

# A Novel Method to Quantify the Uncertainty Contribution of Aerosol-Radiative Interaction Factors

Bishuo He<sup>1</sup>, Chunsheng Zhao<sup>1</sup>

<sup>1</sup>Department of Atmospheric and oceanic sciences, School of Physics, Peking University, Beijing, 100080, China

5 *Correspondence to:* Chunsheng Zhao (zcs@pku.edu.com)

**Abstract.** The IPCC's assessment report shows that the radiative forcing of aerosol-radiation interactions still involves significant uncertainty. The commonly used method for factor uncertainty estimation is the One-at-A-Time (OAT) method, which evaluates factor sensitivity by controlling the change in a single variable while keeping others constant. The outcomes from the OAT method require high data quality to ensure accuracy, and the results are only valid near the selected constant.

10 This study proposes a new method called Constrained Parameter (CP) to quantify the uncertainty contribution of factors in a multi-factor system. This method constrains the uncertainty of a single factor between two Monte Carlo simulations and evaluates its sensitivity by analyzing how this change affects output uncertainty. The most significant advantage of the CP method is that it can be applied to any data distribution, and its results can reflect the overall data characteristics. The proportion of factor interactions in the factor uncertainty contributions can be obtained by comparing the results calculated  
15 by the CP method and the OAT method. As an application of the CP method, it performs a detailed analysis of aerosol-radiation interaction factors' uncertainty contributions. The top 3 most sensitive factors are the complex refractive index of aerosol shell materials, light-absorbing carbon parameters, and Mie theory parameters. Due to their high sensitivity and low observational precision, these factors represent significant sources of uncertainty in aerosol-radiation interactions. These factors need to be prioritized for operational observation programs and model parameter inputs.

## 20 1 Introduction

Aerosol-Radiation Interaction (ARI) refers to the direct scattering and absorption of solar radiation by aerosols, and it's a key component of aerosol radiative forcing that can have a significant influence on the climate system (IPCC, 2021). In recent years, numerous studies have focused on Radiative Forcing of ARI ( $RF_{ari}$ ) and its associated impacts. According to the Intergovernmental Panel on Climate Change (IPCC) Sixth Assessment Report (Forster et al., 2021), the estimated  $RF_{ari}$   
25 is  $-0.22[-0.47\sim0.04]\text{W/m}^2$ , a value comparable to the radiative forcing of  $\text{N}_2\text{O}$  at  $0.21[0.18\sim0.24]\text{W/m}^2$ , and second only to that of  $\text{CO}_2$  at  $2.16[1.90\sim2.41]\text{W/m}^2$ ,  $\text{CH}_4$  at  $0.54[0.43\sim0.65]\text{W/m}^2$ , and  $\text{O}_3$  at  $0.47[0.24\sim0.71]\text{W/m}^2$ . Despite the estimated  $RF_{ari}$  has undergone substantial revisions across successive IPCC reports, and its uncertainty has not notably decreased (Houghton, 1996; Houghton, 2001; Solomon, 2007; Stocker, 2014; Forster et al., 2021). Furthermore, significant discrepancies exist between  $RF_{ari}$  estimates derived from surface temperature changes and those from model simulations

30 (Anderson et al., 2003; Hansen et al., 2023), suggesting that the cooling effect of aerosols may be underestimated, potentially due to the omission of key factors in current models. To address these issues, it is crucial to conduct a thorough and precise uncertainty analysis of ARI factors and improve routine aerosol observation projects and model settings to better capture the contributions of critical factors.

The sensitivity of a factor can reflect the influence of the factor on the system output, and the product of the factor  
35 and the uncertainty of the factor itself can reflect the uncertainty contribution of the factor to the output to a certain extent. At present, research on assessing the uncertainty contributions of ARI factors has primarily focused on the sensitivity of these factors (McComiskey et al., 2008; Loeb and Su, 2010; Lee et al., 2011; Srivastava et al., 2011; Thorsen et al., 2020). The fundamental principle of this method is the control variable technique, wherein a perturbation  $dx$  is applied to a specific factor while other factors are held constant, and the resulting change in the output  $dy$  is observed.

40 The main advantage of the OAT evaluation method is its computational efficiency, as it requires only two experiments to determine the sensitivity of a factor, making it particularly suitable for large-scale ensemble models where computational costs are high. To ensure the accuracy of the sensitivity analysis results of the OAT method, two conditions must be met: (1) the covariance among the observed data of each factor must be zero; (2) the sensitivity results obtained are only valid near the selected constant value. For the ARI system, these conditions may not be strictly fulfilled, a discussion  
45 that will be elaborated upon in section 2. Several studies have enhanced evaluation methods to improve the credibility of results. These improvements include replacing satellite remote sensing data with more accurate AERONET global ground-based observation data (Thorsen et al., 2021) and utilizing Monte Carlo simulations to assess the impact of disturbances due to factor uncertainty on system output (Lee et al., 2016; Elsey et al., 2024). Proposing a new method that integrates these improvements to overcome the limitations of OAT analysis could lead to a more accurate understanding of ARI.

50 In addition to the possible errors caused by the evaluation method, the factors discussed in the current assessment work exhibit certain limitations. Due to limitations in observation methods, the evaluation models of ARI typically focus on aerosol optical parameters (AOPs), such as aerosol optical depth (AOD), single scattering albedo (SSA), and asymmetry factor ( $g$ ). Numerous studies have demonstrated that AOPs are the most direct factors influencing  $RF_{ari}$  (Andrews et al., 2006; McComiskey et al., 2008; Loeb and Su, 2010; Chung, 2012; Zhao et al., 2018). However, AOPs are significantly  
55 influenced by various aerosol and environmental parameters, which, in turn, indirectly affect  $RF_{ari}$  (Stock et al., 2011; Fierce et al., 2016; Kuang et al., 2016; Liu et al., 2017; Zhao et al., 2019a, 2021a; Zhao et al., 2021b, 2023). With the growing availability and accuracy of aerosol optical property observation methods, it is essential to analyze the uncertainty of these factors to more comprehensively assess and identify the sources of ARI uncertainty. The absence of a comprehensive evaluation may result in the underestimation of the importance of certain factors.

60 The uncertainty in  $RF_{ari}$  assessment results is also significantly influenced by the model used (Tosen et al., 2021). To reduce computational costs, large ensemble models often rely on numerous parameterization processes that simplify the physical mechanisms, which limits their ability to fully and accurately represent the ARI mechanism. Additionally, there can be considerable differences in model settings. When the IPCC conducts ensemble statistics on assessment results across

different models, the uncertainty may largely stem from discrepancies between the models themselves, leading to reduced accuracy in the conclusions. Therefore, a more effective approach would be to use a radiation mechanism model that more accurately captures the ARI physical processes to calculate  $RF_{ari}$  and conduct factor uncertainty contribution analysis.

This study proposes a new method for factor uncertainty contribution analysis, which employs Monte Carlo simulations to assess the contribution of various uncertainties. As a case study, field observation data on aerosol optical properties from North China are utilized, along with the radiation transfer model SBDART and the Mie theory model, to evaluate  $RF_{ari}$  and AOPs. The analysis examines the uncertainty contributions of aerosol and environmental parameter factors. The high-importance factors identified in the analysis should be prioritized in future routine observation efforts and model configurations to reduce uncertainty in the evaluation results. Section 2 provides a detailed introduction to the new method, while Section 3 presents the analysis results of  $RF_{ari}$  factor uncertainty contributions, along with a comparison to the results from the OAT method.

## 2 Analysis Method of Factor Uncertainty Contributions

This section will provide a comprehensive analysis of the most commonly used method for assessing factor uncertainty contributions through control variables. Additionally, it will introduce a new method for analyzing factor uncertainty contributions, aiming to address potential issues associated with the traditional control variable method.

### 2.1 OAT Method

For a multi-factor system, it can be expressed as

$$y = f(X), \quad (1)$$

Here,  $y$  represents the output variable, and  $X$  denotes the set of input variables, which can be expressed as:

$$X = [x_1, x_2, \dots, x_n]^T, \quad (2)$$

The superscript  $T$  denotes the transpose of the matrix. Given that interactions may exist between factors, the input variables satisfy the functional relationship  $g$  as follows:

$$x_i = g_i(X), \quad (3)$$

$$\frac{\partial x}{\partial x_i} = \left[ \frac{\partial g_1}{\partial x_i}, \frac{\partial g_2}{\partial x_i}, \dots, \frac{\partial g_n}{\partial x_i} \right]^T, \quad (4)$$

Taylor expansion of equation (1) gives:

$$f(X) = f(A) + [\nabla f(A)]^T (X - A) + \frac{1}{2!} [X - A]^T H(A) [X - A] + \dots, \quad (5)$$

Where  $A$  is a fixed value of  $X$ ,  $\nabla f(A)$  represents the first-order derivative of  $f(X)$  at  $A$ , and  $H(A)$  is the Hessian matrix of  $f(X)$  at  $A$ . As  $X$  approaches  $A$ , i.e., as  $X \rightarrow A$ , the higher-order terms beyond the second order tend to zero, satisfying:

$$f(X)_{X \rightarrow A} = f(A) + [\nabla f(A)]^T (X - A) + O^2, \quad (6)$$

If the  $X \rightarrow A$  condition cannot be met, the influence of the higher-order terms in the equation cannot be ignored. Taking the partial derivative of equation (6) concerning the input variable  $x_i$ , we obtain:

$$95 \quad \frac{\partial f(X)}{\partial x_i}_{X \rightarrow A} = \frac{\partial [\nabla f(A)]^T (X-A)}{\partial x_i} = \sum_{j=1}^n \frac{\partial f(A)}{\partial x_j} \frac{\partial g_j(X)}{\partial x_i}, \quad (7)$$

When the variables are independent of each other,

$$\frac{\partial g_j(X)}{\partial x_i} = 1, j = i, \quad (8)$$

$$\frac{\partial g_j(X)}{\partial x_i} = 0, j \neq i, \quad (9)$$

The sensitivity analysis results of the OAT method can be obtained

$$100 \quad S_{OAT} = \frac{\partial f(X)}{\partial x_i}_{X \rightarrow A} = \frac{\partial f(A)}{\partial x_i}, \quad (10)$$

There is a linear relationship between the output variable and all variables

$$y|X \rightarrow A = KX + C, \quad (11)$$

Where  $K = [\nabla f(A)]^T$ ,  $C = f(A) - A[\nabla f(A)]^T$ , and the uncertainty of each input variable and output variable has a transfer relationship

$$105 \quad D_{\sigma_y^2} = K^T D_{\sigma_{x_i}^2} K, \quad (12)$$

Here,  $\sigma_y$  and  $\sigma_{x_i}$  are the standard deviations of the output variable and each input variable, respectively, and  $D$  represents a diagonal matrix. Under these conditions, the uncertainty of the output can be decomposed into factor sensitivity and factor uncertainty, expressed as follows:

$$U_y^2 = \sum S_i^2 \times U_{x_i}^2, \quad (13)$$

110 When the variables are not independent, we have:

$$S_{OAT} - \frac{\partial f(A)}{\partial x_i} = \sum_{j=1, j \neq i}^n \frac{\partial f(A)}{\partial x_j} \frac{\partial g_j(X)}{\partial x_i}, \quad (14)$$

It can be concluded that the sensitivity analysis results obtained by the OAT method are valid only when:

- (1)  $X \rightarrow A$ ;
- (2) The variables are independent of each other.

115 When these two conditions are met, the analysis results of the OAT method can strictly reflect the sensitivity of the input variable  $x_i$  to the output  $y$ .

## 2.2 Applicability of OAT Method in ARI system

For the ARI system, meeting these two conditions is challenging for the following reasons:

- (1) In aerosol observations, inaccuracies in certain instruments or uncertainties arising from the inversion process of the joint observation system can lead to significant uncertainties in the generated observation data. As a result, the statistical average of the measurement results may not accurately reflect the true properties of aerosols. This discrepancy means

that there can be a considerable deviation between the calculated  $A$  value  $A_{cal}$  and the actual  $A$  value  $A_{real}$ , resulting in obtained results that are not entirely accurate.

- (2) Due to the influence of multiple factors, such as aerosol sources, aging processes, and changes in the atmospheric environment, it is essential to consider that the observed values of the physical and chemical properties of aerosols exhibit significant variability over time (e.g., diurnal, seasonal, and interannual changes) and space (e.g., coastal vs. inland, urban vs. rural, boundary layer vs. free atmosphere). This variability can lead to inhomogeneity in aerosol optical properties, resulting in trends or patterns in the observed data rather than a strict normal distribution. When using the OAT method for sensitivity analysis, the statistical mean may not accurately represent the data, thus introducing additional sources of error. To address this, it is necessary to first eliminate the influence of trends in the data. Overcoming this challenge requires analyzing the actual physical environment, which may involve additional time and computational costs.
- (3) For ARI, the interactions between factors are significant, and it is not feasible to assume that all the factors discussed are strictly independent. The covariance between the observed data may not be zero. When using the OAT method to analyze factor sensitivity, it is crucial to consider the relative magnitude of the covariance between the observed data of each factor. When the covariance between the data is large, applying a disturbance to one factor while holding the others constant does not reflect the actual physical situation, and thus fails to satisfy the strict conditions required for the OAT method. As a result, the final analysis may contain errors in the factor interaction terms.
- (4) The outcome of sensitivity analysis is to ascertain the uncertainty contribution of various factors. It is essential to perform separate statistical analyses on the sensitivity of these factors and observational uncertainty. To address the challenge of high uncertainty in the evaluation results of  $RF_{ari}$ , a more practical discussion should focus on how constraints imposed by observations, or improvements in observational accuracy, can enhance the reliability of the results. While sensitivity analysis does not directly answer this question, it offers valuable insights into the significance of each factor from a different perspective, guiding future efforts to reduce uncertainty.

In summary, when employing the OAT method to analyze factor sensitivity within the ARI system, there are strict requirements and numerous limitations regarding data quality. Forced application of this method may lead to discrepancies between the results and actual conditions. Besides the OAT method, various sensitivity analysis techniques have been widely utilized across many fields (Hamby, 1995; Christopher and Patil, 2002; Saltelli et al., 2005; Marino et al., 2008). Each of these methods also has specific requirements for data quality. Therefore, to enhance the reliability of the evaluation results for  $RF_{ari}$ , it is crucial to adopt a more suitable analysis method to assess the uncertainty contributions and significance of the influencing factors.

### 2.3 CP Method

Building on the history match method (Edwards et al., 2011; Williamson et al., 2013; Lee et al., 2016), this study introduces the Constrained Parameter (CP) method to quantitatively rank the uncertainty contributions of various factors. The central

155 concept of the CP method is to define the importance of a variable's uncertainty by constraining the value range of the input variable and observing how this constraint affects the standard deviation of the output variable. The specific analytical approach includes the following steps:

- (1) A Monte Carlo (MC) simulation is conducted on the system, where the range of each input parameter is determined based on the distribution of actual measurement results. The initial MC simulation allows for the exploration of all possible states of the system given the input variable distribution, enabling the calculation of the standard deviation  $\sigma_y$  of the output variable. To enhance the efficiency of the MC simulation, Latin Hypercube Sampling is employed for data sampling.
- (2) For a specific input variable, the distribution range is constrained, reducing its standard deviation from  $\sigma_x$  to  $\sigma_x'$ , while keeping the standard deviation of the other input variables unchanged. However, when the factors are not independent, constraining the distribution of one input variable may also alter the distributions of the other input variables.
- (3) Conduct another MC simulation using the updated range of input variables to obtain the new standard deviation  $\sigma_y'$  of the output variable.
- (4) The sensitivity of the input variable to the output variable is defined as:

$$S_{CP} = \frac{\sqrt{\sigma_y^2 - \sigma_y'^2}}{\sqrt{\sigma_x^2 - \sigma_x'^2}} = \frac{\sqrt{d\sigma_y^2}}{\sqrt{d\sigma_x^2}}, \quad (15)$$

170 Since only a specific input variable is constrained while the standard deviations of the distributions of the other input variables remain unchanged, the change in the distribution of the output variable is solely influenced by the alteration in the uncertainty of the constrained input variable. Therefore, the definition of  $S_{CP}$  is specifically related to the uncertainty of the data, and it can also be referred to as the sensitivity of uncertainty. This method is not limited to specific system equations and can be applied to all multi-factor systems.

175 When the factors are strictly independent of each other, the covariance between the observed data is equal to zero, which can be expressed mathematically as:

$$cov(x_i, x_j) = E(x_i x_j) - E(x_i)E(x_j) = 0, \quad (16)$$

Satisfying the error transfer formula, we obtain:

$$\sigma_y^2 = \frac{\partial f(X)^2}{\partial x_1^2} \cdot \sigma_{x_1}^2 + \dots + \frac{\partial f(X)^2}{\partial x_i^2} \cdot \sigma_{x_i}^2 + \dots + \frac{\partial f(X)^2}{\partial x_n^2} \cdot \sigma_{x_n}^2, \quad (17)$$

180 For the CP method, we can get

$$\sigma_y'^2 = \frac{\partial f(X)^2}{\partial x_1^2} \cdot \sigma_{x_1}^2 + \dots + \frac{\partial f(X)^2}{\partial x_i^2} \cdot \sigma_{x_i}'^2 + \dots + \frac{\partial f(X)^2}{\partial x_n^2} \cdot \sigma_{x_n}^2, \quad (18)$$

$$d\sigma_y^2 = \frac{\partial f(X)^2}{\partial x_i^2} \cdot d\sigma_{x_i}^2, \quad (19)$$

$$S_{CP} = \frac{\sqrt{d\sigma_y^2}}{\sqrt{d\sigma_x^2}} = \frac{\partial f(X)}{\partial x_i} = S_{OAT}, \quad (20)$$

Thus, when the factors are independent of one another, the sensitivity analysis results obtained using the CP method will align with those obtained through the OAT method. Consequently, the difference between the results of the CP method and the OAT method highlights the effects of factor interactions, providing insights into how these interactions may affect factor uncertainty contributions.

The advantages of the CP method are as follows:

- (1) To ensure accuracy, the OAT method must strictly satisfy the condition of  $X \rightarrow A$ , meaning that the sensitivity analysis results are only valid near the value of  $A$ . In contrast, the CP method examines the relationship between factor uncertainty and output uncertainty. The sensitivity results derived from this method reflect the overall data distribution rather than focusing on a specific fixed value. Consequently, the analysis results obtained from the CP method are more representative and applicable.
- (2) When the distribution of one factor is constrained, it influences the distributions of other interacting factors as well. Consequently, any changes to the constraints of the input variable will also lead to alterations in the distributions of these other variables. Different constraints include two categories: one is the difference in data distribution types, such as uniform distribution and normal distribution; the other is the difference in data standard deviation, which is reflected in different degrees of improvement in observation accuracy. As a result of this influence, the output distribution will be affected by the level of constraint applied to the factor, leading to different sensitivity outcomes. Therefore, the results of the CP method can reflect the impact of different data constraints on the uncertainty of the output, which cannot be reflected in the OAT method.
- (3) The analytical method is used to obtain the quantitative ranking results of factor uncertainty contributions, aiming to solve the problem of large output uncertainty by focusing on high-uncertainty contribution factors. The sensitivity analysis result  $S_{CP}$  illustrates the relationship between factor uncertainties and output uncertainties. The resulting ranking provides a direct response to this issue. The high uncertainty contribution factors identified by the CP method are essential elements in observation and model design that require our attention and enhancement. In contrast, the results from the OAT method represent statistical sensitivity concepts, serving as indirect indicators of factor uncertainty contributions, and lack robust physical grounding.

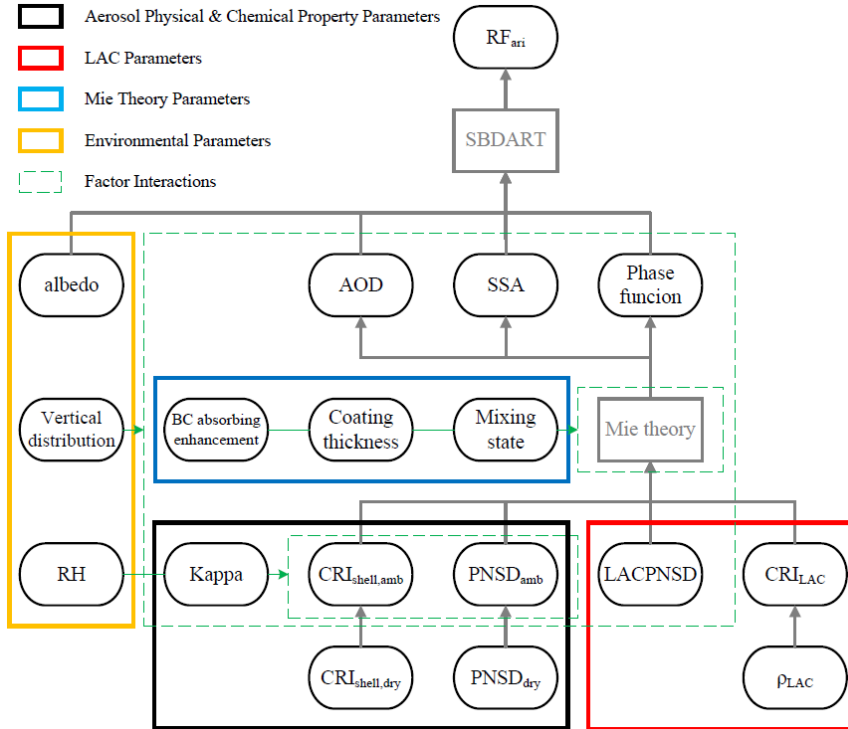
Therefore, the CP method is employed to quantify the contribution of factor uncertainty, and the results obtained offer a more accurate representation of each factor's importance in practical physical terms. This approach enhances our understanding of how various factors influence the overall uncertainty, enabling more informed decision-making in observation projects and model development.

### 3 Calculation of Uncertainty Contribution of $RF_{ari}$ Factors

In this section, the uncertainty analysis method proposed in this paper is applied to the ARI system to verify its feasibility. A detailed discussion is provided regarding the importance of each factor within the ARI system, highlighting how this method enhances our understanding of their contributions to overall uncertainty.

#### 3.1 Analysis of ARI Factors

Aerosol particles in the environment exhibit complex characteristics influenced by multiple factors. To effectively simulate the ARI system and minimize excessive parameterization, this study employs the radiative transfer mechanism model to calculate  $RF_{ari}$ . The model used is SBDART (Santa Barbara DISORT Atmospheric Radiative Transfer), developed by Ricchiazzi et al. (1998), which is capable of simulating and calculating radiation processes involving aerosols, the atmosphere, surfaces, clouds, and solar spectra. Additionally, the Mie theory (Mie, 1908) is utilized to characterize the radiative properties of individual aerosol particles, allowing for the calculation of aerosol optical parameters (AOPs) such as aerosol optical depth (AOD), single scattering albedo (SSA), and asymmetry factor (g). These parameters serve as a critical input for the SBDART model. The results of the factor analysis are presented in Figure 1.



**Figure 1: Analysis of ARI factors.**

In this analysis, we adopt a core-shell model assumption for aerosol particles, assuming that the core-shell composition is uniform. Specifically, the shell material is primarily composed of scattering materials, while the core consists



230 of light-absorbing carbon (LAC). The radiative characteristics of individual aerosol particles are determined by the complex refractive index of the core-shell material,  $CRI_{shell,dry}$ ,  $CRI_{LAC}$ , and the size of the core-shell particles. LAC is modeled as a combination of dense elemental carbon (EC) and hollow air (Zhao et al., 2020). By measuring the densities of EC and LAC, denoted as  $\rho_{EC}$  and  $\rho_{LAC}$ , we can calculate the complex refractive index of LAC through a weighted approach.

235 For a group of particles, it is essential to consider the size spectrum distribution of the aerosol particles and the LAC size spectrum distribution,  $PNSD_{dry}$  and  $LACPNSD$ , respectively, to perform weighted calculations of the radiative characteristics of the aerosol ensemble. Additionally, aerosol particles absorb moisture from the environment, influenced by the hygroscopic parameter ( $Kappa$ ) and the ambient relative humidity (RH). This moisture absorption leads to changes in the complex refractive index of the shell material,  $CRI_{shell,amb}$ , and alters the ambient particle size spectrum distribution,  $PNSD_{amb}$ .

240 The strict assumptions of Mie theory often diverge from real-world conditions, resulting in discrepancies between theoretical calculations and observed phenomena. Numerous studies have explored these discrepancies (Volten et al., 2001; Cappa et al., 2012; Fierce et al., 2016; Zhang et al., 2017; Freedman, 2020). To better understand the impact of these Mie theory assumptions on  $RF_{ari}$ , we will analyze the uncertainty contributions of several key factors, including the mixing state of aerosols ( $MS$ ), LAC absorbing enhancement ( $LACAE$ ), and coating thickness ( $CT$ ).

245 In the real atmospheric environment, aerosols and environmental parameters exhibit a vertical profile distribution, leading to significant variations in aerosol radiative capabilities at different altitudes. To investigate the impact of different vertical distribution types (VD) on  $RF_{ari}$ , we employ the vertical distribution parameterization scheme developed by Liu et al. (2009), which is grounded in aircraft observations. Using this scheme, we calculate the vertical distribution of  $PNSD_{amb}$  and  $LACPNSD$ . Additionally, the vertical distribution of environmental parameters is established based on reanalysis data.

250 According to the categories, all factors are divided into four categories:

- (1) Aerosol physical and chemical property parameters, including  $CRI_{shell,dry}$ ,  $PNSD_{dry}$ , and  $Kappa$ ;
- (2) LAC parameters, including the real part  $n_{LAC}$  and imaginary part  $k_{LAC}$  of  $CRI_{LAC}$ ,  $\rho_{LAC}$ , and  $LACPNSD$ ;
- (3) Mie theory parameters, including  $MS$ ,  $CT$ , and  $LACAE$ ;
- (4) Environmental parameters, including  $VD$ ,  $RH$ , and  $albedo$ .

255 The uncertainty contributions of the four types of factors are discussed separately to determine the type of factors with the strongest impact.

All the factors depicted in the Fig.1 influence  $RF_{ari}$ . We evaluate the uncertainty contributions of each factor using both the OAT method and the CP method, comparing the differences between the two approaches. Additionally, since AOD, SSA, and  $g$  are direct input parameters for SBDART and have the most immediate effects on  $RF_{ari}$ , we also discuss the sensitivity of each factor in relation to these AOPs.

260

3.2 Data Sources and Mode Environment Settings

In the simulation experiment, aerosol and environmental parameters are derived from a combination of field observations, previous research summaries, and instrument observation network data. Typical aerosol and environmental data representative of North China are utilized for the simulation. The calculation of  $RF_{ari}$  incorporates integrated results across the full solar spectrum (0.25–4.00  $\mu\text{m}$ ), focusing specifically on the instantaneous results at noon on the summer solstice. Aerosol data are sourced from the Peking University observation station (116°W, 40°N) and the Taizhou observation station (120°W, 33°N). Environmental data are drawn from the fifth-generation ECMWF reanalysis data (ERA5) provided by the European Centre for Medium-Range Weather Forecasts (ECMWF), as well as Moderate Resolution Imaging Spectroradiometer (MODIS) observation data collected from the Terra and Aqua satellites. The details are summarized in Table 1.

Properties	Values	Data Source
$CRI_{shell}$	$(1.58 \pm 0.2) + 1e^{-3}j$	Peking University Observation Site
$CRI_{LAC}$	$(1.67 \pm 0.36) + (0.67 \pm 0.35)j$	Zhao et al., 2020
$CRI_{EC}$	$2.26 + 1.26j$	Taylor et al., 2015
$CRI_{air}$	$1 + 1e^{-3}j$	Zhao et al., 2020
$\rho_{EC}$	1.8	Bond and Bergstrom, 2006
$\rho_{LAC}$	$0.95 \pm 0.3$	Zhao et al., 2019b
$Kappa$	$0.22 \pm 0.2$	Peking University Observation Site
$MS$	$0.7 \pm 0.3$	Gong et al., 2016
$PNSD_{dry}$	/	Taizhou Observation Site
$LACPNSD$	/	Taizhou Observation Site
$VD$	/	Liu et al., 2009
$RH$	/	ERA5 Data
$albedo$	/	MODIS Data
Location Settings	116° W, 40° N	/
Date Settings	April 1	/
Time Settings	12:00 local time	/

Table.1 Data sources and SBDART environment parameter settings. The aerosol optical properties represent urban-industrial aerosols observed in East Asia.

3.3 Quantitative Ranking Results of ARI Factor Uncertainty Contributions

The sensitivity analysis of the factors affecting  $RF_{ari}$  and AOPs was conducted using both the OAT method and the CP method. The results of this analysis are illustrated in Figure 2 and Figure 3.

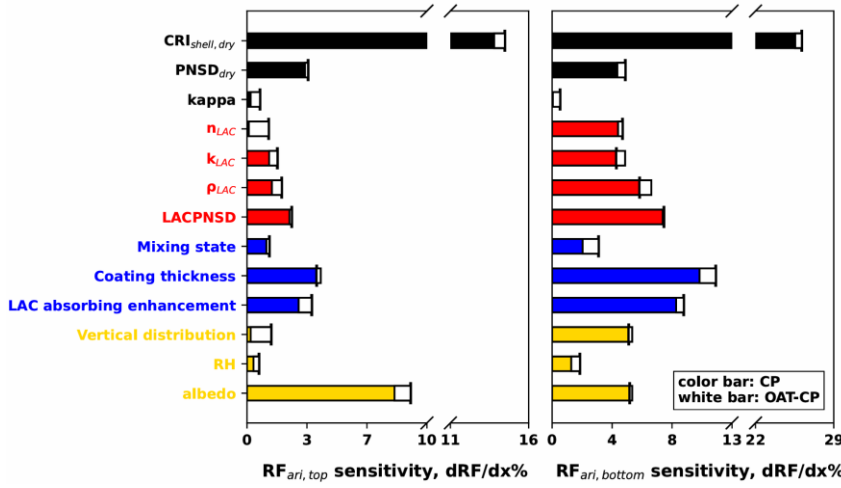


Figure 2: The factor uncertainty contribution analysis results of  $RF_{ari}$ . The results from the CP method are represented by color bars, while the differences between the CP method and the OAT method are indicated by white bars.

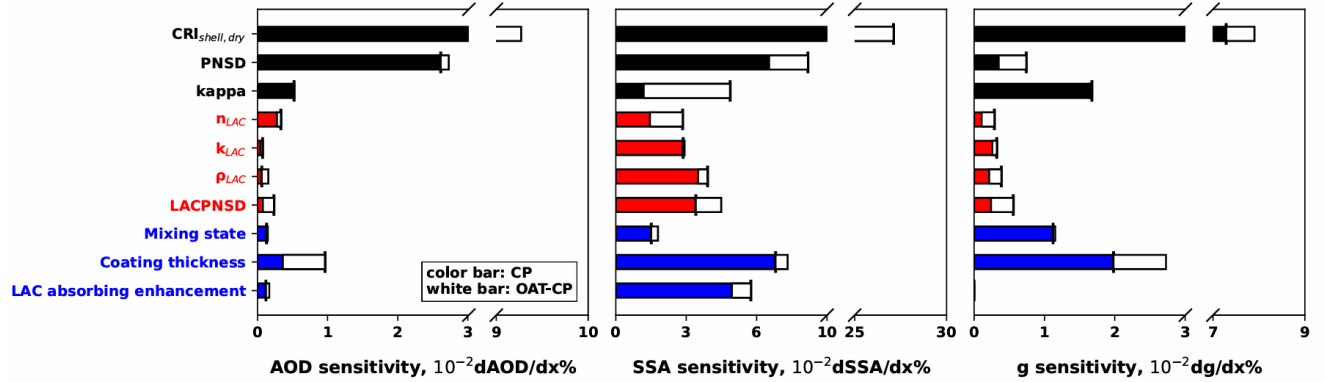


Figure 3: The factor uncertainty contribution analysis results of AOPs. The results from the CP method are represented by color bars, while the differences between the CP method and the OAT method are indicated by white bars.

### 3.3.1 ARI Factor Uncertainty Contribution Ranking Results

The results indicate that among the four parameter categories, the aerosol physical and chemical property parameters exhibit the most significant sensitivity. Specifically,  $CRI_{shell, dry}$  demonstrates the highest sensitivity across all five sensitivity analyses. Besides,  $PNSD_{dry}$  shows strong sensitivity to both AOD and SSA, while  $kappa$  exhibits pronounced sensitivity to g. When the core-shell structure model of the Mie theory is not considered, these three parameters sufficiently characterize the complex refractive index, particle number size distribution, and hygroscopic properties of aerosols. They are thus crucial for understanding the radiative forcing characteristics of aerosols.

The Mie theory parameters exhibit the second highest sensitivity. Due to the fact that changes in the aerosol mixing state can strongly influence both AOPs and  $RF_{ari}$ ,  $CT$  demonstrate significant sensitivity across all parameters. The  $LACAE$  primarily affects the aerosol's absorption characteristics, leading to strong sensitivity to SSA, which results in high sensitivity

to both  $RF_{ari,top}$  and  $RF_{ari,bottom}$ . Additionally,  $MS$  influence the ratio of LAC to coating materials, significantly affecting the shape of the aerosol particle number size distribution; consequently, it shows considerable sensitivity to  $g$ .

295 The sensitivity of LAC parameters ranks third. Specifically, the parameters  $n_{BC}$ ,  $k_{BC}$ , and  $\rho_{BC}$  influence the aerosol's CRI, while  $LACPNSD$  affects both the LAC particle size spectrum distribution and the aerosol mixing state. The results indicate that, as the primary absorptive component of aerosols, the complex refractive index of LAC significantly impacts aerosol absorption characteristics, leading to a pronounced effect on SSA. This, in turn, results in strong sensitivity of both  $RF_{ari,top}$  and  $RF_{ari,bottom}$ . Furthermore,  $LACPNSD$  exhibits the highest sensitivity among the LAC parameters, highlighting the substantial influence of the aerosol mixing state on  $RF_{ari}$ . Notably, the limited availability of observations  
300 for LAC parameters may contribute to considerable evaluation errors.

This study also examines the influence of environmental factors on  $RF_{ari,top}$  and  $RF_{ari,bottom}$ . Three environmental parameters are discussed:  $VD$ ,  $RH$ , and  $albedo$ . Among these, both  $RH$  and  $albedo$  demonstrate significant sensitivity to  $RF_{ari,top}$  and  $RF_{ari,bottom}$ . These environmental parameters effectively characterize the impact of boundary layer characteristics, vertical humidity profiles, and surface conditions on  $RF_{ari}$ . The results indicate that the effects of  
305 environmental factors on  $RF_{ari}$  are comparable to those of the aerosol's radiative characteristics and should not be overlooked in research calculations. Notably, the sensitivity of  $VD$  to radiative forcing differs markedly between the top of the atmosphere and the surface. While  $VD$  has minimal impact on  $RF_{ari,top}$ , it exhibits considerable sensitivity to  $RF_{ari,bottom}$ , suggesting that the type of boundary layer significantly influences surface heating rates but has a lesser effect on the overall ground-atmosphere radiation budget.

### 310 3.3.2 Comparison of Results between CP Method and OAT Method

The sensitivity analysis results indicate that the OAT method overlooks the impact of factor interactions, while the CP method accounts for these interactions. Consequently, the differences between the results from the two methods provide a measure of the influence of factor interactions on the sensitivity outcomes. In the analysis of  $RF_{ari,top}$  and  $RF_{ari,bottom}$ , the proportion of interaction effects ranges from 1.1% to 91%, with an average of 25%. After weighting according to sensitivity,  
315 the average difference is calculated to be 10%. For AOPs, the proportion of interactions varies from 0.33% to 386%, with an average of 56% and a weighted average of 25%. This variability suggests that different factors experience varying degrees of influence from interactions, with some factors significantly affected. Therefore, using the OAT method for sensitivity analysis may lead to an average relative error of 10% for  $RF_{ari}$  and 25% for AOPs, due to the neglect of factor interactions.

The CP method enables sensitivity analysis for data with varying degrees of factor constraints and non-normal  
320 distributions. The OAT method's sensitivity results are only valid near the chosen  $A$  value, meaning that changes in the  $A$  value may significantly impact the results. Additionally, the choice of  $dx$  in the  $\frac{dy}{dx}$  calculation can also influence outcomes. To explore these aspects, we computed results for the following seven sensitivity analysis cases:

- (1) Using the CP method, when the data is normally distributed, constrain the data distribution of a certain factor so that the standard deviation is reduced from  $\sigma_{x_i}$  to  $\sigma_{x_i}'$ , and perform sensitivity analysis;
- 325 (2) Using the CP method, when the data is normally distributed, constrain the data distribution of a certain factor so that the standard deviation is reduced from  $\sigma_{x_i}$  to  $2\sigma_{x_i}'$ , and perform sensitivity analysis;
- (3) Using the CP method, when the data is uniformly distributed, constrain the data distribution of a certain factor so that the standard deviation is reduced from  $\sigma_{x_i}$  to  $\sigma_{x_i}'$ , and perform sensitivity analysis;
- (4) Using the OAT method perform sensitivity analysis;
- 330 (5) Using the OAT method, set the  $A$  value as 0.9 times that of the case (4), and perform sensitivity analysis;
- (6) Using the OAT method, set the  $A$  value as 1.1 times that of the case (4), and perform sensitivity analysis;
- (7) Using the OAT method, set the  $dx$  value as 0.5 times that of the case (4), and perform sensitivity analysis;
- (8) Using the OAT method, set the  $dx$  value as 2 times that of the case (4), and perform sensitivity analysis.

A sensitivity analysis of  $RF_{ari,top}$  was performed on all the above situations, and the results are shown in Table 2.

	$CP_{normal-normal}$	$CP_{normal-normal}'$	$CP_{uniform-normal}$	$OAT$	$OAT_{0.9A}$	$OAT_{1.1A}$	$OAT_{0.5dx}$	$OAT_{2dx}$
$CRI_{shell,dry}$	14.8	15.7	14.6	14.2	8.90	19.3	14.9	14.08
$PNSD_{dry}$	3.31	4.49	4.41	3.15	3.20	3.05	3.20	3.15
$\kappa$	0.71	0.59	0.37	0.20	0.20	0.15	0.20	0.18
$n_{BC}$	1.17	1.19	1.20	0.10	0.30	0.10	0.40	0.20
$k_{BC}$	1.65	1.99	0.90	1.20	1.40	1.45	1.60	1.43
$\rho_{BC}$	1.88	1.60	1.46	1.35	1.70	1.50	0.80	1.60
$LACPNDS$	2.43	2.59	2.70	2.30	2.25	2.80	1.80	2.53
$MS$	1.22	1.81	1.47	1.05	0.55	1.05	1.10	0.80
$CT$	3.78	4.99	4.36	4.00	5.00	3.30	3.60	4.15
$LACAE$	3.51	3.25	2.62	2.80	2.80	3.30	2.30	3.05
$VP$	1.31	0.71	0.06	0.20	0.20	0.30	0.70	0.05
$RH$	0.65	0.81	0.43	0.35	0.35	0.35	0.30	0.35
$albedo$	8.87	8.24	8.50	8.00	8.15	8.35	7.90	8.25

335 **Table 2: Comparison of the analysis results of the CP method and the OAT method under different scenario settings.**

In cases (1) and (2), we varied the standard deviations of the constrained factors while applying the CP method, ensuring that the data distribution remained consistent. The analysis reveals a difference in results ranging from 1.7% to 48%, with an average difference of 21%. The weighted average calculated based on sensitivity is 14%. Under varying constraints, factors exert different influences on one another due to their interactions. Consequently, the final output is shaped not only  
340 by the constraints imposed on individual factors but also by these interactions, leading to differing sensitivity analysis results.

The results demonstrate that the CP method can accurately quantify how factors contribute to the reduction of output uncertainty under varying levels of observation accuracy improvement. In contrast, the OAT method overlooks the influence of factor interactions on the outcomes, making it incapable of performing differential analyses under different observation constraints, which represents a significant limitation.

345 In cases (1) and (3), we applied the CP method with save standard deviations of the factors before and after the constraints. However, the differing data distributions lead to a notable variation in analysis results, ranging from 1.3% to 95%, with an average difference of 15% and a weighted average of 4.9%. In scenarios where the volume of observational data is limited or influenced by external factors, the data cannot be guaranteed to be strictly normally distributed, and a linear trend may appear. The presence of this linear trend, identified through the CP method, can cause substantial variability among the factors, suggesting that the uncertainty contributions of certain factors are significantly influenced by the data distribution—an aspect not captured in the OAT method's analysis.

355 In cases (4), (5), and (6), we changed the selected  $A$  values for the OAT method vary from -10% to +10%. The differences in the analysis results vary from 0% to 50%, with an average difference of 22% and a weighted average difference of 20%. Some factors do not act linearly on the output, which makes the sensitivity analysis results of such factors highly dependent on the choice of  $A$  value. Consequently, even minor variations in the  $A$  value can result in significant errors. Therefore, when employing the OAT method for sensitivity analysis, careful attention must be given to the stability of the results.

360 In cases (4), (7), and (8), we changed the selected  $dx$  values in the OAT method range from -50% to +100%. The differences in the analysis results vary from 0% to 300%, with an average difference of 37% and a weighted average difference of 7.8%. The sensitivity analysis outcomes for certain factors are highly sensitive to the chosen  $dx$  value, and different strategies for selecting  $dx$  can result in varied analysis results. Mathematically, smaller  $dx$  values tend to provide a more accurate reflection of the actual sensitivity. However, in practice, the choice of  $dx$  is influenced by the model's accuracy and the distribution of actual observed data, necessitating certain trade-offs. This variability contributes to the stability issues observed in the analysis results produced by the OAT method.

365 A comprehensive comparison indicates that the CP method yields results that are representative of the entire data distribution. It effectively calculates differences in uncertainty contributions under various factor constraints and distinguishes between sensitivity results from non-normal and normal data distributions. In contrast, the OAT method provides results that are primarily relevant near a fixed value, and when data quality standards are not met, its results may exhibit poor stability.

## 370 4 Conclusions and Discussions

The evaluation results of  $RF_{ari}$  indicate significant uncertainty, with notable discrepancies between observational and simulation outcomes. This discrepancy contributes to the overall uncertainty in climate sensitivity assessments. This study

introduces a novel method for analyzing factor uncertainty contributions, enabling a quantitative ranking of the contributions from various factors and addressing the extent to which enhancing observational accuracy can reduce result uncertainty. Additionally, through a comprehensive analysis of the factors of the ARI system, this research identifies several previously overlooked factors of importance, providing valuable insights for aerosol observation projects and model settings.

This study analyzes the advantages and disadvantages of the OAT method, which is currently the most commonly used method in the ARI factor uncertainty contribution analysis. While the OAT method facilitates rapid quantification of factor sensitivity, it also brings the defects of high data quality requirements and poor stability. For ARI systems, the OAT method faces challenges due to the low accuracy of observational data, potential linear trends in the data distribution, and significant interactions among factors. Additionally, this method only provides sensitivity results close to fixed values, making it less reliable both mathematically and physically. As a result, the OAT method may produce substantial errors. To address these challenges, this study introduces a new analysis method, CP, designed for sensitivity analysis of both input and output uncertainties. This method is universally applicable to all multi-factor systems. Unlike traditional methods that focus on sensitivity near specific values, CP is based on collective data distribution, providing a more comprehensive representation. It directly addresses how improvements in data accuracy can enhance result certainty, offering practical insights. Additionally, CP can assess differences in factor uncertainty contributions under various observational constraints and with non-normally distributed data, broadening its applicability.

This study employs Mie theory to calculate the AOPs and utilizes the SBDART radiative transfer model to simulate  $RF_{ari}$ . The factors across all physical processes are categorized based on their modes of influence into four groups: aerosol physical and chemical property parameters, Mie theory parameters, LAC parameters, and environmental parameters. Each category undergoes a separate uncertainty contribution analysis. The results reveal that among all factors,  $CRI_{shell,dry}$  holds the highest importance. Additionally, both the LAC parameters and Mie theoretical parameters demonstrate high uncertainty contributions, indicating that the scattering and absorptive properties of aerosols, along with the assumptions inherent in Mie theory, substantially influence  $RF_{ari}$ . Due to the challenges associated with direct observation, these factors have been insufficiently addressed in routine observation projects and model settings. To mitigate the high uncertainty associated with  $RF_{ari}$  evaluations, it is imperative to focus attention on these critical factors.

The quantitative ranking results of factor uncertainty obtained in this study using the CP method are highly dependent on the model employed and the distribution of input aerosol optical property data. The more accurately the model describes the actual physical processes and the higher the precision of the aerosol optical property data, the closer the evaluation results from the CP method will align with observed values. Therefore, this study utilizes the Mie theoretical model and the SBDART radiation mechanism model, which provide a more accurate representation of the single-particle radiation process, along with field experimental data from direct observations of aerosol optical properties. This approach aims to minimize the uncertainty introduced by the model and data accuracy. Using different model frameworks or aerosol optical property data from polluted aerosols in cities outside of North China to conduct the same factor sensitivity analysis may yield significantly different results.

## **Code availability**

The code used in this study can be found at <https://github.com/sGhotHe/Code>.

## **Data Availability**

410 The data used in this study can be found at <https://github.com/sGhotHe/Data>.

## **Author Contribution**

Bishuo He: Data curation, formal analysis, investigation, methodology, resources, software, validation, visualization, writing – original draft preparation.

Chunsheng Zhao: Conceptualization, funding acquisition, project administration, supervision, writing – review & editing.

## **415 Competing Interests**

The authors declare that they have no conflict of interest.

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