Wet-Radome Attenuation in ARM Cloud Radars and Its Utilization in Radar Calibration Using Disdrometer Measurements

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Abstract

A relative calibration technique has been developed for the U.S. Department of Energy's (DOE) Atmospheric Radiation Measurement (ARM) user facility Ka-Band ARM Zenith Radars (KAZRs). This method uses the signal attenuation caused by water on the radome to estimate reflectivity factor (Ze) offsets. The wet-radome attenuation (WRA) is assumed to follow a log-linear relationship with rainfall rate during light and moderate rain, as measured by a collocated surface disdrometer. The technique has an uncertainty of approximately 3 dB, due to factors such as disdrometer measurement error, rain variability between radar and disdrometer sample volumes, and the fitting function's uncertainty for the WRA behavior. A practical advantage of this WRA-based approach to shorter-wavelength radar monitoring is that, while it requires a reference disdrometer, it proves feasible for a wider range of collocated disdrometer measurements compared to traditional direct disdrometer comparison at the onset of light rain. This technique thus offers a cost-effective monitoring tool for remote or long-term radar deployments.

This calibration technique was applied during the ARM TRacking Aerosol Convection interactions ExpeRiment (TRACER) from October 2021 through September 2022. The estimated Ze offsets were compared against traditional radar calibration and monitoring methods using available datasets from this campaign. Results show that the WRA-based offsets align closely with mean offsets found between cloud radars and from direct disdrometer comparison near the onset of rain, while also reflecting similar offset and campaign-long trends when compared to collocated, independently calibrated radar wind profiler. Nevertheless, overall, the KAZR Ze offsets estimated during TRACER remained stable at approximately 2 dB lower than the disdrometer estimates from the campaign start until the end of June 2022, afterward, the offsets increased to around 7 dB by the campaign's end. This increase is linked to a drop of about 1 dB in transmitter power toward the end of the project.

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Short Summary

A relative calibration technique is developed for the cloud radar by monitoring the intercept of the wet-radome attenuation log-linear behavior as a function of rainfall rates in light and moderate rain conditions. This resulted KAZR Ze offset during the ARM TRACER campaign is compared favorably with the traditional disdrometer comparison near the rain onset, while also demonstrates similar trends with respect to collocated and independently calibrated reference radars.

1 Introduction

The U.S. Department of Energy (DOE) Atmospheric Radiation Measurement (ARM) user facility operates millimeter-wavelength cloud radars (35 and 94 GHz) at various global fixed and mobile sites (e.g., Mather and Voyles, 2013; Miller et al., 2016; Kollias et al., 2007, 2020). These "cloud" radars are often more sensitive than traditional centimeter-wavelength weather radars, allowing them to detect cloud droplets more effectively. However, this sensitivity comes with a trade-off, as shorter wavelengths are prone to partial or complete attenuation in clouds and precipitation. Such attenuation introduces uncertainties in key radar-derived properties like reflectivity factor (Ze), affecting cloud and hydrological retrieval accuracy (e.g., Matrosov, 2005; Deng et al., 2014; Zhu et al., 2019).

Given the importance of accurate Ze measurements, the routine deployment and operation of cloud radars necessitate frequent calibration and monitoring activities. In general, more rigorous radar calibration efforts can be implemented (e.g., Russchenberg et al., 2020), but these approaches are often system-specific and require highly skilled engineers or technicians, significant time, and specialized equipment (within ARM, e.g., Mead, 2010). For weather and climate applications, radar-based research has increasingly turned to "relative" calibration techniques, which rely on Ze estimates from nearby reference instruments or expectations based on intrinsic properties of the hydrometeors or other media (e.g., Bringi and Chandrasekar, 2001; Giangrande et al., 2005; Protat et al., 2011; Kollias et al., 2019; Maahn et al., 2019; Williams et al., 2023). Several of these “natural” calibration concepts have proven effective for quantifying radar performance in many

hydrological applications requiring Ze estimates within 2-3 dB. The simplest approach is often a cross-comparison of Ze characteristics with collocated, calibrated reference radars. For example, extended comparisons of clouds near ARM ground sites using CloudSat radar measurements have successfully monitored the long-term ARM cloud radar record (Protat et al., 2011; Kollias et al., 2019). For finer-scale comparisons during ARM deployments, the Ka-Band ARM Zenith Radar (KAZR) is often collocated with a Radar Wind Profiler (RWP, 915 or 1290 MHz) and the Ka- and X-band Scanning ARM Cloud Radar (KaSACR/ XSACR), which are easier to monitor using independent techniques better suited to scanning and/or longer-wavelength radar.

Among the various methods of relative cloud radar monitoring, a common approach relies on surface disdrometer observations. The reflectivity factor can be estimated for assumed rain properties using techniques such as T-matrix scattering algorithms applied to the drop size distribution of rain measured by the surface disdrometer (Mishchenko et al., 1996). Comparing radar-measured reflectivity near the surface with disdrometer-estimated reflectivity provides a common way to estimate radar calibration offsets (e.g., Kollias et al., 2019; Myagkov et al., 2020; Russchenberg et al., 2020; and Lamer et al., 2021). Disdrometer comparison techniques like this have been implemented as routine procedures for radar monitoring, such as in the Aerosol Cloud Tracer Gas Research Infrastructure (ACTRIS) network in Europe (Dupont et al., 2022). For radars that experience negligible attenuation in rain, such procedures are often straightforward to implement across a variety of widespread precipitating conditions (e.g., Williams et al., 2023). However, for shorter radar wavelengths, where gaseous attenuation, rain attenuation, and wet-radome attenuation are not negligible, applying this approach can be more complicated.

Specifically, the two-way attenuation associated with radome wetting (referred to here as wet radome attenuation or WRA) is a well-known phenomenon. During rainfall, water droplets bead on the surface of the radar radome, forming a wet film that eventually flows off the radome once it reaches sufficient mass, similar to the water layer on a car window. Droplets impacting the radome during persistent rain further alter the water depth through bouncing and splashing (Gibble, 1964; Anderson, 1975; Yu et al., 2021). For long-wavelength radars, WRA is often considered negligible (Thompson et al., 2012; Kurri and Huuskonen, 2008). However, for shorter-wavelength radars, the impact of WRA is potentially more significant. For example, at X-band, Bechini et al. (2010) and Gorgucci et al. (2013) observed a loss of 5 dB in moderate rain by comparing simultaneous X-band radar measurements using spherical radomes with a collocated video

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disdrometer. This WRA has been shown to depend on the thickness of the water film (d) on the radome, which in turn is a function of rain rate, as described by the Gibble formula (Gibble, 1964; Anderson, 1975):

$$d = \left(\frac{3\mu_k r R}{2g}\right)^{1/3} \quad , \quad (1)$$

where μ_k is the kinematic viscosity of water (that also varies with temperature), r is the radome radius, R is the rain rate, and g is the gravitational acceleration. Additional relations between WRA and R have been developed based on the Gibble's $R^{1/3}$ formula by Frasier et al. (2013) and Gorgucci et al. (2013) for X-band radar calibration studies.

Few studies have considered WRA for assessing cloud radar offsets at Ka-band (35 GHz). As the water absorption coefficient is inversely proportional to wavelength (Bertie et al. 1996, Segelstein 1981), the WRA at Ka-band is approximately as three times as that at X-band for the same depth of rainwater on the radome. It is understood that WRA will impact direct estimates of the offset between cloud radar and disdrometer Ze estimates in rainy conditions, and faulty offset assessment after rain ends may occur owing to extended radome drying delays. Therefore, direct comparison concepts previously cited typically consider only the periphery cloud, drizzle or light rain conditions (i.e., R < 1-2 mm hr^{-1}) at the onset of a rainfall event to minimize various forms of attenuation. This often is a very stringent and subjective employment of these conditions: First, it limits the opportunities for direct disdrometer monitoring of cloud radar to a selected window of rainfall rates and event timing. Identifying these light rain or drizzling conditions is also contingent on the requirements for collecting high-quality disdrometer measurements (i.e., those that require significant droplet number counts), wherein a separate rain rate cut-off may be required to avoid significant WRA. Overall, it is potentially useful to establish other forms of cloud radar monitoring that could benefit from a wider range of observations collected during precipitation window.

In this study, we first identify intervals of WRA for Ka-band radars by comparing observations from ARM's KAZR with a collocated suite of instruments, including a surface disdrometer, a calibrated RWP, and KaSACR/XSACR observations collected in vertical pointing (VPT) modes during the Tracking Aerosol Convection Interactions Experiment (TRACER). We then develop a new WRA fitting technique and apply it to calibrate the Ze offset for KAZR using TRACER measurements. The performance of this technique is evaluated against three traditional

relative calibration or monitoring methods for Ka-band radar: (i) direct disdrometer comparisons of Ze in light rain at the onset of rain events, (ii) a cross-comparison with independently calibrated RWP measurements, and (iii) a cross-comparison with collocated scanning KaSACR measurements.

The paper is organized as follows. Section 2 introduces the radar datasets and supporting TRACER datasets used in this study. In Section 3, a relative calibration technique is developed with daily KAZR and KaSACR measurements collected during light and moderate rainfall conditions. In Section 4, the technique is applied to the KAZR measurements during the TRACER campaign to assess the long-term calibration offset trend for KAZR, and the result is evaluated against other calibration methods. A summary of the performance of this WRA technique for relative offset monitoring is provided in Section 5.

2 TRACER Dataset Description and Comparisons

The TRACER campaign took place in the Houston, TX region from 1 October 2021 to 30 September 2022 (Jensen et al., 2019, 2022, and 2023) with a goal of studying the interactions of aerosols and convective clouds. The main surface measurement site was located at La Porte, TX housed the deployment of the first ARM Mobile Facility (AMF1; Miller et al., 2016). The AMF1 consists of several ground-based remote-sensing and profiling instruments, and included the deployment of the KAZR, KaSACR/XSACR, and radar wind profiler (RWP) units that serve as the radars for this study. The surface instrumentation also included multiple laser and video disdrometers as reference anchors.

2.1 TRACER Cloud Radars (KAZR and KaSACR/XSACR)

The KAZR (Widener et al., 2012) is a successor to ARM's highly successful millimeter-wavelength cloud radar (MMCR). The KAZR has a flat radome inclined at 4°. A complete list of KAZR specifications is provided in Table 1. The KAZR transmits and receives two types of pulses: (i) the burst pulse, a simple narrow pulse of radio-frequency energy (referred to as "GE" mode), and (ii) the chirp pulse, a longer, frequency-modulated pulse with higher transmitted energy and greater sensitivity, but with data collection starting at a higher range due to the larger blind zone imposed by the longer pulse length (referred to as "MD" mode). Although the MD mode is more

189 sensitive to clouds (i.e., has a lower minimum detectable Ze), only the KAZR GE mode data are
190 used for disdrometer comparisons, as near-surface observations are required.
191 The KaSACR and XSACR are co-mounted on a scanning pedestal (Kollias et al., 2014a,
192 2014b). During TRACER, the KaSACR/XSACR typically followed a 10-minute scanning pattern:
193 (i) two low-level plan position indicator (PPI) scans at 1° and 2° elevation, followed by (ii) 6
194 hemispheric range height indicator (HSRHI) scans at 30° azimuth intervals, and then (iii) 2 minutes
195 of vertical pointing (VPT) mode. This study utilizes the 2-minute VPT mode segment from each
196 10-minute scanning sequence (i.e., nominal scanning VPT mode). The specifications during VPT
197 mode are listed in Table 1. For one event on September 3-4, 2022, the KaSACR/XSACR was
198 temporarily operated exclusively in VPT mode (i.e., stationary VPT mode) for radar cross-
199 calibration purposes. The KaSACR has an inclined radome similar to the KAZR but is relatively
200 newer, with potentially less deterioration of its hydrophobic coating. The XSACR has a conical
201 radome with a slant angle of 45° to the surface. Overall, the WRA effect is expected to be smaller
202 for the XSACR compared to either Ka-band radar, due to wavelength-dependent differences as
203 well as the improved radome design. The KaSACR calibration offsets between May and
204 September 2022 are expected to be stable based on ground clutter analysis using relative
205 calibration adjustment (RCA) techniques (Skolnik, 2000; Hunzinger et al., 2020) and are reported
206 to be close to 0 dB, according to the ARM TRACER radar b1 data processing report (Feng et al.,
207 2024).
208 To compare with Ze estimates from disdrometer measurement, radar measurements at 500
209 m are selected and corrected for gaseous attenuation using nearby radiosonde measurements (e.g.,
210 Ulaby et al., 1981). Rain attenuation is also corrected using specific attenuation coefficient (K)
211 estimates from disdrometer measurement, assuming a uniform layer between the surface and 500
212 m. There is concern that the radar might saturate, particularly for the KaSACR near its minimum
213 range, which could introduce a low bias in measured Ze compared to disdrometer Ze. Based on
214 communication with an ARM radar engineer, the power associated with the highest voltage
215 digitizable by the radar's Analog-to-Digital Converter (ADC) is 5.9 dBm. The corresponding
216 KAZR saturation reflectivity at 500 meters is approximately 45 dBZ, given its calibration constant
217 of -12 dBm. Similarly, the KaSACR saturation reflectivity at 500 m is about 31 dBZ, given its
218 calibration constant of -26 dBm. The measured radar reflectivities from both KAZR and KaSACR

at 500 m are generally less than 25 dBZ, well below the saturation threshold. Additional supporting evidence through radar profile comparisons can be found in the supplementary material.

2.2 Surface Disdrometer Measurements and Value-Added Products

A Parsivel2 laser disdrometer (LDIS) and a two-dimensional video disdrometer (VDIS) unit were deployed at the main site during TRACER in very close proximity to the cloud radars. For disdrometer geophysical quantities and data quality control, procedures follow the standard drop size distribution (DSD) filtering in Giangrande et al. (2019) implemented by ARM in their precipitation value-added products (Video Disdrometer Quantities--VDISQUANTS and Laser Disdrometer Quantities--LDQUANTS, Hardin et al., 2020). These products employ several fall speed checks, temperature, drop shape/canting assumptions, larger drop restrictions (no drop sizes > 5 mm) and drop count thresholds (> 20 drops per minute for a valid DSD) that impact estimates of hydrometeor Ze and *K* for radar frequencies using a T-matrix scattering algorithm (Mishchenko et al., 1996). As further discussed within the disdrometer literature (Tokay et al., 2001, 2013; Giangrande et al., 2019; Wang et al., 2021), the VDIS is considered the more reliable and sensitive disdrometer to a wider range of drop sizes under nominal light rain operating conditions. Therefore, the estimated Ze at Ka-band in VDISQUANTS is used within this study as our ground truth for KAZR calibration and surface rain rate, while the LDIS products have been used as an independent reference for monitoring RWP Ze estimates (e.g., Williams et al., 2023), which is required for additional direct radar comparisons in Section 4.

2.3 Radar Wind Profiler (RWP)

The RWP deployed during TRACER was operated using an adaptive scanning mode, switching between a traditional boundary layer horizontal wind mode and a vertically pointing precipitation mode adopted by ARM for its recent deep convective cloud campaigns (e.g., Tridon et al., 2013; Giangrande et al., 2013, 2016). When the signal-to-noise ratio in the vertical beam exceeded a predefined threshold, the RWP switched into this precipitation mode and employs a single vertically pointing beam operation. This mode transmitted short- and long-pulses to observe echoes close to the radar with fine resolution, or further from the radar with coarser resolution. Important to this study, the TRACER RWP mode switching sometimes prevented the RWP from immediately observing the periphery lightly precipitating clouds as they passed over

the AMF1 site. However, this mode-switching sampling issue does not impact the bulk KAZR-RWP Ze cross-comparisons because we primarily consider daily average behaviors. As before, the RWP Ze measurements in precipitation mode were calibrated independently using collocated LDIS observations (i.e., Williams et al., 2023), who found a standard deviation of 2 - 4 dB between the RWP at 500 m and LDIS.

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3 Cloud Radar Ze Calibration and Monitoring: Development of a New WRA Technique

3.1 Identification of WRA: KaSACR/XSACR in Stationary VPT Modes

Figure 1a-c show the measured reflectivity (Ze) from the KaSACR/XSACR and the KAZR GE mode on 03-04 September 2022, when the KaSACR/XSACR was operated exclusively in a stationary vertically pointing (VPT) mode. Two intervals of widespread rainfall were captured: the first around 17-19 UTC and the second from 20–02 UTC. A radar "bright band" signature, indicative of the melting level, appears around 5 km AGL during this event. After 02 UTC (20 LT), light rain gave way to high, scattered clouds through the night, until thick anvil clouds from nearby convection moved in around 15 UTC (09 LT). Overall, the KaSACR/XSACR reported similar Ze values under peripheral cloudy conditions and during light rain, where rain attenuation and WRA were minimal. As expected, larger discrepancies between XSACR and KaSACR (with the KaSACR showing lower, attenuated Ze values) occurred during heavier rainfall from 22-00 UTC. The KAZR consistently reported lower Ze values than the KaSACR, with differences often exceeding 5 dB throughout the event.

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The Ze difference between the KaSACR and KAZR values in Fig.1d exhibits strong temporal variation but limited vertical variation, indicating that the difference is likely driven by the radar or its local environment (e.g., WRA) rather than atmospheric features. The minimum difference of ~7 dB in high clouds, observed around 17-18 UTC and again the next morning (15-17 UTC on 4 September), suggests an overall Ze offset between the KAZR and KaSACR. A minimum difference of ~7 dB in rain (at 19, 21, and 23 UTC) indicates similar WRA behavior for both KAZR and KaSACR. However, a prolonged increase in this difference after moderate rain, especially under humid conditions at night (0-12 UTC, or 18-6 LT), suggests that the KAZR and KaSACR may experience additional discrepancies after rain or in high humidity, possibly due to the older, less hydrophobic radome of the KAZR, as noted in the Cloud, Aerosol, and Complex

Terrain Interactions (CACTI) campaign (Varble et al. 2021; Hardin et al. 2020). Accurate correction for KAZR wet-radome attenuation is challenging and beyond the scope of this study; however, WRA behavior in rain can provide a basis for tracking KAZR calibration, as will be demonstrated in the following sections.

The time series of rain rate (R), K and Ze estimates at Ka- and X-bands from VDISQUANTS for the 03-04 September 2022 case are shown in Fig. 2a and b. The sampled R from the disdrometer is commonly less than 1 mm hr^{-1}, but approach 5 mm hr^{-1} around 2330 UTC. The Ze from KAZR, KaSACR/ XSACR at 500 m are plotted in Fig. 2b. For all collocated precipitating samples, the XSACR Ze (black crosses) has a high correlation with estimated Ze (rr = 0.95), while KAZR Ze (blue crosses) are biased low when directly compared to the disdrometer Ze, which is exacerbated further in heavy rain contexts. KaSACR Ze (red cross) falls in between XSACR and KAZR Ze values.

Figure 2c shows the differences between measured and estimated Ze (Dze) for KAZR, KaSACR, and XSACR. The XSACR exhibits a minimum Dze of 0 dB when the rain rate is below 0.1 mm hr^{-1}, but this difference can reach 5 dB around 23:30 UTC. The KaSACR Dze is approximately 1 dB at 18 and 21 UTC, while the KAZR Dze is around 7 dB, suggesting calibration offsets of around 1 dB for KaSACR and 7 dB for KAZR. Both KaSACR and KAZR Ze are further biased lower by an additional 13 dB when the rain rate reaches approximately 5 mm hr^{-1} around 23:30 UTC. This 13 dB reduction in KAZR and KaSACR estimates is significantly larger than the expected two-way attenuation in rain at Ka-band (~2 dB, Figure 2a), suggesting that other factors, such as WRA, contribute increasingly to the observed offset in rain. Additionally, WRA for both KAZR and KaSACR likely shows similar dependence on rain rates.

The estimated Ze from VDISQUANTS during the entire TRACER campaign are plotted as a function of R in Fig. 3. The estimated Ze for both X- and Ka-bands exhibits a log-linear relationship with R. When R exceeds 2 mm hr^{-1}, the Ze values begin to diverge, and the difference between the two wavelengths increases as R rises, likely due to resonance effects associated with non-Rayleigh scattering (Baldini et al., 2012). The Z-R relation is fitted in black line with $Z = 200R^{1.4}$, which is slightly smaller than the WSR-88D Z-R relation in convective summer deep convection ($Z = 300R^{1.4}$, Crosson, 1996). The cumulative probability distribution (CDF) of rain rates (red line in Figure 3) shows that about 15% of disdrometer samples have $R < 0.1$ mm hr^{-1},

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315 indicating limited data for traditional direct disdrometer comparison at precipitation onset.
316 However, approximately 85% of TRACER data samples have $R < 5$ mm hr^{-1}, suggesting that this
317 large range of data sample is suitable for the WRA technique applications discussed in the
318 following sections.

319 3.2 Identification of WRA: KaSACR/XSACR in its Scanning-VPT Mode
320
321 To further illustrate the WRA, we compared radar and disdrometer measurements while
322 the KaSACR/XSACR operated in its nominal 10-minute scanning sequence during a stratiform
323 rain event observed on 11 August 2022, between 01-04 UTC (Fig. 4). The radars were exposed to
324 persistent rainfall, ranging from 1 mm hr^{-1} at 01 UTC to over 5 mm hr^{-1} around 02:15 UTC, leading
325 to strong radar signal attenuation, particularly visible in the KAZR Ze vertical gradient above 4
326 km (Fig. 4a). After 03 UTC, the surface rain intensity was so low that the disdrometer could not
327 effectively measure rain drop size distributions (DSDs) for Ze estimates due to insufficient drop
328 counts (<20 drops/minute) (Fig. 4b).
329 The disdrometer-estimated surface Ze at Ka- (black diamonds) and X-bands (blue
330 diamonds) in Fig. 4c consistently show values close to 30 dBZ when rain rates are near 1 mm hr^{-1},
331 while the KAZR Ze is around 15 dBZ, resulting in a Dze of 15 dB against the disdrometer, as
332 shown in Fig. 4d. During this event, there is an 8-minute gap in every 2 minutes of VPT
333 measurements due to the PPI and HSRHI scans. The collocation of the 2-minute VPT data is
334 extended to a 6-minute window by averaging KaSACR/XSACR and VDISQUANTS data over a
335 ±2-minute interval.
336 The KaSACR Ze values (red crosses) in Fig. 4c display a sawtooth pattern within each 10-
337 minute scanning cycle. Each cycle begins with Ze values close to the XSACR Ze, followed by a
338 decline towards the KAZR Ze value as time progresses, with the scaling possibly related to the
339 rain rate. In contrast, the 03-04 September 2022 case in Fig. 2b shows parallel Ze trends between
340 the KAZR and KaSACR. The increasing Dze trend in each 6-minute period (red crosses) in Fig.
341 4d is more pronounced, indicating that the sawtooth behavior in KaSACR Ze and Dze results from
342 rainwater accumulation on the radome during the 2 minutes of vertical pointing. If the KaSACR
343 signal were saturating, it would consistently remain saturated rather than fluctuating. A closer
344 examination of XSACR Ze and Dze trends (black crosses) in Fig. 4c and d reveals minimal

variability with rain rates across the scanning cycle, likely due to the weaker water absorption coefficient at X-band and the reduced water accumulation on the conical XSACR radome.

The differing KaSACR patterns between the events in Figures 2 and 4 are associated with rainwater accumulation and the KaSACR/XSACR radar's cycling between scanning and stationary VPT modes. At the start of each scanning VPT period, the radome is covered by a relatively thin film of rainwater, having shed water during the RHI and PPI scans. In VPT mode, excess rainwater rapidly accumulates on the radome, causing increased attenuation. Consequently, WRA for the KaSACR is modulated by the 10-minute scanning cycle. By contrast, during the continuous stationary VPT observations of KAZR and KaSACR on 03-04 September, rainwater accumulated steadily on their radomes, resulting in similar WRA patterns, and the measured Ze and Dze were parallel with a consistent offset of approximately 7 dB.

3.3 WRA Fitting Calibration Technique

In this section, we examine the WRA behavior toward developing a relative calibration technique for cloud radar monitoring. Figure 5a shows the estimated Ze by KaSACR at 500 m (black cross) after gaseous and rain attenuation corrections and the corresponding VDISQUANTS-estimated Ze (red cross) as a function of R for the 03-04 September case. A very well-correlated monotonic relationship between the VDISQUANTS-estimated Ze and R in logarithmic space is observed. However, the KaSACR-measured Ze is biased low relative to the estimated Ze, and the offset ($D_{ze} = Ze_{\mathrm{dis}} - Ze_{\mathrm{meas}}$ shown in Fig. 5b) with increasing R. The *Dze* approaches 0 dB at R < 0.1 mm hr $^{-1}$, when minimal WRA is expected due to the limited water on the radome. However, *Dze* increases up to 15 dB at R ~ 5 mm hr^{-1}, which is potentially a disadvantage when considering cloud radar observations in precipitation. However, this characteristic range of WRA relative to R provides an opportunity for exploring relative radar calibration techniques.

Given a quasi-linear correlation between *Dze* and R in logarithmic space in Fig. 5b, a weighted linear least-squares fit of the *Dze* with R in logarithm can be applied, as described in Equation 2:

$$D_{ze} = a + b\log(R) \quad (2)$$

For the cases shown in Fig. 5b, the fitted slope b is estimated to be 8.6. The intercept "a" captures the radar calibration offset and the WRA when R is 1 mm hr^{-1}. Given the KaSACR calibration

offset is close to 0, the intercept primarily reflects WRA at this rain rate, yielding an intercept of approximately 11.1 dB.

This log-linear relation between *Dze* and *R* is different from the $R^{1/3}$ dependence described by Gibble's formula (Eq.1), which is applied by Frasier et al. (2013) and Gorgucci et al. (2013) in X-band radar calibrations. Since the water absorption coefficient at Ka-band is approximately three times that at X-band, we divide the result of Eq. 2 by 3 and compare it with the fitting relations from Frasier et al. (2013, solid blue line) and Gorgucci et al. (2013, solid black line) in Figure 6. It is important to note that the X-band radars used in the studies by Frasier et al. (2013) and Gorgucci et al. (2013) were equipped with spherical radomes, whereas the ARM KAZR and KaSACR radars used flat inclined radomes. Despite these differences, the relationship derived in this study intersects with those of Frasier et al. (2013) and Gorgucci et al. (2013) at R=0.2 mm hr^{-1}, aligning with the majority of our data. When R > 0.2 mm hr^{-1}, our WRA fitting results exceed those of Gorgucci et al. (2013) by less than 0.5 dB, although Gorgucci et al.'s relation is 0.5-1 dB higher than that of Frasier et al. (2013). When R < 0.2 mm hr^{-1}, our WRA fitting result is 0.5-1 dB lower than both previous studies. The observed differences (within 1 dB) are smaller than the data scatter in Fig. 5b (standard deviation of 3 dB) and the discrepancies between the two previous studies, suggesting that the log-linear fitting in Eq. 2 is suitable for WRA correction when R is below 5 mm hr^{-1}, the selected threshold for our analysis. The calibration offset calculation associated with the WRA fitting functions will be further examined in Section 4.

Assuming that radar calibration offsets are independent of R, and that WRA depends intrinsically on R, the radar calibration offset can be determined by monitoring the fitted intercept in Eq. 2. Figure 5e shows the fitted intercept of *Dze* of KAZR is 18.5 dB, about 7.5 dB higher than that of KaSACR, which is consistent with the observed offset between KaSACR and KAZR in Figure 1d and the time series in Figure 2c. Alternatively, we can also assume negligible WRA at very low rain rates, e.g., R = 0.05 mm hr^{-1}, making *Dze* (R = 0.05) a reliable measure of the radar calibration offset (C) for monitoring radar performance. For the KaSACR on 03-04 September case (Fig. 5a), the *Dze* (R= 0.05) is -0.1 dB, while for the KAZR, it is 7.3 dB, consistent with direct comparisons between KaSACR, KAZR, and VDISQUANTS. This finding suggests that the WRA technique provides robust offset estimates for this case. The corrected Ze values using the log-linear fitted *Dze* in Eq. 2 are compared with VDISQUANTS Ze in Fig. 5c and 5f for KaSACR and

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KAZR, respectively. The correlation coefficient (rr) improves to ~0.9, with a mean bias of 0 dB and a standard deviation of 3.0 dB for both KaSACR and KAZR.

To further explore the intrinsic WRA dependence on *R,* we applied the WRA log-linear fitting calibration technique to KaSACR in its scanning-VPT modes. Due to water shedding during the scanning cycle, we used the last-minute measurement of each 2-minute VPT period within the 10-minute scanning cycle. To obtain a range of samples, we identified five stratiform rain days—May 25, August 5, 11, 19, and 29—and combined data from these events. The data collected from those five days are plotted along with the corresponding VDISQUANTS-estimated Ze (red cross) as a function of rain rates in Fig. 5g. For these events, $Dze_{(R=0.05)}$ is -0.9 dB, with slope "b" fitted to 8.6. The corrected Ze using this log-linear fitted *Dze* is compared with the VDISQUANTS Ze in Fig. 7i, demonstrating a strong correlation with the reference Ze, along with a smaller standard deviation (rr=0.91; mean bias, 0 dB; and standard deviation, 2.0 dB).

Recall the $Dze_{(R=0.05)}$ of -0.1 dB for stationary VPT mode in 03-04 September case, the difference between the two KaSACR offsets is less than 1 dB, which is well within the standard deviation of the estimated Ze (3 dB) as a function of *R*, and aligns closely with the 1 dB offset from the direct disdrometer comparison at light rain onset in Fig. 2. This suggests that the *R* dependence of WRA is a valid assumption, therefore the interceptor or $Dze_{(R=0.05)}$ in the fitting of Eq. 2 can be a useful metric for radar offset monitoring.

The time and height plots of Ze from KaSACR, XSACR, and KAZR GE and MD modes on 03-04 September 2022 (after the WRA correction is applied) are shown in Figure 7. For the precipitating period, KaSACR is adjusted with Eq. 2 with a slope of 8.6 and constant of 11.1 (Table 2 or Fig. 5b). XSACR is modified with the offset of 3 dB from VDISQUANTS (black cross in Fig 2d), and KAZR GE mode is corrected using Eq. 2 with a slope of 8.6 and an intercept of 18.5 (Table 2, or Fig. 5b). For non-precipitating periods, the calibration offsets for KaSACR and XSACR are assumed to be 0 dB based on the previous discussion, while the KAZR GE mode is calibrated with an offset of 7 dB. In contrast to the apparent difference of more than 5 dB between KAZR and KaSACR shown in Figure 1, the corrected Ze values from KAZR and KaSACR are comparable to those from XSACR in cloud and light rain conditions. Under the relatively heavy rain conditions (e.g., 2330 UTC), XSACR Ze along the fall streaks maintains magnitudes near 30 dBZ from the surface up to the melting layer, while Ze estimates from KAZR and KaSACR

gradually decrease from the surface to the melting layer, likely due to increasing attenuation in Ka-band observations. This comparison in Figure 7 further supports the applicability of the WRA fitting technique to KAZR measurements and KaSACR in VPT modes, providing reasonable estimates for wet-radome corrections during precipitation and radar offset monitoring.

4 Application and Evaluation of the WRA Offset Monitoring During TRACER

4.1 Daily TRACER KAZR Calibration Offset Applications

We apply the WRA fitting technique on the *Dze* and *R* relationship using VDISQUANTS Ze estimates versus KAZR Ze for each day with measured precipitation throughout TRACER campaign. The fitted slopes from the daily events typically range from 6 to 10, with *rr* generally exceeding 0.7. The fitted slopes and associated fitting errors depend on the distribution of data samples. For example, in rain events with short durations or limited variability in intensity, data samples may cluster within a narrower range, resulting a relatively lower correlation coefficient between the fitted Ze and disdrometer Ze, potentially indicating less reliable results.

To mitigate uncertainty associated with "daily" fitting as above, one may assume that the *Dze* and *R* relation has a constant slope over longer windows. In this study we consider applying the WRA fitting technique with an average slope of 8, selected as a representative value for extended rain conditions across the entire TRACER campaign dataset. As a sensitivity study of this composite slope, we conduct offset calculations with proxy slope values at 6, 8 and 10 for both KAZR and KaSACR in the 03-04 September 2022 case. Table 2 presents the results of these tests. As the slopes increase from 6 to 10, the calibration offsets for both KAZR and KaSACR decrease by approximately 3 dB, as expected. With increasing slope values, the least-squares fit prioritizes the data samples around 0.1 - 1 mm hr^{-1}, resulting in a mathematical decrease in C.

To further illustrate, we applied the WRA fitting with a slope of 6 to the KaSACR observations in Figure 5a. The fitted relation is represented by the red dashed line in Figure 6. It can be seen that the fitted Ze with a slope of 6 lies between the results from Frasier et al. (2013) and Gorgucci et al. (2013). For most data samples (concentrated around 0.1 - 1 mm hr^{-1}), the difference between the two WRA fitting results remains within 1 dB. The resulting C with slope of 6 is larger than that with a slope of 8. However, the offset deviation due to possible fitting slope fitting changes (shown in Table 2) is 3 dB, which is within the standard deviation of the estimated

Ze as a function of R (~3 dB). Therefore, even with fitting slope errors associated with this relative WRA technique, drifts larger than the 3 dB in the long-term calibration trend would be meaningful and identifiable.

The calculated KAZR calibration offsets during the entire TRACER campaign are shown in Fig. 8a (black asterisk for the daily value, thin dash line representing the mean campaign-wide trend). The calibration offsets remain relatively stable around 2 dB, with a standard deviation of 3 dB until 1 July 2022 (273 days since 1 Oct. 2021 in Fig. 8). After this date, the calibration offset increases to around 7 dB in September. This shift is larger than the uncertainty of the fitting method and the standard deviation of the fitting data, which is found to be linked to a drop of about 1 dB in transmitter power toward the end of the project in TRACER radar b1 data processing (Feng et al., 2024) and in Figure 9c.

4.2 Evaluation of the TRACER KAZR Calibration Trend

By monitoring the $Dze_{(R=0.05)}$ from each rainy day that meets our stratiform and duration selection criteria, we determine a relative radar calibration offset trend. This offset includes additional uncertainty due to fitting uncertainty and the assumption of negligible WRA at $R \sim 0.05$ mm hr^{-1}. Combining this WRA fitting technique with other, typically less frequent, absolute radar calibration references would be ideal and cost-effective for KAZR long-term calibration. To evaluate the KAZR calibration offset trend over the entire TRACER campaign, we performed three separate tests to demonstrate the potential offset uncertainty and/or advantages of the current WRA fitting technique compared to other established methods.

4.2.1 Direct KAZR-Disdrometer Comparison Near to Light Rain Onset

As previously noted, a wet radome film may not form immediately at the onset of light rain, so WRA is often assumed to be negligible when calibrating radar using disdrometer measurements near these rain onset windows. We perform a direct KAZR-disdrometer comparison at or near light rain onset for qualifying KAZR calibration events. The onset mean offset for each day is calculated if there are data samples with $R < 0.1$ mm hr^{-1} lasting for 5 consecutive minutes within each observed rain event. The onset mean offsets are shown in Fig. 8a (red diamonds). For days with an onset mean offset, these values are typically close to those calculated using the WRA

fitting technique. However, this method's applicability depends on the variation in precipitation rate over the 5-minute sampling period and the minimum sensitivity of VDISQUANTS. The former introduces large uncertainty, while the latter limits the number of data samples, as shown in Fig. 8a.

4.2.2 WRA Fitting Technique Against the Calibrated RWP Ze

As an independent cross-comparison, we also apply the WRA fitting technique with respect to calibrated RWP Ze at RWP time resolution (less than 8 seconds), using interpolated disdrometer rain rates over the entire TRACER campaign. Here, *Dze* is replaced by the difference between KAZR and RWP measurements. The WRA calibration offsets using RWP measurements are shown with black asterisks in Fig. 8b. First, we observe fewer available RWP data points, due to RWP mode switching during transient rain events. For days with available RWP measurements, the calibration offsets closely align with those derived using disdrometer-estimated Ze in Fig. 8a and direct disdrometer comparisons. The offset trend drift from early July to September is smoother and more clearly defined than the trend observed with disdrometer measurements, likely due to better temporal resolution. Overall, the consistency in temporal trend and magnitude of calibration offsets between disdrometer and RWP measurements indicates strong performance of the new WRA fitting technique.

4.2.3 Cross-Comparison Between KaSACR and KAZR

As previously mentioned, KaSACR calibration offsets remained stable between May and September 2022. Furthermore, its calibration offsets, calculated from the WRA fitting technique with scanning VPT and stationary VPT measurements in Fig. 6, are approximately -0.9 to -0.1 dB, respectively, and around 1 dB from direct disdrometer comparison at light rain onset. We tentatively assign a calibration offset of 0 dB for KaSACR observations. Cross-comparison between KaSACR VPT mode and KAZR observations can then be used to quantify the KAZR calibration offset trend. Since KaSACR and KAZR operate at the same frequency, this cross-comparison uses full-profile samples rather than measurements at a specific height level, as cumulative gaseous and rain attenuation should be consistent across range gates.

For this cross-comparison, we first match the closest KaSACR profiles to KAZR profiles and interpolate KaSACR height ranges to align with KAZR height ranges. We then select data

samples using a signal-to-noise ratio threshold of 5 dB for both KaSACR and KAZR. In precipitating events, KaSACR in scanning VPT mode is expected to exhibit a sawtooth or modulated WRA cycling behavior, while KAZR VPT operates under consistent/continuous WRA (see Fig. 2). We categorize the collocated profiles into precipitating and non-precipitating periods using collocated surface rain rates from disdrometer measurements. Finally, the daily mean offsets between KaSACR and KAZR observations in non-precipitating clouds are calculated and shown in Fig. 8b (red diamonds). These calculated offsets display a trend similar to that observed from the WRA fitting technique against RWP measurements in Fig. 8b, further supporting the validity of the WRA calibration offset behaviors and strengthening confidence in the offset drift observed at the end of the campaign.

To extend the method to different disdrometer setups, we applied the WRA fitting technique to LDQUANTS estimates. Additionally, we tested sensitivity to fitting functions of log-linear and $R^{1/3}$ dependencies to account for potential discrepancies. Figures 9a and 9b present the results with a 2-day running average. The daily calibration offsets show slight variations between LDQUANTS and VDISQUANTS, indicating minor differences in disdrometer measurements (Wang et al. 2021). While the calibration offsets from the log-linear and $R^{1/3}$ fittings can differ by up to 2 dB for certain day, the overall trends remain similar, with a mean offset of approximately 2 dB before July 2022, increasing to around 7 dB afterward. The increase of calibration offsets is well correlated with the noticeable decrease of transmitted power (Figure 9c) observed at the end of the project.

5 Summary

In this study, we have demonstrated the wet radome influence on Ka-band radar observations through comparisons that included KaSACR VPT observations under scanning (that may shed water buildup) and stationary (non-shedding) conditions. The WRA is attributed to both wet film and cumulative rainwater collecting on the radar radome. This attenuation influence increases, as the rain rate increases. In campaign settings, it was found this attenuation may exceed 10 dB under a modest rain rate of 5 mm hr $^{-1}$. Taking advantage of the intrinsic WRA dependence on rain rates as obtained in moderate rain events from the AMF1 deployment in Houston, TX

563 during the TRACER field campaign, a new relative calibration monitoring technique was
564 developed for use with the ARM KAZR (or similar cloud radar systems) observations.
565 The well-correlated relation between *Dze* and *R* (in logarithmic space) on precipitating
566 days is fitted with a log-linear equation. This rain dependence of WRA serves as the basis for this
567 relative WRA calibration technique. The corrected KAZR Ze with fitted *Dze,* which includes the
568 WRA and Ze offset, agrees very well with both disdrometer-estimated and RWP-measured Ze.
569 The radar calibration offset is calculated from the fitted *Dze -R* relation when *R* equals 0.05 mm
570 hr^{-1}, assuming WRA is negligible at this light rain rate. The daily fitted slopes over the course of
571 the TRACER campaign vary between 6 and 10 due to different data sampling in different rain
572 types. A slope sensitivity study suggests that the calibration offset deviations due to slope variation
573 are likely within the standard deviation of the estimated Ze as function of *R*, as well as those typical
574 of underlying/collocated disdrometer measurement uncertainty (i.e. ~2-3 dB). The KAZR
575 calibration offsets calculated with a constant slope of 8 during the TRACER campaign are stable
576 near 2 dB compared to the disdrometer estimate with a standard deviation of 3 dB through June
577 2022. After that time, the calibration offsets increase to more than 7 dB.
578 The performance of the WRA fitting calibration technique is evaluated by comparing it
579 with direct disdrometer measurements at the onset of rain events. The wet-radome technique
580 consistently identifies a sound calibration offset over the entire project and arguably outperforms
581 the direct disdrometer and radar comparison at the onset of light rain by reducing noise and
582 increasing temporal consistency. The WRA fitting calibration technique is also applied to the
583 KAZR observation against the calibrated RWP Ze reference. This test reveals sound performance
584 and a clear and smooth matching trend in the July to September change in TRACER KAZR offsets,
585 indicating that the new technique can be applicable to other calibrated reference radars with
586 collocated surface rain rate measurements. The KAZR offset assessed from the cross-comparison
587 between the stable and calibrated KaSACR VPT mode and KAZR observations in non-
588 precipitating clouds also agree with the calibration offset trend from the WRA fitting technique.
589 The daily calibration offsets vary due to the uncertainty of disdrometer measurements and the
590 fitting function of WRA, however the generally long-term trend from the WRA fitting technique
591 seems robust.
592

Determining the calibration offset and monitoring the long-term trend of ARM KAZR is the first step towards studying cloud seasonal and inter-seasonal variation. Having an easily adjustable cloud radar calibration method with collocated disdrometer or RWP data available will also facilitate cloud microphysical property retrieval, cloud process studies, and cloud variation associated with climate change using ARM KAZR measurements. This technique has the advantage of utilizing data from a broader range of light and moderate rain cases, avoiding the stringent requirements of other shorter-wavelength radar monitoring methods, which often rely on disdrometers or other radars and require observations of cloud, drizzle, or light rain at the onset of precipitation. Future plans include testing this newly developed WRA technique at other ARM fixed sites (e.g., in more humid, marine, or oceanic environments) to assess the extent of any necessary site-specific refinements for different radars and sampling conditions, acknowledging that wet-radome attenuation is inherently dependent on both the radome and radar characteristics. Recently, this WRA monitoring technique has been applied to data from other ARM field campaigns, such as the Surface Atmosphere Integrated Field Laboratory (SAIL) and the Eastern Pacific Cloud Aerosol Precipitation Experiment (EPCAPE). Alongside TRACER, the offset trends derived from these three campaigns have shown favorable agreement with results from other independent KAZR calibration techniques documented in ARM radar b1 data processing reports (Feng et al., 2024; Matthew et al., 2024; Rocque et al., 2024).

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Table 1. List of parameters for KAZR GE mode, KaSACR/XSACR in vertical pointing (VPT) mode, and RWP in precipitation mode.

	KAZR (GE mode)	KaSACR (VPT mode)	XSACR (VPT mode)	RWP (Precipitation mode)
Frequency (GHz)	34.0	35.3	9.71	1.29
Wavelength	8.57mm	8.50mm	3.09cm	23.3cm
Beam width (degree)	0.3	0.3	1.0	>3
Time resolution (s)	2	4	3	5-8
Range resolution (m)	30	25	25	225
Minimum range (m)	160	Others: 428 0903/04: 453	288	335
Radome diameter (m)	1.82	1.82	1.82	N/A

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Table 2. Sensitivity study of the slope value in the log-linear fitting for KAZR and KaSACR calibration on 03-04 September 2022 case in Figure 1. *b* and *a* are the slope and constant, respectively, in the log-linear fitting in Eq. 2. $D_{Ze}(R=0.05)$ is the radar calibration offset when rain rate (R) equals 0.05 mm hr $^{-1}$. More details can be found in Section 3.3.

	KAZR				KaSACR			
b	*a*	D_{Ze} (R=0.05)	Correlation coefficient (rr)	Standard deviation (dB)	*a*	D_{Ze} (R=0.05)	Correlation coefficient (rr)	Standard deviation (dB)
6	17.1	9.3	0.88	3.8	9.8	2.0	0.89	3.4
8	18.1	7.7	0.90	3.9	10.9	0.5	0.91	3.4
8.6	18.5	7.3	0.91	4.1	11.1	-0.1	0.92	3.5
10	19.1	6.3	0.92	4.4	12.0	-1.0	0.93	3.7

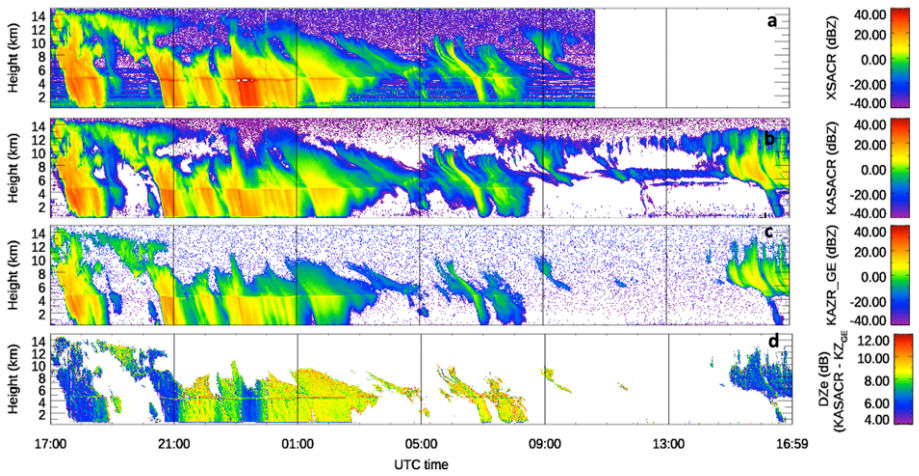

Figure 1. Measured radar reflectivity on 03-04 September 2022 from the TRACER field campaign. a) XSACR, missing data after 10:40 UTC on 04 September 2022, b) KaSACR, c) KAZR GE mode, d) Ze difference (DZe) between the KaSACR and the KAZR GE mode.

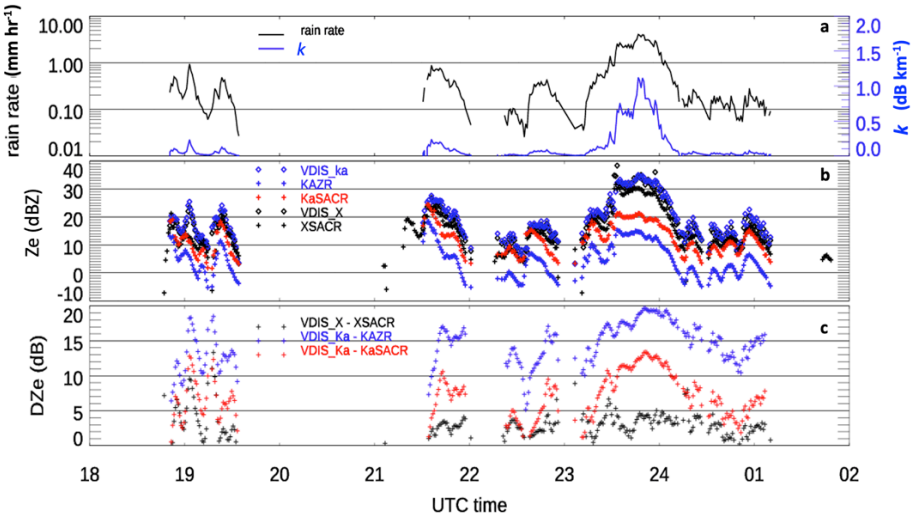

Figure 2. Measurements and comparison on 03-04 September 2022 between VDISQUANTS and radars. a) the timeseries of VDISQUANTS rain rate (black line) and rain droplet specific attenuation coefficients (*K*, blue line) at Ka band. b) the time series of measured Ze from KAZR GE (blue +), KaSACR (red +), and XSACR (black +) at 500 m after gaseous and rain attenuation corrections, and estimated Ze from VDISQUANTS at Ka (blue diamond) and X (black diamond) bands. c) Ze difference (DZe) between radar and disdrometer for XSACR (black cross), KaSACR (read cross), and KAZR (blue cross). For this case, SACR was operated in the stationary VPT mode.

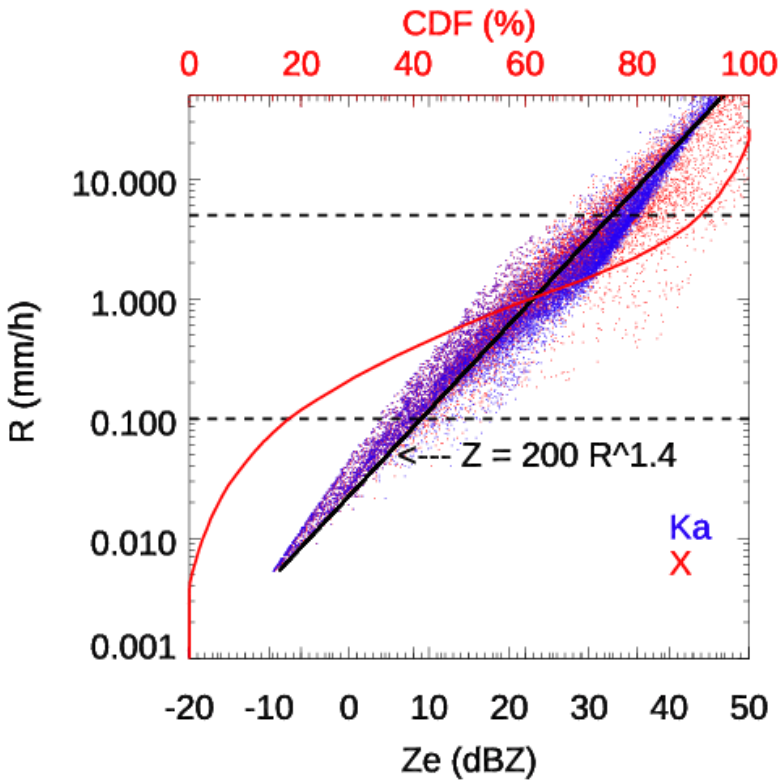

Figure 3. The estimated Ze from VDISQUANTS for Ka (red dots) and X bands (black dots) during the entire TRACER campaign, plotted as a function of rain rate (R). The red line is the cumulative probability function (CDF) of R. The two vertical black lines are at rain rates of 0.1 and 5.0 mm hr^{-1}, respectively. The Z-R relation is fitted in black line with $Z = 200R^{1.4}$, which is slightly smaller than the WSR-88D Z-R relation in convective summer deep convection ($Z = 300R^{1.4}$, Crosson, 1996)

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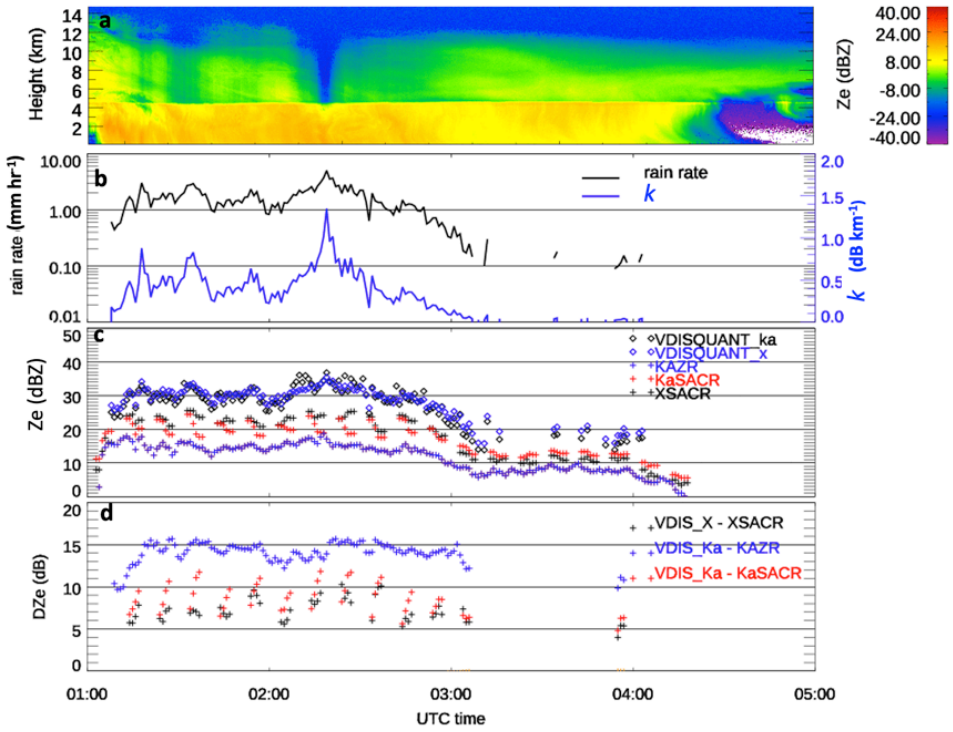

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718 Figure 4. Radar and VDISQUANTS comparison for the case on August 11. a) Measured radar
719 reflectivity (Ze) from the KAZR GE mode. b-d are similar to Fig. 2a-c. For this case, KaSACR
720 and XSACR measurements are the scanning VPT mode and collocated with the VDISQUANTS
721 with a ±2 minutes averaging window.

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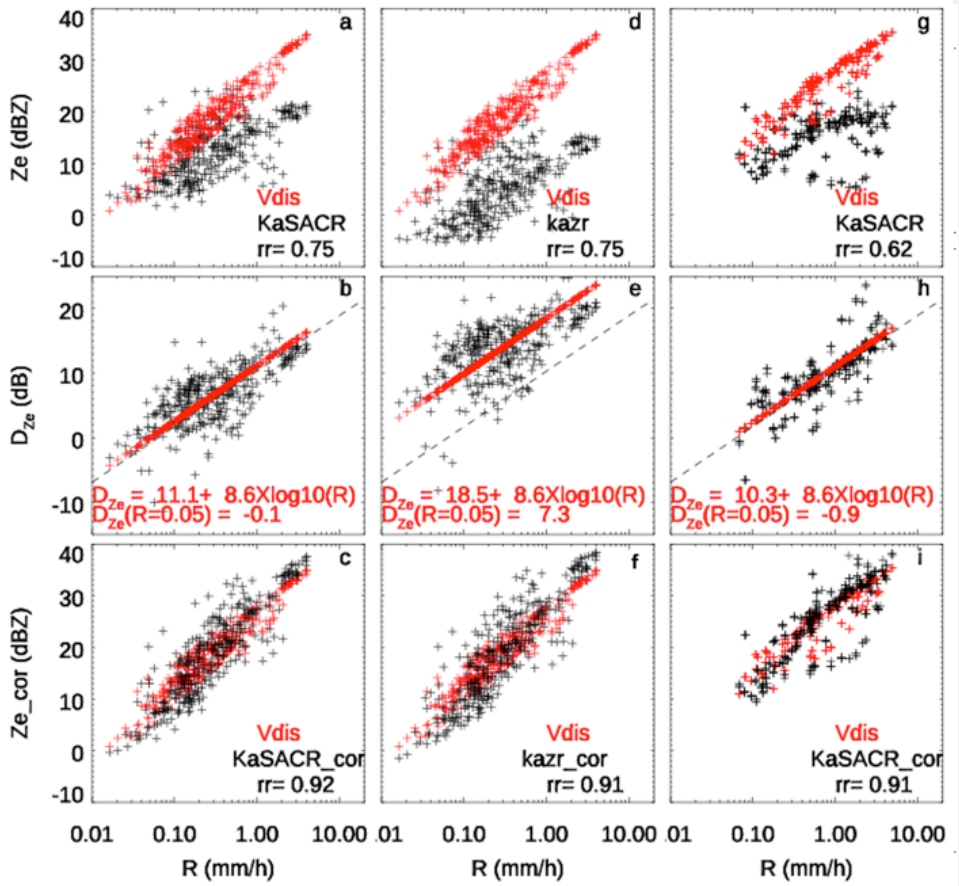

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724 Figure 5. a) Scatter plot of radar measured Ze (black cross) at 500 m and VDISQUANTS-estimated
725 Ze (red cross) as a function of rain rate *R,* b) Difference between measured Ze and VDISQUANTS-
726 estimated Ze (Dze in black). The log-linear fitting in Eq. 2 with slope *b* at 8.6 are plotted in red
727 cross, c) Scatter plot of radar measured Ze (black cross) after log-linear fitting correction along
728 with the VDISQUANTS-estimated Ze (red cross) for KaSACR stationary VPT (a-c) and KAZR
729 GE (d-f) on 03-04 September, and KaSACR stationary VPT (g-i) collected on May 25, August 05,
730 11, 19 and 29. The correlation coefficients between the measured Ze and estimated Ze (rr) before
731 and after the fitting correction are noted. The dashed black lines in second row (b, e, h) are the log-
732 linear fitting with a= 10.3 and b= 8.6 for KaSACR in Table 2.

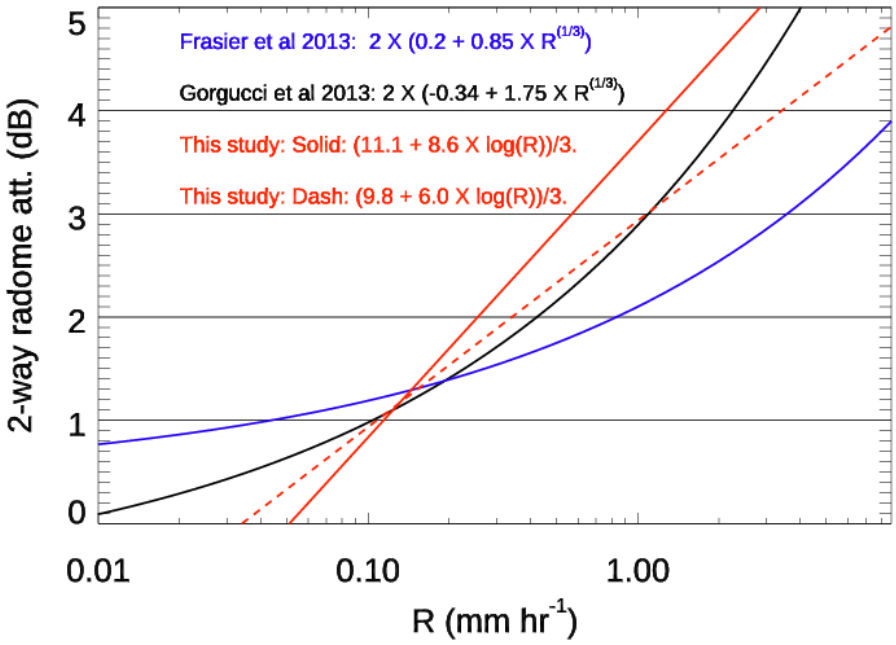

Figure 6. Two-way radome attenuation as a function of rain rate (R) using the log-linear WRA fitting relation in Eq. 2 with slopes of 8.6 (solid red) and 6.0 (dashed red) in this study at Ka-band, which is divided by 3 and compared with two previous studies about X-band radars from Frasier et al. 2013 and Gorgucci et al. 2013.

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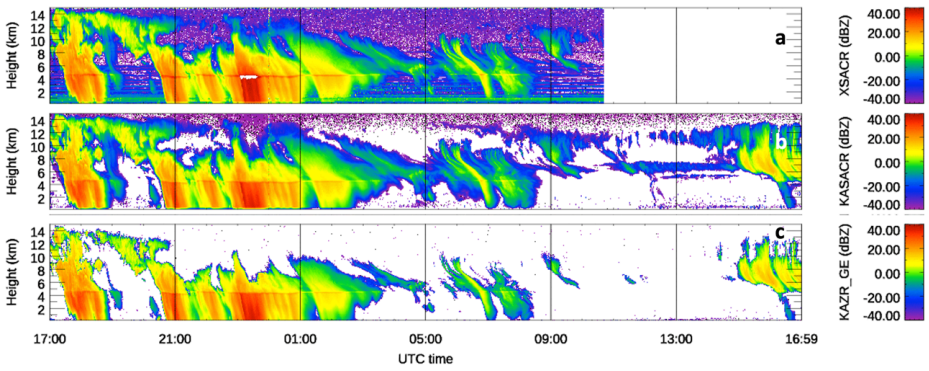

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749 Figure 7. The same as Figure 1a-c except after WRA correction and radar calibration. For the
750 precipitating period, KaSACR is corrected using Eq. 2, with a slope of 8.6 and constant of 11.1.
751 XSACR is corrected with the offset of 3 dB from VDISQUANTS (black cross in Fig 2d), and
752 KAZR GE mode is corrected using Eq. 2, with a slope of 8.6 and constant of 18.5. For non-
753 precipitating periods, the calibration offsets of KaSACR and XSACR are assumed to be 0 dB,
754 while the KAZR GE mode is calibrated with offset of 7 dB.

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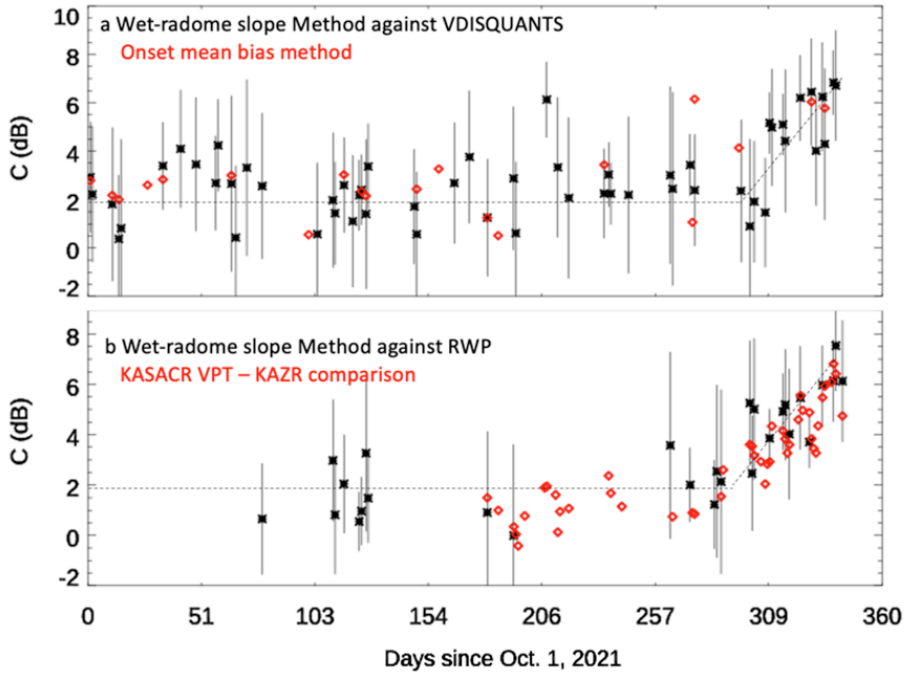
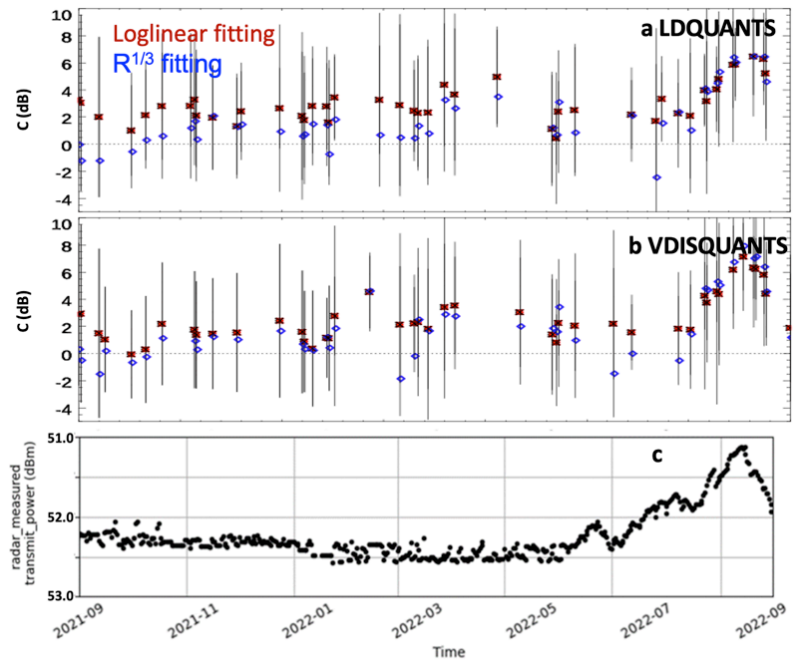


Figure 8. a) KAZR daily calibration offsets (*C*) from the mean KAZR bias method at the onset of light rain (red diamond) and the WRA fitting technique (black asterisk) against the VDISQUANTS data. Black vertical bar is the standard deviation of corrected Ze against the estimated Ze. b) KAZR daily calibration offset from the WRA fitting technique against the calibrated RWP measurement in black asterisk with vertical standard deviation bar. Red diamonds stand for the daily cross-comparison between the KaSACR VPT mode and the KAZR GE mode in non-precipitating clouds since May 26, 2022. The dashed black line is the mean trend outline from the WRA fitting technique in Fig. 8a.



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772 Figure 9 KAZR daily calibration offsets (*C*) from log-linear fitting with Eq. 2 (red asterisk with
773 black standard deviation bar) or the $R^{1/3}$ relation (blue diamond) against a) LDQUANTS and b)
774 VDISQUANTS data. The daily offsets are smoothed with 2-day window. c) KAZR transmitted
775 power. Noticeable decrease of transmitted power is well correlated with the increase of calibration
776 offset.

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Data availability

The KAZR, KaSACR and XSACR data at the TRACER campaign in this study are a1-level data. The surface disdrometer VDISQUANTS and interpolated sounding data are c1-level value added product data. They are all available at ARM data discovery at https://adc.arm.gov/discovery/#/ and through the following DOIs. The calibrated radar wind profiler data is ARM PI product and can be obtained from the data developer, Dr. Christopher R. Williams, through email (christopher.williams@colorado.edu) contact.

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Author contribution

MD developed the main concept for the WRA calibration technique and led the manuscript preparation. SG, MJ, and KJ contributed to the data analysis process. CW provided the calibrated RWP data and contributed to its analysis and write-up. JC, YF, AM, MR, and MD, as part of the ARM radar data mentor team, provided TRACER-related radar information and additional KAZR calibration used in TRACER b1 data processing. IL and TW, as ARM radar engineers, supplied critical information on radar hardware, software, and radar saturation. AZ and DW contributed as the disdrometer mentors and VAP developers. ZZ and EL provided valuable insights regarding radar wet radome attenuation. All coauthors helped to edit and comment the manuscript draft.

Competing interests

The authors declare that they have no conflict of interest.

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