

We thank the editor and both reviewers for their comments and their time spent considering our manuscript. We are pleased that the manuscript was well-received overall. Below, we offer our responses to the reviewer and editor comments and explain the corresponding changes we have made to the manuscript. The reviewer/editor comments are in black, ours are in red. Where section, figure or line numbers are given these refer to the clean version of the revised manuscript (the version with changes marked is hard to read within the methods and results section because we have revised these significantly).

We first offer an overall response to the main issues raised.

1. Structure and flow of the paper

It is clear from general comment 1 of reviewer 1, much of the general comment of reviewer 2, and the initial comments of the editor that the flow of the manuscript needed revision. We tried a narrative style where the reader is led through the manuscript in the same manner that we discovered the results, but we agree that this proved confusing because it mixed methods and results, and some results that came later in the paper “overwrote” results from earlier in the paper. We have now:

- Comprehensively restructured the methods (section 2) and results (section 3) following the suggestions of the reviewers. The equations and solutions are stated in their most general form up front and before any results are presented.
- We have included basal friction from the start (Fig. 1 and Eq. 8 onwards) and throughout the results (Fig. 3 onwards).
- We have described and discussed the potential for it to be impossible to satisfy horizontal force balance at the first place where we solve the equations (L195).

2. Interpretation of “undefined crevasse depths” and when calving occurs

Reviewer 1 twice raises a concern about the interpretation of undefined crevasse depths and the definition of calving. Mathematically, these undefined crevasse depths arise when the term in the square root of Eq. 19 becomes negative, so that there is no real solution. Physically, this indicates that the horizontal forces on the nascent calving block (Fig. 1) cannot be balanced. Or, in other words, the resistive stress that opens crevasses exceeds the tensile strength of the ice, for any configuration of crevasse depths. We feel that it is natural to call this situation “calving” – the forces that resist calving are unable to balance the forces that promote calving.

As pointed out by reviewer 1, this definition differs from Buck (2023) and Coffey et al. (2024), both of whom define calving as occurring when the total fractional crevassing, f , is equal to 1. We agree that $f=1$ should signify calving, and in the revised manuscript we now include results where we do have $f=1$ (Fig. 4b, blue; section 3.3.1). We overlooked this possibility in the original manuscript, however for the reasons outlined in section 3.3.1 we do not think it is the most physical of the possibilities for calving and it has not changed the manuscript overall.

We still maintain that the undefined crevasse depths should be interpreted as calving and feel that these did not arise in the work of Buck or Coffey for two reasons. First, we are considering significantly higher resistive stresses than Buck or Coffey. Their papers consider buttressed floating ice shelves (with a limiting case of a freely floating ice shelf), whereas we

consider grounded tidewater glaciers. The resistive stress at the front of a grounded tidewater glacier is higher than at a buttressed or freely floating ice shelf, which leads to larger (or even undefined) crevasse depths – and it is natural that if total fractional crevassing reaches 1 at the front of an unconfined floating ice shelf (Buck 2023, Coffey 2024), then crevasse depths are at risk of becoming undefined when the resistive stress is significantly higher. Second, the variable that scales the resistive stress in our results is the fractional calving front water depth w/H (i.e., how close to flotation the glacier is). This water depth also controls the water pressure in the basal crevasse, so the resistive stress and the water pressure in the basal crevasse are both responding to the calving front water depth. This differs from Buck and Coffey because their resistive stress is varied independently from the water pressure in the basal crevasse. We have now:

- Included a possible solution where the total fractional crevassing reaches 1 (section 3.3.1) and Fig. 5a.
- Described in more detail why we think the undefined crevasse depths should be interpreted as calving and included this formally in the solution of the equations (L195-203).
- Described the differences between Buck, Coffey and our results in L210-220 and derived the connection between our mathematical expressions and theirs in Appendix A.

3. Novelty relative to Buck (2023)

Reviewer 2 raises the issue of the novelty of our results relative to Buck (2023). At a superficial level, the difference is that we apply the revised crevasse depth framework to grounded tidewater glaciers (with floating glaciers as an edge case), whereas Buck (2023) applied it to buttressed floating ice shelves. Thus, our results pertain to, for example, Greenland’s outlet glaciers, whereas the results of Buck pertain to the floating ice shelves around Antarctica. But, maybe more importantly, the dynamics that emerge from applying the framework to grounded tidewater glaciers are very different from floating ice shelves, with key differences being: (i) the resistive stresses close to the front of grounded tidewater glaciers are higher than at floating ice shelves, meaning that for much of the grounded glacier parameter space there are no stable crevasse depths (i.e., horizontal forces cannot be balanced); (ii) we introduce a non-zero ice tensile strength, which was not considered in Buck (2023). As well as being an important factor to introduce in general (because the fracture of any material should depend on its intrinsic strength), the tensile strength results in a threshold ice thickness (Eq. 25, 400 m approx.) that shows promise in explaining the separation between different calving styles of grounded glaciers (L400-412); (iii) we consider the role of basal friction in suppressing calving. A key property of basal friction is that it disappears when the ice reaches flotation, and thus the presence of basal friction in the new calving framework provides a potential explanation for why many glaciers appear to calve at or close to flotation, as shown by the data from Ma et al. (2019) that is plotted on Fig. 5.

Thus, although the initial theoretical basis is the same as Buck (2023), we present a different physical application that is in a different part of the “parameter space”, has quite different dynamics, we introduce new ideas that show promise in explaining key overarching calving dynamics observed at grounded glaciers, and we offer observational support (Fig. 5). For these reasons we feel this study is a significant contribution. In terms of changes to the manuscript, we have:

- Modified the abstract to clarify the advance and difference to Buck (2023) – L5
- Made clearer that non-zero ice tensile strength and basal friction are factors that were not considered in Buck (2023) – L77, 373, 489.
- Explicitly discussed differences in the theoretical framework between this study, Buck (2023) and Coffey et al. (2024) – L208-218.
- Shown how our results map onto Buck (2023) when you (i) assume flotation and (ii) assume zero ice tensile strength – Appendix A.

Reviewer 1

General comments

Following Buck (2023), The authors modified the crevasse depth law with a simple method to account for the stress concentration under crevassing, a variable density of water in basal crevasses, and non-zero ice tensile strength. The framework has the potential to understanding differing calving styles and a better parameterization of calving in numerical models. However, there are major concerns that need to be resolved before considering publication.

1. The structure of the analytical model can be confusing. The heart of the analytical model – the horizontal force balance (Eqn11) – involves many hidden assumptions that the authors prove to be invalid in sections afterwards. For instance, Eqn11 assumes no basal friction (proved to be inaccurate in Sec.3.5), static condition (proved to be wrong when there is no real solution to Eqn15,16, line 335 “the forces on the nascent calving block cannot be balanced, so the block accelerates relative to the glacier...”). To improve readability of the paper, it might be better to start with the most general form of force balance by taking basal friction and acceleration into account in Eqn.11.

Please see our response to the first significant concern above – in summary, we have comprehensively restructured much of the methods (section 2) and results (section 3) to start with the most general formulation and avoid ‘overwriting’ results from earlier in the paper. In particular, basal friction is now included at the earliest opportunity (Fig. 1 and Eq. 8) and integrated throughout the results section. The potential for it to be impossible to satisfy the static condition is noted as a formal part of the crevasse size solution (case 4 of the 4 solution cases presented in L179-198), and we immediately discuss our interpretation of this in L197-203.

We considered adding an explicit acceleration term to the horizontal balance, and appreciate the suggestion, but felt that this would complicate the maths without adding physical insight. Ultimately, we would find that a non-zero acceleration is necessary to solve the equations in solution case 4 (L195), and then we would have the same physical interpretation as outlined in L197-203. Since we have worked hard to try to present the maths as simply as possible, we wish to avoid further complication and hope the reviewer understands this perspective.

2. I’m confused by the authors’ definition of calving: when there is no real solution to surface/basal crevasse depth (Eqn15,16), which, to me, implies invalid assumptions underlying current analytical model. For instance, in Fig4, an increase in ρ_c will give real solutions to Eqn15,16. Does this mean $\rho_c=1000 \text{ kg/m}^3$ is just not physical? In line 85, the authors state that “it is assumed there is an open hydraulic

connection from the bed below the glacier to the calving front”, does this contradict with the later assumption of $\rho_c=1000\text{kg/m}^3$? If we incorporate an inertia term in Eqn. 11, will it be guaranteed to have real solutions instead?

Please see our overall responses 1 and 2, and our previous response, for changes made to the paper to address these points. Addressing explicitly the questions posed here, we don't feel that undefined crevasse depths invalidate the analytical model. Rather, our interpretation is that undefined crevasse depths means that it is not possible to satisfy the static equations with any combination of crevasse depths. This means there must be an acceleration of the nascent calving block, which we would interpret as calving. This is now outlined in L195-203.

In Fig. 4 we agree there are cases where increasing ρ_c will give real solutions, but we don't feel this is problematic or that this means $\rho_c=1000\text{ kg/m}^3$ is unphysical. Higher ρ_c means a reduction in overall basal crevasse water pressure (L256) and therefore a reduction in the overall force opening the basal crevasse. The reduction can be sufficient that it becomes possible to satisfy the static balance, leading to real solutions. Our interpretation would then be that $\rho_c=1000\text{ kg/m}^3$ will rapidly lead to calving, whereas a higher value of ρ_c does not result in calving.

By “open hydraulic connection” we mean there is a communication of pressure (so that the pressure at the bottom of the crevasse is the same as the pressure at the bottom of the ocean), rather than that the densities of crevasse and ocean water have to be the same. This has been clarified in L90.

As a side note, calving was previously defined as “total fractional crevassing $f = 1$ ” in literature (Buck, 2023, Coffey et al., 2023 Theoretical stability of ice shelf basal crevasses with a vertical temperature profile), which seems more intuitive and physical to me. I'm curious whether there are plausible ways to modify the analytical model (i.e., relax some assumptions), to avoid the “undefined crevasse fraction” issue.

Hopefully our responses so far now cover this point. Note that in revising the paper we discovered a solution we had overlooked that does have $f=1$ (section 3.3.1), but we do not favour this overall as a modified calving criterion because it does not allow for the existence of floating ice shelves and does not explain the threshold in calving styles discussed in section 4.2.

1. Section 3.2, shall the tensile strength be nondimensionalized by $\rho_i g H_i$? Does it vary with ice thickness? The authors might want to justify why in many figures tensile strength is fixed while ice thickness is varying across a wide range? (Fig.5, 6, 7, 8, 9)

Thank you for raising this point. The ice tensile strength is occasionally non-dimensionalised in the paper for mathematical convenience, but in general it should be independent of ice thickness because it is a material parameter – i.e., it is a physical property of ice – which is why it is fixed in many figures. This has been noted in L301. Ice thickness is varied across a wide range because we wish to consider the implications of our formulation at the full range of Greenland's tidewater glaciers.

2. Figure 7, 9: The original paper for the observational data also has a stability phase diagram of terminus configuration (Figure 3 in Ma et al., 2017), and it seems to explain the data better. It is reasonable that the authors (no shear failure) have different predictions than Ma et al., 2017 (including shear failure). However, in Ma et

al., 2017, ice tensile strength is 0 (Figure 1), which is claimed to be invalid in this manuscript instead? Why is there a contradiction?

This is an interesting point. We don't feel there is a contradiction between our results and those of Ma et al. (2017), rather that we make different assumptions about the ice tensile strength. Ma et al. (2017) assume that ice tensile strength is 0, so that tensile failure occurs when the (maximum principal) stress is greater than 0, whereas we assume a non-zero tensile strength and that tensile failure occurs only when the stress exceeds this tensile strength. In Ma et al. (2017), calving occurs close to flotation at all ice thicknesses (their Fig. 3), whereas in our results calving occurs close to flotation only above a certain ice thickness (Fig. 5b-c and Fig. 6). If Ma et al. (2017) had assumed a non-zero tensile strength, we think it is likely that their simulations with smaller ice thicknesses would not undergo calving because the stresses would not exceed the tensile strength, bringing their results into line with ours. We have made a minor change at L434 to reflect this as we feel that paragraph (L429-436) covers this issue, but we can make further changes if deemed necessary.

You could ask why then we prefer having non-zero ice tensile strength? This is because of the need to explain the existence of unconfined ice shelves (which otherwise cannot exist – section 3.3.1 and Fig. 5a) and because the ice tensile strength leads to the thickness threshold which appears to map onto a threshold in calving behaviour (section 4.2).

Specific comments

1. Figure 5: A question comes to mind that “why happens for thick termini that are at flotation? (commonly observed across Greenland)” Does the figure imply termini thicker than 300m can never be at flotation stably?

This is now Fig. 4d. These results are intended to illustrate the sensitivities present in the framework, rather than being results that apply to glaciers in general. This has been clarified in L253. The revised results section 3.3, and particularly Fig. 5, cover the stability of glaciers in general.

2. Line 245, “when we do assume zero tensile strength, the total fractional crevassing is either 1 or undefined for all possible calving fronts, hence this is not a useful calving law”. The sentence could be rephrased. This conclusion is drawn based on assumptions made in this paper but might not be general?

This sentence has been removed in the overall restructuring of the methods and results. In particular, section 3.3.1 of the results now explicitly considers the case of zero tensile strength.

3. Line 285: “if we use Eq.22 in the modified crevasse sizes Eqs. 15& 16 then for grounded glaciers, calving occurs...” Eqs. 15 & 16 is derived by assuming no basal friction in Eqn. 11, right? Is it equivalent between: 1) what the authors did here; and 2) including τ_b in Eqn. 11 -> rederive Eqn. 12 -> combining 12,13,14 -> expression for ds'/H , db'/H by considering basal friction. Does 2) seem easier to understand?

Yes – your suggestion would be equivalent – thank you for the suggestion. As stated above, we have now restructured the methods following your suggestions.

4. Figure 9: the observations have different crevasse spacing, L , right? If the calving criterion is very sensitive to L , maybe the authors should include the information of L for the observation data as well, before comparing with the analytical model?

Figure 9 is now Figure 6b. Thank you for raising this point. Unfortunately, observational data for crevasse spacing are limited, especially for basal crevasses, and so we do not have the necessary information to estimate a crevasse spacing for every glacier on this figure. Within the scope of this present study, we feel it is sufficient to consider the sensitivity to the assumed crevasse spacing, and this is now done in L279-281, L300-304 and Appendix B.

Reviewer 2

GENERAL COMMENT:

The manuscript “Calving from horizontal forces in a revised crevasse-depth framework” by Slater and Wagner modifies the ‘classic’ crevasse-depth calving law by introducing feedback with the background stress field and the water density within basal crevasses. This work builds on recent analytical formulations to improve the ‘classic’ crevasse-depth law in a largely theoretical exercise. The manuscript is of immediate interest of folks in the cryosphere community and is appropriate for the readership of the Cryosphere journal.

Thank you for your interest and time spent on this review.

While the manuscript provides a thorough introduction to calving laws, I found it quite difficult to follow. The structure poses some challenges, particularly in the introduction. Although the discussion of calving laws is detailed, it took me several readings to fully understand it. For instance, it wasn’t immediately clear that Nye (1955) is considered the ‘classic’ crevasse-depth law (is that correct?). There have been many modifications since Nye’s original stress-balance formulation, and the authors do a good job to list them. However, later in the methodology sections (i.e. 2.2), the manuscript includes a detailed formulation of this approach, but it’s unclear where these equations originate from—Nye? Weertman? Furthermore, in line 111, the ‘line of argument’ from Buck (2023) is introduced, which raises the question: are we still discussing the original formulation? While I’m not suggesting the formulas are incorrect, these sections are quite confusing, and the definition of the ‘classic’ formulation remains ambiguous. Following this, Buck (2023)’s modifications are presented in Section 2.3, but the integration of equations (1–2) with the classic formulation (equations 3–8) is unclear. After reading these sections, I got completely lost on the novelty of this paper leaving me with this question: What is the main difference with Buck 2023?

Finally, in the results section (i.e. 3.5), the equations are further edited with the inclusion of basal friction. I appreciated this part, and I think it is an important aspect of the manuscript given the ongoing discussion in the community surrounding the importance of sliding laws. However, this section mixes methods and results, which had to bring me back to the initial equations, further slowing down the reading process. Wouldn’t it be perhaps more efficient to introduce the novel formulation at the beginning of the methodology section and move the classic laws in the appendix? I know this would be a major edit for this manuscript and ultimately it is the authors’ personal choice, but it is a scenario that is perhaps worth considering.

To be clear, I am not suggesting that this work lacks novelty, and I commend the authors for the detailed mathematical analysis presented—it is evident that this required significant time and effort. However, the structure in which the methods and results are presented makes the manuscript occasionally slow and difficult to follow. These issues should be addressed to improve clarity and accessibility before publication.

Please see our overall responses 1 and 3 at the top of this document – we have comprehensively restructured the methods and results sections following your comments here.

We now see that the introduction of the classic law could be confusing, particularly because it did blend a bit the classic law with Buck (2023) by allowing for a variable density of water in the basal crevasse. Our motivation for doing so was that we wished to demonstrate how that modification alone has limited effect on crevasse depths (Fig. 2). We have rephrased this section (2.2) to clarify our definition of the classic law, to make clear what references the equations come from, and to avoid the confusion of mentioning Buck (2023) at this stage. We have also added a clarifying statement on the terminology ‘classic’ at the end of section 2.1 (L106).

Note that we have not moved the “classic” law to an appendix because we have found in discussing this work with others (and even with researchers who are familiar with the subject) that this is useful background. We also think it is worth recapping how we can use the calving front boundary condition to switch from thinking about crevasse depth as a function of resistive stress to thinking about crevasse depth as a function of frontal water depth. We have now made this an explicit section (section 2.3) to clarify this point. Essentially, we feel that including a recap of the more familiar “classic” law should help more readers to understand what follows, and hope the reviewer understands this motivation.

MINOR COMMENTS:

Line 20: There is also a large body of literature which analyze the how individual rifts and the modulation of their infill (ice mélange) can lead to calving, whilst in complete absence of the factors listed here (e.g. Borstad 2017 GRL and Larour 2021 PNAS). This aspect is important to mention here.

Thank you – this has been added (L22).

Line 192: I am not sure what is meant with ‘an example of the modified crevasse sizes’.

At this point we wish to show a specific example of how the modified crevasse formulation that we have introduced differs from the classic crevasse formulation. We hope that the overall restructuring of the methodology makes this clearer.

Line 316: Unfortunately, this sentence at this point of the manuscript leaves me questioning the novelty again. What is the main difference with Buck 2023?

Line 320: See my general comment above.

Please see our responses above. Note that for these specific lines (now L373 onwards), we have clarified in the following sentences what we have added.

Specific Editor comments:

The revised formulation introduces several tuneable parameters, many of which are difficult to quantify—particularly the variable water density in basal crevasses, which plays a key role in determining calving sensitivity. Without validation through real-world observations or detailed model simulations, it remains unclear whether the resulting formulation may be overly dependent on parameter tuning.

This is a fair concern. Our first response would be that the introduction of more realistic physical processes into the calving formulation does indeed bring more physical parameters, but this isn't necessarily a bad thing provided that the formulation is more physically accurate. However, we do also address the problem of parameter sensitivity in L391-396 where we note that despite the many input parameters, it is quite possible that the only parameter that the final calving criterion relies on is the thickness threshold H_{σ} . Ultimately, we completely agree that candidate calving laws need validation and that is something we wish to do in future work.

Another concern is that the observational data used for comparison are clustered in a narrow envelope near the flotation criterion (e.g., Fig. 9a). The authors predict that under conditions of high ice thickness and low water depth, the ice front should remain stable, yet no corresponding observations are provided to support this claim.

Yes – the formulation that we have put forward does indeed suggest that high ice thickness/low water depth combinations are stable, but this arises because we have not considered shear failure. Bassis & Walker (2012) and Ma et al. (2017) both showed that shear failure prevents high ice thickness/low water depth combinations from being stable, which explains why there are no observations of glaciers in that part of the parameter space on Fig. 5 (formerly Fig. 9). We have not considered shear failure in this manuscript because it would add significant additional complexity to do so, and we feel that the manuscript is already relatively complex and makes a significant contribution even without shear failure. We have however acknowledged this point at L443.