Authors' Response to Reviews of

Implementation and validation of a supermodelling framework into CESM version 2.1.5

W.E. Chapman et al. Geoscientific Model Development, EGUsphere-2024-2682

RC: Reviewers' Comment, AR: Authors' Response, \square Manuscript Text

We thank the reviewers for their thoughtful comments, and have included an acknowledgment to their work in the manuscript. We highlight that the manuscript has gone through a few significant changes due to this review and we believe it is in a much stronger condition. It has been refined greatly with an eye towards readability and flow. We include many more error statistics (see table 1 in the supplemental material). The github repository has been restructured for user clarity (which was a concern of reviewer 1, and this has resulted in new versions on zenodo), and we highlight the improved use-ability of the code and modeling framework. Additionally, the GPCP dataset has been remapped with a new interpolation and this updated many figures, though the broad findings are unchanged.

1. Reviewer #1

- RC: This paper describes a supermodelling framework that combines the effects of the physics parameterization suites from two versions of the Community Atmosphere Model. The physics suites are combined by nudging each version (model component) to the averaged state on a periodic time interval, as in data assimilation.
- RC: Supermodelling is an interesting idea with interesting potential applications, but I think that the manuscript is not ready for publication for three reasons. First, the method is not described in enough detail to allow a reader to reproduce the results. For instance, I couldn't find a tag of the code listed in the manuscript that would allow me to recreate the figures in the manuscript. Furthermore, the scripts have hardwired paths (not variables) with little instruction given as to what lines in the scripts need to be modified. Second, the main application cited is improvement of supermodeled climatologies over the individual components, but only one or two improved fields are shown in the manuscript. The authors argue that improvement will come with tuning, but one might expect to see improvement even with simple equal weighting of the components. It might interest readers to see more discussion of which fields are improved and which are degraded, along with any insights that the authors have regarding the reasons that some fields are improved and others are not. Third, there are many typos in the manuscript, some of which impede understanding of the meaning. I list just a sample of them below. My recommendation is that the authors invest more time in the manuscript and deliver a more polished version.

1.1. Author response:

We would like to sincerely thank the reviewer for their time and effort in evaluating our manuscript. We appreciate the constructive points raised and have made substantial revisions to improve clarity, documentation, and presentation of results. Below, we address each of the major concerns raised by the reviewer.

1. Clarity and Readability of the Manuscript

We acknowledge the reviewer's comment regarding typos and overall polish. In response, we have carefully revised the manuscript to improve clarity, correct errors, and enhance readability. We appreciate this feedback and believe that the current version is significantly more refined.

2. Reproducibility and Code Documentation

We understand the importance of reproducibility and have taken significant steps to improve documentation. The original manuscript included a GitHub repository containing all necessary code to reproduce the figures, but we recognize that the accompanying documentation may not have been sufficiently clear. We highlight that this is not the same repository that the supermodel built is in, which is stated in the **Code and data availability** section. This link to the repository has been highlighted in the supermodel REPO. Additionally, we have expanded on how a user can port their supermodel on any new machine. To address this:

- We have substantially expanded the README and associated documentation to provide explicit guidance on setting up and running the supermodel framework.
- We now explicitly link to a separate repository that reconstructs every figure from the manuscript. This was included in the original submission but may not have been sufficiently highlighted. It is now directly referenced both in the manuscript and the README.
- We have added further instructions on obtaining and installing CESM2.1.5 and the associated CONDA
 python environments to ensure users can set up the required environment, including explicit instructions
 on necessary modifications.

We believe these changes significantly enhance the reproducibility of our work.

3. Model Configuration and Hardcoded Paths

We would like to clarify that our implementation did not contain hardcoded paths except for those referencing the supported instance of CESM2.1.5. However, we recognize that clearer guidance on configuring paths for other environments would be beneficial. To this end, we have:

- Added explicit instructions for users to install their own version of CESM2.1.5.
- Clearly indicated where modifications should be made within the codebase to adapt it to different computing environments.

4. Evaluation of Model Performance

The reviewer notes that the manuscript primarily focuses on introducing the platform and does not extensively analyze the improvement of supermodeled climatologies. While we maintain that the primary goal of this work

is to introduce the framework, we agree that additional analysis can provide valuable context. Additionally, we have removed the sentence in the abstract that may mislead readers and now it is focused more on the platform itself. Therefore, we have expanded our discussion to:

- Include a more detailed comparison of improved and degraded fields of the prognostic variables (U,V,T,Q,PS) at multiple model levels.
- Included an RMSE table in the supplemental to capture the model state biases for the reader.
- · Improved upon our insights into why certain fields show improvement while others do not.
- Clarify that while tuning will play a role in further optimizing performance, some improvements can already be observed with equal weighting.

These additions should help readers better understand both the potential and limitations of the approach.

Final Note

We appreciate the reviewer's feedback and believe that the revisions significantly enhance the manuscript. We hope that the changes we have made address all concerns and improve the clarity and reproducibility of our work. Thank you again for your time and consideration.

1.2. Minor Comments

RC: This part of the caption of Fig. 2 seems to have typos: "SUMO5 (teal); supermodel which uses CAM5-physics (SUMO5); supermodel supermodel which uses CAM6-physics (SUMO6) (purple) at location"

... SUMO5 (teal); supermodel which uses CAM5-physics (SUMO5); supermodel supermodel which uses CAM6-physics (SUMO6) (purple) a supermodel which uses CAM5-physics (SUMO5; teal); a supermodel which uses CAM6-physics (SUMO6; purple)...

- RC: Lines 32-33: "Additionally, biases which are shared across the individual models in an NIE cannot be corrected due to the linear nature of post-process averaging." But does the supermodel succeed in correcting such shared biases? Can the authors offer any insight into when and why shared biases can be corrected?
- AR: This line has been adjusted to point to literature in which the improvement of shared biases is indeed improved in supermodeling. We refer the reader to the revised text. We also encourage the reviewer to read the community comment by Gregory Duane, an expert in super modeling. Duane and Shen (2023) reveal that often improvements are manifest in representations of localized structures, rather than in reductions in RMS error. We have searched for evidence of this, but find no direct measure of improvement in our system. We have adjusted the text to include these references. Please see lines 37-40 in the new manuscript.
- RC: Line 80: "the adaptation of the existing nudging toolbox (reference)". Typo. Please include whatever reference you're referring to here.
- AR: Fixed, Thank you.

- RC: Lines 178–180: "We show results for four experiments: CAM5, CAM6, the supermodel which uses CAM5-physics, but is nudged to the combined state, SUMO5, and the supermodel which uses CAM6-physics, SUMO6." Does SUMO6 nudge to the combined state? If not, how is it different from CAM6? The sentence ends before the SUMO6 configuration is clearly described.
- AR: We apologize for the confusion, we were using shorthand though it is best to be explicit. SUMO6 is also nudged to the combined state. This has been fixed in the text.

We show results for four experiments: CAM5, CAM6, the supermodel which uses CAM5-physics, but is nudged to the combined state, SUMO5, and the supermodel which uses CAM6-physics, but is nudged to the combined state, SUMO6.

- RC: Line 195: "(Fig. ??, right column)". Typo.
- AR: This has been fixed, thank you.
- RC: Lines 195–196: "Correlations between the SUMO5 and SUMO6 experiments are much higher (3, left column)" How can a correlation be as high as 3? Correlations must lie between -1 and 1.
- AR: The 3 refers to pointing the reader at Figure 3, not a correlation score. We have made this more clear in the text
- RC: Fig. 4: I'm surprised that CAM5 and CAM6 have such similar distributions of wind speed. Is there a computational or physical constraint on this distribution?
- AR: There are no computational or physical constraints, though the models have been tuned at NCAR to represent fields well in their creation, likely this is why the distributions are similar.
- RC: Line 258: "One reason to develop supermodels lies in their potential to have smaller mean-field biases." In the example of surface precipitation shown in Fig. 7, the spatial pattern of errors looks similar (shared) in CAM5 and CAM6. The hope implied in lines 32–33 was that such error could be reduced below both components by supermodelling. But Fig. 7 shows that this doesn't happen for surface precipitation. Do the authors have an explanation for this failure?
- AR: Currently, our theory is that when we train the super model, these biases will all improve. However, for now we point to the under synchronization in the tropics as a potential cause. Generally, in the manuscript, we have de-emphasized the point that the model could contain lower biases and instead focus on the platform specifications and the system.
- RC: Line 258: "The work presented her" Typo.
- AR: Fixed! Thankyou.
- RC: Lines 278–279: "Positive values (grey) indicate that the SUPERense is outperforming the NIEnse and vise-versa." Are positive values grey or green?

Positive values (green grey) indicate that the SUPERense is outperforming the NIEnse and vise-versa while negative values (blue) indicate the opposite.

RC: Lines 289–290: "This circumvents the in CESM costly initialization stage and introduces effectively PAUSE/RESUME capability (Fig. 1)." Typos?

AR: Yes, we have fixed the typos.

The exchange of information is managed through a novel Python-FORTRAN I/O interface that avoids the need to stop and start each model. This circumvents the in CESM costly initialization stage and introduces effectively PAUSE/RESUME capability (Fig. 1). This circumvents in CESM the costly initialization stage and introduces a PAUSE/RESUME capability (Fig. 1). This Python-FORTRAN bridge was also used to manage the timestamps in the output files, and efficiently write the pseudo-observations files.

- RC: Lines 300-301: "To test our implementation we linked the CAM5/CAM6 atmosphere and confirmed that synchronization across various temporal scales and variables Even though the supermodels only exchange limited information . . ." What did you confirm?
- AR: We have fixed the typo that clarifies the text.

To test our implementation we linked the CAM5/CAM6 atmosphere and confirmed that synchronization occurs across various temporal scales and variables.

- RC: Lines 317–319: "To create all model runs and build your own supermodel, refer to Chapman et al. (2024). This second repository contains the setup for the SuperModel and its constituent models, including source modifications, model build scripts, and namelists for running the described CAM versions." Is a tag of the CESM repository listed somewhere so that readers can reproduce the figures in the paper identically?
- AR: Yes, though this was in the original manuscript, we have highlighted the text in the model README so it is easier to find and link to the figure repository in the new documentation.

We thank the reviewers for their thoughtful comments, and have included an acknowledgment to their work in the manuscript. We highlight that the manuscript has gone through a few significant changes due to this review and we believe it is in a much stronger condition. It has been refined greatly with an eye towards readability and flow. We include many more error statistics (see table 1 in the supplemental material). The github repository has been restructured for user clarity (which was a concern of reviewer 1, and this has resulted in new versions on zenodo), and we highlight the improved use-ability of the code and modeling framework. Additionally, the GPCP dataset has been remapped with a new interpolation and this updated many figures, though the broad findings are unchanged.

Though you had only included questions as minor points to strengthen the manuscript, we have incorporated those points into our revised manuscript and share the main changes of those points below.

2. Reviewer #2

RC: The present paper describes the implementation of a supermodel framework in which the two conventional climate models CAM5 and CAM6 are interacting, or synchronized, during their simulation through the regular exchange of nudging terms for some of their state variables. Through an appropriate tuning of the computation of these nudging terms, and because of the higher dimensionality of the supermodel benefiting from the advantages of each of its components, one might expect some compensation of the component model errors and an improved representation of the climate dynamical system. The present paper is a preliminary step towards such an assessment, providing a significant step in developing such

kind of supermodels, sufficiently efficient to be used for climate studies. The paper is well structured and written (though quite a few typos remain and deserve a more careful reading of the whole text). The objective are clearly stated, and the results clearly demonstrate an efficient supermodel (about 3-4 years of simulated years per days) and a rather appropriate synchronisation of the model variables, as indicated in particular by a high frequency variability commensurate with the conventional models. I have a few general comments and a longer list of minor comments that follow. The general comments should not be understood as a major revision, as I consider the present paper as a technical contribution to the Geoscientific Model Development Journal. These comments are meant to widen a bit the analysis and whenever possible enhance the physical interpretation of the results and discuss their implications, possibly in light of previous works (which I am not familiar with).

2.1. General Comments

- RC: 1. The synchronisation is convincing for U, V and T, except over the tropics. Can you formulate hypotheses why this happens? Is it consistent with previous studies? To what extent is it an issue for the supermodelling strategy? Do you see ways to improve this synchronisation? For variables that are not part of the nudging strategy, the synchronisation is rather weak. To what extent is it also an issue for the supermodelling strategy?
- RC: 2. Have you analysed the supermodel behavior for other fields than wind and precipitation? What about radiative fluxes or surface turbulent fluxes? Do you keep a reasonable energy budget in the supermodels? If not, this should clearly prevent you to apply the approach for the coupled system, shouldn't it?
- RC: 3. With respect to natural variability, you focus on the PNA and NAO types of variability. Have you analysed other modes of variability, like the MJO or convectively-coupled equatorial waves? To what extent is their simulated behaviour over the tropics consistent with the reduced high-frequency variability over the tropics?

We sincerely thank the reviewer for their insightful feedback, which raises important questions about the synchronization characteristics and overall performance of the supermodel. Below, we address each point in turn and outline directions for further investigation. We have altered the text in the manuscript to address all of the points, or to point to new avenues of research, in the manuscript.

1. Synchronization in the Tropics and for Non-Nudged Variables

We acknowledge the reviewer's observation that synchronization is weaker in the tropics and for variables outside the nudging strategy. One possible explanation for this is that tropical dynamics are more governed by convective and diabatic processes rather than large-scale balanced dynamics, making them inherently more chaotic and less constrained by the imposed nudging. Previous studies (e.g., [Counillon et al., 2023]) have also observed similar challenges in achieving full synchronization in the tropics, suggesting this may be a fundamental limitation of the approach when applied to regions dominated by deep convection. However, there is hope for improvements in coupled models because surface fluxes can be synchronized via sea surface temperature leading to improvements in climatological precipitation patterns in the tropics, as seen in Shen et al. [2016], in the COSMOS model. This is because of the ocean-atmosphere interaction is strongest in the tropics.

For variables that are not explicitly nudged, weaker synchronization is expected, as their evolution remains primarily determined by the underlying physical parameterizations of each component model. While this does

not necessarily undermine the supermodelling approach, it does suggest that expanding the set of exchanged variables or optimizing the nudging parameters could improve synchronization. Future work should explore whether increased nudging frequency or selective tuning of nudging coefficients could help address this issue.

2. Energy Budget and Additional Fields

The reviewer raises an important point regarding radiative and surface turbulent fluxes, as well as the overall energy budget of the supermodel. While our current analysis has primarily focused on wind and temperature fields, we recognize that maintaining a reasonable energy balance is crucial, particularly for future applications in coupled models.

Although we have not conducted a detailed analysis of radiative fluxes or surface energy budgets in this study, this is a key direction for further verification. Ensuring that the supermodel maintains physical consistency in terms of energy conservation will be necessary before extending the approach to coupled systems. Future studies should include a comprehensive assessment of energy fluxes and potential corrections to avoid spurious energy imbalances. We have included in our conclusion that coupling this model to an ocean state requires that the fluxes are represented well, and that work is underway to address what can be done to tune the model in that way. Additionally, we cite a study which has conducted a supermodel on coupled fluxes and mention the findings in their work (see, Duane and Shen [2023], Shen et al. [2016]).

3. Modes of Variability in the Tropics

We appreciate the reviewer's suggestion to analyze additional modes of variability beyond PNA and NAO, particularly in the tropics. Given that tropical variability is often strongly influenced by high-frequency convective processes (such as the Madden-Julian Oscillation (MJO) and convectively coupled equatorial waves), a deeper assessment of these features within the supermodel framework would indeed be valuable. We find this analysis potentially beyond the scope of the current manuscript, however, we include a discussion of this point in the manuscript to make the readers aware of the potential issue. We anticipate that due to the large scale nature of the MJO that the synchronization actually might be quite high. Alternatively, it is possible that requiring higher frequency coupling could more directly address this point, this is a point to explore in future work.

Our current results indicate that tropical high-frequency variability is somewhat damped, which may have implications for the representation of these modes. Investigating how the supermodel handles MJO dynamics, equatorial waves, and other modes of tropical variability is an important area for future research. This could involve spectral analysis of convective variability or direct comparisons with observed MJO characteristics.

Final Remarks

While our current study has focused on demonstrating the technical feasibility of the CAM5/CAM6 supermodel and confirming basic synchronization behavior, we agree that a deeper assessment of synchronization patterns, energy budgets, and tropical variability is necessary to fully evaluate the approach. These questions provide a roadmap for future work, particularly as we move toward trained and dynamically weighted supermodels.

We thank the reviewer for these constructive suggestions, which will help guide the next stages of supermodel development.

2.2. Line Specific Comments

RC: p2, l28: the NMME and CMIP acronyms need to be defined.

AR: Fixed, thank you.

... rather than decades. Though, decadal non-local corrections have been made in a simplified coupled ocean-atmosphere model (Brajard et al. 2021).

RC: p3, l60: typo: one of the two 'to be' needs to be removed.

AR: Fixed, thank you.

RC: p3, l80: what does 'reference' stand for here? Did you forget to add a reference here?

AR: Thank you for this comment, yes we had intended to place a reference to our previous manuscript which leveraged the nudging toolbox. It is now in place.

RC: p3, l81: I guess it is 'component models' rather than 'components model'.

AR: We agree, thank you, it has been fixed.

RC: p4, l123-124: do you mean that sea surface temperatures are constant over each day in CAM (there is thus a small jump at the end of each day)?

AR: No, we are sorry for the confusion, each time-step has an independent SST field which is smoothly interpolated from time-step to time-step between monthly values.

which are linearly interpolated to obtain specified independent values at each time-step daily values, as well as the evolution of aerosol emissions and trace gas concentrations (including CO_2).

RC: p5, 1127: why using a bilinear interpolation and not a conservative one? At least for precipitation, a conservative interpolation sounds more appropriate. Besides, what is the resolution of ERA5 and GPCP datasets?

AR: We appreciate the comment and have switched the precipitation to a conservative regridding and have updated the text. This altered Figure 7 and Figure 9 in the manuscript (slightly) though we note that the results have not changed due to this shift. Additionally, we have added the original resolution of the fields.

We verify the model against the $\sim 0.25^{\circ}$ ERA5 reanalysis product hersbach2020era5 for all fields except precipitation, which is verified against the 1° NOAA GPCP product Adler2003. For verification, every observational the ERA5 product is bi-linearly interpolated to the native CAM grid prior to any metric calculation. The GPCP product is regridded to the native CAM grid using a conservative mapping method.

RC: p5, l151-154: I feel this technical development requires a bit more explanation to more fully understand how you overcome this challenge of submitting jobs through a single PBS/SLURM scheduler.

AR: We apologize, we have updated how the challenge is handled.

We also tackled the challenge of submitting multiple jobs through a single PBS or SLURM scheduler. This addresses the issue of asynchronous model queuing, where one model might clear the submission queue while the other remains pending, thereby saving considerable computational time.

To address the challenge of submitting multiple jobs through a single PBS/SLURM scheduler, we implemented a batch submission script that allows two model simulations to be launched concurrently while managing resource allocation efficiently. Our approach ensures that both models utilize the available compute nodes without interfering with each other, thus avoiding scenarios where one model monopolizes the queue while the other remains pending.

Specifically, our script:

- 1. **Prepares model runs** by creating initialization files for both simulations.
- 2. **Defines model-specific execution settings**, including the number of processing elements required for each job.
- 3. **Partitions compute resources dynamically** by selecting appropriate node allocations from \$PBS_NODEFILE, ensuring that both jobs receive the necessary resources without conflicts.
- 4. **Executes model runs in parallel** using background processes (δ), allowing both jobs to start simultaneously while still being managed within a single job submission.
- 5. Waits for all processes to complete using wait, ensuring that computational resources are fully utilized before job completion.

This method ensures efficient job scheduling and mitigates the risk of asynchronous queuing delays, ultimately reducing computational time.

- RC: Section 2.4: I am a bit confused about how the nudging is performed. Do you average the instantaneous state of the atmosphere over the two model, and then use it for nudging over the 6 following hours (thus the fields toward which the model is nudged are constant over the 6-hour window)? Besides, which nudging timescale to you use?
- AR: We have clarified this portion of the text significantly. We encourage the reader to see this section, and include it below to address the comment directly.

At the beginning of the physics timestep, the first component model outputs the model state variables—Zonal wind (U), Meridional wind (V), Temperature (T), and Specific Humidity (Q)—and initiates a model pause by writing a PAUSE file. Subsequently, CAM calls a Python script that waits for the second model to reach the beginning of its physics timestep and then combines the outputs from both models at the same timestamp. If the component model grids differ, Python interpolation routines are invoked to ensure consistency. Once the output has been processed, the Python script removes the PAUSE file, allowing the model to resume operation without the need for re-initialization or re-entering the queue.

A nudging tendency is then applied to each component model, following Equation (1), which nudges the model state toward the combined model state (X_{combined}) during the first timestep after the models resume running [e.g.,][]Chapman and Berner [2024]. The user can set the nudging timescale (τ); in

this experiment, we use a relaxation timescale of 6 hours. Though we emphasize that the tendency is only applied at the first timestep after the combination.

$$\frac{dX}{dt} = F(X) + \frac{X_{\text{combined}} - X}{\tau} \tag{1}$$

where X is the model state, F(X) represents the model's internal tendencies, and τ is the nudging relaxation timescale.

To address the challenge of submitting multiple jobs through a single PBS/SLURM scheduler, we implemented a batch submission script that allows two model simulations to be launched concurrently while managing resource allocation efficiently. Our approach ensures that both models utilize the available compute nodes without interfering with each other, thus avoiding scenarios where one model monopolizes the queue while the other remains pending.

RC: p6, l167-168: while being an important effort toward open science, this sentence does not seem to be at the right place in these technical description.

AR: We have removed this comment

The CAM5/CAM6 SuperModel, including the CESM Fortran-Python-bridge, supermodel module toolbox with namelist section, and scheduler scripts, are readily available via the Github Repository. Our use of GitHub for version control and distribution reflects our dedication to open science, promoting a culture of sharing code and knowledge. It is deployed on two HPC platforms 1) the National Center for Atmospheric Research's Derecho Computer and 2) the Norwegian Research Infrastructure Services' machine Betzy.

RC: p7, l171-172: this would be interesting to have the elapsed (integrated also) time also for CAM5 and CAM6, to document the overloading of the model synchronisation.

AR: We have added this language to the manuscript.

... increase the wallclock time. We acknowledge that this is a significant slowdown from a CAM5/CAM6 simulation which can accomplish a year long simulation in ~ 2.5 hours with identical computational resources.

RC: p7, l177: can you elaborate a bit more on this difficulty when adding specific humidity in the nudged state variables?

AR: The main challenges with including specific humidity (Q) in the nudging process stem from the intrinsic properties of moisture in the atmosphere and its coupling with cloud and precipitation processes. In our experience—and as noted in previous studies—several issues arise when directly adjusting Q. Because of these factors, prior work (e.g., Chapman et al. 2024; Raeder et al. 2021) has shown that attempts to nudge Q can introduce more problems than they solve. By allowing Q to evolve freely, we avoid these complications while still effectively constraining the dynamical fields (U, V, and T) that drive the large-scale circulation and, indirectly, the moisture distribution. These considerations motivated our decision to exclude Q from the direct nudging process in the CAM5/CAM6 supermodel implementation. Although this approach may not be entirely satisfying from a theoretical standpoint, it provides a pragmatic solution that leads to a more stable and realistic mean state representation.

We have added a sentence to address this in the manuscript:

We now demonstrate the synchronization and resulting mean state representation for the CAM5/CAM6 supermodel for the period 1979 through 2005, The supermodel uses an interaction timescale of $\eta=6$ hours and employs snapshot nudging to the unweighted averaged state. In this implementation, the information in U, V, and T are exchanged and nudged while Q is left to evolve freely. We speculate that the main challenges with including specific humidity (Q) in the nudging process stem from the intrinsic properties of moisture in the atmosphere and its coupling with cloud and precipitation processes.

RC: p8, l195: I guess your refer to Figure 3.

AR: Thank you! This has been adjusted.

RC: p8, l196: 'Fig.' is missing before '3'.a

AR: Thank you! This has been adjusted.

RC: p8, l199-200: without any more detailed analysis, I would argue that the whole atmospheric physics might be at play (most of it is strongly different between CAM5 and CAM6). Besides because the U, V and T forcing in the tropics is in general weaker than in the extratropics, this is rather expected that the model are more sensitive to their own physics, isn't it?

AR: Thank you for your comment, we have chosen to remove this sentence to reflect the uncertainty that you describe.

Synchronization is strong in the U, V, and T fields poleward of 15, especially in the storm track regions. The Maritime continent region (Lat: [15S,15N], Lon:[60E,200W]) displays the least amount of synchronization , which might be related to SUMO5 and SUMO6 having different deep convective parameterization schemes.

RC: 15. p8, l202: missing ending bracket.

AR: Thank you! This has been corrected.

RC: 16. p8, l202-203: The link between the two parts of the sentence remains unclear, and not obviously consistent with what you write l199-200.

AR: We were missing a period, and that has been added, we also clarified our meaning about the pressure levels/

The supplemental material shows the same analysis for pressure levels of 750 hPa and 900 hPa (Fig. 1S and Fig. 2S). Generally, we see greater synchronization at of U.V, & T at higher pressure levels, while Q has a greater synchronization nearer to the surface, which could be a result of a similar sea surface temperature field.

RC: p8, 1207-208: the link is interesting, but probably hard to fully understand for most readers. A bit more explanation would be welcome.

AR: we have opted to remove the sentence to not confuse readers:

This issue is structurally related to the double penalty problem in modernmachine learning for Numerical Weather Prediction (Brenowitz et al., 2024).

RC: p8, l218: missing closing bracket.

AR: Thank you! This has been corrected.

RC: p10, l222: do you mean increasing or reducing the relaxation timescale?

AR: We have clarified our meaning

Moving to relaxation timescales tends to reduce this damping, so that we hypothesize using interaction timescales of 6h or less is beneficial with regard to minimizing the damping of high frequency variability. In nudging studies, moving to an observations frequency of less than 6 hours seems to alleviate effects of damping davis2022specified, so we hypothesize that increasing the SUMO interaction frequency will be beneficial with regard to minimizing the damping of high frequency variability.

RC: p12, l251: do you mean the correlation between the PNA pattern of SUMO5 and that of SUMO6?

AR: We apologize for the confusion this sentence caused, you are indeed correct. We have amended the language.

The principal components (PC) corresponding to the supermodel PNA show a Pearson correlation coefficient of 0.992, while the correlation between the PNA PC from CAM6 and SUMO6 is 0.27. The principal components corresponding to the SUMO5 and SUMO6 PNA exhibit a Pearson correlation coefficient of 0.992, whereas the correlation between the CAM6 PNA PC and the SUMO6 PC is only 0.27.

RC: p12, l255: do you have an interpretation or an hypothesis for such a different result between PNA and NAO? Has it been seen in previous studies?

AR: We do not, likely the NAO represents a weaker signal more greatly affected by internal variability, rather than surface forcing and thus. However, we choose not to speculate in the manuscript.

RC: p13, l258: I guess it should be 'here', not 'her'.

AR: Thank you! This has been corrected.

RC: p13, l267-268: My understanding is that Figure 4S is showing the differences between the non-interacting ensemble and the supermodel ensemble. It does not seem to correspond to what you are referring to here.

AR: This figure was incorrectly linked in the Supplemental and has now been corrected and the correct figure is linked.

RC: p16, l289: I would remove the 'in' before CESM.

AR: Thank you! This has been corrected.

RC: p17, Code and data availability: a recap about the CAM versions and the place where to find the code would be welcome in this section.

AR: Thank you! The link has been added!

References

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