints. Concerning the remaining zones, the prevalence of a combination of flood attributes is not as strongly skewed. 548 549 For example, zone 0, which has a low SF total, ranges mediumly in SLP, ELV, and BLD; although, it prevails on the higher end for FTP, and it has the greatest IMP. Regarding zone 3, 550 there are no extremes in flood characteristics; yet, zone 3 has the second highest total SF. With 551 zone 4, it has the highest BLD and FTP; yet the values of the other flood attributes extend 552 moderately. Lastly, concerning the box plot of zone 5, it does not depict many extremes in flood 553 554 characteristics, except a relatively low FTP and high IMP. Regarding total SF, zone 5 retains low SF reports (slightly higher than that of zone 0). Overall, via visual inspection, it appears that 555 some flood characteristics, particularly BLD, SLP, and ELV, maintain stronger effects on total SF 556 557 reports. This was also found in (Agonafir et al., 2022), where the random forest algorithm detected the relative importance of BLD, SLP, and ELV to be greater than IMP and FTP. For the 558 zones with moderate flood characteristics, modeling forecasting techniques, specifically machine 559 learning methods, have utility, as the algorithms possess the ability to detect intricacies within a 560 561 learned environment.

562 4.2 Model Results

563 4.2.1 Validation Results of Models

The evaluation of the models with varying complexities is conducted via the assessment of R² 564 values. Each model utilized a training set between 2010 to 2018 to produce daily predictions for 565 the testing range from 2018 through 2019, and goodness-of-fit was determined. Each model, 566 aside from the GLM, underwent 50 runs, and the average of the mean and median R² values of 567 568 all nodes were tabulated in Table 1. The model results are mapped, at the zonal level, in Fig. 8. Ordered from least to greatest, the results, depicting the mean R², for the models are the 569 following: GLM (0.26), FFN (0.35), RNN (0.36), CNN (0.36), GCN (0.43), and GWN (0.51). 570 Thus, the GWN is the model with the best performance. Moreover, the delta between the model 571 with the lowest R^2 (GLM) and the highest (GWN) is found to be significant at a value of 0.25. 572





- Furthermore, when only comparing ANNs, there is a 0.16 delta between the GWN's R^2 (highest) and FNN's R^2 (lowest). Lastly, inspecting the difference in R^2 between the simplest introduction of the feed forward (FFN) to the statistical model (GLM), there is a 0.09 delta, and between the
- 576 simplest graph neural network (GCN) to the GLM, there exists a 0.08 delta. Contiguously, the
- 577 results bring forth apparent connections. Firstly, there is notable performance improvement from
- the feed forward models (FFN, RNN, and CNN) to the GWN, while minimal (in some zones) to
- 579 no improvement exists from the FFN to the RNN or to the CNN. This indicates that LSTM and
- convolutional layers benefit from the extensive structural detail, such as gating mechanisms, $\frac{1}{2}$
- dilations, and skip connections, of the GWN. Secondly, as illustrated by the increase in \mathbb{R}^2
- sea achieved by the FFN when comparing to the GLM, a simple machine learning model
- 583 outperforms the generalized linear regression model. Finally, there is an overall improvement
- from the introduction of the graph architecture to the feed forward process, as highlighted by the
- 585 mean performance of the GCN being greater [by 0.07] than the RNN, and CNN. This suggests
- that the graph-based structure assists in environmental learning for certain datasets. Principally,
- 587 due to the substantial differences in model performance, this exploration proves that careful
- consideration must be taken when choosing an appropriate technique for forecasting endeavors.



589

Fig. 8 Maps of the mean R² values for each of the models in the exploration. The R² values of the GLM, FFN, RNN,
 CNN, GCN and GWN are shown in Fig. 8a, 8b, 8c, 8d, 8e, and 8f, respectively.

592

Table 1. A listing of the R^2 values for each model at each zone and the mean and median

594 determinations.





Zones	0	1	2	3	4	5	Median	Mean	
GLM	0.20	0.20	0.24	0.38	0.25	0.27	0.25	0.26	
FFN	0.26	0.39	0.17	0.57	0.39	0.34	0.35	0.35	
RNN	0.25	0.39	0.23	0.56	0.40	0.33	0.36	0.36	
CNN	0.26	0.39	0.22	0.57	0.40	0.34	0.36	0.36	
GCN	0.37	0.45	0.28	0.58	0.44	0.44	0.43	0.43	
GWN	0.35	0.59	0.31	0.72	0.55	0.52	0.54	0.51	
Median	0.26	0.39	0.24	0.57	0.40	0.34			
Mean	0.28	0.40	0.24	0.56	0.41	0.37			

595



596

597 Fig. 9 The bar plots of the mean R^2 of each model at each zone.

598 4.2.2 Zonal Analysis

599 As spectral delineation has created each zone with varying physical traits, analyzing the results at the zonal level provides additional insights into model strengths. First, it is essential to 600 inspect the relationship between R² (Fig. 9) and total SF per zone (Fig. 2g). There appears to be a 601 general trend, where R² values are greater in zones with a larger quantity of total complaints. For 602 instance, zones 0 and 2 have lower total SF reports, and the R² values for these zones are also the 603 604 lowest. Moreover, zone 3 has the second highest quantity of complaints, and it has the best performance of all models. Thus, more available response data appears to be a benefit to the 605 606 models. Moreover, the graph-based models significantly boost the quality of predictions, especially in the cases of zones 0 and 5. This may be attributed to the message-passage capability 607 608 of separate nodes (zones), such that a zone is not only learning its specific environment, but also





gaining a sense of the surroundings. Nonetheless, while there appears to be a positive link 609 between quantity of complaints and validation values, there are other factors influencing model 610 performance. For instance, zone 1 has the highest number of SF reports; yet, the mean R² values 611 are lower (0.40) than those of zone 4 (0.41), which has less than half the complaints. In addition, 612 zone 5 outperforms zone 0 in all models [by a difference of 0.09 mean R^2], despite having a 613 similar quantity of SF reports. These observations indicate the presence of other factors 614 influencing zonal differences in modeling prediction aptitude. For example, concerning zone 1, 615 616 additional variables may prove useful as model inputs. Specifically, zone 1 is comprised of regions mostly along the waterbodies of the Long Island Sound, Lower New York Bay, Jamaica 617 Bay, and the Atlantic Ocean; furthermore, this sector also has the lowest elevation. Thus, the 618 zone's vulnerability to sea level rise could be heightened due to a combination of low elevation 619 and proximity to water bodies. Accordingly, an additional variable expressing sea level rise may 620 benefit modeling endeavors for the zone. Regarding zone 0, the lower performance within the 621 cluster compared to zone 5 may be attributed to potential bias within the crowdsourced platform. 622 Agonafir et al found that commuters who drive are more likely to report SF (Agonafir et al., 623 2022). Given that zone 0 encompasses various Manhattan neighborhoods, and Manhattan is the 624 borough with the highest influx of commuters (City of New York, 2019), employing both public 625 transportation and vehicles, the crowdsourced response data may exhibit subtle inconsistencies, 626 posing challenges in detecting flooding patterns. Hence, the model performance in a zone may be 627 628 affected by the amount of SF complaints, an insufficient set of variables or bias in the crowdsourced platform. 629

Next, the zonal analysis will gear towards the examination of individual model performance. 630 631 An evident observation of the model results is the GWN exhibiting the highest R² [oftentimes, at a great margin] across all the zones, except for one. Now, as the sole deviation from this trend of 632 633 GWN dominance occurs at zone 0, the continued examination at the zonal level will begin at this curious exception. In the case of zone 0, the GCN outperforms the GWN by a marginal delta of 634 0.02. The difference is slight, as thus, considering the low volume of response data in the sector, 635 the variation likely does not hold significance in model comparison. Nevertheless, within zone 0, 636 637 there exist remarkable takeaways. The graph neural networks (GCN and GWN), when compared to the FFN, RNN, and CNN, demonstrate stronger prediction accuracies. As the differences 638 639 range from 0.09 to 0.12 in \mathbb{R}^2 values at zone 0, the results pronounce the benefits of the graph structure. The graph neural networks add value by not only including locational elements, but by 640 641 also allowing various areas to be connected and communicate with each other, and for a location, such as zone 0, with limited data, feeding a model with added information assists in the learning 642 643 of environmental patterns. This merit of the graph-based architecture is additionally seen when inspecting the results of zone 1, 2, 4, and 5. Specifically, zone 5, also with low response data (the 644 total SF complaints of zone 5 are less than a third of zone 3), obtains GCN and GWN R² values, 645 ranging from deltas of 0.10 to 0.19 greater than those of the non-graph-based ANN models. The 646 647 region where there is a balance in model performance between the GCN and the FFN, RNN, and 648 CNN is zone 3. Since zone 3 has a high number of SF complaints, the non-graph-based ANNs 649 are not as encumbered by low data volume; hence, their performance is competitive with the 650 GCN. Nonetheless, for all zones, the GWN transcends, and, due to key elements in the graph-





based neural network structure, such as neighboring nodal data gains, the GCN also attainsstrong prediction results.

Also, at a zonal inspection, it is observed that the ANNs overwhelmingly outperform the 653 GLM. The difference in \mathbb{R}^2 values from GLM to an ANN range from 0.05 to 0.17 for zone 0, 654 0.19 to 0.39 for zone 1, 0.18 to 0.34 for zone 3, 0.14 to 0.30 for zone 4, 0.06 to 0.25 for zone 5. 655 Hence, it is seen that the employment of even a simple neural network may have substantial 656 benefits to data-driven urban flood modeling. The only exception to the observation lies in zone 657 2. In zone 2, the GLM achieves a higher R^2 than the FFN, RNN, and CNN by a difference of 658 0.07, 0.01, and 0.02, respectively. Zone 2 has the lowest SF reports, at roughly half of the 659 response data as that of zone 0 (the zone with the second fewest) and less than one-eighth the SF 660 complaints as zone 1 (the zone with the highest SF complaints). Therefore, an inference is that 661 the GLM is not necessarily outperforming the other ANNs; however, due to very limited 662 response data, the other ANNs are not performing at their fullest aptitudes. 663

664 Finally, while the zonal analysis has illustrated the advantages of ANN modeling for urban flooding and the benefits of applying a graph-based structure, the examination principally 665 underscores the aptitude of the GWN. In Fig. 9, the comparative analysis demonstrates that 666 under conditions where the R^2 values of the FFN, CNN, or RNN edge closely to those of the 667 GCN, the GWN maintains a dominant performance. Conversely, when the validation 668 determinations of the GCN ascend the other ANNs, the GWN upholds its position. The observed 669 670 outcomes stem from the comprehensive nature of the GWN, incorporating key elements from 671 preceding ANN models. These advanced features include the integration of convolutional and LSTM layers and the incorporation of the self-adaptive adjacency matrix within the graph 672 architecture. Moreover, the structure within each component of the GWN are multiplexed, as 673 opposed to simple additions. In a latter section, 4.3 Graph Wavenet Deconstruction, the ancillary 674 complexities and their influence on model results will be explored in more detail. 675

676 *4.2.3 Feature Importance*

To illustrate how flood-related factors affect a model's performance, a feature importance 677 analysis is conducted. The infrastructural dynamic variables (SB and CB) are removed from each 678 model, and the results are compared against the original R^2 values of each model (when all the 679 680 variables are present). Likewise, the climatic dynamic variables (MR, TR, and SN) are also removed and compared against the original R² values. This approach, which assumes a linear 681 relationship between input variables and the target variable, provides insights into the 682 contributions of the variables in isolation. The difference in R² values for each set of variable 683 removal from the original R^2 is divided by the original R^2 to see the extent of effect. The results 684 are shown in Fig. 10. While acknowledging the simplicity of this method and its reliance on 685 linear relationships, it offers an interpretable way to rank the importance of dynamic predictors 686 within the context of the models. 687







688

689 Fig 10 Plots of R² decrease with variable exclusion.

There are a few notable observations of the feature importance results. First, the most 690 691 perceptible effect is that of the climatic variables on the GLM. The GLM experiences significant 692 decrease when the precipitation predictors are absent. As precipitation is the fundamental cause 693 of urban flooding, without its representation, the simplistic calculations of the GLM do not suffice for strong prediction capabilities. Next, it is seen that the performance of the FFN is more 694 reliant on the infrastructural variables than that of the CNN and RNN. An implication of this 695 finding may be that the CNN and RNN models have more adept utilization of the seasonality and 696 697 temporal nature of precipitation occurrence due to their enhanced spatial and sequential pattern recognition time-series data. Lastly, an observation is that the GWN appears to be less dependent 698 on either set of variables. Of all the models, the R² of the GWN decreases by the least relative 699 extent for both exclusions. This strengthens the assertion that the GWN is more robust, as it 700 possesses an improved capability of acquiring the environment, despite being given a lean set of 701 702 variables. Nonetheless, there are differences in performance decline, as the GWN performs better with the set of infrastructural-only variables. This observation may be attributed to its graph-703 704 based structure. Particularly, the graph-based models are aided by locational information, and the infrastructural predictors allow the models to sense the presence of chaos. If there are sewer 705 706 backups and catch basin issues reported throughout the city, the models are alerted towards a more probable occurrence of street flooding. On an ending note, the feature importance plots 707 identify model aptitude within a particular set of variables, further dissecting key model strengths 708 709 and limitations.





710 4.3 Graph Wavenet Deconstruction

The GWN, extending beyond a basic encompassment of the characteristics of the ANN 711 models in this study, elevates each fusion with intricate compositions and pathways. For 712 instance, in its graph-based structure, although the foundational nodes and messaging through 713 vertices (edges) are shared by the GCN, the GWN transcends with the incorporation of the 714 715 advanced adjacency matrix. The matrix, skillfully integrating static attributes and facilitating early temporal review through sequenced data during the node-edge creation process, provides 716 tailored inputs to each filter. Furthermore, in regards to the recurrent and convolutional aspects, 717 the GWN builds upon the passage of information via dilation factors and residual and skip 718 connections, exceeding the simplified structures of the RNN and CNN. Specifically, the RNN 719 720 features a feedback mechanism via the LSTM layer, which learns information via a lookback period of six days. While the GWN also includes a lookback of six days, the temporal learning 721 onsets at the adjacency matrix; additionally, the inputs proceed through gated activation 722 functions and merge by element wise multiplication, as opposed to sequential summation 723 724 processes. This careful procedure allows for improved biases and weights; moreover, it reduces 725 the occurrences of vanishing gradients or exploding activations, which are known risks of RNN 726 modeling (H. Lin et al., 2022; Rangapuram et al., 2018). Now, transitioning to the comparison of the convolutional structure between the GWN and the CNN, the layers of the GWN exhibit a 727 728 higher level of knowledge transfer. First, the dilation factor of the GWN allows for different convolutional layers to capture varying time ranges (Rathore et al., 2021); therefore, each layer 729 730 brings a distinctive evaluation of pattern recognition, allowing for a holistic perception of the temporal environment. Second, the residual and skip connections enable a direct extraction from 731 732 layers with pertinent information. To prevent distortion of the vital information as it passes sequentially layer to layer until reaching the current layer, the skip connections allow the current 733 layer to retrieve the information a previous (not immediately preceding) layer before it undergoes 734 subsequent convolutions. As thus, the sophistication of the GWN convolutions allow for a more 735 evolved and exclusive learning progression. Due to the complexity of the graph, recurrent and 736 737 convolutional fundaments, the GWN not only incorporates, but ascends.

To highlight the improvements facilitated by the added components of the GWN, an 738 additional model run is performed. In this GWN simulation (hereinafter referred to as GCR), the 739 740 adjacency matrix is excluded, while preserving spatial and temporal aspects. The mean and median R^2 values are determined to be 0.46 and 0.47, respectively (Table A1). When contrasting 741 the GCR with the GWN, which achieves mean and median values of 0.51 and 0.54, respectively, 742 the impact of excluding the adjacency matrix becomes evident. The GCR experiences a decrease 743 of 0.05 in the mean and 0.07 in the median. Additionally, at the zonal level, every cluster 744 demonstrates a reduction in performance. Furthermore, this isolation of the GWN from the 745 adjacency matrix emphasizes the vital role played by the intricate convolutional and recurrent 746 747 features of the GWN. Notably, the primary distinction between the GCN and GCR lies in the temporal and convolutional aspects. The results, wherein the GCR outperforms the GCN with a 748 mean and median \mathbb{R}^2 difference of 0.03 and 0.04, respectively, emphasize the strengths of 749 temporal and spatial learning introduced by the GWN. Therefore, as theorized, the success of the 750 GWN may be attributed to the multiple traits within the algorithm. 751





752 4.4 Limitations and Future Considerations

753 4.4.1 The FFN, RNN and CNN

The added complexities by the RNN and CNN yield minimal model performance. The FFN 754 obtains a mean R^2 value of 0.35, and the RNN and CNN each obtain mean R^2 values of 0.36. 755 Only in zone 2, there exists a substantive improvement by the RNN and CNN, where the R^2 756 values are 0.06 and 0.05 greater than the FFN, respectively. A plausible explanation for the 757 limited benefits is the simplicity of the model layers, of which lack the detail and mechanisms 758 needed to produce discernable results. This assertion gains credibility when considering the 759 performance of the GWN, where an interleaved system of data flow, employing skip connections 760 and advanced gating mechanisms, achieves superior prediction accuracy. Another contributing 761 factor may be the absence of significant temporal dependency within the dataset. Given the 762 763 nature of urban flooding, often ensuing in the form of a flash flood, where the onset and finality 764 of the disaster occurs within a brief timespan of 6 hours (NWS, 2022), flooding on one day, oftentimes, does not exert influence on the following day. Simplified models designed to capture 765 spatial and temporal dependencies may overlook these subtle patterns. Lastly, many of the 766 variables, including the response variable, are retrieved from the NYC 311 dataset, and 767 768 crowdsourced data is not as accurate in illustrating the environment as physical measurements. Thus, a simplified feedback loop or spatial assessment may not suffice. The limitations of the 769 crowdsourced platform are further discussed in the next section. In summary, while the neural 770 network architecture attains noticeable improvements in model performance, the basic LSTM or 771 convolutional layers are not as advantageous; this may be attributed to the temporal nature of 772 urban flooding and the limitations of crowdsourced data. 773

4.4.2 The Crowdsourced Platform

Crowdsourcing has been applied in previous urban flood modeling initiatives, particularly in 775 cities like NYC, where flood data is scarce. The incorporation of residential reports provides 776 insights into flooding occurrences, of which, otherwise, would not be obtained. However, while 777 this method is valuable, the leveraging of eyewitness accounts is not as exact as physical 778 measurements. Also, another issue of crowdsourced data is the potential for bias – a greater 779 780 inclination of certain types of people to report issues. For example, it has been indicated that certain socio-demographical attributes may be factors in SF complaints, thereby possibly 781 indicating that a particular set of residents are more likely to utilize the platform (Agonafir et al., 782 2022). Hence, there are bias concerns. Nonetheless, there exists strength in the reports, as they 783 are taken by individuals observing an event. For instance, the bias attributed to socio 784 785 demographics is a *potential* consideration, since it may also be inferred that specific neighborhoods prone to flood occurrences may be comprised of a certain set of socio-786 787 demographics. Moreover, the validity of the crowdsourced data's depiction of flooding occurrence is reinforced by the climatic, topographical, and infrastructural predictors holding 788 substantial significance in the crowdsourced response variable, SF complaints (Agonafir et al., 789 2021, 2022). Furthermore, the 311 NYC street flooding reports, at the very least, capture the 790 791 concerns of residents inclined to report, potentially identifying those most at personal risk. Indeed, the attribute of commuters who drive holds a sizable relative importance in Agonafir et 792





al. (Agonafir et al., 2022), and as the leading cause of death from flooding is vehicular, accurate
predictions in these regions may prove lifesaving. In essence, in metropolitans with limited data,
crowdsourcing, despite some drawbacks, enables the continuity of predictive modeling,
sustaining efforts that would otherwise cease.

797 Moreover, in metropolitans, particularly in the specific study area of NYC, flood sensors 798 [measuring water levels] are being installed, enabling proximate applicability of this explorative analysis. The findings presented here accentuate the models best suited for the local landscape, 799 with the GWN delivering promising results. Despite the constraints of the crowdsourced 800 platform, the GWN attains an R^2 of 0.72 for zone 3, demonstrating its potential. Anticipating 801 even greater predictive accuracy with actual measurements from sensors, this study outlines 802 803 techniques applicable to the urban city. Once physical data becomes accessible, this model exploration provides policymakers and stakeholders with an outline of the strengths and 804 weaknesses of models, ascending in complexity, while also pinpointing the overall, most 805 effective model for forecasting floods during a predicted rain event. 806

807 5. Conclusions

By a diverse, novel pooling of machine learning techniques, this study advances our understanding of urban flooding, offering detailed insights into risk zones, comparing the performance of various models, and emphasizing the effectiveness of graph-based neural networks, particularly the Graph Wavenet. Listed below are the key appreciations of the research:

813	٠	Spectral clustering has utilization in risk zone identification and border delineation. The
814		analysis of these zones reveals relationships between specific physical characteristics
815		(such as slope, elevation, and building density) and the occurrence of street flooding.
816		Notably, zones with higher elevation and lower building density exhibited lower
817		susceptibility to flooding, emphasizing the importance of urban characteristics in flood
818		risk assessment.

- Machine learning models demonstrate superior performance to the GLM. Unlike the
 GLM, which assumes linearity in the parameters, machine learning models offer greater
 flexibility by adapting to complex, nonlinear patterns present in the data.
- By a systematic evaluation of the performance of varying flood prediction models,
 ranging from traditional statistical models to advanced neural networks, the GWN
 emerges as the most suitable model for urban flood forecasting in NYC, outperforming
 other models, including the GCN, CNN and RNN. Hence, there is significance in
 incorporating advanced spatio-temporal aspects and dynamic graph creation for accurate
 flood forecasting.
- Via zonal analysis, graph-based structures are shown to be particularly beneficial in areas
 with sparse data, where traditional models may struggle.

The discoveries of this research accord practical value onto urban stakeholders, especially in
cities such as NYC, where water measurement sensors are currently being deployed. This
synergy between advanced modeling techniques, particularly spatio-temporal graph neural





- 833 networks, and emerging sensor technologies ensures informed decision-making, enabling urban
- 834 planners and emergency responders to safeguard communities, reduce economic losses, and
- enhance overall resilience to the challenges posed by urban flooding.
- 6. Appendix A

837 Table A.1

Zones	0	1	2	3	4	5	Median	Mean
GCR	0.29	0.56	0.28	0.68	0.52	0.42	0.47	0.46

838

839 7. Code Availability

- The processed data and the codes used in this study are available from the corresponding authors upon reasonable request.
- 842 8. Data Availability
- 843 Physical, topographical, and crowdsourced data from this study are publicly available at NYC
- 844 Open Data and NYC311. Radar and gauge data are available from EOL/UCAR and NOAA
- 845 databases, respectively.

846 9. Author Contribution

- 847 Candace Agonafir: Conceptualization, Data Curation, Formal Analysis, Investigation, Methodology,
- 848 Software, Validation, Visualization, Writing Original Draft and Preparation. **Tian Zheng**:
- 849 Conceptualization, Formal Analysis, Funding Acquisition, Methodology, Project Administration,
- 850 Resources, Supervision.

851 10. Competing Interests

852 The authors declare that they have no conflict of interest.

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