



1 **Tide-Surge Interaction near Singapore and Malaysia using** 2 **a Semi-empirical Model**

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11 **Abstract.** Tide-surge interaction (TSI) plays a substantial role in determining the characteristics of surges
12 over shallow regions. A variety of approaches have been used to study TSI globally, and TSI have been
13 found to occur in Singapore and the east coast of Peninsular Malaysia. However, the characteristics of
14 TSI in Singapore and the east coast of Peninsular Malaysia have yet to be studied in detail. We study the
15 TSI at seven tide gauges along the east coast of Peninsular Malaysia and Singapore. Here, we propose a
16 modified statistical framework that accounts for irregularity in the tidal cycle. We find evidence of TSI
17 at all seven locations, with characteristics varying smoothly along the coastline: the highest non-tidal
18 residuals are found to occur most frequently before tidal high water at the southern region of this coastline
19 and in Singapore, both before and after tidal high water in the middle of the coastline, and after tidal high
20 water at the northern region. We also propose a semi-empirical model to investigate the effects of tidal
21 phase alteration, which is one the mechanisms of TSI. Results of our semi-empirical model reveal that
22 tidal phase alteration caused by wind-driven surges is substantial enough to generate significant change
23 in the timing of the largest surges.

24 **Short summary**

25 Identifying tide-surge interaction (TSI) can be a complex task. We enhance existing statistical methods
26 with a more robust test that accounts for complex tides, and investigate the influence of tidal phase



27 alteration on TSI using a semi-empirical model. We apply these techniques to tide-gauge records from
28 the east coast of Singapore and Malaysia. We found TSI at all studied locations, and that tidal phase
29 alteration can change the timing of large surges with minimal impact on their height.

30 **1 Introduction**

31 Coastal regions are vulnerable to the combined effects of tides and surges, which can induce significant
32 sea-level variations and pose substantial risks to coastal communities and ecosystems (Hsiang et al., 2017;
33 Diaz, 2016; von Storch et al., 2015; Hinkel et al., 2014). The height of large storm surges can be amplified
34 by high tides if they coincide, increasing the risk of coastal flooding and threatening lives and properties.
35 The likelihood and impact of such destructive events are further aggravated by sea-level rise (Sreeraj et
36 al., 2022; Calafat et al., 2022; Marcos and Woodworth, 2017; Feng et al., 2015; Woodworth and
37 Blackman, 2004). To identify the appropriate response to such events, we must understand the
38 fundamental processes and their mutual interactions.

39 A dependence between tides and surges has long been noticed at coastal locations (Keers, 1968),
40 and recognised to be caused by interaction between tides and surges (Pugh and Vassie, 1978; Wolf, 1978).
41 This interaction is non-linear and can lead to complex coastal dynamics characterized by amplification or
42 attenuation of water levels, which are influenced by local bathymetry, coastline geometry, and
43 atmospheric conditions (Idier et al., 2019). Strong tide-surge interaction has been observed in shallow
44 waters and estuaries (Wolf, 1981). The main mechanism behind tide-surge interaction is mutual phase
45 alteration (Rossiter, 1961). The generation of surges over a water body is influenced by the depth of the
46 water body. As changes in depth occur partially due to tides, the height of surges can be influenced by
47 tides. The propagation speed of tides is also dependent on depth, which can change due to surges
48 (Proudman, 1957, 1955). Further studies that analysed shallow-water equations along the coast found that
49 the non-linear tide-surge interaction is caused by the advection term, non-linear bottom friction term, and
50 the non-linear shallow water effects of the shallow-water equations (Zhang et al., 2021; Idier et al., 2012).

51 Studies of tide-surge interaction have employed a range of modeling approaches, including
52 statistical methods (Arns et al., 2020; Haigh et al., 2010; Dixon and Tawn, 1994), numerical models
53 (Costa et al., 2023; Yang et al., 2023; Horsburgh and Wilson, 2007; Prandle and Wolf, 1978), and



54 analytical models (Horsburgh and Wilson, 2007). Horsburgh and Wilson (2007) provided a simple
55 mathematical explanation for the abundance of large non-tidal residuals at timings halfway up the rising
56 tide and down the falling tide. Dixon and Tawn (1994) proposed a statistical framework where they split
57 the tidal range into five equiprobable bands and used a chi-square test to determine whether residuals
58 above a height threshold fall uniformly into each band. Horsburgh and Wilson (2007) proposed a modified
59 version of the framework where the tide is instead split into 13 hourly bands between 6.5 hours before
60 and after tidal high water (HW).

61 Application of such frameworks revealed that extreme residuals are most often found 3–5 hours
62 before HW in the Bay of Bengal (Antony and Unnikrishnan, 2013) and the North Sea (Horsburgh and
63 Wilson, 2007), and typically about 2 hours before HW in the English Channel (Haigh et al., 2010). In
64 China and New Zealand, observed tide-surge interaction varies along the coastline: the frequency of
65 extreme residuals peaks before HW at certain locations, after HW at others, and is independent of tides
66 at the remaining locations (Costa et al., 2023; Feng et al., 2019). Numerical models have shown that the
67 inclusion of tide-surge interaction often results in better water level predictions, especially over coastal
68 and shelf waters, whereas the omission of the interaction may lead to under or overestimation of surges
69 at certain locations (Fernández-Montblanc et al., 2019; Idier et al., 2012). For example, Antony et al.
70 (2020) showed that numerically modelled peak water levels generated during Cyclone Aila at the head of
71 the Bay of Bengal would have been overestimated if tide-surge interaction was not simulated.

72 Tide-surge interaction in the regional waters surrounding Singapore has previously been studied
73 using hydrodynamic models. Using the Finite Volume Coastal Ocean Model (Chen et al., 2003), Chen et
74 al. (2012) found that tide-surge interaction is negligible during large surges and mainly contributes by
75 altering the time of tidal high and low water. Using a multi-scale modelling approach, Kurniawan et al.
76 (2015) found tide-surge interaction to be important when simulating non-tidal barotropic flow. Kurniawan
77 et al. (2015) recommend the inclusion of tide-surge interaction in operational forecast models to produce
78 more accurate tides and surges. When applying a data-driven modelling approach, Kurniawan et al. (2014)
79 also found that the tidal cycle influences non-tidal residuals.

80 Here, we focus on investigating tide-surge interaction at seven tide gauge locations near Singapore
81 and the east coast of Peninsular Malaysia using modified statistical methods and a new semi-empirical



82 model. The typical wave height is 0.5–1.5 m (Yaakob et al., 2016; Marzin et al., 2015). Our analysis
83 found that that tides in this region can reach 2.7–3.6 m and the largest non-tidal residuals over the past 30
84 years exceed 0.8 m. Understanding how these components interact and combine provides insight into the
85 contributors to coastal water levels. Hydrodynamical processes have a strong influence on the water levels
86 at the seven tide gauges (Tay et al., 2016; Luu et al., 2016; Kurniawan et al., 2015; Karri et al., 2014;
87 Tkalic et al., 2013a; Chen et al., 2012). The seven gauges are located within the Sunda Shelf, which has
88 typical depth of 40–80 m. The shallowness of this shelf likely enhances the interaction between tide and
89 surge, and its expanse allows for phase changes in the tides to compound as the tide propagates across the
90 shelf. Our research objectives are (1) examining the tide gauge records to characterise the tide-surge
91 interaction at each individual tide gauge location and the spatial pattern across locations, and (2)
92 explaining the observed interaction characteristics through a simple semi-empirical model.

93 We apply a modified version of the statistical method by Horsburgh and Wilson (2007) to
94 determine the presence of tide-surge interaction at each tide gauge location and to characterise these
95 interactions. The existing method groups residuals above a height threshold into 13 hourly bands between
96 6.5 hours before and after HW and compares the resulting distribution to the uniform distribution using a
97 chi-square test. However, as the duration and skewness of the tidal cycle can vary from cycle to cycle,
98 the uniform distribution is not the most suitable null distribution. Our key modification to the existing
99 methodology is to replace the uniform distribution with a “No-TSI distribution” as the null distribution.
100 Due to variation in the duration of each tidal cycle, the No-TSI distribution is generally not uniform. A
101 distinction between the No-TSI distribution and a uniform distribution should be made especially at
102 locations with mixed tides, where the duration of tidal cycles can vary significantly. We compare the tide
103 gauge data to the No-TSI distribution using an exact statistical test using bootstrapping instead of the chi-
104 square test. In addition, we propose a simple approach to compare the tide-surge interaction across
105 locations that have different tidal characteristics (diurnal, mixed, semidiurnal).

106 We aim to provide an explicit explanation of the observed tide-surge interaction through our semi-
107 empirical model by combining historical tide and surge data with winds, coastal geometry, and
108 bathymetry. The semi-empirical model accounts for the mechanism of tidal phase alteration: wind-
109 induced surges perturb the depth of the water body which influences the propagation speed of the tide.



110 This results in differences between observed tides and tides predicted from harmonic analysis, which are
111 detected as non-tidal residuals. We aim to use our model to show that this mechanism can significantly
112 influence the timing of extreme residuals to produce signals of tide-surge interaction.

113 **2 Data and methods**

114 **2.1 Tide gauge data, tides and residuals**

115 Hourly water level from tide gauges at seven locations (Fig. 1) along the east coast of Peninsular Malaysia
116 and Singapore are obtained from the University of Hawaii Sea Level Center (Caldwell et al., 2001).
117 Details of the tide gauges are tabulated in Table 1. Observations have been made over at least 29 years at
118 each location with a data completion rate of 95–99 %. The length of these records is close to the 30-year
119 threshold typically considered the minimum length required for analysis of extreme sea levels
120 (Rasmussen et al., 2018). Nonetheless, within Southeast Asia, these stations have some of the longest
121 records.

122 To compute the tidal level and non-tidal residuals, we use the equation

123

$$124 \quad X(t) = Z(t) + T(t) + R(t). \quad (1)$$

125

126 $X(t)$ is the hourly water level recorded by a tide gauge at time t . $Z(t)$ is the 1-year (8766-hour after
127 accounting for leap years) moving average of $X(t)$. A 1-year window was chosen because intra-annual
128 behaviour of residuals is well understood to be periodic due to seasonal variations, and its influence on
129 residuals are of interest in this study (Tkalic et al., 2013b). The 1-year moving average is calculated only
130 if at least 85 % of the data in the 8766-hour window is available. This reduces our usable data to 87–99
131 % across the seven locations. $T(t)$ is the tidal level which we estimate using UTide, a tidal harmonic
132 analysis package implemented in Matlab (Codiga, 2011). $X(t) - Z(t)$ is split into two equal halves based
133 on the start and end dates in Table 1 and used as inputs to UTide, as UTide does not recommend using
134 records longer than 18.6 years as input. UTide was used to identify the amplitudes and phases of 66 tidal
135 constituents with periods of up to 32 days through harmonic analysis. Constituents with a signal-to-noise



136 ratio of at least 2 are used to construct $T(t)$. $R(t)$, the residual, is then estimated as $R(t) = X(t) - Z(t) -$
137 $T(t)$. We denote the residual obtained through this procedure as R_{gauge} .

138 A summary of the tidal characteristics at the seven locations is tabulated in Table 2. The tides at
139 these locations lie within the microtidal (<2 m) and mesotidal (2–4 m) ranges with diurnal tidal ranges of
140 close to 2 m except at Cendering and Geting where diurnal tidal ranges are 1.5 m and 0.8 m respectively.
141 The daily tidal range can be as large as 3.6 m at Johor Baharu and Kuantan. In a shelf with a depth of 40–
142 80m, tides of such magnitude cause water depth to deviate from its mean by up to about $\pm 4\%$. The
143 periodicity of tides at a location can be described by the tidal form factor F which compares the relative
144 importance of the following diurnal and semidiurnal tidal constituents (Pugh and Woodworth, 2014a):

$$145 \quad 146 \quad F = \frac{K_1 + O_1}{M_2 + S_2}. \quad (2)$$

147
148 A common classification considers a location with a factor of <0.25 to be semidiurnal, 0.25–1.50 to be
149 mixed with mainly semidiurnal tides, 1.50–3.00 to be mixed with mainly diurnal tides and >3.00 to be
150 diurnal (Pugh and Woodworth, 2014a). Based on this classification, the tides at all stations are identified
151 to be mixed, with Cendering and Geting being mainly diurnal while all other stations to the south are
152 mainly semidiurnal.

153 **2.2 Identifying tide-surge interaction**

154 To determine whether tide-surge interaction is present at each of the seven tide gauge locations, we apply
155 a modified version of the statistical method by Horsburgh and Wilson (2007) on the processed tide gauge
156 records (Sect. 2.1). This method compares the timing of extreme residuals to the nearest HW.

157 To identify extreme residuals, the 99th percentile and above of residuals are longlisted. There are
158 many clusters of residuals in the longlist, where the residuals within each cluster are consecutive
159 measurements, each measured 1 hour from the last. The largest residual in each cluster is shortlisted and
160 sorted. Starting from the largest, shortlisted residuals are added to the set of extreme residuals unless the
161 residual was measured within 1 week (168 hours) of another extreme residual within the set. Some other
162 thresholds used in published studies range from 12–60 hours (Arns et al., 2020; Feng et al., 2019;



163 Rasmussen et al., 2018; Buchanan et al., 2016; Horsburgh and Wilson, 2007). We choose a threshold of
164 168 hours to reduce the odds of double counting long-lasting surges while still retaining enough
165 observations to infer statistical conclusions.

166 To compare locations with predominantly semidiurnal tides with locations with predominantly
167 diurnal tides, we split the extreme residuals into two groups. We define a tidal cycle as the duration from
168 one local minima in $T(t)$ to the observation immediately preceding the next local minima as illustrated
169 in Fig. 2b. One group of extreme residuals were observed during tidal cycles of 21 hours or shorter,
170 representing extreme residuals that occurred during semidiurnal cycles. The other group contain extreme
171 residuals observed during tidal cycles of at least 22 hours, representing extreme residuals that had
172 occurred during diurnal tides. This separation between 21-hours-or-less and 22-hours-or-more was chosen
173 based on the characteristics of the duration of tidal cycles at the seven locations, where the distribution of
174 the duration of tidal cycles were found to be bimodal at each location and the 22-hour mark tends to
175 distinguish the two modes (Fig. S1).

176 The HW in the same tidal cycle as each extreme residual is identified and the timing difference
177 between the extreme residual and the respective HW is quantified at hourly resolution. Across the set of
178 extreme residuals, the frequency of extreme residuals found a certain number of hours relative to HW, h ,
179 is counted. This frequency is plotted as a *frequency distribution* in the form of a histogram (Fig. 3). Box
180 plots below the histograms show the median and its 95 % confidence interval, the interquartile range
181 (IQR), a range that extends up to $1.5 \times \text{IQR}$ from the limits of the IQR, and the outliers (Fig. 3).

182 We use the frequency distribution to test the null hypothesis that assumes that there is no tide-
183 surge interaction. To do so, we test whether the frequency distribution is drawn from a null distribution
184 representing a scenario where extreme events are equally likely to occur at any stage of a tidal cycle.

185 **2.3 No-Tide-Surge Interaction distribution**

186 In existing studies, a uniform distribution is chosen as the null distribution (Horsburgh and Wilson, 2007;
187 Haigh et al., 2010; Antony and Unnikrishnan, 2013; Feng et al., 2019; Costa et al., 2023). However, the
188 uniform distribution is not the most suitable null distribution to represent the null hypothesis. Instead, we
189 propose a “No-Tide-Surge Interaction distribution” or “No-TSI distribution” as the null distribution. The



190 No-TSI distribution is the *expected* frequency distribution in the absence of tide-surge interactions. Figure
191 2 illustrates how this distribution is obtained. The No-TSI distribution is empirically derived from $T(t)$,
192 the tidal level obtained by applying UTide to the tide gauge records at each location. It is a distribution
193 that depends on the local tidal characteristics and hence is location specific. For a given location, the null
194 distribution is generally non-uniform because the length of the tidal cycle varies. For example, tidal cycles
195 of 14 hours or longer are relatively rare at Tanjong Pagar, so randomly selected times that occur at 7 hours
196 from the nearest tidal HW will also be relatively rare (Fig. 3a). This leads to non-uniform sampling of the
197 number of hours from the nearest tidal HW. The No-TSI distribution corresponds to uniform sampling in
198 time, which is non-uniform with respect to the number of hours from the nearest tidal HW. Thus, the No-
199 TSI distribution is obtained by counting the number of tide-gauge observations found at a certain number
200 of hours relative to HW as illustrated in Fig. 2.

201 The No-TSI distribution allows us to account for the complex mixed tides at each location, which
202 causes the tidal cycles at the coast to have a period of any duration from 8 to 26 hours (Fig. S1). Let $f(h)$
203 be the number of tide gauge measurements collected at h hours from HW. Assuming independence
204 between tide and surge, the probability that an extreme event will be found at h is $p_h = f(h)/\sum_h f(h)$:
205 the normalized frequency of $f(h)$ at h . Note that p_h is a probability mass function over the domain h . Let
206 n be the number of extreme events that occurred at this tide gauge over its length of records. Assuming
207 that extreme events are mutually independent, the probability that k out of n extremes are found at h
208 hours from HW is $C_k^n p_h^k (1 - p_h)^{n-k}$ where C_k^n is the binomial coefficient. This is the binomial
209 distribution $\sim \text{Bin}(n, p_h)$. The No-TSI distribution at h is the mean of this binomial distribution, np_h .
210 This means that the No-TSI distribution is the probability mass function p_h multiplied by n , and
211 conversely p_h is the normalized No-TSI distribution such that $\sum_h p_h = 1$. We use the 2.5th and 97.5th
212 percentiles of the binomial distribution at each h to obtain the 95% confidence interval of the No-TSI
213 distribution. For testing the null hypothesis, a bootstrapping method is used to calculate p -values
214 (Appendix A).



215 2.4 Semi-empirical model

216 One effect of tide-surge interaction is tidal phase alteration, where surge-caused increase in water depth
217 advances the timing of HW. The aim of our semi-empirical model is to investigate the first-order effects
218 of phase alteration on the height and timing of residuals due to wind-driven surges. Singapore and the
219 east coast of Peninsular Malaysia are located within the Sunda Shelf and lies to the west of the Riau
220 Islands and southwest of the South China Sea (Fig. 1). The typical bathymetry of 40–80 m in this region
221 of the Sunda shelf terminates at about 700 km away from the coast, declining steeply at the edge of the
222 Sunda Shelf where it borders the South China Sea that have depths of 4,000 m and deeper. The unique
223 topography of this region with an extensive area that is shallow and relatively uniform in depth has led
224 us to adopt a simplified version of the sea-level gradient equation to estimate surge using wind velocity:

$$225 \frac{\partial \zeta}{\partial x} = \frac{\rho_{\text{air}} C_d |\mathbf{W}| \mathbf{W} \cdot \hat{\mathbf{x}}}{\rho g D}, \quad (3)$$

226
227 where we have assumed that the coastal sea is shallow enough to keep only terms with water depth in the
228 denominator but is deep enough to justify ignoring bottom stress (Pugh and Woodworth, 2014b). In Eq.
229 (3), ζ is the sea level and x is spatial displacement in a specified direction, making $\partial \zeta / \partial x$ the sea-level
230 gradient along x . ρ_{air} is the density of air, C_d is the drag coefficient at the sea surface, ρ is the density of
231 seawater, g is the gravitational acceleration, D is the undisturbed water depth, \mathbf{W} is the wind velocity
232 vector, and $\hat{\mathbf{x}}$ is a unit vector parallel to x . Winds over central South China Sea have been found to be the
233 main determining factor of hourly water level variations in the Singapore Strait (Tkalic et al., 2013a).
234 To compare the wind-driven surge at the seven tide gauge locations of interest, we assume that the surges
235 at these locations result from winds over the same region of the shallow shelf. For our semi-empirical
236 model, we use the region that is bounded by the red rectangle in Fig. 1, masking out land. A rectangular
237 region was chosen for simplicity, with one edge passing through the Tanjong Pagar and Geting gauge
238 locations and the remaining three edges encompassing as much of the shallow shelf as possible. The edges
239 of the rectangle parallel to the Malaysian coast are roughly 833 km long and are separated by a longitude
240 of 6.5° , making the edges perpendicular to the coast roughly 759 km long. Note that x in Eq. (3) is defined



242 to be parallel to these perpendicular edges. Using bathymetry from the General Bathymetric Chart of the
243 Oceans (GEBCO Compilation Group, 2023), we find that $D = 58$ m within the bounded region (after
244 masking out grid boxes over land). This was obtained by averaging the bathymetry values within the red
245 rectangle (Fig. 1). In this region, $g = 9.78 \text{ ms}^{-2}$.

246 To estimate the wind-driven surge, we assume that ρ_{air} , C_d , ρ , g and D are spatially and
247 temporally homogeneous over the bounded region and that C_d is independent of wind speed (Wróbel-
248 Niedzwiecka et al., 2019). We also assume that the spatial average of \mathbf{W} captures the first-order influence
249 of regional winds on surge through averaging the wind components over the bounded region. These
250 approximations allow us to easily integrate Eq. (3) with respect to x over the length of $L_{\text{wind}} = 759$ km
251 to estimate the wind-driven surge. Surges are not only a product of instantaneous winds but are also
252 partially a result of winds over a past number of hours. To account for the time taken for the winds over
253 the bounded region to cause surges at the tide gauge locations, we use a 25-hour running average of
254 $|\mathbf{W}|\mathbf{W} \cdot \hat{\mathbf{x}}$ to estimate the wind-driven surge. The 25-hour averaging also serves to average out the
255 dependence of D on tides, providing additional justification on our homogeneity assumption of D . Based
256 on those assumptions, we estimate the wind-driven surge, R_{wind} , as:

257

$$258 \quad R_{\text{wind}} = \frac{\partial \zeta}{\partial x} L_{\text{wind}} = k L_{\text{wind}} \overline{|\langle \mathbf{W} \rangle_A| \langle \mathbf{W} \rangle_A \cdot \hat{\mathbf{x}}}, \quad (4)$$

259

260 where \mathbf{W} is the wind velocity with its zonal (u) and meridional (v) components obtained from the hourly
261 10m winds of ERA5 (Hersbach et al., 2018), $\langle \mathbf{W} \rangle_A$ represents a spatial average of \mathbf{W} over the area
262 bounded by the red rectangle in Fig. 1 (after masking out grid boxes over land), $\hat{\mathbf{x}}$ is a normal vector along
263 x pointing towards the Malaysian coast as shown in Fig. 1, $\overline{|\langle \mathbf{W} \rangle_A| \langle \mathbf{W} \rangle_A \cdot \hat{\mathbf{x}}}$ represents a 25-hour moving
264 average of $|\langle \mathbf{W} \rangle_A| \langle \mathbf{W} \rangle_A \cdot \hat{\mathbf{x}}$, and $k = \rho_{\text{air}} C_d / \rho g D$. Plotting $\overline{|\langle \mathbf{W} \rangle_A| \langle \mathbf{W} \rangle_A \cdot \hat{\mathbf{x}}}$ against R_{gauge} , the residuals
265 obtained empirically from tide gauges (Sect. 2.1), at all seven locations reveal a correlation of 0.7–0.8
266 (Fig. S2). This leads us to fit the running average of $\overline{|\langle \mathbf{W} \rangle_A| \langle \mathbf{W} \rangle_A \cdot \hat{\mathbf{x}}}$ to the residuals using a simple linear
267 regression to obtain the constant k and our estimate for R_{wind} at each location.



268 With the speed of tidal waves given by $c = \sqrt{gD}$ (Pugh and Woodworth, 2014b) and treating
269 R_{wind} as a perturbation to the undisturbed water depth D , the tide advancement time caused by a change
270 in D due to R_{wind} is

$$272 \Delta t = \frac{L_{\text{tide}}}{\sqrt{gD}} - \frac{L_{\text{tide}}}{\sqrt{g(D+R_{\text{wind}}/2)}} \approx \frac{L_{\text{tide}} R_{\text{wind}}}{\sqrt{gD} 4D}, \quad (5)$$

273

274 where L_{tide} is the distance travelled by the tidal wave under the influence of R_{wind} . The approximation
275 assumes that $R_{\text{wind}} \ll D$. We also assume that the tides travel straight towards the coast in the direction
276 of \hat{x} , allowing us to equate $L_{\text{tide}} = L_{\text{wind}}$. We then calculate the effects on residual height due to tide
277 advancement from R_{wind} as $R_{\text{phase}} = T(t + \Delta t) - T(t)$. R_{phase} can be viewed as a phase shift in the
278 tidal levels, where extreme R_{phase} tend to cluster on the rising or falling tides instead of during tidal high
279 or low water (Horsburgh and Wilson, 2007). Finally, we use the procedure described in Sect. 2.2 to obtain
280 the timing of extreme R_{wind} , R_{phase} and $R_{\text{sum}} = R_{\text{wind}} + R_{\text{phase}}$ relative to HW and their frequency
281 distributions.

282 3 Results and discussion

283 3.1 Observed tide-surge interaction

284 We found evidence of tide-surge interaction at each location, where the frequency distributions deviate
285 significantly from their respective No-TSI distribution (Fig. 3). Based on how we have defined extremes,
286 we find that extreme residuals are unlikely to happen close to HW. This means that while the residuals
287 exceeding the 99th percentile can occur close to HW, the peak of each cluster of exceedances is unlikely
288 to be found in the time window close to HW. Across the locations, this time window generally begins 2–
289 3 hours before HW and ends 3–5 hours after HW. Beyond this time window, the frequency of extreme
290 residual increases, giving us frequency distributions that are mostly bimodal. At the four southernmost
291 stations, the primary mode is found before HW: at -5 hours at Tanjung Pagar and Sedili, at -6 hours at
292 Johor Baharu and at -7 hours at Tioman. Outside Southeast Asia, similar signals have been found at Port



293 Otago in New Zealand (Costa et al., 2023), Shijiusuo, Lianyungang and Xiamen along the coast of China
294 (Feng et al., 2019), Hiron Point at the Bay of Bengal India (Antony and Unnikrishnan, 2013), and
295 Aberdeen, North Shields, Immingham, Cromer and Sheerness at the North Sea (Horsburgh and Wilson,
296 2007). At Kuantan, Cendering and Geting, the primary mode is found after HW, at +6, +6 and +4 hours
297 respectively. Outside Southeast Asia, such signals have appeared less commonly but have been found at
298 Onehunga in New Zealand (Costa et al., 2023) and at Kaohsiung and Zhapo in China (Feng et al., 2019).

299 In a separate quantitative test, we perform significance testing using the bootstrapping method
300 described in Appendix A with 1,000,000 bootstrap samples. To account for family-wise error rate due to
301 our multiple comparisons at seven locations, we apply the Bonferroni correction to our chosen
302 significance level of 0.05 and require a p -value below $0.05/7 = 0.007$ to reject the null hypothesis. We
303 find that the p -value of obtaining the frequency distribution from the No-TSI distribution is below the
304 required level at all seven locations, allowing us to reject the null hypothesis that the frequency
305 distribution was drawn from the No-TSI distribution at a significance level of 0.05 (Fig. S3). This provides
306 further evidence supporting the presence of tide-surge interaction during semidiurnal tides at all seven
307 tide gauge locations studied.

308 Comparing our results from the seven tide gauges along the Singapore and Malaysian east coast,
309 we find a spatial pattern in the tide-surge interaction. At the southernmost stations of Tanjong Pagar,
310 Johor Baharu and Sedili, the mass of the frequency distribution is heavily concentrated around their
311 primary modes, which are found before HW. At Tioman, the primary mode is still found before HW, but
312 the secondary mode has a distinctly heavier weight than the previous three stations. At Kuantan, tide-
313 surge interaction has crossed over to another regime where the primary mode occurs after HW, but the
314 secondary mode found before HW still carries comparative weight. At Cendering and Geting, the
315 northernmost stations, the primary mode after HW is much heavier than the secondary mode before HW.
316 This spatial pattern can also be seen using the box plots, which are compiled in Fig. 4. The tight
317 interquartile range at Tanjong Pagar, Johor Baharu and Sedili shows that the mass of their frequency
318 distributions is concentrated at -6 to -4 hours relative to HW. The larger interquartile range at Tioman
319 shows that there is a more equal mass between the two modes, with the median at -5 hour revealing that
320 the distribution is still heavier towards the negative values. The opposite is true at Kuantan, with its similar



321 interquartile range to Tioman but with its median at +0.5 instead. At Cendering and Geting, the lower
322 quartile is closer to HW, showing that the difference in relative mass between the two modes has
323 increased.

324 During diurnal tides, we found no extreme residuals at Tanjung Pagar, Johor Baharu and Sedili.
325 Few extreme residuals were found during diurnal tidal cycles at Tioman and Kuantan, while many were
326 found at Cendering and Geting (Fig. S4). This is expected as Cendering and Geting experience mainly
327 diurnal tides, in contrast to the other locations. Two observations are available at Tioman, which are too
328 few to confidently determine the presence of tide-surge interaction even though both observations were
329 found at least 6 hours after HW. The same can be said for Kuantan, where seven observations are available
330 and were mostly found at least 6 hours after HW. Nonetheless, we calculate their p -values and compare
331 them to $0.05/4 = 0.0125$. We find that their p -values are insufficient to reject the null hypothesis that
332 the observed frequency distribution was drawn from the No-TSI distribution at a significance level of
333 0.05 and fails to provide evidence of tide-surge interaction during diurnal tidal cycles at these two
334 locations. At Cendering and Geting, we continue to see the pattern where extreme residuals are unlikely
335 to happen close to HW. This leads to a bimodal distribution with the primary modes at both locations
336 found after HW, like their semidiurnal counterparts. The mode is 14 hours after HW at Cendering and 13
337 hours after HW at Geting. Respective p -values provide evidence of tide-surge interaction at both locations
338 (Fig. S5).

339 3.2 Semi-empirical model results

340 We obtain R_{wind} by fitting $\overline{|\langle W \rangle_A| \langle W \rangle_A} \cdot \hat{x}$ to the tide gauge residuals as described in Sect. 2.4. R_{wind}
341 has a correlation of 0.7–0.8 with the tide gauge residuals (Fig. S2). This corresponds to an explained
342 variance (coefficient of determination) of 0.5–0.6. This suggests R_{wind} is an adequate proxy of wind-
343 induced surges.

344 We obtain the timing of extreme R_{wind} using the procedure described in Sect. 2.2 and compare it
345 to its No-TSI distribution to determine whether there is any dependence between R_{wind} and tide. The
346 reason for doing so is to show that the observed dependence between R_{gauge} and tide is not caused by any
347 correlation between wind and tide, which are generated by independent processes. The validation of this



348 assumption would imply that the observed dependence between R_{gauge} and tide is not caused by possible
349 correlation to a common third independent variable, but that tide-surge interaction is indeed present. We
350 find that the resulting frequency distributions for R_{wind} do not deviate significantly from their No-TSI
351 distribution and provide no evidence of dependence between R_{wind} and tide (Fig. S6–S9), indicating the
352 absence of such an independent variable.

353 To estimate the influence of tidal phase modulation, we compute Δt using Eq. (5) and then
354 calculate $R_{\text{phase}} = T(t + \Delta t) - T(t)$ (Sect. 2.4). We apply the procedure of Sect. 2.2 to obtain the
355 extremes of R_{phase} and find a clear dependence between R_{phase} and tide (Fig. S10–S13). During semi-
356 diurnal tidal cycles, extreme values of R_{phase} are most found 2–4 hours before HW at all seven locations
357 (Fig. S10). During diurnal cycles, extreme values are most found 3–5 hours before HW (Fig. S12). As
358 with R_{gauge} and R_{wind} , no extremes were found during diurnal cycles at Tanjong Pagar, Johor Baharu
359 and Sedili.

360 The prevalence of extreme R_{phase} within a narrow window of time relative to HW is due to R_{phase}
361 being largest at 1/4 of a tidal cycle before HW, as illustrated in Fig. S14. As the natural period of a semi-
362 diurnal tidal cycle is about 12–13 hours, a sinusoidal tidal waveform has the steepest gradients about 3
363 hours from its local maxima. This results in the tidal waveform having the greatest difference from a
364 slightly horizontally displaced copy at close to 3 hours from HW. This mechanism is described in detail
365 by Horsburgh and Wilson (2007).

366 However, extreme values of R_{phase} are not generally found at 6 hours before HW during diurnal
367 tides. This is because a sinusoidal wave with amplitude A and frequency ω has a gradient that is
368 proportional to the product $A\omega$. Since semidiurnal components of tides have about twice the frequency
369 of their diurnal counterparts, diurnal constituents need to have at least twice the amplitude of semidiurnal
370 constituents to have the same or stronger influence on R_{phase} . While the tides at Cendering and Geting
371 are mainly diurnal, the amplitude of the diurnal constituents is less than twice that of the semidiurnal
372 constituents (Table 2). Therefore, the semidiurnal signal has a stronger influence on the timing of extreme
373 R_{phase} .



374 We calculate $R_{\text{sum}} = R_{\text{wind}} + R_{\text{phase}}$ and use the procedure outlined in Sect. 2.2 to find the
375 timing of the R_{sum} extremes. The results during semidiurnal tidal cycles are shown in Fig. 5. The
376 frequency distributions and p -values for R_{sum} suggest the presence of tide-surge interaction at Tanjong
377 Pagar, Johor Baharu, Sedili, Tioman and Kuantan (Fig. 5 and S15). No significant interaction is identified
378 at Cendering and Geting. This can also be seen in Fig. 4 where the medians of the frequency distributions
379 at Cendering and Geting do not significantly differ from zero while the medians at the other five locations
380 do. We find that the frequency distribution of R_{sum} has a single mode as opposed to the bimodal
381 frequency distribution of the tide gauge residuals. At the five locations where R_{sum} provides an indication
382 of tide-surge interaction, the modes of their frequency distributions of R_{sum} lie within 2–4 hours before
383 HW, following R_{phase} . During diurnal tidal cycles, we find no evidence of tide-surge interaction (Fig.
384 S16–S17).

385 We find that R_{phase} can significantly influence the distribution of the extreme values of R_{sum} .
386 This is despite R_{phase} contributing to <1% of the variance of R_{sum} at all seven tide gauge locations (Fig.
387 S18). By an alternative metric, the ratio between the standard deviation of R_{phase} and the standard
388 deviation of R_{wind} is only 0–1%. Thus, while the magnitude of R_{sum} is effectively fully dependent on
389 R_{wind} , the timing of its largest values is dependent on R_{phase} . We have shown that the process of tidal
390 phase alteration—where wind-induced surges perturb the depth of the water body and influences the
391 propagation speed of the tide—produces a significant and measurable tide-surge interaction at five
392 locations. This result is complementary to Chen et al. (2012), who found that the influence of tide-surge
393 interactions on large surges is negligible, although tide-surge interaction may alter the time of tidal high
394 and low water.

395 However, our semi-empirical model is unable to accurately predict all the characteristics of tide-
396 surge interaction found in R_{gauge} (Fig. 3). At Tanjong Pagar, Johor Baharu, Sedili and Tioman, extreme
397 residuals typically occur even earlier than what our model suggests. Tidal phase alteration shifts the
398 timings of extreme residuals towards times where tides are rising or falling the quickest, and no further.
399 Our model is also unable to produce the bimodal distribution found in the tide gauge data illustrated in
400 Fig. 3 and failed to produce statistically significant tide-surge interaction at Cendering and Geting. This



401 suggests that the mechanism of tidal phase alteration cannot fully explain the observed tide-surge
402 interaction and that additional explanations are required to fully account for the observations. One
403 possible contributor is that shallower water during low tides can result in higher surges from near-shore
404 winds (Pugh and Woodworth, 2014b). Kurniawan et al. (2014) had found that the tidal cycle influences
405 non-tidal residuals. This could result in a further shift of the extremes towards tidal low water, which
406 would be closer to the observed tide-surge interaction.

407 **4 Conclusions**

408 We have introduced the No-TSI distribution to be used in determining the presence of tide-surge
409 interaction. The No-TSI distribution can account for irregular tidal cycles that can lead to non-uniform
410 sampling with respect to the number of hours from HW. Hence, the No-TSI distribution is generally not
411 a uniform distribution. When determining the presence of tide-surge interaction, the observed frequency
412 distribution should be compared to the No-TSI distribution instead of a uniform distribution.

413 Analysis of tide gauge records using the No-TSI distribution provides evidence of tide-surge
414 interaction at all seven tide-gauge locations along the Peninsular Malaysian east coast and Singapore. The
415 observed interactions have a smooth spatial dependence along the coastline. During semi-diurnal tidal
416 cycles at the southernmost location of Tanjong Pagar, extreme residuals are mostly found around 5 hours
417 before tidal HW with a much smaller number of extremes occurring after HW. Moving northwards,
418 similar patterns are found at Johor Baharu and Sedili, until we reach Tioman where extremes are mostly
419 found before HW but many extremes can also be found after HW. Northwards from Kuantan, most
420 extremes are found after HW.

421 To investigate the contribution of tidal phase alteration, we proposed a semi-empirical model. We
422 used 10 m winds from ERA5 to estimate the effects of tidal phase alteration. At the five southern stations
423 of Tanjong Pagar, Johor Baharu, Sedili, Tioman and Kuantan, we found the residual component caused
424 by advancement of tidal HW can significantly alter the timing of extremes despite being responsible for
425 less than 1% of the variance of the total residual. This demonstrates the effects of tidal phase alteration
426 on the timing of extremes.



427 Our model has explored one of the underlying mechanisms behind tide-surge interaction but is
428 not designed to forecast water level or extreme events. A forecast model would require much more
429 accurate modelling of the wind-driven surge. Inclusion of other underlying mechanisms of tide-surge
430 interaction, such as the effect of tidal level on surge generation, would also be beneficial. Accounting for
431 tide-surge interaction has been found to improve water level predictions in this region and other parts of
432 the world (Antony et al., 2020; Fernández-Montblanc et al., 2019; Kurniawan et al., 2015; Idier et al.,
433 2012). Knowledge of the interplay between tide-surge interaction and extreme sea levels can aid in the
434 design of effective strategies for coastal planning, risk assessment, and mitigation measures, and will
435 benefit from more comprehensive analyses. When studying extreme sea level in Southeast Asia, the
436 relatively short length of available tide gauge records poses a challenge, providing a focus for further
437 research.

438 **Appendix A: Calculating p -value with bootstrapping**

439 We label the *frequency distribution* obtained in Sect. 2.2 as $\mathbf{k}^{(0)}$. $\mathbf{k}^{(0)}$ is a function of h , the number of
440 hours relative to HW. Consider the scenario where out of the n extreme events in \mathbf{k} , k_0, k_1, k_2, \dots number
441 of events had occurred 0,1,2, ... hours after HW respectively and k_{-1}, k_{-2}, \dots number of events had
442 occurred 1,2, ... hours before HW respectively. The probability that this outcome is obtained from the No-
443 TSI distribution is $p_{\{\mathbf{k}\}} = \frac{n!}{\prod_h k_h!} \prod_h p_h^{k_h}$ or $n! \prod_h p_h^{k_h} / k_h!$. This is a multinomial distribution. We label the
444 *frequency distribution* of R_{gauge} as $\mathbf{k}^{(0)}$. For the bootstrapping procedure, we calculate $\log p_{\{\mathbf{k}^{(0)}\}}$: the
445 log-probability of obtaining the *frequency distribution* of R_{gauge} , $\mathbf{k}^{(0)}$, from the normalised No-TSI
446 distribution. To obtain a bootstrap sample, we then randomly draw n events from the normalised No-TSI
447 distribution. We label the frequency distribution of this bootstrap sample as $\mathbf{j}^{(1)}$ and we calculate
448 $\log p_{\{\mathbf{j}^{(1)}\}}$. Random draws are repeated 10^6 times until we obtain $\log p_{\{\mathbf{j}^{(m)}\}}$ for $1 \leq m \leq 10^6$. By the
449 definition of p -values, we expect $p \times 10^6$ number of bootstrap samples to have a log-probability that is
450 less than $\log p_{\{\mathbf{k}^{(0)}\}}$ and $1 - p \times 10^6$ number of bootstrap samples to have a log-probability of at least



451 $\log p_{\{k^{(0)}\}}$. Hence, the proportion of $\log p_{\{j^{(m)}\}}$ that is less than $\log p_{\{k^{(0)}\}}$ is the p -value representing the
452 likelihood of the null hypothesis claiming absence of tide-surge interactions.

453

454 *Code and data availability.* The hourly tide gauge data can be downloaded from the University of Hawaii Sea Level
455 Center (UHSLC) at <https://uhslc.soest.hawaii.edu/data/?rq> (Caldwell et al., 2001). The UTide MATLAB functions
456 can be downloaded from [https://www.mathworks.com/matlabcentral/fileexchange/46523-utide-unified-tidal-](https://www.mathworks.com/matlabcentral/fileexchange/46523-utide-unified-tidal-analysis-and-prediction-functions)
457 [analysis-and-prediction-functions](https://www.mathworks.com/matlabcentral/fileexchange/46523-utide-unified-tidal-analysis-and-prediction-functions) (Codiga, 2011). The ERA5 hourly data can be downloaded from
458 <https://doi.org/10.24381/cds.adbb2d47> (Hersbach et al., 2018). The bathymetry data can be downloaded from
459 GEBCO at <https://download.gebco.net/> (GEBCO Compilation Group, 2023). The analysis code used to produce
460 the figures and tables can be downloaded from <https://doi.org/10.5281/zenodo.10570585>.

461

462 *Author contributions.* ZYK: conceptualisation; data curation; formal analysis; investigation; methodology;
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464 investigation; methodology; writing – review and editing. DS: writing – review and editing. ADS:
465 conceptualisation; writing – review and editing. BPH: funding acquisition; supervision (supporting); writing –
466 review and editing. JD: funding acquisition; supervision (supporting); writing – review and editing. LYC: funding
467 acquisition; project administration; resources; supervision (lead); conceptualisation; investigation; methodology;
468 writing – review and editing.

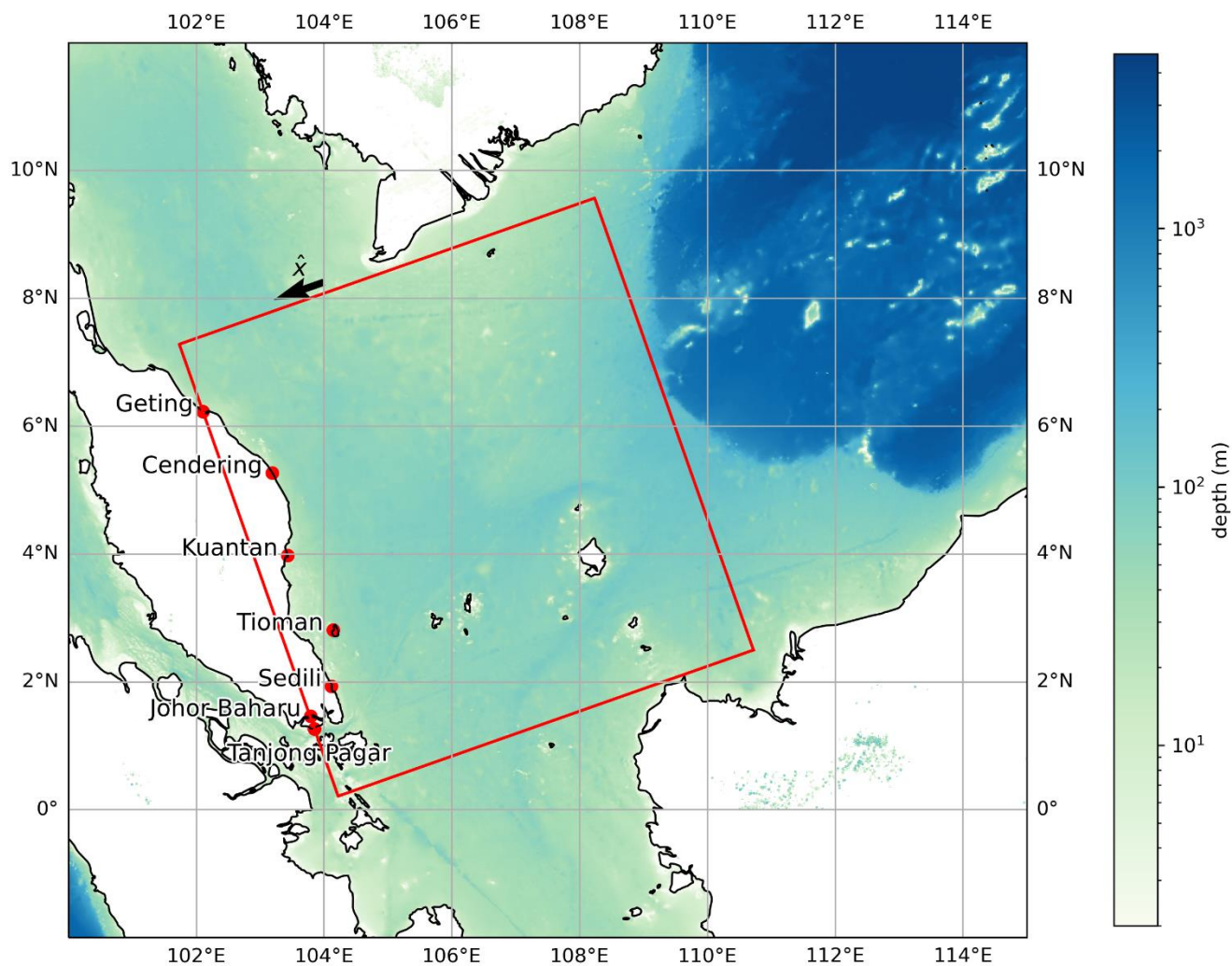
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471

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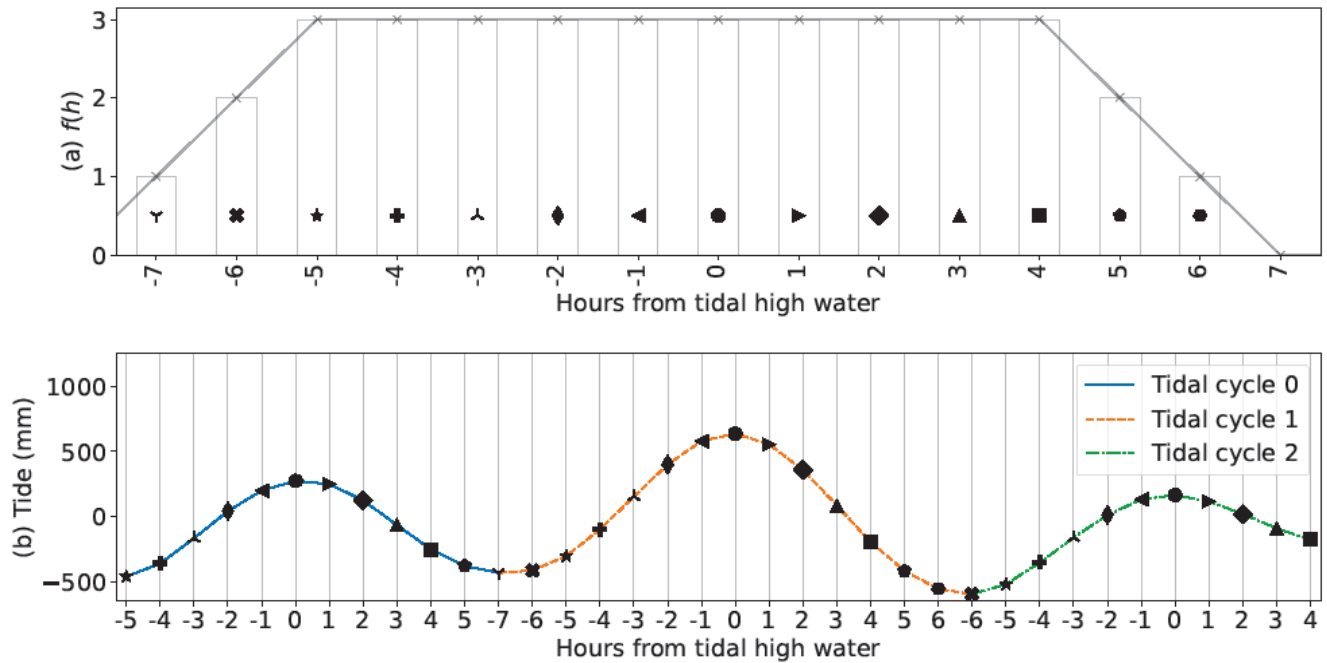
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478

479 **Figure 1: Bathymetry (in m) of the region of interest of this study, obtained from GEBCO, the**
480 **General Bathymetric Chart of the Oceans (GEBCO Compilation Group, 2023). The seven tide**
481 **gauge stations analysed are marked in red circles. The red rectangle denotes the region where 10**
482 **m winds are considered when calculating R_{wind} (Sect. 2.3). The region is roughly a rectangle of 759**
483 **km by 833 km. The unit vector \hat{x} used in Eq. (3) is shown in the figure.**

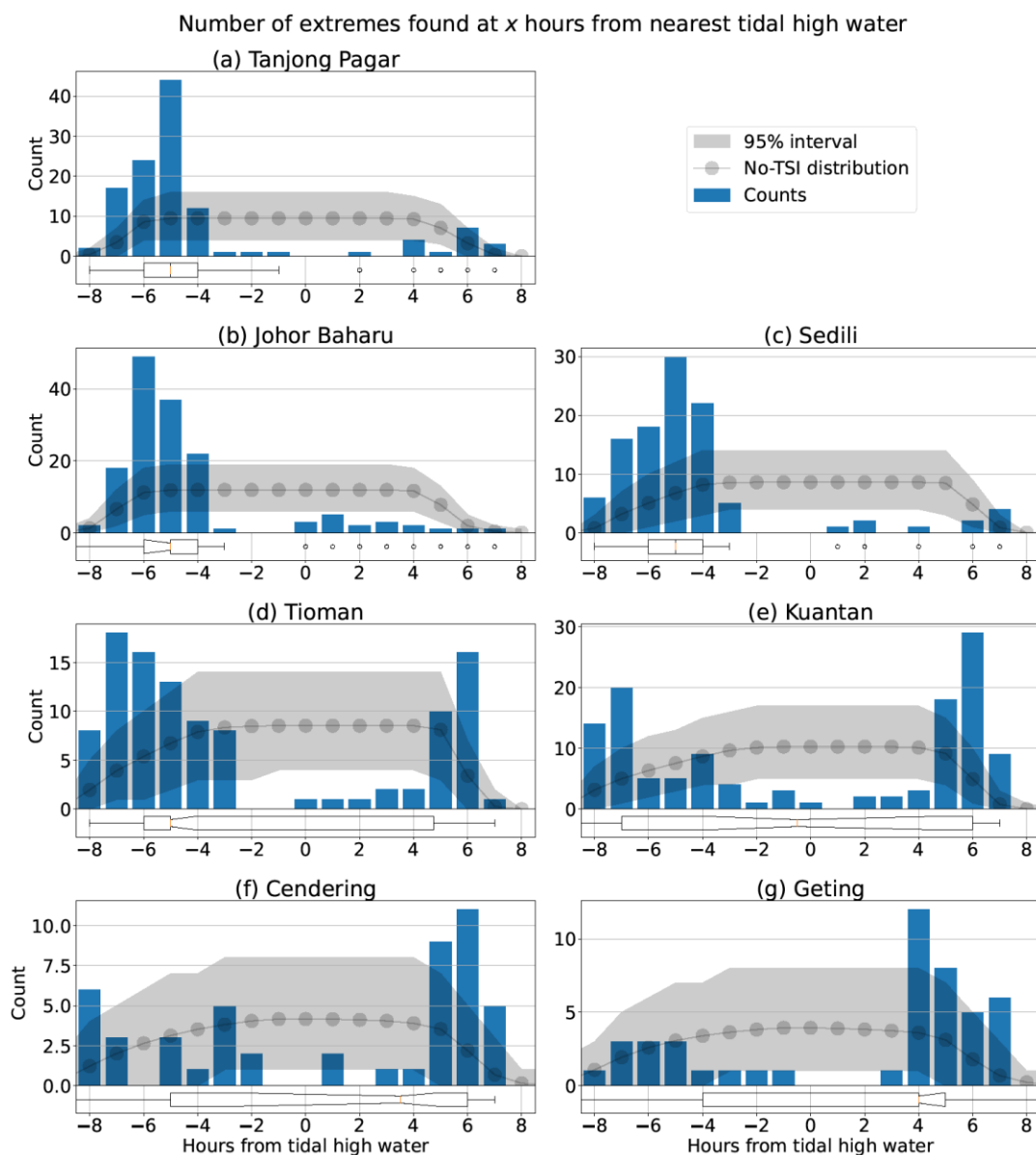
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485

486 **Figure 2: An example of how the No-TSI distribution is obtained, using three tidal cycles at Tanjong**
487 **Pagar tide gauge station between 1 and 2 Jan 1989 (GMT). The number of hourly measurements**
488 **made at h hours from HW are counted and denoted as $f(h)$, the No-TSI distribution before**
489 **normalization and scaling by the number of events (Sect. 2.2). In this example, if an extreme**
490 **residual can occur at any hour with equal probability, it will be 3 times more likely to happen at**
491 **HW than at 7 hours before HW. This is observed from (b) where $-5 \leq h \leq 4$ occur thrice, $h = -6$**
492 **and $h = 5$ occur twice, and $h = -7$ and $h = 6$ occur once, resulting from the three irregular tidal**
493 **cycles.**

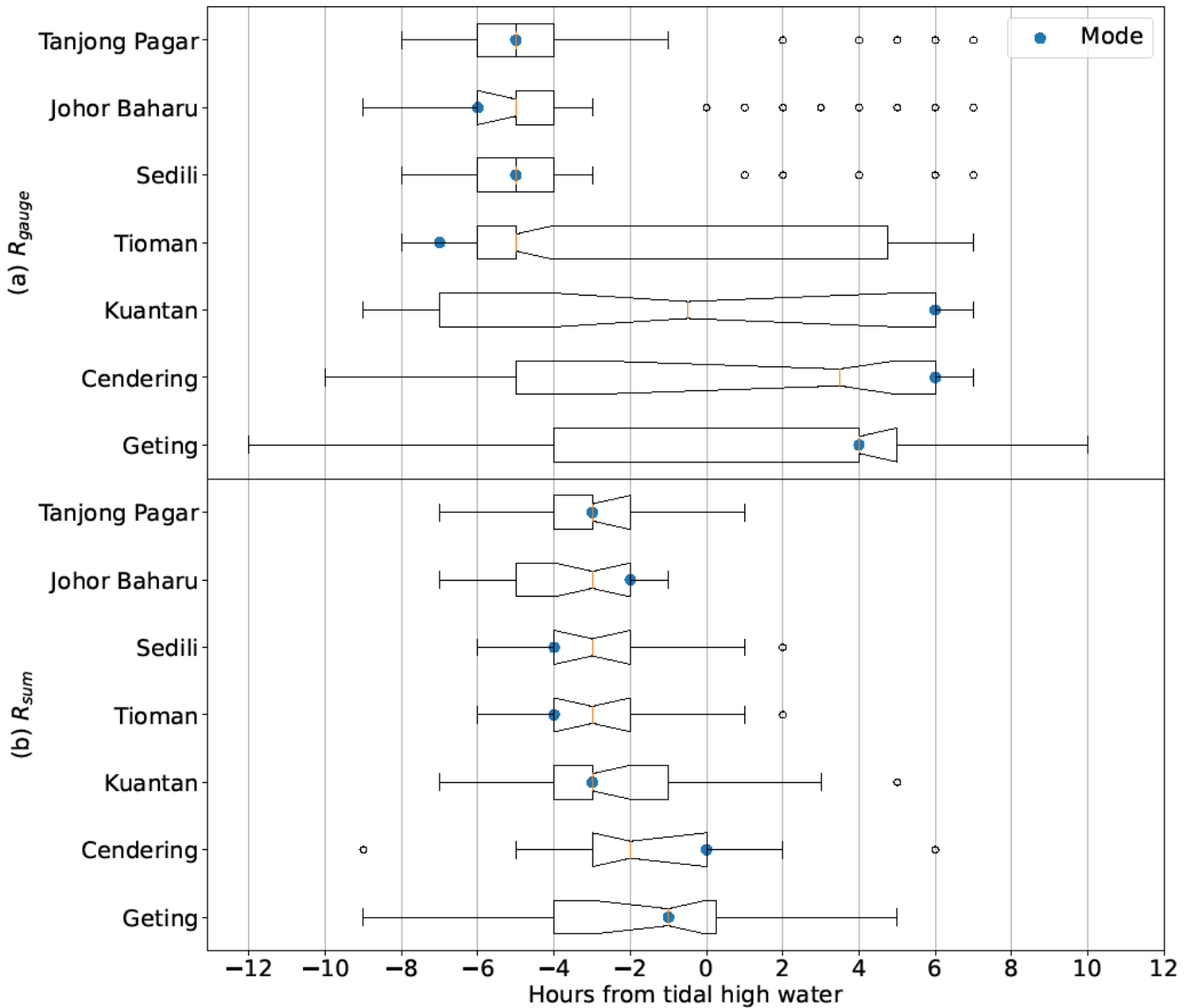
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495

496 **Figure 3: Frequency distribution—the number of extreme events that have occurred at a certain**
497 **number of hours relative to HW—of extreme residuals (R_{gauge}) during semidiurnal tidal cycles**
498 **(Sect. 2.2). The plots are truncated at ± 8 hours from HW. The frequency distribution is compared**
499 **to the No-TSI distribution, shown in grey, to determine the presence of tide-surge interaction (Sect.**
500 **2.2). Summary statistics of the frequency distribution are shown using the horizontal notched box**
501 **plot (Sect. 2.2). The whiskers of the box plot at (b) Johor Baharu, (e) Kuantan, (f) Cendering and**
502 **(g) Geting extend beyond ± 8 hours from HW, and their full extent is shown in Figure 4.**

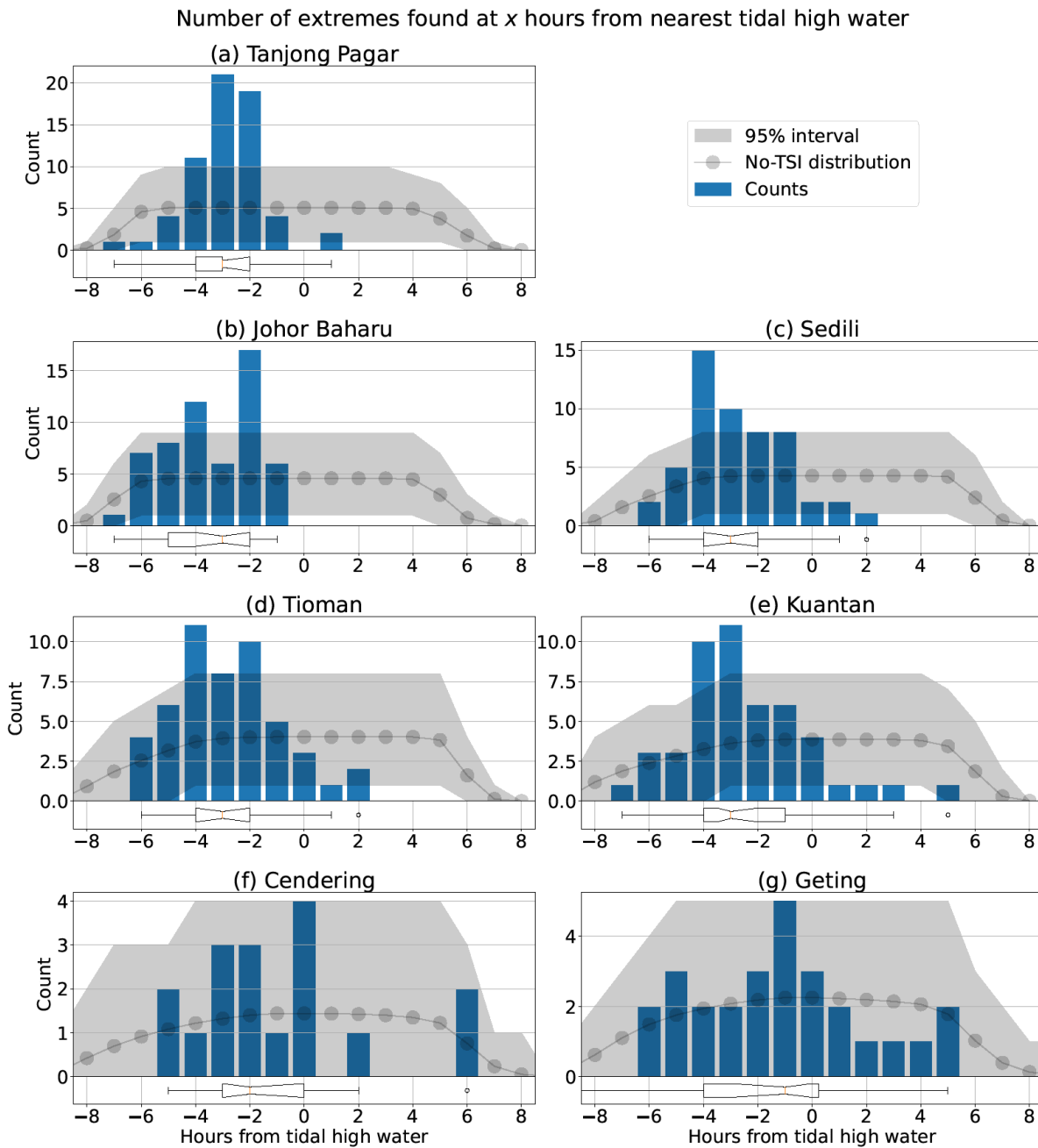
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504

505 **Figure 4: Compilation of the box plots in Fig. 3 and Fig. 5. Results presented in Fig. 3 on the timing**
 506 **of extreme residuals are compiled in subplot (a) and results presented in Fig. 5 on extreme values**
 507 **of R_{sum} are compiled in subplot (b). The box plots illustrate summary statistics of the distribution**
 508 **$k^{(0)}$ at each location, where orange lines indicate the medians, notches indicate the 95% confidence**
 509 **interval of the medians, blue circles indicate the modes, notched rectangles indicate the**
 510 **interquartile range (IQR), whiskers indicate a range that extends up to $1.5 \times IQR$ from the limits of**
 511 **the IQR, and black circles indicate outliers outside this range.**

512



513

514 **Figure 5: The frequency distribution for extreme values of R_{sum} and the No-TSI distribution**
515 **during semidiurnal tidal cycles, truncated at ± 8 hours from tidal HW. Truncated horizontal**
516 **notched box plots illustrate some summary statistics of the frequency distribution, and their full**
517 **extents are shown in Fig. 4.**

518



519 **Table 1: Data availability of the tide gauges used in this study. Completion rate is the percentage of**
520 **usable hourly observations out of the duration of records. Usable rate is the percentage of usable**
521 **observations subtracting 1-year moving averages (Sect. 2.1).**

Location	Latitude	Longitude	Start	End	Years	Completion (%)	Usable (%)
Tanjong Pagar	1.262	103.853	1988-01-01	2018-12-30	31.0	95.42	89.24
Johor Baharu	1.462	103.792	1983-12-19	2013-12-31	30.0	95.02	87.11
Sedili	1.932	104.115	1986-12-23	2015-12-09	29.0	98.08	98.08
Tioman	2.807	104.140	1985-11-13	2015-12-31	30.1	96.47	89.22
Kuantan	3.975	103.430	1983-12-22	2015-12-31	32.0	98.70	98.70
Cendering	5.265	103.187	1984-11-01	2015-11-30	31.1	96.58	90.58
Geting	6.227	102.107	1986-12-17	2015-12-31	29.0	99.14	99.14

522



523 **Table 2: Summary of the tidal characteristics at the study locations including tidal range, four tidal**
524 **constituents (K_1 , O_1 , M_2 , S_2), and the tidal form factor (F). Units, where applicable, are in metres**
525 **(m). The diurnal tidal range is the difference between mean higher high water and mean lower low**
526 **water, and is also referred to as the great diurnal tidal range or great diurnal range (NOAA, 2000).**
527 **Maximum tidal range is the greatest difference between higher high and lower low water within a**
528 **single day, and is much larger than the diurnal tidal range.**

Location	Tidal Range		K_1	O_1	M_2	S_2	F
	Diurnal	Max					
Tanjong Pagar	2.2	3.3	0.31	0.30	0.80	0.32	0.54
Johor Baharu	2.4	3.6	0.31	0.31	0.88	0.34	0.50
Sedili	1.8	2.8	0.35	0.31	0.56	0.16	0.91
Tioman	2.1	3.5	0.46	0.34	0.60	0.19	1.03
Kuantan	2.0	3.6	0.53	0.36	0.53	0.18	1.26
Cendering	1.5	2.7	0.49	0.31	0.30	0.12	1.90
Geting	0.8	1.4	0.25	0.13	0.17	0.08	1.56

529



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