

Reviewer 1:

General comments: This study employs an idealized model to investigate the topographic modulation on the layered circulation in the South China Sea. The topic should be of interest to those who focus on the circulation dynamics in marginal sea. Overall, I think the authors have illuminated the key physics within the cross-layer interactions over continental slope. Therefore, I just have some suggestions and recommend a minor revision before it is published.

Response: Thanks for the kind suggestions from the reviewer! We carefully revise the manuscript following your suggestions and comments.

Specific comments: 1. Considering that the work is based on an idealized model, I think the authors should present the caveats in their manuscript to help the readers make a correct understanding of the linkage between the theoretical findings and observations or realistic simulations.

Response: Thank you for your insightful comment. We fully acknowledge that our study is based on an idealized model, which inherently involves certain simplifications. To address this concern and provide readers with a clear understanding of the linkage between our theoretical findings and observations or realistic simulations, we have revised the manuscript to discuss the caveats of our approach. Specifically, we have highlighted the following points:

Simplifications in the Model Setup:

Our model simplifies certain configurations (e.g., boundary conditions, topographic features, and stratification) to focus on the fundamental dynamics of the system. While these simplifications are necessary to isolate key mechanisms, they may not capture the full complexity of real-world conditions. This may limit the quantitative application of our results to specific observational data.

Extrapolation of Findings:

The primary goal of our study is to provide theoretical insights into the mechanisms underlying layered circulation and their response to changes in upper-layer motions, rather than to perfectly replicate observed patterns. These insights and understandings have broad applicability in various processes/phenomenon in other regions.

In the revised manuscript we highlighted those point:

Line 120-123: This model simplifies the configurations to focus on the fundamental dynamics of the system. While these simplifications are essential for isolating key

mechanisms, they may not capture the complexity of real-world conditions, potentially limiting its quantitative applicability to realistic processes.

Line 318-323: The primary goal of our study is to provide theoretical insights into the mechanisms driving layered circulation and their response to changes in upper-layer motions. The results underscore the intricate balance between topographical features and oceanic circulation. These insights have broad applicability to understanding similar processes and phenomena in other regions, and help to predict the behavior of marginal sea circulation under varying forcings conditions.

Technical corrections:

1. Eq. (1): the range of integration within the layer should be explicitly written as $\int_{H_i}^{H_j} dz$

Response: Corrected, thanks.

2. L348: the literature is repeated.

Response: Corrected, thanks.

Reviewer 2:

The authors designed an idealized numerical model setup to mimic the South China Sea (SCS) and its connection with the west Pacific Ocean in order to understand the control of the slope topography in the three-layer circulation system in the SCS.

In my opinion, the numerical design is too simplified to reflect the complexity in the interactions between the three layered circulations, the setup is flawed and does not provide convincing results to support their quantitative conclusions.

Response: Thank you for the thoughtful suggestions and comments, which have significantly helped us refine and clarify our work. We have carefully considered your comments and revised our manuscript accordingly.

We acknowledge that this process-oriented study adopts certain simplifications, such as boundary conditions, topographic features, and turbulent mixing intensity. Our primary objective is to use these simplified simulations to isolate and better understand the key processes driving layered circulation. This approach allows us to clearly demonstrate how variations in the strong upper-layer circulation influence the overall layered circulation over the slope. Similar approaches were applied in previous studies and successfully obtained insights into the circulation dynamics. The results also show that the processes observed in this simulation are consistent with established understandings from previous studies. We have improved the description of model configuration to avoid misunderstanding.

Below, we have provided detailed responses to your specific concerns, particularly the details and explanations on configuration of the boundary condition, the turbulent mixing intensity, and the stability of the simulation.

The major flaws of the numerical setup are listed below:

1. The depth of the west Pacific Ocean is set to the same as the SCS (4000 m), and adopts the same initial temperature and salinity profile. This means that there is no density gradient in the deep layer between the Pacific Ocean and the SCS which is needed to form the

intrusion of the denser western Pacific water into the SCS and the resultant cyclonic deep layer circulation. I don't understand how can the model reproduce this deep circulation in this case?

Response: Yes, the maximum depths of the SCS and Pacific basins are set as 4000 m to represent the deep basins. These two basins are connected through the Luzon Strait (LS), which has a depth of only 2500 m. Although the initial temperature and salinity distributions are horizontally uniform, the intensified turbulent mixing within the deep SCS basin gradually leads to a density difference between the two sides of the LS (Figure R1). Specifically, the deep SCS exhibits lower density compared to the Pacific basin. The formation of this cross-strait density difference is consistent with previous understandings and is widely recognized as the source of the deep pressure gradient between the SCS and the Pacific. This gradient subsequently drives the deep intrusion and the development of deep cyclonic circulation (e.g., Tian et al., 2009; Zhou et al, 2023; Zhu et al.2019, Cai et al., 2021, 2023). Associated with the layered exchange current in LS, the layered circulations were developed accordingly inside the SCS basin (Figure R2)

We apology for the misunderstanding caused by the initial description. In the revised manuscript, Figure R1 and R2 will be used as the supplementary figure to better clarify the configuration details.

Line 99-100: The SCS and Pacific basins were connected by a narrow strait (representing the LS) with a depth of 2500 m.

Line 142-151: Although the initial temperature and salinity distributions are horizontally uniform, the intensified turbulent mixing within the deep SCS basin gradually leads to a density difference between the two sides of the LS. Specifically, the deep SCS exhibits lower density compared to the Pacific basin (Figure S1). Under the density difference, the westward pressure gradient was formed that drives the deep intrusion from the open ocean towards the SCS. Those features are consistent with established understandings from previous studies (e.g., Wang, Xie et al. 2011, Zhu et al., 2017, 2019; Cai, Chen et al. 2023; Zhou et al., 2023). Associated with the simulated layered exchanging current, the layered circulations developed inside the SCS basin. The upper, middle, and deep layers exhibit circulation in cyclonic, anticyclonic, and cyclonic directions, respectively (Figure S1).

Reference:

- Cai, Z., D. Chen and J. Gan (2023). "Formation of the Layered Circulation in South China Sea With the Mixing Stimulated Exchanging Current Through Luzon Strait." *Journal of Geophysical Research: Oceans* 128(3).
- Cai, Z. and J. Gan (2021). "Dynamics of the Layered Circulation Inferred from Kinetic Energy Pathway in the South China Sea." *Journal of Physical Oceanography* 51(5): 1671-1685.
- Tian, J., Q. Yang, and W. Zhao, 2009: Enhanced Diapycnal Mixing in the South China Sea. *J. Phys. Oceanogr.*, 39, 3191–3203, <https://doi.org/10.1175/2009JPO3899.1>.
- Zhou, C., Xiao, X., Zhao, W. et al. Increasing deep-water overflow from the Pacific into the South China Sea revealed by mooring observations. *Nat Commun* 14, 2013 (2023). <https://doi.org/10.1038/s41467-023-37767-4>
- Zhu, Y., Sun, J., Wang, Y., Li, S., Xu, T., Wei, Z. and Qu, T., 2019. Overview of the multi-layer circulation in the South China Sea. *Progress in Oceanography*, 175, pp.171-182.

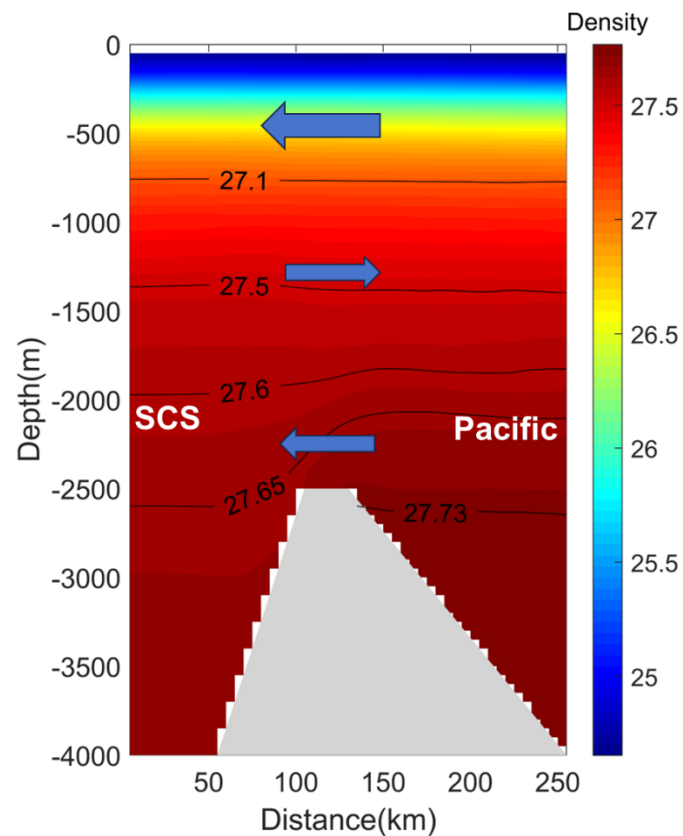


Figure R1. Vertical transect of density (represented by color shading and contour lines) across the Luzon Strait. The left side represents the SCS basin, while the right side corresponds to the Pacific basin. Schematic arrows indicate the direction of the exchange flow between the two basins.

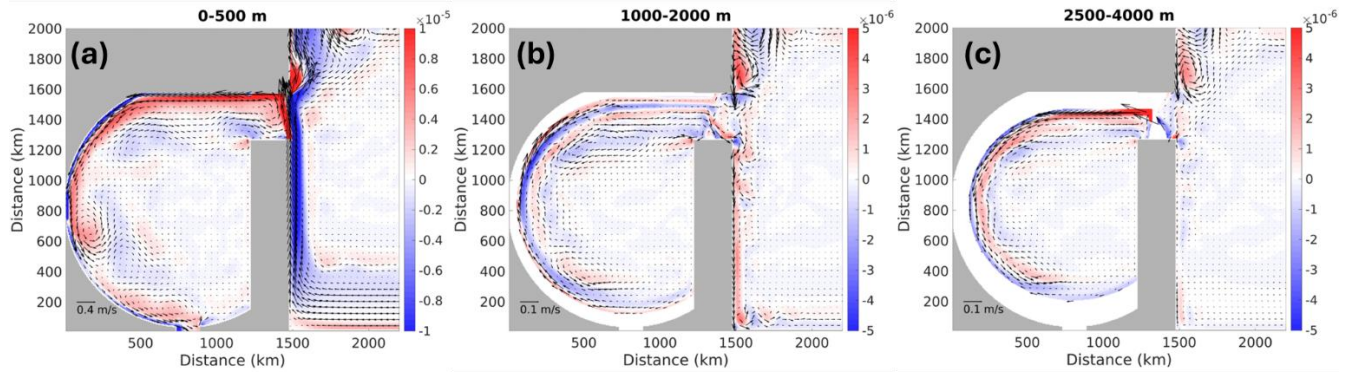


Figure R2. The horizontal circulation (arrows) and depth averaged vorticity (color) of (a) upper layer 0-500 m, (b) middle layer 1000-2000 m and (c) deep layer 2500-4000 m in the standard case.

2. What is the reason for setting three values of K_v for surface, middle and deep water layers, respectively? There is not even a linear transition between the three values in the setting. It is unclear how sensitive is the model to such artificial setting, and whether an abrupt jump of the values at the boundary cause instability of the flows and their interactions.

Response: Thank you for your question regarding the parameterization of vertical diffusivity (K_v). The K_v profile in our model is mainly based on observational work by Yang et al. (2016) (Figure R3). Yang et al. (2016) provide estimates of K_v for specific depth intervals: 500–1500 m, 1500 m to the bottom, and 500 m above the seafloor. Similarly, Wang et al. (2017) report K_v values of $O(10^{-4} \text{ m}^2/\text{s}^2)$ in the continental shelf break region and $O(10^{-3} \text{ m}^2/\text{s}^2)$ in deep waters. Those values are “generally consistent with diapycnal diffusivity estimates from turbulence microstructure measurements and finescale parameterizations” (Wang et al., 2017).

In this study, we focused on exploring the response of the layered slope current, particularly in the semi-enclosed middle and deep layers, to changes in the upper-layer circulation. Thus, we designed the mixing intensity based on those observed findings to form and maintain the deep/middle circulations. But did not delve into the detailed processes of the intensified turbulent mixing. Similar approaches were also adopted in our previous work and other studies (e.g., Cai et al., 2023; Emile-Geay and Madec, 2009; Huang and Jin, 2002; Quan and Xue, 2019; Zhao et al., 2020).

Regarding concerns about discontinuities in the K_v profile, we examined model outputs, including density and velocity distributions over the slope. While there is discontinuity in K_v , the larger K_v primarily helps to homogenize the density gradient. No significant instabilities or disruptions were observed in the slope currents or density profiles (Figure R4).

In the revised manuscript, we clarified those points:

Line 114-118: The K_v was designed based on observational work by Yang et al. (2016) and estimations by Wang et al. (2017) to form the circulation in the semi-enclosed middle and deep layers. Then, simulations were conducted to explore the response of the layered slope current, particularly in the semi-enclosed middle and deep layers, to changes in the upper-layer circulation.

Reference:

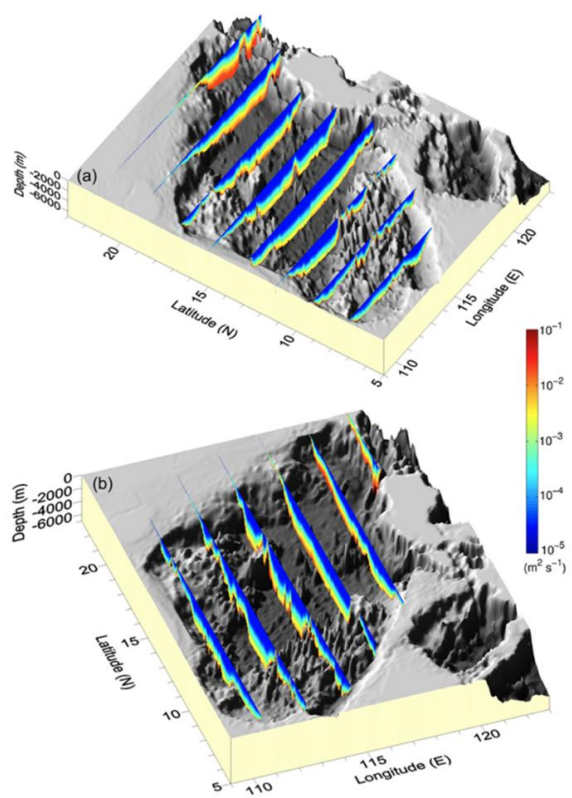
- Cai, Z., D. Chen and J. Gan (2023). "Formation of the Layered Circulation in South China Sea With the Mixing Stimulated Exchanging Current Through Luzon Strait." *Journal of Geophysical Research: Oceans* 128(3).
- Emile-Geay, J., and G. Madec, 2009: Geothermal heating, diapycnal mixing and the abyssal circulation. *Ocean Sci.*, 5, 203-217, doi:10.5194/os-5-203-2009.
- Huang, R. X., and X. Jin, 2002: Deep Circulation in the South Atlantic Induced by Bottom-Intensified Mixing over the Mid-ocean Ridge. *Journal of Physical Oceanography*, 32, 1150-1164, doi:[https://doi.org/10.1175/1520-0485\(2002\)032<1150:DCITSA>2.0.CO;2](https://doi.org/10.1175/1520-0485(2002)032<1150:DCITSA>2.0.CO;2).
- Quan, Q., and H. Xue, 2019: Influence of Abyssal Mixing on the Multilayer Circulation in the South China Sea. *Journal of Physical Oceanography*, 49, 3045-3060,

doi:<https://doi.org/10.1175/JPO-D-19-0020.1>.

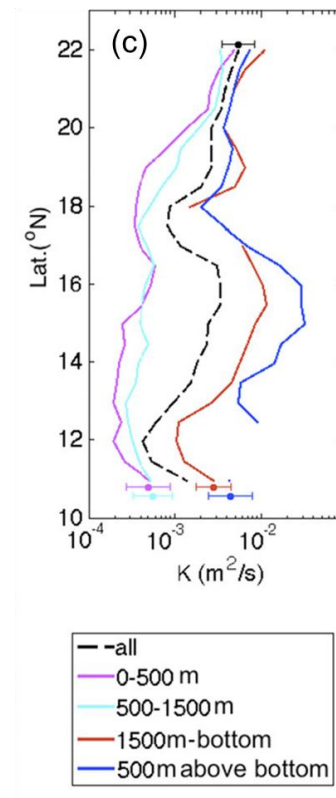
Yang, Q., W. Zhao, X. Liang, and J. Tian, 2016: Three-Dimensional Distribution of Turbulent Mixing in the South China Sea. *J. Phys. Oceanogr.*, 46, 769–788, <https://doi.org/10.1175/JPO-D-14-0220.1>.

Wang, X., Z. Liu, and S. Peng, 2017: Impact of Tidal Mixing on Water Mass Transformation and Circulation in the South China Sea. *J. Phys. Oceanogr.*, 47, 419–432, <https://doi.org/10.1175/JPO-D-16-0171.1>.

Zhao, X., C. Zhou, X. Xu, R. Ye, and W. Zhao, 2020: Deep circulation in the South China Sea simulated in a regional model. *Ocean Dynamics*, 70, 1461–1473, doi:10.1007/s10236-020-01411-2.



Wang et al., 2017



Yang et al., 2016

Figure R3. (a-b) The spatial distributions of the tide-induced diapycnal diffusivity estimated from internal tide energetics along the (a) zonal sections and (b) meridional sections. From Wang et al, 2017; (c) Depth-averaged diffusivity ($\text{m}^2 \text{s}^{-1}$) for different layers

in the meridional direction. The error bars indicate the uncertainty of standard deviation.
From Yang et al., 2016

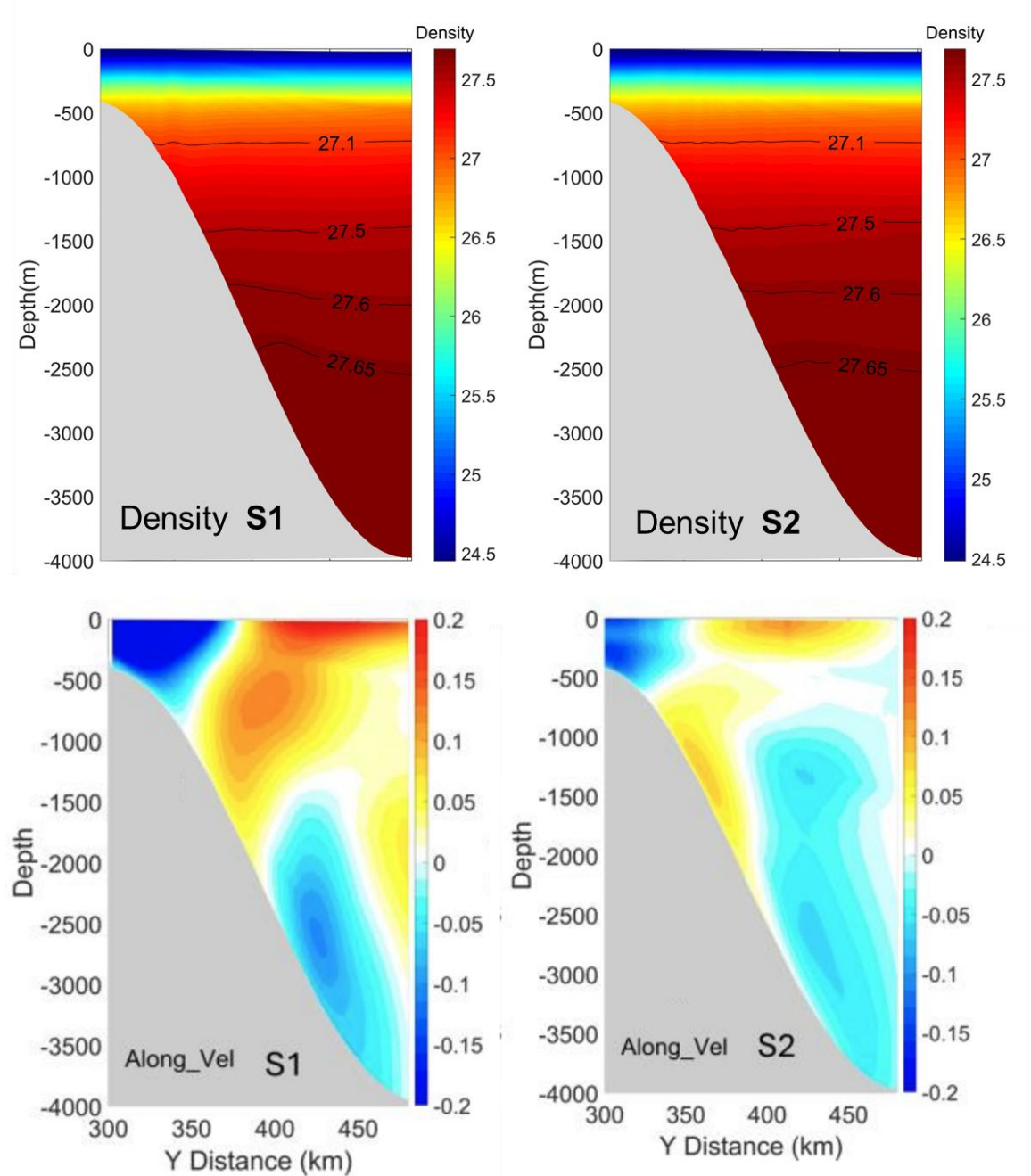


Figure R4. Vertical transects of (upper panel) density and (lower panel) along-slope velocity (Along_Vel) over sections S1 and S2.

3. The simulation is run for 25 years only. This is probably sufficient for a shallow shelf sea but is definitely too short for the SCS and west pacific ocean to develop a stable or quasi-stable states of the circulations, especially for the middle and deep layers. This means the system is still in a fast developing phase with instable states, and I have serious concern on using the results for quantative analysis of the three-layer circulations.

Response: We understand the reviewer's concern on the stability of simulation. Following reviewer's concerns, we've checked the time series of the vorticity in different layers (Figure R5). Generally, even for the middle and deep layers, the simulation time is sufficient to reach a stable or quasi-stable state. Since the mixing intensity inside the SCS is two orders of magnitude larger than the Pacific (Tian et al., 2009; Yang et al., 2016), under the intensified density difference crossing the LS, the layered circulations are quickly generated and reached the stable state.

In the revised manuscript, we clarified this point:

Line 126-127. The simulation ran for 25 years, with the analysis was conducted on the results from the final 5 years average after the layered circulation reached a stable state.

Reference:

- Tian, J., Q. Yang, and W. Zhao, 2009: Enhanced Diapycnal Mixing in the South China Sea. *J. Phys. Oceanogr.*, 39, 3191–3203, <https://doi.org/10.1175/2009JPO3899.1>.
- Yang, Q., W. Zhao, X. Liang, and J. Tian, 2016: Three-Dimensional Distribution of Turbulent Mixing in the South China Sea. *J. Phys. Oceanogr.*, 46, 769–788, <https://doi.org/10.1175/JPO-D-14-0220.1>.

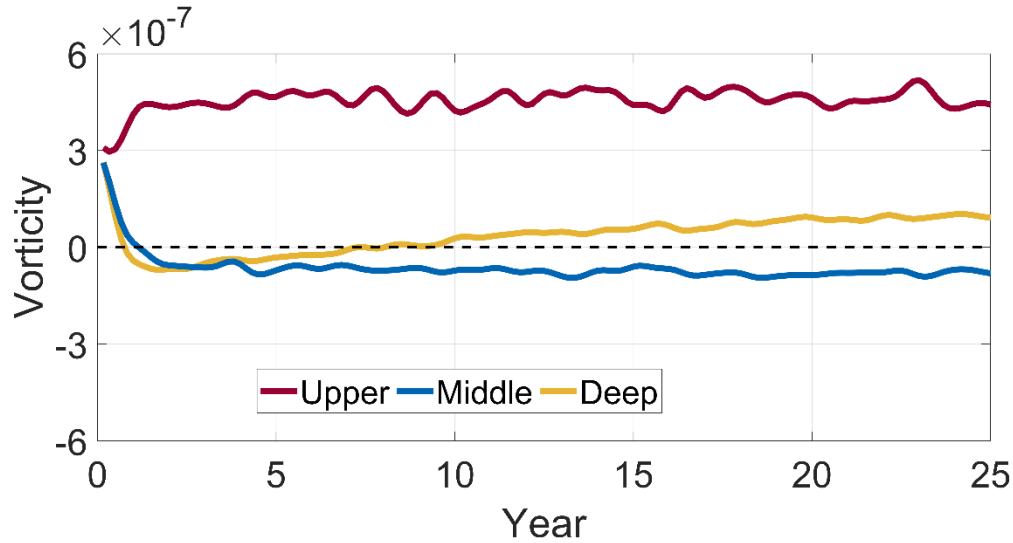


Figure R5. Time series of the domain-averaged vorticity averaged in the upper 500 m (Upper), 1000-2000 m (Middle), and below 2500 m (Deep)

4. It seems the authors mix the descriptions of the simulation results with results from existing literature for formation of the three-layer circulations, see line 123-129. As the authors described, density differences between the SCS and the Pacific ocean is needed to drive the deep intrusion, but such feature was not implemented in the model setup (see point 1).

Response: Thank you for your comment. We apologize for the confusion caused by the initial description. The citations included in the manuscript are intended to highlight that, although an idealized configuration was used, the results and processes observed in this simulation are consistent with established understandings from previous studies. They help prove that the model successfully captures the key processes, thereby ensuring the reliability of the results in exploring the underlying dynamics.

To address this concern and prevent further misunderstanding, we have revised the manuscript as:

Line 142-148: Although the initial temperature and salinity distributions are horizontally uniform, the intensified turbulent mixing within the deep SCS basin gradually leads to a density difference between the two sides of the LS. Specifically, the deep SCS exhibits

lower density compared to the Pacific basin (Figure S1). Under the density difference, the westward pressure gradient was formed that drives the deep intrusion from the open ocean towards the SCS. Those features are consistent with established understandings from previous studies (e.g., Wang, Xie et al. 2011, Zhu et al., 2017, 2019; Cai, Chen et al. 2023; Zhou et al., 2023).

For the density difference, we responded in your comments 1, thanks!

5. It is unclear to me how the authors managed to adjust the outflux and influx at the open boundary to these exact values. My concern is that the model results may be largely driven by the specified input/output at the boundary, rather by the internal dynamics of the system. The authors need to justify why such configuration is reasonable. For instance, it is stated that the influx/outflux was defined in the **upper water layer** at the **southeastern** and **northwestern** boundaries of the open ocean (line 99-100). What is set for the deeper water layers in these open boundaries, and for other parts of the open boundary in the Pacific ocean? Please clarify these and justify that the system is not purely driven by the boundary setting.

Response: Thank you for the comment on the model configurations.

Based on current understanding, the upper-layer influx through the Luzon Strait (LS) is induced by the western boundary current (Kuroshio Current) as it passes through the strait (Nan et al., 2015). The middle-layer outflux and deep-layer intrusion, on the other hand, are largely driven by density differences caused by contrasting turbulent mixing intensities (e.g., Tian et al 2007; Zhu et al, 2019; Zhou et al.,2023). Thus, the upper layer intrusion, as noted by the reviewer, is related to the boundary flux, while the middle and deep layer exchanging current are governed by internal dynamics. These established understandings guided the design of our model configuration.

In this study, we focused on the influence of upper layer circulation intensity on the layered current. For the upper layer circulation, the key is to provide the western boundary current

in Pacific and the intrusion through LS. Thus, the upper influx (25 Sv)/outflux (20 Sv) was defined at the southeastern/northeastern boundary of the open ocean (Figure R6). The other regions of the southern, eastern and northern boundaries are set as walls. In the SCS basin, the southern strait was opened, allowing the intrusion through LS, which subsequently drives the upper-layer circulation. By changing the influx and outflux through the southeastern and northeastern boundaries, the upper intrusion and upper SCS circulation can be modified intrinsically.

In the deep and middle layer, the exchange current is generated and maintained by the contrasting turbulent mixing intensity as we responded above (Figure R1).

We acknowledge that the idealized configuration is used in this process-oriented simulation. However, it captures the major processes involved in the layered circulation and helps explore how changes in the upper-layer circulation influence the layered currents. Following reviewer's concerns, the Figure R6 was added in the revised manuscript, and we refine the manuscript to clarify the configuration of boundary current:

Line 60-64: Based on current understanding, the upper-layer influx through the Luzon Strait (LS) is induced by the Kuroshio Current as it passes through the strait (Nan et al., 2015). The middle-layer outflux and deep-layer intrusion, on the other hand, are largely driven by density differences caused by contrasting turbulent mixing intensities (e.g., Tian et al., 2009; Zhu et al., 2019; Zhou et al., 2023).

Line 104-110: In the upper layer, an influx of 25 Sv and an outflux of 20 Sv were specified at the southeastern and northeastern boundaries of the open ocean, respectively (Figure 2c). The SCS was opened to the south with the depth of 400 m (Figure 2a), to allow the upper-layer intrusion to develop intrinsically during the simulation. To simulate the density differences and exchange currents in the middle and deep layers of the LS, the model incorporated variable contrasting mixing coefficients (K_v) between the SCS and the Western Pacific Ocean (Tian, Yang et al. 2009, Yang, Zhao et al. 2016).

Reference:

- Nan, F., Xue, H. and Yu, F., 2015. Kuroshio intrusion into the South China Sea: A review. *Progress in Oceanography*, 137, pp.314-333.
- Tian, J., Q. Yang and W. Zhao (2009). "Enhanced diapycnal mixing in the South China Sea." *Journal of Physical Oceanography* 39(12): 3191-3203.
- Zhu, Y., Sun, J., Wang, Y., Li, S., Xu, T., Wei, Z. and Qu, T., 2019. Overview of the multi-layer circulation in the South China Sea. *Progress in Oceanography*, 175, pp.171-182.
- Zhou, C., Xiao, X., Zhao, W. et al. Increasing deep-water overflow from the Pacific into the South China Sea revealed by mooring observations. *Nat Commun* 14, 2013 (2023). <https://doi.org/10.1038/s41467-023-37767-4>
- Yang, Q., W. Zhao, X. Liang and J. Tian (2016). "Three-Dimensional Distribution of Turbulent Mixing in the South China Sea." *Journal of Physical Oceanography* 46(3): 769-788.

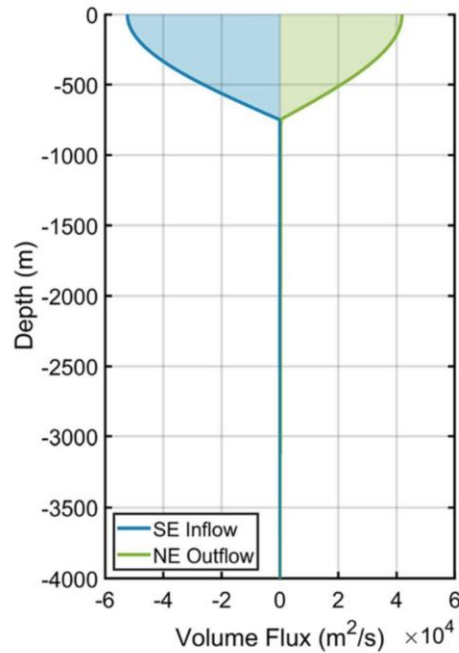


Figure R6. Vertical profile of the volume inflow/outflux ($\text{m}^2 \text{s}^{-1}$) through the southern/northern part of the eastern boundary. The total volume transports are set as 25 and 20 Sv, respectively.

Given the major flaws mentioned above, I am not convinced by the quantitative numbers, e.g. 10% increase in the intensity of the middle anticyclonic circulation and 27% increase

in the deep cyclonic circulation (line 299-300) given in the summary. A more comprehensive sensitivity study on how a change in the specific configurations would affect such numbers is needed. This includes not only the influx/outflux setting in the surface layer at the open boundary but also the run time, the setting of Kv and the initial temperature&salinity profile.

Response: Thanks for the comment. We agree with the reviewer that the quantitative values provided in the summary are reliable only under the current simulation configuration. In the revised manuscript, we did not highlight those quantitative numbers. In the description of the results, we clarified that the values are based on the idealized simulation with specific settings. Realistic simulations would provide more reliable quantitative results, which require future investigation.

As addressed in previous comments, the runtime of the simulation is sufficiently long to ensure a steady-state solution. The Kv used in the model are based on observational estimates, and the initial temperature and salinity profiles are derived from reanalysis data. These configurations have also been used in our previous investigations to explore the dynamics of the layered circulation in SCS.

In the revised manuscript, we removed the quantitative numbers and clarified the results are based on the simplification configuration

Line 120-123: This model simplifies the configurations to focus on the fundamental dynamics of the system. While these simplifications are essential for isolating key mechanisms, they may not capture the complexity of real-world conditions, potentially limiting its quantitative applicability to realistic processes.

Line 330-332: it was found that the intensification of the upper-layer circulation resulted in the increase in the intensity of the middle anticyclonic circulation and deep cyclonic circulation.

Line 352-355: It should be noted that those understandings are based on process-oriented simulation with simplified configurations. In the following analysis, a more realistic simulation will provide more quantitative insights into the topographic modulation on the layered circulation in the marginal seas.

Besides a more comprehensive sensitivity study, I suggest the authors to perform analysis using more realistic simulation/reanalysis results that are readily available, e.g. from the global HYCOM. The multi-year averaged results (climatology) should provide a more convincing dataset for the analysis, and it has a more realistic representation of the complex topography and the three-layer circulations. A result comparison between the idealized model setup and the more realistic setup would provide more insights into the topographic modulation on the layered circulation in the SCS.

Response: We totally agreed that the realistic simulation or reanalysis dataset would give more details in those processes. However, as all factors change simultaneously in such setups, it may be challenging to isolate specific processes carefully. The process-oriented simulations offer a different perspective by isolating individual processes and illustrating the role of upper-layer circulation more clearly.

Besides, the intensified mixing intensity in the SCS was related to the dissipation of internal waves over complicated topography, which was not well resolved by the global models. Thus, the global model, such as HYCOM or OFES, did not capture the layered circulation features in the SCS (Figure R7). We are refining a regional high-resolution realistic simulation in this region (part of the work was under review in Journal of Physical Oceanography) and prefer to explore the topographic modulation on the layered circulation in the SCS using realistic simulation in our following work.

In the revised manuscript, we clarify this point.

Line 352-355: It should be noted that those understandings are based on process-oriented simulation with simplified configurations. In the following analysis, a more realistic simulation will provide more quantitative insights into the topographic modulation on the layered circulation in the SCS.

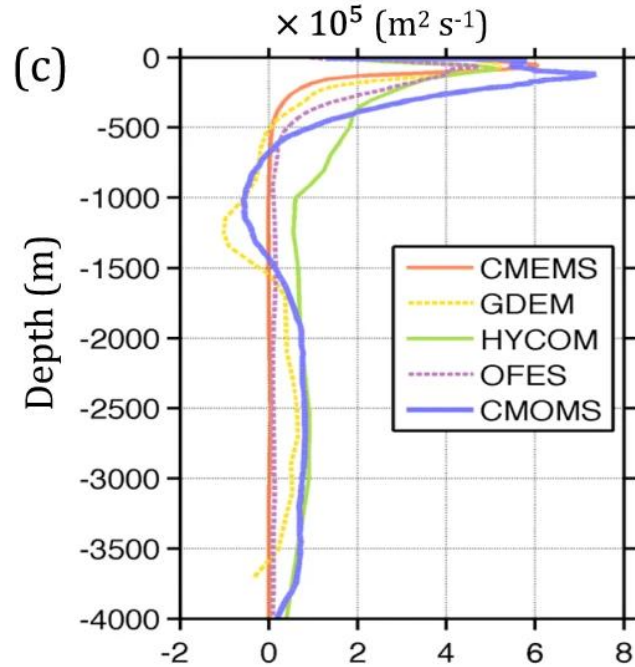


Figure R7. Vertical profile of the 20-year time domain-integrated relative vorticity obtaining from geostrophic currents based on hydrographic data from GDEM (Generalized Digital Environmental Model; yellow dashed line), global models of CMEMS (The European Copernicus Marine Environment Monitoring Service; solid orange line), HYCOM (Hybrid Coordinate Ocean Model; green solid line) and OFES (Ocean General Circulation Model For the Earth Simulator; purple dashed line), and CMOMS (China Sea Multi-scale Modeling System; blue solid line) as a function of depth. From Gan et al., 2022.

References:

Gan, J., Kung, H., Cai, Z. et al. Hotspots of the stokes rotating circulation in a large marginal sea. Nat Commun 13, 2223 (2022). <https://doi.org/10.1038/s41467-022-29610-z>

Reviewer 3.

This manuscript studies the vertical structure and dynamics of the continental slope circulation in the South China Sea. Layer-integrated vorticity diagnostics from Primitive-Equation numerical simulations with idealized geometry are used to study the sensitivity of the circulation to the upper-layer inflow in the Luzon Strait. It is shown that the vertical structure of the circulation (respectively cyclonic, anticyclonic, and cyclonic for the top, middle and bottom layers) is linked to the surface intensified flow's interaction with the curved geometry of the marginal basin.

I see several major issues in the manuscript. Briefly, the most important ones involve the attribution of the middle and bottom layer's driving mechanisms, potentially significant spurious flows associated with pressure gradient errors in the simulations, and the quantification and interpretation of the viscous term in the model. Text and figures read generally fine, but there are English language problems in the text, and several figures lack axis labels. The major and minor points are detailed below.

Response: Thank you for the helpful suggestions and comments. In response to the reviewer's feedback, we have carefully examined the pressure gradient errors and improved the physical interpretation of the results. Additionally, we have refined the language throughout the manuscript and made enhancements to the figures. Below, we provide a detailed response to each comment.

Major points:

M1 (Section 2, pressure gradient errors): The known problem of spurious flow associated with numerical pressure gradient errors in terrain-following models such as ROMS always needs to be examined before a process study can be performed adequately. The authors need to show how the magnitude of the spurious circulation that arises in their model with an unforced, initially laterally-uniform stratification everywhere compares to the slope currents in their forced simulations. The physical signal of the slope currents is weak (less than 10 cm/s in the middle and bottom layers), and the spurious flow needs to be much smaller than that. With 30 vertical levels, a 5 km grid, and the $O(1e-2)$ bottom slopes

involved, pressure gradient errors are likely to be non-negligible in the SCS's continental slope. Without smoothing the topography, the only solution is to refine the horizontal and vertical grids until the spurious flow becomes negligible. This numerical effect needs to be thoroughly examined before the results can be interpreted appropriately.

Response: Thanks for the reminder. In response to the reviewer's concerns, we examined the layered circulation and the magnitude of the bottom pressure gradient in an unforced scenario with an initially laterally uniform stratification (Figures R1 and R2). Overall, while some spurious flow associated with numerical pressure gradient errors was observed, no distinct circulation pattern was formed, and the magnitudes of these errors are significantly smaller than the mean circulation in the cases presented in the manuscript.

In this simulation, the strong upper-layer intrusion from the open ocean, combined with the contrasting mixing intensity that induces exchange currents, provides substantial external physical forcing. Additionally, the sigma layers were refined near the bottom layer to improve accuracy. Thus, we think the physical signal of the slope current, and the analysis are reliable.

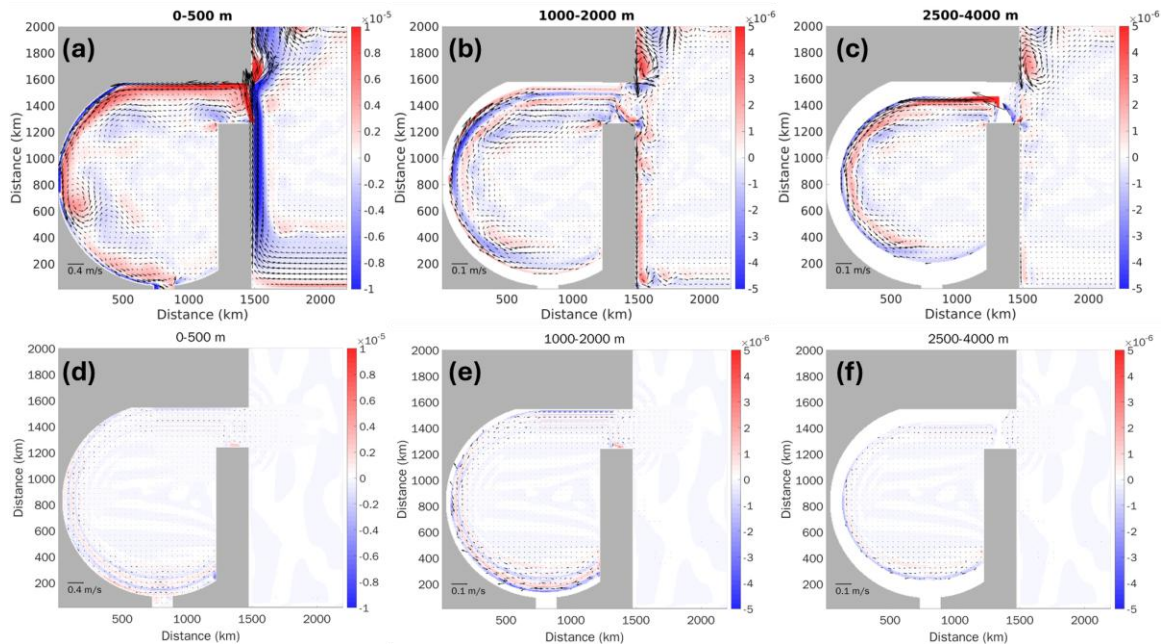


Figure R1. The horizontal circulation (arrows) and depth averaged vorticity (color) of (a) upper layer 0-500 m, (b) middle layer 1000-2000 m and (c) deep layer 2500-4000 m in the

standard case. The color indicates the depth-averaged vorticity in each layer. (e-f) are same as (a-c) but for the unforced simulation.

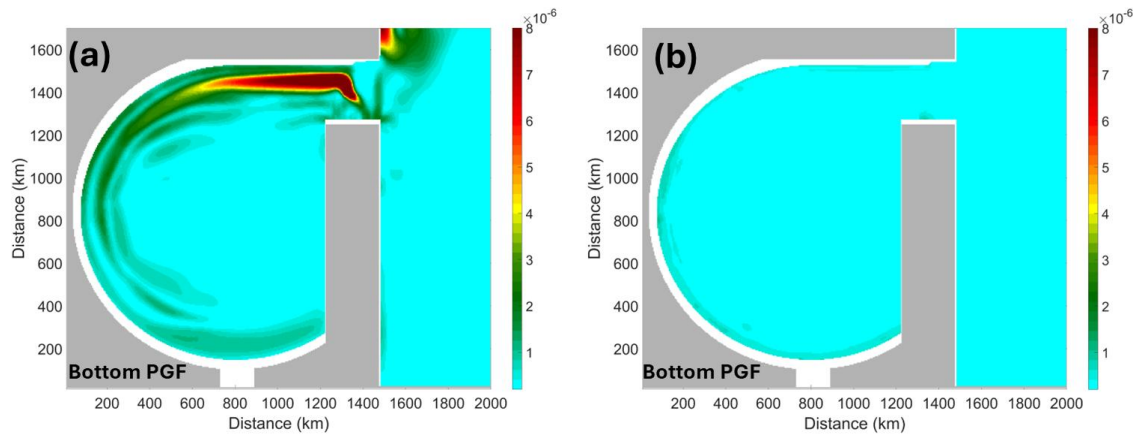


Figure R2. The magnitude of bottom pressure gradient force ($PGF = \sqrt{PGF_x^2 + PGF_y^2}$) in (a) standard case in manuscript and (b) unforced simulation.

M2: Related to point M1, what is the vertical spacing of the sigma levels? Are they refined near the surface and bottom to improve representation of the boundary layers?

Response: Yes, the sigma levels were refined near the surface and bottom (Figure R3). Near the surface and bottom, the vertical spacing is approximately 0.01 to improve the representation of the boundary layers.

In the revised manuscript, we clarified it:

Line 103-104: Near the surface and bottom boundaries, the vertical resolution is refined with spacing of approximately 0.01.

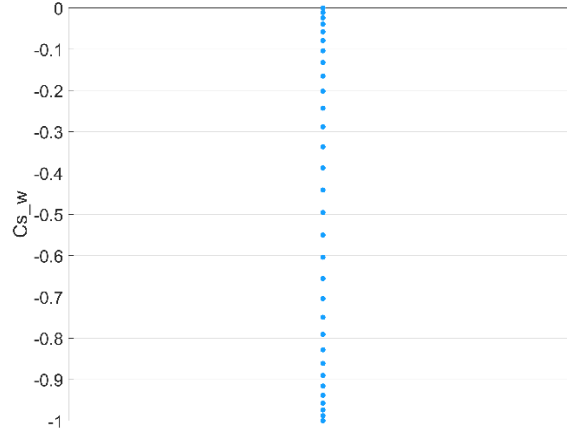


Figure R3. The vertical spacing of the sigma levels in the simulation.

M3: (lines 105-108): All results may be sensitive to these coefficient choices (particularly flow in the top and bottom layers). This needs to be thoroughly examined if a spatially-varying viscosity coefficient is used.

M4: Related to M3, what was the turbulent closure scheme used? This information is missing in the text.

Response: These two comments are related to the mixing coefficient in the simulation, so we addressed them together.

For the layered circulation in the middle and deep layers, they are mainly maintained by the outflux and deep intrusion through LS, respectively. According to previous investigations, exchange currents in the deep and middle layers are largely driven by density differences caused by contrasting turbulent mixing intensities (Tian et al., 2009; Yang et al., 2016; Zhu et al., 2019; Zhou et al., 2023). In the observation work of Yang et al (2016), they provided estimates of K_v for specific depth intervals: 500–1500 m, 1500 m to the bottom, and 500 m above the seafloor (Figure R4). Similarly, Wang et al. (2017) report K_v values of $O(10^{-4} \text{ m}^2/\text{s}^2)$ in the continental shelf break region and $O(10^{-3} \text{ m}^2/\text{s}^2)$ in deep waters.

In this study, we focused on exploring the response of the layered slope current, particularly in the semi-enclosed middle and deep layers, to changes in the upper-layer circulation.

Thus, in the simulation, we adopted the estimation in the observation of Yang et al (2017), without using a turbulent closure scheme. Similar approaches have been employed in our previous works and other studies (e.g., Cai et al., 2023; Emile-Geay and Madec, 2009; Huang and Jin, 2002; Quan and Xue, 2019; Zhao et al., 2020).

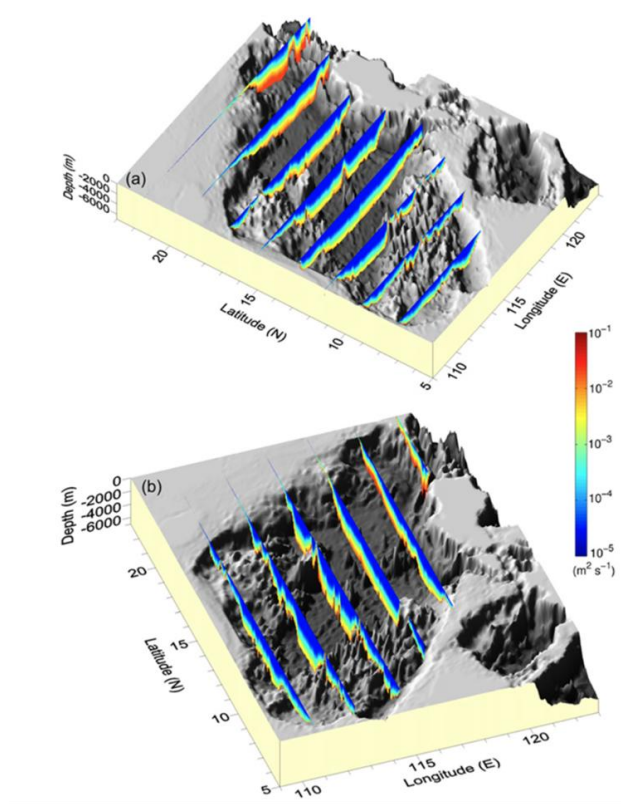
Although an idealized configuration was used, the results and processes observed in this simulation are generally consistent with established understandings from previous studies. The intensified turbulent mixing within the deep SCS basin gradually leads to a density difference between the two sides of the LS. Specifically, the deep SCS exhibits lower density compared to the Pacific basin (Figure R5). Under the density difference, the westward pressure gradient was formed that drives the deep intrusion from the open ocean towards the SCS. Associated with the simulated layered exchanging current, the layered circulations developed inside the SCS basin. The upper, middle, and deep layers exhibit circulation in cyclonic, anticyclonic, and cyclonic directions, respectively (Figure R5). Those features are consistent with established understandings from previous studies (e.g., Wang, Xie et al. 2011, Zhu et al., 2017, 2019; Cai, Chen et al. 2023; Zhou et al., 2023).

In the revised manuscript, we clarified those point:

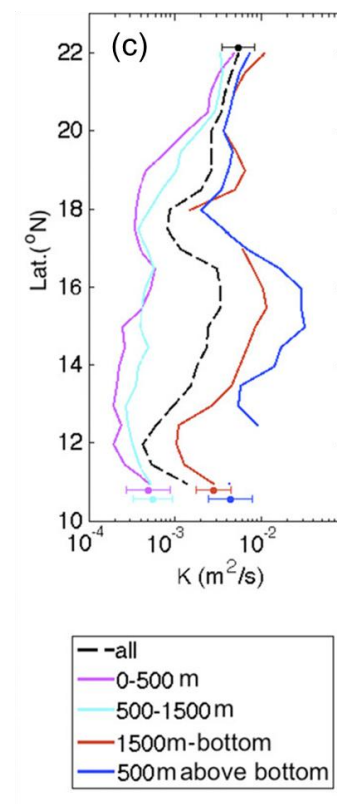
Line 114-118: The K_v was designed based on observational work by Yang et al. (2016) and estimations by Wang et al. (2017) to form the circulation in the semi-enclosed middle and deep layers. Then, simulations were conducted to explore the response of the layered slope current, particularly in the semi-enclosed middle and deep layers, to changes in the upper-layer circulation

Line 142-151: Although the initial temperature and salinity distributions are horizontally uniform, the intensified turbulent mixing within the deep SCS basin gradually leads to a density difference between the two sides of the LS. Specifically, the deep SCS exhibits lower density compared to the Pacific basin (Figure S1). Under the density difference, the westward pressure gradient was formed that drives the deep intrusion from the open ocean towards the SCS. Those features are consistent with established understandings from previous studies (e.g., Wang, Xie et al. 2011, Zhu et al., 2017, 2019; Cai, Chen et al. 2023;

Zhou et al., 2023). Associated with the simulated layered exchanging current, the layered circulations developed inside the SCS basin. The upper, middle, and deep layers exhibit circulation in cyclonic, anticyclonic, and cyclonic directions, respectively (Figure S1).



Wang et al., 2017



Yang et al., 2016

Figure R4. (a-b) The spatial distributions of the tide-induced diapycnal diffusivity estimated from internal tide energetics along the (a) zonal sections and (b) meridional sections. From Wang et al, 2017; (c) Depth-averaged diffusivity ($\text{m}^2 \text{s}^{-1}$) for different layers in the meridional direction. The error bars indicate the uncertainty of standard deviation. From Yang et al., 2016

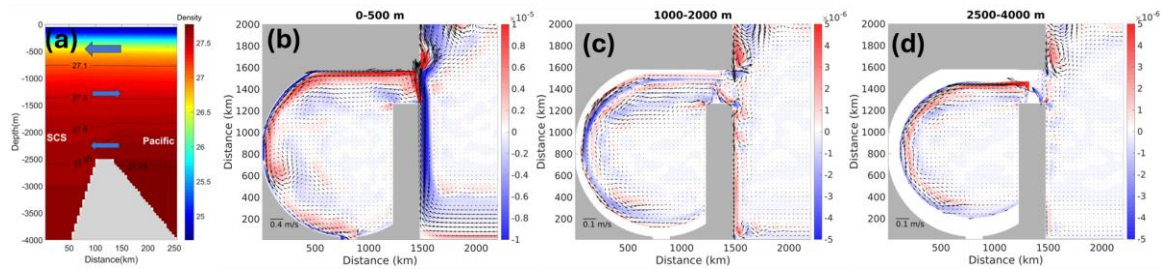


Figure R5. (a) Vertical transect of density (represented by color shading and contour lines) across the Luzon Strait. The left side represents the SCS basin, while the right side corresponds to the Pacific basin. Schematic arrows indicate the direction of the exchange flow between the two basins. (b-d) The horizontal circulation (arrows) and depth averaged vorticity (color) of (a) upper layer 0-500 m, (b) middle layer 1000-2000 m and (c) deep layer 2500-4000 m in the standard case.

Reference:

- Cai, Z., D. Chen and J. Gan (2023). "Formation of the Layered Circulation in South China Sea With the Mixing Stimulated Exchanging Current Through Luzon Strait." *Journal of Geophysical Research: Oceans* 128(3).
- Emile-Geay, J., and G. Madec, 2009: Geothermal heating, diapycnal mixing and the abyssal circulation. *Ocean Sci.*, 5, 203-217, doi:10.5194/os-5-203-2009.
- Huang, R. X., and X. Jin, 2002: Deep Circulation in the South Atlantic Induced by Bottom-Intensified Mixing over the Midocean Ridge. *Journal of Physical Oceanography*, 32, 1150-1164, doi:https://doi.org/10.1175/1520-0485(2002)032<1150:DCITSA>2.0.CO;2.
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- Yang, Q., W. Zhao, X. Liang, and J. Tian, 2016: Three-Dimensional Distribution of Turbulent Mixing in the South China Sea. *J. Phys. Oceanogr.*, 46, 769–788, https://doi.org/10.1175/JPO-D-14-0220.1.
- Wang, X., Z. Liu, and S. Peng, 2017: Impact of Tidal Mixing on Water Mass Transformation and Circulation in the South China Sea. *J. Phys. Oceanogr.*, 47, 419–432, https://doi.org/10.1175/JPO-D-16-0171.1.
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Geophysical Research Letters **38**(5): n/a-n/a.

Zhao, X., C. Zhou, X. Xu, R. Ye, and W. Zhao, 2020: Deep circulation in the South China Sea simulated in a regional model. *Ocean Dynamics*, 70, 1461-1473, doi:10.1007/s10236-020-01411-2.

Zhu, Y., J. Sun, Y. Wang, Z. Wei, D. Yang and T. Qu (2017). "Effect of potential vorticity flux on the circulation in the South China Sea." Journal of Geophysical Research: Oceans **122**(8): 6454-6469.

Zhu, Y., Sun, J., Wang, Y., Li, S., Xu, T., Wei, Z. and Qu, T., 2019. Overview of the multi-layer circulation in the South China Sea. *Progress in Oceanography*, 175, pp.171-182.

Zhou, C., Xiao, X., Zhao, W. et al. Increasing deep-water overflow from the Pacific into the South China Sea revealed by mooring observations. *Nat Commun* 14, 2013 (2023). <https://doi.org/10.1038/s41467-023-37767-4>

M5 (lines 113-114): Is the system at a near-steady state at this point? Some metric such as a global KE time series should show this clearly and help determine how long the simulations need to be. Also, I assume this is a 5-year average? If so, please mention that here.

Response: Thank you for the reminder from the reviewer. In response to the reviewer's concern, we've checked the time series of the basin-averaged vorticity in different layers (Figure R6). Generally, even for the middle and deep layers, the simulation time is sufficient to reach the steady state.

Yes, the 5-year average was used.

In the revised manuscript, we clarify this point:

Line 126-127: The simulation ran for 25 years, with the analysis was conducted on the results from the final 5 years average after the layered circulation reached a stable state.

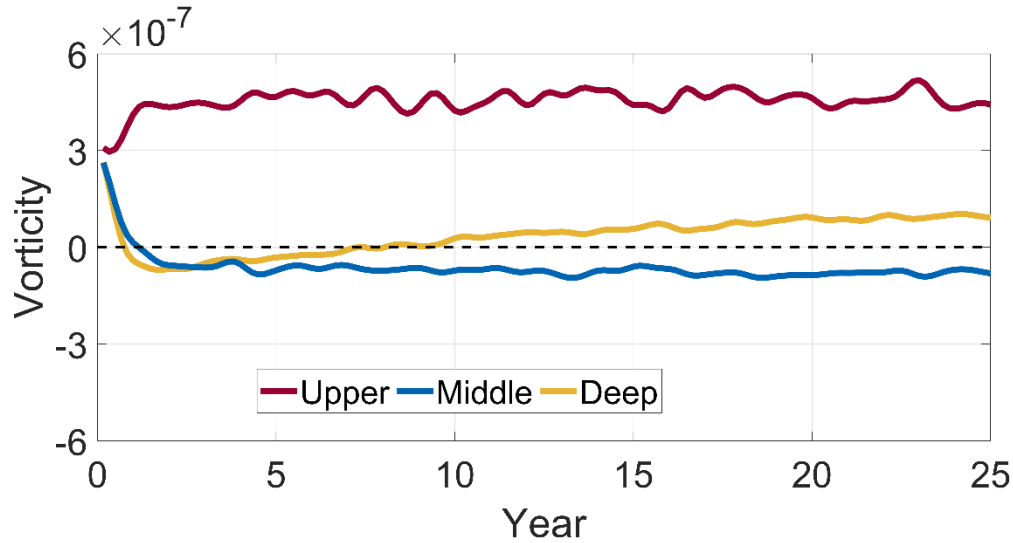


Figure R6. Time series of the domain-averaged vorticity averaged in the upper 500 m (Upper), 1000-2000 m (Middle), and below 2500 m (Deep)

M6 (Figure 2, Section 2): The topography in the southern boundary of the LS has a more irregular shape than the SCS and Pacific parts of the domain. What is the reason for this choice, and how sensitive are the results to this geometry (compared to a configuration where the LS's southern boundary joins the interior of the SCS smoothly like what is seen in the LS's northern boundary in Figure 2a)?

Response: In this study, our aim is to understand how changes in the upper-layer circulation modulate the layered circulation over the meandering slope, particularly in the semi-enclosed middle and deep layers. To facilitate the formation of the upper-layer cyclonic circulation, a shallow opening with a depth of approximately 400 m was configured to allow outflux, enabling the upper-layer intrusion from the Luzon Strait. This opening represents the relatively shallow straits in the southern part of SCS. It was not specifically designed but simply provided to allow the outflux.

Considering that the primary regions of coupling among the three layers are not near the southern boundary, and the depth of the southern opening is relatively shallow, its influence on the overall results is minimal.

In the revised manuscript, we clarified this point:

Line 106-107: The SCS was opened to the south with the depth of 400 m (Figure 2a), to allow the upper-layer intrusion to develop intrinsically during the simulation.

M7 (Lines 176-177, Equation 1): There is no separation between the vertical and horizontal viscosity terms. It is therefore impossible to distinguish physical bottom Ekman pumping from numerical lateral viscosity.

M8 (lines 190-192, 216-217): I think it is indeed likely that the near-bottom cross-slope flow dominates near-bottom vertical velocity, but this has not been shown directly. Besides near-bottom flow across isobaths, bottom Ekman pumping can also produce important vertical velocity and vortex stretching. This effect is not examined here because the term is excluded from the analysis and from Equation 2 (the approximately equal sign is an assumption rather than a result). Figure 5c shows that bottom friction may be important in the bottom layer's vorticity budget, though it is unclear because the viscous term combines lateral and vertical friction.

Response: These two comments are related to the viscous term and effect of the bottom Ekman pumping, so we addressed them together.

Due to the magnitude of the horizontal viscosity term is much smaller than the vertical one (Figure R7), it was combined with the vertical term, and we did not separate the two terms. In the revised manuscript, we clarified that this point to avoid misunderstanding:

Line 197-198: The horizontal viscosity is much smaller than vertical viscosity term and they are included in the \overrightarrow{VIS} term for simplicity.

For the Equation (2), following reviewer's suggestion, we examined the effect of the Ekman pumping by modifying it as:

$$\begin{aligned}
 & -\nabla_h \cdot \int_{-H}^z \vec{\bar{V}}_h dz \approx \\
 & -\nabla_h \cdot \int_{-H}^z \vec{\bar{V}}_{h_geo} dz - \nabla_h \cdot \int_{-H}^z \vec{\bar{V}}_{h_vis} dz = \overbrace{-(\bar{v}_{b_geo} H_y + \bar{u}_{b_geo} H_x)}^{CGT_b} + \underbrace{\frac{\beta}{f} \int_{-H}^z \bar{v}_{geo} dz}_{\beta \text{ effect}} \overbrace{-\nabla_h \cdot \int_{-H}^z \vec{\bar{V}}_{h_vis} dz}^{Fric} \quad (2)
 \end{aligned}$$

One more term was added $-\nabla_h \cdot \int_{-H}^z \vec{V}_{h_vis} dz$ (*Fric*), which represent the effect of the bottom Ekman pumping that induced by the bottom stress of the slope current.

As pointed out by the reviewer, the deep layer (Figure R7 and Figure 5c in the manuscript) has quite large vertical viscosity terms. We examined its effect on the deep ζ_DIV_D (ζ_DIV_D), which features a downward flux (negative value) over the northern slope and upward flux (positive value) over the southern part. Generally, the *Fric* has contribution to the deep ζ_DIV_D and features with a relatively uniform downward motion. It has the same direction as the Ekman transport induced by the bottom stress of the deep cyclonic slope current. However, the primary pattern and magnitude of the ζ_DIV_D are determined by the bottom geostrophic cross-isobath transport (CGT_b) (Figure R8).

Additionally, bottom Ekman pumping is induced by bottom frictional stress, which responds to and is only affected by the bottom layer circulation, while the bottom pressure is modulated by the motions of water in the entire water column above it. In this study, we observed that changes in the upper-layer circulation intensify the middle and deep circulations over the slope. The changes in the upper layer circulation may not affect the bottom friction directly but modulate the bottom pressure distribution over the slope. This modulation then leads to the stronger vertical stretching/squeezing within the water column, and in turn impacts the circulation. Thus, in the analysis, we pay more attention to the effect of bottom cross-isobath geostrophic transport.

Following reviewer's concerns, in the revised manuscript, the updated Equation (2) and Figure R8 was adopted, and we mentioned the role of the bottom Ekman pumping.

Line 265-273: For the deep layer, the viscosity term has an important effect in the vorticity budget (Figure 5c). Similarly, the *Fric_D* term contributes to the deep ζ_DIV_D and is characterized by a relatively uniform downward motion (Figure 7d). However, the primary pattern and magnitude of the ζ_DIV_D are largely controlled by the CGT_b that the pressure distribution maintained the mean downwelling in the northern side and the upwelling over the southern slope (Figure 7b, d). Since the *Fric_D* is induced by the bottom frictional stress as response to the deep layer slope current, while the bottom pressure is modulated by the

motions of water in the entire water column above it, we further examine the maintenance of the bottom pressure over the slope

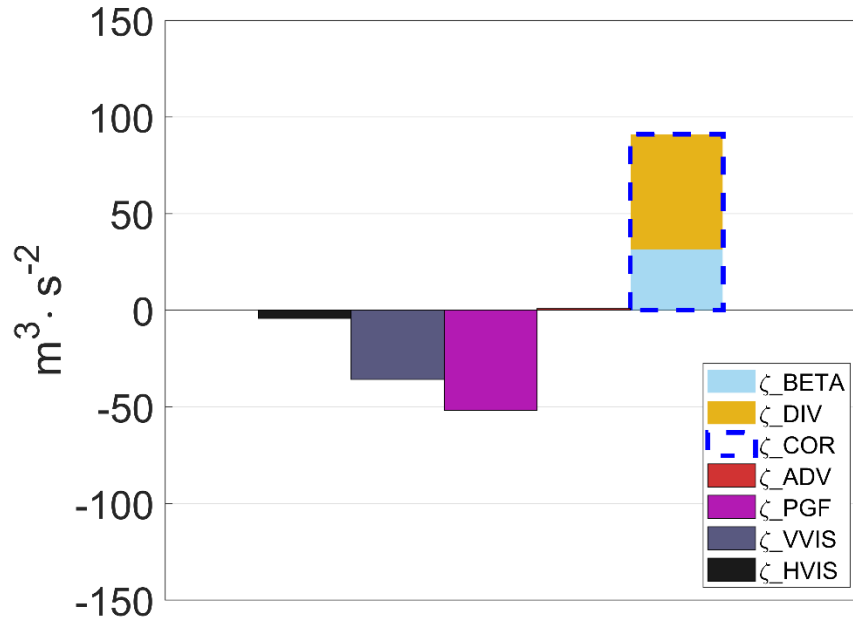


Figure R7. Similar as Figure 5c in the manuscript. The layered-integrated vorticity budget (Equation 1) for the standard case in the layers of 2,500–4,000 m. The ζ_{VIS} is decomposed into the horizontal (ζ_{HVIS}) and vertical (ζ_{VVIS}) component, respectively.

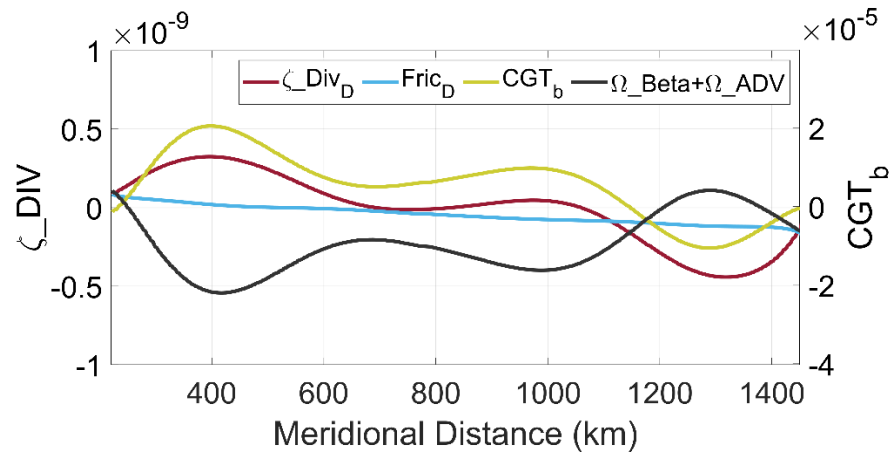


Figure R8. Meridional changes of the ζ_{DIV_D} , $Fric_D$, CGT_b and $\Omega_{BETA} + \Omega_{ADV}$ over the slope. This figure will be used as Figure 7d in the revised manuscript.

M9 (lines 238-240): Source/sink Stommel and Arons-like dynamics does not include topography, so it cannot be consistent with a flow where cross-slope bottom geostrophic flow is dominating the bottom layer dynamics. The only way to test this type of dynamics unambiguously is to perform experiments with a vertical wall (as in the adjacent rectangular basin representing the Pacific) instead of a slope.

Response: Thanks for the reminder from reviewer. Following reviewer's comment, we removed this sentence to avoid misunderstanding.

M10: Since the model has a 5 km resolution, it should be eddy-resolving in the SCS, where the first baroclinic deformation radius is around 60 km in the SCS (e.g., Figure 6 in Chelton et al, 1998 or Figure 8 in LaCasce & Groeskamp, 2020). Because mesoscale eddies and sloping topography are present, a competing theory for the cyclonic layers' flow in a basin like this is eddy-slope interaction (Neptune Effect, e.g., Holloway, 1987, see also Stewart et al., 2024 and references therein). It may be possible to test this hypothesis by changing the horizontal resolution: If by coarsening the grid spacing until eddies are no longer resolved results do not change, then an eddy-free interpretation may be correct. But if the Neptune effect is important in one or both cyclonic layers, these layers will have stronger flow with finer, eddy-resolving resolutions, and the interpretation needs to be revisited.

M11: What is the first baroclinic deformation radius in the model (especially in the SCS's deep basin, and in the SCS's slope)? This information is relevant for addressing point M10 and for comparing how well the model represents the real SCS's stratification.

Response: These two comments are related to the formation dynamics of layered circulation in the SCS, thus we addressed them together.

As a semi-enclosed marginal sea, the circulation in the SCS is closely related to the external flux through the LS. Generally, the cyclonic-anticyclonic-cyclonic circulation in the upper, middle, and deep layers is maintained by the influx-outflux-influx pattern through the LS (Figure R9). The theoretical understanding was obtained based on the potential vorticity

conservation constraint (Yang and Price, 2000; Zhu et al, 2007) or depth-integrated vorticity dynamics (Equation 1 and Figure 5 in the manuscript). In the depth-integrated vorticity dynamics, the net planetary vorticity influx/outflux maintained the cyclonic/anticyclonic circulations in each layer and is mainly balanced by the bottom pressure torque and the bottom friction curl. These insights have provided robust physical explanations for layered circulation in various regions (e.g., Karcher et al., 2007; Zhu et al., 2017; Kastner et al., 2024; Jiang et al., 2024; Li and Gan et, 2023).

When numerical simulations reduce resolution, it may not adequately resolve the slope. As an alternative approach, flat-bottom simulations could be conducted to check the formation of basin circulation without eddy-slope interaction (Figure R10). With flat bottom, the external flux could drive the basin scale circulation, and the direction of this circulation aligns well with predictions from potential vorticity conservation constraint or depth-integrated vorticity dynamics.

In this study, we focused on basin-scale circulation, and those theoretical frameworks effectively explain the processes of basin circulation and the coupling among different layers. Following these frameworks, we examined the mechanisms by which changes in upper-layer circulation modulate layered circulation. We appreciate the reviewer's suggestion to explore the Neptune Effect in future investigations. In the revised manuscript, we have highlighted that the Neptune Effect could be another potential mechanism influencing layered circulation in marginal seas like the SCS. We plan to explore this in our future studies.

Line 355-359: In addition to the processes revealed in this study, other mechanisms, such as the Neptune Effect involving the eddy-slope interaction (e.g., Holloway, 1987, Stewart et al., 2024), may also play a role in influencing circulation dynamics in marginal seas like the SCS. It will be incorporated into our future investigations to improve understanding.

For the deformation radius, following reviewer concern, we calculated the deformation radius using the method of Chelton et al. (1998) (Figure R11). Over the deep basin, the deformation radius is approximately 70 km, consistent with the values reported by Chelton

et al. (1998) and LaCasce & Groeskamp (2020). Over the slope, the deformation radius gradually decreases to approximately 35 km as the depth decreases.

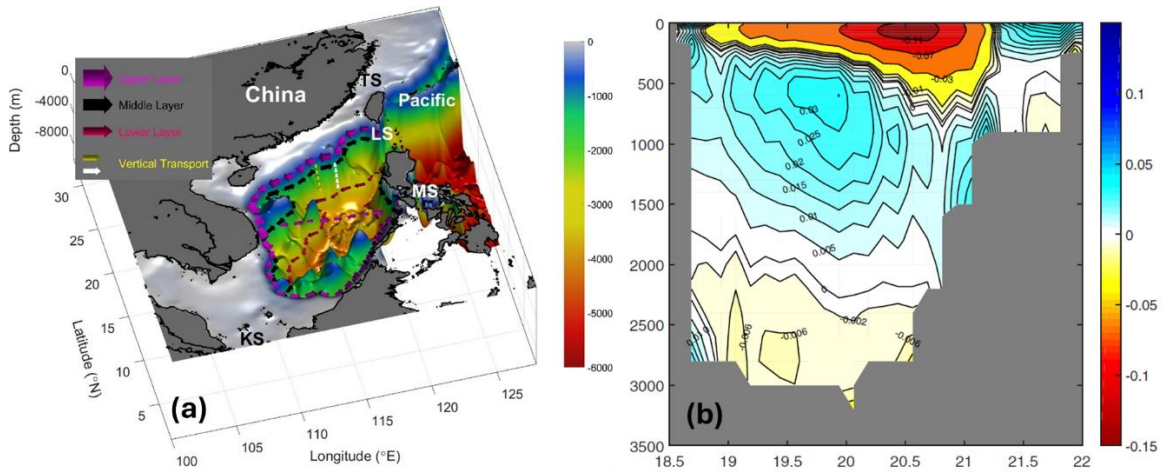


Figure R9. (a) Schematic annual mean CAC circulation in the South China Sea. Color contours represent bathymetry (m). LS: Luzon Strait; TS: Taiwan Strait; MS: Mindoro Strait; and KS: Karimata Strait. (From Cai et al., 2020). (b) zonal geostrophic velocity in the Luzon Strait at 120845'E. Positive values indicate eastward flow in m/s. The dashed lines represent the interfaces of density layers in the Luzon Strait. (From Zhu et al., 2017)

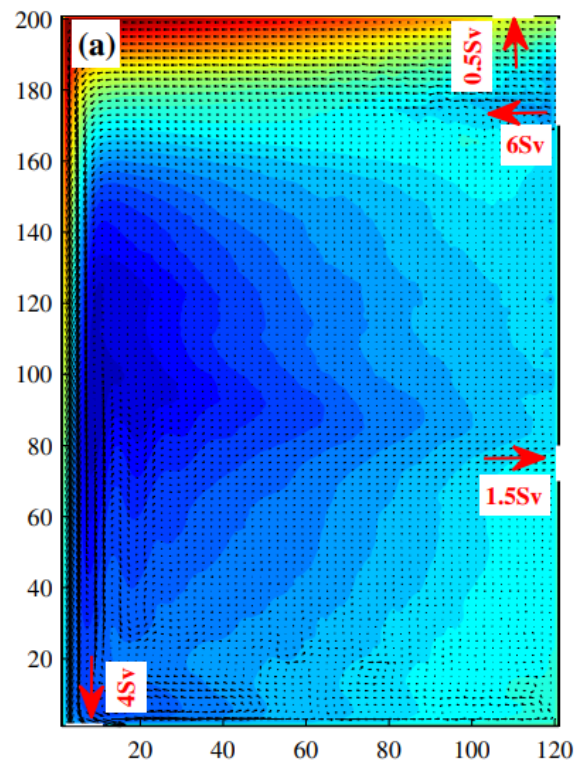


Figure R10. Basin circulation with flat bottom driven by the external flux (From Chen and Xue, 2014)

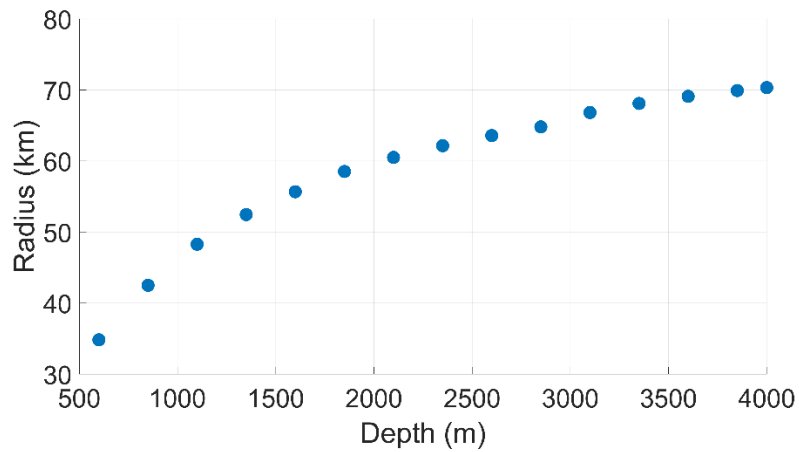


Figure R11. Changes of the first baroclinic deformation radius with the depth over the slope at the latitude of 15.5 N.

Reference:

- Cai, Z., Gan, J., Liu, Z., Hui, C. R., & Li, J. (2020). Progress on the formation dynamics of the layered circulation in the South China Sea. *Progress in Oceanography*, 181, 102246.
- Chen, G., & Xue, H. (2014). Westward intensification in marginal seas. *Ocean Dynamics*, 64, 337-345.
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- Kastner, S. E., G. Pawlak, S. N. Giddings, A. E. Adelson, R. Collin, and K. A. Davis, 2024: The Influence of Caribbean Current Eddies on Coastal Circulation in the Southwest Caribbean Sea. *J. Phys. Oceanogr.*, **54**, 2119–2132, <https://doi.org/10.1175/JPO-D-24-0049.1>.
- Li, J., & Gan, J. (2023). How the forcing dynamics of the western boundary currents in the Pacific respond to the North Equatorial Current. *Progress in Oceanography*, 210, 102950.
- Jiang, H., Xin, X., Xu, H. *et al.* Three-layer circulation in the world deepest hadal trench. *Nat Commun* 15, 8949 (2024). <https://doi.org/10.1038/s41467-024-53370-7>
- Yang, J., Price, J., 2000. Water-mass formation and potential vorticity balance in an abyssal ocean circulation. *J. Mar. Res.* 58 (5), 789–808. <https://doi.org/10.1357/002224000321358918>.
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M12 (lines 322-323, Data Availability statement): The repository in the DOI (<https://doi.org/10.5281/zenodo.13835538>) contains only *.mat files. Based on the file names, I assume these can be used to replot the figures, but they are not sufficient to reproduce the results. To ensure reproducibility, the authors need to provide all the source codes used in the calculations, as well as the configuration files for the ROMS model applications.

Response: We appreciate reviewer's suggestion on the data availability. The .mat files there are the averaged results from the last five years of the model output. For the source codes and configurations, these can be made available upon request to the corresponding author. We revised the Data availability accordingly to ensure clarity, thanks!

Minor points:

m1: (lines 30, 232, 311): The term "Cascading" is typically used to refer to a specific process driven by surface buoyancy loss. To avoid ambiguity, I suggest using "downwelling" instead.

Response: Thanks for the kind suggestions, we corrected it as downwelling in the revised manuscript.

m2 (lines 94-95): Is the southern model strait the same depth as the Luzon Strait?

Response: The southern strait is quite shallow with a depth of ~400 m. We clarify it in the revised manuscript.

Line 106-107: The SCS was opened to the south with the depth of 400 m (Figure 2a), to allow the upper-layer intrusion to develop intrinsically during the simulation

m3: Figure 1: The real topographic gradients in the SCS are more difficult to see with these color limits. It may be better to change the lower limit to something closer to 4 km, even though this would saturate the color scale in the Western Pacific troughs.

Response: Thank you for your suggestion regarding the colormap in Figure 1. We understand that adjusting the lower limit to approximately 4 km could enhance the visibility of topographic gradients in the South China Sea (SCS). However, such a change would result in the saturation of the color scale in other regions

Given that we have included transects to illustrate the slope, we prefer to maintain the original colormap. Thanks.

m4 (line 292): Stimulated or simulated?

Response: Thanks for your careful review. We have corrected it to "simulated" in the revised manuscript.

m5 (line 303): "curved" is probably a better description, Since the basin is circular.

Response: Thanks for kind suggestion, we corrected it as curved in the revised manuscript.

m6 (Figures 6, 7 and others): Several axes are missing labels, units, or both.

Response: We correct those figures, thanks so much!

m7 (Figure 6d): It may be better to flip Figure 6d 90 degrees clockwise to have depth in the y-axis.

Response: Thank you for the kind suggestion. We intentionally used the horizontal axis to represent depth, so that the transition from left to right corresponds to moving from shallow to deep regions, being similar as the horizontal map.

References:

Chelton et al. (1998): Geographical Variability of the First Baroclinic Rossby Radius of Deformation, *Journal of Physical Oceanography*.

LaCasce & Groeskamp (2020): Baroclinic Modes over Rough Bathymetry and the Surface Deformation Radius, *Journal of Physical Oceanography*.

Holloway (1987): Systematic forcing of large-scale geophysical flows by eddy-topography interaction, *Journal of Fluid Mechanics*.

Stewart et al. (2024): Formation of eastern boundary undercurrents via mesoscale eddy rectification, *Journal of Physical Oceanography*.