



Advances in Surface Water and Ocean Topography for Fine-Scale Eddy Identification from Altimeter Sea Surface Height Merging Maps

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Abstract. The recently launched Surface Water and Ocean Topography (SWOT) satellite mission has reduced the noise
20 levels and increased resolution, thereby improving the ability to detect previously unobserved fine-scale signals. We employed a method to utilize the unique and advanced capabilities of SWOT to validate the accuracy of identified eddies in merged maps of a widely used Archiving, Validation, and Interpretation of Satellite Oceanographic (AVISO) data product and a newly implemented two-dimensional variational method (2DVAR), which uses a $1/12^\circ$ grid and reduces decorrelation of spatial length scales. The findings indicate that SWOT provides an enhanced capability in resolving fine-scale and
25 mesoscale eddies in the South China Sea compared with conventional in-situ data, such as drifting buoys. The validation results demonstrated that compared with AVISO, the 2DVAR method exhibited greater consistency with the SWOT observations, especially at small scales, confirming the accuracy and capability of the 2DVAR method in the reconstruction and resolution of fine-scale oceanic dynamical structures.



30 **1 Introduction**

The ocean has diverse spatial length scales of dynamical processes, from mesoscale signals at approximately 100–1000 km to sub-mesoscale processes below 100 km. These processes are primarily revealed through the absolute dynamic topography (ADT), which is a kind of sea surface height (SSH) above the geoid. ADT also plays a substantial role in the thermohaline circulation, atmosphere–ocean interactions, physical–biological–biochemical interactions, and the numerical modeling of coupled atmospheric-oceanic systems (Chelton et al., 2007; Ma et al., 2016; Mahadevan, 2016; Wunsch and Heimbach, 2013).

Global satellite altimeters offer systematic ADT measurements and high-resolution mapping of ocean topography, currently providing the most effective data for detecting and tracking oceanic dynamic signals (Chelton et al., 2007; Mason et al., 2014; Zhang et al., 2023). Due to differences in orbit cycles and swaths from different satellites, the observing data exhibit misalignment in both space and time. Consequently, ensemble Kalman filtering or data assimilation techniques based on optimal estimation methods are employed to merge data from different satellites, yielding a spatiotemporally continuous ADT map (Cohn, 1997; Le Traon et al., 1998; Taburet et al., 2019). Diverse merging methods result in disparate capacities for capturing oceanic dynamic signals which can be assessed by the metrics such as effective resolution and eddy kinetic energy (Ballarotta et al., 2020; Pascual et al., 2007; Taburet et al., 2019; Wang et al., 2021). Those assessment methods that rely on conventional measurement data are inherently limited by linear and long temporal sampling, low resolution, and other observational uncertainties, making them unsuitable for assessing merged maps in regions characterized by intricate multiscale oceanic dynamic signals.

The Surface Water and Ocean Topography (SWOT) satellite, launched in December 2022, comprises a new generation of Ka-band radar interferometers (KaRIn), which reduces instrument noise by two orders of magnitude compared to that of the conventional satellites (Abdalla et al., 2021; Fu et al., 2024). The KaRIn technique allows the mapping of two-dimensional ADT with a 120-km wide swath, which is over five times the width of a conventional nadir, and offers an unprecedented 15-km spatial resolution for an altimeter satellite (Dufau et al., 2016; Morrow et al., 2019; Wang and Fu, 2019). Globally, SWOT data has undergone in-situ observational calibration and validation and data assimilation application studies before its formal use for global mapping, confirming the capability of detecting previously unobserved fine-scale signals, reinforcing the capabilities of ocean monitoring, signifying a pivotal advancement in enhancing spatial resolution (Martin et al., 2024; Ubelmann et al., 2024; Verger-Miralles et al., 2024; Zhang et al., 2024). However, the intrinsic challenge posed by the discrepancy between low temporal and high spatial resolution requires further interpretation before direct utilization as inputs for ADT merged maps in future research endeavours.

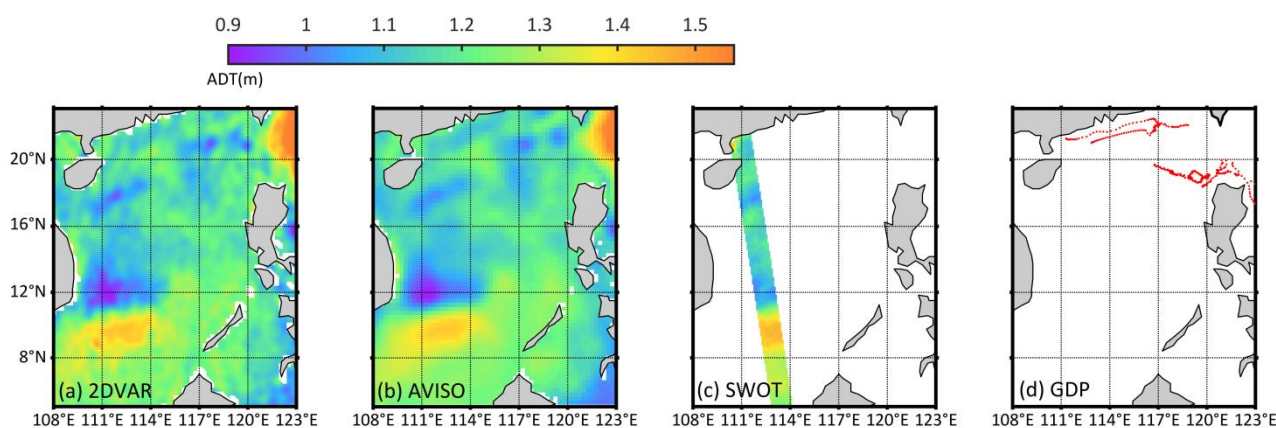
This study aimed to authenticate the accuracy and reliability of diverse merging methods in reconstructing oceanic dynamic signals, with particular emphasis on fine-scale eddies. This study provides a new application scenario and method for international state-of-the-art sea surface observation data. Simultaneously, it provides a new assessment for the information quality of merged maps which can provide further guidance for subsequent merging methods.



2 Materials and Methods

2.1 ADT Merging Maps

65 We employed two types of ADT merged data to generate corresponding eddy identification ensembles (Figs. 1a, b). The first
 ADT merged map was a product released by AVISO, which uses the optimal interpolation method (Pujol et al., 2016) with a
 global $1/4^\circ$ grid resolution. Since the reprocessed products are currently unable to cover the science phase of SWOT satellite
 mission, a near-real-time product is used to study the science phase of SWOT data, while the reprocessed product is used for
 the calibration and validation (CALVAL) phase of SWOT data. The second ADT product was produced using a 2DVAR
 70 method with a $1/12^\circ$ grid resolution, and this method employs optimized background and observation errors to decorrelate
 the length scales in the merging process, with an improved method for calculating the background error covariance matrix
 (Liu et al., 2020). Both AVISO and 2DVAR methods were based on the principle of optimal estimation and were calculated
 using all available on-orbit altimeter mission data, including Jason-3, Sentinel-3A, HY-2B, Saral/AltiKa, Cryosat-2,
 Sentinel-3B, and Sentinel-6A. Notably, the 2DVAR method successfully reduced the effective resolution to approximately
 75 half that of AVISO (approximately 80 km), enhancing the resolution of signals from fine-scale to mesoscale eddies,
 particularly in areas with rich eddy kinetic energy, such as the SCS and the Northwest Pacific Ocean (Jiang et al., 2022; Liu
 et al., 2023).



80 **Figure 1. Four datasets of absolute dynamic topography (ADT) in the South China Sea. (a) 2DVAR, (b) AVISO, (c) SWOT, and (d) GDP. The ADT data in (a), (b), and (c) were obtained on September 12, 2023, and (d) covers the entire period of the Science phase.**

2.2 Eddy Identification

The study area SCS is a significant dynamical marginal sea in the northwest Pacific. In the SCS, the first obliquely pressured Rossby deformation radius was less than 20 km in winter (Cai et al., 2008), suggesting a rich environment for fine-scale oceanic dynamical processes. Additionally, the SCS receives energy transport from the sub-mesoscale energy reservoir of



85 the Kuroshio Current via the western boundary currents, resulting in a dense concentration of mesoscale and fine-scale processes on the 10-km scale (Ni et al., 2021; Zu et al., 2019).

Currently, the main methods for eddy identification based on satellite altimeters include the Okubo-Weiss (OW) parameter method, the sea surface topography method, and the Lagrangian coherent structure (LCS) method. Among these, the sea surface topography method provides the clearest and most cohesive identification of eddies, regardless of their size or
90 boundary (Chen et al., 2021). Therefore, this research employed a sea surface topography method based on contour analysis for eddy identification in 2DVAR and AVISO ADT merged maps, as well as in SWOT maps (Ni, 2014). To avoid the influence of grid resolution, different merged maps were interpolated to a high-resolution grid with the same accuracy. The outermost circle of the closed contours containing the unique centre was recognized as the ‘quasi-eddy edge’, and only a minimum of three points were retained. Each quasi-eddy edge was then contracted inward until it corresponded to a single
95 centre. Lastly, the geometric centre of the innermost circle of the closed 1-mm step contours was identified as the eddy centre. This process allowed the determination of the eddy boundary, type, radius, and amplitude. All eddies with an amplitude of less than 2 cm were excluded from further analysis.

2.3 Eddy Validation

The accuracy and reliability of the identified eddies were validated and assessed using two observational ADT datasets as
100 true values. First, the Level-3 LR ADT v0.3 datasets from the SWOT product were used for eddy validation, and a visualization method was employed to examine the clarity and intuitiveness of the eddy boundaries. The Level-3 data are more suitable for capturing fine-scale to mesoscale structures compared to the Level-4 products, which rely on merging methods and data from other satellites (Ballarotta et al., 2024). The 2-km sampling interval allowed the SWOT data to capture finer-scale signals that are not the primary focus of the current research. Therefore, spatial average filtering with a
105 $1/12^\circ$ grid was conducted to filter out those finer-scale signals (Fig. 1c), highlighting the fine-scale to mesoscale eddies in this study. The SWOT mission has two phases: the CALVAL phase, which involved 1-day rapid sampling from April to July 2023, and the science phase, which included 21-day repeat sampling between September and November 2023. This study leveraged the unique characteristics of these two phases to conduct a comprehensive assessment of the spatial and temporal dynamical structures. In both phases, the nadir data of SWOT were excluded due to unstable errors and a lack of interest in
110 traditional technology. The CALVAL phase sampled a limited area of the sea surface due to the fixed 1-day rapid-sampling orbit cycle. Fortunately, the rapid-sampling orbit coverage included the SCS, repeatedly mapping the same location, which ensured the smooth capture of time-evolving fine-scale eddy structures in the SWOT data.

Before the validation process, all identified eddies were preliminarily evaluated to ensure they could be matched with a specific SWOT eddy. Once a successful match is established, the eddy reconstruction of the ADT map will be considered
115 correct and will be retained along with its corresponding eddy captured from the SWOT map. Only eddies that met the following three criteria were considered to match the SWOT eddy, which was assumed to be actual:

- 1) The rotation direction or type of the merged-map eddy and the SWOT eddy are the same



- 2) The distance between the centre of the merged-map eddy and the SWOT eddy is less than 50 km
- 3) The difference in radius between the merged-map eddy and the SWOT eddy is less than 120 km

120 The criteria were set according to the KaRIn swath, which is approximately 120 km for the full swath and approximately 50 km for the half swath. After filtering out eddies that cannot be matched with SWOT, a systematic standardization process was adopted to make merged-map eddies comparable with the SWOT eddies in terms of spatial scales and relative location (Chen and Yu, 2024). Firstly, the scale normalization factor α was calculated for each SWOT eddy to adjust it to a fixed size based on the eddy radius:

$$125 \quad \alpha_i = \frac{\frac{1}{N} \sum_{i=1}^n r_i}{r_i} \quad (1)$$

where i is the index of the i th eddy in the SWOT ensemble, N denotes the total number of the eddies, and r represents the radius of the eddy. To eliminate the absolute positional differences, we established a local coordinate system with the centre of normalized SWOT eddy as the origin. The geographic coordinates of the i -th SWOT eddy centre ($X_{i,S}$, $Y_{i,S}$) were subtracted from those of the corresponding merged-map eddy centres ($X_{i,c}$, $Y_{i,c}$) and boundary points ($X_{i,bm}$, $Y_{i,bm}$):

$$130 \quad \begin{cases} (X'_{i,c}, Y'_{i,c}) = (X_{i,c} - X_{i,S}, Y_{i,c} - Y_{i,S}) \\ (X'_{i,bm}, Y'_{i,bm}) = (X_{i,bm} - X_{i,S}, Y_{i,bm} - Y_{i,S}) \end{cases} \quad (2)$$

the new centre and boundary points of the i th merged-map eddy in the local coordinate system are ($X'_{i,c}$, $Y'_{i,c}$) and ($X'_{i,bm}$, $Y'_{i,bm}$), where bm denotes the index of the boundary point.

Based on the coordinate system transformation, the position information of the merged-map eddies under the new coordinate system was scaled using the SWOT eddy normalization factor α . Considering that eddy scaling is related to the radial distance, this step applied a polar coordinate transformation to extract the radial distances $r_{i,c}$, $r_{i,bm}$ and angles $\theta_{i,c}$, $\theta_{i,bm}$ of the points:

$$\begin{cases} r_{i,c} = \sqrt{(X'_{i,c})^2 + (Y'_{i,c})^2} \\ \theta_{i,c} = \arctan\left(\frac{Y'_{i,c}}{X'_{i,c}}\right) \\ r_{i,bm} = \sqrt{(X'_{i,bm})^2 + (Y'_{i,bm})^2} \\ \theta_{i,bm} = \arctan\left(\frac{Y'_{i,bm}}{X'_{i,bm}}\right) \end{cases} \quad (3)$$

By multiplying the coordinates with the normalization factor α , we implemented the scaling. The scaled coordinates were then transformed back to obtain geometrically similar coordinates ($X''_{i,c}$, $Y''_{i,c}$) and ($X''_{i,bm}$, $Y''_{i,bm}$).



$$140 \quad \begin{cases} X''_{i,c} = r_{i,c} \cdot \alpha_i \cdot \cos(\theta_{i,c}) \\ Y''_{i,c} = r_{i,c} \cdot \alpha_i \cdot \sin(\theta_{i,c}) \\ X''_{i,bm} = r_{i,bm} \cdot \alpha_i \cdot \cos(\theta_{i,c}) \\ Y''_{i,bm} = r_{i,bm} \cdot \alpha_i \cdot \sin(\theta_{i,bm}) \end{cases} \quad (4)$$

To compare with SWOT, this section also describes how the validation of eddies using traditional in-situ drifter observations. The Global Drifter Program (GDP) data provide the positions of a 15-m depth drogue drifter at a 1-hour frequency and have been frequently employed in the validation and assessment of surface dynamic signals (Zhang and Qiu, 2018). These data enable studies of fine-scale to mesoscale dynamical structures, comparative evaluation of global ocean numerical models, and provide input data for forecasting (Lumpkin and Elipot, 2010; Yu et al., 2019). Due to its Lagrangian nature, the drifter is more likely to respond to low pressure and high velocity in the central region of the eddy, and then become entrained within the eddy as it rotates toward the centre (Ohlmann et al., 2017). Thus, the trajectory of the drifter allows for the observation and capture of fine-scale and mesoscale eddies in this research. The region of interest in this study is situated within the convergence zone of the subtropical circulation, it contains several drifter sampling areas and involves a long drift time. However, the GDP datasets are only available during the scientific phase of the SWOT mission (Fig. 1d).

3 Results

3.1 Accuracy and Reliability of Identified Eddies

In this section, composite maps of normalized eddy ensembles for 2DVAR and AVISO ADT merged maps will be presented first, followed by a summary of the errors and characteristics of the identified eddies.

The coloured areas in Fig. 2 represent the distributions of the normalized radii of eddies identified by 2DVAR and AVISO, which were successfully matched with SWOT eddies. All identified eddies were categorized into three groups based on the radii of SWOT eddies: those with radii below 10 km, between 10 km and 20 km, and exceeding 20 km were classified as fine-scale (Fig. 2a), intermediate-scale (Fig. 2b), and mesoscale (Fig. 2c) eddies, respectively. The dashed circle lines in each component represent the normalized SWOT eddies, and the size of the coloured area outside these dashed circles illustrates the discrepancy between the merged-map eddies and SWOT eddies. A grid space extent equal to twice the normalized SWOT eddy radius was chosen.

Despite geographical and radius distribution discrepancies, the merged map shows a certain degree of accuracy and similarity with SWOT in Fig. 2. As the eddy scale increases from Figs. 2a to 2c, the maxima on the eddy composite maps are situated closer to the origin, and the error proportions beyond the dashed circles decrease. This suggests that the merged map is more accurate at reconstructing mesoscale eddies compared to fine-scale eddies.

For reconstructing the same SWOT eddy categories, the two merged maps exhibit different performance. In Fig. 2(b1), the 2DVAR merged-map eddy boundaries show the highest consistency with the normalized SWOT eddy, without significant



outward protrusion or noticeable inward indentation. In contrast, AVISO only shows consistency at larger scales (Fig. 2(c2)) with the normalized SWOT eddy boundaries, without the wide purple band shown in Fig. 2(b2) outside the dashed circle line. Additionally, 2DVAR results in more matches with SWOT across all categories, particularly for SWOT eddies with scales less than 10 km (Fig. 2a), where the number of matches is three times greater than those achieved by AVISO. For all matched eddies, the average radius of the matched SWOT, 2DVAR, and AVISO eddies is approximately 20 km, 40 km, and 65 km, respectively, indicating a significant difference between the merged maps. The size range for all matched 2DVAR eddies, from 15 to 117 km, is closer to that of SWOT (ranging roughly from 7 to 54 km) than the broader span of 15 to 134 km for AVISO. Compared to the normalized eddies from AVISO, that of 2DVAR are more concentrated, and their boundaries are more precise relative to the dashed circle representing the actual SWOT eddies. This indicates that 2DVAR performs better than AVISO in reconstructing smaller eddies.

Table 1. Root mean square error (RMSE) and Extremes: Eddy Radius, Amplitude, and Centre Location (2DVAR, AVISO vs. SWOT).

	SWOT Categories	2DVAR	AVISO
	RMSE of Radius [km]	27.44	49.72
	RMSE of Amplitude [cm]	3.16	3.20
	RMSE of Centre Location [km]	26.41	27.08
Max./Min. radius [km]	SWOT radius \leq 10	67.33/15.13	66.91/15.16
	10 < SWOT radius < 20	98.28/15.63	128.57/15.74
	SWOT radius \geq 20	116.79/18.37	134.52/23.70
	Max./Min. radius of SWOT eddy [km]	54.92/6.29	53.56/7.71

Note: In row four, the "Max./Min. radius" specifies the range of merged-map eddy radii for each SWOT category corresponding to Figure 2, with the leading number being the maximum and the trailing number being the minimum radius.

The discrepancies in eddy radius between the merged maps and SWOT maps should not be ignored. To provide a more detailed assessment, the root mean square error (RMSE) for the eddy radius, amplitude, and centre location was also summarized in Tab. 1. Among these statistics, the RMSE in eddy radius, especially for AVISO, is comparable to the SWOT radius itself, illustrating that the spatial scale is a significant issue in the ADT merged map. The 2DVAR merging method has reduced the radius error by approximately 20 km compared to AVISO, mostly attributed to its accurate capturing of mesoscale eddies. The amplitude error is about 3 cm for both merged maps, which is half the maximum amplitude of the SWOT eddies (as shown in Section 3.2). The center location error was calculated using the physical location, which is caused by the positional deviation of local maxima or minima in ADT signals. However, the errors in amplitude and centre position do not show a notable improvement in 2DVAR compared to AVISO.

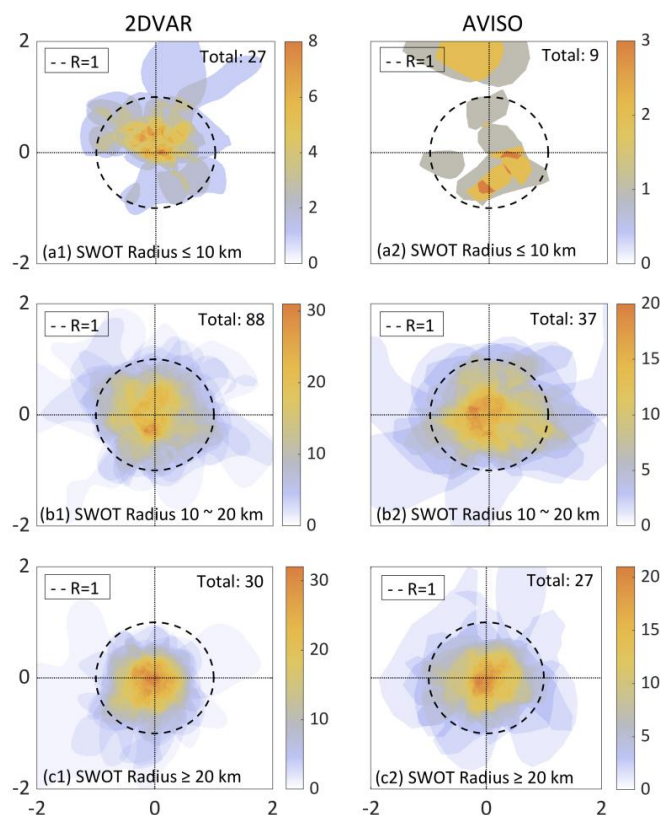


Figure 2. Composite maps of normalized eddy identified from 2DVAR (left column) and AVISO (right column) merged maps. The circle dashed lines mark the normalized SWOT eddies with a radius of less than 10 km (a), 10 to 20 km (b), and more than 20 km (c).

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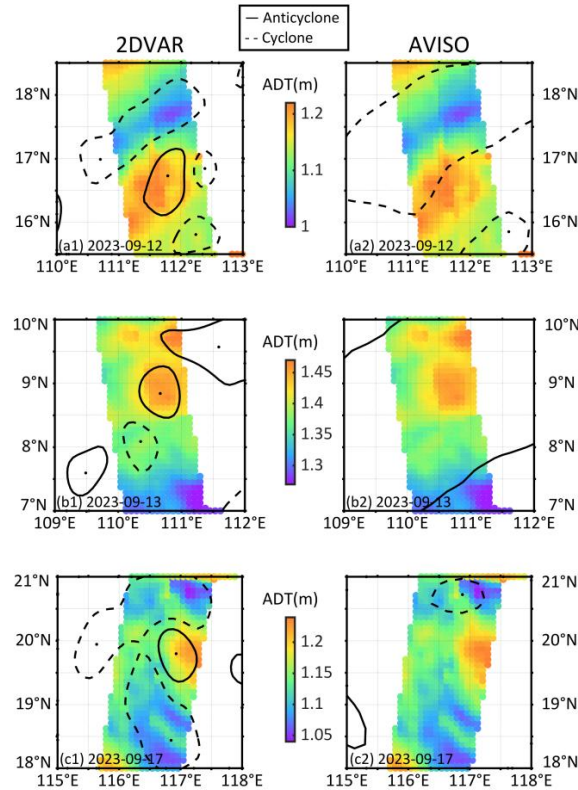
3.2 Eddy Boundaries Verification in Space and Time

This section presents a detailed visual display of merged-map eddies compared with SWOT eddies and the eddy boundaries with drifter trajectories to further validate the reliability and accuracy of the identified eddies.

Figure 3 provides a detailed comparison of eddies from two merged maps using science-phase SWOT mission data in the central area of the SCS. The coloured slices is Level-3 observations directly from the KaRIn measurement. A high degree of agreement was found between the eddies identified using 2DVAR and SWOT at scales ranging from 50 to 200 km. Specifically, the anticyclones at 111.5°E, 16.7°N in Fig. 3(a1), 110.7°E, 8.8°N in Fig. 3(b1), and 117°E, 19.8°N in Fig. 3(c1), as well as the cyclones at 110.5°E, 17°N in Fig. 3(a1), and 117°E, 18.5°N in Fig. 3(c1) all show better consistency in shape with SWOT map. Although the 2DVAR maps exhibit better consistency at small scales, AVISO maps still perform well at large scales, ensuring the basic identification of eddies. Despite the substantial improvement of 2DVAR over AVISO in terms of spatial scale, there are still instances where eddy identification is inaccurate, such as some noise eddies at 112.5°E, 16.9°N in Fig. 3(a1). This is particularly true at low latitudes, where ADT merged maps typically exhibit larger errors due to complex oceanic dynamical structures, tropical orbit space, and atmospheric effects.

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210 **Figure 3.** SWOT data with the two-dimensional variational method (2DVAR) (left column) and AVISO (right column) eddies. The black solid (dashed) line represents the anticyclonic (cyclonic) eddy.

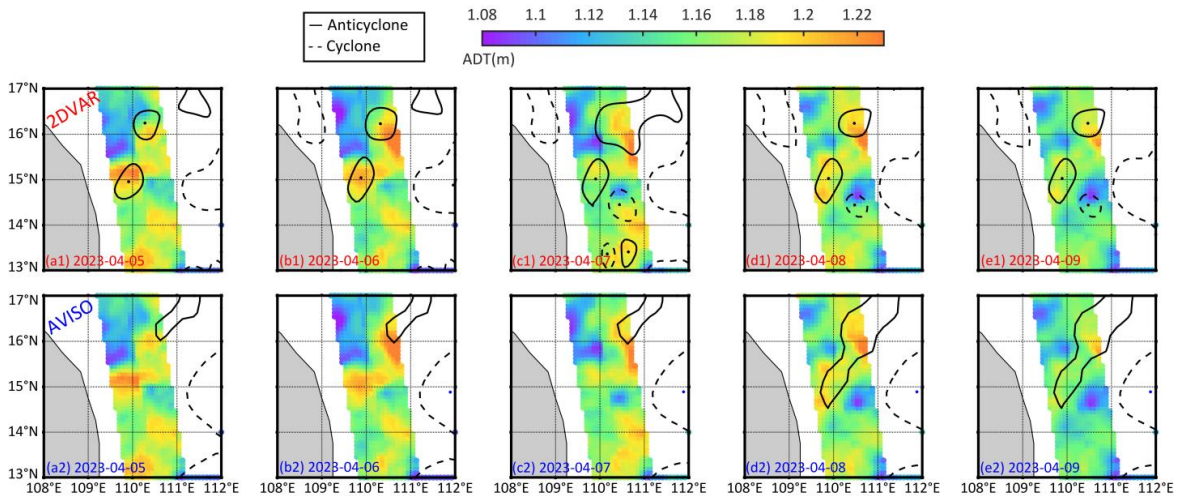
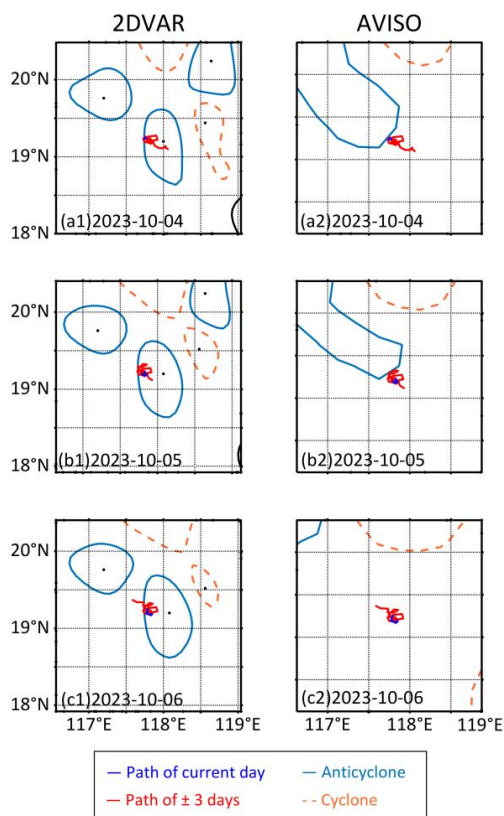


Figure 4. Observation data of SWOT with the 2DVAR (top) and AVISO (bottom) merged maps. The solid black line (dashed) represents the anticyclonic (cyclonic) eddy, and the colour-filled plot contains the KaRIn and Nadir data from SWOT.



215 The CALVAL phase can be utilized to capture the evolution of small-scale structures over time, distinct from the science phase. A duration of five days was chosen for this section, which corresponds to the period of fine-scale structure evolution. In the 2DVAR maps, two anticyclones with a 50-km scale were identified at 110°E, 15°N, and 110.5°E, 16.2°N, as shown in Figs. 4(a1)–(d1) (April 5–8, 2023). These anticyclones were in high agreement with the colour boundaries in the bottom SWOT data. The two anticyclone eddies shown in the 2DVAR map were recognized as large mesoscale eddies by AVISO (Figs. 4(a2)–(e2)).

220 Additionally, a 50-km scale cyclone was identified by its low centre surface and circular shape at 110.5°E, 14.5°N in the SWOT map on April 5, 2023 (Fig. 4a). This cyclone was successfully captured by 2DVAR as it matured on April 7, 2023 (Fig. 4(c1)), despite a certain degree of relative positional deviation from the actual eddy. In contrast, AVISO identified this area as a non-eddy region (Fig. 4(c2)).



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Figure 5. Trajectories of drifting buoys with 2DVAR (left column) and AVISO (right column). The light blue solid (orange dashed) line, dark blue line segment, and red line segment represent the anticyclonic (cyclonic) eddies, the trajectory for the current day, and the trajectories for the three days before and after, respectively.

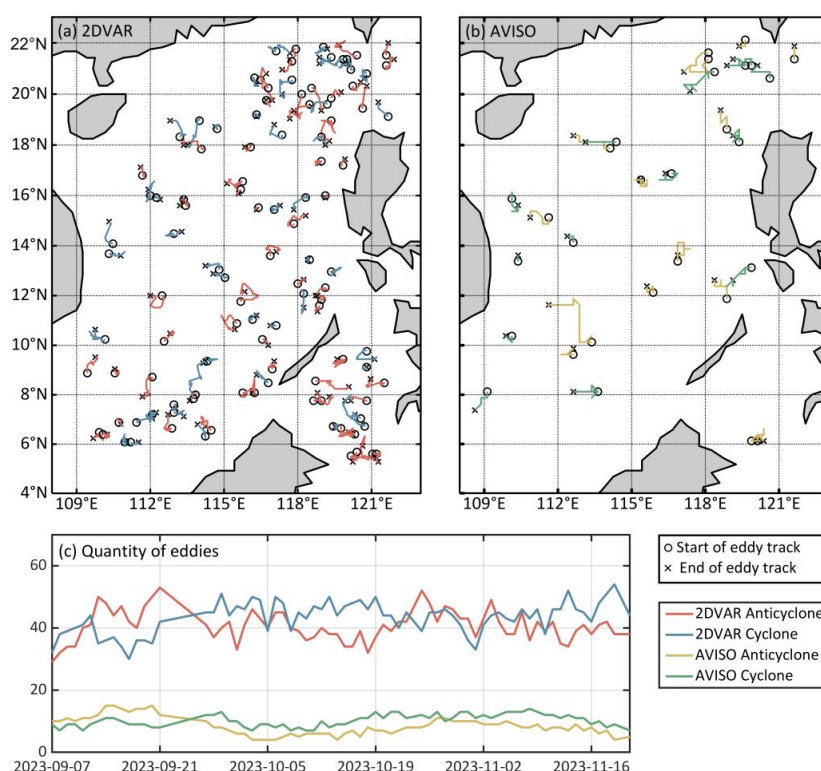
230 An example of the GDP drifter trajectories compared to the corresponding merged-map eddies is shown in Fig. 5. During October 4–6, 2023, an anticyclonic eddy was identified in 2DVAR at 118°E and 19°N, with a total of seven clustered drifter buoy trajectory segments within it. This illustrates that the buoy was continuously rotating at a relatively fixed position for



about seven days. In comparison, AVISO did not capture this anticyclonic eddy at the same position, but it tended to identify a larger-scale anticyclonic eddy near it. This suggests the accuracy and reliability of the smaller mesoscale eddy identified by 2DVAR, despite a slight positional deviation.

235 However, due to being constantly entrained by a single eddy and rotating within it, the number of eddies that can be detected by a drifter buoy is limited compared to the rapid mapping provided by SWOT.

3.2 Eddy Distribution and Characteristics

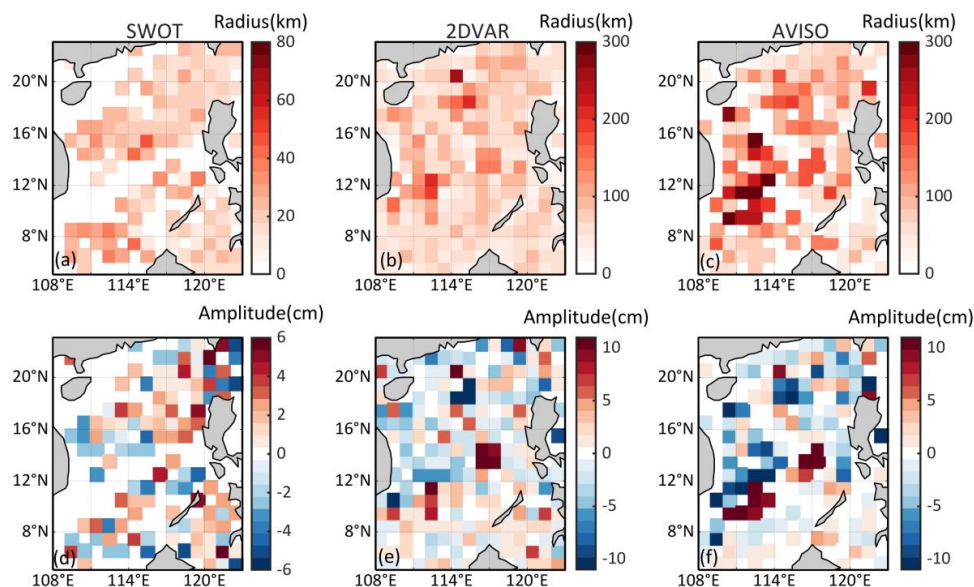


240 **Figure 6. Eddies and tracks identified during the SWOT science phase in (a) 2DVAR and (b) AVISO merged maps. The red (yellow) and blue (green) lines represent the anticyclone and cyclone tracks in the 2DVAR (AVISO) merged maps, respectively. The black circles and crosses indicate the start and end positions of the eddies, respectively. (c) The number of eddies over time. The red (yellow) and blue (green) lines represent the daily count of anticyclones and cyclones, respectively, as identified in the 2DVAR (AVISO) merged maps.**

The eddy distributions and their tracks were mapped in Fig. 6 to provide a clearer representation of the identified eddies. The total number of anticyclones identified in the ADT merged maps was higher than that of cyclones, and the eddy tracks exhibited a northeast-southwest propagation and distribution pattern (Figs. 6a–b). This quantitative relationship and distribution pattern are consistent between the two merged maps and are thought to be related to the path of eddies detached from the Kuroshio and intruding into the SCS via the Luzon Strait (approximately 121°E, 20°N) (Huang et al., 2017; Jia and Chassignet, 2011).



250 However, there was a significant discrepancy in the number of eddies identified by the two merged maps: 2DVAR identified approximately four times as many eddies as AVISO, both in terms of the total number of eddies from September to November and the daily number of eddies (Fig. 6c). Notably, in the western part of the Luzon Strait, around 119°E, 20°N, and below 12°N, 2DVAR identified a significantly greater number of eddies compared to AVISO.



255 **Figure 7. Distributions of radius (top) and amplitude (bottom) for SWOT (left column), 2DVAR (middle column), and AVISO (right column) are presented. The colour intensity is proportional to the radius, with darker colours indicating larger radii. Similarly, the colour intensity is proportional to the amplitude, with darker red (blue) indicating larger positive (negative) amplitudes.**

The distributions of radius and amplitude for the eddies from merged maps and SWOT maps are displayed in Fig. 7. The radii of the eddies identified in the 2DVAR and AVISO maps are concentrated in the range of 50–300 km (Figs. 7b–c), while the radii of the SWOT eddies are mostly under 50 km (Fig. 7a). This is partly due to the 120 km-wide observation swath of SWOT, which restricts the capture of eddies larger than 120 km.

Larger mesoscale eddies were captured in the southwestern part of the SCS in the merged maps (Figs. 7b–c), whereas no eddies were observed in the SWOT maps (Fig. 7a). This is because eddies in this region may only exist at scales larger than the SWOT observation swath. Both merged maps captured a considerable number of larger mesoscale eddies with radii exceeding 200 km, which were more uniformly distributed in the northern and southwestern parts of the SCS, attributed to the influence of topographic effects (Su et al., 2020).

265 However, the radii of 2DVAR eddies are approximately 50–100 km smaller than those of AVISO, and a greater number of fine-scale and mesoscale eddies with radii below 150 km were captured in the central and southern parts of the SCS. This is attributed to the smaller effective resolution of 2DVAR (Liu et al., 2020).

270 The amplitudes of 2DVAR and AVISO are within ± 10 cm, while the amplitudes of SWOT are within ± 6 cm, which is 4 cm smaller than those of the merged maps in both positive and negative directions.



4 Summary and discussion

275 This research leverages cutting-edge SWOT data to develop an advanced evaluation framework centred on eddy identification within merged maps, achieving superior validation capabilities. Initially, the identified eddies are meticulously normalized and compared with actual eddies. Subsequently, eddy boundary details of the identified eddies are visually compared with those of the merged maps. Finally, the method is validated through in-situ observations, ensuring robustness and reliability. This comprehensive approach provides a rigorous assessment of the authenticity and precision of the merged-map eddies, with a detailed analysis of the evaluation outcomes. The main outcomes were summarized as follows:

- 280
- The 2DVAR method captured a markedly higher quantity of fine-scale eddies and exhibited a 50% improvement in the RMSE of eddy radii compared to AVISO, when validated against SWOT.
 - Eddies identified in the 2DVAR demonstrated superior coherence and agreement with SWOT data, especially for fine-scale eddies, compared to AVISO.

The results show that 2DVAR identified a significantly greater number of accurate fine-scale and mesoscale eddies 285 compared to AVISO, which is consistent with earlier evaluations of 2DVAR in terms of error analysis, wave number energy spectrum, effective resolution, and OSSE (Observing System Simulation Experiment) (Archer et al., 2020; Jiang et al., 2022). The successful matches with SWOT eddies on scales less than 20 km further support the argument that fine-scale to mesoscale eddies may have been overlooked in the merged maps.

To be noticed, the results showed in this research should be interpreted as the best-case scenario because the eddy 290 identification used for the 2DVAR, AVISO and SWOT maps was identical, implying that the method is perfect. However, several deficiencies may cause errors, including inappropriate eddy determinations in daily maps without matching with track results. It is because that the eddies moves as tens of kilometers a day which is almost the same with the SWOT swath, resulting in short-trajectory eddies being incorrectly determined as actual eddies in SWOT or merged maps. Also, ignoration of non-closure of contour lines in SWOT maps might be a deficiency too. Most of the eddy scales in the SWOT maps do not 295 exceed 50 km, which limits their ability to fully represent mesoscales eddies, especially those larger than 50 km. Additionally, despite being accurate in terms of radius scale and boundary details, a significant discrepancy remains in terms of positional deviation, which may result in a false match between merged-map eddies with the actual eddies. To address method deficiencies, one possible avenue for improvement would be to use AI or machine learning algorithms for eddy identification and matching, along with auto tracking algorithms to select eddies that persist over time within a limited swath. 300 Compared to the GDP, the validation capability of SWOT is enhanced in both temporal and spatial aspects. This is attributed to the high cost and sparse distribution of drifter platform observations. In contrast, the CALVAL phase of SWOT provided a robust dataset for studying short scale dynamical structures over time. SWOT has now entered the official operational phase, which means it will no longer provide regionally repetitive data of one-day rapid sampling, and the data from the CALVAL phase have become particularly valuable.



305 The innovative approach presented in this research optimizes and broadens the applications for SWOT data, marking an advancement in the assessment of dynamic signals at the sea surface, particularly at fine-scale. Since the SWOT data have proven their ability to represent fine-scale eddies through in-situ calibration experiments (Zhang et al., 2024), they can be used as input information for the 2DVAR merging method in the future. With the release of the latest available data, our research will continue to leverage SWOT for enhancing merging methodologies and validating sea surface dynamical structures. The combination of SWOT and 2DVAR will theoretically help improve the effective resolution and accuracy of the merged maps, and this work can provide technical support for oceanographic understanding and prediction capabilities.

Code availability

The codes are available from Zenodo (<https://doi.org/10.5281/zenodo.13629576>).

Data availability

315 The 2DVAR data are available from Zenodo (<https://doi.org/10.5281/zenodo.11219285>). The 1/4°AVISO Reprocessed and Nrt data are available from the Copernicus Marine Service repository (2023, 2023b). The SWOT Level 3 KaRIn Low-Rate Sea Surface Height Data Product, version 1.0, is available at (AVISO/DUACS, 2024). The drifter data were supported by GDP (Elipot et al., 2016).

Author contribution

320 XZ and LL conceptualized and designed the methodology; XZ conducted the investigation; JF developed the software; ZL and ZW curated the data and performed formal analysis; ZZ provided resources; XLJ supervised the project; ZXD managed its administration; FX acquired funding; XZ wrote the original draft; and all authors reviewed and edited the manuscript.

Competing interests

The authors declare that they have no conflict of interest.

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