1	Topographic modulation on the layered circulation in South China Sea
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Abstract: The South China Sea (SCS) is the largest semi-enclosed marginal sea in western Pacific. It exhibits a unique vertically rotating cyclonic, anticyclonic, and cyclonic circulation in its upper, middle, and deep layers. Over slope topography, these layered currents interact and significantly shape the structure and intensity of the basin circulation. In this study, we employ process-oriented numerical simulations to investigate how upper-layer processes, characterized by greater magnitude and variability, influence the layered circulation over the irregular topographic slope. The simulations reveal that stronger upper intrusion from open ocean directly enhances upper layer circulation, which subsequently strengthens the middle and the deep slope currents. Vorticity dynamics illustrate that changes in the middle and deep slope current are largely related to the vertical stretching (ζ _DIV) induced by bottom geostrophic cross-isobath transport (CGT_b). As the upper-layer cyclonic slope current intensifies, it modulates the bottom pressure distribution, resulting in stronger negative ζ DIV predominantly over the northwestern slope to intensify the middle anticyclone slope current. Similarly, for the deep cyclonic slope current, the CGT_b maintains downwelling in the northern part and upwelling over the southern slope. Over the southern slope, the strengthening of the positive CGT_b is induced by the increment of the advection of relative vorticity and planetary vorticity in water column, in which the middle layer has important contribution, but the upper layer has a minimal impact. Conversely, on the northern slope, the strengthening of the negative CGT_h is primarily influenced by the upper layer.

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1. Introduction

Marginal seas circulation plays crucial role in the mass transport and regional climate dynamics, with circulation patterns being strongly influenced by their unique topographic features (Millot 1999, Omstedt, Elken et al. 2004, Oey, Ezer et al. 2005, Gan, Li et al. 2006, Johns and Sofianos 2012). This topographic regulation results in intricate layered slope currents that flow in different directions at various depths (Yuan 2002, Wang, Xie et al. 2011, Lan, Zhang et al. 2013, Gan, Kung et al. 2022). These layered currents interact over slope topography, significantly shaping the structure and intensity of the overall circulation (Gan, Liu et al. 2016, Quan and Xue 2018). For instance, in the Gulf of Mexico, loop current eddies influence not just the upper-layer circulation but also the deep flow, illustrating the importance of vertical coupling in transferring energy and variability to deeper currents (Tenreiro, Candela et al. 2018). Understanding these dynamics helps elucidate the behavior of marginal sea's circulation (Liang, Spall et al. 2017, Zhu and Liang 2020, Olvera-Prado, Moreles et al. 2023).

The South China Sea (SCS) is the largest semi-enclosed marginal sea located in the tropical region. It exhibits a unique mean cyclonic, anticyclonic, and cyclonic (CAC) circulation in its upper, middle, and deep layers (Wang, Xie et al. 2011, Shu, Xue et al. 2014, Lan, Wang et al. 2015, Gan, Liu et al. 2016, Zhu, Sun et al. 2017). The strong upper layer circulation is driven by the Asia monsoon and Kuroshio intrusion from Luzon Strait (LS), while the middle and deep circulations are maintained by the outflux and deep intrusion through LS, respectively. Based on current understanding, the upper-layer influx through the Luzon Strait (LS) is induced by the Kuroshio Current as it passes through the strait (Nan et al., 2015). The middle-layer outflux and deep-layer intrusion, on the other hand, are largely driven by density differences caused by contrasting turbulent mixing intensities (e.g., Tian et al., 2009; Zhu et al., 2019; Zhou et al., 2023). Over the slope topography, the CAC circulation affects each other through the vertical coupling among them (Shu, Wang et al. 2018). For example, the study of Quan and Xue (2018) demonstrated that perturbations in the upper layer can transit through the water column and affect deeper circulation by altering layer thickness. This coupling is particularly evident over the strong boundary current that in the northern basin and along the western boundary. Numerical experiments by Wang et al. (2018) suggest that, although the basin-scale circulation is primarily driven by the LS overflow, upwelling patterns are essential in shaping the detailed structure of the deep-water circulation. Similar processes have been observed in other marginal seas as well (e.g., Testor et al., 2018; Wang et al., 2024; Xu et al., 2009; Olvera-Prado, Moreles et al. 2023).

Despite advances in understanding the major features of mean layered circulation, the response of this circulation to changes in external forcings—particularly the strong upper ocean

processes—and the specific mechanisms involved remain poorly understood. A comprehensive understanding of how topographically modulated vertical coupling over basin slopes influences the structure and intensity of mean circulation is crucial for exploring the long-term evolution of marginal sea circulation. For instance, Kuroshio intrusion has been observed to weaken with decadal variations, while upper ocean currents have shown acceleration in response to a warming climate (Peng et al., 2022; Chen et al., 2019; Nan et al., 2013). How the layered circulation in marginal seas responds to these changes remains unclear. This study employs process-oriented simulations to elucidate how upper-layer processes, which exhibit greater intensity and variability, influence layered circulation over the curved bottom slope in the SCS. The paper is organized as follows: Section 2 explains the configuration of the simulation. Section 3 offers the response of layered slope current intensity to the changes of the upper circulation. Section 4 explores the underlying physical mechanisms. Finally, Section 5 provides a summary of our findings.

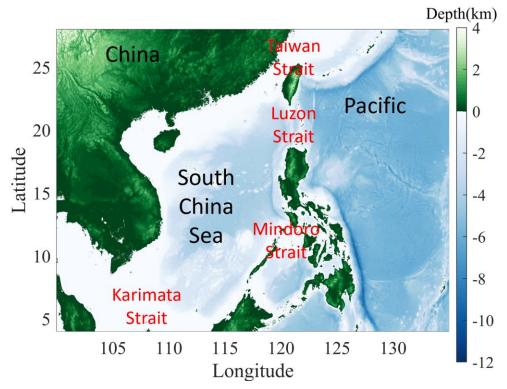


Figure 1. Location and bathymetry (km) of the South China Sea, showing Luzon Strait, Taiwan Strait, Mindoro Strait, and Karimata Strait.

2. Methodology

Based on the Regional Ocean Modeling System (ROMS) (Shchepetkin & McWilliams, 2005), we performed a three-dimensional process-oriented simulation in this study (Cai et al., 2023). The model setup included a circular basin on the west representing the SCS and a

rectangular basin on the east representing the Western Pacific Ocean. The slope in the SCS increases from 400 to 4000 m and the central basin has the depth of 4000 m. The SCS and Pacific basins were connected by a narrow strait (representing the LS) with a depth of 2500 m.

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The model employed a uniform horizontal grid with a 5 km resolution, and the vertical structure utilized stretched, terrain-following coordinates with 30 layers (Song and Haidvogel 1994) were adopted with 30 layers. Near the surface and bottom boundaries, the vertical resolution is refined with spacing of approximately 0.01. In the upper layer, an influx of 25 Sv and an outflux of 20 Sv were specified at the southeastern and northeastern boundaries of the open ocean, respectively (Figure 2c). The SCS was opened to the south with the depth of 400 m (Figure 2a), to allow the upper-layer intrusion to develop intrinsically during the simulation. To simulate the density differences and exchange currents in the middle and deep layers of the LS, the model incorporated variable contrasting mixing coefficients (K_v) between the SCS and the Western Pacific Ocean (Tian, Yang et al. 2009, Yang, Zhao et al. 2016). In the SCS and the western half of the LS, K_v values were set as $5 \cdot 10^{-4} m^2 s^{-1}$ between 500 and 1,500 m, 2 · $10^{-3}m^2s^{-1}$ below 1,500 m, and $5 \cdot 10^{-3}m^2s^{-1}$ in the layer 500 m from the bottom. In the upper 500 m of SCS and LS, and throughout the entire water column of the open ocean, a background K_v of $2 \cdot 10^{-5} m^2 s^{-1}$ was applied. The K_v was designed based on observational work by Yang et al. (2016) and estimations by Wang et al. (2017) to form the circulation in the semi-enclosed middle and deep layers. Then, simulations were conducted to explore the response of the layered slope current, particularly in the semi-enclosed middle and deep layers, to changes in the upper-layer circulation. A zonal wind stress with meridional variations was applied over the open ocean, while the atmospheric buoyancy flux over the SCS was simplified by setting it to zero. This model simplifies the configurations to focus on the fundamental dynamics of the system. While these simplifications are essential for isolating key mechanisms, they may not capture the complexity of real-world conditions, potentially limiting its quantitative applicability to realistic processes.

The model was initialized with horizontally uniform temperature and salinity profiles derived from the mean data of the World Ocean Atlas, averaged over the region west of the LS. The simulation ran for 25 years, with the analysis was conducted on the results from the final 5 years average after the layered circulation reached a stable state.

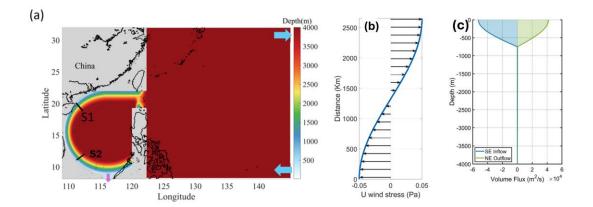
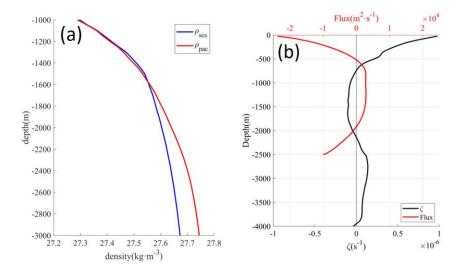


Figure 2. (a) The topography and geometry used in the idealized process-oriented simulation. The black lines show the realistic surrounding coastline. S1 and S2 are two vertical sections for showing slope current. (b) Distribution of the wind stress. (c) Vertical profile of the volume inflow/outflux (m²/s) through the southern/northern part of the eastern boundary

3. Results

In the LS, the influx occurs in the upper and deep layers, while the outflux occurs in the middle layer between them (Figure 3b). The upper intrusion is intrinsically linked to the western boundary current in the open ocean, i.e. Kuroshio Current. In the middle and bottom layers, the exchange currents are primarily related to the density differences between the South China Sea (SCS) and the Pacific. Although the initial temperature and salinity distributions are horizontally uniform, the intensified turbulent mixing within the deep SCS basin gradually leads to a density difference between the two sides of the LS. Specifically, the deep SCS exhibits lower density compared to the Pacific basin (Figure S1). Under the density difference, the westward pressure gradient was formed that drives the deep intrusion from the open ocean towards the SCS. Those features are consistent with established understandings from previous studies (e.g., Wang, Xie et al. 2011, Zhu et al., 2017, 2019; Cai, Chen et al. 2023; Zhou et al., 2023). Associated with the simulated layered exchanging current, the layered circulations developed inside the SCS basin. The upper, middle, and deep layers exhibit circulation in cyclonic, anticyclonic, and cyclonic directions, respectively (Figure S1). The horizontally averaged vorticity features with the positive-negative-positive values in the respective depth of the basin (Figure 3b).



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Figure 3. (a) Vertical profile of domain averaged density ρ (kg·m⁻³) in SCS and Pacific between 1000m to 3000m. (b) Black line shows the vertical profile of the SCS basin-averaged vorticity (s⁻¹) and the red line shows the flux through LS (m²·s⁻¹). The positive/negative vorticity represents the cyclonic/anticyclonic circulation, and the positive/negative value flux represents the outflux/influx through LS.

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To investigate how the changes in upper layer current modulates the layered circulation, additional numerical experiments were conducted by adjusting the northeastern outflux to 22Sv, 23Sv and 24Sv, thus the upper LS intrusion was adjusted to 3Sv (Case U3), 2Sv (Case U2) and 1Sv (Case U1). In these scenarios, the middle and deep exchanging currents, which were primarily sustained by the contrasting densities between the SCS and the open ocean, remained relatively unchanged (Figure 4a). Inside the basin, the enhancement of the upper layer inflow directly intensified the upper layer cyclonic circulation (Figure 4 c-f). And subsequently strengthened the middle anticyclonic slope current, particularly in the northwestern part of the basin (transect S1, Figure 4c, d). Additionally, although not directly connected to the upper layer, the deep cyclonic slope current also exhibited increased strength (Figure 4c-f). Using the domain-averaged vorticity as an indicator, it was observed that the intensification of the upper layer circulation resulted in a 10% increase in the intensity of the middle anticyclonic circulation and a 27% increase in the deep cyclonic circulation (Figure 4b). Given that only the upper layer circulation is directly amplified by the upper intrusion, the remote influence from upper layer processes over the basin slope significantly impacts the intensity of the layered circulation, which was explored below.

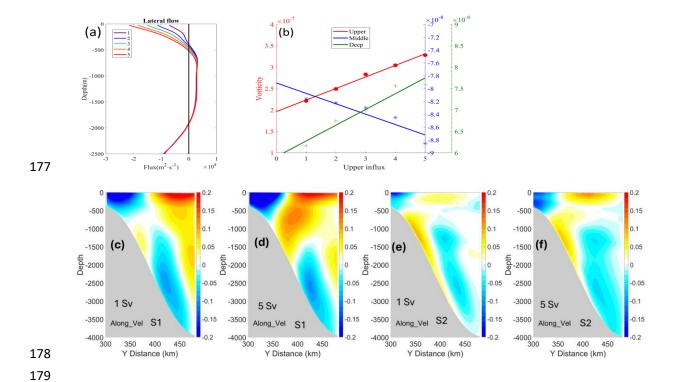


Figure 4. (a) Vertical profile flux across the LS under varying upper layer influx. (b) Changes in the basin-averaged vorticity between 0-500 m (Upper), 1000-2000 m (Middle) and 3000-4000 m (Deep) with different upper influx. (c-f) The along-slope current $(m \cdot s^{-1})$ over the section S1 and S1 in Standard case (upper intrusion is 5 Sv) and Case_U1 (upper LS intrusion is 1Sv), respectively. The locations of the two transects are shown in Figure 1a. The transect locations are indicated in Figure 1a. Positive values represent anticyclonic flow, while negative values indicate cyclonic flow.

4. Discussion

To understand how the upper layer processes modulate the layered current over the slope, we first investigated the layered-integrated vorticity budget for each layer (Gan, Liu et al. 2016, Cai, Chen et al. 2023):

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$$\overbrace{\int_{A} [\nabla \times \int_{H_{1}}^{H_{2}} (\overrightarrow{PGF}) dz] dA}^{\zeta_PGF} + \overbrace{\int_{A} [\nabla \times \int_{H_{1}}^{H_{2}} (\overrightarrow{ADV}) dz] dA}^{\zeta_ADV} + \underbrace{\int_{A} \left[-f \nabla \cdot \int_{H_{1}}^{H_{2}} (\overrightarrow{V}_{h}) dz \right] dA}_{\zeta_DIV} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{H_{2}} (v) dz \right] dA}_{\zeta_BETA} + \underbrace{\int_{A} \left[-\beta \cdot \int_{H_{1}}^{$$

 $\overbrace{\int_{A} [\nabla \times \int_{H_{1}}^{H_{2}} (\overrightarrow{VIS}) dz] dA}^{\zeta_{-}VIS} = 0 \quad (1)$

where \overrightarrow{PGF} is pressure gradient force, \overrightarrow{ADV} is nonlinear advection, \overrightarrow{VIS} is the turbulent viscosity. The horizontal viscosity is much smaller than vertical viscosity term and they are included in the \overrightarrow{VIS} term for simplicity. COR is the Coriolis force and the domain-integrated ζ_COR represents the lateral planetary vorticity flux. The H_1 and H_2 represent the bottom and upper depth of each layer, respectively. Inside the basin, the ζ_COR can be further decomposed into the vertical stretching induced by the divergence of the horizontal flow (ζ_DIV) and β

effect of the meridional current (ζ _BETA).

The circulation in SCS is primarily governed by geostrophic balance, manifested as ζ_COR balanced by the ζ_PGF in both layers. It suggests that the mean cyclonic/anticyclonic circulation is related to the lateral planetary vorticity influx/outflux (Figure 5) (Cai and Gan 2019, Cai, Chen et al. 2023; Zhu et al., 2017, 2019). Consequently, the strengthening of the upper LS intrusion directly intensifies the upper layer cyclonic slope current by providing more positive planetary vorticity flux. In the semi-enclosed middle and deep layers, the vorticity input is mainly provided by the ζ_DIV , as also highlighted in the previous studies (Zhu, Sun et al. 2017, Wang, Du et al. 2018, Cai, Chen et al. 2023). The positive ζ_DIV in the upper and deep layers reflects the downward and upward flux, which squeeze the middle layer and provide the negative vertical flux (negative ζ_DIV) for the anticyclonic circulation. Therefore, the intensification of the middle and deep slope currents is largely attributed to vertical stretching over the basin slope.



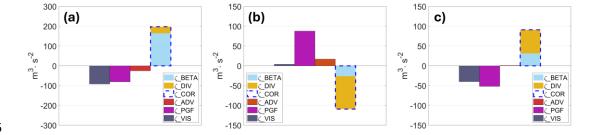


Figure 5. The layered-integrated vorticity budget (Equation 1) for the standard case in the layers of (a) 0–500, (b) 1,000–2,000, and (c) 2,500–4,000 m.

a. Intensification of middle anticyclonic slope current

For the middle anticyclonic slope current, the negative middle-layered ζ_{-} DIV (ζ_{-} DIV_M) mainly occurs over the northwestern slope (Figure 6a), where a relatively strong anticyclonic slope current is observed. In this area, the upper layer generally exhibits positive ζ_{-} DIV (ζ_{-} DIV_U), indicating downward squeezing from the upper layer that helps maintain the middle anticyclonic slope current (Figure 6 b). The increased squeezing from the upper slope current is expected to intensify the middle anticyclonic slope current (Figure 4 c, d). Since the stretching/squeezing imposed on the slope current is closely related to the vertical motion (Liang, Spall et al. 2017), the mean vertical motions over the slope can be understood as follows:

$$\overline{w} = -\nabla_h \cdot \int_{-H}^{z} \overline{\vec{V}}_h dz \approx -\nabla_h \cdot \int_{-H}^{z} \overline{\vec{V}}_{h_geo} dz - \nabla_h \cdot \int_{-H}^{z} \overline{\vec{V}}_{h_vis} dz$$

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$$= \underbrace{-(\bar{v}_{b_geo}H_y + \bar{u}_{b_geo}H_x)}_{CGT_b} + \underbrace{\frac{\beta}{f} \int_{-H}^{z} \bar{v}_{geo} dz}_{\beta \text{ effect}} \underbrace{-\nabla_h \cdot \int_{-H}^{z} \bar{V}_{h_vis} dz}_{Fric}$$
(2)

where H is the topography, _geo represents the geostrophic component of the horizontal current, which is maintained by the distribution of bottom pressure. _vis represent the vertical viscosity component. H_x and H_y are the horizontal gradients of the bottom slope, \overline{u}_{b_geo} and \overline{v}_{b_geo} are the bottom geostrophic currents. When the current flows over the slope, the bottom pressure distribution interacts with the curved topography and the resulting geostrophic crossisobath transport (CGT_b) to influence the vertical motions over the slope. The Fric represent the effect of the bottom Ekman pumping that induced by the bottom stress of the slope current. Generally, the CGT_b largely governs the mean vertical motion over northwestern slope, which in turn squeezes and stretches the middle and upper slope currents. This process is crucial in maintaining the vorticity input through ζ _DIV (Figure 6 d), thereby sustaining the dynamics of the slope currents.

Associated with the intensification of the upper layer cyclonic slope current, the stronger slope current modulates the bottom pressure distribution over the slope, leading to stronger vertical squeezing (ζ DIV) within the water column. The increase in squeezing gradually deepens the isopycnal surface and strengthens the middle anticyclonic slope current (Figure 6e).

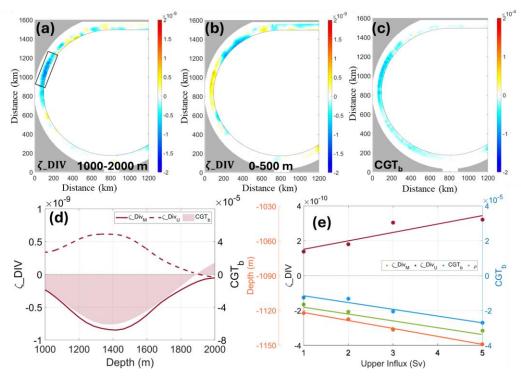


Figure 6. (a-c) ζ _DIV integrated between 1000-2000 m (ζ _DIV_M), 0-500 m (ζ _DIV_U), and CGT_b over the region of middle anticyclonic slope current between 1000-2000 m. The black line indicates the 2000 m isobath line. (d) Change of the ζ _DIV integrated between 100-2000 m

 (ζ_DIV_M) , between 0-500 m (ζ_DIV_U) with the depth over the northwestern slope. (e) Changes of the ζ_DIV_M , ζ_DIV_U , CGT_b and the depth of isopycnal surface of 1027.4 kg/m³ with different upper LS influx. (d) and (e) was plotted using the data averaged over the region of black box in (a)

b. Intensification of the deep cyclonic slope current

For the deep cyclonic slope current, the deep ζ _DIV (ζ _DIV_D) features a downward flux (negative value) over the northern slope and upward flux (positive value) over the southern part (Figure 7a, d). It suggests the sinking from the northern basin and upwelling from the southern basin would sustain the abyssal cyclonic circulation. Same as the middle anticyclonic slope current, the ζ _DIV_D is. For the deep layer, the viscosity term has an important effect in the vorticity budget (Figure 5c). Similarly, the $Fric_D$ term contributes to the deep ζ _DIV_D and is characterized by a relatively uniform downward motion (Figure 7d). However, the primary pattern and magnitude of the ζ _DIV_D are largely controlled by the CGT_D that the pressure distribution maintained the mean downwelling in the northern side and the upwelling over the southern slope (Figure 7b, d). Since the $Fric_D$ is induced by the bottom frictional stress as response to the deep layer slope current, while the bottom pressure is modulated by the motions of water in the entire water column above it, we further examine the maintenance of the bottom pressure over the slope.

To explain the maintenance of the bottom pressure distribution, the vertical integrated vorticity dynamic was employed (Gan, Liang et al. 2013, Cai and Gan 2021):

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$$\overbrace{\nabla \times \int_{-H}^{0} (\overrightarrow{PGF}) dz}^{\Omega_PGF} + \overbrace{\nabla \times \int_{-H}^{0} (\overrightarrow{ADV}) dz}^{\Omega_ADV} + \underbrace{\beta \int_{-H}^{0} v dz}_{\Omega_BETA} - \overbrace{\nabla \times \int_{-H}^{0} (\overrightarrow{VIS}) dz}^{\Omega_VIS} = 0$$
(3)

Where $\Omega_{-}PGF = \nabla \times \int_{-H}^{0} (\overrightarrow{PGF}) dz = -(\overline{v}_{b_geo}H_{y} + \overline{u}_{b_geo}H_{x})$, thus represents the effect of CGT_{b} . It illustrates that the bottom pressure distribution is maintained by the nonlinear advection of relative vorticity ($\Omega_{-}ADV$), advection of planetary vorticity ($\Omega_{-}BETA$), and net viscosity of the current flowing over the slope topography. Among them, the $\Omega_{-}BETA$ and $\Omega_{-}ADV$ play the major role in sustaining the bottom pressure distribution of the deep cyclonic slope current (Figure 8 c, d).

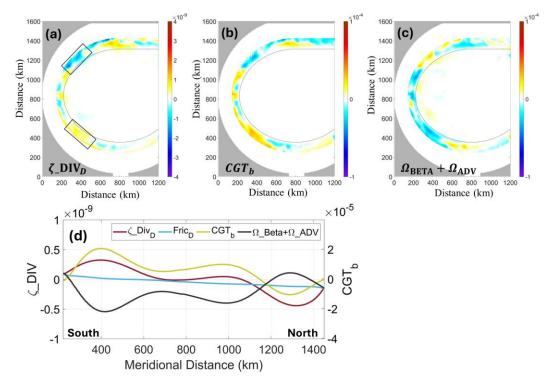
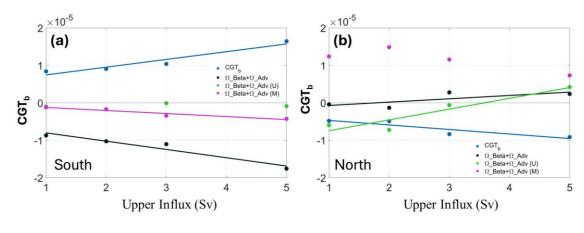


Figure 7 (a-c) ζ _DIV integrated below 3000 m of the deep cyclonic slope current (ζ _DIV_D), CGT_b and Ω _BETA + Ω _ADV over the region of middle anticyclonic slope current below 3000 m. The black line indicates the 4000 m isobath line. (d) Meridional changes of the ζ _DIV_D, Fric_D, CGT_b and Ω _BETA + Ω _ADV over the slope.

As the upper intrusion intensifies, the bottom pressure distribution adjusts in response to changes in the layered circulation, resulting in a gradual strengthening of the negative CGT_b over the northern slope and positive CGT_b over the southern part (Figure 8 a-b). Over the southern slope (Figure 8a), the strengthening of the positive CGT_b is induced by the increase of the $\Omega_BETA + \Omega_ADV$ in the water column, in which the middle layer $[\Omega_BETA + \Omega_ADV$ (M)] provides approximately 40% of the total strengthening trend, while the upper layer $[\Omega_BETA + \Omega_ADV$ (U)] has a negligible impact. Conversely, over the northern slope, the strengthening of the $\Omega_BETA + \Omega_ADV$ is primarily influenced by the upper layer, with the middle layer has the negative effect (Figure 8b). Thus, the intensification of downward CGT_b over the northern slope is directly modulated by the strengthening of the upper cyclonic slope current, while the intensification of upward CGT_b over the southern slope is mainly driven by the strengthening of the middle anticyclonic slope current. These changes in CGT_b enhance deep stretching, thereby strengthening the deep cyclonic slope current accordingly (Figure 8c).



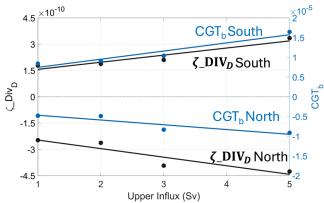


Figure 8. (a) Changes of the CGT_b , $\Omega_{Beta} + \Omega_{Adv}$ in the total water column, $\Omega_{Beta} + \Omega_{Adv}$ in the layer between 0-500 m ($\Omega_{Beta_U} + \Omega_{Adv_U}$), $\Omega_{Beta} + \Omega_{Adv}$ in the between 1000-2000 m ($\Omega_{Beta_M} + \Omega_{Adv_M}$) over the southern slope (black box in Figure 8a). (b) same as (a) but over the northern slope (black box in Figure 8a). (c) Change of the CGT_b and ζ_DIV_D over the northern and southern slope.

5. Summary

Marginal sea circulation plays a crucial role in mass transport and regional climate dynamics. Through process-oriented numerical simulations, we examined how upper-layer processes, which are characterized by greater intensity and variability, impact the layered circulation over the curved bottom slope in SCS. The primary goal of our study is to provide theoretical insights into the mechanisms driving layered circulation and their response to changes in upper-layer motions. The results underscore the intricate balance between topographical features and oceanic circulation. These insights have broad applicability to understanding similar processes and phenomena in other regions, and help to predict the behavior of marginal sea circulation under varying forcings conditions.

The numerical experiments show that the simulated layered exchange currents through the LS introduce lateral planetary vorticity flux and facilitate the development of a layered basin

circulation within the SCS. Inside the basin, the intensification of upper-layer inflow directly enhances the upper-layer cyclonic circulation, which in turn strengthens the middle anticyclonic slope current, particularly in the northwestern part of the basin. Furthermore, even though the deep cyclonic slope current is not directly connected to the upper layer, it also exhibits increased strength. Using domain-averaged vorticity as an indicator, it was found that the intensification of the upper-layer circulation resulted in the increase in the intensity of the middle anticyclonic circulation and deep cyclonic circulation.

The vorticity dynamics illustrate that the changes in the middle and deep slope current is largely related to the vertical stretching over the slope (ζ_DIV). When the current flows over the slope, the bottom pressure distribution interacts with the curved topography and the resulting geostrophic cross-isobath transport (CGT_h) influences the vertical motions. For the middle anticyclonic slope current, the negative middle ζ_DIV predominantly occurs over the northwestern slope, where a relatively strong anticyclonic slope current is present. As the upperlayer cyclonic slope current intensifies, it modulates the bottom pressure distribution over the slope, providing stronger vertical squeezing ζ DIV within the water column, which gradually strengthens the middle anticyclonic slope current. For the deep cyclonic slope current, the deep ζ _DIV is also largely controlled by the CGT_h over the slope, with the pressure distribution maintaining downwelling flows in the northern part and upwelling over the southern slope. Over the southern slope, the strengthening of the positive CGT_h is induced by the increase of the nonlinear advection of relative vorticity and planetary vorticity in the entire water column, in which the middle layer provides approximately 40% of the total strengthening trend, while the upper layer has a negligible impact. Conversely, on the northern slope, the strengthening of the negative CGT_h is primarily influenced by the upper layer, with the middle layer has the negative effect. The results from this process-oriented study deepen understanding of the intricate balance between topographical features and layered circulation, which help to improve the predictions of the long-term behavior of marginal sea circulation under varying climatic conditions. It should be noted that those understandings are based on process-oriented simulation with simplified configurations. In the following analysis, a more realistic simulation will provide more quantitative insights into the topographic modulation on the layered circulation in the marginal seas. In addition to the processes revealed in this study, other mechanisms, such as the Neptune Effect involving the eddy-slope interaction (e.g., Holloway, 1987, Stewart et al., 2024), may also play a role in influencing circulation dynamics in marginal seas like the SCS. It will be incorporated into our future investigations to improve understanding.

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Data availability. All data used in this paper are available at https://doi.org/10.5281/zenodo.13835538. The source code can be obtained upon request from the corresponding author.

Author contributions. QT conducted the investigation, developed the methodology, and carried out the writing (original draft preparation). ZC was responsible for the conceptualization, supervision, and writing (review and editing). ZL was responsible for the conceptualization and writing (review and editing).

Competing interests. The contact author has declared that none of the authors has any competing interests.

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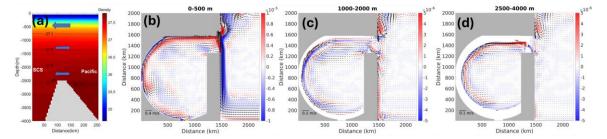


Figure S1. (a) Vertical transect of density (represented by color shading and contour lines) across the Luzon Strait. The left side represents the SCS basin, while the right side corresponds to the Pacific basin. Schematic arrows indicate the direction of the exchange flow between the two basins. (b-c) The horizontal circulation (arrows) and depth averaged vorticity (color) of (b) upper layer 0-500 m, (c) middle layer 1000-2000 m and (d) deep layer 2500-4000 m in the standard case.

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