

# Prediction of Hysteretic Matric Potential Dynamics Using Artificial Intelligence: Application of Autoencoder Neural Networks

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## Abstract

Information on soil water potential is essential to assess soil moisture state, to prevent soil compaction in weak soils, and to optimize crop management. In lack of direct measurements, the soil water potential values must be deduced from soil water content dynamics that can be monitored at plot scale or obtained at larger scale from remote sensing information. Because the relationship between water content and soil water potential in natural field soils is highly ambiguous, the prediction of soil water potential from water content data is a big challenge. The hysteretic relationship observed in nine soil profiles in the region of Solothurn (Switzerland) is not a simple function of texture or wetting and drainage cycles but depends on seasonal patterns that may be related to soil structural dynamics. Because the physical mechanisms governing seasonal hysteresis are unclear, we developed a deep neural network model that predicts water potential changes using rainfall, potential evapotranspiration, and water content time series as inputs. To adapt the model for multiple locations, we incorporated a Deep Autoencoder Neural Network as a classifier. The autoencoder compresses the water content time series into a site-specific feature that is highly representative of the underlying water content dynamics of each site and quantifies the similarity of dynamic patterns. By adding the Autoencoder's output as an additional input and training the neural network model with three stations located in three major classes founded by the autoencoder, we predict matric potential for other sites. This method has the potential to deduce the dynamics of matric potential from water content data (including satellite data) despite strong seasonal effects that cannot be captured by standard methods.

## 34 1. Introduction

35 The soil water characteristics curve SWC relates the matric potential (MP) and water content (WC) and  
36 is the key physical property to quantify soil water dynamics (Tuller & Or, 2023). The SWC (also  
37 denoted as soil water retention curve or pressure-saturation relationship) depends on both soil texture  
38 and structure and differs with soil types and soil textural classes (Rawls, et al., 2003; Shwetha & Varija,  
39 2015). The SWC contains information on the pore size distribution and allows the assessment of flow  
40 and transport properties for different hydration states (Rostami, et al., 2015; Menon, et al., 2020). To  
41 provide a complete characterization of the actual soil moisture state and flow regimes, information on  
42 both the matric potential and the water content must be specified. Information on volumetric water  
43 content is needed to assess the free storage capacity, optimize water management, and to formulate  
44 mass balance. The matric water potential is a component of the total and hydraulic soil water potential  
45 and determines the water flow in direction of decreasing water potential to achieve equilibrium with its  
46 surroundings (Ma, et al., 2022). The matric potential is also of particular interest to assess mechanical  
47 stability of a soil (Holthusen, et al., 2010; Lu, et al., 2010). The capillary and adsorptive forces expressed  
48 with the matric potential define the unsaturated soil strength mitigating soil compaction by heavy  
49 machinery in construction work, farming, and forestry (Smith, et al., 2001). For example, matric  
50 potential thresholds are defined in various regions of Switzerland to prevent mechanical damage and  
51 regulate the maximum load linked to factors like soil type, texture, and vehicle impact (Bundesamt für  
52 Energiewirtschaft, 1997). Other important potential thresholds are the wilting point and the field  
53 capacity, characterizing the plant available water (Gupta, et al., 2023).

54 It would be optimal to determine the soil moisture status relative to these potential thresholds based on  
55 information of water content using the SWC, without direct measurement of the matric potential. In that  
56 case, matric potential dynamics could be deduced from remote sensing water content data that are  
57 available at various scales. However, the application of this procedure is limited by two effects. Firstly,  
58 under saturated conditions, the water potential can change without modifying the volumetric water  
59 content. The transition of conditions with negative water potential within the capillary fringe to positive  
60 pressures below a water table is crucial for the triggering of landslides (Gallipoli, et al., 2003). Secondly,

61 the SWC under field conditions is often an ambiguous relationship between potential and water content  
62 due to hysteretic and dynamic effect as will be discussed next.

63 The SWC is typically measured in the lab as series of equilibrium states obtained during drainage, with  
64 one water content value assigned to the applied pressure. The results of such small-scale experiments  
65 are not sensitive to structural pores that can be found at the field scale (Romero-Ruiz, et al., 2018) and  
66 can thus be expressed as function of basic soil properties (texture, bulk density, content of organic  
67 material) using pedotransfer functions (PTF; Zuo & He, 2021). Because these PTFs ignore the effects  
68 of soil structures including macropores and cracks (Basile, et al., 2019) and are trained with data from  
69 small samples with artificially high initial saturation conditions, their applicability to model dynamic  
70 processes in the field is limited. Another limitation is the underlying assumption of an unambiguous  
71 relationship between water content and matric potential (and hydraulic conductivity). In all land surface  
72 models, water content is linked by an unambiguous relationship between water content and matric  
73 potential. In reality, this relationship is highly ambiguous under field conditions as was analyzed in  
74 detail by Hannes et al. (2016) and as we will show later in this paper as well.

75 Hannes et al. (2016) analyzed long-term experiments and concluded that the high variation of matric  
76 potential values for the same water content are a result of hysteresis, dynamic effects, and structural  
77 changes during the season. Hysteresis is related to differences in wetting and drying cycles (Capparelli  
78 & Spolverino, 2020) as controlled by different pore structures controlling air- or water invasion and  
79 differences in receding or advancing wetting angles (Fomin, et al., 2023). Hysteresis is often manifested  
80 in coarse textured soils and occurs as well during slow processes. Another process resulting in an  
81 ambiguous pressure-saturation relationship is dynamic effects with water contents that are not in  
82 equilibrium with the quickly changing potential (Ross & Smettem, 2000). Finally, the size of structural  
83 pores is not constant with time but changes with season, water content, and soil formation processes  
84 (Fu, et al., 2021). The combined effect of hysteresis, non-equilibrium, and structural changes makes it  
85 extremely challenging to deduce soil matric potential from information on water content. Also, the  
86 implementation of these combined effects in physically-based models of unsaturated water flow is not  
87 straightforward. As an alternative approach to physically-based models, machine learning can be

88 applied to simulate the complex relationship between matric potential and water content under field  
89 conditions. In this study, we will apply a deep neural network (DNN).

90 Deep neural networks (DNN) have demonstrated their effectiveness as a powerful numerical tool for  
91 resolving complex patterns. Their ability to learn from data and recognize intricate relationships makes  
92 them valuable in various fields, including the modeling of soil water characteristics. For example, Jain,  
93 et al. (2004) and Achieng (2019) used artificial neural network (ANN) models to predict the hysteretic  
94 water content from observed matric potential values. However, both publications simulated lab data  
95 under equilibrium conditions and cannot be applied for the more complex dynamic processes in the  
96 field. In addition, the models were site-specific and needed both water content and matric potential  
97 information for the training. Here we will apply a different DNN using an autoencoder approach. As  
98 we will explain in the theory section, the autoencoder condenses the complexity of temporal (and  
99 spatial) patterns into a single (or a few) number(s). The hypothesis of this study is that the autoencoder  
100 value is a new and unique characterization of the soil moisture dynamics and can be used to predict  
101 matric potential dynamics from observed water content data. The paper is organized as follows: in  
102 section 2, the study sites and the basics of the deep neural network with the autoencoder approach are  
103 presented. The results section compares the model performance of site-specific deep neural network  
104 (DNN) and shows the possibility to build a generalized DNN using the autoencoder analysis as model  
105 input. Limits and possible applications of the model approach are discussed in section 5.

## 106 2. Material and methods

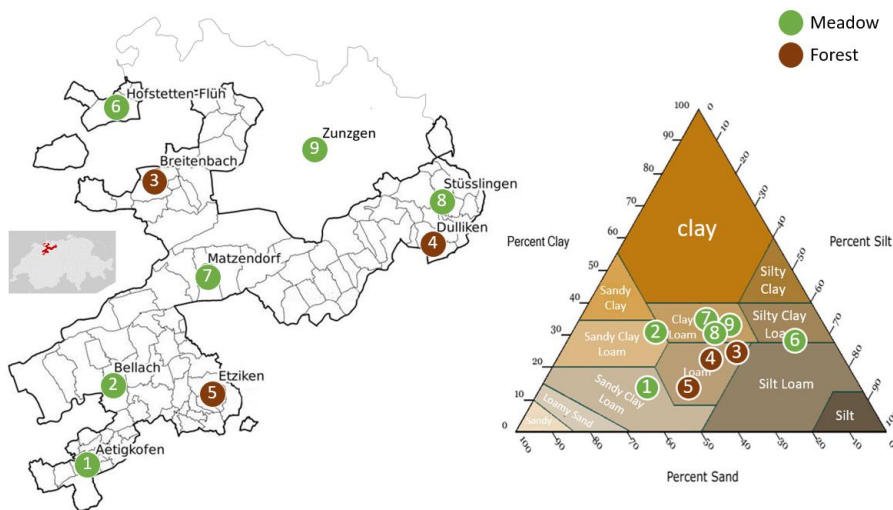
107 In a first step, matric potential time series were simulated at nine sites in the region of Solothurn  
108 (Switzerland) using site specific ANN model, to proof that the ANN models can predict matric potential  
109 from water content dynamics with site specific training. In the next step, the autoencoder analysis of  
110 water content dynamics of all sites was conducted. Finally, the site-specific ANN model was enhanced  
111 and transformed into a multisite model by combining two deep neural networks. This transformation  
112 allowed for a more comprehensive and versatile predictive framework of matric potential as function  
113 of water content.

## 114 2.1 Study area and soil moisture data

115 The study area covers mainly the canton of Solothurn in Switzerland (Fig.1), and thus an area of  
116 approximately 629 km<sup>2</sup>. The climate in Solothurn is classified as oceanic climate (Cfb) according to  
117 Koppen and Geiger climate classification, with an average yearly temperature of 9.5 °C and annual  
118 precipitation of around 1400 mm. Approximately half of the annual precipitation in the canton  
119 undergoes the process of evaporation (~~Auer, et al., 2005~~; Spreafi & Weingartner, 2005). During the  
120 year, the average temperature varies by 19 °C with the highest temperature occurring in the month of  
121 July and the lowest average temperature in January. Regarding precipitation patterns, the month of June  
122 has the highest level of precipitation, while March stands out as the driest month. Soil moisture  
123 dynamics (see below) were studied for the period from 2011 to 2022. For this period, climatic data  
124 ~~were~~ available on the data portal of MeteoSwiss (~~Federal Office for Meteorology and Climatology,~~  
125 2023) (IDAweb, 2024). The data was gathered from the closest meteorological stations to each of the  
126 nine sites in the Solothurn region.

127 Soil moisture data were downloaded from the 'soil monitoring network' (~~Bodenmessnetz; BMN,~~  
128 2023) (BODENMESSNETZ, 2024) collecting data from 65 stations distributed over eleven cantons of  
129 Switzerland. The network's primary objective is to provide real-time soil moisture information for  
130 mitigating soil compaction. ~~BMN~~ BODENMESSNETZ also plays a role in raising awareness among  
131 farmers and foresters about soil compaction, providing a tool to assess the current situation and adjust  
132 the use of heavy machinery based on weather conditions. As the network has been running since 2011,  
133 it now serves as a valuable resource by offering long-term diverse information, including land use,  
134 precipitation amounts, and matric potential measured at various depths (20 and 35 cm depth in most of  
135 the stations, using T8 and T32 tensiometers from METER group). Only at nine sites that are located in  
136 the region of Solothurn, the water content was measured at 20 cm depth (Stevens Hydra Probe). For  
137 these nine sites, daily values in volumetric water content (20 cm), matric potential (20 cm) and  
138 precipitation values were used. The matric potential in the downloaded data was given in kPa and was  
139 transferred to matric potential head with units of cm (1 cm is 0.1 kPa), considering a water density of  
140 1000 kg m<sup>-3</sup> and gravity acceleration of 10 m s<sup>-2</sup>.

141 As the soil moisture decreases, water is drawn from the tensiometer, creating a negative pressure or  
 142 tension. During dry periods, cavitation may occur, causing water vaporization and air bubble formation  
 143 (Mendes & Buzzi, 2013), or tensiometers had to be refilled (Sadeghi, et al., 2020). To address these  
 144 challenges and ensure accurate data collection, various data preprocessing and filtering techniques were  
 145 implemented. These techniques involved identifying and removing outliers, systematically excluding  
 146 data points with water potential values within the problematic dry ranges and filtering out data points  
 147 with extremely low or high water content values. The study also flagged abrupt changes in volumetric  
 148 water content (VWC) and matric potential (MP) for further investigation, as these could indicate  
 149 measurement anomalies. Additionally, a thorough analysis of weekly trends in the data was conducted  
 150 to identify systematic variations over time (see Appendix A).

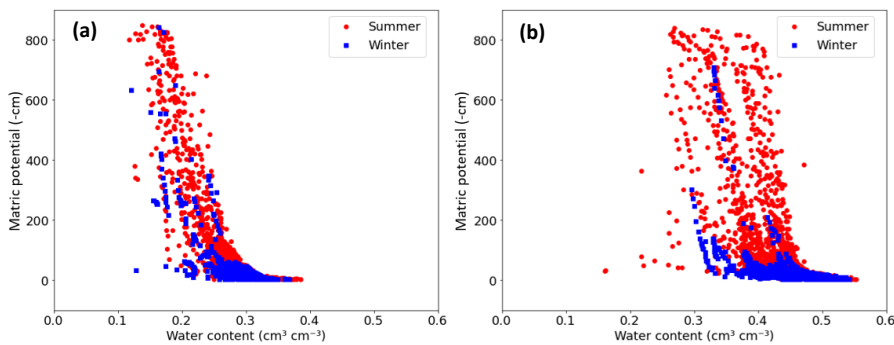


151  
 152 **Figure 1** Overview of the study area with site locations, soil texture, and land cover. The primary focus  
 153 is on the canton of Solothurn, outlined by the black border on the map, with an additional site from the  
 154 canton of Basel (site 9, Zunzgen). Within this region, three sites are categorized as forests, while the  
 155 remaining six sites are designated as meadows. The analyzed soil horizons (20 cm depth) of the study  
 156 area encompasses five soil textural classes as shown in the soil texture triangle.

157 The analyzed soil horizons of the selected locations can be assigned to five different soil textural classes  
 158 (figure 1) and two different land covers (meadow and forest). The location denoted as Matzendorf (site  
 159 #7) contains the highest clay content, whereas locations such as Aetigkofen (site #1) are predominantly  
 160 sandy. Across these nine locations, different relationships between matric potential and water content

161 were deduced from field data as shown in Figure 2 for two sites with low and high variations in water  
 162 content for similar potential values. To show the relevance of seasonal patterns, we differentiate  
 163 between summer (April to September) and winter period (remaining months).

164



165

166 **Figure 2** Soil-Water characteristics curve (SWC) measured in the field at two sites classified into  
 167 summer (April to September) and winter period (remaining months) from 2012 to 2023. (a) The Eetziken  
 168 site (site #5) shows small changes in the SWC dynamics over the years, for both the warm and cold  
 169 period. (b) A contrasting scenario was found for the site in Bellach (site #2) that was characterized by  
 170 a wide range of water content for similar potential values. The unit of matric potential, represented as -  
 171 cm, is equivalent to -0.1 kPa.

## 172 2.2 Deep neural network (DNN)

173 A basic artificial neural network (ANN) comprises one or two hidden interconnected layers, with each

174 layer tasked with the conversion of an input vector ( $\mathbf{x}$ ) into a hidden state vector ( $\mathbf{h}$ ), as described by

175 (Bertels & Willems, 2023). This conversion is accomplished through the utilization of a weight matrix

176 ( $\mathbf{W}$ ) and a bias vector ( $\mathbf{b}$ ), integrated with an activation function (denoted as "act" in eq (1)) with eq.

177 (1):

$$178 \mathbf{h} = f(\mathbf{x})(\mathbf{x}) = \text{act}(\mathbf{W} \cdot \mathbf{x} + \mathbf{b} \cdot \mathbf{x} + \mathbf{b}) \quad (1)$$

179 Where  $f(\mathbf{x})$  represents the transformation function applied to the input vector ( $\mathbf{x}$ ), with a weight matrix

180 ( $\mathbf{W}$ ) and a bias vector ( $\mathbf{b}$ ), integrated with an activation function (denoted as "act").

181 To construct a deep neural network (DNN), multiple layers (more than two hidden layers) are

182 interconnected to form a 'multilayer perceptron.' The training process involves finding optimal values

183 for the weights and biases in the network using suitable optimization techniques (Bertels & Willems,

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184 2023). In this study, DNN was built to predict the daily MP for the nine sites. The process involved  
185 several key steps. First, in the design of the neural network, activation functions were carefully selected  
186 and integrated to introduce non-linearity into the model's transformations (Montesinos López, et al.,  
187 2022). The Rectified Linear Unit (ReLU) activation function was employed to mitigate vanishing  
188 gradient problem and enhance the model's ability to handle noisy input. The inclusion of ReLU was  
189 motivated by considerations of computational efficiency, with some attention given to the potential  
190 issue of "dying ReLU" (Montesinos López, et al., 2022; Lu, 2020).

191 Next, the neural network was structured with a total of six layers, including four hidden layers as  
192 suggested by Achieng (2019). All layers were densely connected, fostering strong information flow  
193 between neurons. Crucially, batch normalization was incorporated after the second hidden layer. Batch  
194 normalization is a technique that normalizes the activations within a layer during training, which can  
195 help mitigate issues like internal covariate shift and accelerate convergence (Ioffe, 2015). The choice  
196 of the optimization method was the Adam optimizer, a powerful tool for training neural networks. It  
197 adaptively adjusted learning rates, thereby optimizing the learning process, and enabling rapid  
198 convergence while employing Mean Squared Error (MSE) as the loss function (Kingma & Ba, 2014).  
199 To prevent overfitting by the Adam optimizer, an early stopping mechanism was implemented. This  
200 mechanism continuously monitored the loss function for the hold out data during training, ceasing the  
201 process if no improvement or a sudden increase was detected over a predetermined number of  
202 consecutive epochs.

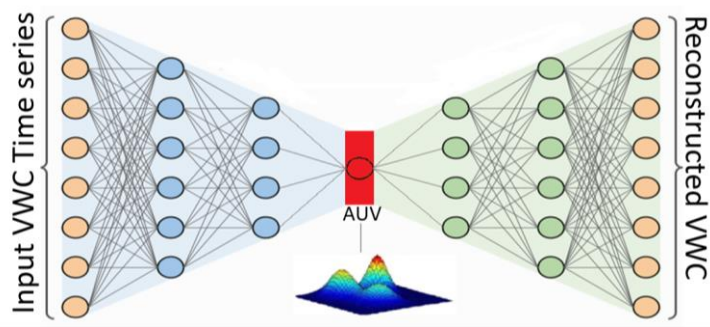
203 The initial deep neural networks (DNN) were configured with 4 input parameters and the daily  
204 logarithmic scaled matric potential (MP) value as output. The input parameters consisted of  
205 precipitation, potential evapotranspiration, measured VWC, and the weekly percentage change in  
206 VWC. As the prediction process progressed, two major issues were identified. Firstly, the influence of  
207 the VWC measurements on the training process was found to be predominant. Consequently, a decision  
208 was made to increase the weight of precipitation and potential evapotranspiration in the calculation  
209 process by incorporating three new input parameters: the weekly total precipitation and  
210 evapotranspiration (the sum of the current day and the preceding six days), along with the difference



211 between these two new components. Secondly, the use of logarithmic scaled MP values was found to  
212 be highly sensitive to data availability. Therefore, a decision was made to retrain the model using  
213 absolute linear MP values (see Appendix B). In total, the final model was equipped with 7 input  
214 parameters to predict the absolute linear MP values for a given location. For each site, a site-specific  
215 DNN was built. The extent of the training data is predominantly influenced by site-specific  
216 characteristics. For instance, sites characterized by sandy soils necessitated a shorter training duration  
217 in contrast to sites with a higher clay content. Typically, the training dataset spanned a duration of 4 to  
218 7 years. During this period, 70% of the data were randomly selected for training, while the remaining  
219 30% were set aside as holdout data (Gholamy, et al., 2018). The extra years of data beyond the initial  
220 training period were reserved for validation purposes.

### 221 2.3 Autoencoder neural network

222 The autoencoder, consisting of an encoder and a decoder, is an unsupervised deep neural network that  
223 learns how to efficiently compress input data into a meaningful representation and subsequently  
224 reconstruct the original data from this compressed form (Chen & Guo, 2023). By connecting the encoder  
225 and decoder, the autoencoder effectively captures important patterns and variations present in the data,  
226 enabling comprehensive analysis and interpretation (Chen & Guo, 2023). In this study, an autoencoder  
227 neural network (figure 3) was built to analyze the measured VWC time series at 20 cm depth for the 9  
228 sites.

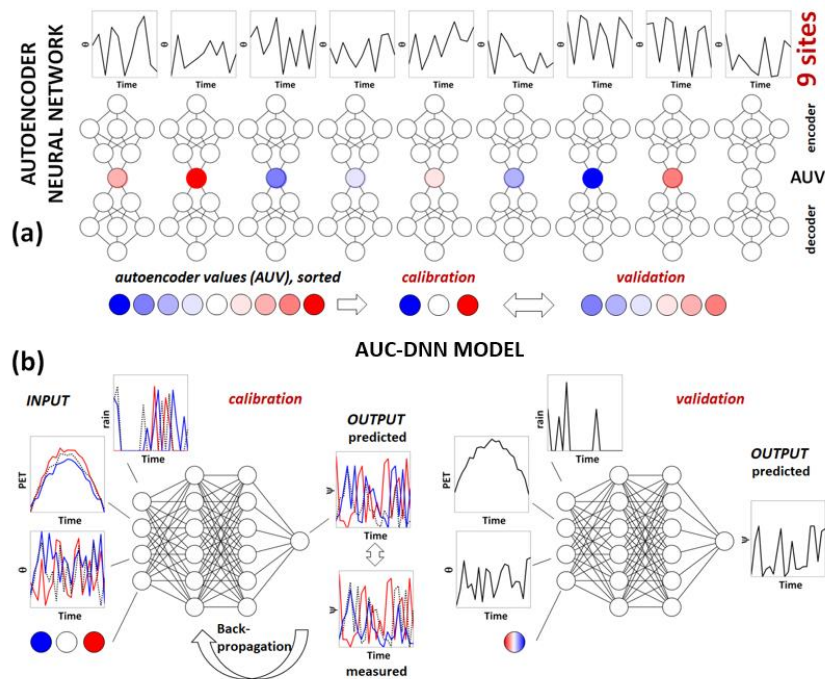


229  
230 **Figure 3** Autoencoder deep neural network for volumetric water content dynamic analysis. In this  
231 illustration, a densely connected autoencoder is utilized to compress the dynamic information of  
232 Volumetric Water Content (VWC) into a singular value, AUV, highlighted in red. The process begins  
233 with the encoder, depicted in blue, extracting the AUV from the measured volumetric water content

234 time series (left orange layer). Subsequently, the densely connected decoder, represented in green,  
235 utilizes the AUV to reconstruct the VWC (orange layer at the right). Both the encoder and decoder,  
236 characterized by dense connections, optimized the AUV value by minimizing the error between the  
237 measured VWC and the reconstructed VWC.

238 The process was as follows. Firstly, an encoder neural network was created for each site. Its objective  
239 was to take the VWC time series as input and gradually reduce its dimensionality through hidden layers  
240 (Chen & Guo, 2023). The encoders' output was a single site-specific latent representation, called  
241 Autoencoder Value (AUV), and captures essential features of the VWC dynamics (Chen & Guo, 2023).  
242 Subsequently, a decoder neural network was developed to utilize the AUV value as reference to  
243 reconstruct the original VWC time series data. The success of this reconstruction depends on the  
244 training process, which aimed to optimize the AUV value by minimizing the error between the original  
245 VWC time series and its reconstructed counterpart by minimizing the mean squared error (MSE) value  
246 to less than 0.1.

247 After the optimization process, for each site one autoencoder value (AUV) was obtained. These AUV  
248 were scaled and then used to build a combined model (Figure 4) as follows. The AUV were sorted into  
249 three categories. Subsequently, one site from each category was selected. Finally, the data from the  
250 three chosen sites, each representing one category, were used to train the combined AUC-DNN model.  
251 The final combined model was thus equipped with 8 input parameters to predict the dynamic MP for a  
252 specific location. These parameters consisted of the same 7 inputs employed in the DNN model (section  
253 2.2), complemented by the AUV. The neural network structure, as detailed in section 2.2, remained  
254 unchanged, employing the same optimization techniques.



255  
 256 **Figure 4** Application of two different types of deep neural network for the prediction of matric potential  
 257  $\psi$ . In this conceptual example, the water moisture dynamics of nine sites is considered. (a) The  
 258 autoencoder neural network captures the characteristic features of the soil water content ( $\theta$ ) dynamics,  
 259 assigning an autoencoder value (AUV) to each site. These values are sorted to AUV classes (one site  
 260 from each class was used for calibration, remaining sites for validation). (b) The combined AUC-DNN  
 261 model is built using the calibration sites with rainfall, potential evapotranspiration (PET), water content,  
 262 and AUV as part of the 8-input parameters. The predicted matric potential ( $\psi$ ) is compared to measured  
 263 values for backpropagation. The calibrated DNN is then used to predict  $\psi$  for the remaining sites.

264 Initially, 70% of the data from each of the training sites were randomly selected for the training dataset.  
 265 Subsequently, the remaining 30% of the data were set aside as the holdout dataset, serving as a  
 266 benchmark for assessing model performance. The developed AUC-DNN was then applied for the other  
 267 six sites (with the same input variables including AUV) to predict the entire datasets of those unseen  
 268 sites. The combined model has thus the strengths of both components—the DNN' ability to understand  
 269 dynamic MP patterns and the feature extraction capabilities of the autoencoder. This shift in the model's  
 270 strength extends it from being site-specific to encompassing multiple sites, enabling it to gain a broader  
 271 understanding of how the dynamic MP and AUV values relate.

## 2.4 Statistical evaluation

The evaluation of model performance is carried out by comparing the model predictions to the measured data. While there is no universal consensus on a standardized evaluation procedure, it is widely recognized that a multi-objective approach should be adopted e.g., (Boyle, et al., 2000; Willems, 2009). In this study, a combination of four evaluations tools was adopted. First, a scatter plot of observations against simulated values was utilized to visualize the degree of alignment with the identity line (often referred to as the 1:1 line). This graphical approach allowed for a qualitative assessment of model performance. A closer concentration of data points near the 1:1 line indicated higher agreement between calculated and observed values. Moreover, this graphical method includes the 95 % confidence interval area which help in scrutinizing the model's consistency across different prediction ranges and detecting potential biases within the model's performance (Ritter & Muñoz-Carpena, 2013). The second criterion evaluates the distribution of (signed) prediction errors (eq(2)). Ideally, the error distribution should be centered around zero, following a normal distribution pattern around this point with low standard deviation. Such a distribution indicates an unbiased model with errors that tend to balance out. Deviations from this pattern may suggest model bias or other unexpected characteristics in the prediction errors  $PE$  (Ouden, et al., 2012).

$$PE = O_i - P_i \quad (2)$$

with observed  $O_i$  and predicted matrix potential value  $P_i$ . The third evaluation metric was the root means squared error (RMSE; eq (3a)). RMSE with a value of zero indicates perfect fit, while higher RMSE value means worse model performance (Ritter & Muñoz-Carpena, 2013). The final criterion for model evaluation involved the use of the dimensionless goodness-of-fit indicator (eq (3b)), known as the (Nash & Sutcliffe, 1970) coefficient of efficiency (NSE). NSE, which ranges from negative infinity to 1, serves as an indicator of model performance, with a value of 1 indicating a perfect fit, while a negative NSE suggests that using the means of the observed values is a better representative for the data than the evaluated model itself (Ritter & Muñoz-Carpena, 2013; Gupta & Kling, 2011). An NSE value of  $\geq 0.55$  was established as  $> 0.75$  indicates a very good model, while an NSE value  $< 0.5$  signifies unsatisfactory results (Moriassi et al., 2007). In Gupta et al. (1999) a threshold NSE-value of 0.80 was

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used for a good model performance (Jiang, et al., 2020) and an NSE value > 0.80 as criterion for an optimal model is applied here as well. The RMSE and NSE are defined by:

$$RMSE = \sqrt{\frac{\sum(O_i - P_i)^2}{N}} \quad (3a)$$

$$NSE = 1 - \frac{\sum(O_i - P_i)^2}{\sum(O_i - \bar{O})^2} \quad (3b)$$

where  $O_i$  represents the measured value,  $P_i$  the simulation output, and  $\bar{O}$  the mean of the observed values, all within the context of a sample size  $N$ .

### 3. Results

Following the model discussion in section 2.2 and 2.3, we present first the results of the site-specific tests of predicting matric potential dynamics with a deep neural network (water content, rainfall and evapotranspiration as input data), before the role of autoencoder value is considered.

#### 3.1 Deep neural network modeling without autoencoder

The site-specific DNN model was used to simulate the time series for all nine sites. In Figure 5, the results are shown for the Stüsslingen site (size #8, clay loam, meadow). The model was trained on data that had 1825 days of observations from January 2012 to January 2020. The data was split randomly into two parts: 1) a calibration dataset that had 1277 days and 2) a holdout dataset that had 548 days. The model was then validated on data from February 2018 to January 2023 (1379 days). A strong agreement between the model and the observed data was discovered in both the training and validation datasets (figure 5c) as reflected by the low RMSE value and the high NSE value (table 1). Furthermore, it was noticed that the error distribution exhibited a predominantly normal pattern with minimal bias towards higher observed values compared to the predicted values (figure 5d). These findings suggest that the site-specific DNN-model was not only able to be generalized well to unseen data but also demonstrated a reliable ability to predict MP.

The statistical evaluation (Table 1) reveals a consistent performance across both the training and validation periods for the Stüsslingen site, offering compelling evidence that the model avoids

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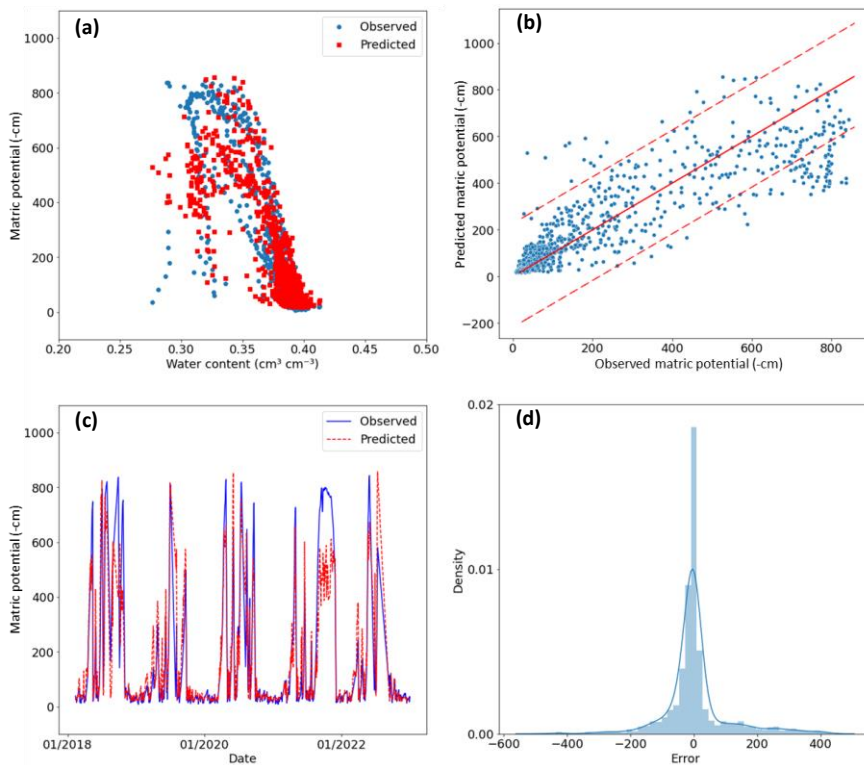
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325 overfitting. Additionally, when it comes to predicting MP values, the 95 % confidence interval indicates  
 326 that the model can capture well the overall dynamics (Figure 5b). However, the model performance  
 327 exhibits higher deviations for values exceeding 400 cm and consistently underestimates values higher  
 328 than 600 cm (figure 5b), which could explain the mild positive skewness observed in the distribution  
 329 of prediction errors in figure 5d.



330  
 331 **Figure 5** Graphical evaluation of the performance of the site-specific deep neural network (DNN) for  
 332 validation for the Stüsslingen site (site #8) for the validation period 2018 to 2022. **(a)** Comparison  
 333 between the simulated and measured soil water characteristics curve. **(b)** Scatter plot comparing  
 334 simulated and measured matric potential values, providing a visual representation of the level of  
 335 conformity to the identity line. The two dashed lines represent the 95% confidence interval around the  
 336 identity line, providing a visual assessment of the level of agreement. **(c)** Model validation presenting  
 337 time series with the observed and predicted matric potential. **(d)** Analysis of the distribution of  
 338 prediction errors (observed minus predicted values) with positively mild skewed distribution

339 Comparing the performance for the ‘holdout’ period (randomly chosen days between 2012 and 2019)  
 340 of the nine site-specific DNN models, the NSE index is larger than 0.55 (‘good’) for all and larger than

341 0.80 (\*optimal) for six sites. For all sites it was thus possible to build a DNN model with good model  
342 performance for the randomly chosen test days. However, for the validation period, only four showed  
343 optimal performance (NSE > 0.80). For two forest sites with an optimal performance for the holdout  
344 period (Dulliken, site #4, and Etziken, site #5), the NSE dropped from a range between 0.82 and 0.88  
345 to a range between 0.73 and 0.75 (table 1). Obviously, the model captured the overall short term  
346 dynamics during training (randomly chosen days) but faced problems in the precise prediction of the  
347 long validation period. An extended training period may be necessary to enhance the model's accuracy  
348 for these specific sites. Three grassland sites (Bellach, site #2, Matzendorf, #6, and Hofstetten-Flüh, #5)  
349 showed good but not optimal performance already during the holdout period. As discussed in the next  
350 section, this may be related to large variations of the pressure values for similar water contents and the  
351 corresponding large AUV. Notably, the lower performance observed in the holdout period for  
352 Hofstetten-Flüh could be also linked to data limitations, as only 1200 days were used to train the model  
353 for this specific site (compared to 1825 sites for the other sites).

354 **Table 1** Statistical assessment of calibration (1825 days, until year 2019/2020) and validation results  
355 (years 2018/2019/2020 until years 2020/2021/2022) for nine sites. The holdout dataset was part of the  
356 training period and includes 548 days (30 % of calibration).

Location	AUV (-)	Training (holdout)		Validation	
		NSE (-)	RMSE (-cm)	NSE (-)	RMSE (-cm)
1 Aetigkofen	1.95	0.92	48	0.89	60
2 Bellach	7.00	0.70	98	0.62	125
3 Breitenbach <sup>a, b</sup>	3.56	0.86	82	0.83	96
4 Dulliken <sup>a</sup>	2.19	0.82	55	0.73	103
5 Etziken <sup>a</sup>	1.90	0.88	56	0.75	70
6 Hofstetten-Flüh <sup>b</sup>	5.59	0.76	90	0.63	123
7 Matzendorf	6.39	0.76	83	0.59	133
8 Stüsslingen	4.49	0.80	71	0.80	98
9 Zunzgen	6.44	0.87	62	0.83	73

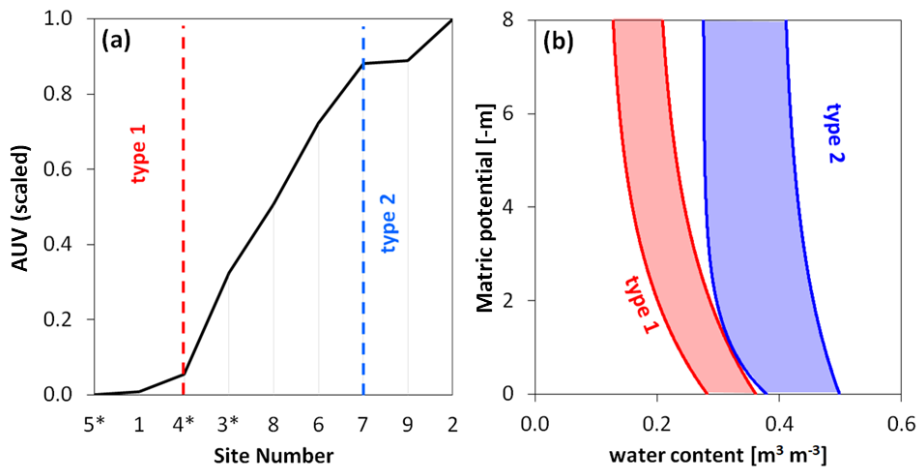
357 <sup>a</sup> forest sites.

358 <sup>b</sup> Sites with limited available data. For those sites, only 1200 days were used for training; Within this training period, a subset  
359 of 360 randomly selected days was designated as a holdout dataset; the validation period for those specific sites was from  
360 2018/2019 to 2022.

### 361 3.2 Autoencoder DNN

362 The Autoencoder values (AUV) deduced from the time series analysis of the volumetric water content  
363 for the period 2012-2022 can be classified in three main groups (figure 6). Soil water characteristics

364 curves (SWC) with low water content at saturated conditions and a small variation of water content for  
 365 similar potential values are assigned to 'type 1', contrasting 'type 2' with large water content values  
 366 and variations. These types of SWC are related to small ('type 1') and high ('type 2') autoencoder  
 367 values (AUV). Sites with AUV between these two classes, are denoted in the following as 'transitional'  
 368 type. As shown in Table 1, the AUV of forest soils are small (mainly 'type 1') with large NSE values.  
 369 In contrast to the forest soils, there are grassland sites with high AUV ('type 2') but small NSE.  
 370 Probably, the high variations of the SWC curve for 'type 2' require longer training periods to capture  
 371 the high variations in the pressure-saturation relationship.



372 **Figure 6** Autoencoder value (AUV) and its relation to the soil water characteristics curve (SWC). (a)  
 373 The AUV of the nine sites with three sites of small (type 1) and three sites of high (type 2) AUV. (b)  
 374 The type 1 of the SWC has small water contents close to saturation and a narrower range of water  
 375 contents for similar water contents compared to type 2 with high water content values and variations.  
 376 Type 1 shows the data range of Aetigkofen (site #1) and Type 2 for Bellach site (#2). The site numbers  
 377 are chosen in alphabetic order and as shown in Figure 1 (Aetigkofen (1), Bellach (2), Breitenbach (3),  
 378 Dulliken (4), Etziken (5), Hofstetten-Flüh (6), Matzendorf (7), Stüsslingen (8), Zunzgen (9); sites with  
 379 forest are marked with \*).

### 381 3.3 Deep neural network using the autoencoder value (AUC-DNN)

382 As mentioned in the previous section, the nine sites could be grouped into three main types according  
 383 to the scaled autoencoder value (AUV). Consequently, it was assumed that the creation of a DNN  
 384 model, which incorporates AUV in conjunction with the previously built site-specific neural network,  
 385 could enable predictions for unseen sites. Ideally, the model should be trained with a balanced dataset,  
 386 including one site from the 'type 1' category, one site from the 'type 2' category, and a few sites from



387 the ‘transitional’ category to capture the full transition between the ‘type 1’ and ‘type 2’. However, due  
 388 to the data limitation, the model was trained for only three sites representing the three types (Etziken,  
 389 site #5, for ‘type 1’; Bellach, #2, for ‘type 2’; Stüsslingen, #8, for the ‘transitional type’) and was then  
 390 used to predict the six unseen sites. The impact of the small training set (only one site for transitional  
 391 type) was clear in the model results, which exhibited some instability, changing from one run to another  
 392 as the model was not able to assume the same transitional function between sites consistently. Therefore,  
 393 the model was run 20 times, then the average result for these runs was taken as a representative  
 394 outcome. The application of the new DNN model with AUV to predict the dynamic of matric potential  
 395 is shown in Figure 7 for Breitenbach (site #3, loam, forest) as unseen site. The model was found to fall  
 396 slightly behind the previously designed DNN model, but still can predict the dynamic in a good way.  
 397 Notably, the NSE value for this model for Breitenbach site was 0.71 over the entire period from 2012  
 398 to 2022 (Table 2).

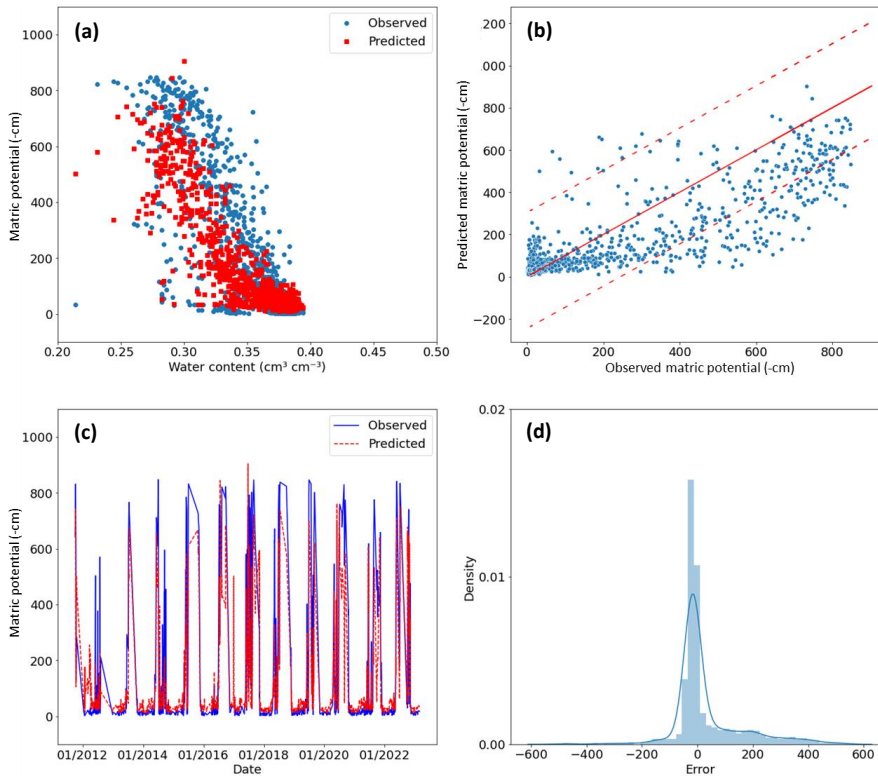
399 **Table 2** AUC-DNN Model performance for the period 2012-2022. Three training sites were used to  
 400 build the AUC-DNN model that was then applied for the other six sites. The sites are listed according  
 401 to the corresponding autoencoder value (AUV). The asterisks mark the sites with forest; The AUV  
 402 was scaled from 1.9 to 7.0 to simplify input. Alternatively, scaled values ranging from 0 to 1 could  
 403 also be utilized.

Location	AUV	AUV (type)	used as	NSE (-)	RMSE
5 Etziken*	1.90	Type 1	Training site	0.82	70
1 Aetgikofen	1.95	Type 1	Validating site	0.76	88
4 Dulliken*	2.19	Type 1	Validating site	0.65	100
3 Breitenbach*	3.56	Transitional	<del>Training</del> Validating	0.71	73
8 Stüsslingen	4.49	Transitional	<del>Validating</del> Training	0.85	116
6 Hofstetten-Flüh	5.59	Transitional	Validating site	0.60	113
7 Matzendorf	6.39	Type 2	Validating site	0.58	123
9 Zunzgen	6.44	Type 2	Validating site	0.69	104
2 Bellach	7.00	Type 2	Training site	0.71	104

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404  
 405 It was noticed that the error distribution exhibited a predominantly normal pattern with a bias towards  
 406 higher observed values compared to the predicted values (figure 7d). The analysis indicates the model's  
 407 proficiency in forecasting dynamic trends rather than precise values (figure 7c). The results align with  
 408 the anticipated scenario as the AUV for Breitenbach (3.56) was relatively close the Stüsslingen AUV  
 409 value (4.49). Therefore, the underestimation detected in Stüsslingen for the site-specific DNN (figure

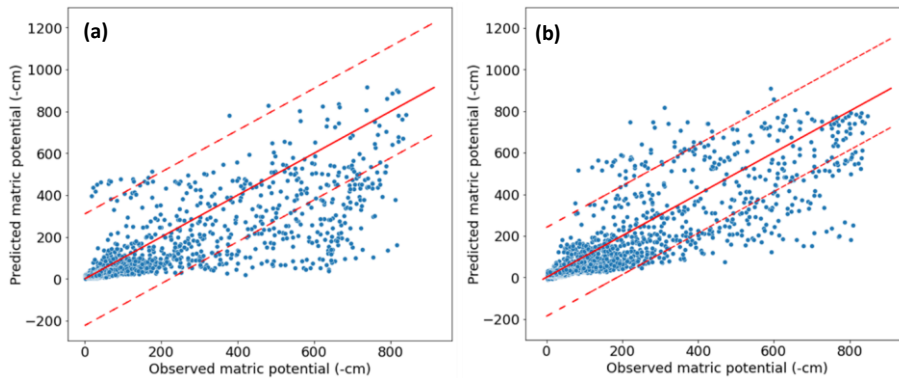
410 5b) is expected to exist in Breitenbach as well. The average model performance for all sites is presented  
 411 in Table 2. The NSE values was  $> 0.55$  for the 6 unseen sites (validating sites) and provided strong  
 412 evidence that the model can be relied upon for the dynamic MP predictions.



413  
 414 **Figure 7** Evaluation of the Deep Neural Network with Autoencoder (AUC-DNN) model performance  
 415 at the Breitenbach site for the period 2012-2022. **(a)** Comparison between the expected Soil Water  
 416 characteristics curve (SWC) and the observed SWC. **(b)** Scatter plot that compares observed data points  
 417 with their corresponding simulated values, providing a visual representation of the level of conformity  
 418 to the identity line. The two dashed lines represent the 95% confidence interval around the identity line,  
 419 providing a visual assessment of the level of agreement. **(c)** Time series comparison showing the  
 420 observed and predicted matric potential for the entire period. **(d)** Analysis of the distribution of  
 421 prediction errors (observed minus modelled value) using positively mild skewed distribution.

422 The NSE values for the unseen sites (validating sites) varied from 0.58 to 0.76, indicating a spectrum  
 423 of model performance, ranging from acceptable to good. The low NSE values observed for Matzendorf  
 424 (site #7) suggest that the model's utility is more suited for capturing overall trends and dynamics rather  
 425 than precise values. This evaluation was further supported by examining a scatter plot (Figure 8) that

426 compares the observed data points with their corresponding simulated values for the sites scored the  
427 lowest and the highest NSE, Matzendorf (site #7) and Aetigkofen (site #1). The plot revealed a wider  
428 95% confidence interval for Matzendorf (figure 8a) in comparison to Aetigkofen (figure 8b), indicating  
429 that the lower the NSE value is, the more challenging it became for the model to predict the exact MP  
430 values. However, the model performance indicated the ability of the AUC-DNN model to predict  
431 dynamic MP without the necessity of site-specific training data, marking a transition from the DNN  
432 site-specific nature to a more versatile multi-site model.



433  
434 **Figure 8** Comparison between observed data points and their corresponding simulated values for two  
435 sites with lowest and highest efficiency coefficient NSE. **(a)** Matzendorf (site #7) with NSE of 0.58. **(b)**  
436 Aetigkofen (site #1) with NSE of 0.76. The solid lines mark the 1:1 correspondence, the dashed lines  
437 the 95% confidence interval.

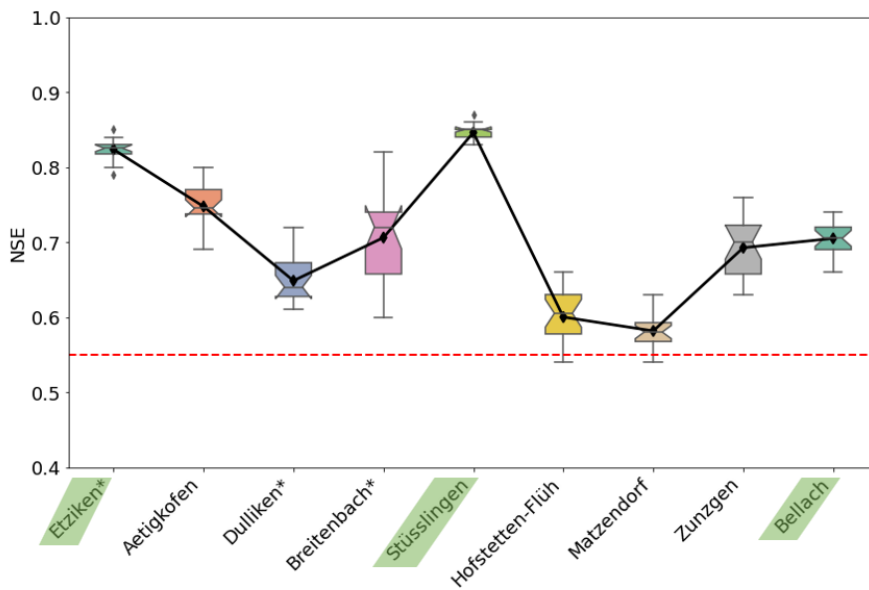
#### 438 4. Discussion

439 Based on the analysis of the simulation results presented in section three, it can be asserted that the  
440 model was successfully built. However, as discussed in the next subsection, the model is expected to  
441 have certain drawbacks due to the limited number of available sites. In the other subsections, the  
442 relationship between the autoencoder value and soil properties and its application for satellite data will  
443 be discussed.

##### 444 4.1 Limits of the deep neural network with autoencoder value (AUC-CNN)

445 First, the model's statistical evaluation revealed that the matric potential (MP) at a depth of 20 cm could  
446 be simulated with acceptable precision. However, a high variability in the evaluation is indicated by the

447 NSE values for the unseen sites. This variance is attributed to the model's limited generalization  
 448 capacity, as it was trained on just three sites. Furthermore, the model was not able to catch the whole  
 449 dynamic for the training sites due to the limited length of available data. For example, Bellach (site #2),  
 450 a training site that has a high AUV-value, had NSE value of 0.71 for the training period (table 2), which  
 451 indicates that the model was able to catch the general trend for this site, but still can't predict the exact  
 452 value of the MP. The effect of this result was obvious on the sites that are closed to AUV 'type two'  
 453 category (e.g., Hofstetten-Flüh and Matzendorf, sites #6 and #7, with NSE of 0.60 and 0.58,  
 454 respectively).  
 455 The stability of the AUC-DNN model was insufficient, as the model showed different prediction quality  
 456 upon running the model repeatedly for the same training sites (figure 9). This variability in the outcomes  
 457 indicates that the model can find different MP dynamics scenarios inside the training data. Therefore,  
 458 it is recommended to train the model for more than one site in the same AUV type.



459  
 460 **Figure 9** Variation of prediction results for 20 Runs for the AUC-DNN model quantified with the  
 461 efficiency coefficient NSE. The highest variation was with the unseen sites in the transitional and type  
 462 2 categories. Each box represents the interquartile range, with the line inside denoting the median. The  
 463 black diamond markers connect the mean values for each station, providing insight into the central  
 464 tendency of the data. Notches on the boxplots offer a visual indication of the uncertainty around the  
 465 median. The red dashed line represents the defined threshold for the NSE, set at 0.55 ; sites with forest  
 466 are marked with \*; training sites are highlighted in green.

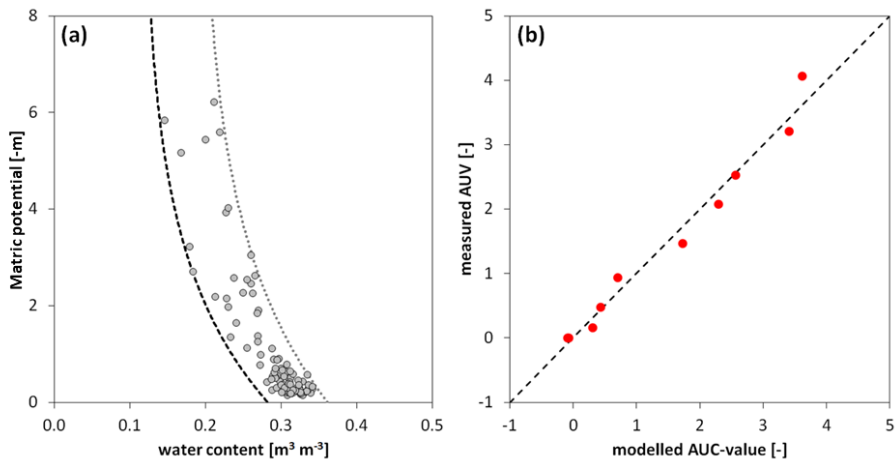
467 Especially for the ‘transitional type’, choosing a site in the beginning, in between, and in the end of the  
468 category would stabilize the modeling results. However, in this study, there was no possibility to  
469 provide the model with extra data to solve the prediction instability. Therefore, a solution was  
470 implemented by 1) closely monitoring the model manually to ensure it captures the dynamic from all  
471 three sites. This involved training the model with nearly identical time periods for each site and visually  
472 confirming comprehensive coverage of the cloud of points for the retention curve of each site, avoiding  
473 concentration on specific patterns during training. The process also includes 2) running the model for  
474 20 times, then averaging the results. Additionally, the statistical evaluation plots as shown in Figure 8,  
475 were used to detect instances with very low or very high MP prediction values.

476 For the set of sites analysed in this study, the model showed good generalization capacity and stability.  
477 However, the nine sites were similar with respect to climate and geology and the range of soil textural  
478 classes (see Figure 1) was relatively narrow. In a future study, the AUC approach will be applied for  
479 sites differing in climate and soil textural classes. We expect that the model can predict the dynamic  
480 matric potential for a new site as long as the autoencoder value falls within the range of AUV of the  
481 training sites. To predict the soil moisture dynamics for soils with autoencoder values outside of the  
482 range of training data, the model must be re-built using additional training data.

483

#### 484 4.2 Relationship between AUV and Interpretation of AUV and its relationship to 485 physical soil properties

486 As discussed in section 3.2, the autoencoder value (AUV) is low for soil water characteristics curves  
487 (SWC) with low saturated water content and low variations of water content for a certain matric  
488 potential value (type 1) and high AUV for large values and variations of water content (type 2). To  
489 ~~define~~provide a more quantitative relationship between SWC and AUV, the SWC data were  
490 characterized as follows: the time average of volumetric water content (VWC) and SWP were calculated  
491 for 15 days for the period 2015 to 2022. The envelope of these data was then calculated by fitting a  
492 minimum and maximum pressure saturation relationship including the averaged data (see Figure 10a).



493  
 494 **Figure 10** Relationship between autoencoder value (AUV) and soil water characteristics curve (SWC).  
 495 (a) 15-days average of SWC data for Aetigkofen (symbols; site #1). The two lines are exponential  
 496 functions building the envelope of the SWC curve. (b) Linear model for the nine sites linking the  
 497 parameters of the exponential model with the ‘measured’ AUV (deduced from measured water content  
 498 data).

499 The two boundary lines of the SWC were then characterized by a ‘saturated’ and ‘residual’ water  
 500 content and a shape parameter defining an exponential decrease of water content with increasing  
 501 absolute matric potential values. The SWC of each site can thus be described by six parameters (three  
 502 parameters per boundary line). As shown in Figure 10b, a linear model expressing the AUV as function  
 503 of these six parameters can be built. It was simpler models with less parameters could not possible to  
 504 reproduce the AUV as linear model of soil texture all sites. Despite the positive correlation between  
 505 AUV and average water content, the average water content alone is not sufficient to explain the range  
 506 of AUV for all sites. Also combining average water content with soil texture information could not  
 507 reproduce the AUVs of all sites, indicating that the soil moisture dynamics represented by AUV is not  
 508 only dependent of on static soil textural attributes but seasonal structural features as well.

509 Accordingly, there is no simple interpretation of AUV based on texture and average water content, but  
 510 the dynamic variation of water content must be considered as well. Due to the relevance of the variation  
 511 in water content for similar matric potential value, the use of a variational autoencoder (VAE) instead  
 512 of the typical autoencoder could be considered. In contrast to the typical autoencoder that maps the  
 513 input information into a single point (or a few points), the VAE produces a probability distribution

514 capturing the variability (second moment) of the data. This could be specifically of interest for clay  
515 soils with high water contents (much larger than the residual water content) for the entire range of matric  
516 potential values. By including a probabilistic approach in the compressing and decompressing step, the  
517 variability of the data could be captured more efficiently using VAR.

518

#### 519 4.3 Application for satellite data

520 The AUC-DNN model was used to analyze satellite-based volumetric water content (VWC) satellite  
521 data, including SMAP L4 and L3, SMOS products, and Sentinel data. Subsequently, a comparison was  
522 carried out for the AUV for both site-specific measurements and earth observation (EO) measurements  
523 for the same region. The initial findings highlighted a disparity between the dynamics captured by EO  
524 products and the actual dynamics. Therefore, if the objective is to establish a robust system capable of  
525 detecting changes in water retention dynamics on a regional scale, it is considered necessary to enhance  
526 the calibration of EO in Europe. Only with EO-data that can reproduce the essential of the soil moisture  
527 dynamics as manifested in the AUV, the matric potential dynamics can be deduced from EO-data. For  
528 future EO-data with improved capacity to capture regional soil moisture dynamics, the concept  
529 presented in this study (AUC-DNN) could be used to predict matric potential dynamics at global scale  
530 (see Appendix C).

#### 531 5. Summary and conclusions

532 The soil water potential (SWP) determines water flow direction, water ability for plants, and mechanical  
533 stability. Because it cannot be measured directly by remote sensing techniques at larger scales, it is  
534 often deduced from water content information, assuming an unambiguous relationship between water  
535 content and SWP. However, this relationship under dynamic field conditions is highly ambiguous due  
536 to hysteresis, dynamic effects, and soil structural changes that cannot be modeled with a physically-  
537 based model. To enable prediction of SWP from soil water content, we apply a deep neural network  
538 (DNN) with an autoencoder to define unique features of the soil moisture dynamics. By inserting the  
539 autoencoder value (AUV) together with climatic data and water content measured at nine sites in the

540 region of Solothurn (Switzerland) in a deep neural network (AUC-DNN), the soil water potential could  
541 be predicted. The main findings of the study can be summarized as follows:

- 542 • The SWC of the nine sites can be classified in three types based on the width of pressure-  
543 saturation relationship and the water content close to saturation
- 544 • These SWC-types are manifested in different autoencoder values (AUV)
- 545 • The AUV is not a simple function of average water content or soil texture but includes structural  
546 effects as well
- 547 • The AUC-DNN model could predict successfully the SWP dynamics of sites without site-  
548 specific training

549 The autoencoder value (AUV) is thus a new descriptor of the complex soil moisture dynamics that  
550 cannot be captured with physically based models. Future satellite generation may be sensitive enough  
551 to measure the AUV from remote sensing water content data. The approach presented in this paper will  
552 then enable the prediction of the soil matric potential at the global scale using remote sensing water  
553 content data.

## 554 Appendix A: Data Quality Assurance and Trend Analysis

555 As a precaution for data quality, the Absolute Matric Potential (AMP) and volumetric water content  
556 (VWC) data were scrutinized to identify potential errors the data. The process includes different steps  
557 that were necessary to discover anomalies, checking the integrity of the data, and detecting systematic  
558 changes with time.

### 559 **1- Flagging Abrupt Changes in VWC and MP:**

#### 560 **VWC Flagging and removing:**

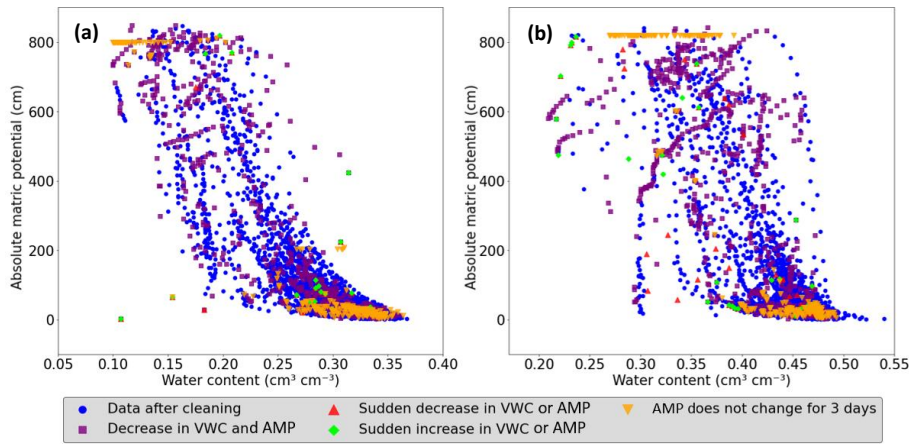
- 562 • Differences between consecutive (daily) time steps in the water content time series were  
563 calculated.
- 564 • Instances with daily differences exceeding  $0.1 \text{ cm}^3/\text{cm}^3$  were flagged and denoted as sudden  
565 decreases or increases in VWC.



- 566 • Instances with VWC below  $0.1 \text{ cm}^3/\text{cm}^3$  or exceeding  $0.7 \text{ cm}^3/\text{cm}^3$  were identified and removed  
567 from the dataset. These extreme values were considered as measurement anomalies or outliers  
568 affecting the overall dataset's reliability.
- 569 • Instances with  $\text{AMP} < 1 \text{ cm}$  was removed from the data to overcome limitations in the used  
570 method. The water potential can change without modifying the volumetric water content after  
571 this limit, which could make the results of the model not accurate enough.
- 572 • The differences between consecutive time steps in AMP -time series was calculated; instances  
573 with daily differences exceeding 500 cm were flagged and called sudden decreases or increases  
574 in AMP (figure A1).
- 575 • The threshold AMP-value of 850 cm was employed in a specific step, where instances with  
576 AMP exceeding 850 cm were removed from the dataset, addressing the physical properties of  
577 water as it starts to boil in the tensiometers under pressure after this limit.
- 578 • Periods of concurrent decrease in AMP (indicator for wetting) and decrease in VWC (drying)  
579 were flagged (figure A1).
- 580 • Periods with matric potential values remaining constant over a three-day rolling window were  
581 flagged (figure A1).

## 582 **2- Utilizing Index Windows for Data Manipulation and Data Removal**

583 To address flagged instances mentioned before, a systematic approach is employed. For each  
584 flagged instance, three additional indices are generated around it to construct an index window,  
585 spanning one day before (index\_1), the flagged instance itself (index\_0), and two days after  
586 (index\_2 and index\_3). This four-day index window was eliminated from the dataset (figure  
587 A1). The decision to eliminate this window was informed by a visual assessment of  
588 measurements as it was noticed that when a measurement error occurs, the accuracy of the  
589 preceding day is affected. Furthermore, it was assumed that the device requires two subsequent  
590 days to restore normal measurement precision. This process contributes to a refined dataset,  
591 providing a more accurate representation of the underlying trends in AMP and VWC.



592

593 **Figure A1** Comparison of data before and after cleaning procedure: the blue circles depict the remaining  
 594 data after applying the cleaning criteria. Each distinct marker represents eliminated points, each  
 595 corresponding to a specific criterion (e.g., the square purple marker for simultaneous decrease in  
 596 volumetric water content (VWC) and the absolute matric potential (AMP), the red upward-pointing  
 597 triangle is the marker for sudden decreases, the lime diamond for sudden increases, and the orange  
 598 downward-pointing triangle marks periods of unchanged AMP). This provides insights into the reasons  
 599 for data removal and illustrates the profound impact of the data cleaning process in retaining high-  
 600 quality data points. In (a) the cleaning process for sandy clay loam site in Aetigkofen (site #1) is shown,  
 601 in (b) the cleaning process for the Matzendorf site (site #9, clay loam soil).

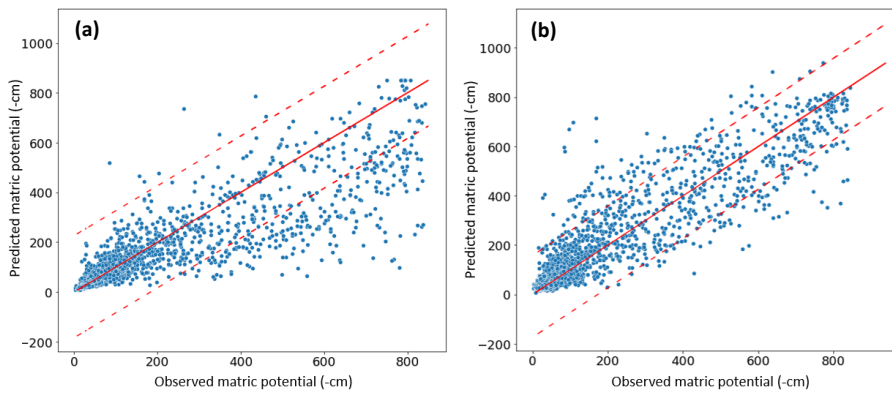
## 602 Appendix B: Running the model with Logarithmic MP value.

603 The AUC-DNN showed a good performance in predicting the dynamic MP for the different 6 unseen  
 604 sites. However, it was clear that the model prioritizes tends to focus on capturing significant changes in  
 605 values rather than accurately representing the values themselves. This tendency is attributed to the  
 606 substantial difference between the highest and lowest absolute values (approximately 850 cm), leading  
 607 the model to emphasize major fluctuations while neglecting minor ones. To address this issue and  
 608 enhance the model's precision in capturing the exact AMP, a suggestion has been made to train the  
 609 model for the same three sites but with the logarithmic value for the AMP. This modification aims to  
 610 strike a better balance, ensuring that both major and minor changes are effectively captured while  
 611 maintaining accuracy in representing the specific values of MP.

612 To qualitatively assess the model training performance under the logarithmic scale, a scatter plot (Figure  
 613 B1) was generated, comparing observations against simulated values for the second training site  
 614 (Stüsslingen). The reason for choosing a training site was to understand how the model captures the

615 dynamics when trained with logarithmic matric potential. The results suggest that using logarithmic  
616 scale, the model prioritized the prediction of the exact absolute value of matric potential (AMP), which  
617 makes the model to optimize predictions for the absolute values between 0 to 200 cm. This approach is  
618 giving the same importance to small and large changes in the AMP, which causes that the model  
619 assigned a higher weight to small changes according to their higher frequency, while neglecting less  
620 frequently occurring major dynamic shifts. Consequently, the model's accuracy went down beyond 200  
621 cm (figure B1a) when compared to the model trained on non-logarithmic AMP-values (figure B1b). To  
622 maintain a balanced consideration of changes, logarithmic MP was avoided in the main part of the  
623 paper.

624



625 **Figure B1** Visual comparison of model performance, comparing the observed and simulated values for  
626 the Stüsslingen training site. **(a)** the model trained with logarithmically scaled AMP-values, while in  
627 **(b)** The model trained with absolute linear matric potential (AMP) values. The solid line denotes the  
628 1:1 correspondence, and dashed lines represent the 95% confidence interval.  
629

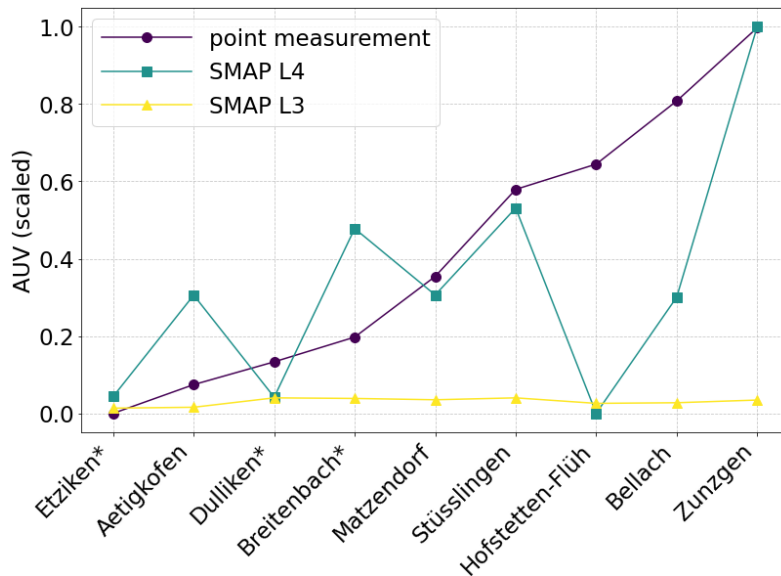
## 630 Appendix C: SMAP data and Autoencoder for global scale analysis

631 SMAP (Soil Moisture Active Passive) is a NASA satellite mission that was established to help in  
632 improving weather forecasts and global drought monitoring. SMAP data products are available at  
633 different levels of processing, from Level 1 (L1; instrument measurements) to Level 4 (L4; model-  
634 derived value-added products). For this study, SMAP L3 and SMAP L4 products for measuring  
635 moisture content were used. The main difference between the two products is that SMAP L3 depends  
636 on the passive radiometer measurements, while SMAP L4 products are derived from a data assimilation

637 system that combines the L-band brightness temperature observations from SMAP with a land surface  
638 model and meteorological forcing data (Reichle, et al., 2019). SMAP L3 products for moisture content  
639 are primarily affected by vegetation and surface roughness, allowing them to capture surface soil  
640 moisture variations. In contrast, the incorporation of land surface models in SMAP L4 products reduces  
641 its sensitivity to vegetation covers and surface roughness, making the products more representative of  
642 the profile soil moisture conditions (Reichle, et al., 2019; [SadriUcla](#), Wood, & [PanSadri](#), 2018).

643 The autoencoder's encoded representations offer a unique opportunity to compare the spatial patterns  
644 inherent in "point measurement" with remote sensing data such as SMAP L3 and SMAP L4 data. The  
645 autoencoder method could illuminate how these diverse data streams align or diverge, providing crucial  
646 insights into the compatibility and complementarity of ground and satellite measurements. The process  
647 was applied for the data between the years 2015 to 2022. All the data (SMAP L4, SMAP L3, and on-  
648 site measurements) were given to the autoencoder neural network together. Subsequently, the resulting  
649 autoencoder values were scaled. Finally, a comparison was made to show if the satellite measurements  
650 and the on-site measurements have the same measured dynamics.

651 The autoencoder analysis of SMAP L3 (figure C1) indicates that satellite measurements struggle to  
652 capture the dynamic change of the water content, as all locations yield approximately the same  
653 Autoencoder Value (AUV). In contrast, the SMAP L4 product (figure C1) exhibits fluctuations in AUV  
654 results. For instance, Stüsslingen and Matzendorf align closely with on-site measurements in terms of  
655 AUVs. However, for Hofstetten-Flüh, the SMAP L4 product indicates a very small AUV, suggesting  
656 an expected dynamic in line with a type 1 soil water retention curve (figure 6b). In contrast, on-site  
657 measurements indicate a higher AUV for Hofstetten-Flüh, suggesting a closer association with a type  
658 2 soil water retention curve. These findings underscore the imperative for developing a new  
659 methodology to calibrate satellite data in the Switzerland area. The prevalent uniformity in SMAP L3  
660 results and the notable disparities between on-site measurements and satellite data across various  
661 products highlight the need for a more refined approach to ensure accurate and reliable dynamic soil  
662 moisture assessments.



663  
 664 **Figure C1** Comparative analysis of Autoencoder Neural Network results for SMAP L3 and SMAP L4  
 665 satellite data, alongside with profile measurements. The fluctuating AUV values indicate varying  
 666 degrees of alignment with on-site measurements across different locations. Sites with forest are marked  
 667 with \*.

668 **Code and data availability**

669 The related input data for the AUC-DNN model and Python code are openly accessible under  
 670 <https://doi.org/10.5281/zenodo.10600669> and <https://doi.org/10.5281/zenodo.10602397> respectively.  
 671 The input for the autoencoder and its python codes are openly accessible under  
 672 <https://www.doi.org/10.5281/zenodo.10605108>

673 **Author contributions**

674 NA, AC, and PL designed the research. NA and PL performed the research. NA and MR analyzed the  
 675 soil moisture time series. SM was responsible for the soil moisture network. NA wrote the codes and  
 676 built the model. NA and PL wrote the manuscript with substantial input from all co-authors.

677 **Competing interests**

678 The contact author has declared that none of the authors has any competing interests.

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