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2 Distributions of Various Landscapes

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- 4 Noriaki Ohara¹, Andrew D. Parsekian¹, Benjamin M. Jones², Rodrigo C. Rangel¹.6,
- 5 Kenneth M. Hinkel³, and Rui A. P. Perdigão^{4,5}
- 6 ¹University of Wyoming, Laramie, WY, USA
- 7 ²University of Alaska Fairbanks, Fairbanks, AK, USA
- 8 ³Michigan Technological University, Houghton, MI, USA
- 9 ⁴Meteoceanics Institute for Complex System Science, IUC Physics of Complex Coevolutionary
- 10 Systems & Fluid Dynamical Systems, Washington, DC, USA
- 11 ⁵Synergistic Manifolds, Lisbon, Portugal
- 12 Department of Earth Sciences, University of Toronto, Toronto, Ontario, Canada

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- 14 Corresponding author: Noriaki Ohara (nohara1@uwyo.edu)
- 15 Summary
- 16 Snow distribution characterization is essential for accurate snow water estimation for water
- 17 resource prediction from existing in-situ observations and remote sensing data at a finite spatial
- 18 resolution. Four different observed snow distribution datasets were analyzed for Gaussianity. It
- 19 was found non-Gaussianity of snow distribution is a signature of wind redistribution effect.
- 20 Generally, seasonal snowpack can be well approximated by Gaussian distribution for fully snow-
- 21 covered area.

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Abstract

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23 Seasonal snowpack is an important predictor of available water resources in the following spring 24 and early summer melt season. Total basin snow water equivalent (SWE) estimation usually 25 requires a form of statistical analysis that is implicitly built upon the Gaussian framework. 26 However, it is important to characterize the non-Gaussian properties of snow distribution for 27 accurate large-scale SWE estimation based on remotely sensed or sparse ground-based 28 observations. This study quantified non-Gaussianity using sample negentropy, the Kullback-29 Leibler divergence from Gaussian distribution, for field-observed snow depth data on the North 30 Slope, Alaska, and three representative SWE distributions in the western US from the Airborne 31 Snow Observatory (ASO). Snowdrifts around lakeshore cliffs and deep gullies can bring 32 moderate non-Gaussianity in the open, lowland tundra of North Slope, Alaska, while the ASO 33 dataset suggests that subalpine forests may effectively suppress the non-Gaussianity of snow 34 distribution. Thus, non-Gaussianity is found in areas with partial snow cover and wind-induced snowdrifts around topographic breaks in slope and other steep terrain features. The snowpacks 35 may be considered weakly Gaussian in coastal regions with open tundra in Alaska and alpine and 36 37 subalpine terrains in the western US if the land is completely covered by snow. The wind-38 induced snowdrift effect can be potentially partitioned from the observed snow spatial 39 distribution guided by its Gaussianity.

1 Introduction

Modeling of the spatial variability of snow is important for large-scale earth surface modeling since atmospheric circulation is sensitive to snow cover presence (e.g., Aas et al., 2016; Meng, 2017; Mott et al., 2015, 2017; Nitta et al., 2014; Younas et al., 2017). Since subgrid variability often causes appreciable bias in weather predictions, (e.g. Lalande et al., 2023; Rudisill et al., 2024), accurate snow cover quantification can potentially improve the predictability of weather, planetary boundary-layer evolution, convective cloud formation, and even tropical cyclogenesis (Santanello et al., 2018). Hence, the subgrid variability of snow cover has been incorporated into operational regional weather forecasting models such as the High-Resolution Rapid Refresh (HRRR) model (He et al., 2021).

- 51 Observations of seasonal snow storage in mountainous areas through remote sensing and ground-52 based measurements are a direct and reliable indicator of the water supply during the following 53 spring season in downstream regions (e.g. Fleming et al., 2023; Sengupta et al., 2022). However, 54 total basin snow water equivalent (SWE) estimation usually requires a statistical relationship 55 such as the snow depletion curve (SDC), which correlates with observables such as the snow 56 cover area fraction (SCF). Based on a study of the observed snow distributions in Reynolds 57 Creek Experimental Watershed in Idaho, Luce et al. (1999) showed that one snow distribution can reasonably represent the SDC evolution for the rest of the season. Also, Luce and 58 59 Turboton (2004) showed a high degree of similarity in nine years of dimensionless 60 depletion curves measured in the same basin. Shamir and Georgakakos (2007) demonstrated the
 - consistency of SDC over a season in the American River using a distributed model. The

62 subseasonal and interseasonal consistency in SDCs suggests the possibility for subgrid snow characterization as well as basin wide SWE estimation from SCF data such as the MODIS 63 64 product (Hall et al., 2006). 65 As remote sensing technologies advance, seasonal snow distribution characterization becomes 66 more approachable with multi-sensor methods. For example, Tarricone et al. (2023) analyzed 67 three Interferometric Synthetic Aperture Radar (InSAR) image pairs to assess SWE evolution 68 using the snow-focused multi-sensor method with Uninhabited Aerial Vehicle Synthetic 69 Aperture Radar (UAVSAR) and an L-band InSAR data as well as optical fractional snow-70 covered area (SCA) information. However, to estimate the total basin SWE in water resource 71 management practices, statistical empirical relationships are required to fill gaps in the spatial 72 and temporal resolutions—even when using these remote sensing observations (Tsang et al., 73 2022). For example, Meloche et al. (2022) assumed log-normal distribution to represent the subpixel variability of remotely sensed data. Thus, uncertainty and subgrid variability must be 74 75 accounted for when using statistical characterization in SWE estimation. 76 The most popular choice for the probability density function (PDF) of snow is log-normal 77 distribution, which inherently eliminates negative snow depth (Donald et al., 1995; Liston, 2004; 78 and many others). Brubaker and Menoes (2001) chose a beta distribution, while Kolberg and 79 Gottschalk (2006) selected a two-parameter γ-distribution. Although these common distributions 80 are in the exponential family, they were primarily chosen for convenience. Indeed, the representativeness of these parametric probability distributions remains questionable for different 81 82 landscapes and snowpack ages (e.g., Skaugen & Randen, 2013; Egli & Jonas, 2009; He, Ohara, 83 & Miller, 2019). Moreover, these approaches for bounded distributions may not work for 84 evolving snowpacks with partial SCA where zero values are present in the probability domain. 85 In theory, without microtopography and meteorological effects, since the landing location of 86 each snow particle fallen from the atmosphere is considered an independent and identically 87 distributed (iid) random variable, the resulting snow depth or SWE distribution should 88 asymptotically approach a Gaussian distribution due to the central limit theorem. He, Ohara, and 89 Miller (2019) reported non-Gaussian snow distribution in open areas as well as Gaussian snow 90 distributions in many of the forested, fully snow-covered areas during the peak snow season 91 using airborne Light Detection and Ranging (LiDAR) observations in the Snowy Range, 92 Wyoming. This implies the presence of both systematic (non-Gaussian) and random (Gaussian) 93 mechanisms in snow accumulation and ablation processes. Therefore, it is possible to identify 94 the potential factors as "signals" that make the snow distribution deviate from a Gaussian 95 distribution by analyzing the resultant snow distributions. 96 This study applies negentropy to analyze the non-Gaussianity of snow distributions in Arctic 97 tundra, as well as alpine and subalpine landscapes in North America. Negentropy measures the

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departure in entropy between a sampled distribution and Gaussian distribution of identical

non-Gaussian components because pure random noise asymptotically becomes Gaussian in

variance and mean. Signals of interest (e.g., systematic snowdrift patterns) can be extracted as

theory. This is the main idea of independent component analysis (ICA; Hyvärinen et al., 2000).

This work presents the quantified non-Gaussianity of the observed snow distributions through a

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103 variety of snow distribution data, including intense direct hand measurements within 30-m grids

104 using a probe, and indirect measurements using a snowmachine-attached ground-penetrating

105 radar (GPR), UAV-based photogrammetry, as well as the Airborne Snow Observatory (ASO)

SWE products. 106

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2 Methods

2.1 Negentropy

109 To measure the non-Gaussianity of any data, we implement the information-theoretic metric of

110 negentropy as the objective function since negentropy is equal to the Kullback-Leibler

divergence between p_r and a Gaussian distribution with the same mean and variance as p_r . 111

112 There is a well-known proposition that Gaussian density has the largest information entropy

113 among all unbounded distributions with the same first and second-order statistics. As such, the

114 non-Gaussianity of an observed distribution can be quantified by negentropy J, which is defined

115 as follows (Hyvärinen et al., 2000):

$$J(X) = S(X_{gauss}) - S(X)$$
 (1)

117 where S is the information entropy of X. The information entropy can assume a diversity of

metrics ranging from the most general capturing microphysical event-scale codependence in

nonlinear statistical mechanics (Perdigão 2018) or simply assuming basic event-scale

119 120 independence in classical information theory (Shannon (1948) statistical entropy). For the

121 purpose of this study, we take the latter simple form, which is defined as:

$$122 S(X) = -\int p_x(\eta) \log[p_x(\eta)] d\eta_{\alpha}.$$
 (2)

123 where p_x is the PDF of X, and η is a dummy variable for the integration. The Edgeworth

expansion (Edgeworth, 1905) can provide an approximation for a PDF of X, as follows:

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$$p_x(X) = \frac{\phi(U)}{\sigma} \left[1 + \frac{\kappa_3}{6} H_3(U) + \frac{\kappa_4}{24} H_4(U) + \frac{\kappa_3^2}{72} H_6(U) + \cdots \right]$$
(3)

126 where

U = standardized random variable of X127

 $H_k(U)$ = Chebyshev-Hermite polynomials 128

129 $\phi(U)$ = standard normal density

130 κ_k = k-th order cumulant of U.

131 Substituting the Edgeworth series into the negentropy definition, Comon (1994) obtained the

132 analytical expression:

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$$J(X) = \frac{1}{12} \kappa_3^2 + \frac{1}{48} \kappa_4^2 + \frac{7}{48} \kappa_4^4 - \frac{1}{8} \kappa_3^2 \kappa_4 + O(n^{-2}). \tag{4}$$

134 This is the estimator of negentropy at fourth-order cumulant. In practice, a more intuitive

135 approximation is commonly used, as follows: Formatted: German (Germany)

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136	$J(X) = \frac{1}{12} \text{skew}(U)^2 + \frac{1}{48} \text{kurt}(U)^2$	(5)
137	where skew and kurt are the skewness and kurtosis of standardized variable, U , respectively.	
138 139 140 141	The sample estimation of the higher-order moment and cumulant (e.g., skew and kurtosis coefficients) is known to be sensitive to the presence of outliers. In this study, the interquartile range (IQR) method was adopted for outlier removal with a minimum removal that lies outsid the range of three times IQR.	
142 143 144 145 146	While negentropy metrics and corresponding Edgeworth approximations have been previously explored and further developed in atmospheric sciences and in physics, including derivations implementations to higher-order distributions, elaborate numerical and analytical estimators (Pires and Perdigão 2007, Perdigão 2010, Perdigão 2017), the present study brings a simplifie treatment not yet explored in Hydrology/hydrology and tailored for swift and seamless integrat within hydrological and water resource systems investigations.	and d
148	2.2 Data collection	
149	We analyzed four types of data with different collection methodologies at various scales in thi	S
150	study, as listed in Table 1. The first is manual snow depth surveys using a GPS-aided snow pro-	obe
151	(Magnaprobe; Sturm & Holmgren, 2018), the second is snow depth transects using a	

snowmachine-attached GPR, the third is snow depth maps using UAV-based photogrammetry, and the last is the SWE product of the ASO. The first three datasets are for the open tundra in the

methodologies will be presented in Results section below. Figure 1 displays the map of the snow

Arctic Coastal Plain (ACP) of Alaska while the ASO data are for the alpine and subalpine

regions of the continental USA. Detailed data specifications associated with the collection

depth surveys in North Slope, Alaska, USA.

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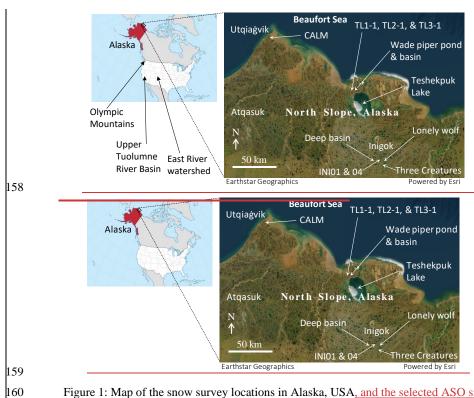


Figure 1: Map of the snow survey locations in Alaska, USA, and the selected ASO sites.

Table 1: List of snow datasets

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Site name	Location	Lon/Lat	Spatial	Elevation	Data	Date	Sample	Landscape and	Fori
			resolut	range	collection		size	land cover	
			ion		method				Fori
TL1-1	Teshekpuk,	70.738°N,	~1m	0.91~1.2	Magnaprobe	<u>April</u>	<u>951</u>	Open tundra,	Fori
	AK	153.970°W		0 m MSL		24,		sedge and	
						<u>2022</u>		herbaceous	Fori
TL2-1	Teshekpuk,	70.740°N,	~1m	<u>2.35~2.5</u>	Magnaprobe	<u>April</u>	<u>925</u>	Open tundra.	Fori
	<u>AK</u>	153.956°W		4 m MSL		25,		sedge and	For
						2022		herbaceous	FOI
<u>TL3-1</u>	Teshekpuk,	70.739°N,	<u>~1m</u>	1.86~2.1	<u>Magnaprobe</u>	<u>April</u>	904	Open tundra.	Fori
	<u>AK</u>	153.928°W		8 m MSL		25,		sedge and	Fori
						2022		<u>herbaceous</u>	
Wade piper	Teshekpuk,	70.751°N,	<u>~1m</u>	2.18~2.5	Magnaprobe	<u>April</u>	927	Open tundra,	Fori
pond	AK	153.870°W		0 m MSL		27,		sedge and	For
						2022		<u>herbaceous</u>	
Wade piper	Teshekpuk,	70.746°N,	<u>~1m</u>	3.68~3.8	Magnaprobe	<u>April</u>	960	Open tundra.	Fori
<u>basin</u>	<u>AK</u>	153.854°		8 m MSL		<u>29,</u>		sedge and	For
		W				<u>2022</u>		<u>herbaceous</u>	
Inigok	Inigok, AK	70.001° N,	~0.5m	<u>37.8~59.</u>	GPR	May,	<u>16655</u>	Open tundra.	Fori
		153.068°		1 m MSL		<u>2019</u>		sedge and	Fori
CALM	T Taulin to the	<u>W</u>	0.25	1.02	UAV	Mon	2.020.240	herbaceous	-
CALM	Utqiagvik,	71.3026°	<u>0.25m</u>	<u>-1.93~</u>		May, 2019	2,928,240	Open tundra, sedge and	Fori
	<u>AK</u>	<u>N,</u> 156.6008°		3.8 m MSL	photogramme	2019		herbaceous	_ <u>_</u> _
		W		MISL	try			Herbaceous	For
Upper	California	37.461°N,	50 m	1,142~	ASO SWE	April 3,	470,213,	Steep rocky	Fori
Tuolumne		119.494°W		3,965 m	product	2013		alpine terrain,	
River				MSL,	*			partially	For
								forested	Fori
East River	Colorado	39.037°N	<u>50 m</u>	2,343~	ASO SWE	March	667,883	Alpine and	
_		106.978°W		3,901 m	product	31,		subalpine	For
				MSL		2018		forest	Fori
Olympic	Washingto	47.792°N	<u>50 m</u>	0~2,432	ASO SWE	<u>March</u>	2,066,907	Dense forest	F
Mountains	<u>n</u>	123.650°W		m MSL	product	<u>29,</u>		and high peaks	Fori
	1					2016			Fori

3 Results

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3.1 Manual snow surveys at Teshekpuk, North Slope, Alaska (May 2022)

Snow depth data were collected using a Magnaprobe (Sturm & Holmgren, 2018) in five 30 x 30-m grids with 1 m grid spacing north of Teshekpuk Lake, North Slope, AK, in May 2022. The GPS location of each measurement was automatically recorded. Figure 2 presents the interpolated snow depth distributions and corresponding histograms (right columns) in five areas near Teshekpuk. The observer measured the point scale snow depth at approximately every 1 m along a line toward flags placed 1 m apart on the surface. Since the data points were selected from undisturbed snow, the locations are unevenly distributed despite the snowpacks generally being highly hardened by wind. The relative spatial locations are considered accurate since the operator stood on the same side of the probe and followed pre-marked lines based on the tape measure; however, the absolute plotted coordinate in the figures may not be trustworthy due to

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176	the GPS horizontal accuracy < 3 m. The topography of these grids in the ACP are very flat with
177	elevation variation of less than 1 meter while accurate absolute elevation data are hard to
178	compare due to the spatial inaccuracy of the Magnaprobe.
179	The graphics in the left column of Figure 2 present the point depth observation locations and
180	interpolated snow depth distributions using the nearest distance method. The number of data
181	points denoted by the black dots is n=951 (TL1-1), n=925 (TL2-1), n=904 (TL3-1), n=927
182	(Wadepiper Pond), and n= 960 (Wadepiper Basin).
183	The corresponding snow depth histograms and three fitted distributions are displayed in the right
184	column. The statistics mean, standard deviation, skew coefficient, and negentropy (J) are
185	reported on the top part of each graph. In general, the snow depth distributions in these areas are
186	almost Gaussian distributions since the computed negentropy is small. However, the negentropy
187	of snow distribution affected by wind-induced snowdrift (sastrugi) on frozen lakes is larger than
188	the tundra covered by sedge and herbaceous vegetation. In practice, the non-Gaussianity of
189	seasonal snow depth may have been negligible in the coastal open tundra (including frozen open
190	waters) in the Teshekpuk study area in May 2022.

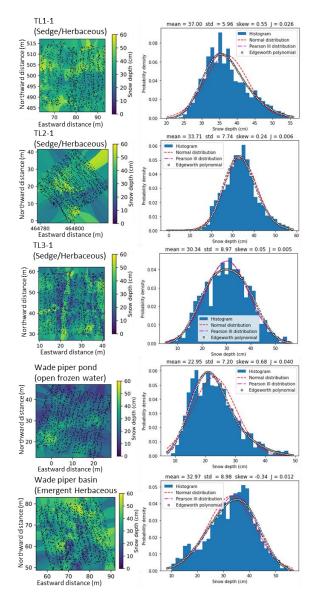


Figure 2: Manual snow distributions in the Teshekpuk Lake area, North Slope, Alaska (May 2022) and corresponding histograms with fitted probability density functions (PDFs). J denotes the computed negentropy. Snow depth histograms in open tundra in 30 m x 30 m squares are generally categorized as "weak-non-Gaussian." The approximated center coordinates of the grids

- 196 are 70.738°N, 153.970°W (TL1-1), 70.740°N, 153.956°W (TL2-1), 70.739°N, 153.928°W (TL3-
- 197 1), 70.751°N, 153.870°W (Wadepiper Pond), and 70.746°N, 153.854° W (Wadepiper Basin).

3.2 Snow depth surveys using GPR along multiple transects in Inigok, North Slope, AK (April 2019)

- 200 The Inigok area of North Slope, Alaska (70.001° N, 153.068° W) is characterized by paleo sand
- dunes (Carter, 1981), hydro-geomorphological processes, and permafrost landforms such as
- 202 thermokarst lake formation and drainage. The landscape is characterized by relatively steep
- 203 terrain and substantial wind-induced snowdrifts (deeper than 5 m), especially around lake shores
- and drainage channels (e.g., Rangel et al., 2023).
- 205 Snow depth surveys using a GPR are particularly effective for deep-snow areas since the
- 206 Magnaprobe is only 1.5 m long. Considering the lower limit of the selected GPR antenna, we
- 207 collected several GPR transects (Malå ProEx, 800 MHz, GuidelineGeo, Sundbyberg, Sweden)
- around Inigok, where the snowpack was deeper than in the coastal area. The antenna was placed
- 209 on a sled towed by a snowmachine traveling < 5km h⁻¹. The effect of compaction by the
- 210 snowmachine was considered negligible because the snow was highly wind-packed and therefore
- 211 was not affected by the weight of the snowmachine during data collection. The GPR data were
- 212 processed in ReflexW (Sandmeier Software, Karlsruhe, Germany) using a low frequency noise
- 213 removal (dewow) and a linear gain with topographic correction adapted from the ArcticDEM
- 214 (Rangel et al., 2023b). Maps of snow depth estimated from the GPR transects are shown in
- 215 Figure 3. The line color denotes the observed snow depth (the darker, the deeper). A substantial
- snowdrift developed near the lakeshore's banks due to its steep topography.
- 217 Figure 4 displays the histograms of GPR snow depth data in Inigok, North Slope, Alaska, in May
- 218 2019 when using (A) all transect data and (B) the frozen lake sections only. The snow depth
- 219 histogram of all transects shows strong non-Gaussianity due to a mix of steep and flat terrain.
- However, the histogram of the partial dataset only for the frozen lakes shows much weaker non-
- Gaussianity. In fact, snow distribution after removing the deep-snow parts can be reasonably
- approximated by the Gaussian distribution with a negentropy of 0.037, which is the same level as
- Wadepiper Pond (Figure 2) in the previous section (J = 0.040). Therefore, the snowdrift due to
- steep terrain is considered a major source of non-Gaussianity in snow depth in open tundra.

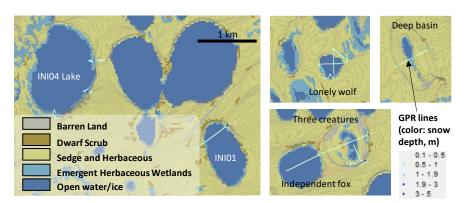


Figure 3: Snow depth surveys using GPR along multiple transects in Inigok, North Slope, Alaska (27 and 28 April 2019) superimposed over the land cover map with 1 meter interval contour lines. The approximated center coordinates of the maps are 153.105W 70.005N (INI04 & INI01), 152.949W 69.993N (Lonely wolf), 153.274W 69.992N (Deep basin), and 153.032W 69.942N (Three creatures & Independent fox).

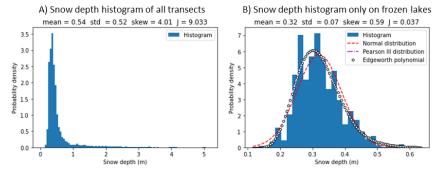


Figure 4: Snow depth histograms of GPR snow survey data from Inigok, North Slope, Alaska (April 2019) using A) all transects and B) sections on frozen lake only. Snow distributions in the Inigok area are highly non-Gaussian, while the frozen lake subset shows weak non-Gaussianity.

3.3 Snow depth distribution based on UAV footage of a drained lake basin within the CALM 1-km grid near Utqiagʻvik, AK (May 2019)

Figure 5 (left panel) presents the observed snow distribution of a drained thermokarst lake basin referred to as Central Marsh, part of the Circumpolar Active Layer Monitoring (CALM) Network located east of Utqiagʻvik, Alaska. The snow depth was estimated by differentiating the snow surface elevation and the snow-free ground elevation using UAV surveys with the photogrammetry technique. The images were collected on August 4, 2019 (snow-free), and April 15, 2019 (snow-covered), using a Phantom 4 UAV (P4RTK). Images were post-

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processed/georeferenced to NAD83 Zone 4 North in ellipsoid heights using a propeller aeropoint and Pix4D (version 4.3.33 for the April survey, 4.4.12 for the August survey) at 0.25 m spatial resolution (Nichols, 2020). The vertical accuracies of these measurements are 18 cm and 10 cm for the April and August surveys, respectively. The horizontal resolution for the snow depth is 1 m.

The CALM site is situated in the ACP in northern Alaska, which has typical complex terrain due to the recently drained thermokarst lake with sparse or negligible vegetation and well-developed polygons. There is an obvious smoothed bluff in the center of the domain, and the west side of this bluff tapers into the drained lake basin. The incised drainage channels cause steep land features that capture sizable snowdrifts in the southern part. In the southern portion of the area, the polygons are formed by ground surface cracks with ice wedge development beneath <u>found in lower and higher center parts in the left panel of Figure 5</u>.

The negentropy distribution in the moving window may be obtained from this gridded snow data at a very high spatial resolution. The right panel of Figure 5 presents the computed negentropy map in the CALM area with a 30-m moving window. Overall, non-Gaussianity in the CALM site was found to be weak—even with the smoothed bluff and despite high snow depth. However, as whiter parts in right panel of Figure 5 are found along the drainage channels, topographic discontinuity around the incised gully seems to cause significant non-Gaussianity. Additionally, vegetation patches may bring spotty non-Gaussianity in the northern part of the area. Conversely, since the southern parts covered by the polygons except the drainage channels show darker color (J <0.025), the ground surface polygon does not make snow distribution non-Gaussian. Overall, snowpack in the coastal parts of the ACP can reasonably be approximated by Gaussian distribution since most of the CALM area showed a small negentropy of less than 0.2.

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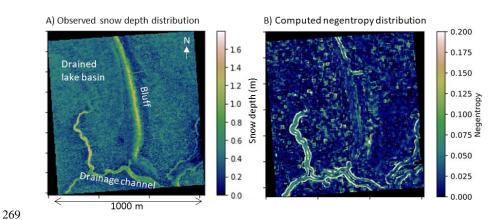


Figure 5: Snow depth distribution based on UAV photogrammetry and the computed negentropy distribution of 30-m moving windows in a drained lake basin in the CALM 1-km grid (71.3026° N, 156.6008°W) near Utqiagʻvik, Alaska.

Figure 6 presents the snow depth histogram, which looks like a Gaussian distribution with a long tail due to snowdrift around the gullies in the CALM grid. In fact, when the deep snowdrifts of the gully and the bluff are removed from the samples, the histogram more closely resembles a Gaussian distribution (see the right panel in Figure 6).

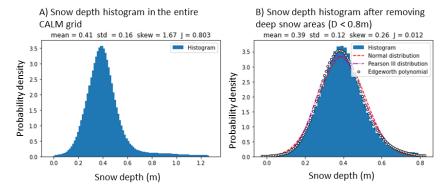


Figure 6: Snow depth histogram based on the UAV photogrammetry of a drained lake basin in the CALM 1-km grid near Utqiagʻvik, Alaska. Removing the deep snow parts caused by wind-induced snowdrift results in a near-perfect fit by Gaussian distribution.

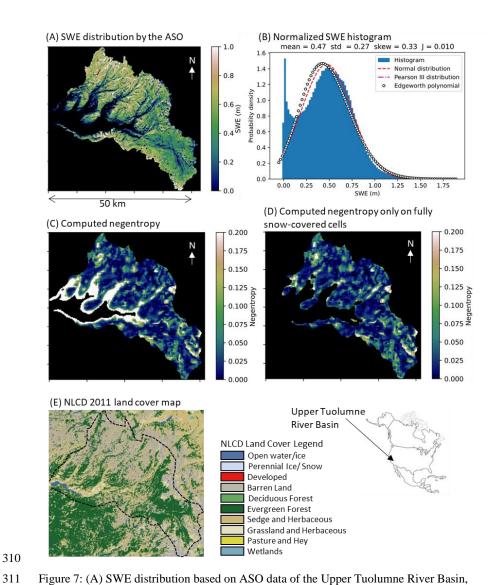
3.4 SWE products based on ASO data for the selected watersheds

SWE is a stable and direct indicator of snow/water distribution in landscapes. As such, the SWE products from the Airborne Snow Observatory (ASO) were selected (Painter et al., 2016) to examine the Gaussianity of snow distributions in different climate zones and landscapes with

- 285 alpine to subalpine snowpack. The snow depth and SWE distributions were estimated from the
- 286 coupled imaging spectrometer and scanning LiDAR, then combined with distributed snow
- 287 modeling (including snow density simulation). The ASO snow products are considered one of
- 288 the most comprehensive instantaneous snow distribution estimations at fine resolution (50 m).
- 289 We used the processed snow product to characterize the medium-scale snow distribution with the
- 290 same outlier treatment (IQR method) as described above.
- 291 The analysis of three representative SWE datasets in the western US is presented. These include
- 292 Upper Tuolumne River watershed in California (USCATB, April 3, 2013), East River watershed
- above Gunnison, Colorado (USCOGE, March 31, 2018), and the Olympic Mountains in 293
- Washington (USWAOL, March 29, 2016). 294

3.4.1 Tuolumne River Watershed, California

- 296 Figure 7 presents the composite graphics of the data and the analysis results for the Upper
- 297 Tuolumne River watershed on April 3, 2013. Panel A shows the SWE distribution estimated by
- 298 the ASO, while panel B visualizes the normalized SWE histogram or PDF within the entire
- 299 domain with the fitted theoretical distributions. Panels C and D are the negentropy distributions
- 300 of the SWE within 1500-m moving windows with and without partially snow-covered cells.
- 301 Panel E shows the NLCD 2011 land cover map for reference. The watershed (1175 km²) is one
- of the drainages to the California Central Valley through the Hetch Hetchy reservoir in the 302
- 303 southern Sierra Nevada Mountain Range. The boundary of the catchment is mostly comprised of
- 304
- steep rocky alpine terrain (which contributes to the attractive land features of Yosemite National
- 305 Park), whereas the bottom of the valley is relatively flat due past glacial processes. The snow
- 306 distribution (panel A) shows a clear relationship with elevation, while the SWE barely exceeded
- 307 1 m during the observation period in peak snow season. The overall SWE histogram (panel B)
- 308 illustrates strong non-Gaussianity because of snow-free and shallow accumulation areas in the
- 309 watershed (bounded distribution effect).



California, USA from April 3, 2013 (USCATB, 37.461°N, 119.494°W); (B) normalized SWE histogram; (C) negentropy map of the SWE within 1500-m moving windows; (D) negentropy map of only fully snow-covered cells; (E) NLCD 2011 land cover map.

However, the local negentropy map with moving windows (panel C) shows small non-Gaussianity except in the low-elevation areas. In fact, the majority of high non-Gaussianity cells are from partially snow-covered cells. When the partially snow-covered cells are removed in

319 bounded distribution effect in the probability domain from the partially snow-covered cells 320 brings substantial non-Gaussianity into the snow distribution. 321 Additionally, the spatial resolution of 50 m may be too coarse to capture the local snowdrift 322 effect discussed in sections 3.2 and 3.3. using the very fine resolution data since snowdrift extent 323 around steep cliff is often smaller than the resolution of medium to large scale snow products. 324 Therefore, even with fully snow-covered areas, fine resolution data is required for snowdrift 325 characterization which is potentially important for more accurate snow storage estimation. 326 However, further study is recommended using finer resolution snow data although the combined 327 effect of steep terrain and vegetation on snowdrift is highly complicated and hard to characterize 328 even with modern remote sensing technology. 329 3.4.2 East River, Colorado 330 The ASO dataset of the East River above Gunnison, Colorado (USCOGE) was selected as a 331 representative basin in the Rocky Mountains region. This dataset includes the U.S. Department 332 of Energy (DOE)'s East River community observatory, where comprehensive field data have 333 recently been collected (Kakalia et al., 2020). The data domain, which does not agree with the 334 watershed boundary, is approximately 1670 km² with the elevation ranging from 2,343m 335 (Gunnison) to 3,901 m. Figure 8 displays the corresponding analysis results of the East River

panel D, the local negentropy falls by less than 0.15 in most of the watershed. Therefore, the

318

336

area on March 31, 2018.

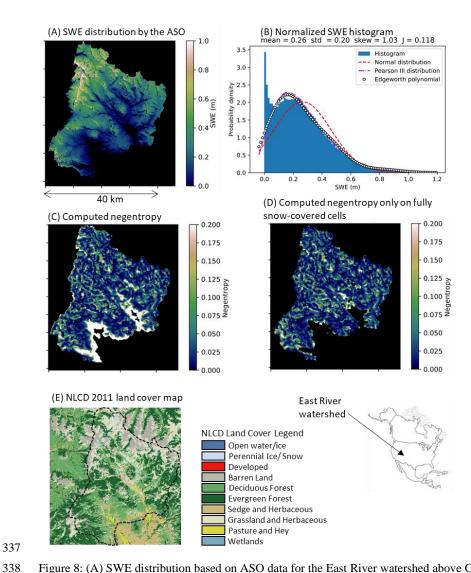


Figure 8: (A) SWE distribution based on ASO data for the East River watershed above Gunnison, Colorado, USA from March 31, 2018 (USCOGE, 39.037°N 106.978°W); (B) normalized SWE histogram; (C) negentropy map of the SWE within 1500-m moving windows; (D) negentropy map of only fully snow-covered cells; (E) NLCD 2011 land cover map.

Besides the obvious bounded distribution effect of partially snow-covered cells, this case study illustrates the non-Gaussianity induced by the steep topographic features around the high peaks in the Rocky Mountains. However, it is interesting that the range of negentropy remains less than

0.5 in fully snow-covered areas in panel D despite very steep topography in the East River
watershed. At Inigok, for example, it is a flat/low-rolling-hills landscape that is punctuated by
very abrupt, very steep bluffs that cause the large drifts. In contrast, while East River certainly
has much more total topographic relief, it does not have the same long, flat fetch area where the
wind can build unimpeded, nor does it have similar abrupt erosional bluffs. Also, since the lower
negentropy (darker colored) parts in panel D generally agree with the evergreen and deciduous
forest cover extent in the NLCD land cover map in panel E, the subalpine forest may reduce non-
Gaussianity in snow distribution. However, the general characteristics of the sample's
negentropy distribution in Upper Colorado are consistent with the Upper Tuolumne River
watershed in the Sierra Nevada Mountain Range.

3.4.3 Olympic Mountains, Washington

The last example of snow non-Gaussianity quantification is the Olympic Mountains in Washington, USA, which represent the Northern Pacific Coastal Range under strong oceanic influence. The elevation ranges from sea level to 2430 m. The Olympic Mountains consist of a cluster of steep-sided peaks, heavily forested foothills, and incised deep valleys. The ASO data have a large spatial coverage (5,330 km²) when compared to the other two ASO datasets presented here.

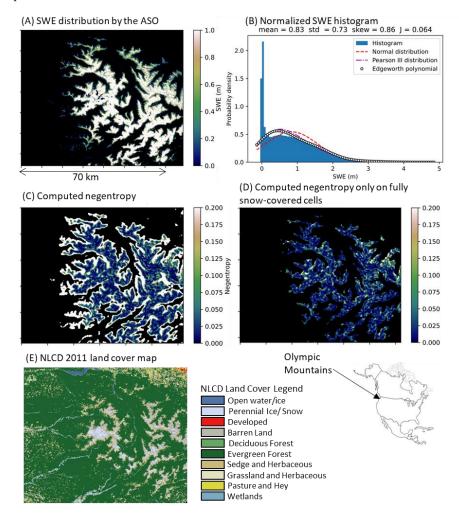


Figure 9: (A) SWE distribution based on ASO data for the Olympic Mountains, Washington, USA from March 29, 2016 (USWAOL, 47.792°N 123.650°W); (B) normalized SWE histogram;

- 365 (C) negentropy map of the SWE within 1500-m moving windows; (D) negentropy map of only
- fully snow-covered cells; (E) NLCD 2011 land cover map.
- 367 The black areas in the high elevation range in panel A are the approximate glacier extent
- 368 excluded from the analysis (Painter et al., 2018). A large fraction of partially snow-covered cells
- 369 also introduces non-Gaussianity in SWE in this region. Meanwhile, dense evergreen forests in
- 370 the Olympic Mountains seem to effectively reduce the non-Gaussianity of SWE above the snow
- 371 line during the ASO scanning period. Overall the non-Gaussianity of the snowpack may be
- 372 considered small when compared to the other two examples, which is likely due to denser forest
- 373 cover. Presumably, the vegetation cover minimizes the wind-induced snow redistribution process
- and makes the snow distribution more Gaussian. These characteristics—i.e., non-Gaussianity in
- 375 partially snow-covered areas and high Gaussianity in forested areas—are common features of the
- 376 SWE distributions throughout the western US.

4 Discussion

- 378 The sample negentropy values presented here are generally consistent with each other despite the
- variety of data collection methods used at different scales. The level of random noise in the
- datasets depends on the data collection methods. Among the datasets discussed here, one may
- anticipate that the ASO data have the largest Gaussian bias due to multiple remote sensing,
- 382 resampling, assimilating, and modeling procedures covering remarkable spatial coverages with
- 383 uniform data quality. The UAV-based LiDAR data at the North Slope CALM site are expected
- 384 to have a noticeable random bias with a vertical accuracy of approximately 12 cm. The GPR
- snow depth observations should have a smaller but appreciable Gaussian bias due to snow
- 386 quality variation and non-flat snow surface elevation (antenna angle vibration), although the
- 387 continuous measurement minimizes the random relative error in the snow depth estimation. The
- hand-measured snow depth data using a probe may include the least Gaussian bias, while the
- 389 sampling spacing was not uniform and in addition, due to relative poor spatial positioning
- 390 control with the Magnaprobe's onboard GPS unit. Despite these differences, it is encouraging
- that the quantified Gaussian levels were comparable and consistent since they share common
- 392 features.
- 393 The stability of the sample estimator of negentropy may be a potential issue, especially when the
- sample size is small. Additionally, since the higher-order statistical moments are sensitive to the
- 395 presence of outliers in the sample, an outlier removal filter is recommended for large samples.
- The IOR method with a threshold of 3 IOR above the third quarter (O3), which is much stricter
- 397 than the usual threshold (typically 1.5 IQR), has been applied for the UAV photogrammetry data
- and the ASO datasets for computational stability. Even with the large threshold (small outlier
- 399 removal), the proposed method using negentropy appears to be effective in characterizing the
- 400 Gaussianity of snow distribution, which has been a common implicit assumption for existing
- 401 gridded data and models. This study visualized the limitation of such a common distribution
- 402 assumption for snow distribution, specifically for areas with partial snow cover.
- 403 To summarize the analyses presented here, five categories of Gaussianity were defined and
- associated with a magnitude of sample negentropy value (see Table 12). Most of the fully snow-

covered areas fell into the category "almost Gaussian," with a negentropy less than 0.03. Notably, a negentropy less than 0.01 is considered nearly perfect Gaussian, as can be seen in the previous sections.

The Gaussianity characterization of snow distribution appears to be useful in distinguishing the snowdrift-affected areas using the sample negentropy. Simultaneously, this finding can justify the implicit Gaussian assumption for snow distribution for overall SWE estimation, particularly for snowpack characterization from remotely sensed information. For instance, the effect of higher-order statistical moments can be negligible in most fully snow-covered areas. Conversely, some additional statistical treatment for higher order statistics may be required for the areas with the non-Gaussian effects around snow lines, open wind-swept areas, and sharp terrains. Additionally, since consistent pattern in skew coefficient was not identified from the snow datasets, the commonly-used log-normal distribution may not be suitable for those areas.

Table $\frac{42}{2}$: Summary of the analysis using the sample negentropy.

Class	Negentropy	Landscape & land cover type	Examples	
Strong non- Gaussian	0.2 < J	Partially snow-covered areas, mixture of landscapes (steep- flat)	CALM, Inigok, Upper Tuolumne, East River, Olympic Mountains	
Non-Gaussian	$0.1 < J \le 0.2$	Snowdrift around steep terrain	CALM	
Weak non- Gaussian	$0.03 < J \le 0.1$	Snowdrift on a frozen lake, vegetation cluster	Teshekpuk, Inigok, CALM	
Nearly Gaussian	$0.01 < J \le 0.03$	Most of the uniform terrain in open tundra and alpine forest	Teshekpuk, CALM, Upper Tuolumne, East River, Olympic Mountains	
Gaussian	J ≤ 0.01	Open tundra (sedge, polygons), most forested areas	Teshekpuk, Upper Tuolumne, East River, Olympic	

It is encouraging that snow depth and SWE distributions are generally well approximated by the Gaussian or weak non-Gaussian distribution, which is a fundamental assumption for statistical characterization of sub-gird variability used in snowpack estimation by remote sensing. The non-Gaussianity found in the partially snow-covered areas may also be modeled by truncated normal distribution although it must be tested further. Moreover, weak non-Gaussian distribution would enable the Edgeworth expansion method proposed by Pires and Perdigão (2007). For instance, the non-Gaussian asymptotic method or information metric can effectively determine the saddle point approximation of the joint probability density functions (PDF) through maximizing the Shannon entropy between the remotely sensed signal and the SWE. Thus, the quantification of

428	non-Gaussiany	in snow der	th/SWE dist	ributions w	ould be an i	mportant milestone	toward

- 429 <u>accurate snow water quantification using remote sensing techniques as well as grid-based snow</u>
- 430 and earth surface models.

5 Conclusions

431

- 432 A Gaussian snow distribution is a common underlying assumption for finite scale models or
- 433 gridded datasets. The present study tested this assumption using the sample negentropy of
- 434 various snow data. We found two main sources of non-Gaussianity: (1) partial snow cover effect
- 435 (bounded distribution) and (2) wind-induced snowdrift effect around steep terrain features. The
- 436 second effect may amplify the first one in wind-swept alpine areas since snow erosion remains
- shallow on rocky ridges and peaks. The snowdrift around lakeshore cliffs and deep gullies can
- 438 bring moderate non-Gaussianity in the open tundra of North Slope, Alaska. However, the wind-
- 439 packed snow in the coastal plain region of the North Slope may generally be categorized as
- 440 weakly Gaussian during mid to late winter due to the continuous snow cover. This implies that
- 441 the non-Gaussianity of the snowpack may not be neglected during the snow accumulation season
- 442 and late spring season. Interestingly, small ground surface features (e.g., low-centered and high-
- 443 centered ice wedge polygons) make snow distribution more Gaussian, while snowdrift (snow
- 444 dunes) on a flat frozen lake seems to be less Gaussian than on tundra or in a drained lake basin.
- 445 Our analyses of the ASO SWE products reinforced the findings for snowpacks on the tundra.
- 446 Although SWE data was chosen instead of snow depth for practical reasons, the common
- 447 features in non-Gaussianity remain valid. Additionally, the snow diffuser effect of forests was
- 448 illustrated in three representative areas in the western US. This effect was reported by He et al.
- 449 (2019) based on airborne LiDAR snow depth measurements on the Snowy Range, Wyoming,
- 450 USA. Hence, it is likely that vegetation cover generally makes snow distribution more Gaussian
- in the snow accumulation process; however, further verification of this relationship is
- 452 recommended.
- Overall, a Gaussian distribution is a suitable approximation for snow spatial distribution when
- 454 the ground is completely covered by snow. Higher-order statistics associated with landscape type
- 455 may potentially improve the SWE estimation in wind-swept open terrain and near snow lines.
- The level of non-Gaussianity will determine the choice of statistical tool to correct the systematic
- 457 bias in snow measurements. Meanwhile, this study suggests the possibility of partitioning the
- 458 extent of wind-induced snowdrifts by means of independent component analysis (Comon et al.,
- 459 2010).

460

Author contribution

- NO performed the analysis, and RAPP offered technical advice. NO, ADP, RCR, and BMJ
- 462 provided the field observed data for the case studies in Alaska. ADP, BMJ, KMH, RAPP, and
- 463 RCR actively participated in the discussions and manuscript improvement. NO prepared the
- 464 manuscript with contributions from all co-authors.

465 Competing interests

The authors declare that they have no conflict of interest.

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475	Data Availability Statement
476 477 478	The data used in this research are publicly available at the NSF Arctic Data Center: https://doi.org/10.18739/A24746T0K , and https://doi.org/10.18739/A2NV99C4P
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