

1 **Characterization of Non-Gaussianity in the Snow**  
2 **Distributions of Various Landscapes**

3  
4 **Noriaki Ohara<sup>1</sup>, Andrew D. Parsekian<sup>1</sup>, Benjamin M. Jones<sup>2</sup>, Rodrigo C. Rangel<sup>1, 6</sup>,**  
5 **Kenneth M. Hinkel<sup>3</sup>, and Rui A. P. Perdigão<sup>4, 5</sup>**

6 <sup>1</sup>University of Wyoming, Laramie, WY, USA

7 <sup>2</sup>University of Alaska Fairbanks, Fairbanks, AK, USA

8 <sup>3</sup>Michigan Technological University, Houghton, MI, USA

9 <sup>4</sup>Meteoceanics Institute for Complex System Science, IUC Physics of Complex Coevolutionary  
10 Systems & Fluid Dynamical Systems, Washington, DC, USA

11 <sup>5</sup>Synergistic Manifolds, Lisbon, Portugal

12 <sup>6</sup>Department of Earth Sciences, University of Toronto, Toronto, Ontario, Canada

13

14 Corresponding author: Noriaki Ohara (nohara1@uwyo.edu)

15 **Summary**

16 Snow distribution characterization is essential for accurate snow water estimation for water  
17 resource prediction from existing in-situ observations and remote sensing data at a finite spatial  
18 resolution. Four different observed snow distribution datasets were analyzed for Gaussianity. It  
19 was found non-Gaussianity of snow distribution is a signature of wind redistribution effect.  
20 Generally, seasonal snowpack can be well approximated by Gaussian distribution for fully snow-  
21 covered area.

## 22 **Abstract**

23 Seasonal snowpack is an important predictor of available water resources in the following spring  
24 and early summer melt season. Total basin snow water equivalent (SWE) estimation usually  
25 requires a form of statistical analysis that is implicitly built upon the Gaussian framework.  
26 However, it is important to characterize the non-Gaussian properties of snow distribution for  
27 accurate large-scale SWE estimation based on remotely sensed or sparse ground-based  
28 observations. This study quantified non-Gaussianity using sample negentropy, the Kullback–  
29 Leibler divergence from Gaussian distribution, for field-observed snow depth data on the North  
30 Slope, Alaska, and three representative SWE distributions in the western US from the Airborne  
31 Snow Observatory (ASO). Snowdrifts around lakeshore cliffs and deep gullies can bring  
32 moderate non-Gaussianity in the open, lowland tundra of North Slope, Alaska, while the ASO  
33 dataset suggests that subalpine forests may effectively suppress the non-Gaussianity of snow  
34 distribution. Thus, non-Gaussianity is found in areas with partial snow cover and wind-induced  
35 snowdrifts around topographic breaks in slope and other steep terrain features. The snowpacks  
36 may be considered weakly Gaussian in coastal regions with open tundra in Alaska and alpine and  
37 subalpine terrains in the western US if the land is completely covered by snow. The wind-  
38 induced snowdrift effect can be potentially partitioned from the observed snow spatial  
39 distribution guided by its Gaussianity.

40

## 41 **1 Introduction**

42 Modeling of the spatial variability of snow is important for large-scale earth surface modeling  
43 since atmospheric circulation is sensitive to snow cover presence (e.g., Aas et al., 2016; Meng,  
44 2017; Mott et al., 2015, 2017; Nitta et al., 2014; Younas et al., 2017). Since subgrid variability  
45 often causes appreciable bias in weather predictions (e.g. Lalande et al., 2023; Rudisill et al.,  
46 2024), accurate snow cover quantification can potentially improve the predictability of weather,  
47 planetary boundary-layer evolution, convective cloud formation, and even tropical cyclogenesis  
48 (Santanello et al., 2018). Hence, the subgrid variability of snow cover has been incorporated into  
49 operational regional weather forecasting models such as the High-Resolution Rapid Refresh  
50 (HRRR) model (He et al., 2021).

51 Observations of seasonal snow storage in mountainous areas through remote sensing and ground-  
52 based measurements are a direct and reliable indicator of the water supply during the following  
53 spring season in downstream regions (e.g. Fleming et al., 2023; Sengupta et al., 2022). However,  
54 total basin snow water equivalent (SWE) estimation usually requires a statistical relationship  
55 such as the snow depletion curve (SDC), which correlates with observables such as the snow  
56 cover area fraction (SCF). Based on a study of the observed snow distributions in Reynolds  
57 Creek Experimental Watershed in Idaho, Luce et al. (1999) showed that one snow distribution  
58 can reasonably represent the SDC evolution for the rest of the season. Also, Luce and Tarboton  
59 (2004) showed a high degree of similarity in nine years of dimensionless depletion curves  
60 measured in the same basin. Shamir and Georgakakos (2007) demonstrated the consistency of  
61 SDC over a season in the American River using a distributed model. The subseasonal and

62 interseasonal consistency in SDCs suggests the possibility for subgrid snow characterization as  
63 well as basin wide SWE estimation from SCF data such as the MODIS product (Hall et al.,  
64 2006).

65 As remote sensing technologies advance, seasonal snow distribution characterization becomes  
66 more approachable with multi-sensor methods. For example, Tarricone et al. (2023) analyzed  
67 three Interferometric Synthetic Aperture Radar (InSAR) image pairs to assess SWE evolution  
68 using the snow-focused multi-sensor method with Uninhabited Aerial Vehicle Synthetic  
69 Aperture Radar (UAVSAR) and an L-band InSAR data as well as optical fractional snow-  
70 covered area (SCA) information. However, to estimate the total basin SWE in water resource  
71 management practices, statistical empirical relationships are required to fill gaps in the spatial  
72 and temporal resolutions—even when using these remote sensing observations (Tsang et al.,  
73 2022). For example, Meloche et al. (2022) assumed log-normal distribution to represent the sub-  
74 pixel variability of remotely sensed data. Thus, uncertainty and subgrid variability must be  
75 accounted for when using statistical characterization in SWE estimation.

76 The most popular choice for the probability density function (PDF) of snow is log-normal  
77 distribution, which inherently eliminates negative snow depth (Donald et al., 1995; Liston, 2004;  
78 and many others). Brubaker and Menoes (2001) chose a beta distribution, while Kolberg and  
79 Gottschalk (2006) selected a two-parameter  $\gamma$ -distribution. Although these common distributions  
80 are in the exponential family, they were primarily chosen for convenience. Indeed, the  
81 representativeness of these parametric probability distributions remains questionable for different  
82 landscapes and snowpack ages (e.g., Skaugen & Randen, 2013; Egli & Jonas, 2009; He, Ohara,  
83 & Miller, 2019). Moreover, these approaches for bounded distributions may not work for  
84 evolving snowpacks with partial SCA where zero values are present in the probability domain.

85 In theory, without microtopography and meteorological effects, since the landing location of  
86 each snow particle fallen from the atmosphere is considered an independent and identically  
87 distributed (iid) random variable, the resulting snow depth or SWE distribution should  
88 asymptotically approach a Gaussian distribution due to the central limit theorem. He, Ohara, and  
89 Miller (2019) reported non-Gaussian snow distribution in open areas as well as Gaussian snow  
90 distributions in the forested, fully snow-covered areas during the peak snow season using  
91 airborne Light Detection and Ranging (LiDAR) observations in the Snowy Range, Wyoming.  
92 This implies the presence of both systematic (non-Gaussian) and random (Gaussian) mechanisms  
93 in snow accumulation and ablation processes. Therefore, it is possible to identify the potential  
94 factors as “signals” that make the snow distribution deviate from a Gaussian distribution by  
95 analyzing the resultant snow distributions.

96 This study applies negentropy to analyze the non-Gaussianity of snow distributions in Arctic  
97 tundra, as well as alpine and subalpine landscapes in North America. Negentropy measures the  
98 departure in entropy between a sampled distribution and Gaussian distribution of identical  
99 variance and mean. Signals of interest (e.g., systematic snowdrift patterns) can be extracted as  
100 non-Gaussian components because pure random noise asymptotically becomes Gaussian in  
101 theory. This is the main idea of independent component analysis (ICA; Hyvärinen et al., 2000).  
102 This work presents the quantified non-Gaussianity of the observed snow distributions through a

103 variety of snow distribution data, including intense direct hand measurements within 30-m grids  
 104 using a probe, and indirect measurements using a snowmachine-attached ground-penetrating  
 105 radar (GPR), UAV-based photogrammetry, as well as the Airborne Snow Observatory (ASO)  
 106 SWE products.

## 107 **2 Methods**

### 108 **2.1 Negentropy**

109 To measure the non-Gaussianity of any data, we implement the information-theoretic metric of  
 110 negentropy as the objective function since negentropy is equal to the Kullback–Leibler  
 111 divergence between  $p_x$  and a Gaussian distribution with the same mean and variance as  $p_x$ .  
 112 There is a well-known proposition that Gaussian density has the largest information entropy  
 113 among all unbounded distributions with the same first and second-order statistics. As such, the  
 114 non-Gaussianity of an observed distribution can be quantified by negentropy  $J$ , which is defined  
 115 as follows (Hyvärinen et al., 2000):

$$116 \quad J(X) = S(X_{gauss}) - S(X) \quad (1)$$

117 where  $S$  is the information entropy of  $X$ . The information entropy can assume a diversity of  
 118 metrics ranging from the most general capturing microphysical event-scale codependence in  
 119 nonlinear statistical mechanics (Perdigão 2018) or simply assuming basic event-scale  
 120 independence in classical information theory (Shannon (1948) statistical entropy). For the  
 121 purpose of this study, we take the latter simple form, which is defined as:

$$122 \quad S(X) = - \int p_x(\eta) \log[p_x(\eta)] d\eta, \quad (2)$$

123 where  $p_x$  is the PDF of  $X$ , and  $\eta$  is a dummy variable for the integration. The Edgeworth  
 124 expansion (Edgeworth, 1905) can provide an approximation for a PDF of  $X$ , as follows:

$$125 \quad p_x(X) = \frac{\phi(U)}{\sigma} \left[ 1 + \frac{\kappa_3}{6} H_3(U) + \frac{\kappa_4}{24} H_4(U) + \frac{\kappa_3^2}{72} H_6(U) + \dots \right] \quad (3)$$

126 where

127  $U =$  standardized random variable of  $X$

128  $H_k(U) =$  Chebyshev-Hermite polynomials

129  $\phi(U) =$  standard normal density

130  $\kappa_k =$  k-th order cumulant of  $U$ .

131 Substituting the Edgeworth series into the negentropy definition, Comon (1994) obtained the  
 132 analytical expression:

$$133 \quad J(X) = \frac{1}{12} \kappa_3^2 + \frac{1}{48} \kappa_4^2 + \frac{7}{48} \kappa_4^4 - \frac{1}{8} \kappa_3^2 \kappa_4 + O(n^{-2}). \quad (4)$$

134 This is the estimator of negentropy at fourth-order cumulant. In practice, a more intuitive  
 135 approximation is commonly used, as follows:

136 
$$J(X) = \frac{1}{12} \text{skew}(U)^2 + \frac{1}{48} \text{kurt}(U)^2 \tag{5}$$

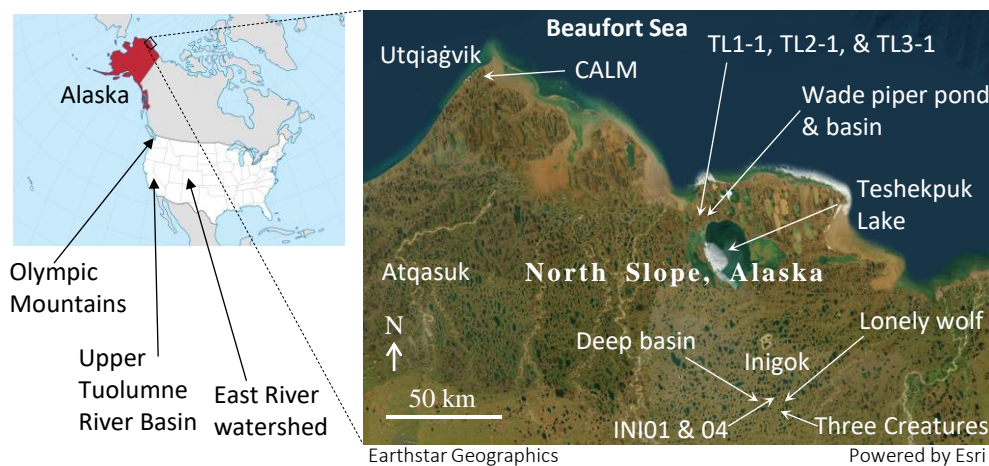
137 where skew and kurt are the skewness and kurtosis of standardized variable,  $U$ , respectively.

138 The sample estimation of the higher-order moment and cumulant (e.g., skew and kurtosis  
 139 coefficients) is known to be sensitive to the presence of outliers. In this study, the interquartile  
 140 range (IQR) method was adopted for outlier removal with a minimum removal that lies outside  
 141 the range of three times IQR.

142 While negentropy metrics and corresponding Edgeworth approximations have been previously  
 143 explored and further developed in atmospheric sciences and in physics, including derivations and  
 144 implementations to higher-order distributions, elaborate numerical and analytical estimators  
 145 (Pires and Perdigão 2007, Perdigão 2010, Perdigão 2017), the present study brings a simplified  
 146 treatment not yet explored in hydrology and tailored for swift and seamless integration within  
 147 hydrological and water resource systems investigations.

148 **2.2 Data collection**

149 We analyzed four types of data with different collection methodologies at various scales in this  
 150 study, as listed in Table 1. The first is manual snow depth surveys using a GPS-aided snow probe  
 151 (Magnaprobe; Sturm & Holmgren, 2018), the second is snow depth transects using a  
 152 snowmachine-attached GPR, the third is snow depth maps using UAV-based photogrammetry,  
 153 and the last is the SWE product of the ASO. The first three datasets are for the open tundra in the  
 154 Arctic Coastal Plain (ACP) of Alaska while the ASO data are for the alpine and subalpine  
 155 regions of the continental USA. Detailed data specifications associated with the collection  
 156 methodologies will be presented in Results section below. Figure 1 displays the map of the snow  
 157 depth surveys in North Slope, Alaska, USA.



158  
 159 Figure 1: Map of the snow survey locations in Alaska, USA, and the selected ASO sites.

160

161 Table 1: List of snow datasets

Site name	Location	Lon/Lat	Spatial resolution	Elevation range	Data collection method	Date	Sample size	Landscape and land cover
TL1-1	Teshekpuk, AK	70.738°N, 153.970°W	~1m	0.91~1.20 m MSL	Magnaprobe	April 24, 2022	951	Open tundra, sedge and herbaceous
TL2-1	Teshekpuk, AK	70.740°N, 153.956°W	~1m	2.35~2.54 m MSL	Magnaprobe	April 25, 2022	925	Open tundra, sedge and herbaceous
TL3-1	Teshekpuk, AK	70.739°N, 153.928°W	~1m	1.86~2.18 m MSL	Magnaprobe	April 25, 2022	904	Open tundra, sedge and herbaceous
Wade piper pond	Teshekpuk, AK	70.751°N, 153.870°W	~1m	2.18~2.50 m MSL	Magnaprobe	April 27, 2022	927	Open tundra, sedge and herbaceous
Wade piper basin	Teshekpuk, AK	70.746°N, 153.854°W	~1m	3.68~3.88 m MSL	Magnaprobe	April 29, 2022	960	Open tundra, sedge and herbaceous
Inigok	Inigok, AK	70.001° N, 153.068° W	~0.5m	37.8~59.1 m MSL	GPR	May, 2019	16655	Open tundra, sedge and herbaceous
CALM	Utqiagvik, AK	71.3026° N, 156.6008° W	0.25m	-1.93~3.8 m MSL	UAV photogrammetry	May, 2019	2,928,240	Open tundra, sedge and herbaceous
Upper Tuolumne River	California	37.461°N, 119.494°W	50 m	1,142~3,965 m MSL	ASO SWE product	April 3, 2013	470,213	Steep rocky alpine terrain, partially forested
East River	Colorado	39.037°N 106.978°W	50 m	2,343~3,901 m MSL	ASO SWE product	March 31, 2018	667,883	Alpine and subalpine forest
Olympic Mountains	Washington	47.792°N 123.650°W	50 m	0~2,432 m MSL	ASO SWE product	March 29, 2016	2,066,907	Dense forest and high peaks

162

### 163 3 Results

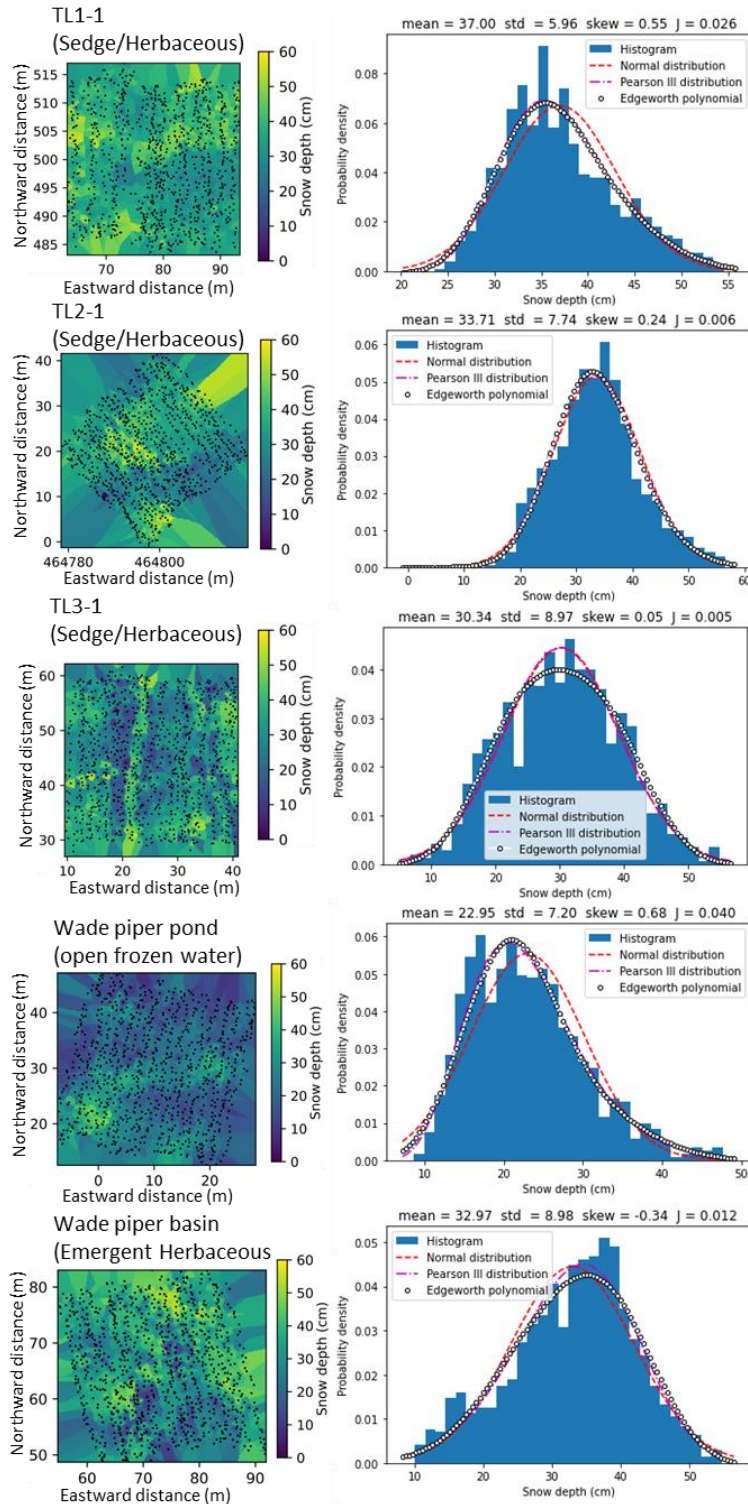
#### 164 3.1 Manual snow surveys at Teshekpuk, North Slope, Alaska (May 2022)

165 Snow depth data were collected using a Magnaprobe (Sturm & Holmgren, 2018) in five 30 x 30-  
 166 m grids with 1 m grid spacing north of Teshekpuk Lake, North Slope, AK, in May 2022. The  
 167 GPS location of each measurement was automatically recorded. Figure 2 presents the  
 168 interpolated snow depth distributions and corresponding histograms (right columns) in five areas  
 169 near Teshekpuk. The observer measured the point scale snow depth at approximately every 1 m  
 170 along a line toward flags placed 1 m apart on the surface. Since the data points were selected  
 171 from undisturbed snow, the locations are unevenly distributed despite the snowpacks generally  
 172 being highly hardened by wind. The relative spatial locations are considered accurate since the  
 173 operator stood on the same side of the probe and followed pre-marked lines based on the tape  
 174 measure; however, the absolute plotted coordinate in the figures may not be trustworthy due to

175 the GPS horizontal accuracy  $< 3$  m. The topography of these grids in the ACP are very flat with  
176 elevation variation of less than 1 meter while accurate absolute elevation data are hard to  
177 compare due to the spatial inaccuracy of the Magnaprobe.

178 The graphics in the left column of Figure 2 present the point depth observation locations and  
179 interpolated snow depth distributions using the nearest distance method. The number of data  
180 points denoted by the black dots is  $n=951$  (TL1-1),  $n=925$  (TL2-1),  $n=904$  (TL3-1),  $n=927$   
181 (Wadepiper Pond), and  $n= 960$  (Wadepiper Basin).

182 The corresponding snow depth histograms and three fitted distributions are displayed in the right  
183 column. The statistics mean, standard deviation, skew coefficient, and negentropy ( $J$ ) are  
184 reported on the top part of each graph. In general, the snow depth distributions in these areas are  
185 almost Gaussian distributions since the computed negentropy is small. However, the negentropy  
186 of snow distribution affected by wind-induced snowdrift (sastrugi) on frozen lakes is larger than  
187 the tundra covered by sedge and herbaceous vegetation. In practice, the non-Gaussianity of  
188 seasonal snow depth may have been negligible in the coastal open tundra (including frozen open  
189 waters) in the Teshekpuk study area in May 2022.



190

191 Figure 2: Manual snow distributions in the Teshekpuk Lake area, North Slope, Alaska (May  
 192 2022) and corresponding histograms with fitted probability density functions (PDFs).  $J$  denotes  
 193 the computed negentropy. Snow depth histograms in open tundra in 30 m x 30 m squares are  
 194 generally categorized as “weak-non-Gaussian.” The approximated center coordinates of the grids



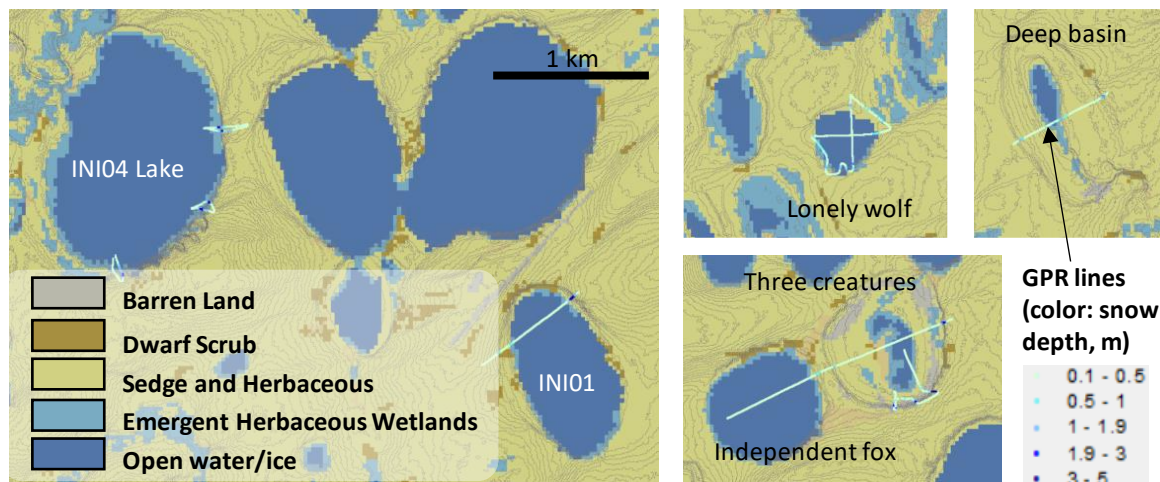
195 are 70.738°N, 153.970°W (TL1-1), 70.740°N, 153.956°W (TL2-1), 70.739°N, 153.928°W (TL3-  
196 1), 70.751°N, 153.870°W (Wadepiper Pond), and 70.746°N, 153.854° W (Wadepiper Basin).

### 197 **3.2 Snow depth surveys using GPR along multiple transects in Inigok, North Slope,** 198 **AK (April 2019)**

199 The Inigok area of North Slope, Alaska (70.001° N, 153.068° W) is characterized by paleo sand  
200 dunes (Carter, 1981), hydro-geomorphological processes, and permafrost landforms such as  
201 thermokarst lake formation and drainage. The landscape is characterized by relatively steep  
202 terrain and substantial wind-induced snowdrifts (deeper than 5 m), especially around lake shores  
203 and drainage channels (e.g., Rangel et al., 2023).

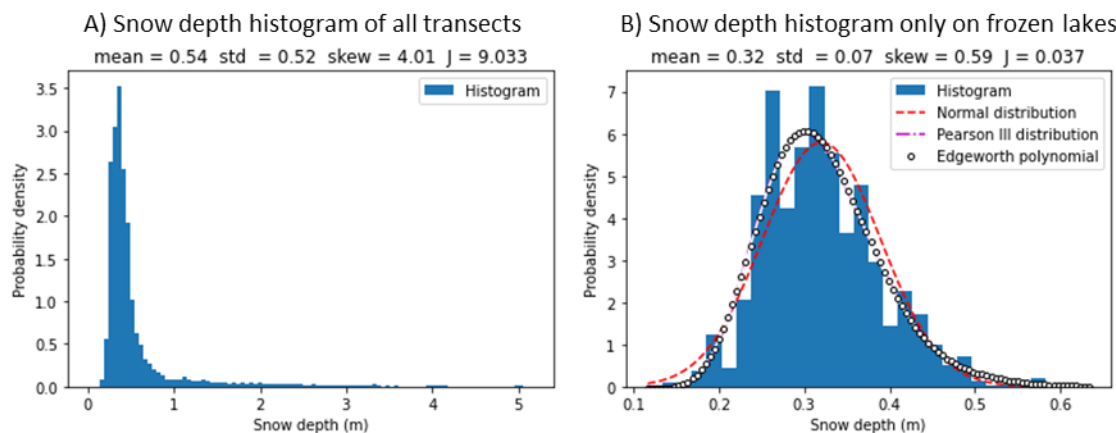
204 Snow depth surveys using a GPR are particularly effective for deep-snow areas since the  
205 Magnaprobe is only 1.5 m long. Considering the lower limit of the selected GPR antenna, we  
206 collected several GPR transects (Malå ProEx, 800 MHz, GuidelineGeo, Sundbyberg, Sweden)  
207 around Inigok, where the snowpack was deeper than in the coastal area. The antenna was placed  
208 on a sled towed by a snowmachine traveling  $< 5\text{ km h}^{-1}$ . The effect of compaction by the  
209 snowmachine was considered negligible because the snow was highly wind-packed and therefore  
210 was not affected by the weight of the snowmachine during data collection. The GPR data were  
211 processed in ReflexW (Sandmeier Software, Karlsruhe, Germany) using a low frequency noise  
212 removal (dewow) and a linear gain with topographic correction adapted from the ArcticDEM  
213 (Rangel et al., 2023b). Maps of snow depth estimated from the GPR transects are shown in  
214 Figure 3. The line color denotes the observed snow depth (the darker, the deeper). A substantial  
215 snowdrift developed near the lakeshore's banks due to its steep topography.

216 Figure 4 displays the histograms of GPR snow depth data in Inigok, North Slope, Alaska, in May  
217 2019 when using (A) all transect data and (B) the frozen lake sections only. The snow depth  
218 histogram of all transects shows strong non-Gaussianity due to a mix of steep and flat terrain.  
219 However, the histogram of the partial dataset only for the frozen lakes shows much weaker non-  
220 Gaussianity. In fact, snow distribution after removing the deep-snow parts can be reasonably  
221 approximated by the Gaussian distribution with a negentropy of 0.037, which is the same level as  
222 Wadepiper Pond (Figure 2) in the previous section ( $J = 0.040$ ). Therefore, the snowdrift due to  
223 steep terrain is considered a major source of non-Gaussianity in snow depth in open tundra.



224

225 Figure 3: Snow depth surveys using GPR along multiple transects in Inigok, North Slope, Alaska  
 226 (27 and 28 April 2019) superimposed over the land cover map with 1 meter interval contour  
 227 lines. The approximated center coordinates of the maps are 153.105W 70.005N (INI04 &  
 228 INI01), 152.949W 69.993N (Lonely wolf), 153.274W 69.992N (Deep basin), and 153.032W  
 229 69.942N (Three creatures & Independent fox).



230

231 Figure 4: Snow depth histograms of GPR snow survey data from Inigok, North Slope, Alaska  
 232 (April 2019) using A) all transects and B) sections on frozen lake only. Snow distributions in the  
 233 Inigok area are highly non-Gaussian, while the frozen lake subset shows weak non-Gaussianity.

234

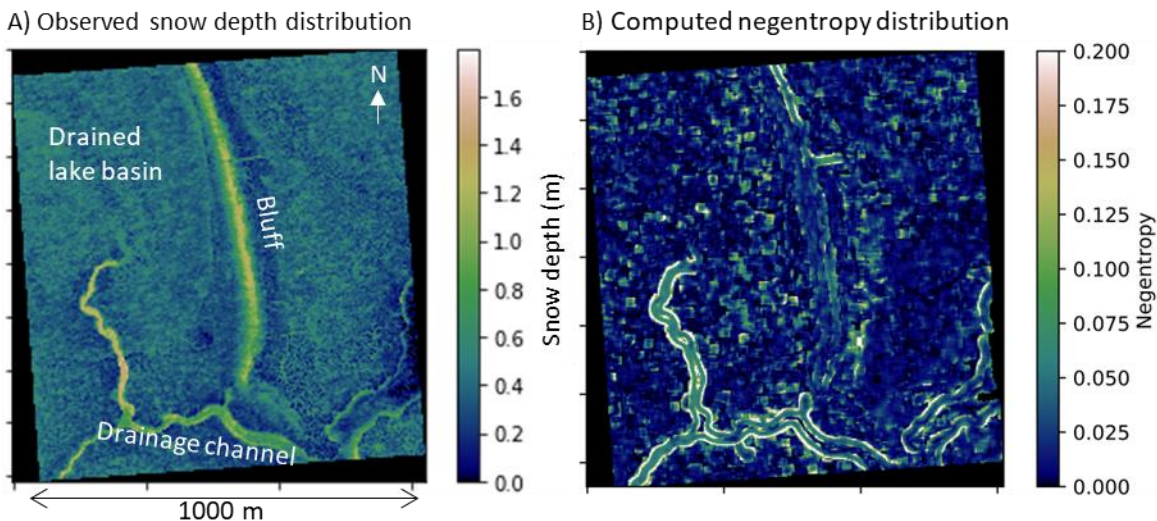
### 235 3.3 Snow depth distribution based on UAV footage of a drained lake basin within 236 the CALM 1-km grid near Utqiagvik, AK (May 2019)

237 Figure 5 (left panel) presents the observed snow distribution of a drained thermokarst lake basin  
 238 referred to as Central Marsh, part of the Circumpolar Active Layer Monitoring (CALM)  
 239 Network located east of Utqiagvik, Alaska. The snow depth was estimated by differentiating the  
 240 snow surface elevation and the snow-free ground elevation using UAV surveys with the  
 241 photogrammetry technique. The images were collected on August 4, 2019 (snow-free), and April  
 242 15, 2019 (snow-covered), using a Phantom 4 UAV (P4RTK). Images were post-

243 processed/georeferenced to NAD83 Zone 4 North in ellipsoid heights using a propeller aeropoint  
244 and Pix4D (version 4.3.33 for the April survey, 4.4.12 for the August survey) at 0.25 m spatial  
245 resolution (Nichols, 2020). The vertical accuracies of these measurements are 18 cm and 10 cm  
246 for the April and August surveys, respectively. The horizontal resolution for the snow depth is 1  
247 m.

248 The CALM site is situated in the ACP in northern Alaska, which has typical complex terrain due  
249 to the recently drained thermokarst lake with sparse or negligible vegetation and well-developed  
250 polygons. There is an obvious smoothed bluff in the center of the domain, and the west side of  
251 this bluff tapers into the drained lake basin. The incised drainage channels cause steep land  
252 features that capture sizable snowdrifts in the southern part. In the southern portion of the area,  
253 the polygons are formed by ground surface cracks with ice wedge development beneath found in  
254 lower and higher center parts in the left panel of Figure 5.

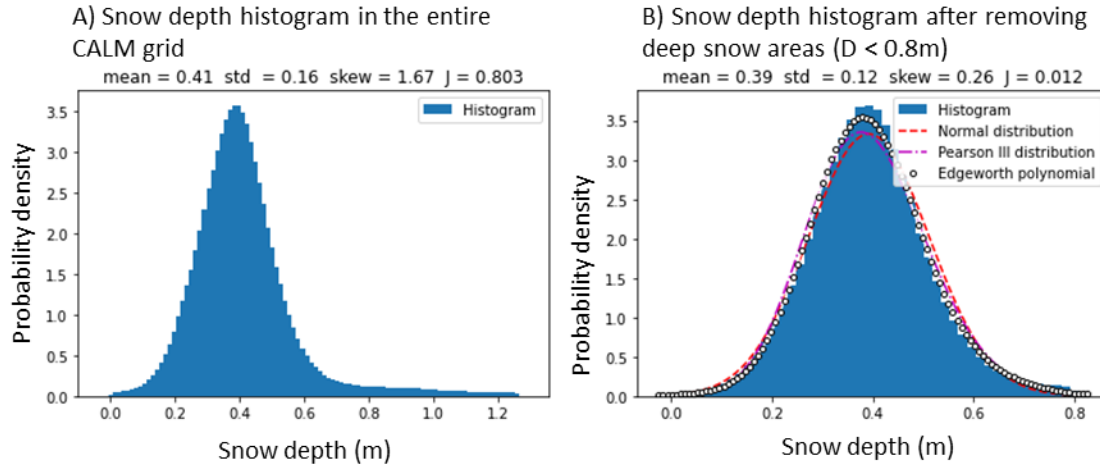
255 The negentropy distribution in the moving window may be obtained from this gridded snow data  
256 at a very high spatial resolution. The right panel of Figure 5 presents the computed negentropy  
257 map in the CALM area with a 30-m moving window. Overall, non-Gaussianity in the CALM site  
258 was found to be weak—even with the smoothed bluff and despite high snow depth. However, as  
259 whiter parts in right panel of Figure 5 are found along the drainage channels, topographic  
260 discontinuity around the incised gully seems to cause significant non-Gaussianity. Additionally,  
261 vegetation patches may bring spotty non-Gaussianity in the northern part of the area. Conversely,  
262 since the southern parts covered by the polygons except the drainage channels show darker color  
263 ( $J < 0.025$ ), the ground surface polygon does not make snow distribution non-Gaussian. Overall,  
264 snowpack in the coastal parts of the ACP can reasonably be approximated by Gaussian  
265 distribution since most of the CALM area showed a small negentropy of less than 0.2.



266

267 Figure 5: Snow depth distribution based on UAV photogrammetry and the computed negentropy  
268 distribution of 30-m moving windows in a drained lake basin in the CALM 1-km grid (71.3026°  
269 N, 156.6008°W) near Utqiagvik, Alaska.

270 Figure 6 presents the snow depth histogram, which looks like a Gaussian distribution with a long  
 271 tail due to snowdrift around the gullies in the CALM grid. In fact, when the deep snowdrifts of  
 272 the gully and the bluff are removed from the samples, the histogram more closely resembles a  
 273 Gaussian distribution (see the right panel in Figure 6).



274  
 275 Figure 6: Snow depth histogram based on the UAV photogrammetry of a drained lake basin in  
 276 the CALM 1-km grid near Utqiagvik, Alaska. Removing the deep snow parts caused by wind-  
 277 induced snowdrift results in a near-perfect fit by Gaussian distribution.

278 **3.4 SWE products based on ASO data for the selected watersheds**

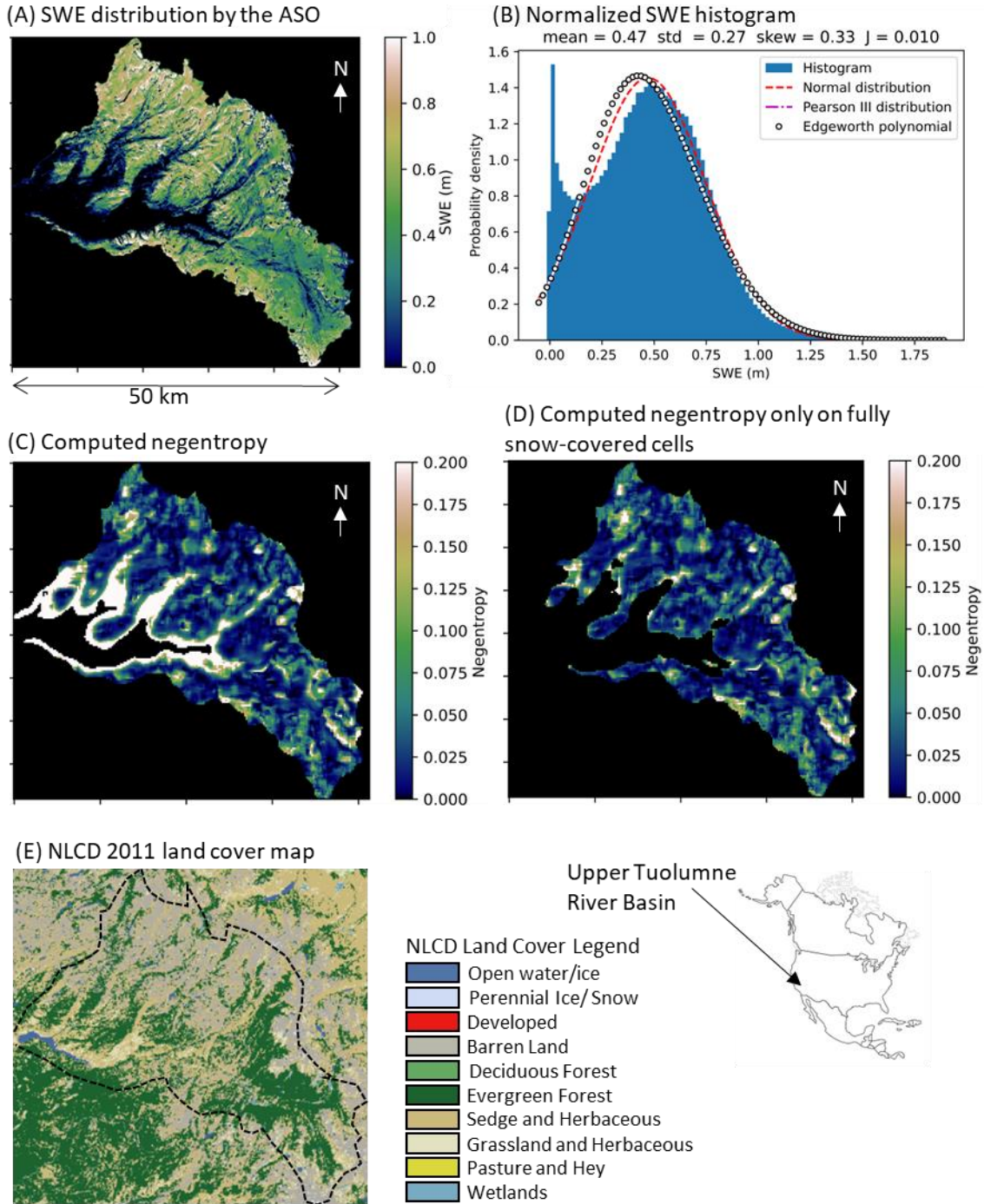
279 SWE is a stable and direct indicator of snow/water distribution in landscapes. As such, the SWE  
 280 products from the Airborne Snow Observatory (ASO) were selected (Painter et al., 2016) to  
 281 examine the Gaussianity of snow distributions in different climate zones and landscapes with  
 282 alpine to subalpine snowpack. The snow depth and SWE distributions were estimated from the  
 283 coupled imaging spectrometer and scanning LiDAR, then combined with distributed snow  
 284 modeling (including snow density simulation). The ASO snow products are considered one of  
 285 the most comprehensive instantaneous snow distribution estimations at fine resolution (50 m).  
 286 We used the processed snow product to characterize the medium-scale snow distribution with the  
 287 same outlier treatment (IQR method) as described above.

288 The analysis of three representative SWE datasets in the western US is presented. These include  
 289 Upper Tuolumne River watershed in California (USCATB, April 3, 2013), East River watershed  
 290 above Gunnison, Colorado (USCOGE, March 31, 2018), and the Olympic Mountains in  
 291 Washington (USWAOL, March 29, 2016).

292 **3.4.1 Tuolumne River Watershed, California**

293 Figure 7 presents the composite graphics of the data and the analysis results for the Upper  
 294 Tuolumne River watershed on April 3, 2013. Panel A shows the SWE distribution estimated by  
 295 the ASO, while panel B visualizes the normalized SWE histogram or PDF within the entire  
 296 domain with the fitted theoretical distributions. Panels C and D are the negentropy distributions  
 297 of the SWE within 1500-m moving windows with and without partially snow-covered cells.  
 298 Panel E shows the NLCD 2011 land cover map for reference. The watershed (1175 km<sup>2</sup>) is one

299 of the drainages to the California Central Valley through the Hetch Hetchy reservoir in the  
300 southern Sierra Nevada Mountain Range. The boundary of the catchment is mostly comprised of  
301 steep rocky alpine terrain (which contributes to the attractive land features of Yosemite National  
302 Park), whereas the bottom of the valley is relatively flat due past glacial processes. The snow  
303 distribution (panel A) shows a clear relationship with elevation, while the SWE barely exceeded  
304 1 m during the observation period in peak snow season. The overall SWE histogram (panel B)  
305 illustrates strong non-Gaussianity because of snow-free and shallow accumulation areas in the  
306 watershed (bounded distribution effect).



307

308 Figure 7: (A) SWE distribution based on ASO data of the Upper Tuolumne River Basin,  
 309 California, USA from April 3, 2013 (USCATB, 37.461°N, 119.494°W); (B) normalized SWE  
 310 histogram; (C) negentropy map of the SWE within 1500-m moving windows; (D) negentropy  
 311 map of only fully snow-covered cells; (E) NLCD 2011 land cover map.

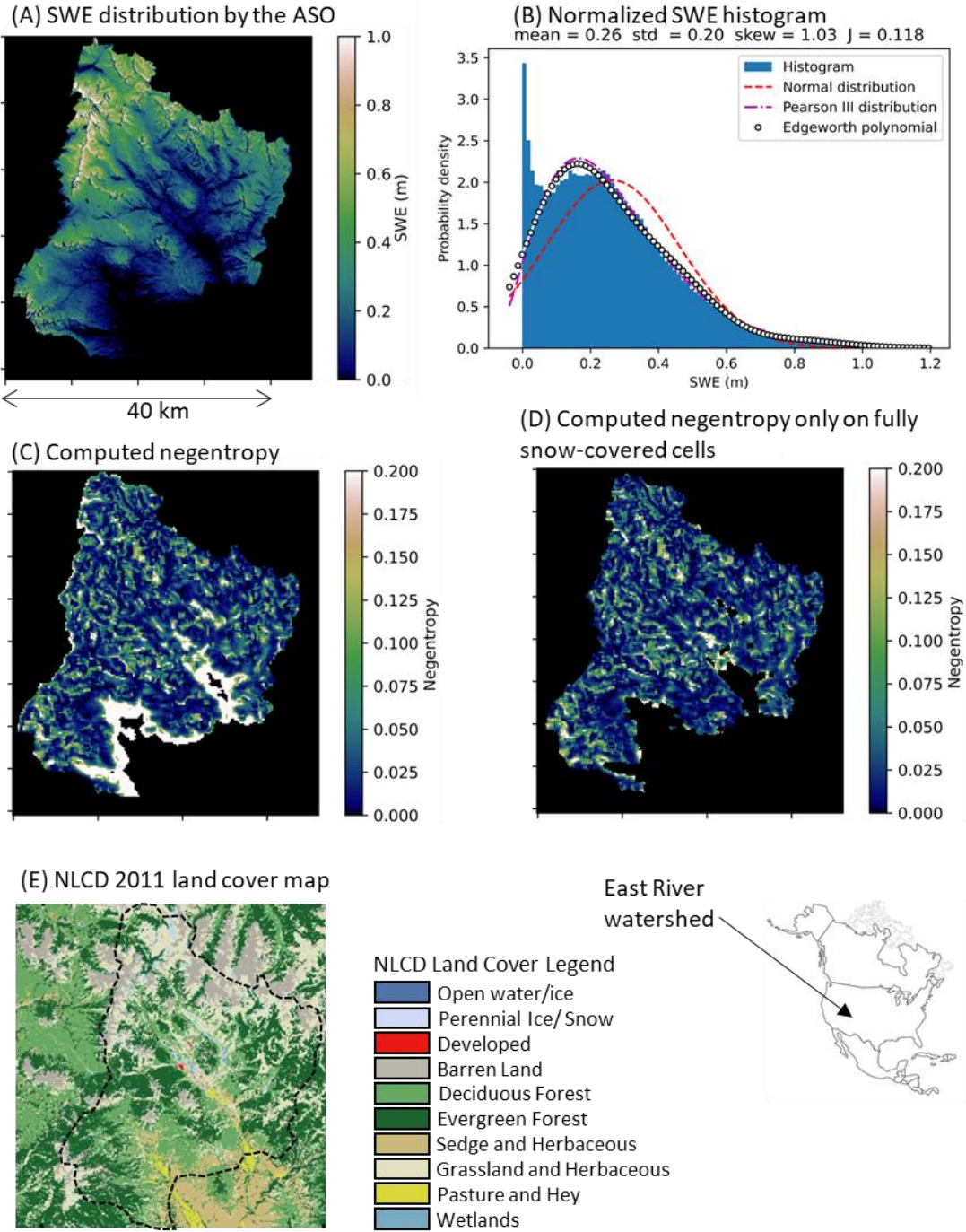
312 However, the local negentropy map with moving windows (panel C) shows small non-  
 313 Gaussianity except in the low-elevation areas. In fact, the majority of high non-Gaussianity cells  
 314 are from partially snow-covered cells. When the partially snow-covered cells are removed in

315 panel D, the local negentropy falls by less than 0.15 in most of the watershed. Therefore, the  
316 bounded distribution effect in the probability domain from the partially snow-covered cells  
317 brings substantial non-Gaussianity into the snow distribution.

318 Additionally, the spatial resolution of 50 m may be too coarse to capture the local snowdrift  
319 effect discussed in sections 3.2 and 3.3. using the very fine resolution data since snowdrift extent  
320 around steep cliff is often smaller than the resolution of medium to large scale snow products.  
321 Therefore, even with fully snow-covered areas, fine resolution data is required for snowdrift  
322 characterization which is potentially important for more accurate snow storage estimation.  
323 However, further study is recommended using finer resolution snow data although the combined  
324 effect of steep terrain and vegetation on snowdrift is highly complicated and hard to characterize  
325 even with modern remote sensing technology.

### 326 **3.4.2 East River, Colorado**

327 The ASO dataset of the East River above Gunnison, Colorado (USCOGE) was selected as a  
328 representative basin in the Rocky Mountains region. This dataset includes the U.S. Department  
329 of Energy (DOE)'s East River community observatory, where comprehensive field data have  
330 recently been collected (Kakalia et al., 2020). The data domain, which does not agree with the  
331 watershed boundary, is approximately 1670 km<sup>2</sup> with the elevation ranging from 2,343m  
332 (Gunnison) to 3,901 m. Figure 8 displays the corresponding analysis results of the East River  
333 area on March 31, 2018.



334

335 Figure 8: (A) SWE distribution based on ASO data for the East River watershed above  
 336 Gunnison, Colorado, USA from March 31, 2018 (USCOGE, 39.037°N 106.978°W); (B)  
 337 normalized SWE histogram; (C) negentropy map of the SWE within 1500-m moving windows;  
 338 (D) negentropy map of only fully snow-covered cells; (E) NLCD 2011 land cover map.

339 Besides the obvious bounded distribution effect of partially snow-covered cells, this case study  
 340 illustrates the non-Gaussianity induced by the steep topographic features around the high peaks  
 341 in the Rocky Mountains. However, it is interesting that the range of negentropy remains less than

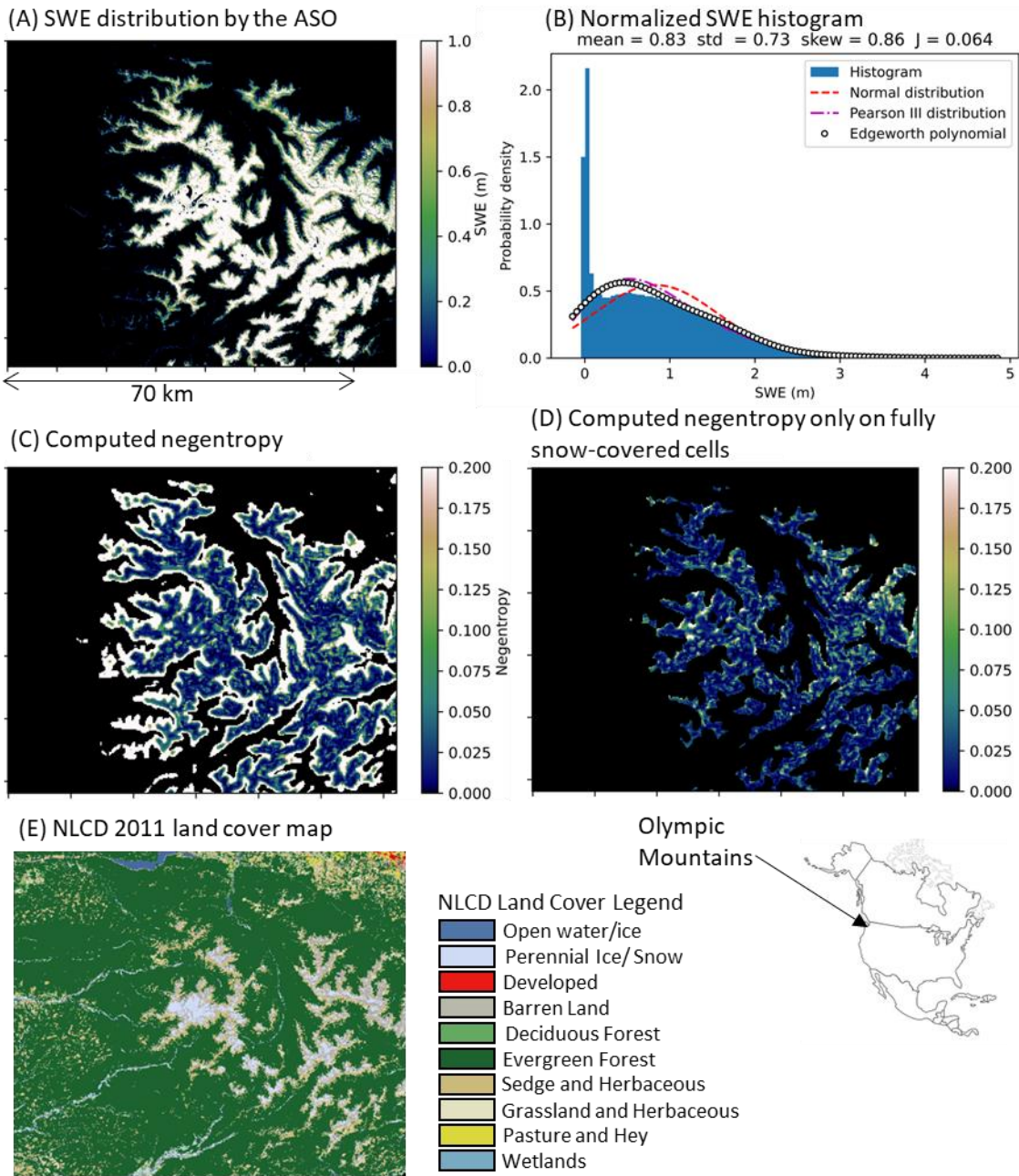


342 0.5 in fully snow-covered areas in panel D despite very steep topography in the East River  
343 watershed. At Inigok, for example, it is a flat/low-rolling-hills landscape that is punctuated by  
344 very abrupt, very steep bluffs that cause the large drifts. In contrast, while East River certainly  
345 has much more total topographic relief, it does not have the same long, flat fetch area where the  
346 wind can build unimpeded, nor does it have similar abrupt erosional bluffs. Also, since the lower  
347 negentropy (darker colored) parts in panel D generally agree with the evergreen and deciduous  
348 forest cover extent in the NLCD land cover map in panel E, the subalpine forest may reduce non-  
349 Gaussianity in snow distribution. However, the general characteristics of the sample's  
350 negentropy distribution in Upper Colorado are consistent with the Upper Tuolumne River  
351 watershed in the Sierra Nevada Mountain Range.

### 352 **3.4.3 Olympic Mountains, Washington**

353 The last example of snow non-Gaussianity quantification is the Olympic Mountains in  
354 Washington, USA, which represent the Northern Pacific Coastal Range under strong oceanic  
355 influence. The elevation ranges from sea level to 2430 m. The Olympic Mountains consist of a  
356 cluster of steep-sided peaks, heavily forested foothills, and incised deep valleys. The ASO data

357 have a large spatial coverage (5,330 km<sup>2</sup>) when compared to the other two ASO datasets  
 358 presented here.



359  
 360 Figure 9: (A) SWE distribution based on ASO data for the Olympic Mountains, Washington,  
 361 USA from March 29, 2016 (USWAOL, 47.792°N 123.650°W); (B) normalized SWE histogram;  
 362 (C) negentropy map of the SWE within 1500-m moving windows; (D) negentropy map of only  
 363 fully snow-covered cells; (E) NLCD 2011 land cover map.

364 The black areas in the high elevation range in panel A are the approximate glacier extent  
 365 excluded from the analysis (Painter et al., 2018). A large fraction of partially snow-covered cells  
 366 also introduces non-Gaussianity in SWE in this region. Meanwhile, dense evergreen forests in

367 the Olympic Mountains seem to effectively reduce the non-Gaussianity of SWE above the snow  
368 line during the ASO scanning period. Overall the non-Gaussianity of the snowpack may be  
369 considered small when compared to the other two examples, which is likely due to denser forest  
370 cover. Presumably, the vegetation cover minimizes the wind-induced snow redistribution process  
371 and makes the snow distribution more Gaussian. These characteristics—i.e., non-Gaussianity in  
372 partially snow-covered areas and high Gaussianity in forested areas—are common features of the  
373 SWE distributions throughout the western US.

## 374 **4 Discussion**

375 The sample negentropy values presented here are generally consistent with each other despite the  
376 variety of data collection methods used at different scales. The level of random noise in the  
377 datasets depends on the data collection methods. Among the datasets discussed here, one may  
378 anticipate that the ASO data have the largest Gaussian bias due to multiple remote sensing,  
379 resampling, assimilating, and modeling procedures covering remarkable spatial coverages with  
380 uniform data quality. The UAV-based LiDAR data at the North Slope CALM site are expected  
381 to have a noticeable random bias with a vertical accuracy of approximately 12 cm. The GPR  
382 snow depth observations should have a smaller but appreciable Gaussian bias due to snow  
383 quality variation and non-flat snow surface elevation (antenna angle vibration), although the  
384 continuous measurement minimizes the random relative error in the snow depth estimation. The  
385 hand-measured snow depth data using a probe may include the least Gaussian bias, while the  
386 sampling spacing was not uniform and in addition, due to relative poor spatial positioning  
387 control with the Magnaprobe’s onboard GPS unit. Despite these differences, it is encouraging  
388 that the quantified Gaussian levels were comparable and consistent since they share common  
389 features.

390 The stability of the sample estimator of negentropy may be a potential issue, especially when the  
391 sample size is small. Additionally, since the higher-order statistical moments are sensitive to the  
392 presence of outliers in the sample, an outlier removal filter is recommended for large samples.  
393 The IQR method with a threshold of 3 IQR above the third quarter (Q3), which is stricter than  
394 the usual threshold (typically 1.5 IQR), has been applied for the UAV photogrammetry data and  
395 the ASO datasets for computational stability. Even with the large threshold (small outlier  
396 removal), the proposed method using negentropy appears to be effective in characterizing the  
397 Gaussianity of snow distribution, which has been a common implicit assumption for existing  
398 gridded data and models. This study visualized the limitation of such a common distribution  
399 assumption for snow distribution, specifically for areas with partial snow cover.

400 To summarize the analyses presented here, five categories of Gaussianity were defined and  
401 associated with a magnitude of sample negentropy value (see Table 2). Most of the fully snow-  
402 covered areas fell into the category “almost Gaussian,” with a negentropy less than 0.03.  
403 Notably, a negentropy less than 0.01 is considered nearly perfect Gaussian, as can be seen in the  
404 previous sections.

405 The Gaussianity characterization of snow distribution appears to be useful in distinguishing the  
406 snowdrift-affected areas using the sample negentropy. Simultaneously, this finding can justify

407 the implicit Gaussian assumption for snow distribution for overall SWE estimation, particularly  
 408 for snowpack characterization from remotely sensed information. For instance, the effect of  
 409 higher-order statistical moments can be negligible in most fully snow-covered areas. Conversely,  
 410 some additional statistical treatment for higher order statistics may be required for the areas with  
 411 the non-Gaussian effects around snow lines, open wind-swept areas, and sharp terrains.  
 412 Additionally, since consistent pattern in skew coefficient was not identified from the snow  
 413 datasets, the commonly-used log-normal distribution may not be suitable for those areas.

414 Table 2: Summary of the analysis using the sample negentropy.

Class	Negentropy	Landscape & land cover type	Examples
Strong non-Gaussian	$0.2 < J$	Partially snow-covered areas, mixture of landscapes (steep-flat)	CALM, Inigok, Upper Tuolumne, East River, Olympic Mountains
Non-Gaussian	$0.1 < J \leq 0.2$	Snowdrift around steep terrain	CALM
Weak non-Gaussian	$0.03 < J \leq 0.1$	Snowdrift on a frozen lake, vegetation cluster	Teshekpuk, Inigok, CALM
Nearly Gaussian	$0.01 < J \leq 0.03$	Most of the uniform terrain in open tundra and alpine forest	Teshekpuk, CALM, Upper Tuolumne, East River, Olympic Mountains
Gaussian	$J \leq 0.01$	Open tundra (sedge, polygons), most forested areas	Teshekpuk, Upper Tuolumne, East River, Olympic

415

416 It is encouraging that snow depth and SWE distributions are generally well approximated by the  
 417 Gaussian or weak non-Gaussian distribution, which is a fundamental assumption for statistical  
 418 characterization of sub-gird variability used in snowpack estimation by remote sensing. The non-  
 419 Gaussianity found in the partially snow-covered areas may also be modeled by truncated normal  
 420 distribution although it must be tested further. Moreover, weak non-Gaussian distribution would  
 421 enable the Edgeworth expansion method proposed by Pires and Perdigão (2007). For instance,  
 422 the non-Gaussian asymptotic method or information metric can effectively determine the saddle  
 423 point approximation of the joint probability density functions (PDF) through maximizing the  
 424 Shannon entropy between the remotely sensed signal and the SWE. Thus, the quantification of  
 425 non-Gaussianity in snow depth/SWE distributions would be an important milestone toward  
 426 accurate snow water quantification using remote sensing techniques as well as grid-based snow  
 427 and earth surface models.

## 428 **5 Conclusions**

429 A Gaussian snow distribution is a common underlying assumption for finite scale models or  
430 gridded datasets. The present study tested this assumption using the sample negentropy of  
431 various snow data. We found two main sources of non-Gaussianity: (1) partial snow cover effect  
432 (bounded distribution) and (2) wind-induced snowdrift effect around steep terrain features. The  
433 second effect may amplify the first one in wind-swept alpine areas since snow erosion remains  
434 shallow on rocky ridges and peaks. The snowdrift around lakeshore cliffs and deep gullies can  
435 bring moderate non-Gaussianity in the open tundra of North Slope, Alaska. However, the wind-  
436 packed snow in the coastal plain region of the North Slope may generally be categorized as  
437 weakly Gaussian during mid to late winter due to the continuous snow cover. This implies that  
438 the non-Gaussianity of the snowpack may not be neglected during the snow accumulation season  
439 and late spring season. Interestingly, small ground surface features (e.g., low-centered and high-  
440 centered ice wedge polygons) make snow distribution more Gaussian, while snowdrift (snow  
441 dunes) on a flat frozen lake seems to be less Gaussian than on tundra or in a drained lake basin.

442 Our analyses of the ASO SWE products reinforced the findings for snowpacks on the tundra.  
443 Although SWE data was chosen instead of snow depth for practical reasons, the common  
444 features in non-Gaussianity remain valid. Additionally, the snow diffuser effect of forests was  
445 illustrated in three representative areas in the western US. This effect was reported by He et al.  
446 (2019) based on airborne LiDAR snow depth measurements on the Snowy Range, Wyoming,  
447 USA. Hence, it is likely that vegetation cover generally makes snow distribution more Gaussian  
448 in the snow accumulation process; however, further verification of this relationship is  
449 recommended.

450 Overall, a Gaussian distribution is a suitable approximation for snow spatial distribution when  
451 the ground is completely covered by snow. Higher-order statistics associated with landscape type  
452 may potentially improve the SWE estimation in wind-swept open terrain and near snow lines.  
453 The level of non-Gaussianity will determine the choice of statistical tool to correct the systematic  
454 bias in snow measurements. Meanwhile, this study suggests the possibility of partitioning the  
455 extent of wind-induced snowdrifts by means of independent component analysis (Comon et al.,  
456 2010).

## 457 **Author contribution**

458 NO performed the analysis, and RAPP offered technical advice. NO, ADP, RCR, and BMJ  
459 provided the field observed data for the case studies in Alaska. ADP, BMJ, KMH, RAPP, and  
460 RCR actively participated in the discussions and manuscript improvement. NO prepared the  
461 manuscript with contributions from all co-authors.

## 462 **Competing interests**

463 The authors declare that they have no conflict of interest.

## 464 **Acknowledgments**

465 This study was supported by the National Science Foundation (NSF) Office of Polar Programs  
466 (OPP) under the awards 1806287, 1806213, and 1806202. The authors thank UIC Science and  
467 CH2MHill Polar Field Services (now Battelle Arctic Research Operations) for their logistical  
468 field support. RP acknowledges support from the European Union under the Horizon Europe  
469 grant 101074004 (C2IMPRESS), the Meteoceanics flagships MR-220617 and MR-070220-  
470 BLUE. We used the NSIDC DAAC Airborne Snow Observatory (ASO) data downloaded from  
471 NSIDC.org.

## 472 **Data Availability Statement**

473 The data used in this research are publicly available at the NSF Arctic Data Center:  
474 <https://doi.org/10.18739/A24746T0K>, and <https://doi.org/10.18739/A2NV99C4P>  
475

## 476 **References**

- 477 Aas, K. S., Gisl nas, K., Westermann, S., & Berntsen, T. K.: A tiling approach to represent  
478 subgrid snow variability in coupled land surface–atmosphere models. *Journal of*  
479 *Hydrometeorology*, 18(1), 49-63, 2017.
- 480 Brubaker, K. L., & Menoes, M. I. C. H. A. E. L.: A technique to estimate snow depletion curves  
481 from time-series data using the beta distribution. In *Proceedings of the Eastern Snow*  
482 *Conference* (Vol. 58, pp. 343-346), 2001.
- 483 Carter, L. D.: A Pleistocene sand sea on the Alaskan Arctic Coastal Plain. *Science*, 211(4480),  
484 381–383. <https://doi.org/10.1126/science.211.4480.381>, 1981.
- 485 Comon, P., & Jutten, C. (Eds.): *Handbook of Blind Source Separation: Independent component*  
486 *analysis and applications*. Academic press, 2010.
- 487 Comon, P., 1994: Independent component analysis, a new concept? *Signal Process.*, 36, 287–  
488 314.
- 489 Donald, J. R., Soulis, E. D., Kouwen, N., & Pietroniro, A.: A land cover-based snow cover  
490 representation for distributed hydrologic models. *Water Resources Research*, 31(4), 995-  
491 1009, 1995.
- 492 Egli, L., & Jonas, T.: Hysteretic dynamics of seasonal snow depth distribution in the Swiss  
493 Alps. *Geophysical research letters*, 36(2), 2009.
- 494 Fleming, S. W., Zukiewicz, L., Strobel, M. L., Hofman, H., & Goodbody, A. G.: SNOTEL, the  
495 Soil Climate Analysis Network, and water supply forecasting at the Natural Resources  
496 Conservation Service: Past, present, and future. *JAWRA Journal of the American Water*  
497 *Resources Association*, 2023.

498 Hall, D. K., G. A. Riggs, and V. V. Salomonson: MODIS/Terra Snow Cover 5-Min L2 Swath  
 499 500m. Version 5. Boulder, Colorado USA: NASA National Snow and Ice Data Center  
 500 Distributed Active Archive Center. <http://dx.doi.org/10.5067/ACYTYZB9BEOS>, 2006.

501 He, S., Ohara, N., & Miller, S. N.: Understanding subgrid variability of snow depth at 1-km scale  
 502 using Lidar measurements. *Hydrological Processes*, 33(11), 1525-1537, 2019.

503 He, S., Smirnova, T. G., & Benjamin, S. G.: Single-Column Validation of a Snow Subgrid  
 504 Parameterization in the Rapid Update Cycle Land-Surface Model (RUC LSM). *Water  
 505 Resources Research*, 57(8), e2021WR029955, 2021.

506 Hyvärinen, A., Karhunen, J., & Oja, E.: Independent component analysis and blind source  
 507 separation. ISBN:9780471221319, |DOI:10.1002/0471221317, John Wiley & Sons, Inc.,  
 508 2001.

509 Kakalia, Z., Varadharajan, C., Alper, E., Brodie, E., Burrus, M., Carroll, R., ... & Agarwal, D.:  
 510 The East River Community Observatory Data Collection: Diverse, multiscale data from  
 511 a mountainous watershed in the East River, Colorado. *Authorea Preprints*, 2020.

512 Kolberg, S. A., & Gottschalk, L.: Updating of snow depletion curve with remote sensing  
 513 data. *Hydrological Processes: An International Journal*, 20(11), 2363-2380, 2006.

514 Lalande, M., Ménégou, M., Krinner, G., Ottlé, C., & Cheruy, F.: Improving climate model skill  
 515 over High Mountain Asia by adapting snow cover parameterization to complex-  
 516 topography areas. *The Cryosphere*, 17(12), 5095-5130, 2023.

517 Liston, G. E.: Representing subgrid snow cover heterogeneities in regional and global  
 518 models. *Journal of climate*, 17(6), 1381-1397, 2004.

519 Luce, C. H., & Tarboton, D. G.: The application of depletion curves for parameterization of  
 520 subgrid variability of snow. *Hydrological processes*, 18(8), 1409-1422, 2004.

521 Luce, C. H., Tarboton, D. G., & Cooley, K. R.: Sub-grid parameterization of snow distribution  
 522 for an energy and mass balance snow cover model. *Hydrological Processes*, 13(12-13),  
 523 1921-1933, 1999.

524 Meloche, J., Langlois, A., Rutter, N., Royer, A., King, J., Walker, B., ... & Wilcox, E. J.:  
 525 Characterizing tundra snow sub-pixel variability to improve brightness temperature  
 526 estimation in satellite SWE retrievals. *The Cryosphere*, 16(1), 87-101, 2022.

527 Meng, C.: Quantifying the impacts of snow on surface energy balance through assimilating snow  
 528 cover fraction and snow depth. *Meteorology and Atmospheric Physics*, 129, 529-538,  
 529 2017.

530 Mott, R., Daniels, M., & Lehning, M.: Atmospheric flow development and associated changes in  
 531 turbulent sensible heat flux over a patchy mountain snow cover. *Journal of  
 532 Hydrometeorology*, 16(3), 1315-1340, 2015.

- 533 Mott, R., Schögl, S., Dirks, L., & Lehning, M.: Impact of extreme land surface heterogeneity on  
534 micrometeorology over spring snow cover. *Journal of Hydrometeorology*, 18(10), 2705-  
535 2722, 2017.
- 536 Nichols, I.O.: Assessing the accuracy of a UAV snow depth survey Utqiagvik (Barrow), Alaska  
537 calm grid, M. S. Thesis, Geological Engineering, Michigan Technological University,  
538 2020.
- 539 Nitta, T., Yoshimura, K., Takata, K., O'ishi, R., Sueyoshi, T., Kanae, S., ... & Liston, G. E.:  
540 Representing variability in subgrid snow cover and snow depth in a global land model:  
541 offline validation. *Journal of climate*, 27(9), 3318-3330, 2014.
- 542 Painter, T. H., Berisford, D. F., Boardman, J. W., Bormann, K. J., Deems, J. S., Gehrke, F., ... &  
543 Winstral, A.: The Airborne Snow Observatory: Fusion of scanning lidar, imaging  
544 spectrometer, and physically-based modeling for mapping snow water equivalent and  
545 snow albedo. *Remote Sensing of Environment*, 184, 139-152, 2016.
- 546 Painter, Thomas H. and Dennis P. Lettenmaier: GPM Ground Validation Airborne Snow  
547 Observatory (ASO) OLYMPEX [indicate subset used]. Dataset available online from  
548 the NASA Global Hydrometeorology Resource Center DAAC, Huntsville, Alabama,  
549 U.S.A. DOI: <http://dx.doi.org/10.5067/GPMGV/OLYMPEX/LIDAR/DATA101>, 2018.
- 550 Pires, C.A., and R.A.P. Perdigão: Non-Gaussianity and Asymmetry of the Winter Monthly  
551 Precipitation Estimation from the NAO. *Mon. Wea. Rev.*, 135, 430–448,  
552 <https://doi.org/10.1175/MWR3407.1>, 2007.
- 553 Perdigão, R.A.P.: Nonlinear statistics and dynamics of atmospheric predictability and  
554 downscaling. <http://hdl.handle.net/10451/2013>, 2010.
- 555 Perdigão, R.A.P.: Fluid Dynamical Systems: From Quantum Gravitation to Thermodynamic  
556 Cosmology. <https://doi.org/10.46337/mdsc.5091>, 2017.
- 557 Perdigão, R.A.P.: Polyadic Entropy, Synergy and Redundancy among Statistically Independent  
558 Processes in Nonlinear Statistical Physics with Microphysical Codependence. *Entropy*  
559 2018, 20, 26. <https://doi.org/10.3390/e20010026>, 2018.
- 560 Rudisill, William, Alan Rhoades, Zexuan Xu, and Daniel R. Feldman: Are atmospheric models  
561 too cold in the mountains? The state of science and insights from the SAIL field  
562 campaign. *Bulletin of the American Meteorological Society*, 2024.
- 563 Rangel, R. C., Ohara, N., Parsekian, A. D., and Jones, B. M.: Arctic Tundra Lake Drainage  
564 Increases Snow Storage in Drifts. *Journal of Geophysical Research: Earth Surface*,  
565 e2023JF007294, 2023a.
- 566 Rangel, R. C., Parsekian, A. D., Ohara, N., and Jones, B. M.: Ground Penetrating Radar (GPR)  
567 data on snow over lakes and drained lake basins in Inigok, North Slope of Alaska, April  
568 2019. Arctic Data Center. doi:10.18739/A2NV99C4P, 2023b.



- 569 Santanello Jr, J. A., Dirmeyer, P. A., Ferguson, C. R., Findell, K. L., Tawfik, A. B., Berg, A., ...  
570 & Wulfmeyer, V.: Land–atmosphere interactions: The LoCo perspective. *Bulletin of the*  
571 *American Meteorological Society*, 99(6), 1253-1272, 2018.
- 572 Sengupta, A., Singh, B., DeFlorio, M. J., Raymond, C., Robertson, A. W., Zeng, X., ... & Jones,  
573 J.: Advances in subseasonal to seasonal prediction relevant to water management in the  
574 western United States. *Bulletin of the American Meteorological Society*, 103(10),  
575 E2168-E2175, 2022.
- 576 Shamir, E., & Georgakakos, K. P.: Estimating snow depletion curves for American River basins  
577 using distributed snow modeling. *Journal of Hydrology*, 334(1-2), 162-173, 2007.
- 578 Skaugen, T., & Randen, F.: Modeling the spatial distribution of snow water equivalent, taking  
579 into account changes in snow-covered area. *Annals of Glaciology*, 54(62), 305-313,  
580 2013.
- 581 Sturm, M., & Holmgren, J.: An automatic snow depth probe for field validation campaigns.  
582 *Water Resources Research*, 54(11), 9695-9701, 2018.
- 583 Tarricone, J., Webb, R. W., Marshall, H. P., Nolin, A. W., & Meyer, F. J.: Estimating snow  
584 accumulation and ablation with L-band interferometric synthetic aperture radar  
585 (InSAR). *The Cryosphere*, 17(5), 1997-2019, 2023.
- 586 Tsang, L., Durand, M., Derksen, C., Barros, A. P., Kang, D. H., Lievens, H., ... & Xu, X.: Global  
587 monitoring of snow water equivalent using high-frequency radar remote sensing. *The*  
588 *Cryosphere*, 16(9), 3531-3573, 2022.
- 589 Younas, W., Hay, R. W., MacDonald, M. K., ul ISLAM, S., & Dery, S. J.: A strategy to  
590 represent impacts of subgrid-scale topography on snow evolution in the Canadian Land  
591 Surface Scheme. *Annals of Glaciology*, 58(75pt1), 1-10, 2017.