

How well can brightness temperature differences of spaceborne imagers help to detect cloud phase? A sensitivity analysis regarding cloud phase and related cloud properties

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Abstract. This study investigates the sensitivity of two brightness temperature differences (BTDs) in the infrared (IR) window of the SEVIRI imager to various cloud parameters in order to understand their information content, with a focus on cloud thermodynamic phase. To this end, this study presents radiative transfer calculations, providing an overview of the relative importance of all radiatively relevant cloud parameters, including thermodynamic phase, cloud top temperature (CTT), optical thickness (τ), effective radius (R_{eff}) and ice crystal habit. By disentangling the roles of cloud absorption and scattering, we are able to explain the relationships of the BTDs to the cloud parameters on the one hand by spectral differences in the cloud optical properties. In addition, an effect due to the nonlinear transformation from radiances to brightness temperatures contributes to the specific characteristics of the BTDs and their dependence on τ and CTT. We find that the dependence of the BTDs on phase is more complex than sometimes assumed. Although both BTDs are directly sensitive to phase, this sensitivity is comparatively small in contrast to other cloud parameters. Instead, the primary link between phase and the BTDs lies in their sensitivity to CTT (or more generally the surface–cloud temperature contrast), which is associated with phase. One consequence is that distinguishing high ice clouds from low liquid clouds is straightforward, but distinguishing mid-level ice clouds from mid-level liquid clouds is challenging. These findings help to better understand and improve the working principles of phase retrieval algorithms.

1 Introduction

Passive spaceborne imagers, with their wide field of view and, in the case of geostationary satellites, high temporal resolution, allow global observations of clouds. These passive instruments typically use solar and/or infrared (IR) window channels to retrieve cloud properties. The advantage of pure IR-based retrievals is that they can be applied during both daytime and nighttime (Nasiri and Kahn, 2008; Cho et al., 2009). Such IR retrievals often use brightness temperature differences (BTDs) of IR window channels, to detect clouds or retrieve cloud properties like optical thickness (τ) or effective particle radius (R_{eff}) (e.g., Inoue, 1985; Krebs et al., 2007; Heidinger et al., 2010; Garnier et al., 2012; Kox et al., 2014; Vázquez-Navarro et al., 2015; Strandgren et al., 2017).

Another cloud parameter which is often retrieved using BTDs (either alone or in combination with other measures) is the cloud thermodynamic phase (ice, liquid, mixed) (Ackerman et al., 1990; Strabala et al., 1994; Finkensieper et al., 2016; 25 Key and Intrieri, 2000; Baum et al., 2000, 2012; Hünerbein et al., 2022; Benas et al., 2023; Mayer et al., 2024). Accurate satellite retrievals of cloud phase are important for various reasons. Firstly, the cloud phase plays an important role in cloud-radiation interactions (Komurcu et al., 2014; Choi et al., 2014; Matus and L'Ecuyer, 2017; Ruiz-Donoso et al., 2020; Forster et al., 2021; Cesana et al., 2022). Several studies highlight its impact on climate sensitivity within general circulation models (Gregory and Morris, 1996; Doutriaux-Boucher and Quaas, 2004; Cesana et al., 2012; Tan et al., 2016; Bock et al., 2020). 30 Accurate observations of the cloud phase are thus essential to improve cloud representation in climate models (Cesana et al., 2015; Atkinson et al., 2013; Matus and L'Ecuyer, 2017; Bock et al., 2020). Additionally, determining cloud phase is often a prerequisite in the remote sensing retrieval of cloud properties, including τ , R_{eff} and water path (Marchant et al., 2016).

However, determining cloud parameters such as the thermodynamic phase from BTDs is a challenging task. Radiative transfer through clouds and the atmosphere is complex, with many parameters that can in principle influence satellite observations. 35 Although radiative transfer models are capable to correctly account for all of these quantities, the relative importance of these parameters is often not fully understood.

Ackerman et al. (1990) were the first to observe a correlation between BTDs in High-Resolution Interferometer Sounder (HIS) data and the different cloud phases as determined by concurrent lidar data. They proposed a trispectral technique to distinguish between ice, water, and clear sky using the BTDs between channels at about $8 \mu\text{m}$ and $11 \mu\text{m}$ (BTD(8.0-11.0)) and 40 between channels at about $11 \mu\text{m}$ and $12 \mu\text{m}$ (BTD(11.0-12.0)). Strabala et al. (1994) expanded on their findings, using MODIS airborne simulator data. They considered clouds of varying τ and found that distinguishing between ice and water clouds using these BTDs is difficult for optically thin clouds. Parol et al. (1991) and Dubuisson et al. (2008) studied the sensitivity of BTDs to effective radius R_{eff} and particle shape for cirrus clouds. Parol et al. (1991) found that the BTD(11.0-12.0) for the Advanced Very High Resolution Radiometer AVHRR aboard the NOAA satellites is sensitive to whether cloud particles are spherical or 45 non-spherical. Dubuisson et al. (2008) showed that the impact of different non-spherical ice crystal shapes on BTD(10.6-12.0) and BTD(8.7-10.6) of the Infrared Imaging Radiometer IIR aboard CALIPSO is small compared to their sensitivity to R_{eff} . The effect of R_{eff} on the BTDs was also considered by Baum et al. (2000), who further extended the trispectral method for MODIS phase retrievals by incorporating information about the horizontal variability of the BTDs. Similar to the study of Strabala et al. (1994), the radiative transfer simulations of Baum et al. (2000) primarily focused on low-level water clouds and 50 high cirrus clouds, and did not consider midlevel clouds. To bridge this gap, Nasiri and Kahn (2008) conducted a sensitivity study that considered also midlevel clouds for the MODIS BTD(8.5-11.0). They showed that BTD(8.5-11.0) is sensitive to cloud top height (CTH) and that this leads to limitations in the phase discrimination in the cloud temperature regime where both liquid and ice can exist.

These studies show that many different parameters influence the BTDs: Cloud parameters considered in previous studies 55 include thermodynamic phase, τ , R_{eff} , ice crystal habit, and CTH. As outlined above, most of the studies so far have however each focused on only a small number of these cloud parameters; an overview over the relative importance of all these cloud parameters is still missing. Especially the influence of CTH or cloud top temperature (CTT) on BTDs has not been studied in

60 detail, with exception of Nasiri and Kahn (2008). Besides cloud parameters also the amount of water vapor in the atmosphere (mainly above the clouds) affects BTDs even in the (relatively) transparent spectral window region 8–12 μm . This has been pointed out by several authors (Strabala et al., 1994; Nasiri and Kahn, 2008; Dubuisson et al., 2008), but the relative importance of atmospheric absorption compared to cloud parameters on BTDs has not been studied systematically.

In addition, the origin of the dependence of BTDs on cloud thermodynamic phase, as observed in satellite measurements and radiative transfer results, is not fully understood. Although phase retrievals are usually based on accurate radiative transfer calculations that take into account all radiative effects, it is argued that variations in the refractive indices of ice and water across the infrared window cause the BTDs to be sensitive to cloud phase (Finkensieper et al., 2016; Key and Intrieri, 2000; Baum et al., 2000, 2012). However, besides these effects of the cloud phase, the phase also correlates with other cloud parameters like CTT and R_{eff} , which in turn have large effects on the BTDs as mentioned above. It is not fully understood which cloud parameters dominate the response of the BTDs in given cloud scenarios. Additionally, traditional explanations of the phase dependence of BTDs have often neglected scattering effects, which as we will show can be substantial. Thus, it is not well understood which physical processes are responsible for the observed phase dependence of the BTDs. A full understanding of the satellite channel dependencies is however critical to design optimal cloud (phase) retrievals and to understand their limitations.

To compute BTDs, satellite radiances are first transformed into brightness temperatures (BT). This transformation by means of Planck's radiation law is a nonlinear function. As nonlinear functions can lead to unexpected behaviour, we expect that there are some effects of the nonlinear relationship between satellite radiances and BTs on BTDs. To our knowledge, the effect of this nonlinear relationship has not been analysed before.

We use Radiative Transfer (RT) calculations to study two BTDs of the SEVIRI imager aboard Meteosat Second Generation (Schmetz et al., 2002): The BTDs between the IR window channels centered at 8.7 and 10.8 μm (BTD(8.7-10.8)) and between those centered at 10.8 and 12.0 μm (BTD(10.8-12.0)). These are the BTDs that are mainly used to identify cloud top phase and determine (ice) cloud properties. Figure 1 shows an example scene of SEVIRI as RGB composite and the two BTDs for the same scene. In this study we first investigate the effect of the nonlinear relationship between radiances and BTs on the BTDs. We then use the RT calculations to analyse dependencies and sensitivities of the BTDs with respect to all radiatively important cloud parameters, namely phase, CTT, R_{eff} , ice crystal habit and optical thickness (τ) at 550 nm, disentangling effects of cloud particle scattering and absorption. We also consider the effect of water vapor in the atmosphere on BTDs by comparing the computed BTDs with scenarios without molecular absorption. The findings of these RT calculations are then used to analyse the information content of the BTDs with respect to cloud phase. Overall in this study we focus on the effect of cloud parameters; the effects of other parameters like viewing angle, surface emissivity or atmospheric temperature profiles are not studied.

The aim of this study is twofold: First, it provides an analysis of the effects of all cloud parameters on the two BTDs, disentangling the interactions among the different parameters. Second, this study improves the physical understanding of the role of the different radiative processes leading to different BTD values. This helps to understand the information content of the BTDs with respect to the thermodynamic phase in order to better understand and improve the working principles of phase

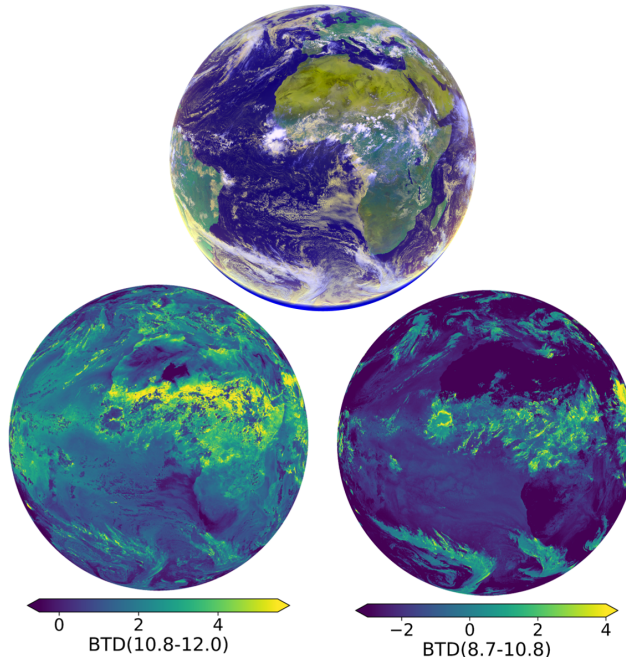


Figure 1. Example scene from SEVIRI on 11.06.2023, 12:00 UTC. Top row: RGB composite with yellow cloud colours indicating higher CTTs; white/blue indicating lower CTTs. Bottom row: the two BTDRs for the same example scene.

retrieval algorithms that use BTDRs and to understand their uncertainties and limitations. We focus on the phase, but our results are also useful to better understand the dependencies of BTDRs for other remote sensing applications where they are typically used, such as the retrieval of τ and R_{eff} . Since BTDRs also depend on atmospheric and surface parameters whose effects are not studied here, this study does not aim at explaining every phenomenon encountered with BTDRs. However, understanding the effects of the cloud parameters helps to disentangle different physical cloud-related processes in all atmospheric or surface conditions.

Finally, we note that besides BTDRs, there are other popular methods for retrieving cloud phase and other cloud properties, such as β ratios (Parol et al., 1991; Pavolonis, 2010; Heidinger et al., 2015). While this study is specifically aimed at BTDRs, understanding the effects of different cloud properties on the radiative transfer through clouds is also useful to better understand the physics underlying β ratio retrievals.

2 Physical background

To visualize relationships and dependencies between radiation at top of atmosphere (TOA) and cloud properties, the representation in form of a causal diagram is very useful. Figure 2 shows cloud parameters that are related to the cloud phase, connected by arrows indicating causal relationships. Other factors influencing the radiation at TOA (in particular passive satel-

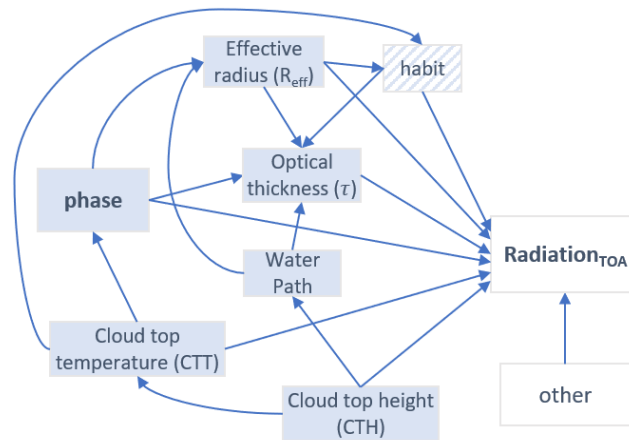


Figure 2. Causal diagram of cloud parameters that are connected to the cloud phase. Arrows indicate causal links.

lite observations), like satellite viewing angles, surface temperature or atmospheric properties, are summarized under "other" in the diagram.

In this paper we use the terms "direct" and "indirect" influence of the cloud phase on the TOA radiation. Direct influence means the effect of changing the cloud phase while all other cloud parameters (R_{eff} , CTT, τ , ...) remain the same (represented by the arrow from phase to TOA radiation in Fig. 2). The indirect influence of the cloud phase is represented by all other paths from phase to TOA radiation in Fig. 2. For example, the phase affects τ and R_{eff} , which in turn affect TOA radiation. Information on these two parameters can give an indication about the cloud phase – e.g. clouds with small R_{eff} are typically liquid clouds; clouds with very low τ are typically ice clouds. Ice crystal habit can influence the TOA radiation as well, but is of course only relevant for ice clouds. CTT and CTH are closely related variables that influence radiation through temperature-dependent cloud emissions and by affecting the atmospheric column above the cloud that can absorb radiation, respectively. CTT is critical for phase determination since for temperatures above 0°C only liquid and below -40°C only ice is physically possible. Between these thresholds, the probability for ice (liquid) clouds increases (decreases) as CTTs get colder (Mayer et al., 2023).

In order to calculate the radiative transfer through a cloud with given cloud (microphysical) parameters, it is necessary to know how much radiation is absorbed, scattered and emitted, i.e. the optical properties of the cloud. The translation from cloud (microphysical) parameters to optical parameters is given by the so-called *single scattering properties*. The single scattering properties are the volume extinction coefficient β_{ext} , the single scattering albedo ω_0 and the scattering phase function p . As an alternative to β_{ext} and ω_0 one can equivalently describe radiative transfer by the absorption coefficient β_{abs} and scattering coefficient β_{sca} , which can be easier to interpret. Definitions and physical interpretations of the single scattering properties can be found in appendix A. The interplay of the single scattering properties, in combination with the cloud water path, determines how much radiation is transmitted through a cloud and, in combination with the cloud temperature, how much radiation is emitted from it. The single scattering properties depend on the wavelength of the radiation and on the cloud parameters R_{eff} ,

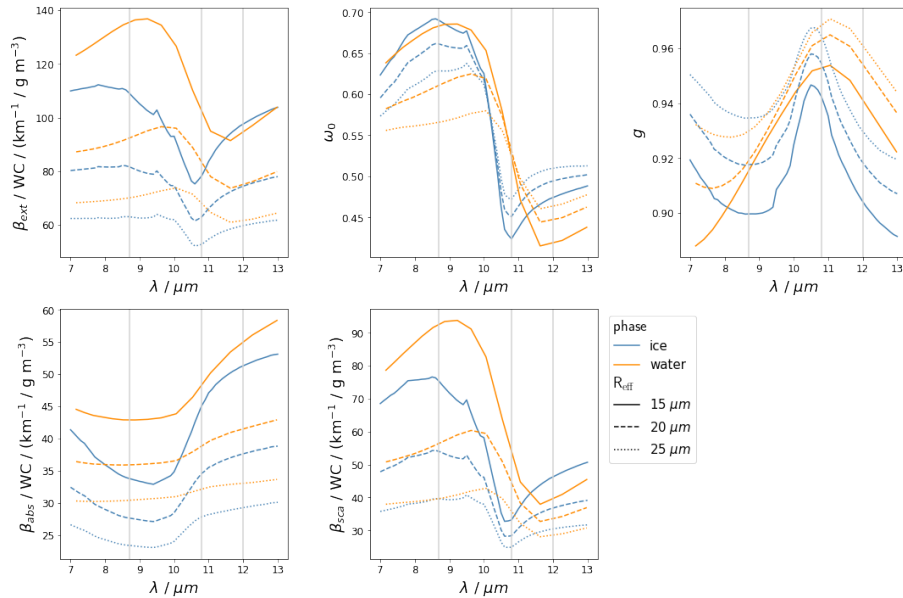


Figure 3. Single scattering properties extinction coefficient β_{ext} , single scattering albedo ω_0 and asymmetry parameter g , as well as absorption coefficient β_{abs} and scattering coefficient β_{sca} (computed from β_{ext} and ω_0) as functions of wavelength for varying cloud phase and effective radius R_{eff} . β_{ext} , β_{abs} and β_{sca} are scaled by the cloud water content WC. Parameterisations for ice according to Baum et al. (2011), for liquid droplets according to Mie theory. For ice clouds, the "general habit mix" was used as ice crystal habit. Vertical grey lines indicate the centre wavelengths of the three IR window channels.

130 habit and phase. They are shown in Fig. 3 for varying R_{eff} and cloud phase. The variations of the single scattering properties due to habit are mostly small in comparison and therefore not shown. Instead of p we show the asymmetry parameter g , as a simpler measure to characterize the scattering process (see appendix A). The spectral variations of β_{abs} , β_{sca} and g translate into different BTD values for different cloud parameters. This will be investigated in detail in the next sections using radiative transfer calculations.

3 Radiative transfer calculations

135 Simulations for the three IR window channels of the SEVIRI instrument centered at 8.7, 10.8 and 12.0 μm were performed for a variety of water and ice clouds using the sophisticated radiative transfer package libRadtran (Mayer and Kylling, 2005; Emde et al., 2016; Gasteiger et al., 2014). LibRadtran represents water and ice clouds in detail and realistically. It has been validated against observations and in several model intercomparison campaigns and has been extensively used to develop or validate remote sensing retrievals (e.g. Mayer et al., 1997; Meerkötter and Bugliaro, 2009; Bugliaro et al., 2011; Stap et al., 140 2016; Piontek et al., 2021b; Bugliaro et al., 2022). The optical properties of water droplets are calculated using Mie theory. For ice crystals, we use the Baum et al. (2011) parameterization of optical properties for three different habits (general habit

mixture, columns, rough aggregates). Simulations of TOA radiances for the SEVIRI IR window channels are made using the one-dimensional radiative transfer solver DISORT (Discrete Ordinate Radiative Transfer) 2.0 by Stamnes et al. (2000) and Buras et al. (2011) with parameterized SEVIRI channel response functions as described by Gasteiger et al. (2014). The complete permutation of τ , R_{eff} , CTT/CTH, crystal habits and phase was simulated and is listed in table 1. The CTT is set to the atmospheric temperature at the altitude of the CTH and represents the temperature at cloud top. For simplicity we keep the cloud geometric thickness constant at 1 km; the impact of variable geometric thickness is discussed in Sect. 6.3. We only consider single-phase (ice or water) and single layered clouds. True mixed-phase clouds and multilayered clouds are not considered.

The simulation setup in terms of atmosphere, satellite/solar geometry and surface type is summarized as well in table 1. In this study, we focus on the influence of cloud parameters. Therefore, we choose a relatively simple setup for the atmospheric parameters, surface parameters and satellite geometry, which is kept constant for all simulations. We use the US standard atmosphere (Anderson et al., 1986) and a surface temperature of 290 K. We place the simulations over the ocean where the surface emissivity is nearly constant for the three IR window channels and set it to 1. The satellite zenith angle (SATZ) is kept constant at 0° (nadir view).

To disentangle cloud effects from effects of the atmosphere, we also compute simulations with molecular absorption switched off. LibRadtran further has the possibility to simulate the IR window channels for cloud layers for which scattering is switched off, meaning that the scattering coefficient in the simulation is set to zero while the absorption coefficient remains constant. This allows to disentangle effects of scattering and absorption in a cloud.

160 4 Effects of Planck's law: the BTD Nonlinearity Shift

Before analysing the results of the RT calculations, we examine the effects of the nonlinear relationship between radiances and BTs on the BTDs. We call these effects *BTD Nonlinearity Shift*. The BTD Nonlinearity Shift is purely due to the nonlinearity in the computation of BTDs and not due to wavelength dependent optical properties of the cloud, which we will focus on in the next sections of this study. BTDs are calculated from measured radiances using Planck's radiation law, which describes the spectral radiance B_λ of a black body emitting radiation at temperature T

$$B_\lambda(T) = \frac{2hc^2}{\lambda^5} (e^{\frac{hc}{\lambda k_B T}} - 1)^{-1}, \quad (1)$$

where h is the Planck constant, c is the speed of light in vacuum and k_B is the Boltzmann constant. The inverse Planck function accordingly maps spectral radiance R_λ to the corresponding temperature

$$T_\lambda(R_\lambda) = \frac{hc}{k_B \lambda} \frac{1}{\ln\left(\frac{2hc^2}{\lambda^5 R_\lambda} + 1\right)} \quad (2)$$

and is used to compute BTs from measured radiances in remote sensing.

The simplest version of the BTD Nonlinearity Shift can be explained using the Schwarzschild equation for radiative transfer. The Schwarzschild equation is a simple version of radiative transfer assuming no cloud scattering and no atmosphere. Its

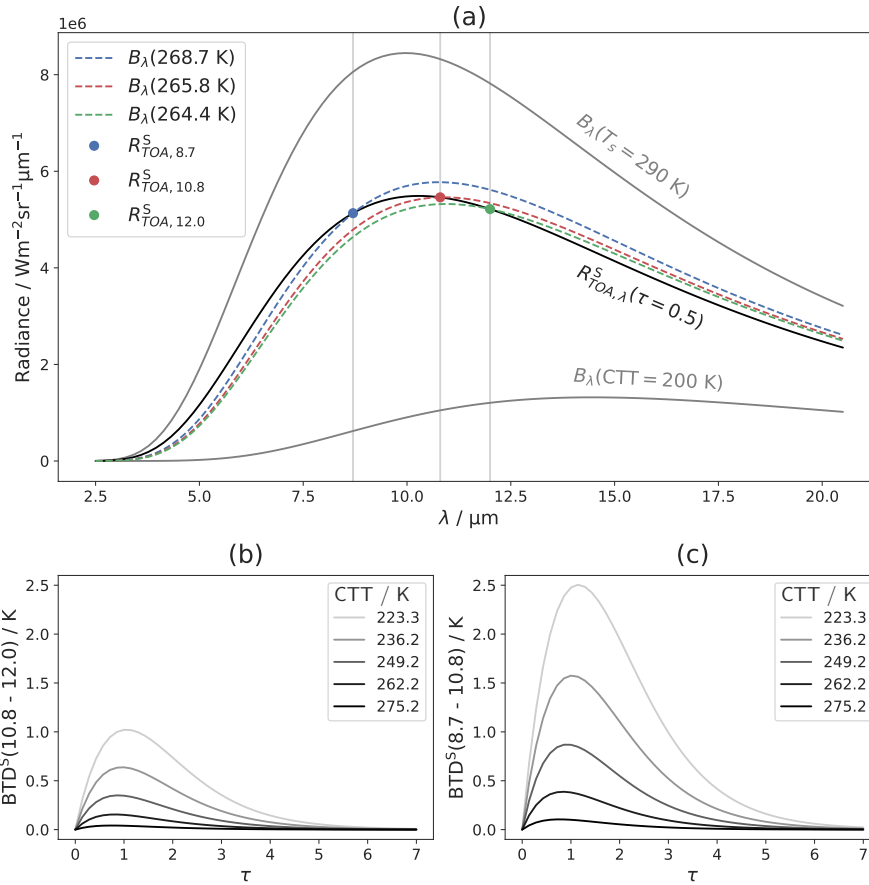


Figure 4. (a) Radiance at top of atmosphere ($R_{\text{TOA},\lambda}^S$) computed with the Schwarzschild equation (black line). Vertical grey lines indicate the centre wavelengths of the three IR window channels with blue, red and green dots at $R_{\text{TOA},8.7}^S$, $R_{\text{TOA},10.8}^S$ and $R_{\text{TOA},12.0}^S$ respectively. The blue, red and green dashed lines correspond to the Planck curves of these three TOA radiances, i.e. $B_\lambda(T_\lambda(R_{\text{TOA},\lambda}^S))$ for each wavelength, where B_λ is the Planck function and T_λ the inverse Planck function. The grey solid curves show the Planck curves of the surface temperature T_s and the CTT as reference. (b) Brightness temperature differences computed with the Schwarzschild equation, BTD^S , as functions of τ for different CTTs and a fixed $T_s=290 \text{ K}$.

Table 1. Setup and cloud Properties for libRadtran radiative transfer calculations (SATZ = satellite zenith angle, SKT = skin temperature)

cloud properties	
phase	liquid, ice
R_{eff} (liquid clouds)	5, 10, 15, 20 μm
R_{eff} (ice clouds)	20, 30, 40, 50 μm
τ	0, 0.1, 1, 2, 3, 5, 7, 10, 15, 30
ice habit	general habit mix (ghm), rough aggregates, solid columns
optical properties	for ice after Baum et al. (2011) for liquid droplets Mie
CTH (liquid clouds)	1, 2, 4, 6, 8 km
CTT* (liquid clouds)	281.7, 275.2, 262.2, 249.2, 236.2 K
CTH (ice clouds)	4, 6, 8, 10, 12 km
CTT* (ice clouds)	262.2, 249.2, 236.2, 223.3, 216.7 K
geometric thickness	1 km
cloud particle scattering	on / off
* corresponds to CTH	
setup of atmosphere, geometry and surface	
atmosphere	US-standard (total column water vapor: 14.3 kg/m ²)
molecular absorption	on / off
SATZ	0°
SKT	290 K
surface type	ocean

solution for one cloud layer is

$$R_{\text{TOA},\lambda}^{\text{S}}(\tau_{\lambda}) = e^{-\tau_{\lambda}} B_{\lambda}(T_s) + (1 - e^{-\tau_{\lambda}}) B_{\lambda}(\text{CTT}), \quad (3)$$

175 where $R_{\text{TOA},\lambda}^{\text{S}}$ is the radiance at TOA at a given wavelength λ with the superscript S for Schwarzschild, and τ_{λ} is the optical thickness of the cloud for this wavelength. The first term in the equation is the transmitted radiance coming from the surface with the surface temperature T_s ; the second term is the radiation emitted by the cloud, assuming that the cloud layer has an approximately constant temperature $T \approx \text{CTT}$. To demonstrate the BTM Nonlinearity Shift we set τ_{λ} equal for all wavelengths,

$\tau_\lambda = \tau$. Figure 4(a) shows the Planck function of the surface temperature, $B_\lambda(T_s)$, and the cloud temperature, $B_\lambda(\text{CTT})$, in grey for exemplary values of $T_s = 290 \text{ K}$ and $\text{CTT} = 200 \text{ K}$. According to the Schwarzschild equation (Eq. 3), $R_{\text{TOA},\lambda}^{\text{S}}$ lies between these two curves, approaching $B_\lambda(T_s)$ for $\tau \rightarrow 0$ and $B_\lambda(\text{CTT})$ for $\tau \rightarrow \infty$. Figure 4(a) illustrates $R_{\text{TOA},\lambda}^{\text{S}}$ for $\tau = 0.5$ (black line). From $R_{\text{TOA},\lambda}^{\text{S}}$ we can now compute the TOA BTs at the three IR wavelengths of interest as $\text{BT}_\lambda^{\text{S}} = T_\lambda(R_{\text{TOA},\lambda}^{\text{S}}(\tau))$, where the superscript S again stands for Schwarzschild. The corresponding Planck curves, i.e. $B_\lambda(\text{BT}_\lambda^{\text{S}})$ for $\lambda \in \{8.7, 10.8, 12.0\}$, are shown in Fig. 4(a) as dashed colored lines. Recall that in this example calculation we have set a constant $\tau = 0.5$, i.e. the same optical properties (transmittance and emissivity) for all wavelengths (see Eq. 3). Naively, one might expect a $\text{BTD} = 0$ (i.e. equal BTs) in this scenario. However, it is evident from the figure that the three BTs are different, with $\text{BT}_{8.7}^{\text{S}} > \text{BT}_{10.8}^{\text{S}} > \text{BT}_{12.0}^{\text{S}}$. Since these differences between the three BTs are not due to optical cloud properties, they must be caused by the nonlinear transformation from radiances to BTs. Hence, the BTD Nonlinearity Shift induces a BTD in situations where, naively, no BTD would be expected.

To get an overview of the BTD Nonlinearity Shift, we compute BTD^{S} for both wavelength combinations ($\text{BTD}(8.7-10.8)$ and $\text{BTD}(10.8-12.0)$) from the results of the Schwarzschild equation (Eq. 3) for varying τ and CTT as

$$\text{BTD}^{\text{S}}(\lambda_0 - \lambda_1) = T_{\lambda_0}(R_{\text{TOA},\lambda_0}^{\text{S}}(\tau)) - T_{\lambda_1}(R_{\text{TOA},\lambda_1}^{\text{S}}(\tau)). \quad (4)$$

Fig. 4(b) shows the computed BTD^{S} as a function of τ for different CTTs and a fixed $T_s = 290 \text{ K}$. These BTD^{S} resemble an arc shape (similar to the well-known BTD arc from Inoue (1985)) and show higher values for lower CTTs, even though the amplitudes of their curves are smaller than for the full RT model, as we will see later. Thus, even if τ_λ is the same for all three wavelengths, $\tau_\lambda = \tau$, the nonlinearity of the inverse Planck function induces positive BTD^{S} values and a dependence on the CTT. More generally, this dependence is mainly a sensitivity to the thermal contrast $\Delta T := T_s - \text{CTT}$; however, for a fixed T_s , as shown in the examples here, it reduces to a dependence on CTT. Notice that for these examples the BTD induced this way reaches up to 2.5 K and thus cannot be neglected.

In the next section we will discuss the effects of cloud properties on the BTDs due to the wavelength-dependent optical properties in the full RT model (described in Sect. 3). The BTD Nonlinearity Shift adds to these effects and is therefore co-responsible for the (positive) BTD values and the CTT dependence of the BTDs which we will discuss in more detail in Sect. 5.6. In appendix B we further analyse the BTD Nonlinearity Shift for the Schwarzschild model as well as the full RT model and disentangle this nonlinearity effect from the physical effects of wavelength-dependent optical properties on the BTDs in RT calculations.

Summarizing this section:

- There is an effect (BTD Nonlinearity Shift) coming from the nonlinearity of the inverse Planck function that induces positive $\text{BTD}(8.7-10.8)$ and $\text{BTD}(10.8-12.0)$ values and a dependence on the CTT (or more generally the surface-cloud-temperature contrast ΔT) in a simple RT model (Schwarzschild equation) even if cloud optical properties (transmittance and emissivity) are the same for all wavelengths.

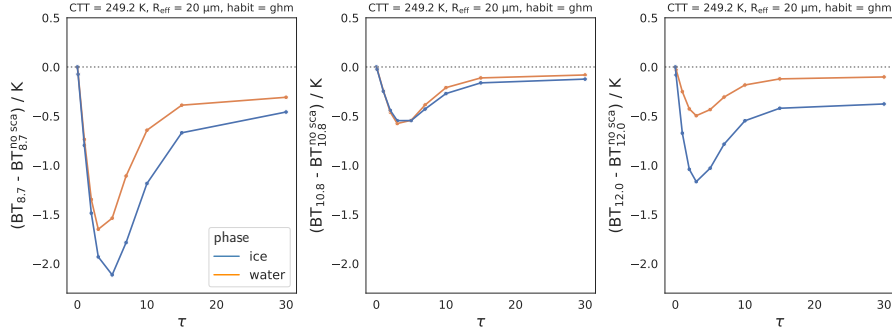


Figure 5. Scattering effects on brightness temperatures (BT): Difference between the BTs for a cloud with scattering and a cloud with scattering switched off for all three IR window channels, i.e. $BT_\lambda - BT_\lambda^{\text{no_sca}}$ for each channel with centre wavelength $\lambda \in \{8.7\mu\text{m}, 10.8\mu\text{m}, 12.0\mu\text{m}\}$, for liquid and ice clouds as functions of optical thickness τ .

5 Effects of cloud properties on BTDs

In this section we analyse the results of the RT calculations described in Sect. 3. We start with the effects of scattering on the BTs of the three window channels separately. We then combine the BTs to BTDs and analyse them as functions of τ , phase, R_{eff} , ice crystal habit and CTT, focusing on the physical relationships between these cloud properties and the BTDs. In order
 215 to disentangle the effects of the different cloud parameters, we always vary only one or two parameters and keep the remaining cloud parameters at fixed "default" values, namely CTH=6 km (corresponding to CTT=249.2 K), $R_{\text{eff}}=20\mu\text{m}$ for both cloud phases and the general habit mix as ice crystal habit.

The following conventions are used throughout this section: blue colours indicate the ice phase; orange/red colours indicate the liquid phase. Solid lines represent a 'normal' atmosphere with molecular absorption; dashed lines mean that molecular
 220 absorption is switched off.

5.1 Effects of scattering on brightness temperatures

Scattering in the infrared window only needs to be considered for cloud particles; Rayleigh scattering by atmospheric molecules is negligible in the infrared window. The effects of cloud particle scattering on the BTs is shown in Fig. 5. It shows the difference between the BTs for a cloud with scattering and a cloud with scattering switched off for the three window channels, i.e. $BT_\lambda - BT_\lambda^{\text{no_sca}}$ for each channel with centre wavelength λ . This is shown as a function of τ (at 550 nm) for an ice and a
 225 water cloud with all other cloud parameters held constant. Switching off scattering in a cloud changes the optical thickness of that cloud, since only absorption now contributes to the extinction of radiation. However, to be able to compare scenarios with and without scattering for fixed cloud microphysics (same water content, R_{eff} , ...), the τ parameter used for this figure is still the "original" optical thickness (with absorption and scattering).

230 All curves in Fig. 5 are negative everywhere, meaning that scattering is a radiation sink for all three wavelengths: Part of the radiation coming from below the cloud is scattered back downwards. However, the amount of radiation lost to scattering is different for the different wavelengths. Scattering has a larger effect on the radiation at $8.7\ \mu\text{m}$ than at 10.8 or $12.0\ \mu\text{m}$, as expected from β_{sca} which is higher at $8.7\ \mu\text{m}$ than at the other two wavelengths (see Fig. 3). For 8.7 and $12.0\ \mu\text{m}$, scattering by ice clouds is more significant than by water clouds; for $10.8\ \mu\text{m}$, scattering leads to a similar radiation loss for both water
235 and ice clouds. Interestingly, scattering effects are visible even when the cloud is opaque (black, $\tau=30$). An explanation is that the observed radiance at TOA does not just come from the top of the cloud. Rather, it comes from the upper layers within the cloud (with decreasing intensity as one moves deeper into the cloud). Radiation emitted anywhere below the cloud top is still subject to scattering on its way to the cloud top.

Using different CTT or Reff values in the calculations (for both the liquid and the ice cloud) mainly changes the magnitude
240 of the negative peaks, but does not change the qualitative results shown in Fig. 5. Similarly, changing the ice crystal habit does not change the qualitative results and has only a small effect on the values shown.

5.2 Effects of optical thickness on BTDs

We begin the study of BTDs by analysing the physical factors that drive the BTDs' behavior in relation to τ . Fig. 6 shows
245 BTD(8.7 - 10.8) and BTD(10.8 - 12.0) as functions of τ for both an ice and a liquid cloud and with molecular absorption switched on and off.

As τ approaches zero in all panels of Fig. 6, i.e. no cloud is simulated, the BTD curves with atmospheric absorption switched
on (solid lines) do not go to zero. They remain above zero for BTD(10.8 - 12.0) and below zero for BTD(8.7 - 10.8). This is the effect of atmospheric absorption, since radiation at $8.7\ \mu\text{m}$ and $12.0\ \mu\text{m}$ is more strongly absorbed by water vapor than at $10.8\ \mu\text{m}$: Compare the curves with (solid lines) and without (dashed lines) molecular absorption for τ approaching zero. As τ
250 increases, the curved shape of the BTD functions is (largely) due to the interplay of transmission and emission from the cloud. As discussed in Sect. 4 the BTD Nonlinearity Shift adds to these effects. Where transmission is dominant (small τ), the spectral differences in extinction (see Fig. 3) lead to an increase in BTD values. Where emission is dominant (large τ), BTD values are small, giving rise to the curved shape of the BTD functions (the well-known BTD arc from Inoue (1985)). The BTD curves become constant at about $\tau \gtrsim 15$.

255 To disentangle the effects of cloud absorption and scattering, Fig. 6(a,b) show the BTDs with cloud particle scattering switched off. As explained in the previous section, the τ parameter used for these figures is still the "original" optical thickness (with absorption and scattering). In Fig. 6(c,d) scattering is switched on. BTD(10.8 - 12.0) in Fig. 6(a) is positive, meaning that radiation at a wavelength of $12.0\ \mu\text{m}$ is more strongly absorbed than at $10.8\ \mu\text{m}$ and more radiation is transmitted through the cloud at $10.8\ \mu\text{m}$. This matches the absorption coefficient, which is higher at 12.0 than $10.8\ \mu\text{m}$ (shown as an inset for the given
260 R_{eff} for convenience, as well as in Fig. 3).

Analogously, Fig. 6(b) shows that radiation at $10.8\ \mu\text{m}$ is more strongly absorbed by the cloud than at $8.7\ \mu\text{m}$, especially for ice clouds. The stronger absorption at 10.8 compared to $8.7\ \mu\text{m}$ can again be seen in the absorption coefficient (shown in inset and in Fig. 3). The spectral differences in the absorption coefficient are stronger between 8.7 and 10.8 than between 10.8 and

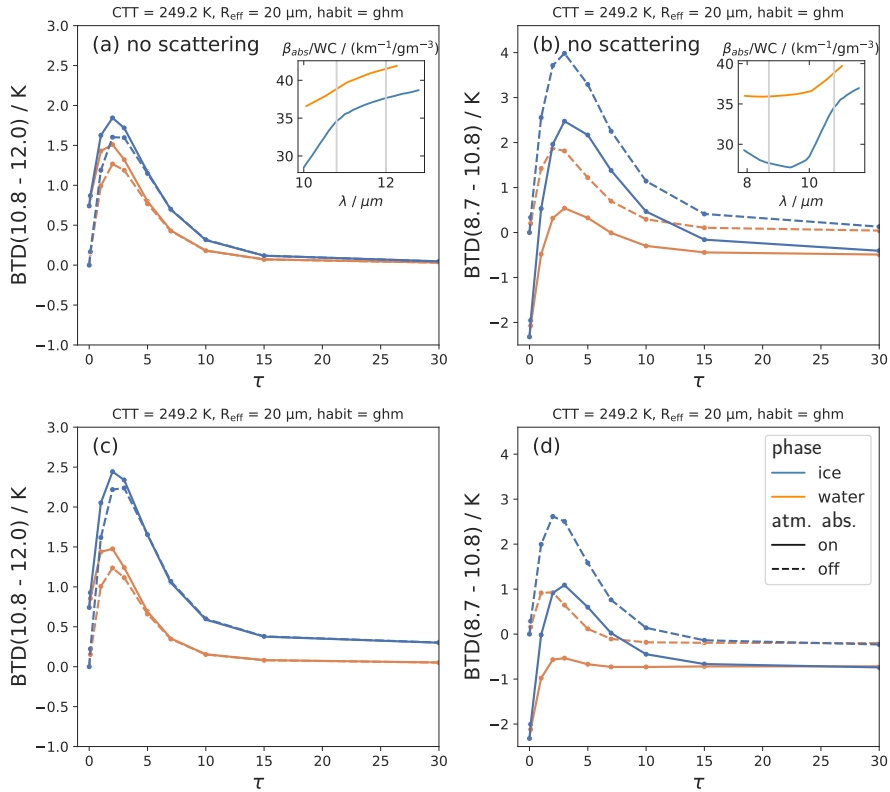


Figure 6. Brightness temperature differences BTD(10.8-12.0) and BTD(8.7-10.8) as functions of τ for cloud particle scattering (a,b) switched off and (c,d) switched on for liquid and ice clouds. Solid lines indicate a "normal" absorbing atmosphere, dashed lines indicate that molecular absorption is switched off.

12.0 μm , leading to higher values of BTD(8.7-10.8) than BTD(10.8-12.0) (compare Fig. 6(a) to Fig. 6(b)). For BTD(8.7-10.8),
 265 note that molecular absorption plays an important role even for optically thick clouds, decreasing BTD(8.7-10.8) everywhere
 by at least 0.5 K, since radiation at 8.7 μm is more strongly absorbed by atmospheric molecules (water vapor) than at 10.8 μm .

Switching on particle scattering (Fig. 6(c)), the BTD(10.8-12.0) values increase for ice clouds and stay about the same for
 liquid clouds. This will be further discussed in the next section (Sect. 5.3). For opaque clouds (large τ), the spectral differences
 in scattering effects lead to non-vanishing BTD(10.8-12.0) values for ice clouds (BTD(10.8-12.0) \approx 0.3 K).

270 For BTD(8.7-10.8), switching on scattering leads to a decrease, since scattering has a stronger effect at 8.7 compared to
 10.8 μm (see Fig. 5). However, the increase in BTD(8.7-10.8) due to cloud absorption (Fig. 6(a)) outweighs this opposing
 scattering effect and the BTD(8.7-10.8) curve is still positive (when atmospheric absorption is not considered). Note the dif-
 ferences with BTD(10.8-12.0), where cloud absorption and scattering are concurrent effects, both leading to an increase in
 BTD(10.8-12.0).

275 The following list summarizes the most important results:

- Stronger absorption and scattering at 12.0 compared to 10.8 μm lead to positive values of $\text{BTD}(10.8-12.0)$.
- Stronger absorption at 10.8 compared to 8.7 μm lead to positive values of $\text{BTD}(8.7-10.8)$; scattering has a mediating effect, reducing $\text{BTD}(8.7-10.8)$ values.
- These trends are consistent with expectations based on absorption and scattering coefficients.

280 5.3 Effects of cloud phase on BTDs

We now discuss the direct dependence of $\text{BTD}(10.8-12.0)$ and $\text{BTD}(8.7-10.8)$ on phase shown in Fig. 6. Direct dependence means that all other parameters such as R_{eff} or CTT are held constant. $\text{BTD}(10.8-12.0)$ in Fig. 6(c) has higher values for the ice phase than the liquid phase for all τ . Comparing the curves with and without scattering (Fig. 6(a) and Fig. 6(c)), we see that this difference between liquid and ice is mainly due to the different scattering properties of cloud particles at the two wavelengths:
 285 For liquid clouds the scattering has a similar effect at 10.8 and 12.0 μm , while for ice clouds radiation at 12.0 μm is scattered more than at 10.8 μm (see Fig. 5), leading to higher $\text{BTD}(10.8-12.0)$ values for ice clouds.

$\text{BTD}(8.7-10.8)$ directly depends on phase only for small to moderate τ ($\tau \lesssim 15$), with higher values for ice than for liquid. This difference is due to absorption properties: The spectral difference in absorption between the two wavelengths is larger for ice clouds (see β_{abs} in the inset of Fig. 6(b) or Fig. 3). Switching on cloud scattering reduces the differences between ice
 290 and liquid clouds in $\text{BTD}(8.7-10.8)$ (compare Fig. 6(b) with Fig. 6(d)). The reason for this can be seen in Fig. 5: The effect of scattering at 8.7 μm is stronger for ice than for water, while it is similar for ice and for water at 10.8 μm . This leads to a stronger decrease in $\text{BTD}(8.7-10.8)$ values for ice than for water clouds when scattering is switched on. However, overall the effect of absorption (leading to larger $\text{BTD}(8.7-10.8)$ values for ice than for water) outweighs this contrasting scattering effect.

In summary, the most important findings are:

- 295 – There is a direct phase dependence of the BTDs due to the dependence of the single scattering properties on cloud phase.
- This effect is of the order of 0.5–1.5 K for $\text{BTD}(10.8-12.0)$ and 0–2 K for $\text{BTD}(8.7-10.8)$, depending on τ , in all modeled scenarios.
- For $\text{BTD}(10.8-12.0)$, mainly scattering is responsible for the direct dependence on cloud phase.
- For $\text{BTD}(8.7-10.8)$, absorption is responsible for the direct dependence on cloud phase, scattering reduces the differences
 300 between the phases.

5.4 Effects of effective radius on BTDs

Fig. 7 shows $\text{BTD}(10.8-12.0)$ and $\text{BTD}(8.7-10.8)$ as a function of τ and R_{eff} for ice clouds (top row) and liquid clouds (bottom row) for the full RT model (i.e. scattering switched on). Note that the range of R_{eff} values for ice and liquid clouds are different in order to simulate realistic cloud conditions. For low τ ($\tau \lesssim 10$), smaller R_{eff} lead to larger values for both BTDs. The effect

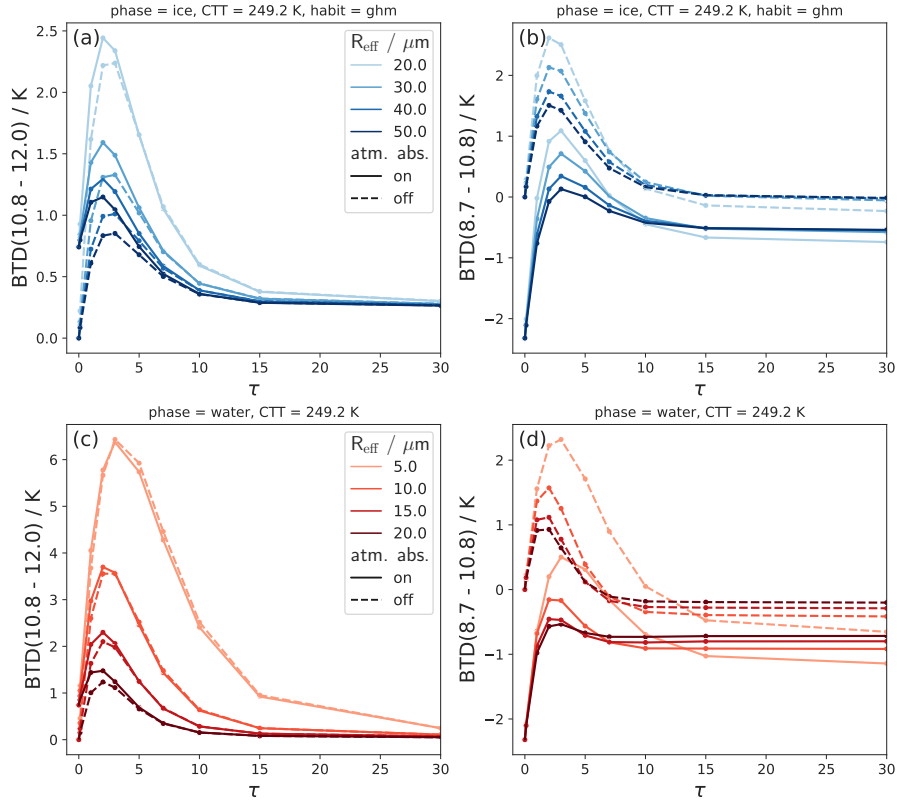


Figure 7. Effects of varying R_{eff} on $\text{BTD}(10.8-12.0)$ and $\text{BTD}(8.7-10.8)$ as functions of τ for ice clouds (top row) and liquid clouds (bottom row). Solid lines indicate a "normal" absorbing atmosphere, dashed lines indicate that molecular absorption is switched off.

305 becomes stronger in a nonlinear way as the R_{eff} becomes smaller. This confirms previous results, for instance Dubuisson et al. (2008), who also found a strong and nonlinear dependence of BTDs on R_{eff} .

The effect of R_{eff} on $\text{BTD}(10.8-12.0)$ results physically from the dependence of particle absorption on R_{eff} : The spectral differences of the absorption coefficient are larger for smaller R_{eff} (see Fig. 3), resulting in lower transmission at 12.0 than at 10.8 μm , and thus higher $\text{BTD}(10.8-12.0)$ values for smaller R_{eff} values. The effect of scattering on $\text{BTD}(10.8-12.0)$ is similar for varying R_{eff} and comparatively small (increases (decreases) the BTD by $\lesssim 0.5$ K for ice (water) clouds). For the interested reader, Fig. C1 in appendix C shows the sensitivity of both BTDs with R_{eff} broken down into effects of absorption and scattering.

315 For $\text{BTD}(8.7-10.8)$, the R_{eff} dependence for small τ is, like the phase dependence, the result of two opposite effects: For smaller R_{eff} , absorption increases for 10.8 compared to 8.7 μm , leading to an increase in $\text{BTD}(8.7-10.8)$. On the other hand scattering increases more for 8.7 than for 10.8 μm , leading to a decrease in $\text{BTD}(8.7-10.8)$. However, the effect due to absorption is stronger and therefore the $\text{BTD}(8.7-10.8)$ increases with decreasing R_{eff} . Unlike $\text{BTD}(10.8-12.0)$, $\text{BTD}(8.7-10.8)$ is still

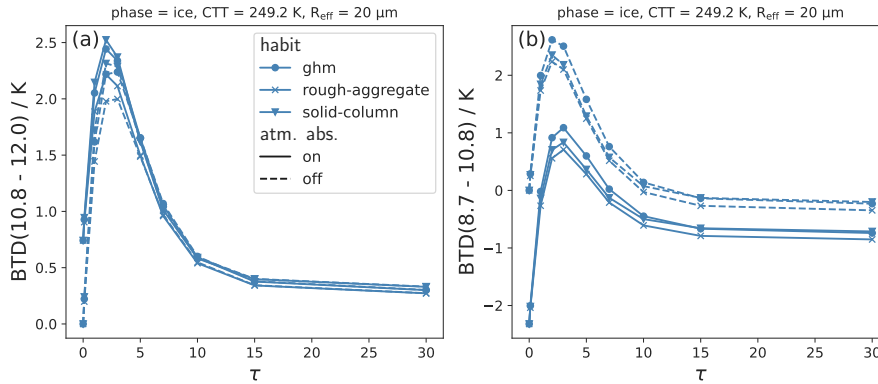


Figure 8. Effects of varying ice crystal habit on (a) BT D(10.8-12.0) and (b) BT D(8.7-10.8) as functions of τ for ice clouds. Solid lines indicate a "normal" absorbing atmosphere, dashed lines indicate that molecular absorption is switched off.

dependent on R_{eff} at large τ : here BT D(8.7-10.8) increases with increasing R_{eff} , contrary to the R_{eff} trend at small τ . The smaller the R_{eff} , the more important this effect becomes.

Summarizing the most important insights:

- 320 – The BT Ds depend strongly and nonlinearly on R_{eff} .
- Physically this dependence is due to larger spectral differences in the absorption coefficient for smaller R_{eff} .
- For BT D(8.7-10.8), stronger scattering for smaller R_{eff} mediates the absorption effects.

5.5 Effects of ice crystal habit on BT Ds

Figure 8 shows the sensitivity of the BT Ds on ice crystal habits (in ice clouds). For both BT Ds, rough aggregates lead to the smallest BT D values. For BT D(8.7-10.8), ice crystals with the general habit mix (ghm) lead to the largest BT D values, while for BT D(10.8-12.0), solid columns lead to slightly higher values. However, the sensitivity on ice crystal habits is relatively small ($\lesssim 0.5 \text{ K}$) compared to other cloud properties. This confirms Dubuisson et al. (2008), who showed that the habit has a small effect on BT Ds compared to the effect of R_{eff} also for other ice crystal shapes than the ones considered here. The relative importance of different cloud parameters will be further discussed in Sect. 6.

330 5.6 Effects of cloud top temperature on BT Ds

Figure 9 shows the sensitivity of both BT Ds to CTT – and thus to CTH – for ice (top row) and liquid (bottom row) clouds. The results with molecular absorption switched off (dashed lines) show how much of this sensitivity is due to the atmosphere. Note that the CTT ranges for ice and liquid clouds are different in order to simulate realistic cloud conditions.

For BT D(8.7-10.8), molecular absorption is relevant for all τ values: Clouds with high CTT, i.e. low CTH, have more
 335 absorbing atmosphere above cloud top, leading to more radiation absorbed at 8.7 compared to $10.8 \mu\text{m}$. For BT D(10.8 - 12.0),

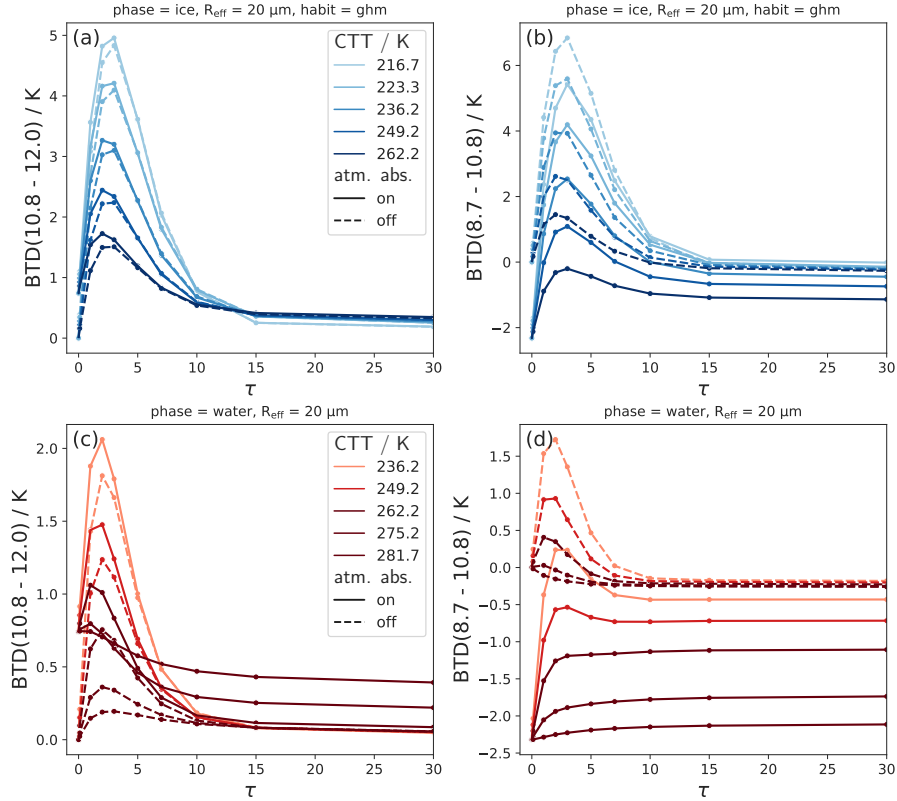


Figure 9. Effects of varying cloud top temperature (CTT) on $\text{BTD}(10.8-12.0)$ and $\text{BTD}(8.7-10.8)$ as a function of τ for ice clouds (top row) and liquid clouds (bottom row). Solid lines indicate a "normal" absorbing atmosphere, dashed lines indicate that molecular absorption is switched off.

this effect is less pronounced and molecular absorption is only relevant when there is a long path through the atmosphere (i.e. low CTH or small τ).

At low τ ($\lesssim 10$), both $\text{BTD}(8.7-10.8)$ and $\text{BTD}(10.8-12.0)$ show a strong dependence on CTT that is not due to molecular absorption. Since the single scattering properties are not CTT dependent (see Sect. 2), this CTT effect on the BTDS is also not
 340 (directly) due to spectral differences in the single scattering properties - in contrast to the effects of the other cloud parameters discussed above. Instead, there are more subtle reasons for this effect: In Sect. 4 we found that the BTD Nonlinearity shift leads to a CTT dependence of the BTDS with higher BTD values for lower CTTs even when optical cloud properties are the same for all wavelengths. This explains part of the CTT dependence in Fig. 9. In appendix B we further discuss the BTD Nonlinearity Shift, allowing also wavelength dependent optical properties. It can be shown that for the Schwarzschild BTD^{S} ,
 345 spectral differences in the extinction coefficient are scaled by the difference between the surface and the cloud top radiance, $B_{\lambda}(T_s) - B_{\lambda}(\text{CTT})$ (see appendix B for a detailed discussion). Hence, the effects of spectral differences in optical properties on BTD^{S} are amplified by larger ΔT , i.e. differences between T_s and the CTT. This is the main reason (besides the BTD

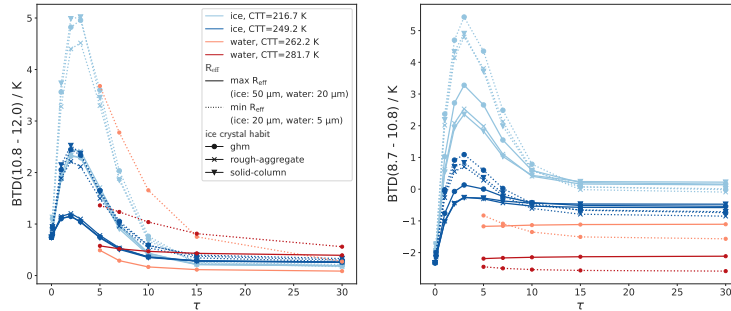


Figure 10. Sensitivity analysis for each BTM varying the phase related cloud parameters τ , R_{eff} , habit, CTT and thermodynamic phase: BTM(10.8-12.0) and BTM(8.7-10.8) for typical upper and lower boundaries of CTT and R_{eff} for ice (blue colors) and liquid (orange/ red colors) clouds. For ice clouds, different habits are shown as different markers. The figures show typical BTM ranges for ice and liquid clouds.

Nonlinearity Shift) for the CTT dependence of the BTMs. Colder CTTs (or rather larger ΔT) thus increase both the BTM Nonlinearity Shift and the effects of spectral differences in optical properties.

350 The following list summarizes the CTT / CTH effects on the BTMs:

- For BTM(8.7-10.8), CTH has a large effect, due to molecular absorption mainly above cloud top.
 - Both BTMs show a strong dependence on CTT (or more generally on ΔT) with higher values for lower CTTs (larger ΔT).
 - The BTM Nonlinearity Shift is co-responsible for the positive BTM values and the CTT (or ΔT) dependence of the
- 355 BTMs, adding to the effects stemming from spectral differences in absorption and scattering properties.

6 Implications for phase retrievals

In the last section we analysed the effects of cloud properties on the BTMs individually, by varying only one cloud property at a time (besides τ). In this section we combine the phase related cloud parameters τ , R_{eff} , ice habit, CTT and thermodynamic phase for a sensitivity analysis of the BTMs. From this analysis we determine typical BTM ranges for ice and liquid clouds and

360 understand which cloud parameters are responsible for the phase information contained in the BTMs. We analyse for which cloud scenarios we can distinguish between liquid clouds and ice clouds, and when they overlap, allowing us to derive implications for phase retrievals. First, in Sect. 6.1, we perform sensitivity analyses for each BTM individually. Next, in Sect. 6.2, we study the sensitivities and phase information content of the two BTMs combined.

6.1 Sensitivity analysis for each BTD

365 To study when BTDs can typically distinguish between liquid and ice clouds, Fig. 10 gives an overview of the sensitivities of the BTDs for "typical" cloud scenarios, as defined in the following. The figure shows the BTDs for upper and lower boundaries of CTT (217 – 249 K for ice, 262 – 282 K for liquid water) and R_{eff} (20 – 50 μm for ice, 5 – 20 μm for liquid water). These ranges are representative for mid-latitude clouds (between 30 and 50°N or S) and are chosen as follows: The CTT boundaries are derived from the active remote sensing product DARDAR (LiDAR/raDAR, Delanoë and Hogan (2010)) - specifically, values
370 close to the 15th and 85th percentiles of ice and liquid CTTs observed for mid-latitude clouds, covering about 70% of CTTs (see Mayer et al. (2023) for detailed information on the data set). The cloud scenarios with the two CTT boundary values per phase are shown in different colors in Fig. 10 (light blue and dark blue for ice clouds; orange and red for liquid clouds). For the R_{eff} boundaries we select the upper and lower limits of all computed R_{eff} scenarios (see table 1). Additionally, as liquid clouds rarely have $\tau < 5$, these values are omitted, since we focus for this sensitivity analysis on "typical" cloud scenarios.
375 For ice clouds, different habits are shown as different markers. Hence, the cloud parameters in Fig. 10 are chosen such that the majority of mid-latitude cloud events for each phase lie between the very bottom and top blue curves for ice and the very bottom and top orange/red curves for liquid.

To verify that the computed ranges of BTD values are realistic, we compare the RT results with measured SEVIRI data using cloud phase information from DARDAR. More details on this comparison and its results can be found in Appendix D. We find
380 good agreement between the RT results and the measured SEVIRI data and conclude that the results of the RT calculations are realistic.

In Fig. 10 BTD(10.8-12.0) shows the highest sensitivity to τ , CTT and R_{eff} . BTD(8.7-10.8) shows the highest sensitivity to τ , CTT and molecular absorption (closely linked to CTH). In comparison to τ and CTT/CTH the sensitivity to R_{eff} is lower for BTD(8.7-10.8) and mainly relevant for small CTT. For both BTDs, the direct sensitivity to cloud phase, i.e. holding all other
385 cloud parameters constant, plays mostly only a minor role: For BTD(10.8-12.0) the direct phase dependence is of the order of 0.5–1.5 K; for BTD(8.7-10.8) the direct influence of phase is only significant for small τ values ($\lesssim 10$) and then of the order of 1–2 K (see Sect. 5.3).

For a phase retrieval we need to know for which cloud properties liquid and ice clouds overlap and where they separate for both BTDs. The largest BTD(10.8-12.0) values in the "typical" cloud scenarios (about 2.5 to 5 K in Fig. 10) are only observed
390 for optically thin and cold ice clouds with small R_{eff} . Thus BTD(10.8-12.0) is useful to detect cirrus clouds, especially if they have small R_{eff} (like contrails), and classify them as ice in a phase retrieval. However, our calculations show that certain liquid cloud scenarios with exceptionally low R_{eff} and cold CTTs can also induce remarkably high BTD(10.8-12.0). This can lead to misclassification of these liquid clouds as ice. However, most liquid clouds have lower BTD(10.8-12.0), below about 2.5 K in Fig. 10. Since such low BTD(10.8-12.0) may also indicate ice clouds with "warm" CTTs and/or large R_{eff} , or ice clouds with τ
395 close to zero, a phase classification based on BTD(10.8-12.0) alone is challenging. The lowest BTD(10.8-12.0) values (about 0 to 1 K in Fig. 10) indicate optically thick clouds, but do otherwise not contain much phase information.

As for BTD(10.8-12.0), large BTD(8.7-10.8) (around 1 to 5.5 K in Fig. 10) can indicate ice phase, since only ice clouds with low τ of about $1 < \tau < 7$ reach these values. Low BTD(8.7-10.8) (lower than about -0.5 in Fig. 10) can arise from very thin ice clouds (as BTD(8.7-10.8) decreases to about -2 K as τ goes to zero) or optically thick clouds. For optically thick clouds, BTD(8.7-10.8) decreases with higher CTT (due to lower CTHs and stronger molecular absorption) and smaller R_{eff} - both characteristics typical of liquid clouds. As a general guideline for optically thick clouds, lower BTD(8.7-10.8) indicate a higher probability of a liquid cloud. Overall, the phase information contained in BTD(8.7-10.8) originates mainly from its sensitivity to CTT for clouds with $\tau \lesssim 10$, while for optically thick clouds it stems mainly from its sensitivity to molecular absorption (closely linked to CTH) and (to a lesser extent) R_{eff} . Only in cases of optically thin clouds ($\tau \lesssim 10$) is the phase information of BTD(8.7-10.8) additionally due to the direct phase influence on the (different) absorption properties of liquid and ice particles.

To summarize the main findings:

- The sensitivities of the BTDs are complex.
- BTD(10.8-12.0) shows the highest sensitivity to τ , CTT and R_{eff} . BTD(8.7-10.8) shows the highest sensitivity to τ and CTT/CTH.
- Thin ice clouds can be detected by both BTD(10.8-12.0) and BTD(8.7-10.8) as long as $\tau \gtrsim 1$.
- BTD(8.7-10.8) also provides CTH and R_{eff} information for optically thick clouds, which can be useful for phase determination.
- For BTD(10.8-12.0), typical liquid and ice clouds overlap for most cloud scenarios, with the exception of cold, thin ice clouds. For BTD(8.7-10.8), liquid and ice clouds separate better, but the BTD values of the two phases are close when CTTs (CTHs) are similar. This phase separation is mainly due to the sensitivity of BTD(8.7-10.8) to CTT/CTH.

6.2 Sensitivity analysis for the combination of both BTDs

We perform a similar sensitivity analysis as in the last section for the combination of both BTDs. As Fig. 10, Fig. 11 shows the BTDs for the same upper and lower boundaries of CTT and R_{eff} , but in the space spanned by BTD(8.7-10.8) and BTD(10.8-12.0). Along each line, τ increases from 0 to 30. To make the shape of the curves easier to understand, here also liquid clouds with $\tau < 5$ are shown (in contrast to Fig. 10).

Figure 11 shows that the combined knowledge of both BTD(8.7-10.8) and BTD(10.8-12.0) leads to a better phase classification than considering BTD(8.7-10.8) and BTD(10.8-12.0) individually. For instance, liquid clouds at cold CTTs and small R_{eff} (orange dotted line) separate from ice clouds in Fig. 11 as long as τ is not too large ($\lesssim 10$). In contrast, the same cloud scenario overlaps with ice cloud scenarios when only BTD(8.7-10.8) or BTD(10.8-12.0) are considered individually (Fig. 10).

In order to better showcase the range of BTD values for both phases and identify overlap regions, we use an additional type of plot: Instead of showing only the boundary cases (as in Fig. 11), the left column of Fig. 12 shows (almost) all computed BTD values within the defined boundaries of CTT and R_{eff} in the space spanned by the two BTDs. Only optically thick clouds

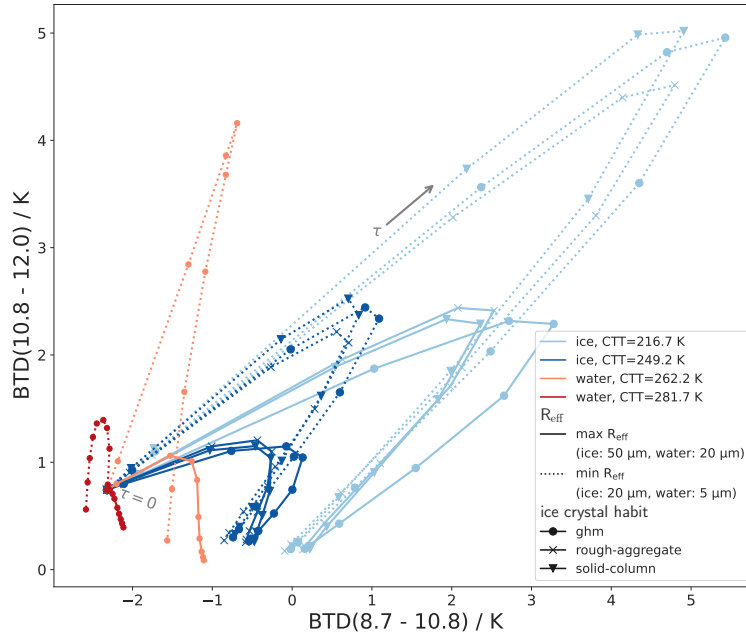


Figure 11. Sensitivity analysis combining both BT Ds and varying the phase cloud parameters τ , R_{eff} , habit, CTT and thermodynamic phase:: Blue lines show ice clouds; orange/red lines show liquid clouds for typical upper and lower boundaries of CTT and R_{eff} . Along each line, τ increases from 0 to 30. For ice clouds, different habits are shown as different markers

($\tau \geq 10$) with very low (< 233 K) or very high (> 273 K) CTTs are removed, i.e. the clouds that are easily categorised as liquid
 430 or ice by a CTT proxy such as $BT_{10.8}$ and for which a categorisation by the BT Ds is therefore not necessary. Liquid clouds are shown as round markers, while ice clouds are shown as crosses. The three subfigures in the left column of Fig. 12 vary only by their color code which encodes τ , CTT and R_{eff} respectively. They show that there is little overlap between the "typical" liquid and ice clouds (i.e. the clouds within the defined CTT and R_{eff} boundaries). The only overlap is for very small τ ($\tau \lesssim 1$), since the BT Ds approach the same values for all clouds, determined by atmospheric properties, as $\tau \rightarrow 0$ (best seen in Fig. 11).
 435 This means that a phase classification for "typical" liquid and ice cloud cases is possible in $BT D(8.7-10.8) - BT D(10.8-12.0)$ - space for $\tau \gtrsim 1$ when atmospheric parameters are known.

However, Fig. 11 and the left column in Fig. 12 also show that liquid and ice BT D values are closest for clouds with similar CTTs. To further explore this issue and to test the limitations of a phase classification using the BT Ds, the right column of Fig. 12 shows BT D values also for clouds outside the "typical" cloud boundaries. The three subfigures show the whole range
 440 of computed cloud scenarios (see table 1), including also exceptionally cold liquid clouds and exceptionally warm ice clouds. Only the "easy" to distinguish cases ($\tau \geq 10$ and either $CTT < 233$ K or $CTT > 273$ K) are removed as before. The figures

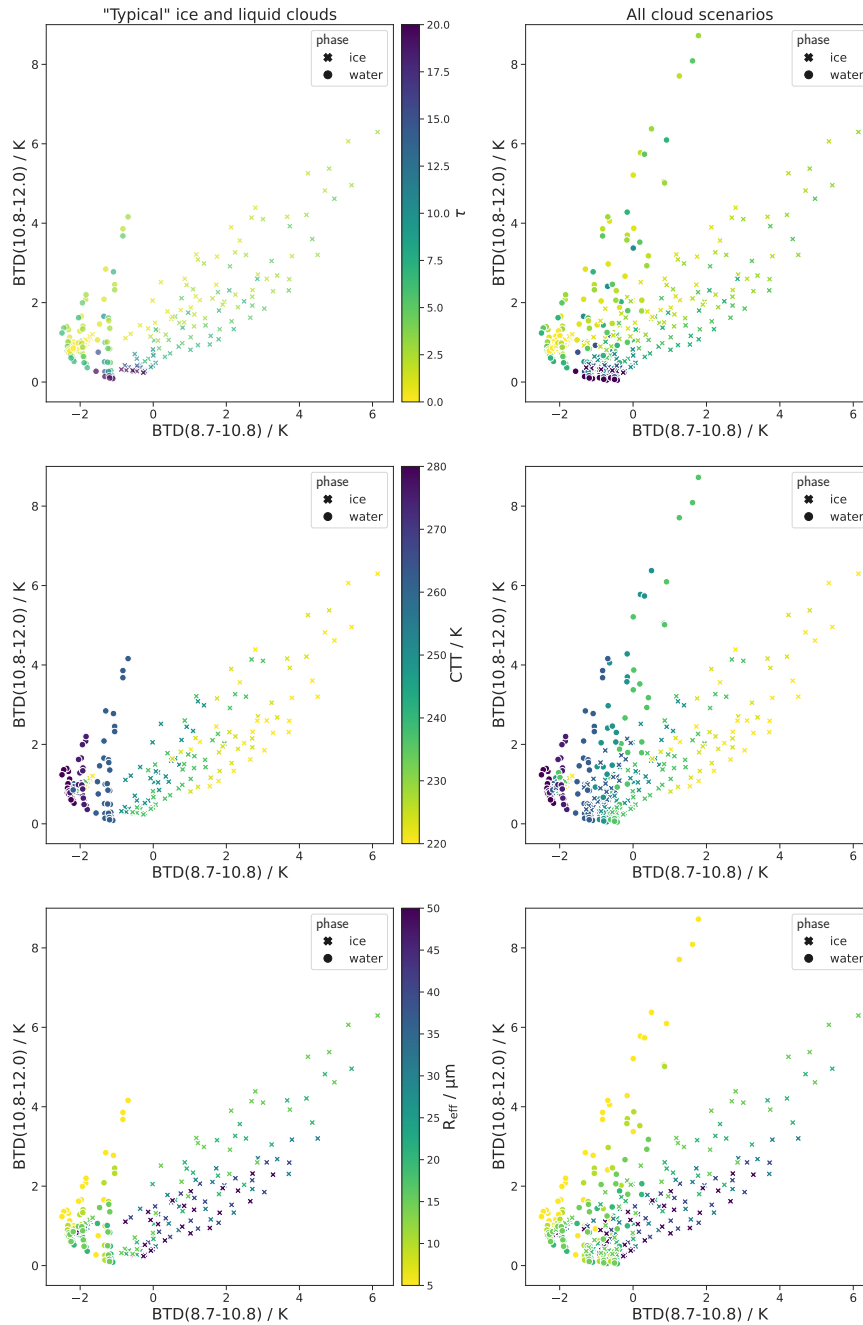


Figure 12. Left column: $\text{BT D}(10.8-12.0)$ and $\text{BT D}(8.7-10.8)$ values within the defined "typical" boundaries of CTT. Round markers indicate liquid clouds; crosses indicate ice clouds. Clouds which can be distinguished using a CTT proxy like $\text{BT}_{10.8}$, i.e. optically thick clouds ($\tau \geq 10$) with very low ($< 233 \text{ K}$) or very high ($> 273 \text{ K}$) CTTs, are not shown. The color code in the three rows encodes τ , CTT and R_{eff} respectively. Right column: Same as left column but for the whole range of computed cloud scenarios (see table 1), including also exceptionally cold liquid clouds and exceptionally warm ice clouds. The color codes of the three rows correspond to the color codes in the left column. Clouds which can be distinguished using a CTT proxy are again not shown.

show that the overlap between liquid and ice clouds is significantly larger compared to the "typical" cloud cases (left column of Fig. 12). The clouds in the overlap region are mainly liquid and ice clouds which have similar CTTs in the midlevel temperature range, i.e. rather cold liquid clouds ($CTT \lesssim 260$ K) and rather warm ice clouds ($CTT \gtrsim 250$ K). We discussed in the last section (Sect. 6.1) that the CTT/CTH is the most important contributor to the differences between liquid and ice clouds for both BTDs. It is therefore not surprising that phase discrimination for clouds with similar CTT/CTH is difficult even when knowledge of both BTDs is combined. Note also that additional information from $BT_{10.8}$, which is often used as a proxy for CTT, does not help much in distinguishing between phases in these cases of midlevel CTTs. For the phase classification of these midlevel clouds, the R_{eff} also plays a role: For R_{eff} values that are rather large for the respective phase, the overlap occurs for all τ values; for R_{eff} values that are rather small for the respective phase, the overlap occurs only for very small or very large τ values.

To summarize the most important results:

- The combined use of $BTD(8.7-10.8)$ and $BTD(10.8-12.0)$ is better suited for phase discrimination than the two BTDs individually.
- The combined use of $BTD(8.7-10.8)$ and $BTD(10.8-12.0)$ can discriminate cloud phase for liquid and ice clouds in their "typical" CTT regimes as long as τ is not too small ($\tau \gtrsim 1$) and when atmospheric parameters are known.
- Clouds in the midlevel CTT regime are challenging: If liquid clouds are particularly cold or ice clouds particularly warm, they can often not be distinguished by the two BTDs. This is especially true for clouds with large R_{eff} for the respective phase.

6.3 Sensitivity to additional cloud parameters: Effects of geometric thickness and vertical R_{eff} inhomogeneity

Cloud properties that have not been discussed so far are cloud geometric thickness and vertical inhomogeneities of microphysical parameters. Both can have an impact on BTDs (Piontek et al., 2021a; Zhang et al., 2010). To estimate how large these effects are, we performed a sensitivity analysis for varying cloud geometric thickness and for vertical inhomogeneities of R_{eff} . Results of this analysis are shown in Fig. E1 and Fig. E2 in the appendix. We find that the sensitivity to both geometric thickness and vertical R_{eff} inhomogeneity is small compared to other cloud parameters ($\lesssim 0.5$ K in most cases). This sensitivity does not significantly affect the regions in the space spanned by the two BTDs which are associated with the different phases and therefore has a comparatively small effect on a potential phase retrieval.

7 Conclusions

The aim of this study is to characterize and physically understand the relation of two IR window BTDs that are typically used for satellite retrievals of the thermodynamic cloud phase. As an example, we select $BTD(8.7-10.8)$ and $BTD(10.8-12.0)$ of the SEVIRI imager, but the main findings can be generalised to other imagers with similar thermal channels. Although modern phase retrievals often rely not only on BTDs but also on other satellite measurements (Baum et al., 2012; Hünnerbein et al.,

2022; Benas et al., 2023; Mayer et al., 2024), it is important to understand the BTM characteristics and capabilities. This knowledge helps to design optimal cloud phase retrievals and to understand their potential and limitations.

475 We present RT calculations that analyse the sensitivities of the two BTMs to cloud phase and all radiatively important cloud parameters related to phase, namely τ , R_{eff} , ice crystal habit and CTT/ CTH. Previous studies of BTMs have tended to focus on only a small number of cloud parameters, and an overview of the relative importance of all cloud parameters and their interdependencies is still missing. We perform a sensitivity analysis of the BTMs, which to our knowledge has never been done for all cloud parameters combined. This provides an overview over the effects of all cloud parameters and shows which
480 parameters are responsible for the observed phase dependence of the BTMs, which is often used for phase retrievals (Ackerman et al., 1990; Strabala et al., 1994; Finkensieper et al., 2016; Key and Intrieri, 2000; Baum et al., 2000, 2012; Hünnerbein et al., 2022; Benas et al., 2023; Mayer et al., 2024). Even though the RT calculations were performed for a specific atmospheric and surface setup, the main insights of this study, including the physical understanding of the effects of cloud properties on BTMs and their relative importance, are valid for any atmospheric or surface condition.

485 To understand the behaviour of the BTMs, we examine the effects of the nonlinear relationship between radiances and BTs through Planck’s radiation law on the BTMs. This nonlinearity induces positive BTM values and a dependence on the CTT (or more generally the surface-cloud-temperature contrast ΔT) in a simple RT model, even when cloud optical properties (transmittance and emissivity) are the same at all wavelengths. This effect is co-responsible for the arc shape of the BTMs as functions of τ and their CTT dependence, in addition to effects due to spectral differences in cloud optical properties. These
490 spectral differences in cloud optical properties can explain the (remaining) dependence of the BTMs on the different cloud parameters.

We find that the dependence on phase is more complex than is sometimes assumed: Although both BTMs are directly sensitive to phase (holding every other cloud parameter constant), this sensitivity is mostly small compared to other cloud parameters, as τ , CTT and R_{eff} . Instead, apart from τ for which the sensitivity is well known, the BTMs show the strongest
495 sensitivity to CTT/ CTH. Since the CTT is associated with phase, this is the main factor leading to the observed phase dependence of the BTMs. Note that more generally, this CTT dependence of the BTMs is more accurately described as a dependence on the surface-cloud temperature contrast ΔT , which reduces to a CTT dependence in our case with a fixed surface temperature. The direct phase dependence merely adds to the CTT/CTH effect, increasing differences between ice and liquid (for BTM(8.7-10.8) only for small $\tau \lesssim 10$).

500 The sensitivity analysis shows that it is straightforward to distinguish “typical” high ice clouds from low liquid clouds using the BTMs. However, it is challenging to distinguish a mid-level ice cloud from a mid-level liquid cloud - especially if the R_{eff} is also similar. The combination of both BTMs increases phase information content and is therefore preferable in a retrieval.

This study was conducted for a simple fixed setup of the atmosphere, surface and satellite viewing geometry in order to focus on the effects of cloud properties. If this setup is changed, we expect the cloud effects on the BTMs discussed in this
505 paper to be superimposed by additional effects: For example, changes in water vapor content or satellite zenith angle shift BTM(8.7-10.8) due to its sensitivity to water vapor absorption. This shift is larger the more water vapor is above the cloud top and therefore depends on the CTH and the vertical atmospheric profile. A different type of surface with spectral differences in

surface emissivity (as for instance a desert surface) shifts the values of both BTDs for optically thin clouds. For potential phase retrievals, these effects should ideally be taken into account.

510 This study focuses on liquid and ice clouds. We expect the BTD values of mixed-phase clouds to lie between ice and liquid values, as they represent a transition between the two. Depending mainly on the CTT/ CTH and to a lesser extent the R_{eff} of mixed-phase clouds, their BTD values are expected to be closer or further away from the liquid or ice BTD values. In that sense, we expect that BTDs can make a useful contribution to the retrieval of mixed-phase clouds and their composition. However, as the CTT/ CTH and R_{eff} values overlap between liquid, mixed-phase and/or ice clouds, we expect the regions of
 515 the different phases in the space spanned by BTD(8.7-10.8) and BTD(10.8-12.0) to also overlap, introducing ambiguity. The use of additional satellite channels containing, for instance, particle size or phase information is necessary to increase the phase information content for a retrieval.

Code and data availability. The libRadtran software used for the radiative transfer simulations is available from <http://www.libradtran.org> (Mayer and Kylling, 2005; Emde et al., 2016).

520 **Appendix A: Single scattering properties**

The single scattering properties are the volume extinction coefficient β_{ext} , the single scattering albedo ω_0 and the scattering phase function p . The volume extinction coefficient β_{ext} describes how much radiation is removed through scattering and absorption (=extinction) from a ray when passing through the cloud and can be expressed as

$$\beta_{\text{ext}} = \beta_{\text{sca}} + \beta_{\text{abs}} \quad (\text{A1})$$

525 where β_{sca} and β_{abs} are the scattering and absorption coefficient, with units of m^{-1} , measuring how much radiation is absorbed and scattered by cloud particles. Note that in this study τ is β_{ext} at wavelength $\lambda = 550 \text{ nm}$ integrated over the path through the cloud; the optical thickness τ_λ at other wavelengths λ is in general different from τ , depending on the other microphysical cloud parameters. The single scattering albedo ω_0 is a measure of the relative importance of scattering and absorption, defined as

$$530 \quad \omega_0 = \frac{\beta_{\text{sca}}}{\beta_{\text{sca}} + \beta_{\text{abs}}} = \frac{\beta_{\text{sca}}}{\beta_{\text{ext}}}. \quad (\text{A2})$$

Hence, as an alternative to β_{ext} and ω_0 one can equivalently describe radiative transfer by β_{abs} and β_{sca} , which can be easier to interpret. The scattering phase function $p(\Omega)$ gives the probability of the scattering angle Ω , i.e. the angle between the incident radiation and the scattered radiation. To understand radiative transfer through a cloud, the most important property of p is the angular anisotropy of the scattering process. This anisotropy is indicated to first order by the asymmetry parameter g , which is
 535 calculated from p as the mean cosine of the scattering angle Ω .

$$g = \int_{-1}^1 p(\cos \Omega') \cos \Omega' d \cos \Omega' \quad (\text{A3})$$

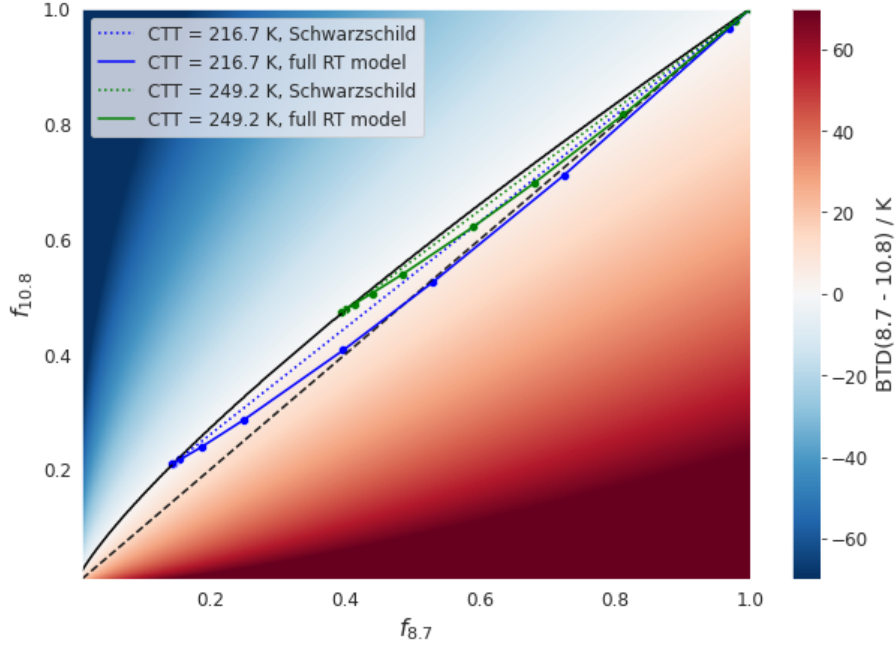


Figure B1. BTD(8.7-10.8) in the space spanned by the radiance fraction $f_{8.7}$ and $f_{10.8}$ (defined as the radiance at TOA scaled by the Planck radiance of the surface with temperature $T_s = 290$ K: $f_\lambda = R_{TOA,\lambda}/B_\lambda(T_s)$). The black solid line indicates $\text{BTD}(8.7-10.8) = 0$; the black dashed line indicates $f_{8.7} = f_{10.8}$. The blue and green lines show $f_{8.7}$ and $f_{10.8}$ values for varying τ at a given CTT: The dotted lines show $f_{8.7}$ and $f_{10.8}$ computed with the Schwarzschild equation (with $\tau_{8.7} = \tau_{10.8}$); solid lines show $f_{8.7}$ and $f_{10.8}$ values computed with the full RT model.

If a particle scatters more in the forward direction ($\Omega = 0^\circ$), g is positive; g is negative if the scattering is more in the backward direction ($\Omega = 180^\circ$) (Bohren and Huffman, 2008).

Appendix B: Disentangling the BTD Nonlinearity Shift from effects of wavelength dependent optical properties

540 An instructive way to look at the BTD Nonlinearity Shift and to disentangle it from effects of wavelength dependent optical properties is the following: To make the radiances at different wavelengths more comparable, we use the Planck radiance corresponding to the surface temperature T_s as a reference. For typical atmospheric profiles (without temperature inversions), this Planck radiance $B_\lambda(T_s)$ is the maximal possible radiance in each wavelength, corresponding to $\tau \rightarrow 0$ (see Eq. 3). We express the TOA radiance as fractions f_λ of this maximal possible radiance, called *radiance fraction* in the following, i.e.

$$545 \quad f_\lambda = \frac{R_{TOA,\lambda}}{B_\lambda(T_s)}, \quad \text{with } f_\lambda \in [0, 1]. \quad (\text{B1})$$

The BTDs can then be expressed as functions of the radiance fractions f_λ

$$\text{BTD}(\lambda_0 - \lambda_1) = T_{\lambda_0}(f_{\lambda_0} B_{\lambda_0}(T_s)) - T_{\lambda_1}(f_{\lambda_1} B_{\lambda_1}(T_s)). \quad (\text{B2})$$

For the sake of brevity, in the following we only discuss BTD(8.7-10.8) as function of $f_{8.7}$ and $f_{10.8}$; BTD(10.8-12.0) has qualitatively the same properties and the same conclusions apply. Figure B1 shows BTD(8.7-10.8) in $f_{8.7}$ - $f_{10.8}$ -space for $T_s =$
550 290 K. If $f_{8.7}$ is (much) larger than $f_{10.8}$, the BTD is positive and if $f_{8.7}$ is (much) smaller than $f_{10.8}$, the BTD is negative, as expected. However, the BTD(8.7-10.8) = 0 line is not at $f_{8.7} = f_{10.8}$ (black dashed line in Fig. B1) as one might naively expect but has a convex shape in $f_{8.7}$ - $f_{10.8}$ -space (shown as black solid line), such that BTD(8.7-10.8) = 0 for $f_{8.7} < f_{10.8}$. Or to put it another way, if the radiance at TOA is the same fraction of its maximal possible radiance at both wavelengths, $f_{8.7} = f_{10.8}$, the BTD is positive. Note that this is a completely general statement, that does not depend on a RT model but simply shows
555 what happens mathematically when the inverse Planck function, T_λ , is applied on fractions of Planck radiance, $f_\lambda B_\lambda(T_s)$, at different wavelengths.

To understand the role of the BTD Nonlinearity Shift we add results of RT computations to Fig. B1 in the following steps: First, we study how radiances computed with the Schwarzschild equation look like in $f_{8.7}$ - $f_{10.8}$ -space. To see the pure BTD Nonlinearity Shift we again set the optical thickness constant at both wavelengths, $\tau_{8.7} = \tau_{10.8} = \tau$. Next, we explore the
560 changes in the Schwarzschild radiance when τ differs at the two wavelengths, i.e. $\tau_{10.8} \neq \tau_{8.7}$. In this case, both the mathematical BTD Nonlinearity Shift and the physical effect of spectrally dependent optical properties are present. Third, we study how the radiance computed with the full RT model looks like in $f_{8.7}$ - $f_{10.8}$ -space.

We start with the Schwarzschild radiance in $f_{8.7}$ - $f_{10.8}$ -space with constant optical thickness at both wavelengths, $\tau_{8.7} = \tau_{10.8} = \tau$. We compute the radiances $R_{\text{TOA},8.7}^S$ and $R_{\text{TOA},10.8}^S$ from the Schwarzschild equation as functions of τ for different
565 values of CTT, as before (see Fig. 4(b)). These radiance results, expressed as radiance fractions $f_{8.7}$ and $f_{10.8}$, are shown in Fig. B1 as dotted lines for two different CTTs. For $\tau = 0$, the TOA radiance is the radiance emitted by the surface and $f_{8.7} = f_{10.8} = 1$. As τ increases, $f_{8.7}$ and $f_{10.8}$ get smaller and BTD(8.7-10.8) > 0, since $f_{10.8}$ and $f_{8.7}$ show a linear relationship and the BTD(8.7-10.8) = 0 line is convex. For large τ ($\tau = 30$) the TOA radiance approaches the radiance emitted by a black body with a temperature equal to the CTT. Hence, the radiance fractions for large τ depend on the CTT and lie on the BTD(8.7-
570 10.8) = 0 line (see Fig. B1). Overall, for increasing τ from 0 to 30, the Schwarzschild radiance fractions form a line from $f_{8.7} = f_{10.8} = 1$ to the radiance fraction values corresponding to the CTT black body radiance. It follows from the convex shape of the BTD(8.7-10.8) = 0 line that lower CTTs lead to larger BTD(8.7-10.8) values (see Fig. B1). The fact that the Schwarzschild radiance fraction line deviates from the BTD(8.7-10.8) = 0 line such that BTD(8.7-10.8) > 0, depending on the CTT, is a representation of the BTD Nonlinearity Shift equivalent to Fig. 4(b). The property that $f_{10.8}$ is a linear function of
575 $f_{8.7}$ can be shown from the Schwarzschild equation. Solving Eq. 3 for $e^{-\tau}$ for a given wavelength λ_0 and inserting it into the Schwarzschild equation for a second wavelength λ_1 gives

$$R_{\text{TOA},\lambda_1}^S = k + m R_{\text{TOA},\lambda_0}^S, \quad (\text{B3})$$

with

$$m = \frac{B_{\lambda_1}(T_s) - B_{\lambda_1}(\text{CTT})}{B_{\lambda_0}(T_s) - B_{\lambda_0}(\text{CTT})}, \quad (\text{B4})$$

$$580 \quad k = B_{\lambda_1}(T_s) - B_{\lambda_0}(T_s)m, \quad (\text{B5})$$

i.e. a linear relationship between R_{TOA,λ_1} and R_{TOA,λ_0} and therefore also between f_{λ_1} and f_{λ_0} .

So far we have set τ constant for all wavelengths in the Schwarzschild equation. To see what happens in the Schwarzschild model for different τ at different wavelengths, i.e. $\tau_{\lambda_0} \neq \tau_{\lambda_1}$, we add a small perturbation to τ_{λ_1} ,

$$\tau_{\lambda_1} = \tau_{\lambda_0} + \delta\tau. \quad (\text{B6})$$

585 Since the Schwarzschild equation neglects scattering, τ_{λ} is determined by the absorption coefficient $\beta_{\text{abs},\lambda}$ and the cloud water path. For $\lambda_1 = 10.8 \mu\text{m}$ and $\lambda_0 = 8.7 \mu\text{m}$, the absorption coefficients $\beta_{\text{abs},8.7} < \beta_{\text{abs},10.8}$, meaning that if scattering is neglected $\tau_{8.7} < \tau_{10.8}$ and $\delta\tau > 0$ for this case. Solving Eq. 3 for a given λ_0 analogue to above for $e^{-\tau_{\lambda_0}}$ and inserting into Eq. 3 for λ_1 gives

$$R_{\text{TOA},\lambda_1}^{\text{S}} = k + m R_{\text{TOA},\lambda_0}^{\text{S}} - \delta\tau e^{-\tau_{\lambda_0}} (B_{\lambda_1}(T_s) - B_{\lambda_1}(\text{CTT})), \quad (\text{B7})$$

590 where we used $e^{-\delta\tau} \approx 1 - \delta\tau$. Hence, since $\delta\tau > 0$ for $\lambda_1 = 10.8 \mu\text{m}$ and $\lambda_0 = 8.7 \mu\text{m}$, $R_{\text{TOA},10.8}^{\text{S}}$ decreases when we add a perturbation $\tau_{10.8} = \tau_{8.7} + \delta\tau$. This makes physical sense, since a larger $\tau_{10.8}$ compared to $\tau_{8.7}$ means that less radiance is transmitted through the cloud at 10.8 compared to 8.7 μm . The amount by which $R_{\text{TOA},10.8}^{\text{S}}$ decreases is determined by the difference between surface and cloud top radiance, $B_{\lambda_1}(T_s) - B_{\lambda_1}(\text{CTT})$, and the factor $\delta\tau e^{-\tau_{\lambda_0}}$. For $\tau_{\lambda_0} \rightarrow 0$, meaning that the cloud water path approaches zero, $\delta\tau \rightarrow 0$. For large τ_{λ_0} , $e^{-\tau_{\lambda_0}} \rightarrow 0$. Hence, the last term in Eq. B7 vanishes for very small
595 or large τ_{λ_0} . For the τ_{λ_0} values in between, the perturbation $\delta\tau$ leads to a decrease of $R_{\text{TOA},10.8}^{\text{S}}$ and therefore of $f_{10.8}$. As a result, the Schwarzschild radiance fraction line in $f_{8.7}$ - $f_{10.8}$ -space deviates from a linear to a concave line. This deviation is stronger for larger $\delta\tau$ (i.e. larger differences between $\tau_{10.8}$ and $\tau_{8.7}$), as well as for larger differences between the surface and the cloud top radiance, $B_{\lambda_1}(T_s) - B_{\lambda_1}(\text{CTT})$.

As a last step of this analysis, we study the full RT model in $f_{8.7}$ - $f_{10.8}$ -space. Recall that in the full RT model, in general,
600 $\tau_{8.7} \neq \tau_{10.8} \neq \tau$, where τ as usually refers to the optical thickness at 550 nm. Figure B1 shows the radiance fractions $f_{8.7}$ and $f_{10.8}$ computed with the full RT model for an ice cloud for varying τ and two different CTTs in blue and green solid lines. Molecular absorption is switched off for these examples. Note that this is an equivalent representation of BTD(8.7-10.8) as the corresponding CTT curves in Fig. 9. For increasing τ from 0 to 30, the radiance fractions of the full RT model form curves from $f_{8.7} = f_{10.8} = 1$ to the radiance fraction values corresponding to the black body radiance of their CTT. These curves are
605 concave, as expected from our theoretical considerations above (see Eq. B7). This concave shape, as explained above, can be attributed to differences in the absorption coefficients of the two wavelengths, $\beta_{\text{abs},8.7} < \beta_{\text{abs},10.8}$. The concave shape results in higher BTD values compared to the Schwarzschild BTD^{S} values, where $\tau_{8.7} = \tau_{10.8} = \tau$ (compare $\text{BTD}(8.7-10.8)$ along the solid and dotted lines in Fig. B1). The figure also shows that the deviation from the linear Schwarzschild radiance fraction lines is larger for lower CTTs - in accordance with our theoretical considerations (see Eq. B7).

610 This leads to the following interpretation of Fig. B1: The Schwarzschild radiance fraction lines in Fig. B1 (dotted lines) represent the pure BTD Nonlinearity Shift, which induces positive BTD values even though τ is the same in all wavelengths. Adding spectral differences between the cloud optical properties "pushes" the radiance fraction lines into a concave shape and further increases BTD. Hence, the difference between the $\text{BTD}(8.7-10.8) = 0$ line and the Schwarzschild radiance fraction lines

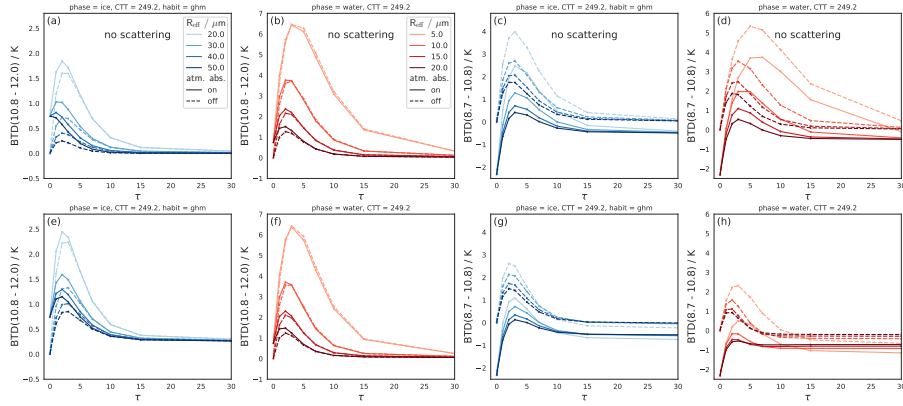


Figure C1. Effects of varying R_{eff} on BTD(10.8-12.0) and BTD(8.7-10.8) as functions of τ for ice clouds (blue) and liquid clouds (orange/red) and scattering switched off (top row) and switched on (bottom row). Solid lines indicate a "normal" absorbing atmosphere, dashed lines indicate that molecular absorption is switched off.

in Fig. B1 is due to the Nonlinearity of the transformation from radiances to BTs; the difference between the Schwarzschild radiance fraction lines and the full RT model (solid lines) in Fig. B1 is due to the spectral differences in cloud optical properties. Lower CTTs increase both the BTD Nonlinearity Shift and the effects of spectral differences between the cloud optical properties.

Appendix C: Effects of R_{eff} on BTDs - disentangling absorption and scattering effects

Figure C1 shows the sensitivity of both BTDs with R_{eff} broken down into effects of absorption and scattering. The two rows show the same cloud scenarios, once with scattering switched off (top row) and once with scattering switched on (bottom row). The figure shows that the effects of absorption lead to increasing values for smaller R_{eff} for both BTDs (top row of Fig. C1).

For BTD(10.8-12.0), the effect of scattering is similar for varying R_{eff} and comparatively small (increases (decreases) BTD(10.8-12.0) by ≈ 0.5 K for ice (water) clouds; compare Fig. C1(a,b) with (e,f)). For BTD(8.7-10.8), scattering effects are stronger than for BTD(10.8-12.0) and depend on R_{eff} : Scattering leads to a stronger decrease of BTD(8.7-10.8) for smaller R_{eff} (compare Fig. C1(c,d) with (g,h)). Since, however, the absorption effects are stronger, BTD(8.7-10.8) increases with decreasing R_{eff} (Fig. C1(g,h)).

Appendix D: Comparison to measured satellite data

Figure D1 shows a comparison of the RT results with measured SEVIRI data. The SEVIRI data was collocated with the active satellite product DARDAR (Delanoë and Hogan, 2010) containing information on the cloud phase (for more details see Mayer et al. (2023)). The plot on the left shows ice clouds; the plot on the right water clouds. As in Sect. 6.1 and Sect. 6, the RT results

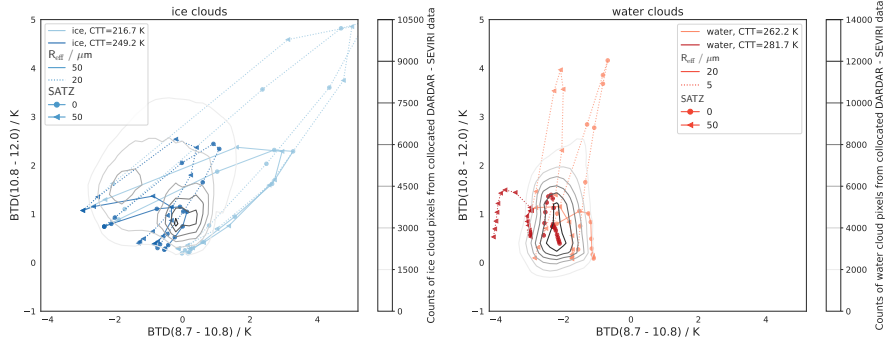


Figure D1. Comparison of RT results with measured SEVIRI data. The RT results are displayed as in Fig. 11, but for a fixed ice crystal habit (ghm) and two SATZ values (different markers). The corresponding counts of measured SEVIRI data is overlaid as contours in grey.

show boundary cases of "typical" cloud scenarios in blue and red, as indicated in the legend. In addition to SATZ=0°, we also show the RT results for SATZ=50°, in order to be able to compare the RT results to a large number of measurements with angles between these two cases. The measured SEVIRI data with the corresponding constraints (i.e. data of ice or water clouds within CTT and SATZ boundaries as for the RT calculations) are plotted on top of the RT results in grey. The figure shows that
 635 the RT results and measured SEVIRI data have a large overlap. Hence, the computed ranges of BTDC values are realistic.

Appendix E: Effects of cloud geometric thickness and vertical R_{eff} inhomogeneity on BTDCs

Figure E1 shows a sensitivity analysis for varying cloud geometric thickness between 1 km and 4 km. For constant τ , a larger cloud geometric thickness means that radiation originates from deeper within the cloud (in terms of geometric depth, implying a larger temperature difference). This depth can differ for different wavelengths, leading to a dependence of BTDCs on geometric
 640 thickness (Piontek et al., 2021a). Figure E1 shows that the sensitivity to geometric thickness is comparably small and mostly \lesssim 0.5 K. An exception are liquid clouds with very small R_{eff} for BTDC(10.8-12.0), where the sensitivity to geometric thickness can exceed 1 K. For the case of liquid clouds with CTT = 281.7 K the CTH is at an altitude of 1 km in the US-standard atmospheric profile. Geometric thicknesses > 1 km are therefore not possible in this case.

Figure E2 shows the sensitivity of the BTDCs to vertical inhomogeneity of R_{eff} . To model this inhomogeneity and capture
 645 its basic effects on BTDCs we use a simple setup of clouds with a total geometric thickness of 2 km, consisting of two 1 km thick layers (layer 1 on top, layer 2 at the bottom, specified in the subscripts). Both layers have the same optical thickness, $\tau_1 = \tau_2 = \tau/2$. Cloud layer 1 has a $R_{\text{eff},1}$ which is either equal, smaller or larger to layer 2, $R_{\text{eff},1} \gtrless R_{\text{eff},2}$ (case A, B or C), such that the average $\overline{R_{\text{eff}}}$ is the same for all three cases (case A: $R_{\text{eff},1} = R_{\text{eff},2} = \overline{R_{\text{eff}}}$; case B: $R_{\text{eff},1} = 0.8\overline{R_{\text{eff}}} < R_{\text{eff},2} = 1.2\overline{R_{\text{eff}}}$; case C: $R_{\text{eff},1} = 1.2\overline{R_{\text{eff}}} > R_{\text{eff},2} = 0.8\overline{R_{\text{eff}}}$). Hence, in case A, the R_{eff} is homogeneous; in case B and C it is inhomogeneous.
 650 This model of vertical inhomogeneity is of course very simplified, but it is useful for calculating a rough estimate of the magnitude of inhomogeneity effects and for understanding the underlying physics.

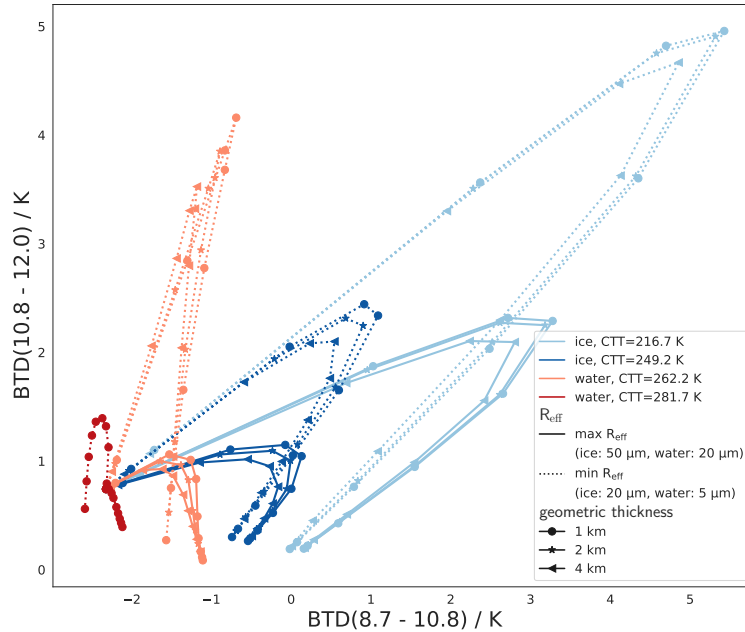


Figure E1. Same as Fig. 11, but for a fixed ice crystal habit (ghm) and varying geometric thickness of the cloud (in different markers)

Overall, the sensitivity to vertical R_{eff} inhomogeneity is comparatively small ($\lesssim 0.5$ K). The effects of the vertical R_{eff} inhomogeneity on the BTDs are due on the one hand to its effects on the transmittance of the surface radiance and on the other hand to its effects on the emittance of the cloud itself. Zhang et al. (2010) show (for ice clouds) that the nonlinear dependence of the optical properties on R_{eff} leads to an increased weighting of small particles in the signal of the transmitted radiance. This leads to larger BTDs for cases where the cloud is (partly) composed of particles smaller than the average (the inhomogeneous cases B and C), where transmittance is the dominant process (small τ). However, as can be seen in Fig. E2 for small τ ($\lesssim 2$), this effect is very small compared to other dependencies, since the cloud transmittance in the infrared window depends mainly on τ and less on the details of the vertical R_{eff} profile of the cloud (Zhang et al., 2010). On the other hand, when the cloud emittance dominates for increasing τ , the signal from the particles at the bottom of the cloud is (partially) absorbed by the top cloud layer. The BTD signal is then dominated by the R_{eff} of the top cloud layer ($R_{\text{eff},1}$). This makes a difference mainly for small R_{eff} values (see $\min \overline{R_{\text{eff}}}$ curves in Fig. E2), as the BTDs depend non-linearly on R_{eff} (see Fig. 7). Figure E2 shows that these vertical R_{eff} inhomogeneity effects on cloud emittance (dominant for large τ) lead to larger overall effects on the BTDs compared to the effects on transmitted surface radiance (dominant for small τ).

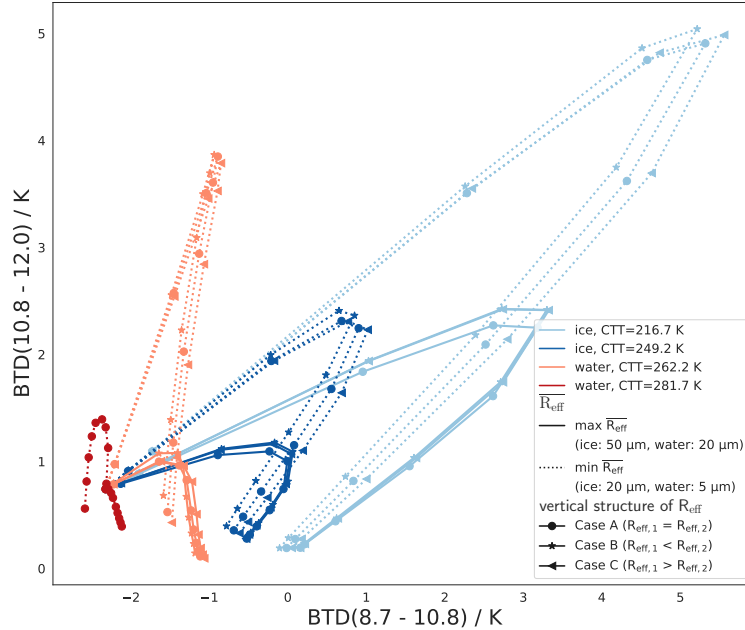


Figure E2. Same as Fig. 11, but for fixed ice crystal habit (ghm) and vertical inhomogeneity of R_{eff} (in different markers): the cloud consists of two layers (layer 1 on top, layer 2 at the bottom, specified in the subscripts), each with geometric thickness of 1 km and the same layer optical thickness, $\tau_1 = \tau_2 = \tau/2$. Cloud layer 1 has a $R_{eff,1}$ which is either equal, smaller or larger to layer 2, $R_{eff,1} \leq R_{eff,2}$ (case A, B or C), such that the average $\overline{R_{eff}}$ is the same for all three cases (case A: $R_{eff,1} = R_{eff,2} = \overline{R_{eff}}$; case B: $R_{eff,1} = 0.8\overline{R_{eff}} < R_{eff,2} = 1.2\overline{R_{eff}}$; case C: $R_{eff,1} = 1.2\overline{R_{eff}} > R_{eff,2} = 0.8\overline{R_{eff}}$). No R_{eff} inhomogeneity is shown for the case of liquid clouds with $CTT = 281.7$ K, since their CTH is at an altitude of 1 km, leaving room for only one cloud layer.

665 *Author contributions.* All authors contributed to the project through discussions. JM carried out the simulations and the analysis of the data with valuable feedback from LB, BM and RM. LB and CV supervised the project and provided scientific feedback. JM took the lead in writing the manuscript. All authors provided feedback on the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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