

- Evaluating the accuracy of downwind methods for quantifying point source emissions
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Abstract. The accurate reporting of methane (CH₄) emissions from point sources, such as fugitive leaks from oil and gas infrastructure, is important for evaluating climate change impacts, assessing CH⁴ fees for regulatory programs, and validating methane intensity in differentiated gas programs. Currently, there are disagreements between emissions reported by different quantification techniques for the same sources. It has been suggested that downwind CH⁴ quantification methods using CH⁴ measurements on the fence-line of production facilities could be used to generate emission estimates from oil and gas operations at the site level, but it is currently unclear how accurate the quantified emissions are. To investigate model accuracy, this study uses fence-line simulated data collected during controlled release experiments as input for eddy covariance, aerodynamic flux gradient and the Gaussian plume inverse methods in a range of atmospheric conditions. The results show that both the eddy covariance and aerodynamic flux gradient methods underestimated emissions in all experiments. Although calculated emissions had significant uncertainty, the Gaussian plume inversion method performed better. The uncertainty was found to have no significant correlation with most measurement variables (i.e. downwind measurement distance, wind speed, atmospheric stability, or emission height), which indicates that the Gaussian method can randomly either underestimate or overestimate emissions. For eddy covariance, downwind measurement distance and percent error had negative correlation indicating that far away emissions sources were likely underestimated or be undetected. The study concludes that using fence-line measurement data as input to eddy covariance, aerodynamic flux gradient or Gaussian plume inverse 21 method to quantify CH_4 emissions from an oil and gas production site is unlikely to generate representative emission estimates.

1 Introduction

 Methane (CH4), the primary component of natural gas (NG), is a potent greenhouse gas with a global warming 25 potential of 27 carbon dioxide ($CO₂$) equivalent over 100 years (US EPA, 2016). Methane emissions reduction is a key part of global initiatives to reduce climate change (Chung, 2021). The 2021 Global Methane Assessment by the Climate and Clean Air Coalitions (CCAC, 2024) and the United Nations Environment Programme (UN Environment Programme, 2024) state that reducing CH⁴ emissions from anthropogenic sources by 45% in 2030 would result in 29 avoiding a global atmospheric temperature increase of 0.3° C in 2045 (Chung, 2021). Such measures would align with the Paris Agreement goal of limiting global temperature rise to 1.5˚C by 2030 (United Nations Climate Change, 2015). The US is one of the countries that reports its total greenhouse gas emissions to the Intergovernmental Panel on Climate Change as part of the Paris Agreement (United Nations Climate Change, 2015). Currently, the amount of CH⁴ emitted from US oil and gas production is calculated by the US Environmental

Protection Agency (EPA) using a bottom-up inventory approach. The inventory approach multiplies emission factors

 (CH⁴ emissions per equipment e.g., separator or emissions per event e.g., liquid unloading) by activity factors (total number of pieces of equipment or events (OAR US EPA, 2023)). This quantification approach has several shortcomings, including: 1. It separately calculates CH⁴ emissions from natural gas and petroleum systems, which practically are not independent systems, and can result in bias based on changes in gas to oil ratios throughout a basin (Riddick et al., 2024a); 2. Some emission factors used are outdated (Riddick et al., 2024b) and others do not account for the temporal and spatial variation in emissions (Riddick and Mauzerall, 2023); and 3. Emission factors do not account for the long-tail distributions in emissions distributions (Riddick et al., 2024b). Recently, mechanistic models, such as the Colorado State University's Mechanistic Air Emissions Simulator (MAES), have been developed to address shortcomings in bottom-up CH⁴ reporting (Colorado State University, 2021) but these still depend on direct measurements to inform emission factors. Top-down methods, including using aircraft and satellites, can also be used to infer emissions. For example, Carbon Mapper satellites can locate and quantify CH⁴ emissions using absorption spectra taken from space (Carbon Mapper, 2024). However, these survey methods only quantify emissions over a very short period of time (< 10 s) and observations are typically made during the day which can often coincide with maintenance activities that can bias emissions and result in overestimation (Riddick et al., 2024a; Zimmerle et al., 2024). Additionally, different top-down technologies measuring the same source have disagreed in their reported emissions which has called into question the credibility of these methods (Brown et al., 2023; Conrad et al., 2023). As a result, ensuring accuracy in models and technologies used in CH⁴ emissions quantification has been a complex issue. The accurate reporting of CH⁴ from fugitive emissions at oil and gas production sites is important for evaluating potential effects on climate change, correctly assessing CH⁴ fees on companies as part of the Methane Emissions 55 Reduction Program created under the 2022 Inflation Reduction Act (OA US EPA, 2023), and validating CH₄ content of reported differentiated gas composition where NG companies differentiate their market products based on the environmental impact (CO2EFFICIENT, 2022). Direct measurements have been recommended to augment/update emissions factors used in bottom-up inventories and for better understanding temporal/spatial variability of emissions (Riddick et al., 2024). Downwind methods are widely used to directly measure CH⁴ emissions from area and point sources at site/basin levels due to their low cost and wide coverage within a short time (Caulton et al., 2018; Heimburger et al., 2017; Riddick et al., 2020, 2022a; Sonderfeld et al., 2017). Commonly used downwind quantification methods include the Gaussian plume inversion method, eddy covariance, backward Lagrangian stochastic models, aerodynamic flux gradient, mass balance method, the EPA Other Test Method (OTM 33) and the Gaussian puff modelling approach (Denmead, 2008; Edie et al., 2020; Foster-Wittig et al., 2015; Jia et al., 2023; Kamp et al., 2020; Nemitz et al., 2018; Shaw et al., 2021). Currently, fence-line methods are used to detect, localize and quantify emissions. This approach uses point sensors fixed to the fence-line of the production site and emissions detected when the measured concentration exceeds a threshold, localized by triangulating multiple detections and quantified using a simple dispersion modelling

- framework, usually based on a Gaussian plume approach (Bell et al., 2023; Day et al., 2024; Jia et al., 2023; Riddick
- et al., 2022a). The detection and localization of simulated fugitive emission have been successful, with controlled
- release testing against point sensors and scanning/imaging solutions reporting a 90% probability of detection for

- 72 emission of between 3.9 and 18.2 kg CH₄ h⁻¹ (Ilonze et al., 2024). Major shortcomings have been identified using a 73 fence-line approach with quantified emissions reported at between a factor of 0.2 to 42 times for emissions between 74 0.1 and 1 kg CH₄ h⁻¹, and between 0.08 and 18 times for emissions greater than 1 kg CH₄ h⁻¹ (Ilonze et al., 2024). As 75 a result, questions have arisen if other approaches, such as the eddy covariance or aerodynamic flux gradient would 76 generate more accurate results. These methods have been suggested as they have been used to quantify emissions 77 from other sectors, i.e. agriculture (Denmead, 2008; Morin, 2019) and landfills (Xu et al., 2014), have been used to 78 quantify emissions in large downwind areas (Vogel et al., 2024), and quantification does not require assumptions 79 made on downwind dispersion coefficients or micrometeorology that are often required for dispersion modelling 80 (Denmead, 2008). 81 Due to interest in using a subset of these methods to quantify emissions from oil and production sites, this study will 82 evaluate the quantification accuracy of the eddy covariance, aerodynamic flux gradient, and Gaussian plume inverse 83 methods. Eddy covariance is a vertical flux gradient measurement that measures CH₄ emissions based on the 84 covariance between CH_4 concentrations measured using a fast-response analyzer (> 10 Hz) and vertical wind vector 85 measured by a fast-response sonic anemometer (>10 Hz) (Figure 1A; Morin, 2019). It is typically implemented over 86 long homogenous fetches where eddy mixing scale is a small fraction of the distance from the site providing more 87 predictable vertical transport. The aerodynamic flux gradient method quantifies CH₄ emissions from a source by 88 comparing CH₄ concentrations at two heights (Figure 1B; Querino et al., 2011). The Gaussian Plume Inverse method 89 calculates CH₄ mole fraction at a point in space (x, y, z) as a function of the downwind distance, perpendicular distance 90 (crosswind), mean wind speed and atmospheric stability (Jia et al., 2023; Riddick et al., 2022b). These approaches 91 were developed to quantify emissions from single-point or area emission sources and have not been tested against a 92 controlled release to evaluate their quantification performance. The aerodynamic flux gradient and eddy covariance, 93 for example, have been used to measure trace gas, e.g., nitrogen oxide and carbon dioxide, fluxes from large croplands 94 (Kamp et al., 2020).
	- \overline{A} B **Eddy Covariance Aerodynamic Flux Gradient** Negative flux Negative flux Positive flux Positive flux (absorption/deposition) (absorption/deposition) $CH₄$ & vertical wind (w) (emission) (emission) measurement Wind $(z2)$ CH₄ & atmospheric $CH₄1$ $CH₄2$ stability (L) at z2 w1 w2] $CH₄1$ $CH₄2$ Wind $(z1)$ CH₄ & atmospheric stability (L) at z1 Vegetation /egetation

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96 Figure 1: Illustrations of eddy covariance (A) and flux gradient measurements (B) where CH₄ is methane concentrations, w is the vertical wind speed, L is the Monin-Obukhov length (measure of atmospheric stability), 97 concentrations, *w* is the vertical wind speed, *L* is the Monin-Obukhov length (measure of atmospheric stability), and z is the measurement height.

- 99 The Gaussian plume inversion method has been used to quantify emissions from oil and gas production sites (Caulton
- 100 et al., 2014; Riddick et al., 2022b) but it assumes a homogenous, steady state flow, uniform dispersion of gas in an

z is the measurement height.

- open area free of obstructions (Hutchinson et al., 2017). Oil and gas emissions are characterized by intermittent, non-uniform, single or multiple point source emissions, varying in leak size, location, height and distance between the
- 103 source and sensor, and are typically in complex aerodynamic environments (i.e. not flat). The need for accurate CH₄
- quantification and reporting necessitates evaluating the performance of these downwind quantification approaches in
- different controlled release and characterized meteorological conditions, to ensure credibility.
- This study aims to investigate the performance of these methods in quantifying emissions for known gas release rates
- and evaluating uncertainties that could result in incorrect CH⁴ reporting. Specifically, the study will (1) evaluate the
- overall quantification accuracy of eddy covariance, aerodynamic flux gradient, and the Gaussian plume inverse
- method in quantifying single-point and multi-point emissions that simulate oil and gas emissions, (2) evaluate the
- probability of these models quantifying within a defined range (i.e. ±30%), and (3) investigate which variables have
- 111 the largest effect on quantification uncertainty.

2 Methods

2.1 Experimental Setup

Controlled release experiments were conducted at the Colorado State University's Methane Emissions Technology

- Evaluation Center (METEC) in Fort Collins, CO, USA, between February 8, and March 27, 2024. The weather
- conditions during the test period were mostly sunny but precipitation was also observed (32 sunny, 7 snowy, 12 rainy,
- 117 7 cloudy and 1 foggy day; Supplementary Information Section 1). Wind speeds were between 0 and 25 m s⁻¹ and
- temperatures ranged between -15 and +19 °C (Supplementary Information Section 1). Two stationary masts holding
- the instrumentation were setup on the North-West corner of METEC to take advantage of the predominant wind
- direction, avoid the largest aerodynamic obstructions and to simulate the likely placement of a fence line instrument
- (Figure 2; Day et al., 2024; Riddick et al., 2022a). Fenceline sensors are typically placed within the oil and gas
- perimeter (~30 m) (Riddick et al., 2022a). This study collected data for both close and far away releases, distances
- between 9 and 94 m.

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Figure 2: Left pane: Map illustration of major pieces of equipment and the measurements points at Colorado State
126 University's Methane Emissions Technology Evaluation Center (METEC) in Fort Collins, CO, USA. 4S denotes University's Methane Emissions Technology Evaluation Center (METEC) in Fort Collins, CO, USA. 4S denotes the location of horizontal separators, 4W are well heads, 4T are tanks, 5S are vertical separators and 5W are well heads. 128 1 is the measurement point for the Microportable Greenhouse Gas Analyzer and 2 is the measurement point for the 129 Aeris analyzers. The red dotted lines with yellow numbers show the average distances (meters) between 129 Aeris analyzers. The red dotted lines with yellow numbers show the average distances (meters) between emission 130 equipment and measurement points. Right pane: Image of METEC showing relative heights of equipment ("ME 130 equipment and measurement points. Right pane: Image of METEC showing relative heights of equipment ("METEC 131 | Colorado State University." 2024). | Colorado State University," 2024).

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To calculate emissions using the aerodynamic flux gradient approach, two sampling inlets were mounted at 2 and 4

134 m heights on mast 2 and connected to the inlets of two Aeris (Hayward, CA, USA) MIRA Ultra Series analyzers

135 (Figure 3A). The analyzers were housed in a temperature-controlled unit and sampled at 5 Hz. Data from the 2 m

136 analyzer were also used as input for the Gaussian Plume Inverse method analysis. To collect CH⁴ concentration data

137 for the eddy covariance method, the inlet tubing of the ABB (Zurich, Switzerland) GLA131 Series Microportable

138 Greenhouse Gas Analyzer (MGGA) sampling at 10 Hz was collocated with an R. M. Young (Traverse City, MI, USA)

139 81000 sonic anemometer (R.M. Young Company, 2023) which measured micrometeorology at 10 Hz, 3 m height

140 above ground level on mast 1 (Figure 3B).

143 Figure 3: A is the aerodynamic flux gradient and Gaussian plume inverse sampling points and B is the eddy covariance 144 sampling point. The two sampling points are 9.4 m apart. sampling point. The two sampling points are 9.4 m apart.

2.2 Controlled Methane Releases

eddy covariance the raw CH4 10 Hz data was used. The aggregated meteorological-concentration data were then

- merged with METEC's release data and metadata, and event tables created. The meteorological-concentration-release
- event data were then separated into single-point and multi-point events. The event tables were split into 20-minute
- emission events for aerodynamic flux gradient and Gaussian plume inverse method as they are dependent on
- atmospheric stability that is typically determined in time durations of 15 to 30 minutes. Shorter duration measurements
- (i.e. <15 minutes) may not represent the mean atmospheric state, while longer periods (> 30 minutes) may cause errors
- especially during rapid transitions in weather conditions (Crenna, 2006). 30-minute events were used for eddy

- 164 covariance processing following published typical averaging times of eddy covariance measurements (Nemitz et al.,
- 165 2018), and its quantification is assumed to be independent of atmospheric stability (Denmead, 2008).
- 166 For eddy covariance and aerodynamic flux gradient, Monin-Obukhov length (*L*) was calculated as the measure of
- 167 atmospheric stability for every 20 or 30-minute time period, depending on the method, using output from the sonic
- anemometer. *L* was calculated from the surface friction velocity (*u**, m s-1 168), mean potential temperature (*Θ*, K), von
- 169 Kármán's constant (*k*, 0.41), gravitational acceleration (*g*, 9.8 m s⁻¹) and the surface (kinematic) turbulent flux of
- 170 sensible heat w'Θ' (Eq. 1 and 2) (Kljun et al., 2015; Stull, 1988).

$$
L = -\frac{u_*^3 \theta}{k_v g \overline{w' \theta'}}
$$
 (1)

171

$$
u_* = \left[\left(\overline{u'w'} \right)^2 + \left(\overline{v'w'} \right)^2 \right]^{1/4} \tag{2}
$$

 For the Gaussian method, atmospheric stability was calculated based on the EPA standard operating procedure for point source Gaussian method (US EPA, 2013). The average local wind stability class (*pgi*) was calculated as the average of atmospheric stability determined using the standard deviation of the wind direction, and the stability calculated from turbulent intensity (ratio of the standard deviation of the wind speed to the average wind speed). The dispersion coefficients used for Gaussian quantification were extracted from the EPA operating procedure that provided coefficients for distances ranging from 1 to 200 m from source (US EPA, 2013). The wind direction (*WD*) and speed (*WS*) were calculated from the wind vectors u and v, based on the manufacturer's

179 configuration: $+u$ values = wind from the east, $+v$ values = wind from the north, and $+w =$ updraft (Eq. 3 and 4). 180

$$
WD = \text{mod}(90 - \text{atan2d}(v, u), 360) \tag{3}
$$

$$
WS = \sqrt{u^2 + v^2} \tag{4}
$$

 The bearing of each release point to the masts' location was calculated using the latitudes and longitudes of the release 182 points provided in the METEC metadata. This bearing was used to determine when the masts were downwind of the release points during the 20/30-minute period. The models' quantification accuracies were tested in three downwind 184 ranges: $\pm 10^\circ$, $\pm 20^\circ$, and $\pm 30^\circ$. A mast was considered downwind when the wind direction was within the specified range for 30% of the 20/30-minute duration. Results for the 20-degree range are presented in the Results section, while the 10- and 30-degree results are included in the Supplementary Material. The 30% threshold was chosen to ensure sufficient data points for evaluating the models. The data were categorized into single release single emission (single emission at the site and the mast was downwind of the release point), multi release single emission (multiple emissions at the site level, but the mast was downwind of a single release point), and multi release multi emission (multiple emissions at the site level, but the mast was downwind of more than one release point).

191 **2.4 Methane Emissions Quantification**

192 **2.4.1 Background Concentration**

 Background concentration was determined for each of the sensors to calculate CH⁴ enhancement. Due to inherent variation in sensors that were used in this study, CH⁴ background was calculated for each sensor separately. CH⁴ 195 background was calculated as the average of the lowest $5th$ percentile of all continuous concentration readings (US EPA, 2013). Methane enhancement was determined as CH⁴ concentration measurement minus the background concentration measurement.

198 **2.4.2 Eddy Covariance**

- 199 Emissions were quantified using the eddy covariance method for all three emissions scenarios (single release single
- 200 emission, multi release single emission and multi release multi emission). Methane flux $(F, \text{kg m}^2 \text{ s}^1)$ was calculated
- 201 as the covariance between the vertical wind speed $(w, m s⁻¹)$ and CH₄ enhancement $(c, g m⁻³)$ over 30 minutes (Eq. 5;
- 202 Denmead, 2008).

$$
F = w'c'
$$
 (5)

203 **2.4.3 Aerodynamic Flux Gradient**

204 Cherodynamic flux gradient quantification was also tested in all three cases. Methane flux $(F, \text{kg m}^2 \text{s}^{-1})$ was calculated 205 based on surface friction velocity (u ^{*}, m s⁻¹), von Kármán's constant (k ^v, 0.41), the difference in the average CH₄ 206 enhancement between the higher and lower height $(g, m⁻³)$, natural log of the higher and lower height, and stability 207 correction factors *Ψ* (Eq. 6; Denmead, 2008; Kamp et al., 2020).

$$
F = \frac{u_* k_v (c_2 - c_1)}{\ln \left(\frac{z_2}{z_1}\right) - \Psi_{c,2} + \Psi_{c,1}}
$$
(6)

208 **2.4.4 Determining the Area of Vertical Flux Contribution**

209 Eddy covariance and aerodynamic flux gradient measurements at a point $(0, 0, z)$ generate vertical fluxes in kg m⁻² s⁻ \quad $\,$ In this study, these fluxes represent emissions from single-point or multi-point sources distributed over an area (m²). The Kljun et al. (2015) footprint model, was used to calculate footprint, and determine the area that contributed 80% (r = 80, $10 \le r \le 90$) of the vertical flux measured by the eddy covariance and aerodynamic flux gradient systems. In previous studies, 80% footprints have been used due to the difficulty of reproducing 90% of the sources under neutral and stable conditions, where footprints tend to be long. The difference between the 80% and 90% contours is typically excessively large, despite minimal flux contributions in that area (Rey-Sanchez et al., 2022). The Kljun et al. (2015) 216 model calculates footprint as a function of effective height $(z_m =$ sensor height (z) – displacement height (m)), 217 roughness length (z_0, m) / mean wind speed $(u_{mean}, m s^{-1}$ - used in this study), height of the boundary layer (h, m) , 218 Obukhov length (*L*, m), standard deviation of the lateral velocity (σ_v , m s⁻¹), and friction velocity (u^* , m s⁻¹) (Kljun et al., 2015). The roughness sublayer in the model was set to 1 (footprint is calculated even if *z^m* is within the roughness layer). The area of vertical flux contribution was calculated as the polygon area covered by the contour. Due to the limitations of the flux footprint model for the measurement height and stability (Kljun et al., 2015), 20/30-minute files 222 flagged by the footprint model when $z_m/L < -15.5$, were excluded from further analysis.

223 **2.4.5 Gaussian Plume Inverse Method**

224 The Gaussian plume inverse method was used to quantify single release single emission and multi release single 225 emission. The quantified emission $(Q, kg h^{-1})$ was calculated from the CH₄ enhancement $(X, g m^{-3})$, wind speed (u, m) 226 s⁻¹), horizontal dispersion coefficient (σ_y , m), vertical dispersion coefficient (σ_z , m), crosswind distance (*y*, m),

227 sampling height (*z*, m), emission height (*hs*, m), and the height of the boundary layer (Equation 7; Riddick et al., 228 2022b).

$$
X(x,y,z) = \frac{0}{2\pi u \sigma_y \sigma_z} e^{-\frac{y^2}{2\sigma_y^2}} \left(e^{-\frac{(z-hs)^2}{2\sigma_z^2}} + e^{-\frac{-(z+hs)^2}{2\sigma_z^2}} + e^{-\frac{-(z-2h+hs)^2}{2\sigma_z^2}} + e^{-\frac{-(z+2h-hs)^2}{2\sigma_z^2}} + e^{-\frac{-(z-2h-hs)^2}{2\sigma_z^2}}\right)
$$
(7)

229 **3 Results**

230 **3.1 Methane Emission Quantification**

231 **3.1.1 Eddy Covariance**

232 For stable, continuous 30-minute release events, emissions calculated using the eddy covariance method were an

233 underestimate for single release single emission, multi release single emission and multi release multi emission events

234 (Figure 4). All data points were below the 1:1 line. A plot of the quantified emission versus controlled release (kg h⁻

235 \rightarrow 1) did not show a linear correlation (R² between 0.03 and 0.36), as all emissions were largely underestimated. The

236 eddy covariance method reported emissions of between 0 and 0.5 kg h^{-1} overall, despite actual emissions being

237 between 0 and about 7 kg h⁻¹ (Figure 4). The underestimation was consistent across all downwind ranges, 10, 20 and

238 30 degrees (Supplementary Material Section 2.1).

239

240 Figure 4*:* Quantified emission calculated using the eddy covariance method. Left pane shows a scatter plot of 241 quantified emission versus total controlled release for a single release at the site level and the mast 241 quantified emission versus total controlled release for a single release at the site level and the mast was downwind of 242 the release point. Center pane shows a scatter plot of quantified emission versus total contro 242 the release point. Center pane shows a scatter plot of quantified emission versus total controlled release for multiple releases at the site level, but the mast was downwind of a single release point. Right pane shows 243 releases at the site level, but the mast was downwind of a single release point. Right pane shows a scatter plot of 244 quantified emission versus total controlled release for multiple releases at the site level and th 244 quantified emission versus total controlled release for multiple releases at the site level and the mast was downwind 245 of more than one release point. The dashed line represents the 1:1 line (points below the line w 245 of more than one release point. The dashed line represents the 1:1 line (points below the line were underestimated), 246 the red line is the linear regression fit of the data, and n is the number of data points. the red line is the linear regression fit of the data, and n is the number of data points.

247 **3.1.2 Aerodynamic Flux Gradient**

248 The aerodynamic flux gradient method also largely underestimated emissions for single release single emission, multi 249 release single emission and multi release multi emission (Figure 5). A plot of quantified emission versus actual release 250 did not show a linear relationship (R^2 between 0.01 and 0.39), and most data points were below the 1:1 line (Figure 251 $\,$ 5). The aerodynamic flux gradient quantified emissions were between 0 and about 1.6 kg h⁻¹ despite actual emissions 252 being between 0 and about 7 kg h⁻¹ (Figure 5). The underestimation was also consistent across all downwind ranges,

253 10, 20 and 30 degrees (Supplementary Material Section 2.2).

254

255 Figure 5*:* Quantified emission calculated using the aerodynamic flux gradient method. Left pane shows a scatter plot 256 of quantified emission versus total controlled release for a single release at the site level and the mast was downwind
257 of the release point. Center pane shows a scatter plot of quantified emission versus total con 257 of the release point. Center pane shows a scatter plot of quantified emission versus total controlled release for multiple releases at the site level, but the mast was downwind of a single release point. Right pane sho 258 multiple releases at the site level, but the mast was downwind of a single release point. Right pane shows a scatter 259 plot of quantified emission versus total controlled release for multiple releases at the site lev 259 plot of quantified emission versus total controlled release for multiple releases at the site level and the mast was 260 downwind of more than one release point. The dashed line represents the 1:1 line (points below th 260 downwind of more than one release point. The dashed line represents the 1:1 line (points below the line were 261 underestimated), the red line is the linear regression fit of the data, and n is the number of data point 261 underestimated), the red line is the linear regression fit of the data, and n is the number of data points.

262 **3.1.3 Gaussian Plume Inverse Method**

 The Gaussian plume inverse method was tested for single release single emission and multi release single emission as the method is only used for single-point sources and preliminary results showed the method provided reasonable results within 20 degrees downwind range (Figure 6; Supplementary Material Section 1.3). For single release single emission, the method quantified emissions within a factor of 1.5 (Figure 6) and showed reasonably linear relationship $267 \text{ (R}^2 \text{ of } 0.65)$ (Figure 6). For multi release single emission, the gradient (m) of the linear regression was 0.95 and R^2 of 0.21. This suggests that the linear relationship cannot be well explained due to a random scatter of calculated emissions.

271 Figure 6: Quantified emission calculated using the Gaussian plume inverse method. Left pane shows a scatter plot of 272 quantified emission versus total controlled release for a single release at the site level and the 272 quantified emission versus total controlled release for a single release at the site level and the mast was downwind of the release point. Right pane shows a scatter plot of quantified emission versus total controlled 273 the release point. Right pane shows a scatter plot of quantified emission versus total controlled release for multiple
274 releases at the site level, but the mast was downwind of a single release point. The dashed lin 274 releases at the site level, but the mast was downwind of a single release point. The dashed line represents the 1:1 line 275 (points below the line were underestimated), the red line is the linear regression fit of the 275 (points below the line were underestimated), the red line is the linear regression fit of the data, and n is the number 276 of data points. of data points.

277 **3.2 Quantification within 30% Uncertainty**

278 **3.2.1 Eddy Covariance**

279 The eddy covariance method showed a very low probability of quantifying emissions within 30% uncertainty $(\pm 30%)$

280 (Figure 7). Only a single measurement in the multi release multi emission category showed an approximately 0.01

281 probability of quantifying within 30% (Figure 7). The errors for eddy covariance were between -100 and -86% for

282 single release single emission, between -100 and -82% for multi release single emission, and between -100 and about

283 +30% for multi release multi emission (Figure 7). This shows that using eddy covariance to quantify single-point and

284 multi-point emissions will largely underestimate emissions.

286 Figure 7: Cumulative distribution function (cdf) of percent errors for eddy covariance. Left pane shows a cdf plot for 287 a single release at the site level and the mast was downwind of the release point. Center pane 287 a single release at the site level and the mast was downwind of the release point. Center pane shows a cdf for 288 multiple releases at the site level, but the mast was downwind of a single release point. Right pane sh 288 multiple releases at the site level, but the mast was downwind of a single release point. Right pane shows a cdf for 289 multiple releases at the site level and the mast was downwind of more than one release point. The 289 multiple releases at the site level and the mast was downwind of more than one release point. The area bounded by 290 the red dotted line shows the region within ± 30 uncertainty. the red dotted line shows the region within ± 30 uncertainty.

3.2.2 Aerodynamic Flux Gradient

 The aerodynamic flux gradient also showed a very low probability of quantifying within 30% uncertainty (Figure 8). In the multi release single emission category results indicate a 0.02 probability of quantifying within 30% (Figure 8) of the true value. The errors for aerodynamic flux gradient were between -100 and -60% for single release single emission, between -100 and 0% for multi release single emission, and between -100 and -70% for multi release multi emission (Figure 8). These data show that the aerodynamic flux gradient will underestimate a point emission. Similar to eddy covariance, quantifying an emission within 30% uncertainty using aerodynamic flux gradient for point sources is highly unlikely.

302 shows a cdf for multiple releases at the site level, but the mast was downwind of a single release point. Right pane
303 shows a cdf for multiple releases at the site level and the mast was downwind of more than one re 303 shows a cdf for multiple releases at the site level and the mast was downwind of more than one release point. The area bounded by the red dotted line shows the region within ± 30 uncertainty. area bounded by the red dotted line shows the region within ± 30 uncertainty.

3.2.3 Gaussian Plume Inverse Method

- The Gaussian plume inverse method showed a higher probability of quantifying an emission correctly within 30%
- uncertainty than eddy covariance and aerodynamic flux gradient methods (Figure 9); ≈0.12 for the single release single
- emission and ≈0.25 for the multi release single emission categories (Figure 9). Percent errors of the Gaussian method
- calculated emissions are between -100 and +250% for single release single emission and between -100 and +800%
- for multi release single emission (Figure 9). This shows that even though the Gaussian method is designed for point
- sources, it is highly likely to miss, underestimate or overestimate an emission. Similar to eddy covariance and
- aerodynamic flux gradient, it is a challenge to correctly quantify a single emission event (single release or multiple
- release) using the Gaussian plume inverse method.

 Figure 9: Cumulative distribution function (cdf) of percent errors for the Gaussian plume inverse method. Left pane shows a cdf for a single release at the site level and the mast was downwind of the release point. Right pane shows a 317 cdf for multiple releases at the site level, but the mast was downwind of a single release point. The area bounded by the red dotted line shows the region within ± 30 uncertainty. the red dotted line shows the region within ± 30 uncertainty.

3.3 Variables Affecting Quantification

3.3.1 Eddy Covariance

 A Spearman's rank correlation analysis of measurement and environmental variables (distance, controlled release, emission height, mean wind speed (*WS*), Monin-Obukhov length (*L*) and contribution area) to percent error in quantification as calculated by the eddy covariance method, showed that downwind distance had significant impact 324 on quantification for the single release single emission ($p = 4.73e-6$), multi release single emission ($p = 2.66e-4$), and multi release multi emission (p=2.00e-3) categories for p < 0.01 significance level (Figure 10). The correlation coefficients were -0.74 for single release single emission, -0.31 for multi release single emission, and -0.30 for multi release multi emission. The negative correlation in all three categories suggests that the percent error became more negative as distance increased i.e., far away emission sources were likely underestimated or undetected. Also,

- controlled release and emission height had significant impact on quantification only in the multi release single
- emission category, p = 2.00e-3 and 9.42e-3 respectively, (Figure 10) but this correlation was inconsistent across the
- three categories. Due to inconsistent correlation, and the errors being close to -100%, the results show that generally,
- quantifying emissions using an eddy covariance approach will not work for emissions typically observed at oil and
- gas production sites.

 Figure 10: Correlation analysis for eddy covariance in the three release categories. The area bounded by the red dotted line shows the region within ± 30 uncertainty.

3.3.2 Aerodynamic Flux Gradient

 A Spearman's rank correlation analysis between the environmental and measurement variables and emissions calculated using the aerodynamic flux gradient method showed that only emission height in the single release single 340 emission category had significant impact on model quantification ($p = 1.79e-3$) (Figure 11). The correlation between emission height and percent error in this category was -0.59 suggesting percent error became more negative as emission height increased. However, the correlation between emission height and percent error in the multi release single emission and multi release multi emission categories is approximately zero, meaning no correlation. Similar to eddy covariance, there is inconsistent correlation, and most errors are close to -100% (Figure 11). The results show that generally, quantifying emissions using an aerodynamic flux gradient approach will not work for emissions typically observed at oil and gas production sites.

 Figure 11: Correlation analysis for aerodynamic flux gradient in the three release categories. The area bounded by the red dotted line shows the region within ± 30 uncertainty.

3.3.3 Gaussian Plume Inverse Method

 The Spearman's rank correlation analysis between the emissions calculated using the Gaussian plume inverse method and measurement/environmental variables showed that only the mean wind speed and atmospheric stability had significant impact on the model quantification (Figure 12). In the single release single emission category, mean wind 354 speed and percent error had a positive correlation $(0.44, p = 2.74e-4)$ indicating that an increase in WS increased the model's positive error. However, in the multi release single emission category, the correlation is opposite (a negative 356 correlation of -0.21, $p = 3.71e-3$) (Figure 12). Atmospheric stability had significant impact on model quantification in the multi release single emission category ($p = 9.15e-5$) but not in the single release single emission category (Figure 12). The correlation analysis for the Gaussian plume inverse model was inconsistent suggesting random errors in quantification. This shows that the model could either underestimate or overestimate an oil and gas emission at random.

 Figure 12: Correlation analysis for the Gaussian plume inverse method in the three release categories. The area bounded by the red dotted line shows the region within ± 30 uncertainty.

4 Discussion

 Methane emissions quantification from oil and gas is a complex system comprising of gas emissions from different heights, different locations, encountering aerodynamic obstacles of different sizes, and of varying duration, amongst others. The ability to precisely quantify an emission using data collected by a point sensor, downwind of a source is directly influenced by plume dynamics. The CH⁴ plume downwind of a source will change in size and shape in different atmospheric conditions, in open areas versus areas with obstacles, diurnally, and in different seasons (Casal, 2008). In this study, the precision to which downwind models (eddy covariance, aerodynamic flux gradient and Gaussian plume-based) could quantify the emission rate of point source(s) were tested in different atmospheric conditions (rain, sunny, snow, windy, calm etc.), and aerodynamic scenarios (emissions sources in open areas, behind obstacles, changing atmospheric stability, and day/night). As a result, testing the models' predicted emission rates to controlled release rates in different conditions introduced real-world scenarios that have not previously been tested, hence better understanding model uncertainty in the application of quantifying emissions from oil and gas production infrastructure.

4.1 Eddy Covariance

- Eddy covariance underestimated or failed to observe almost all emissions released during this study (linear regression
- 379 m between 0 and 0.07, and R^2 between 0.03 and 0.36) (Figure 4). The method measures CH₄ atmospheric fluxes for

 • Obstacles at an oil and gas facility affects wind direction and speed, and these impacts may also vary substantially with small changes in wind direction. Therefore, wind conditions are unlikely to attain steady state during the measurement period, as directed by assumption (1) above.

 • The emission height of oil and gas sources in typical upstream field conditions can be as low as 0.4 m and as high as 6.9 m and measurements are unlikely to be made by fence-line sensor above the roughness sublayer (2 above), i.e. twice the height of the mean obstacle height for ~30 m downwind. 420 • Oil and gas sources are heterogeneous (i.e. varying source distance and height) and can last a short time (e.g. a short maintenance event) or a long time ('normal' fugitive emissions) hence, achieving constant equilibrium, as stated in (3) above, is unlikely. • Footprint models used to generate the area of contribution between the source and the measurement location are designed for area sources with horizontal flow homogeneity (Kljun et al., 2015). Thus, the area of contribution generated for oil and gas point sources is likely inaccurate. **4.3 Gaussian Plume Inverse Method** In contrast to the other methods in this study, the Gaussian plume inverse model both underestimated and overestimated emissions in this study. Linear regression gradient and coefficient of correlation (m between 0.95 and $\,$ 1.49, and R² between 0.21 and 0.65; Figure 6) was better than either eddy covariance or aerodynamic flux gradient. 430 The main assumption of the Gaussian plume model is that CH₄ emitted from a point source enters the air flow, disperses vertically and laterally, forming a conical plume (Riddick et al., 2022b; US EPA, 2013). However, the formation of a conical plume is hindered at oil and gas facilities by obstacles (equipment) and is affected by atmospheric stability. Atmospheric stability in the Gaussian plume inverse model is based on Pasquil-Gifford classification system which accounts for daytime solar insolation (slight, moderate and strong), nighttime cloud cover and surface wind speed at 10 m (Kahl and Chapman, 2018). Solar insolation and cloud cover are not typically measured, and if measured, dispersion parameter models currently available do not use this data, therefore, it is difficult to calculate for continuous fence-line measurements. The modified dispersion parameters developed by EPA (US EPA, 2013) only account for wind conditions i.e., speed and deviation in direction. As a result, plume dynamics during diverse atmospheric conditions such as during snow versus rain or sunny conditions are unaccounted for. In this study, despite the Gaussian model having been developed for point sources, the model did not show consistent correlation with the measurement and atmospheric variables. This showed that there are complexities in continuous monitoring quantification compared to survey solutions where the model is widely applied, that introduce significant uncertainties in quantification. It is suggested that one problem with the Gaussian plume model is that the dispersion coefficients are simply not representative as they were developed for longer distances, in different climatological conditions, and do not transfer well to current applications (Riddick et al., 2022a). We conclude that, while it is better suited than eddy covariance or aerodynamic flux gradient, a Gaussian plume inverse approach will likely have significant uncertainties when used to quantify emissions from oil and gas production sites using data collected at a 448 fence line $({\sim} 30 \text{ m away})$.

4.4 Implications

In the recent years, there has been growing interest and need for accurate CH⁴ quantification from oil and gas sites.

- This is generally done through survey methods and continuous monitoring using fence-line sensors. Continuous
- monitoring involves having stationary sensors measuring meteorology and CH⁴ mixing ratios, which are then used to
- infer emission rate. For point sources, downwind methods such as the Gaussian plume inverse method have been

- widely used, especially for survey quantification. Continuous monitoring is relatively new but fast growing. This
- study's design replicated a continuous monitoring setup.
- Oil and gas point sources could either be single emissions or multiple emissions occurring concurrently. In cases of
- multiple emissions with more than one release point being downwind, the Gaussian model is limited, as it can only
- quantify one source at a time (dispersion coefficients are generated as a function of emission height and source
- distance). As a result, models used in other applications such as eddy covariance and aerodynamic flux gradient have
- been proposed as the solution. However, as this study has shown, eddy covariance and flux gradient approaches are
- unlikely to quantify realistic emission estimates using fence-line measurements. Here, we strongly advise that
- controlled tests under controlled environments are crucial to evaluate modelling approaches' precision and accuracy,
- and associated uncertainties before applying them in the real world. Even though these modelling approaches have
- been reported to work elsewhere (e.g., agricultural and landfill emissions), it does not necessary mean it could work
- in the intended area of application.

Author contributions

- Mercy Mbua: Conceptualization, Data curation, Methodology, Formal analysis, Investigation, Writing original draft,
- Review, and Editing. Stuart N. Riddick: Conceptualization, Methodology, Review, Editing, Project Administration,
- Supervision, and Funding Acquisition. Elijah Kiplimo: Investigation, Review, and Editing. Daniel J. Zimmerle:
- Review, Editing, Funding acquisition, and Project administration.

Declaration of competing interest

- The authors declare that they have no known competing financial interests or personal relationships that could have
- appeared to influence the work reported in this paper.

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- **Data availability**
- Data sets for this research are available in the in-text data citation reference: Mercy, Mbua; Riddick, Stuart N.;
- Kiplimo, Elijah, and Zimmerle, Daniel J. Dataset for evaluating the accuracy of downwind methods for quantifying
- point source emissions. [Dataset]. Dyrad.

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