



# To what extent does CO<sub>2</sub> diurnal cycle impact carbon flux estimates in CarboScope?

Saqr Munassar<sup>1,2,3</sup>, Christian Rödenbeck<sup>1</sup>, Michał Gałkowski<sup>1,4</sup>, Frank-Thomas Koch<sup>5</sup>, Kai U. Totsche<sup>2</sup>, Santiago Botía<sup>1</sup>, Christoph Gerbig<sup>1</sup>

5 <sup>1</sup>Department of Biogeochemical Signals, Max-Planck Institute for Biogeochemistry, Jena, Germany

<sup>2</sup>Institute of Geoscience, Friedrich Schiller University, Jena, Germany

<sup>3</sup>Department of Physics, Faculty of Science, Ibb University, Ibb, Yemen

<sup>4</sup>AGH University of Kraków, Faculty of Physics and Applied Computer Science, Kraków, Poland

<sup>5</sup>Meteorological Observatory Hohenpeissenberg, Deutscher Wetterdienst, Hohenpeißenberg, Germany

10 *Correspondence to:* Saqr Munassar ([smunas@bgc-jena.mpg.de](mailto:smunas@bgc-jena.mpg.de))

**Abstract.** Ignoring the diurnal cycle in surface-to-atmosphere CO<sub>2</sub> fluxes leads to a systematic bias in CO<sub>2</sub> mole fraction simulations sampled at daytime, because the daily mean flux systematically misses the CO<sub>2</sub> uptake during the daytime hours. In an atmospheric inversion using daytime-selected CO<sub>2</sub> measurements at most continental sites and not resolving diurnal cycles in the flux, this leads to systematic biases in the estimates of the annual sources and sinks of atmospheric CO<sub>2</sub>. This study focuses on quantifying the impact of this diurnal cycle effect on the annual carbon fluxes estimated with the CarboScope (CS) atmospheric inversion at regional, continental, and global scales for the period of time 2010–2020. Biogenic fluxes of hourly Net Ecosystem Exchange (NEE) obtained from the data-driven FLUXCOM estimates are used in the inversion together with global and regional atmospheric transport models. Differences between CO<sub>2</sub> mixing ratios simulated with daily averaged and hourly NEE range between around -2.5 and 7 ppm averaged annually throughout a site network across the world. As a consequence, these differences lead to systematic biases in CO<sub>2</sub> flux estimates when ignoring the diurnal variations of the CO<sub>2</sub> flux in the atmospheric inversions. Although the impact on the global average of estimated annual flux is negligible (around 2% of the overall land flux of -1.79 Pg C yr<sup>-1</sup>), we find significant biases in the annual flux budgets at continental and regional scales. For Europe, the annual mean difference in the fluxes arising from the diurnal cycle of CO<sub>2</sub> represents around 48% of the annual posterior fluxes (0.31 Pg C yr<sup>-1</sup>) estimated with CarboScope-Regional (CSR). Furthermore, the differences in NEE estimates calculated with CS increase the magnitude of the flux budgets for some regions such as northern American temperate and northern Africa by a factor of about 1.5. To the extent that FLUXOM diurnal cycles are realistic at all latitudes and for the station set used in our inversions here, we conclude that ignoring the diurnal variations in the land CO<sub>2</sub> flux leads to overestimation of both CO<sub>2</sub> sources in the tropical lands and CO<sub>2</sub> sinks in the temperate zones.

## 1 Introduction

30 Accurate estimation of CO<sub>2</sub> carbon budget is necessary for verifying the reduction of global carbon emissions in line with climate adaptation policies adopted in the Paris Climate Agreement (Glanemann et al., 2020). From a scientific perspective, there is also of high interest in extending our understanding about physical and biogeochemical dynamics of the carbon cycle



in the Earth's climate system. As reported in the Sixth Assessment Report (AR6) of the Intergovernmental Panel on Climate Change (Canadell et al., 2023), the cumulative carbon budget in the atmosphere has recently exceeded 279 PgC by 2019 mainly  
35 due to fossil fuel combustion, cement production, and net emissions associated with land-use change since the industrial era began in 1850. The consequence is global warming with a global mean temperature excess by around 1.1°C between 1850-1900 and 2011-2020. Recently, the annual fossil-fuel related emission of CO<sub>2</sub> increased to 10.9 Pg C yr<sup>-1</sup> over the past decade (2010-2019), with 5.1 Pg C yr<sup>-1</sup> accumulated in the atmosphere, 3.4 Pg C yr<sup>-1</sup> taken up by the terrestrial biosphere, and 2.5 Pg C yr<sup>-1</sup> counted as an ocean sink (Canadell et al., 2023). Fixing the largest amount of atmospheric CO<sub>2</sub> in the biosphere via  
40 photosynthesis, the terrestrial biosphere sink consequently increases in response to CO<sub>2</sub> concentration growth, which is thought to result from three effects: 1) fertilisation by the rise of CO<sub>2</sub> abundance in the atmosphere, 2) increase of nitrogen inputs into soil used by agriculture to enhance plants growth, and 3) prolongation of growing seasons (Friedlingstein et al., 2022). It is important to note, however, that interannual variability in the land sink is large (about 1 Pg C yr<sup>-1</sup>), making it difficult to pin down small emission variations in global atmospheric CO<sub>2</sub> concentrations (Baker et al., 2006). Moreover, due to the  
45 heterogeneity in terrestrial ecosystems, the atmosphere-to-land CO<sub>2</sub> fluxes are also largely variable at temporal and regional subscales (Marcolla et al., 2017), as regularly demonstrated by both Dynamic Global Vegetation Models (DGVMs) and data-based global inversion models, e.g. within the framework of the Global Carbon Project (Friedlingstein et al., 2022).

Atmospheric inverse modelling has increasingly been used at global (Ciais et al., 2010; Kaminski et al., 1999; Peylin et al., 2002; Rödenbeck et al., 2003) and regional scales (c.f. Gerbig et al., 2003; Rivier et al., 2010; Chevalier et al., 2014; Berchet  
50 et al., 2021; Monteil and Scholze, 2021; Munassar et al., 2022) to constrain the surface-atmosphere carbon fluxes and their variabilities based on atmospheric measurements sampled through surface in-situ networks and airborne-based monitoring instruments. Although the observational constraint is meant to drive the solution of the inverse problem, uncertainties and biases in atmospheric transport together with prescribed flux components such as anthropogenic emissions and ocean fluxes can diminish the capability of the inversions in terms of finding the optimal values of the state parameters (Engelen et al.,  
55 2002; Gurney et al., 2003). The atmospheric transport uncertainty especially remains a genuine challenge in inverse modelling to estimate carbon fluxes (Deng et al., 2017; Gerbig et al., 2008; Munassar et al., 2023), specifically over regions where observations either do not exist or are relatively sparse, such as over the tropics (Gurney et al., 2003; Botía, 2022). In fact, already in 2007 Stephens et al. (2007) have found inconsistencies in the vertical atmospheric CO<sub>2</sub> distributions between aircraft measurements and atmospheric models that transfer large amounts of terrestrial carbon from tropics towards northern latitudes,  
60 leading to overestimation of tropical sources and stronger sinks in northern terrestrial land, an effect necessary to maintain mass balance in the carbon budget.

The interhemispheric gradient of the annual mean CO<sub>2</sub> concentration evident by global atmospheric data represents one of the primary atmospheric constraints of the global carbon budget in all global atmospheric tracer inversions (Tans et al., 1990). Originally, this gradient was suggested to result primarily from higher emissions of fossil fuels over the Northern Hemisphere  
65 as compared to those in the Southern Hemisphere. Denning et al. (1995), however, found a significant meridional gradient imposed by the seasonal CO<sub>2</sub> exchange of terrestrial biota, amounting to half of the gradient imposed by fossil fuel emissions,



suggesting a stronger sink in the Northern Hemisphere than previously assumed. This effect has been referred to as “the atmospheric rectifier”, in which photosynthetic fluxes and thermally-induced vertical mixing are correlated in the atmosphere, as they are both driven by solar radiation and have a concurrent response to the same synoptic, diurnal and seasonal scales (Larson and Volkmer, 2008; Denning et al., 1999). That is, in the early afternoon on any sunny day of the growing season, atmospheric CO<sub>2</sub> concentrations are lower near the surface than in the free atmosphere due to strong daytime vertical mixing and, at the same time, active photosynthesis (Stephens et al., 2007). By contrast, during winter nighttime CO<sub>2</sub> concentrations accumulate quickly near the Earth’s surface as ecosystem respiration emits CO<sub>2</sub> into a shallower boundary layer relative to summer. On average, such covariations between the atmospheric transport and terrestrial biospheric fluxes are uniformly distributed in zonal latitude with higher concentration near northern polar regions and lower in the tropics and Southern Hemisphere (Chan et al., 2008). The effect of this CO<sub>2</sub> rectifier becomes uncertain at regional scales along the latitude bands. For instance, model overestimation of the rectifier effect in the northern extratropics would result in a stronger sink in this region that will be compensated within an inversion framework by adding CO<sub>2</sub> sources in the tropics, where there is a poor observational constraint, to maintain the global mass balance (Gurney et al., 2003).

As the atmospheric rectifier effect arises from both diurnal and seasonal variations of the vertical transport and biosphere CO<sub>2</sub> fluxes, information of these variations should be accounted for in inverse modelling. While the seasonal rectifier effect can be reconciled in atmospheric inversions by the seasonal variations of CO<sub>2</sub>, already included in the observational constraint, the diurnal variations are commonly missing in the observational constraint, because in inversions the use of observations is typically restricted to times when the lower atmosphere is well-mixed (i.e. during local noon to afternoon times) (Gerbig et al., 2008). An accurate representation of the rectifier is then dependent on the performance of atmospheric transport models to represent the seasonal and diurnal cycles. Therefore, reconciliation of the diurnal rectifier effect in atmospheric inversions is achievable by including diurnal variations of the biogenic terrestrial fluxes in the prior fluxes, provided that the vertical transport diurnal variations are accounted for. However, not all atmospheric inversions account for the effect of a diurnal cycle in biosphere-atmosphere exchange of CO<sub>2</sub>, given that such an impact is not quantitatively investigated in detail in line with global and regional CO<sub>2</sub> flux budgets.

This study aims to investigate the impact of the diurnal cycle on CO<sub>2</sub> flux estimates derived from the CarboScope inversion (CS), which so far (version v2023) does not account for diurnal variations in the CO<sub>2</sub> flux. In the standard global CS framework, the posterior biogenic fluxes are dominantly driven by the atmospheric data constraint, and the control vector represents deviations from zero biogenic fluxes used as a priori estimate. Unfortunately, the diurnal flux variability cannot be constrained by the atmospheric data, because the atmospheric measurements are only used during day-time hours for surface stations and night-time hours for mountain stations, reflecting that the transport model is expected to have particularly large errors outside these time periods. In the global total carbon flux, the impact of the diurnal cycle effect is attenuated because it is well constrained by the linear rise of CO<sub>2</sub> from year to year, due to the mass conservation of CO<sub>2</sub> in the atmosphere. However, for the fluxes at local scales the diurnal cycle effect can lead to biases in the estimates.



100 In studies focusing on specific land regions, like Europe, it is essential to make use of as many continental measurements as possible. As these measurements are typically located within complex atmospheric circulation patterns, the relatively coarse global transport model is not well suited to represent these measurement locations. Therefore, variations in transport and in fluxes need to be resolved on finer spatial and temporal scales. Unfortunately, due to computational limitations, the transport model, and thus the inversion calculation, needs to be confined to the regional domain of interest then. As the inversion problem is intrinsically global, however, such a regional inversion needs to be nested into a global inversion. Here, we consider the regional inversion for Europe using CarboScope-Regional (CSR) as described in (Munassar et al., 2023; Munassar et al., 2022), which is using the two-step scheme (Rödenbeck et al., 2009) to provide boundary conditions from a global inversion to the regional inversion. Even though the set-up of the regional inversion does include the diurnal cycle in the a priori fluxes, it is nevertheless prone to biases passed on through the lateral boundary conditions calculated by the global inversion currently not taking the diurnal cycle of CO<sub>2</sub> fluxes into account. In addition, the inversion is affected by imperfect representation of diurnal cycle in the transport model.

110 In this study, we focus on the impact of not having the diurnal cycle in the current global CarboScope set-up, both on the result of the global inversion and the inherited impact on the CSR results for Europe. Differences in CO<sub>2</sub> mole fractions simulated with and without diurnal variations in NEE are calculated by forward runs of the global transport model. These differences are then inverted by a global inversion to address the impact in flux estimates. We analysed the flux differences on the global scale, in coarse latitude bands, as well as over a set of regions covering the whole globe. After that, the indirect effect of diurnal variations passed to regional inversions via the far-field influences was evaluated by using CSR in the regional domain of Europe that employs a mesoscale transport model.

120 The organisation of the manuscript is as follows: the next Section describes the methods applied in this experiment elucidating the inversion setup, the prior information obtained from the biosphere flux model, and the atmospheric transport models (Section 2). Results of CO<sub>2</sub> mixing ratio differences calculated with biosphere fluxes through forward model simulations across site network are presented in Section 3, as well as differences in NEE estimates due to the impact of the diurnal cycle effect. Section 4 is devoted to the discussion of the results analysed at global and regional scales highlighting the implications for carbon budget estimates. We summarise the key findings and relating perspectives of this study in Section 5.

## 125 **2 Methods**

### **2.1 Simulating the diurnal rectification of atmospheric CO<sub>2</sub>**

130 Modelled CO<sub>2</sub> mixing ratios are calculated for an atmospheric station network distributed around the world, as typically used for a global atmospheric inversion (Fig. 1). The CS global inversion uses atmospheric data collected from 169 stations around the world. Part of the stations provide continuous measurements, typically at hourly time intervals, while others provide flask samples collected at discrete times (typically weekly). According to the design of this experiment, we chose a subset containing 78 stations that consistently provides data from 2010 onwards, as in the CarboScope inversion run s10oc\_v2022



([http://www.bgc-jena.mpg.de/CarboScope/?ID=s10oc\\_v2022](http://www.bgc-jena.mpg.de/CarboScope/?ID=s10oc_v2022)). The transport model TM3 (Heimann and Körner, 2003) is run with biogenic terrestrial fluxes from FLUXCOM (Jung et al., 2020). As land NEE has the largest diurnal cycle together with atmospheric transport, only the biogenic flux component is taken into account to simulate CO<sub>2</sub> dry mole fractions. Two forward runs are performed to generate simulations of CO<sub>2</sub> dry mole fractions: one with diurnal variations in NEE and one without diurnal variations (by using daily averaged fluxes). Afterwards, the differences between simulations based on daily averaged NEE and simulations based on hourly NEE were calculated for each monitoring site across all the network. These differences in simulated CO<sub>2</sub> dry mole fractions are inverted in CS to quantify the impact in NEE estimates. This was done for practical considerations, as inverting a mole fraction difference is equivalent to performing two inversions and then obtaining the difference between the retrieved fluxes, due to the linearity of atmospheric tracer transport and inverse estimation.

## 2.2 Inversion setups

CarboScope (CS) is used at the global scale using the transport model TM3 (Heimann & Körner, 2003) at a spatial resolution of 5°x4°. As the standard CarboScope CO<sub>2</sub> inversion uses fixed ocean CO<sub>2</sub> fluxes from an interpolation of surface-ocean *p*CO<sub>2</sub> data, the state space vector is confined to the biogenic terrestrial flux component that is corrected spatially and temporally based on Bayesian inference (Enting, 2002). As the fluxes are resolved on a daily time step, the diurnal cycle in terrestrial ecosystems is not accounted for. The spatial and temporal autocorrelations of the prior error are exponentially decaying functions with 1200 km spatial correlation length and 30 days temporal correlation length.

To investigate the effect of the CO<sub>2</sub> rectifier effect on regional fluxes, CSR is used to optimise NEE at 0.5°x0.5° spatial and 3-hourly temporal resolutions over specific regional domains, such as Europe in this study. In this case, the TM3 transport model is replaced with the regional atmospheric transport model STILT, providing output at 0.25° horizontal resolution. It is important to note that a-priori biogenic fluxes used in CSR do account for the diurnal cycle. Thus, our investigation focuses on the influence of the CO<sub>2</sub> diurnal cycle as passed into the regional domain through initial and boundary conditions. The lateral boundary conditions are provided to the regional inversion by the two-step inversion scheme explained in Rödenbeck et al. (2009). Details of CS and CSR configurations, including prior uncertainty prescription, are listed in Table 1. For this experiment setup, ocean fluxes and anthropogenic emissions are omitted in both CS and CSR, because these cancel out in the difference.

The uncertainty of the model-data mismatch is defined similarly in CS and CSR. It comprises a combination of the uncertainties arising from measurements, atmospheric transport, and spatial representation. Weekly values of the errors are assigned to stations based on a classification regarding the ability of atmospheric transport model to represent atmospheric dynamics over the locations of stations. For instance, tall towers, mountain sites, and stations located at/near shores and aircraft samples have an error of 1.5 ppm, while surface sites that represent complex circulations are assigned with a relatively larger error (2.5 ppm). For hourly measurements, the error value is inflated depending on the number of data points assimilated per week such that



the hourly error becomes the weekly error times the square root of the number of weekly hours (e.g., 42 hours in case a time  
165 window of 6 hours per day is chosen and if there are no data gaps).

### 2.3 Transport models

TM3 is an Eulerian transport model that solves the continuity equation (plus parametrisations of boundary layer and convective  
mixing) for atmospheric tracers in a three dimensional grid over the globe (Heimann and Körner, 2003). The model is driven  
by meteorological fields, such as wind velocity, air temperature, surface pressure, and specific humidity, obtained from NCEP  
170 reanalysis data (Kalnay et al., 1996). The tracer advection is determined by the mixing ratio and gradient of the tracer in grid-  
boxes based on the slopes scheme developed by Russell and Lerner (1981). In addition, the vertical transport is resolved by  
vertical diffusion and cumulus cloud transport deduced through evaporation fluxes, which are taken from meteorological fields.  
TM3 is run here at  $5^\circ \times 4^\circ$  spatial resolution with 19 vertical levels spanning the troposphere and the stratosphere. Since the  
model is initialised with a homogeneous background of the tracer concentration, running the model for at least one year before  
175 the period of interest is done to avoid any impact resulting from the model spin-up.

In the regional inversion CSR, the Stochastic Time-Inverted Lagrangian Transport model STILT (Lin et al., 2003) is used at a  
finer horizontal resolution of  $0.25^\circ \times 0.25^\circ$  to resolve the atmospheric mesoscale variability via tracking the dispersion of tracers  
backward in time from starting locations “receptors”. Forecasted meteorological data obtained from the ECMWF Integrated  
Forecasting System (IFS) drive an ensemble of virtual particles at receptor locations, normally over stations where atmospheric  
180 data are sampled. The particles are transported ten days backward and the surface influence functions (“footprints”) are stored  
at  $0.25^\circ$  horizontal resolution and hourly time steps. A daytime window of six hours (11:00 to 16:00 LT) is chosen for low  
elevation stations. For high altitude sites such as mountain stations, a nighttime window of 23:00 to 04:00 LT is used to select  
free troposphere conditions. Note that the vertical resolution of the underlying meteorological data is much higher for STILT  
(89 levels up to about 20 km height) compared to TM3.

### 185 2.4 Biogenic terrestrial fluxes

In Bayesian inversion formalism, an a-priori knowledge of the control parameters is essential to regularise the solution of the  
underdetermined system (Enting, 2002). Typically, prior fluxes of  $\text{CO}_2$  representing the exchange between the surface and the  
atmosphere are taken from bottom-up estimation. As we aim to assess the impact of  $\text{CO}_2$  diurnal cycle on the flux estimate,  
the fluxes are confined to the biogenic terrestrial component. The experiment was designed to invert the differences in mole  
190 fractions simulated with two variants of biosphere fluxes (i.e., with and without the diurnal cycle in the biosphere fluxes),  
rather than the formal way of implementing two inversions that would account for such variations in the prior biosphere fluxes.  
Hourly NEE calculated from FLUXCOM (Bodesheim et al., 2018), a data-driven upscaled flux product, is used as a variant  
that includes information of the  $\text{CO}_2$  diurnal cycle in CS. In addition, another variant of these fluxes was created by averaging  
these fluxes from hourly to daily.



195 To quantify the impact of CO<sub>2</sub> diurnal cycle, first two forward runs using the global model TM3 were performed. The  
differences in CO<sub>2</sub> simulations, extracted for a global set of measurement locations, were calculated by subtraction between  
the daily- and hourly-based simulations. To derive the impact on retrieved fluxes, these differences in CO<sub>2</sub> simulations were  
then subsequently inverted using the standard CS configuration, except that all the prior fluxes and the initial CO<sub>2</sub> mole fraction  
in the model atmosphere were set to zero (while the prior uncertainty remained identical to that of the standard inversion). This  
200 procedure is thus equivalent to using the difference of the results from two hypothetical inversions performed with and without  
diurnal cycle in the priors. To find out the indirect impact on the regional flux estimates in the regional inversion CSR, a two-  
step inversion was done using the inverted differences in the “far-field contribution” from the global inversion.

### 3 Results

#### 3.1 Differences in CO<sub>2</sub> mole fractions

205 We present results from the difference between the two forward runs performed with the transport model TM3 over a set of  
atmospheric stations distributed throughout the globe for the period of time 2010-2020 (the transport model was coupled with  
hourly and daily averaged biogenic fluxes that are obtained from FLUXCOM, see Sect 2.4). The time-averaged differences in  
CO<sub>2</sub> mole fractions between daily and hourly simulations range from -2.49 to 6.97 ppm (1 ppm = 1 μmol mol<sup>-1</sup>), Fig. 1. Most  
of the sites (113) show positive differences with a mean of 0.67 ppm, while the remaining 34 sites demonstrate negative  
210 differences with a mean of -0.41 ppm. A portion of 27 sites of those 34 are flask sites located either in remote islands or at  
shores. Therefore, such sites are affected by large-scale ocean background with little terrestrial influences as well as by areas  
that contain mixed footprints from land and ocean. This implies that ignoring the diurnal cycle of CO<sub>2</sub> leads to an excess of  
CO<sub>2</sub> mole fraction over sites that are dominated by land footprints and to lower mole fractions over sites that are affected by  
ocean footprints in comparison with the simulations done with the diurnal cycle included.

215

The differences due to the CO<sub>2</sub> diurnal cycle effect are also assessed separately for the different types of sites to distinguish  
their representativeness of land and ocean backgrounds. A large number of sites are located in lands and thus can have a good  
representativeness of the biosphere signal. Most of these sites are tall towers (33), continental sites (32), and surface sites (31),  
over which the largest positive mean differences in simulated CO<sub>2</sub> mole fractions occur (0.70 ppm, 0.63 ppm, and 0.77 ppm,  
220 respectively, see Fig. 2, left panel). A number of 29 remote sites, mostly situated in islands, shows a very weak impact with a  
0.02 ppm mean difference. In addition, some sites that poorly represent the biosphere footprints such as ocean, aircraft,  
baseline, and mountain sites have quite small negative differences in CO<sub>2</sub> mole fraction simulations (-0.1 ppm averaged over  
these four types).

A large impact is observed during the growing season as the amplitude of the diurnal cycle reaches its maximum due to the  
225 strong uptake of CO<sub>2</sub> occurring under best conditions of light availability and soil water content. Figure 2 (right panel) shows  
monthly differences of CO<sub>2</sub> dry mole fractions averaged for eleven years (2010-2020) over 88 stations that dominate the



diurnal impact in the Northern Hemisphere. All of these stations are towers, surface, or continental sites, which have a reliable representativeness of land footprints. The differences amid the analysed years range between 0.11 ppm and 1.37 ppm with a mean difference of 0.71 ppm. The median computed over these years is 0.70 ppm confirming a consistency with the mean.

230 The large spreads of the monthly differences across years indicate a remarkable interannual variability of the diurnal impact. In June-July-August the mean difference amounts to 1.33 ppm, larger than the rest of the months, while the smallest differences were found in January-February-December with a mean of 0.38 ppm. The transition periods (March-April-May and September-October-November), close to the onset and termination of carbon uptake period, have moderate and relatively similar differences in CO<sub>2</sub> mixing ratios (0.85 and 1.0 ppm, respectively).

### 235 3.2 Differences in NEE estimates

To outline the impact of CO<sub>2</sub> diurnal cycle on the flux estimates, we next focus on analysing the differences in terrestrial NEE derived by the global CS inversion from the differences in CO<sub>2</sub> mixing ratios for the period 2010-2020. The diurnal cycle effect in the global annual budget of terrestrial biogenic fluxes estimated in the CS inversion results in a difference of 0.04 Pg C yr<sup>-1</sup> averaged over the analysed years with a standard deviation of 0.13 Pg C yr<sup>-1</sup>. This difference in the global scale is rather

240 small and equivalent to about 2 % of the mean annual terrestrial flux (-1.79 Pg C yr<sup>-1</sup>), and only to around 1 % of the prior uncertainty assumed for the biogenic fluxes. These findings suggest that the diurnal cycle of CO<sub>2</sub> does not have a significant impact on the annual global flux budget as, due to the fact that global CO<sub>2</sub> flux estimates are well constrained by the growth rate of atmospheric CO<sub>2</sub> mole fractions, the diurnal cycle effect has to be compensated for between subregions and months. Even though there are noticeable seasonal variations in the impact of CO<sub>2</sub> diurnal cycle effect (Fig. 3), the negative differences

245 during June-July-August are compensated by the positive differences during January-February-December and March-April-May when accounting for the impact on the annual scale. Differences during September-October-November remain around zero.

We next quantified the impact for latitudinal bands. Despite the negligible impact of the diurnal cycle at the global scale, the

250 results indicate quite large differences in these bands (confined to NEE over lands as ocean fluxes are not adjusted in the inversion set-up used here). Figure 4 illustrates that the largest differences are estimated between 90°S–15°S (0.39 Pg C yr<sup>-1</sup>) and between 15°S–15°N band (-0.46 Pg C yr<sup>-1</sup>), on an order of magnitude similar to the original flux. In the bands 15°N–45°N and 45°N–90°N, the differences are smaller than the flux estimates but still non-negligible, with -0.17 and 0.27 Pg C yr<sup>-1</sup> change, respectively. As noted before, the overall difference over global land is quite small owing to the symmetry of

255 differences in sign and magnitude along the latitude bands. The negative differences found in the bands that extend from equatorial to tropical areas in the North (15°S–15°N and 15°N–45°N) are translated to stronger sinks in the corrected flux budgets. On the other hand, the bands containing temperate and boreal zones (90°S–15°S and 45°N–90°N) show positive differences, which imply additional sources in the corrected flux budgets. Note that the size and even the sign of the effects quantified here may depend on the size and distribution of diurnal variations in the flux data set employed in the forward runs,





260 as well as on the inversion set-up and choice of stations. Therefore, they are meant as diagnostics for the diurnal effect of CO<sub>2</sub>.  
Even if the corrections of the flux budgets applied in this paper are denoted in Figures as “CorrectedBudget”, they are tentative  
changes based on the specific diurnal cycles from FLUXCOM and the specific inversion set-up and station set used here.  
The excess of simulated CO<sub>2</sub> mole fractions resulting from using daily NEE makes the inversion adjust to stronger sinks as  
compensatory fluxes, while the underestimation of simulated CO<sub>2</sub> mole fractions (seen at only a few sites) is compensated by  
265 increasing sources. Basically, the correction to be added to the inversion using daily mean priors is an inversion of the  
difference of hourly - daily mean prior fluxes. Therefore, the positive differences shown in Fig. 4 lead to a weaker sink (or  
additional CO<sub>2</sub> sources) in the posterior fluxes and vice versa for the negative differences.

To investigate the aforementioned compensation effect in a set of subregions across the globe, we analysed the differences  
270 calculated with CS over the set of regions used in the TransCom experiment (Gurney et al., 2003). Figure 5 indicates large  
changes in the annual flux budgets over most of the regions. As expected, the results exhibit positive and negative differences  
over land, leading to the compensation in the annual mean difference and flux estimates over the globe. In this context, negative  
differences imply either an underestimation of CO<sub>2</sub> uptake or overestimation of CO<sub>2</sub> release by inversions when neglecting the  
diurnal cycle in the flux. Negative differences are calculated for Northern and Southern Africa, Eurasian temperate forests,  
275 North American boreal forests, and tropical Asia. On the other hand, positive differences are found over North American  
temperate forests, South American tropics and temperate, Eurasia boreal, Australia, and Europe.

The largest negative difference (-0.79 Pg C yr<sup>-1</sup>) among the TransCom regions is found in Northern Africa, which would turn  
the flux budget from a net source of 0.50 Pg C yr<sup>-1</sup> to a net sink of -0.29 Pg C yr<sup>-1</sup>. Over Temperate North America, a large  
positive difference of 0.38 Pg C yr<sup>-1</sup> is found, pushing the flux budget from a net source (about 0.15 Pg C yr<sup>-1</sup>) to an even larger  
280 net source (0.53 Pg C yr<sup>-1</sup>). Given the positive and negative differences seen in “Diff” Fig. 5, the mean annual difference for  
the global scale stays roughly around zero globally (see above). Generally, the posterior fluxes estimated by CS include biases  
with underestimated sinks persisting over regions that show negative differences and with overestimated sinks over regions  
characterised with positive differences. These findings demonstrate that the systematic biases in the annual flux budgets get  
larger when disaggregating the total land to the continental and local scales.

285

### 3.3 Analysis of the diurnal cycle effect of CO<sub>2</sub> over the European continent

This section will address results from the global CS and from CSR for the domain used for the regional inversion covering  
most of Europe (15°W-35°E, 33°S-73°N). It should be noted that this CSR-domain is different than the one used for Europe  
in the TransCom set of regions in CS in Fig 5, and therefore NEE differences and flux estimates are expected to be slightly  
290 different over both domains. The differences for this domain estimated with CS due to missing the CO<sub>2</sub> diurnal cycle in CS  
amounts to 0.12 Pg C yr<sup>-1</sup>, averaged over the period 2010-2020. It represents about 25% of the prior NEE uncertainty assumed  
for annual fluxes for this area, but also exceeds the posterior uncertainty by a factor of 2. Furthermore, the mean flux budget



computed for the respective years was  $-0.37 \text{ Pg C yr}^{-1}$ . Thus, this diurnal effect leads to a bias of around 32% in the annual flux estimates in Europe. There are also slight monthly variations of the impact seen among years (Fig. 6, “CS”).

295 To assess the diurnal effect on the regional inversion for Europe, CSR was used to estimate the differences in NEE due to the diurnal cycle effect passed on from the global inversion via the far-field contributions calculated by CS. The mean differences over all the years appear to be consistent in both the magnitude and temporal patterns between CSR and CS estimates, albeit larger in CSR. The mean difference calculated with CSR results in  $0.15 \text{ Pg C yr}^{-1}$ , representing 32% of the prior uncertainty assumed in CSR. When relating the differences to posterior uncertainty calculated with CSR over Europe, the impact even  
300 exceeds the magnitude of posterior uncertainty by a factor of around 2.5. Additionally, the  $\text{CO}_2$  diurnal effect leads to a bias of around 48% in  $\text{CO}_2$  estimates ( $-0.31 \text{ Pg C yr}^{-1}$ ) that were calculated as the mean annual flux budget for the respective years by CSR.

Although there are notable variations in monthly differences of CSR over years shown in the error bars reflecting the spread over years (see Fig. 6, “CSR”), they agree in the magnitude and in month-to-month variations with those of CS. Positive  
305 differences result during winter and spring, while the differences tend to be negative in the growing season, albeit the mean absolute values are smaller than those that are found during spring. The variations between years appear to be small in winter compared to the larger variations occurring during spring and summer. This consensus in the monthly patterns evident over all the years indicates an underestimation of  $\text{CO}_2$  uptake during the growing season as well as an underestimation of  $\text{CO}_2$  release during the rest of the year.

### 310 3.4 How much does the $\text{CO}_2$ diurnal cycle affect inter-annual variability?

Figure 7 illustrates the annual flux differences concerning the diurnal cycle effect of  $\text{CO}_2$ , and the corresponding flux estimates. The findings indicate how much the lack of the  $\text{CO}_2$  flux diurnal cycle affects annual  $\text{CO}_2$  flux budgets for the individual years, globally and regionally over the CSR-Europe domain. Including the diurnal cycle of  $\text{CO}_2$  generally shifted estimates towards sources over all the years, albeit in different magnitudes. The analysis here confirms that the interannual variability (IAV) of  
315 flux estimates is less sensitive to the diurnal variations at the global scale (“Global”, Fig. 7). Although the mean annual flux differences between daily and hourly NEE-based inversions stay around zero over the analysed years, they can be slightly larger in individual years (standard deviation of  $0.13 \text{ Pg C yr}^{-1}$ ). Furthermore, the similarity of IAV for the annual flux estimates and the corrected estimates ( $0.82 \text{ Pg C yr}^{-1}$  and  $0.88 \text{ Pg C yr}^{-1}$ , respectively) indicates the negligible influence of  $\text{CO}_2$  diurnal variations on the IAV of global estimates. By contrast, the results demonstrate a larger impact on the IAV of the regional flux  
320 estimates over Europe. The NEE differences calculated by CS resulted in an IAV amplitude of  $-0.06 \text{ Pg C yr}^{-1}$ , about half the IAV amplitude of the estimated fluxes ( $-0.14 \text{ Pg C yr}^{-1}$ ).

In terms of the indirect effect of diurnal variations passed to the regional inversion through far-field influences, CSR suggests a slightly weaker uptake ( $-0.16 \text{ Pg C yr}^{-1}$ ) than CS does ( $-0.25 \text{ Pg C yr}^{-1}$ ) after taking into consideration the diurnal cycle effect. The IAV of the differences over Europe calculated with CSR amounts to  $0.09 \text{ Pg C yr}^{-1}$ , suggesting a significant impact when  
325 comparing it with the IAV of the annual flux estimates  $0.20 \text{ Pg C yr}^{-1}$ . Noteworthy is that CS and CSR differ in the atmospheric



transport models, and the spatial correlation of prior uncertainty are differently set. Consequently, such different setups are likely resulting in the discrepancies between CS and CSR in evaluating the impact of the CO<sub>2</sub> diurnal cycle.

To show the spatial patterns of the differences in the domain of Europe, posterior NEE estimated in a regional (CSR) inversion is analysed together with the differences due to the diurnal variations in CS and the corrected estimates. Figure 8 depicts the annual mean of NEE without and with the diurnal cycle of CO<sub>2</sub> taken into account, and the differences, averaged over eleven years. Positive corrections to NEE fluxes occur generally along the Mediterranean coast (southern and western Europe), as well as north-western Europe (southern UK, Benelux, northern Germany). On the other hand, over Scandinavia, northern UK, and in central Europe smaller negative corrections (meaning higher CO<sub>2</sub> uptake in the respective regions) are persistent. These findings refer to a notable impact of CO<sub>2</sub> diurnal cycle on NEE estimated over smaller local domains, particularly over regions where CO<sub>2</sub> exchange between the atmosphere and terrestrial ecosystems is more active. It should be noted that because of the partial compensation between subregions with positive and negative differences, the annual mean difference in NEE fluxes will also become smaller as larger areas are aggregated, underlining the increasing importance of the CO<sub>2</sub> diurnal effect as finer spatiotemporal scales are analysed.

#### 340 **4 Discussion**

The seasonal features of the covariation between atmospheric transport convection and terrestrial CO<sub>2</sub> fluxes discussed in (Denning et al., 1995; 1996a; 1996b) hold true for the diurnal variability of both the atmospheric dynamics and biota. Ignoring the diurnal cycle of CO<sub>2</sub> in the biosphere fluxes used as priors in inversions results in significant biases in CO<sub>2</sub> mole fraction simulations calculated with atmospheric transport models. In this study, we quantified the effect on the CO<sub>2</sub> mole fraction and estimated NEE arising from the diurnal cycle of CO<sub>2</sub> at global and regional scales. We find that CO<sub>2</sub> mole fractions simulated at sites that are dominated by land footprints with the inclusion of the biogenic diurnal variability tend to be lower than those simulated with daily averaged biogenic fluxes; the opposite effect is found for the simulations calculated over sites that are more representative for ocean backgrounds. Also, the impact found over locations with dominant land backgrounds that also have a larger number of sites was much larger in magnitude than that found over locations with ocean backgrounds. This typically points to the prevalence of the diurnal effect over lands, particularly in the biogenic terrestrial ecosystems in the northern Hemisphere.

The differences in simulated CO<sub>2</sub> mixing ratios inevitably lead to differences in NEE estimates derived from atmospheric inversions. Regarding the global total flux, the impact of ignoring the diurnal cycle is compensated for by the seasonal and spatial variations, as the inversion constrains reasonably well the long term mean CO<sub>2</sub> despite when and where the flux adjustments are allocated. This is evident by the small annual difference of 2 % of the global land flux estimate (-1.37 Pg C yr<sup>-1</sup>), which lies within the range of total atmosphere-to-land sinks (1.10 and 1.70 Pg C yr<sup>-1</sup>) estimated by inversions as reported to the Global Carbon Budget (GCB) in Friedlingstein et al. (2022), to which CS contributes. Consequently, neither IAV nor

the magnitude of global flux estimates has significantly changed after applying corrections of the CO<sub>2</sub> diurnal effect over the analysed period of time, indicating a negligible impact in the integrated global flux budget.

360 However, the diurnal cycle of CO<sub>2</sub> strongly influences NEE estimates calculated at regional domains. For example, results analysed over the land region within the CSR domain covering Europe yield an NEE difference of 48% and 32% of the annual estimates calculated by CSR-Europe and the global CS, respectively. The annual mean differences represent a shift of flux estimates towards higher CO<sub>2</sub> sources in both inversions. Even though the diurnal cycle is taken into account in CSR within the regional domain by using biogenic prior fluxes obtained from biosphere flux models at hourly time intervals, the differences  
365 from the global CS are passed to CSR estimates as an indirect effect through the lateral boundary conditions. By comparing two products of lateral boundary conditions obtained from CS and TM5-4DVar global inversions, Munassar et al. (2023) also found a non-negligible sensitivity of regional inversions to systematic biases in lateral boundary conditions. They found an impact of 0.40 Pg C yr<sup>-1</sup> resulting from the lateral boundary conditions over the CSR-domain of Europe for 2018. As the diurnal cycle of CO<sub>2</sub> was missing in the setup of CS used in that study, part of this impact can be potentially attributed to the  
370 diurnal cycle effect. This suggests that the systematic biases in regional inversions due to lateral boundary conditions would be attenuated to approximately 0.25 Pg C yr<sup>-1</sup> if taking into account a bias of 0.15 Pg C yr<sup>-1</sup> arising from the diurnal cycle effect found in CS via this study.

The problem of the seasonal rectifier considered by Denning et al (1995) could be solved by explicitly estimating seasonal variations from the atmospheric data. Unlike this, unfortunately, the diurnal cycle cannot be deduced from the atmospheric  
375 data, primarily owing to the limitation of the assimilated data to either day-time or night-time. Even though a weak variability may emerge due to the diurnal variability of atmospheric vertical transport, it cannot reproduce a realistic rectification observed in atmospheric CO<sub>2</sub> concentrations (Yi et al., 2000) without coupling the transport variability with a-priori information of terrestrial flux variability. In an experiment done at a site level with and without diurnal biosphere variations, (Denning et al., 1996b) found that diurnal CO<sub>2</sub> concentrations simulated with diurnal flux variations were more realistic in phase when  
380 compared to observations, while those simulated with mean prescribed biogenic fluxes follow the phase of the PBL depth. This indicates the importance of accounting for the diurnal variations when retrieving atmospheric CO<sub>2</sub> dry mole fractions. Further assessment of the uncertainty of such variations produced from biosphere models will benefit the characterization of estimated CO<sub>2</sub> flux errors among the inversions contributing to the Global Carbon Project (GCP), but also extend the understanding of biogenic terrestrial variability. Notwithstanding, the FLUXCOM model, used in our experiment, is thought  
385 to have a good ability to resolve the diurnal cycle of CO<sub>2</sub> because the model is trained against observations, meteorology, and remote sensing data using different prediction approaches to reproduce GPP at half-hourly time scales (Bodesheim et al., 2018).

In the tropics (30°S-30°N) the difference was found to be -0.65 Pg C yr<sup>-1</sup> over land, proposing a much stronger sink (-1.48 Pg C yr<sup>-1</sup>) than CS estimated (-0.83 Pg C yr<sup>-1</sup>). Friedlingstein et al. (2022) found that atmospheric inversions suggested the land  
390 tropics to be close to neutral over the past decade ranging between -0.90 and 0.70 Pg C yr<sup>-1</sup> with high uncertainty. After considering the impact of diurnal cycle, CS estimates for the tropical lands will tend to result in stronger CO<sub>2</sub> sinks. On the



contrary, latitude bands containing temperate forest zones show weaker CO<sub>2</sub> uptake when the correction due to the diurnal cycle is taken into account. That is, the land sink over the northern extra-tropics (30°N-90°N) amounts to -0.53 Pg C yr<sup>-1</sup> after correcting for the diurnal cycle effect compared to -1.12 Pg C yr<sup>-1</sup> estimated with CS for 2010-2020. Hence, the underestimation of CO<sub>2</sub> uptake in the tropics and the overestimation of CO<sub>2</sub> uptake in temperate zones are the trade-off that maintains CO<sub>2</sub> mass-balance in the global carbon budgets derived by CS.

Given the non-negligible impact of the diurnal cycle of CO<sub>2</sub> over the latitude bands, the impact is quantified in the context of annual flux budgets at continental and regional scales using CS results over the globe. NEE differences were analysed over a set of regions, encompassing the whole land area around the world, as used in the TransCom experiment (Gurney et al., 2003), and are shown in Fig. 5. The differences over most of the land regions exhibit large biases in the posterior annual fluxes over the analysed regions. This has been outlined by applying flux corrections that suggest additional sources in the posterior annual fluxes over some regions such as the temperate north America region, while stronger sinks are suggested over other regions as is the case of northern Africa. The differences of the two extreme cases in northern Africa and in temperate north America (-0.79 and 0.38 Pg C yr<sup>-1</sup>, respectively) exceed the corresponding uncertainties (0.54 and 0.22 Pg C yr<sup>-1</sup>, respectively) calculated as the spread among different model estimates reported in Gurney et al. (2004) within the TransCom Experiment. The global mean difference is, however, small and consistent with the global total uncertainty. These findings indicate that misallocations of flux adjustments in different regions occur as a result of lacking diurnal information in the atmospheric inversions. Noteworthy, some regions that show large differences such as Africa are repeatedly characterised with a larger uncertainty in inversion estimates by previous studies (e.g., (Gurney et al., 2004; Stephens et al., 2007)). These studies attribute the compensatory fluxes over such regions to the lack of observational constraints and thus may be allocated with the surplus of flux budgets remaining from the well-constrained regions.

NEE differences due to the diurnal cycle effect show year-to-year variations that affect IAV of the flux estimates. This is evident by the sensitivity of NEE IAV to the diurnal cycle of CO<sub>2</sub> assessed over the TransCom land regions (Table 2): Regions with a large mean difference in NEE have a larger IAV of the diurnal cycle impact such as northern Africa, north American temperate, and south American tropics, but also the rest of the land regions suggest a large IAV in NEE differences. This finding implies that both the magnitude of NEE estimates and IAV are affected by the exclusion of CO<sub>2</sub> diurnal cycle at regional scales. Even though evaluating the uncertainty of diurnal variations remains an important assignment, the inclusion of such variations in biogenic prior fluxes used in inversions generally decreases biases in CO<sub>2</sub> mole fraction simulations and thus reduces biases in estimated CO<sub>2</sub> fluxes by inversions.

Based on the results, the stronger uptake dominant in the northern Hemisphere attributed to the CO<sub>2</sub> fertilisation effect and deposition of nitrogen (Ciais et al., 2019; Sarmiento et al., 2010) cannot be predicted accurately by inversions that do not include diurnal cycle of CO<sub>2</sub> in their prior fluxes. The greatest impact of the CO<sub>2</sub> diurnal effect obviously appears over regions with strong biological activities as seen from a diagnostic map of CO<sub>2</sub> mole fractions simulated at the model surface level with the inverted response of the diurnal effect across the world (Fig. 9). Averaging out the diurnal variations in the biosphere flux



model FLUXCOM has led to overestimation of CO<sub>2</sub> mole fractions, largely over the temperate areas where a large amount of carbon is stored in the temperate forests in North America, Europe, Eastern Asia in the Northern Hemisphere as well as over the rainforests of South America and Australia in the Southern Hemisphere (Erb et al., 2018).

430 By contrast, CS tends to underestimate CO<sub>2</sub> mole fractions as the CO<sub>2</sub> diurnal cycle of FLUXCOM is flattened in the tropical areas, in particular central Africa and south eastern Asia. This pattern is also, to a lesser extent, seen over the boreal forests in the further North. These results outline the discrepancies in the annual flux budgets computed over the TransCom regions and over the latitude bands, where the magnitude of flux corrections applied as a reconciliation to the diurnal CO<sub>2</sub> effect. It should be noted that these corrections are used in this study as diagnostics as the diurnal cycle is subject to uncertainty depending on  
435 the accuracy of the biosphere models to reproduce diurnal variations. Additionally, the spatial patterns of mole fractions over Europe in Fig. 9 correspond quite well to the spatial patterns of posterior flux differences estimated by CSR (Fig. 8).

## 5 Conclusions

Ignoring the diurnal cycle in surface-to-atmosphere CO<sub>2</sub> fluxes leads to a systematic bias in CO<sub>2</sub> mole fraction simulations sampled at daytime, because the daily mean flux systematically misses the CO<sub>2</sub> uptake during the daytime hours. In an  
440 atmospheric inversion using daytime-selected CO<sub>2</sub> measurements at most continental sites and not resolving diurnal cycles in the flux (as is the case for the 60-year global CarboScope CO<sub>2</sub> inversion that operates on a daily flux time step due to limitation in computer memory), this leads to systematic biases in the estimates of the annual sources and sinks of atmospheric CO<sub>2</sub>. In case of the absence of diurnal variations in the prior inputs, correcting the flux estimates is essential to reduce these systematic biases. Such a correction can be applied either to the mole fractions before performing the inversions or to the optimised fluxes  
445 after performing the inversions. In this paper, we diagnosed how large such a flux correction would need to be in annual carbon flux budgets derived from CS and CSR for 2010-2020 at global and regional scales. NEE containing the diurnal cycle of CO<sub>2</sub> flux was obtained from the data-driven biosphere flux estimate by FLUXCOM (Bodesheim et al., 2018) at hourly time scales over the globe. These fluxes were transported by the TM3 model to simulate CO<sub>2</sub> mole fractions. Removing the diurnal cycle of NEE by using daily fluxes leads to an increase of simulated CO<sub>2</sub> mole fractions in comparison with simulations done with  
450 hourly NEE because of the diurnal effect described above. The difference between both simulations was inverted to obtain the impact of this effect on the inversion results. Regarding the net fluxes of CO<sub>2</sub> estimated by the global CarboScope (CS) inversion, the difference in the flux budget due to the diurnal cycle was negligible at the global scale, which is expected as the global annual trend of CO<sub>2</sub> is well-constrained by the observations. However, the impact at the regional and local scales amounts to about 51% relative to the sum of differences and flux estimates. The analysis of NEE differences across latitudinal  
455 bands and for the set of regions used in the TransCom experiment points to larger differences exceeding the magnitude of the estimated annual flux budgets in some regions such as North American temperate and Northern Africa. The overall impact noticed from NEE differences assessed in the TransCom regions across the lands suggests a weaker sink in temperate zones,



particularly in the North, than estimated when ignoring the diurnal cycle. Conversely, accounting for the diurnal cycle of CO<sub>2</sub> fluxes leads to stronger CO<sub>2</sub> sinks in parts of the tropics. This illustrates a compensation effect between the regions that have an opposite sign of the effect to retain global mass balance as discussed above. In addition to the mean flux, also the IAV of flux estimates is affected by the diurnal variations. This may indicate that it would be unrealistic to use climatological diurnal variations to correct the atmospheric CO<sub>2</sub> inversions, though further investigations are required to look into the origin of IAV in the NEE differences (e.g., to determine how much biases come from the amplitude of the diurnal cycle of CO<sub>2</sub> in the biosphere model and from BPL in the transport model). Hence, an assessment on the uncertainty of the diurnal cycle effect among atmospheric inversions will be presented in a follow-up study.

NEE estimates derived from a regional inversion, even if using a diurnal cycle in its regional prior, are still prone to an indirect impact of the diurnal cycle effect through the lateral boundary conditions if coming from a global inversion that is missing diurnal variations in its priors. In our case of CarboScope-Regional (CSR) for Europe using boundary conditions from the global CS, such an impact amounts to approximately 50% of the mean annual flux estimates calculated over Europe.

We conclude that incorporating diurnal variations into the prior fluxes, directly or via a suitable correction, is important in global and regional atmospheric CO<sub>2</sub> inversions.

### **Code and data availability**

The simulations of CO<sub>2</sub> mole fractions, NEE differences derived from the inversions, and codes used for the analysis can be made available upon request to the corresponding author.

### **Competing interests**

At least one of the (co-)authors is a member of the editorial board of Atmospheric Chemistry and Physics and the authors also have no other competing interests to declare.

### **Acknowledgments**

The authors thank Sönke Zaehle for his valuable comments on the manuscript in the internal review. SM, CR, and CG acknowledge the computational support of Deutsches Klimarechenzentrum (DKRZ) where the CarboScope inversion system is being run. We also acknowledge the use of hourly NEE data calculated with FLUXCOM and was provided by Jake Nelson and Sophia Walter.

### **Financial support**

This research has been supported by BMBF through the ITMS-M project under contract 01LK2102A.



## 6 References

- 490 Baker, D. F., Law, R. M., Gurney, K. R., Rayner, P., Peylin, P., Denning, A. S., Bousquet, P., Bruhwiler, L., Chen, Y. H., Ciais, P., Fung, I. Y., Heimann, M., John, J., Maki, T., Maksyutov, S., Masarie, K., Prather, M., Pak, B., Taguchi, S., and Zhu, Z.: TransCom 3 inversion intercomparison: Impact of transport model errors on the interannual variability of regional CO<sub>2</sub> fluxes, 1988-2003, *Global Biogeochemical Cycles*, 20, Artn Gb1002  
10.1029/2004gb002439, 2006.
- 495 Bodesheim, P., Jung, M., Gans, F., Mahecha, M. D., and Reichstein, M.: Upscaled diurnal cycles of land-atmosphere fluxes: a new global half-hourly data product, *Earth System Science Data*, 10, 1327-1365, 10.5194/essd-10-1327-2018, 2018.  
Botía, S.: Greenhouse gas exchange in the Amazon: Carbon dioxide and methane insights from the Amazon Tall Tower Observatory, PhD, Wageningen University, Wageningen, 2022.
- 500 Canadell, J. G., Monteiro, P. M. S., Costa, M. H., Cunha, L. C. d., Cox, P. M., Eliseev, A. V., Henson, S., Ishii, M., Jaccard, S., Koven, C., Lohila, A., Patra, P. K., Piao, S., Rogelj, J., Syampungani, S., Zaehle, S., and Zickfeld, a. K.: Global Carbon and Other Biogeochemical Cycles and Feedbacks, in: *Climate Change 2021 – The Physical Science Basis: Working Group I Contribution to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change*, edited by: Intergovernmental Panel on Climate, C. M.-D., V., P. Z., A. Pirani, S.L. Connors, C. Péan, S. Berger, N. Caud, Y. Chen, L. Goldfarb, M.I. Gomis, M. Huang, K. Leitzell, and E. Lonnoy, J. B. R. M., T.K. Maycock, T. Waterfield, O. Yelekçi, R. Yu, and B. Zhou (eds.)).  
505 Cambridge University Press, Cambridge, 673-816, 2023.
- Chan, D., Ishizawa, M., Higuchi, K., Maksyutov, S., and Chen, J.: Seasonal CO<sub>2</sub> rectifier effect and large-scale extratropical atmospheric transport, *Journal of Geophysical Research*, 113, 10.1029/2007jd009443, 2008.
- Ciais, P., Rayner, P., Chevallier, F., Bousquet, P., Logan, M., Peylin, P., and Ramonet, M.: Atmospheric inversions for estimating CO<sub>2</sub> fluxes: methods and perspectives, *Climatic Change*, 103, 69-92, 10.1007/s10584-010-9909-3, 2010.
- 510 Ciais, P., Tan, J., Wang, X., Roedenbeck, C., Chevallier, F., Piao, S.-L., Moriarty, R., Broquet, G., Le Quéré, C., and Canadell, J.: Five decades of northern land carbon uptake revealed by the interhemispheric CO<sub>2</sub> gradient, *Nature*, 568, 221-225, 2019.
- Deng, A. J., Lauvaux, T., Davis, K. J., Gaudet, B. J., Miles, N., Richardson, S. J., Wu, K., Sarmiento, D. P., Hardesty, R. M., Bonin, T. A., Brewer, W. A., and Gurney, K. R.: Toward reduced transport errors in a high resolution urban CO<sub>2</sub> inversion system, *Elementa-Sci Anthropol*, 5, ARTN 20  
515 10.1525/elementa.133, 2017.
- Denning, A. S., Fung, I. Y., and Randall, D.: Latitudinal gradient of atmospheric CO<sub>2</sub> due to seasonal exchange with land biota, *Nature*, 376, 240-243, 10.1038/376240a0, 1995.
- Denning, A. S., Randall, D. A., Collatz, G. J., and Sellers, P. J.: Simulations of terrestrial carbon metabolism and atmospheric CO<sub>2</sub> in a general circulation model: Part 2: Simulated CO<sub>2</sub> concentrations, *Tellus B*, 48, 543-567, 1996a.
- 520 Denning, A. S., Randall, D. A., Collatz, G. J., and Sellers, P. J.: Simulations of terrestrial carbon metabolism and atmospheric CO<sub>2</sub> in a general circulation model, *Tellus B*, 48, 543-567, <https://doi.org/10.1034/j.1600-0889.1996.t01-1-00010.x>, 1996b.
- Denning, A. S., Takahashi, T., and Friedlingstein, P.: Can a strong atmospheric CO<sub>2</sub> rectifier effect be reconciled with a “reasonable” carbon budget? Keynote Perspective, *Tellus B*, 51, 249-253, 1999.
- Enting, I. G.: *Inverse problems in atmospheric constituent transport*, Cambridge University Press, Cambridge ; New York, xv, 525 392 p. pp., 2002.
- Erb, K.-H., Kastner, T., Plutzer, C., Bais, A. L. S., Carvalhais, N., Fetzl, T., Gingrich, S., Haberl, H., Lauk, C., Niedertscheider, M., Pongratz, J., Thurner, M., and Luyssaert, S.: Unexpectedly large impact of forest management and grazing on global vegetation biomass, *Nature*, 553, 73-76, 10.1038/nature25138, 2018.
- Friedlingstein, P., Jones, M. W., O'Sullivan, M., Andrew, R. M., Bakker, D. C. E., Hauck, J., Le Quéré, C., Peters, G. P., Peters, W., Pongratz, J., Sitch, S., Canadell, J. G., Ciais, P., Jackson, R. B., Alin, S. R., Anthoni, P., Bates, N. R., Becker, M., Bellouin, N., Bopp, L., Chau, T. T. T., Chevallier, F., Chini, L. P., Cronin, M., Currie, K. I., Decharme, B., Djeutchouang, L. M., Dou, X., Evans, W., Feely, R. A., Feng, L., Gasser, T., Gilfillan, D., Gkritzalis, T., Grassi, G., Gregor, L., Gruber, N., Gürses, Ö., Harris, I., Houghton, R. A., Hurtt, G. C., Iida, Y., Ilyina, T., Lujckx, I. T., Jain, A., Jones, S. D., Kato, E., Kennedy, D., Klein Goldewijk, K., Knauer, J., Korsbakken, J. I., Körtzinger, A., Landschützer, P., Lauvset, S. K., Lefèvre, N., Lienert, S., Liu, J., Marland, G., McGuire, P. C., Melton, J. R., Munro, D. R., Nabel, J. E. M. S., Nakaoka, S. I., Niwa, Y., Ono, T., Pierrot, D., Poulter, B., Rehder, G., Resplandy, L., Robertson, E., Rödenbeck, C., Rosan, T. M., Schwinger, J., Schwingshackl, C., Séférian, R., Sutton, A. J., Sweeney, C., Tanhua, T., Tans, P. P., Tian, H., Tilbrook, B., Tubiello, F., van der Werf, G. R.,

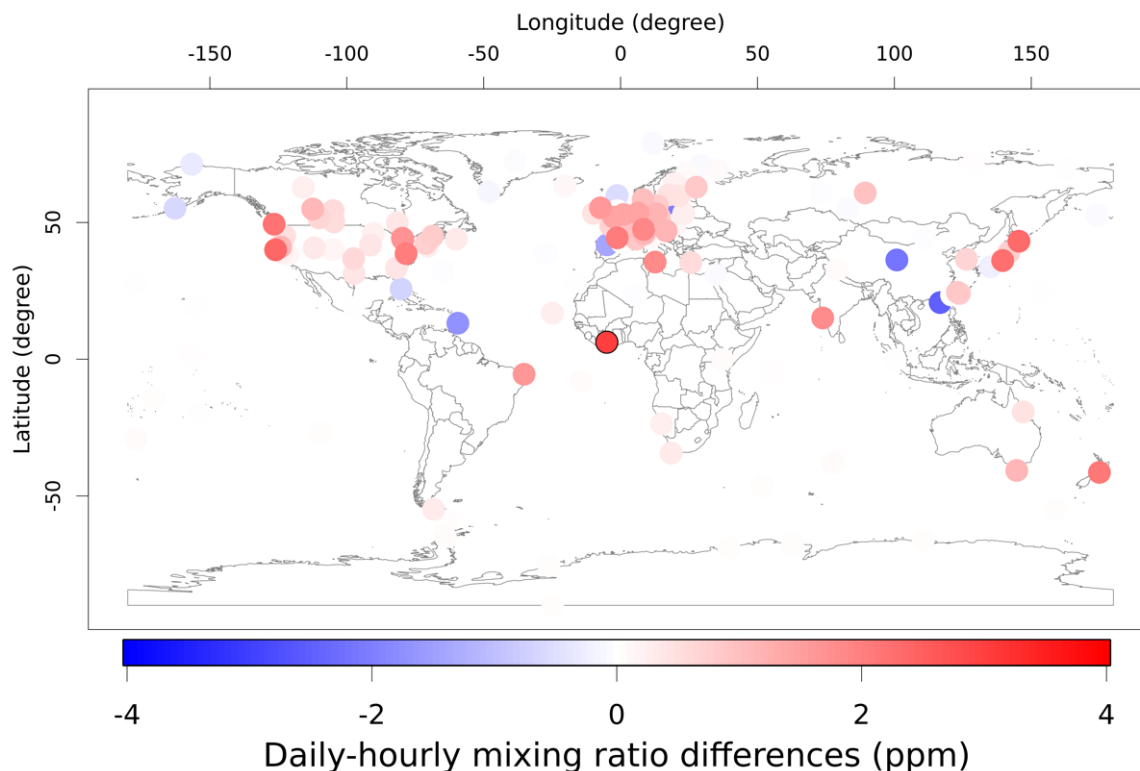




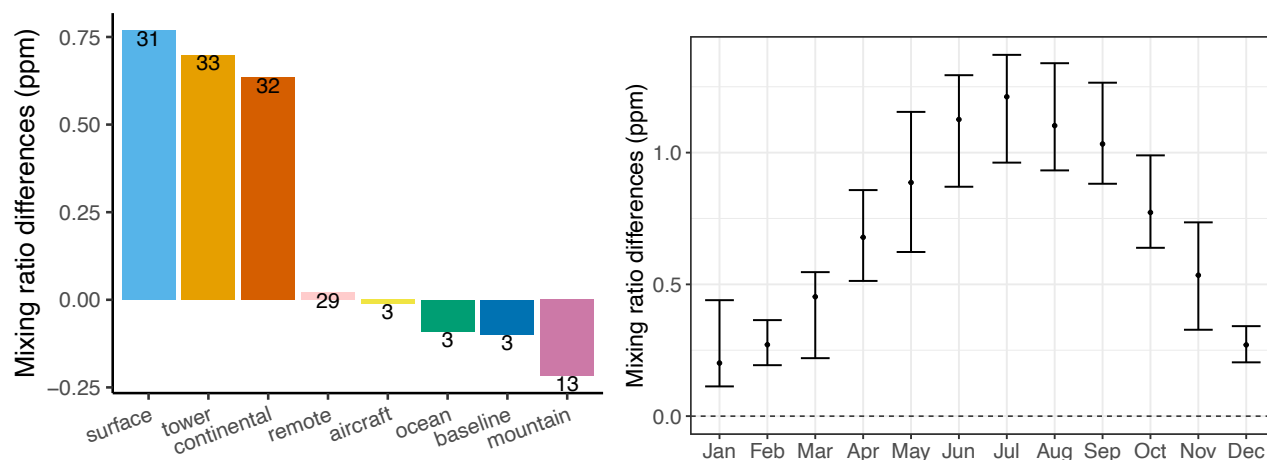
- Vuichard, N., Wada, C., Wanninkhof, R., Watson, A. J., Willis, D., Wiltshire, A. J., Yuan, W., Yue, C., Yue, X., Zaehle, S., and Zeng, J.: Global Carbon Budget 2021, *Earth Syst. Sci. Data*, 14, 1917-2005, 10.5194/essd-14-1917-2022, 2022.
- 540 Gerbig, C., Korner, S., and Lin, J. C.: Vertical mixing in atmospheric tracer transport models: error characterization and propagation, *Atmospheric Chemistry and Physics*, 8, 591-602, DOI 10.5194/acp-8-591-2008, 2008.
- Glanemann, N., Willner, S. N., and Levermann, A.: Paris Climate Agreement passes the cost-benefit test, *Nat Commun*, 11, 110, 2020.
- 545 Gurney, K. R., Law, R. M., Denning, A. S., Rayner, P. J., Baker, D., Bousquet, P., Bruhwiler, L., Chen, Y. H., Ciais, P., Fan, S. M., Fung, I. Y., Gloor, M., Heimann, M., Higuchi, K., John, J., Kowalczyk, E., Maki, T., Maksyutov, S., Peylin, P., Prather, M., Pak, B. C., Sarmiento, J., Taguchi, S., Takahashi, T., and Yuen, C. W.: TransCom 3 CO<sub>2</sub> inversion intercomparison: 1. Annual mean control results and sensitivity to transport and prior flux information, *Tellus B*, 55, 555-579, DOI 10.1034/j.1600-0889.2003.00049.x, 2003.
- 550 Gurney, K. R., Law, R. M., Denning, A. S., Rayner, P. J., Pak, B. C., Baker, D., Bousquet, P., Bruhwiler, L., Chen, Y.-H., Ciais, P., Fung, I. Y., Heimann, M., John, J., Maki, T., Maksyutov, S., Peylin, P., Prather, M., and Taguchi, S.: Transcom 3 inversion intercomparison: Model mean results for the estimation of seasonal carbon sources and sinks, *Global Biogeochemical Cycles*, 18, <https://doi.org/10.1029/2003GB002111>, 2004.
- Heimann, M., and Körner, S.: The global atmospheric tracer model TM3, Model Description and users Manual release, 3, 2003.
- 555 Jung, M., Schwalm, C., Migliavacca, M., Walther, S., Camps-Valls, G., Koirala, S., Anthoni, P., Besnard, S., Bodesheim, P., Carvalhais, N., Chevallier, F., Gans, F., Goll, D. S., Haverd, V., Köhler, P., Ichii, K., Jain, A. K., Liu, J., Lombardozzi, D., Nabel, J. E. M. S., Nelson, J. A., O'Sullivan, M., Pallandt, M., Papale, D., Peters, W., Pongratz, J., Rödenbeck, C., Sitch, S., Tramontana, G., Walker, A., Weber, U., and Reichstein, M.: Scaling carbon fluxes from eddy covariance sites to globe: synthesis and evaluation of the FLUXCOM approach, *Biogeosciences*, 17, 1343-1365, 10.5194/bg-17-1343-2020, 2020.
- 560 Kalnay, E., Kanamitsu, M., Kistler, R., Collins, W., Deaven, D., Gandin, L., Iredell, M., Saha, S., White, G., Woollen, J., Zhu, Y., Chelliah, M., Ebisuzaki, W., Higgins, W., Janowiak, J., Mo, K. C., Ropelewski, C., Wang, J., Leetmaa, A., Reynolds, R., Jenne, R., and Joseph, D.: The NCEP/NCAR 40-year reanalysis project, *B Am Meteorol Soc*, 77, 437-471, Doi 10.1175/1520-0477(1996)077<0437:Tnyrp>2.0.Co;2, 1996.
- 565 Kaminski, T., Heimann, M., and Giering, R.: A coarse grid three-dimensional global inverse model of the atmospheric transport: 2. Inversion of the transport of CO<sub>2</sub> in the 1980s, *Journal of Geophysical Research: Atmospheres*, 104, 18555-18581, 10.1029/1999jd900146, 1999.
- Larson, V. E., and Volkmer, H.: An idealized model of the one-dimensional carbon dioxide rectifier effect, *Tellus B: Chemical and Physical Meteorology*, 60, 525 - 536, 2008.
- 570 Lin, J. C., Gerbig, C., Wofsy, S. C., Andrews, A. E., Daube, B. C., Davis, K. J., and Grainger, C. A.: A near-field tool for simulating the upstream influence of atmospheric observations: The Stochastic Time-Inverted Lagrangian Transport (STILT) model, *J Geophys Res-Atmos*, 108, Artn 4493, 10.1029/2002jd003161, 2003.
- Marcolla, B., Rodenbeck, C., and Cescatti, A.: Patterns and controls of inter-annual variability in the terrestrial carbon budget, *Biogeosciences*, 14, 3815-3829, 10.5194/bg-14-3815-2017, 2017.
- 575 Munassar, S., Rödenbeck, C., Koch, F. T., Totsche, K. U., Gałkowski, M., Walther, S., and Gerbig, C.: Net ecosystem exchange (NEE) estimates 2006–2019 over Europe from a pre-operational ensemble-inversion system, *Atmos. Chem. Phys.*, 22, 7875-7892, 10.5194/acp-22-7875-2022, 2022.
- Munassar, S., Monteil, G., Scholze, M., Karstens, U., Rödenbeck, C., Koch, F. T., Totsche, K. U., and Gerbig, C.: Why do inverse models disagree? A case study with two European CO<sub>2</sub> inversions, *Atmos. Chem. Phys.*, 23, 2813-2828, 10.5194/acp-23-2813-2023, 2023.
- 580 Peylin, P., Baker, D., Sarmiento, J., Ciais, P., and Bousquet, P.: Influence of transport uncertainty on annual mean and seasonal inversions of atmospheric CO<sub>2</sub> data, *J Geophys Res-Atmos*, 107, Artn 4385, 10.1029/2001jd000857, 2002.
- 585 Rödenbeck, C., Houweling, S., Gloor, M., and Heimann, M.: CO<sub>2</sub> flux history 1982–2001 inferred from atmospheric data using a global inversion of atmospheric transport, *Atmos. Chem. Phys.*, 3, 1919-1964, 10.5194/acp-3-1919-2003, 2003.



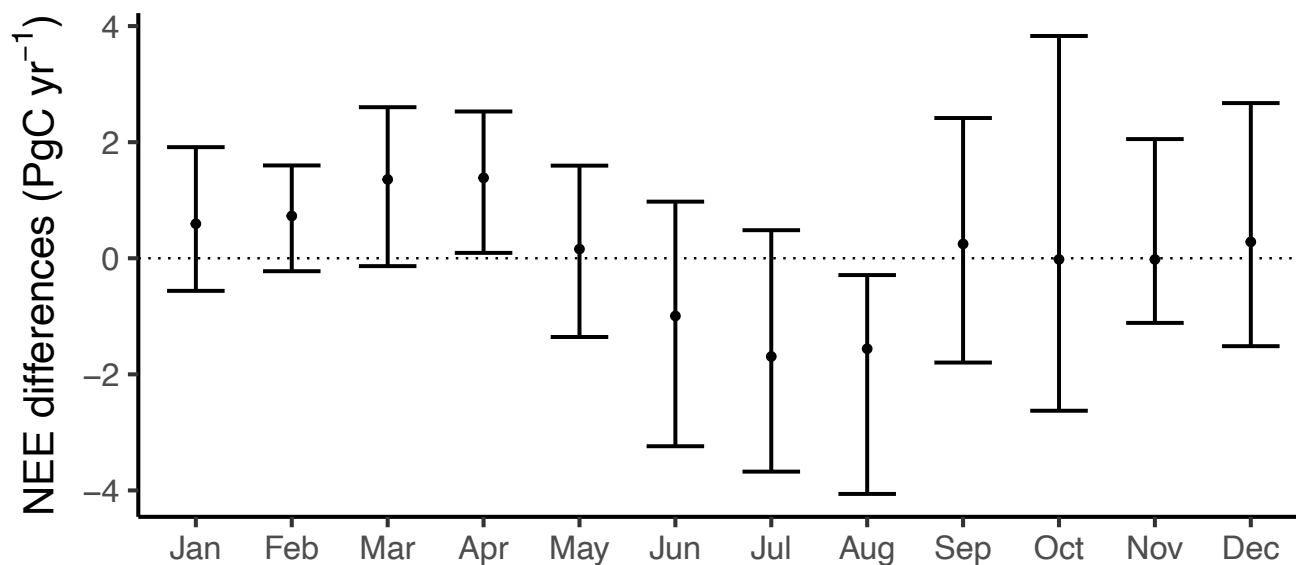
- Rödenbeck, C., Gerbig, C., Trusilova, K., and Heimann, M.: A two-step scheme for high-resolution regional atmospheric trace gas inversions based on independent models, *Atmos. Chem. Phys.*, 9, 5331-5342, 10.5194/acp-9-5331-2009, 2009.
- 590 Russell, G. L., and Lerner, J. A.: A new finite-differencing scheme for the tracer transport equation, *Journal of Applied Meteorology* (1962-1982), 1483-1498, 1981.
- Sarmiento, J. L., Gloor, M., Gruber, N., Beaulieu, C., Jacobson, A. R., Mikaloff Fletcher, S. E., Pacala, S., and Rodgers, K.: Trends and regional distributions of land and ocean carbon sinks, *Biogeosciences*, 7, 2351-2367, 10.5194/bg-7-2351-2010, 2010.
- 595 Stephens, B. B., Gurney, K. R., Tans, P. P., Sweeney, C., Peters, W., Bruhwiler, L., Ciais, P., Ramonet, M., Bousquet, P., Nakazawa, T., Aoki, S., Machida, T., Inoue, G., Vinnichenko, N., Lloyd, J., Jordan, A., Heimann, M., Shibistova, O., Langenfelds, R. L., Steele, L. P., Francey, R. J., and Denning, A. S.: Weak Northern and Strong Tropical Land Carbon Uptake from Vertical Profiles of Atmospheric CO<sub>2</sub>, *Science*, 316, 1732-1735, doi:10.1126/science.1137004, 2007.
- Tans, P. P., Fung, I. Y., and Takahashi, T.: Observational Constrains on the Global Atmospheric Co<sub>2</sub> Budget, *Science*, 247, 1431-1438, doi:10.1126/science.247.4949.1431, 1990.
- 600 Yi, C., Davis, K. J., Bakwin, P. S., Berger, B. W., and Marr, L. C.: Influence of advection on measurements of the net ecosystem-atmosphere exchange of CO<sub>2</sub> from a very tall tower, *Journal of Geophysical Research*, 105, 9991-9999, 2000.



610 **Figure 1:** CO<sub>2</sub> mole fraction differences between daily and hourly NEE-based simulations averaged for 2010-2020. Note, the difference at the site with a black circle is 6.97 ppm, excluded on the legend range for the visibility of other sites with smaller values.

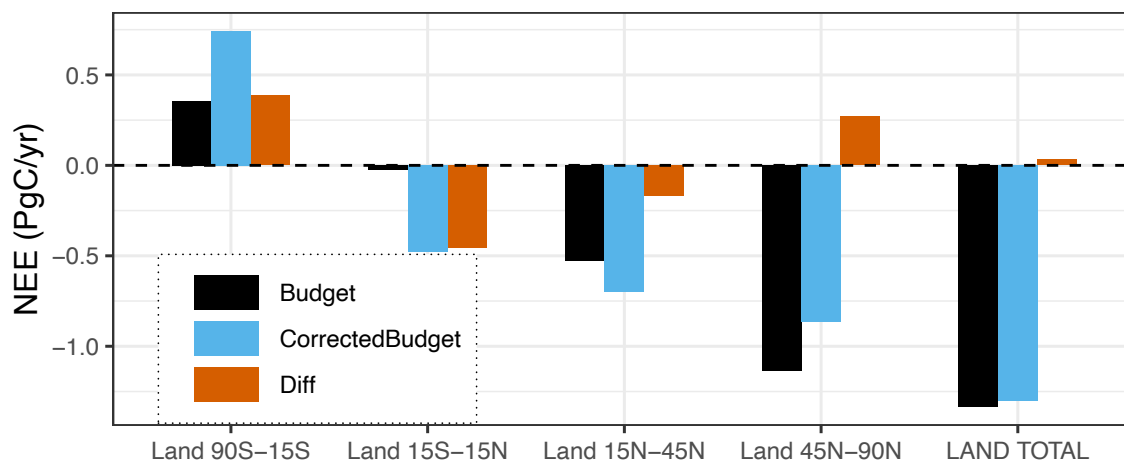


615 **Figure 2:** Differences of CO<sub>2</sub> dry mole fractions between simulations calculated with daily- and hourly-based NEE over specific site classifications and over months. Left panel shows the mean differences averaged over site-specific classifications (on x-axis) for the analysed years (2010-2020), and the numbers mentioned in bars are the number of sites per each classification; right panel denotes monthly differences computed for the northern Hemisphere and averaged over 88 sites representing towers, surface, and continental stations that dominate the impact over northern hemispheric lands (note: error bars refer to the range of differences over the target years (2010-2020)).



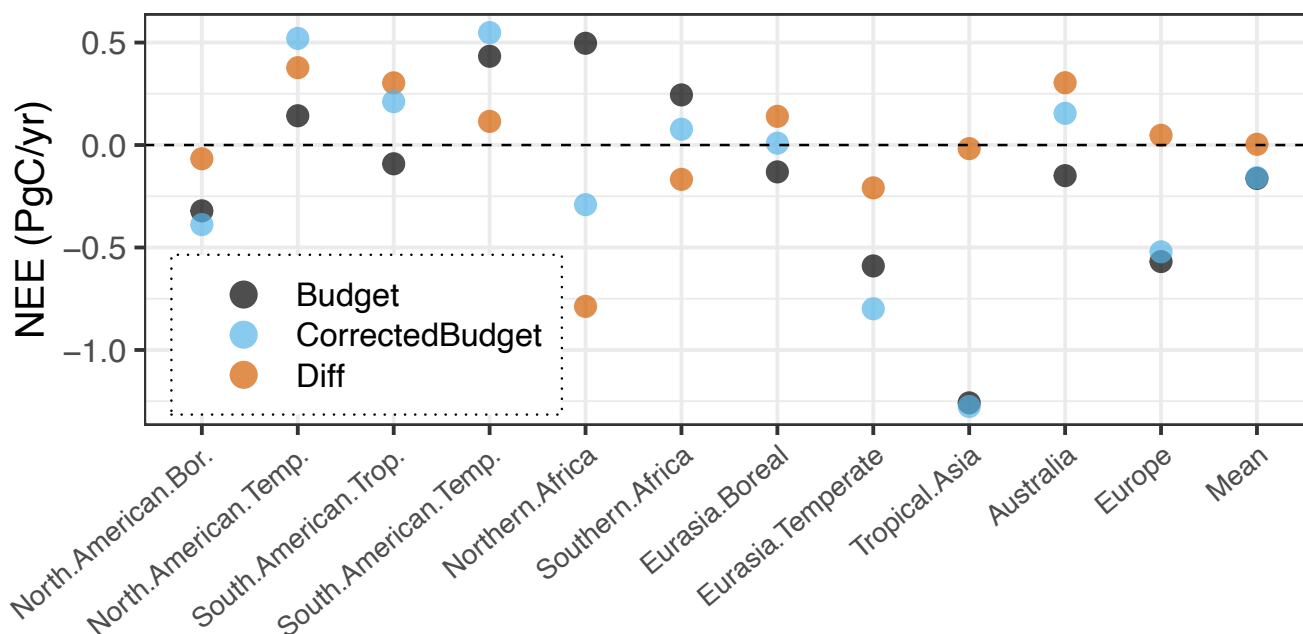
620

Figure 3: Monthly mean differences in global NEE estimates resulting from CO<sub>2</sub> diurnal cycle, averaged over 2010-2020. Error bars refer to min and max differences among all the analysed years.

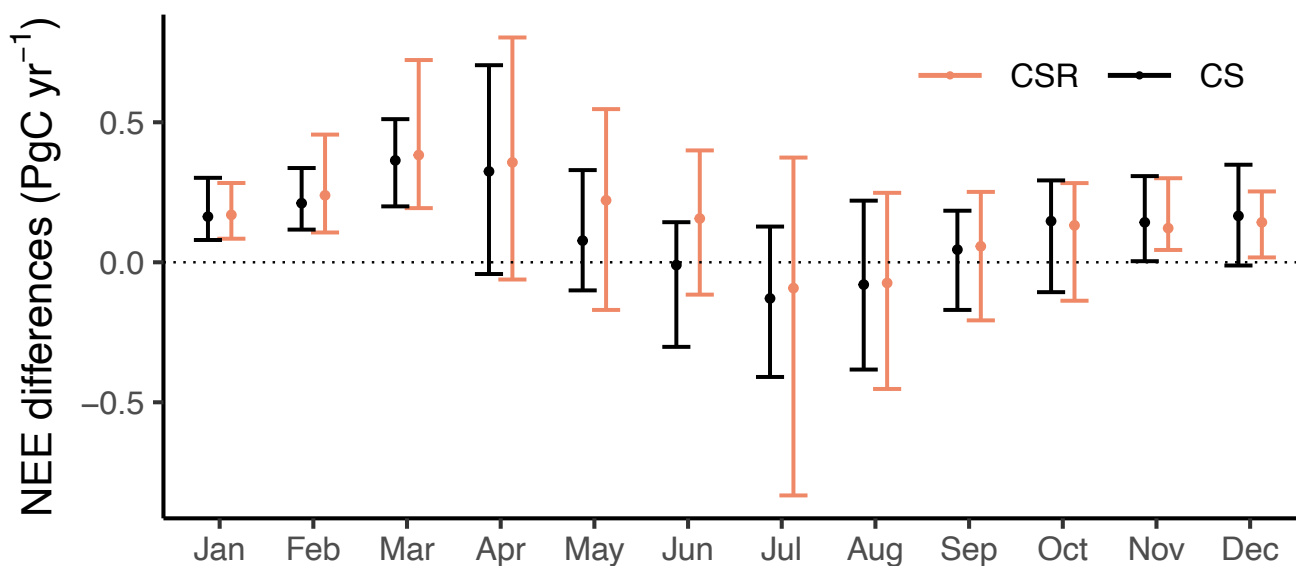


625

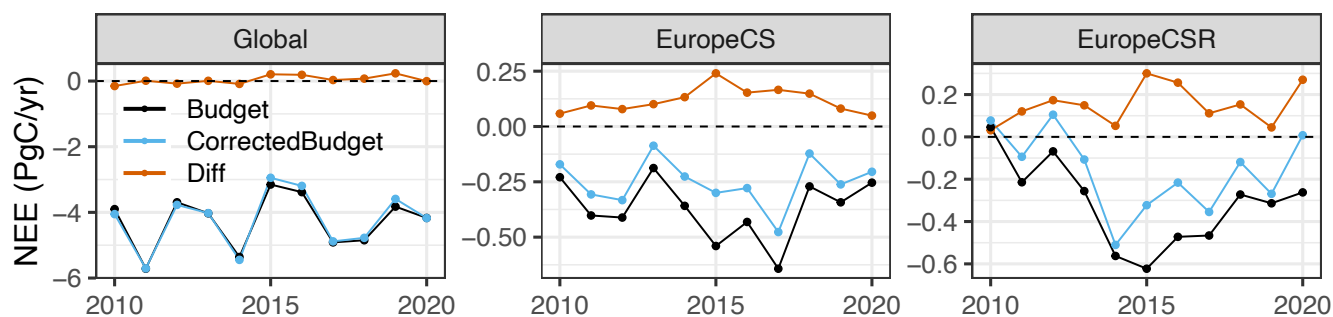
Figure 4: Integrated annual differences of NEE along latitude bands; NEE estimates calculated with CS are also shown before and after the corrections due to the diurnal cycle.



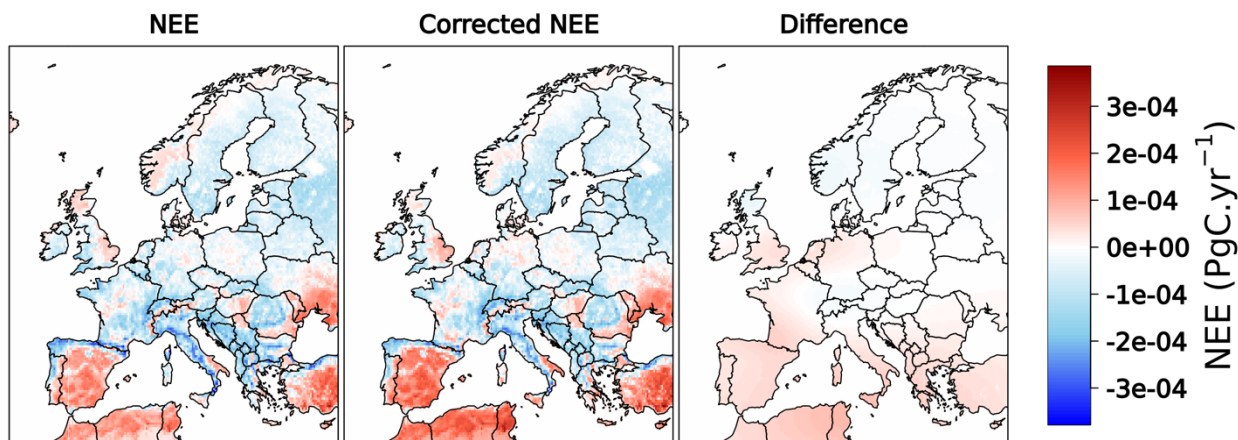
630 **Figure 5: Annual NEE estimates and their respective corrected estimates based on differences due to diurnal cycle effect integrated over TransCom regions, averaged over the time period 2010-2020.**



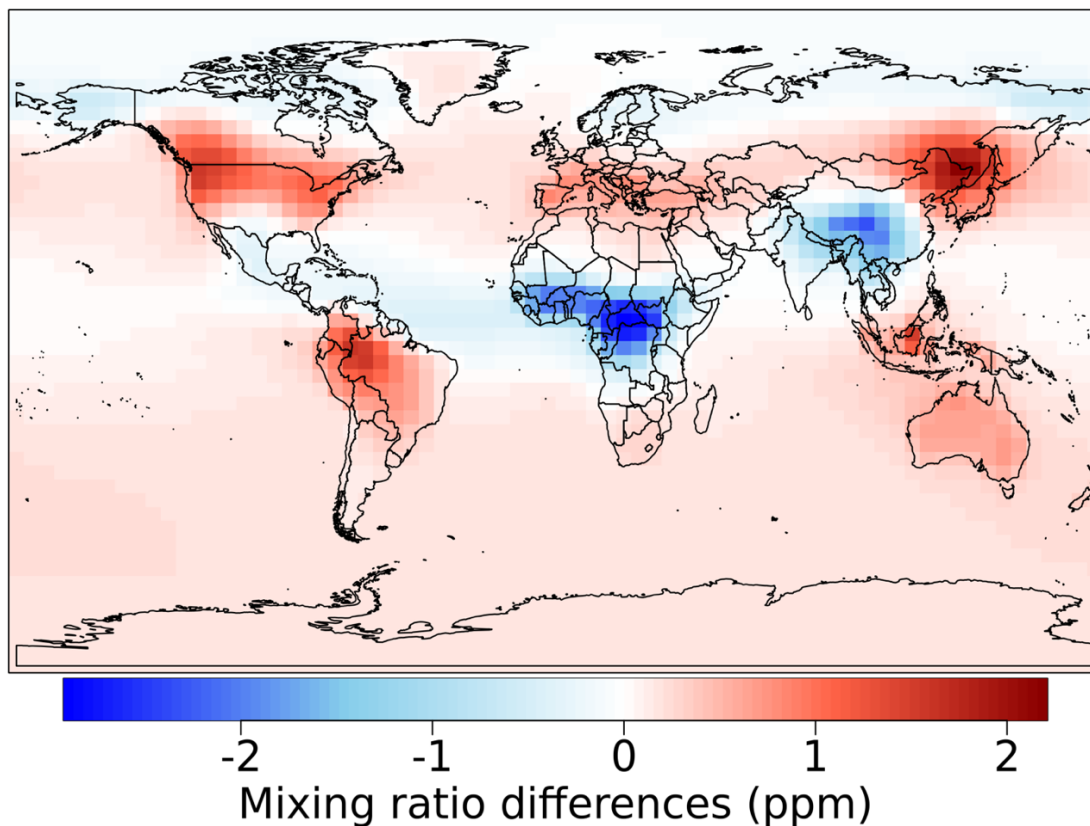
635 **Figure 6: Monthly mean NEE differences resulting from CO<sub>2</sub> diurnal cycle with CSR (red) and CS (black) estimated over Europe using the differences in mixing ratios for the period of time 2010-2020. Error bars mark the range of monthly differences over the analysed years.**



640 **Figure 7: Annual flux budgets (before and after corrections due to CO<sub>2</sub> diurnal cycle) estimated using CS over the globe and Europe using CS and over Europe using CSR for 2010-2020.**



645 **Figure 8: Spatial distributions of NEE, corrected NEE, and differences (from left to right, respectively) calculated as the mean of 2010-2020 over Europe**



650 **Figure 9:** 2-D fields of CO<sub>2</sub> mole fractions simulated using the inverted response of the diurnal cycle (i.e., inverted differences of mole fractions calculated with daily- and hourly- based NEE) for local daytime at the model surface level for the period 2010-2020 over the globe with TM3

655 **Table 1:** CS and CSR inversion setups

Inv.	Domain	Transport model	Diurnal CO <sub>2</sub> flux	Unc. shape	Unc. structure	Spatial resolution of state space
CS	global	TM3 (5°x4°)	no	Flat	exponential	2.5°x2°
CSR	Europe	STILT (0.25° x 0.25°) *	yes	Flat	hyperbolic	0.5°x0.5°

\* - resolution of the driving meteorological fields; STILT is a lagrangian particle model simulating subgrid scale vertical mixing at effectively higher spatial scales.



660 **Table 2: Sensitivity of IAV to the impact of CO<sub>2</sub> diurnal cycle. “Diff. IAV” corresponds to the IAV of the impact of diurnal cycle on retrieved fluxes, “Flux IAV” corresponds to the IAV of the estimated fluxes themselves, and “Flux IAV corr.” corresponds to IAV of estimated fluxes after corrections.**

Land region (TransCom)	Diff. IAV (Pg C yr <sup>-1</sup> )	Flux IAV (Pg C yr <sup>-1</sup> )	Flux IAV corr. (Pg C yr <sup>-1</sup> )
North.American.Bor.	0.04	0.12	0.14
North.American.Temp.	0.13	0.10	0.18
South.American.Trop.	0.29	0.20	0.39
South.American.Temp.	0.18	0.25	0.35
Northern.Africa	0.59	0.23	0.73
Southern.Africa	0.17	0.17	0.26
Eurasia.Boreal	0.07	0.32	0.35
Eurasia.Temperate	0.23	0.23	0.28
Tropical.Asia	0.21	0.18	0.21
Australia	0.12	0.11	0.19
Europe	0.08	0.17	0.24

665