

Separating the albedo reducing effect of different light absorbing particles on snow using deep learning

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Abstract. Several different types of light absorbing particles (LAPs) darken snow surfaces, enhancing snow melt on glaciers and snowfields. LAPs are often present as a mixture of biotic and abiotic components at the snow surface, yet methods to separate their respective abundance and albedo-reducing effects are lacking. Here, we present a new optimisation method enabling the retrievals of dust, black carbon and red algal abundances as well as their respective darkening effects from spectral albedo. This method includes a deep learning emulator of a radiative transfer model (RTM), and an inversion algorithm. The emulator alone can be used as a fast and lightweight alternative to the full RTM with the possibility to add new features, such as new light absorbing particles. The inversion method was applied to 180 ground field spectra collected on snowfields in Southern Norway, with a mean absolute error on spectral albedo of 0.0056, and surface parameters that closely matched expectations from qualitative assessments of the surface. The emulator predictions of surface parameters were used to quantify the albedo reducing effect of algal blooms, mineral dusts and dark particles represented by black carbon. Among these 180 surfaces, the albedo reduction due to light absorbing particles was highly variable and reached up to 0.13, 0.21 and 0.25 for red algal blooms, mineral dusts and dark particles respectively. In addition, the effect of a single LAP was attenuated by the presence of other LAPs by up to 2-3 times. These results demonstrate the importance of considering the individual types of light absorbing particles and their concomitant interactions for forecasting snow albedo.

1 Introduction

Snow albedo is a key component of the Earth's radiation budget, and therefore it is important to both understand and model the drivers of snow albedo variability to project future snow melt and climate (Flanner et al., 2011). In particular, the darkening effect of light absorbing particles (LAPs) constitutes a major source of uncertainty for snow albedo in regional and global climate models (Skiles et al., 2018; Dumont and Tuzet, 2022). This uncertainty is notably due to the variability in the apparent optical properties of LAPs, which determine their impact on surface albedo. The apparent optical properties depend on microscopic and macroscopic parameters such as the size distribution, shape and refractive index of the particles, the mixing state

of the particles with the snow grains, the distribution and abundance of the particles in the snowpack, the shape and size of the snow grains, the surface roughness, the snowpack depth and illumination conditions (Flanner et al., 2021; He, 2022). It is clearly challenging to both measure all these parameters in the field and to constrain all of these parameters in models. Hence, 25 uncertainties in field measurements and model parameterisations are propagated in forward modelling experiments aiming at quantify LAPs impact on snow surface albedo.

By contrast, inverse modelling approaches consider the impact of LAPs in snow directly from their measured apparent optical properties instead of prescribing all the above parameters, circumventing some of the uncertainty associated with forward modelling experiments. In addition, inverse methods offer a remote-only approach to detecting and quantifying LAPs in hard- 30 to-access areas and/or over spatial scales that are too large to cover on foot. They are hence particularly relevant in the context of ongoing (e.g. PRISMA, EnMAP) and emerging (e.g., SBG) satellite missions providing remotely sensed reflectance imagery at high spectral resolution. Inverse methods using physically based models have been developed to retrieve the abundance and impact of LAPs using look-up tables (e.g. Donahue et al., 2023; Chevrollier et al., 2023) or simplified analytical formulas (e.g. Dumont et al., 2017; Kokhanovsky et al., 2021), but these methods are limited in the number of parameters that can be 35 accounted for. They therefore focus on a single LAP type, or merge all LAPs together. In particular, methods using look-up tables are advantageous in that they compare observations with model outputs directly, but the size of look-up tables grows exponentially as new parameters are included and hence they are usually not adapted to discriminate between LAPs. To our knowledge, only one study has developed an inverse method to discriminate between biotic and abiotic LAPs, using optimal estimation (Bohn et al., 2021). Yet, consideration of LAPs separately is necessary because (1) each type of LAP impacts snow 40 albedo differently, (2) the impact of a given LAP depends on the presence of other LAPs (Skiles and Painter, 2018; Kaspari et al., 2014) and (3) their future presence, abundance and impact on snow surfaces depend on different processes, although feedbacks between LAPs can exist (McCutcheon et al., 2021; Harrold et al., 2018). For example, the presence of black carbon depends mainly on the burning of fossil fuels and forests (Bond et al., 2013), while the presence of dust and algae are more dependent on the climate, such as droughts, dust storms or environmental conditions sustaining microbial life (Skiles et al., 45 2018). Developing inverse methodologies discriminating between LAPs is therefore necessary to deepen our understanding of snow surfaces and the role of LAPs in future snowmelt, as well as improving and validating existing albedo models, in particular in their representation of snow algae (Flanner et al., 2021).

Here, we aim at building an efficient, robust and unbiased inversion scheme able to simultaneously retrieve red algal, mineral dust and black carbon abundances and darkening effects from spectral surface albedo. We first integrated new empirical optical 50 properties for red snow algae as well as snow liquid water content (LWC) in the radiative transfer model (RTM) BioSNICAR, then built a a deep-learning emulator of the model and an inversion algorithm utilising this emulator. We present the performance and benefits of the emulator in comparison to the original RTM, explore the robustness of the inversion algorithm, and then apply this new method to field spectra collected in Norway. Finally, we discuss the potential of the method to be upscaled to airborne imagery.

55 2 Methods

2.1 Inversion scheme

The inversion scheme is based on the open source RTM BioSNICAR version 2.1 (Cook et al., 2020), a Python translation of the SNICAR model (Flanner et al., 2021). Directly optimizing BioSNICAR would have been too computationally expensive and hence we built and used a deep learning neural network emulator of the RTM in order to improve the efficiency of the inversion, and notably 1) accelerate the forward runs used in the optimisation algorithm prior the gradient computation and 2) accelerate the gradient computation by leveraging the automatic differentiation framework of TensorFlow (Jouvet et al., 2021). A training dataset of simulations of the original RTM was first generated (section 2.1.1) and used to build the emulator (section 2.1.2), which was then coupled to an optimising algorithm (2.1.3) to invert spectral albedo for surface properties, including the darkening effect of light absorbing particles.

65 2.1.1 Radiative transfer model simulations

The RTM BioSNICAR simulates the bi-hemispherical albedo of snow and ice surfaces by solving the two-stream radiative transfer equations. The model considers the snowpack as homogeneous and plane parallel, and an infinite number of layers with varying snow grain size and shape, density and light absorbing particle concentrations can be prescribed. Several types of incident irradiance can be selected in the model, notably varying with the solar zenith angle. The capabilities and physical equations of the model are similar to the latest SNICAR version, and are detailed in Flanner et al. (2021) and Whicker et al. (2022). Here, the RTM was parametrised with two snow layers of 0.02 and 100 m with varying physical and biological properties (LAPs concentrations, snow grain size, liquid water content, and solar zenith angle), representing snow as a granular medium. Snow grains were represented by spheres as per the original formulation of the SNICAR model (Wiscombe and Warren, 1980; Flanner et al., 2021). Recent work showed that light penetration in snow is better represented using irregularly shaped grains (e.g. Robledano et al., 2023), notably yielding more accurate retrievals of snow specific surface area (SSA), but here we chose to use spherical grains mainly because 1) one objective of this study was to incorporate liquid water in snow using the validated framework of Donahue et al. (2022), which is based on spherical grains, and 2) the main focus of the study was the retrieval of light absorbing particles rather than snow physical properties, hence spherical-equivalent snow SSA were deemed appropriate. Future developments of the emulator may consider more realistic physical representations of snow such as a collection of hexagonal plates (Whicker et al., 2022), irregularly shaped grains (Picard and Libois, 2024), or a random mixture of ice and air phases characterized by their mean chords (Malinka, 2023). The upper layer contained black carbon, mineral dust and red snow algae, and the two snow layers had the snow same grain size and liquid water content. A 2 cm depth was chosen for the upper layer as this depth was used to quantify algal cells in recent field studies (Engstrom et al., 2022; Healy and Khan, 2023), hence the LAP concentrations represent 2 cm equivalents. The second layer was chosen as semi-infinite to remove the dependency of the spectral albedo on the underlying surface, hence the simulations do not represent very thin snowpacks. The illumination was set as direct beam mid-latitude summer irradiance for different solar zenith angles (SZA). The density was kept constant at 600 kg m^{-3} , because it minimally impacts the spectral albedo in comparison to the snow

grain size, which is here an effective optical grain size (Warren, 1982; Gardner and Sharp, 2010) that covers realistic ranges of snow specific surface area for melting snow (1-10 m² kg⁻¹; Dumont et al. (2017); Tuzet et al. (2020)). The parameter ranges for the simulations are given in Table 1. These ranges were not linear but rather manually designed by creating homogeneous meshes, accounting for radiative transfer non-linearity.

Table 1. Parameter ranges used in the RTM simulations for the training of the emulator

Red snow algae (cells mL ⁻¹)	Dust (ppb)	Black carbon (ppb)	Liquid water content (%)	Grain size (μm)	SZA
0-1.5 × 10 ⁵	0-2 × 10 ⁶	0-2 × 10 ³	0-15	350-3000	35-60

The liquid water content (LWC) in snow was implemented in the RTM following the methodology of Flanner et al. (2021) and Donahue et al. (2022). First, the optical properties of 5000 individual water and ice spheres with log-spaced radii ranging from 0.05 to 10000 μm were generated from water and ice refractive indices using the miepython package (Prah, 2023). The ice refractive index was the one compiled from Picard et al. (2016) and Warren and Brandt (2008) as described in Flanner et al. (2021), and the water refractive index was a compilation between the dataset at 0°C from Rowe et al. (2020) beyond 0.7 μm, and the dataset from Segelstein (1981) below 0.7 μm. Then, the optical properties of lognormally distributed water and ice spheres were computed for a given effective radius (Flanner et al., 2021), and mixed using a volume weighed average depending on the LWC (Donahue et al., 2022). For the light absorbing particles, the optical properties of black carbon (BC) and dust were directly available in the model. For BC, we used the uncoated BC optical properties from Flanner et al. (2012) and for the dust we used the optical properties of the dust mixture from Skiles et al. (2017) in the size bin 10-50 μm, which are representative of measurements from dust in snowpacks (Skiles et al., 2017; Flanner et al., 2021). For red snow algae, new empirical optical properties were integrated in the RTM. The single scattering properties of red snow algae were directly derived empirically instead of using Mie theory to avoid making assumptions on pigmentation, refractive index and size distribution of the algae. The absorption coefficient was measured using the filter-pad transmission method (Stramski et al., 2015), the extinction coefficient was measured on a regular spectrophotometer from normal-normal transmittance (Kandilian et al., 2016), and the asymmetry parameter was assumed constant at 0.96 (Dauchet et al., 2015). The absorption coefficient was corrected from the instrument scattering biases with a baseline at 0.8 μm, a smoothing in the 0.3-0.5 μm range where the signal was noisy, and curve sharpening where scattering effects distorted the spectrum. The optical properties are representative of algal bloom from the Greenland ice sheet where the samples were collected (Chevrollier et al., 2023), and are assumed to generalise to all red algal blooms since red snow is caused by only a few species sharing a similar pigmentation (Lutz et al., 2016). The RTM outputs spectral albedo in the 0.205-4.995 μm range with steps of 0.01 μm, and only the spectral range of 0.295-2.405 μm was used here because (1) the sun irradiance is negligible below 0.295 μm, (2) radiometric sensors on ground, airborne or spaceborne platforms rarely detect signals above 2.5 μm, (3) BioSNICAR produces discontinuities around 2.5 μm, and (4) reducing the spectral range allows to reduce the training time of the emulator (see 2.1.2). In addition, the simulated albedos were converted to float16 to reduce the size of the look-up table files. The RTM-derived dataset contained 5,827,464 simulations, with 6 input features (grain size, LWC, BC concentration, dust concentration, red algal concentration, SZA) and a

212 bands albedo target. 90% of the dataset was used for training and 10% for testing the emulator. Prior to training, the input features were normalised to values between 0 and 1 to avoid biases in emulator training that would focus the learning on the parameters with the largest values.

2.1.2 Neural network

A feed forward neural network was designed using the Keras library (Chollet et al., 2015). The number of layers and neurons per layer, which determines the number of weights, was optimised from repeated runs of the Keras tuner bayesian optimisation, which searches for the model architecture with the lowest associated error among prescribed architectures. The chosen network had 12 hidden layers with different numbers of neurons for a total of 266,031 trainable parameters. The activation function for all layers was the exponential linear unit (elu), chosen to avoid a vanishing gradient problem, except for the last one, for which the activation function was linear. The performance of the model was monitored with three evaluation metrics: the mean absolute error (MAE), the mean absolute percentage error (MAPE), and the mean squared error (MSE). The loss of the model training was the mean absolute error, as it yielded the lowest values for all built-in evaluation metrics of Keras. The optimiser of the neural network was the Adaptive Moment estimation (Adam) optimiser with an adaptive learning rate decreasing exponentially, starting from 0.001. The model was trained for 200 epochs with a batch size of 256. For each epoch, the training dataset was shuffled and 10% was used for validation.

2.1.3 Inversion algorithm

The inversion algorithm was a gradient-descent algorithm built using the GradientTape tensorflow object, following the methodology of Jouvét et al. (2021). The goal of the algorithm is to iteratively minimise the cost between a target spectrum and the neural network's predicted spectrum in order to find the closest albedo curve and associated surface properties. The gradient of the cost is computed (and stored) with regards to each variable for 1000 iterations, except for the SZA which was fixed because the sun angle can be calculated prior inversion for a given spectrum. The gradient is then applied to the variables using the built-in Adagrad optimiser from Keras, and the values of the features are kept positive to prevent the gradient-descent from entering non-physical parameter spaces, i.e. negative surface properties. To avoid the retrieval of local minima, a pseudo-random sampling approach was implemented where the inversion was computed for 20 different initialisation points sampled randomly, in order to increase the chances of reaching a cost as low as possible by exploring different areas of the parameter space. The algorithm then selects the retrieval with the lowest cost out of the 20 initialisations as the final retrieval.

2.2 Ground spectroscopy

Hemispherical-Conical Reflectance Factor (HCRF) measurements were collected on snowfields around the Finse Alpine Research Center in summer 2023. In total, 185 measurements were collected using an ASD Fieldspec4 (spectral range 0.35-2.5 μm) and a black tripod, following the methodology of Cook et al. (2017). Each measurement was acquired with the bare fiber (field of view of 25 degrees) in 10 replicates, immediately ($< 10\text{s}$) after a reference spectrum was measured using a calibrated

Spectralon panel. All measurements were performed at nadir view (viewing zenith angle $\theta = 0^\circ$) with the tripod oriented
150 towards the sun to avoid shadow effects. Most (80%) of the measurements were taken for a solar zenith angle between 38° and
 50° , and the remaining (20%) were taken for a solar zenith angle below 59° . The spectra were corrected for the panel spectral
response as well as the step at $1\ \mu\text{m}$ caused by the misalignment of the SWIR and NIR sensors in the ASD FieldSpec, following
Painter (2011). For all spectra the step at $1\ \mu\text{m}$ was however not visible, probably because the instrument was warmed up for
at least an hour prior to the measurements and the selected surfaces were homogeneous enough (Painter, 2011). 5 spectra were
155 removed from the analysis because clear calibration errors were detected.

HCRF measurements have several benefits over using a cosine collector at our specific site: a) The measurements are faster to
execute, making it easier to avoid error due to changing illumination conditions, b) the incoming irradiance is fully re-diffused
by the reflectance panel, avoiding errors arising from the cosine property and levelling of the collector (Aoki et al., 2000), c)
the restricted field-of-view allowed to select relatively homogeneous and flat surfaces, reducing the error arising from micro-
160 topography and shadow effects. Since the measurements are theoretically not equivalent to spectral albedo, the impact of snow
anisotropy on the inversion retrievals was estimated by applying the anisotropy reflectance factor (ARF) measured by Dumont
et al. (2010) to the HCRF spectra. We selected the ARFs measured by Dumont et al. (2010) over a surface with high visible
impurities content at nadir viewing to best fit the type of surface and measurement set up of this study, with incident radiation
angles bounding the minimum and maximum solar zenith angle at the time of our measurements.

165 2.3 Albedo reduction and radiative forcing calculations

Broadband albedo (BBA) was calculated as:

$$BBA = \frac{\sum \alpha(\lambda) \times I(\lambda)}{\sum I(\lambda)} \quad (1)$$

with λ the wavelength in the spectral range of the emulator ($0.295\text{-}2.405\ \mu\text{m}$), $\alpha(\lambda)$ the spectral albedo output by the emulator
and $I(\lambda)$ the spectral irradiance from the RTM for a given SZA. The SZA corresponding to each HCRF measurement was
170 calculated using the pysolar Python package (Stafford et al., 2023). The SZA was set at 50° for measurements taken under
overcast conditions (48%), since it approximates the spectral albedo under diffuse irradiance (Wiscombe and Warren, 1980).
The BBA reduction associated with a given LAP was calculated by differencing the BBA of the retrieved spectrum with the
BBA calculated with the exact same conditions (grain size, SZA, LWC...) except the concentration of the given LAP, which
was set to 0. The daily and instantaneous radiative forcings (W m^{-2}) were calculated by multiplying the BBA reduction
175 with respectively the 24h daily averaged and instantaneous shortwave incoming radiation, as measured with a four-component
radiometer (CNR4, Kipp and Zonen, The Netherlands) at the local weather station (Pirk et al., 2023).

3 Results and discussion

3.1 Performance, benefits and uncertainties of the inversion method

3.1.1 Forward emulator

180 The neural network reproduced the original RTM simulations very accurately, with a mean absolute error (MAE), mean absolute percentage error (MAPE) and mean squared error (MSE) on the spectral albedo of respectively 5.3×10^{-5} , 0.047 %, and 8.5×10^{-9} both for the training and testing sets, indicating that the emulator does not overfit. The maximum MAE of the 5,827,464 samples of the training and testing sets was 5.8×10^{-4} , with 99% of the dataset predicted with a MAE below 8×10^{-5} (Fig. 1a). The spectral residuals of the prediction associated with the highest MAE are below 5.0×10^{-3} (Fig. 1b), and
185 below 2.0×10^{-5} for the lowest MAE (Fig. 1c).

The emulator has several benefits over and above running the full RTM: 1) it executes $\sim 30x$ faster; 2) it is a portable and lightweight Keras model occupying just 1MB of disk space, whereas the full RTM package occupies ~ 1 GB of disk space due to the large optical property database and look up tables that come bundled with it; 3) it enables the exploration of quasi-continuous spaces for all parameters, in comparison to the original RTM Python package which relies on the optical property
190 database for example for the snow grain size or SZA, and 4) it is a Keras model that can be loaded into scripts written in several popular programming languages (including Python, C, and FORTRAN), potentially enabling straightforward RTM integration into larger climate models. The emulator is therefore a practical and efficient alternative to the full RTM for the majority of use cases.

The computation efficiency of the emulator in comparison to the original RTM grows when predicting several spectral albedos
195 at once, but this improvement depends on the number of simulations and the use of multiprocessing. For example, the look-up table of +5,000,000 spectral albedos produced in this study can be generated with fully vectorised operations within the neural network (ie, happen simultaneously in-memory), which makes the computation speed 4 orders of magnitude faster than running the original RTM on a single thread. In the context of this study, the computation efficiency of the emulator also offers the possibility to carry out spectral inversions in a reasonable time.

200 3.1.2 Inversion algorithm

The neural network was incorporated into an inversion algorithm that retrieves the surface parameters required by the RTM to best reproduce a spectrum given as input. The inversion algorithm was evaluated on an ideal dataset with known surface properties to assess its ability to converge to an optimal solution, when it exists. 2000 sets of surface properties were sampled pseudo-randomly and fed into the emulator to produce a synthetic dataset of 2000 spectral albedos, which were then inverted.
205 The inversion algorithm reproduced the 2000 albedo curves with a mean absolute error (MAE) of 5×10^{-7} and the retrieved surface properties matched those of the synthetic dataset almost perfectly (Table 2), indicating that the algorithm is capable to reach an optimal solution if one exists. The standard deviation between the 20 different initialisation points for the albedo MAE, the algal concentration, the dust concentration, the BC concentration, the LWC and grain radius were respectively $1 \times$

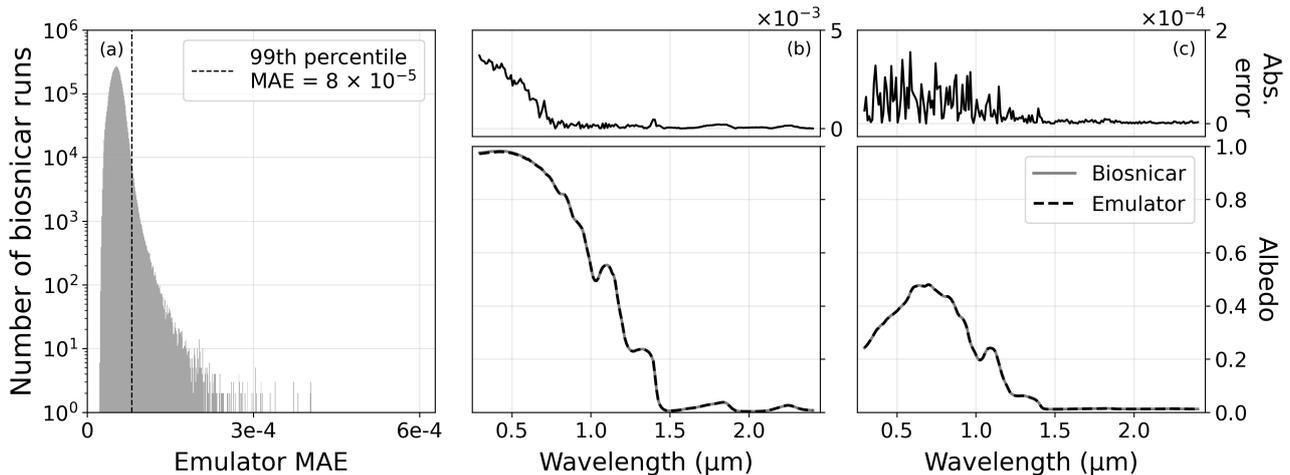


Figure 1. Performance of the emulator in reproducing the RTM simulations. (a): distribution of the mean absolute error (MAE) of the residuals between the original RTM model runs and the predictions of the emulator. Emulator-predicted vs. RTM-simulated albedos corresponding to the (b) highest and (c) lowest mean absolute residuals, with the associated spectral residuals above. Note that the scale on the MAE distribution is logarithmic.

Table 2. Mean error between the original and retrieved surface properties; slope and bias of the correlations between the original and retrieved surface properties.

Surface property	Algal concentration	Dust concentration	BC concentration	LWC	Grain radius
Mean Absolute Error (MAE)	5 cells mL ⁻¹	116 ppb	0.1 ppb	4×10^{-5} %	0.003 μm
Slope	0.99996	0.999897	0.9998	0.9999991	0.999997
Bias	1.02 cells mL ⁻¹	116.5 ppb	0.09 ppb	-1.52×10^{-7} %	0.005 μm

10⁻⁴, 497 cells mL⁻¹, 1.3×10^4 ppb, 14 ppb, 0.03 % and 4 μm. These variations are low and produce nearly undetectable effects on the spectral albedo in our model configuration, indicating that the algorithm is stable and reaches a similar solution despite starting from a different and random point. At present, the inversion method is fast enough to be scaled to satellite observations, with a computation time of about 50mn to invert 100km² of Sentinel-2 imagery at 60m resolution (tensorflow v2.16.0, CPU AMD Ryzen 7 7700X and RAM 64Gb). The method is hence efficient enough in speed and accuracy to open the possibility of separating the abundance and impact of LAPs at large scale.

215 3.2 Application to ground spectra

The inversion algorithm successfully reproduced the ground HCRF spectra measured on snowfields in Southern Norway (N=180, average MAE = 0.0056, max. MAE = 0.0089), including the apparent optical properties of LAPs (Fig. 2). Figure 2 shows the retrievals for four different surface types with distinct signatures: (a) relatively clean old snow with low concentra-

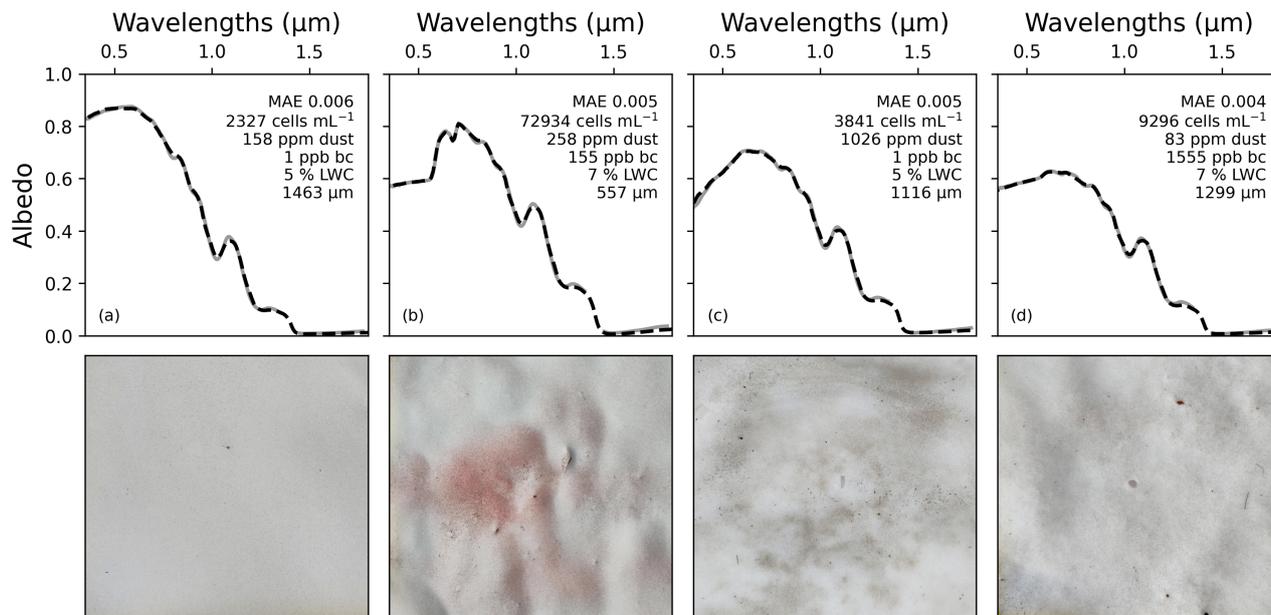


Figure 2. Field reflectances (gray) vs retrieved spectral albedos (dashed black) and associated surface properties for four different surface snow types: (a) relatively clean snow, (b) very red snow, (c) dust-loaded snow, and (d) dark particles-loaded snow. The scale of the images at the bottom is approximately 45x45 cm and is centered on the middle point of the footprint of the reflectance measurements.

tions of LAPs, (b) red snow surface with high algal concentration, (c) brown snow surface with high dust concentrations and
 220 (d) dark snow surface with high BC concentrations. The model accurately reproduces the red algal pigment features, and the
 retrieved concentrations of algae for the entire dataset covered the range of typically measured values (up to 1.2×10^5 cells
 mL⁻¹), with higher concentrations being associated with visibly redder surfaces (Fig. A1). The typical UV-absorbing feature
 of dust and the UV-VIS flattening signature of black particles were equally well reproduced (Fig. 2c, d). No measurements
 were performed to know whether BC was present in the snow and the retrieved BC concentrations are likely to represent
 225 dark particles of different origin, most of them coming from the vegetation around the snowfields. Therefore, BC is hereafter
 referred to as dark particles.

The standard deviation on the dust, algal and dark particle concentrations between the 20 random initialisations of the
 inversion algorithm was 514 ppb, 25 cells mL⁻¹ and 0.6 ppb respectively. This variability produces negligible effects on the
 spectral albedo, which shows that the uncertainties of the inversion method are primarily related to the assumptions on the
 230 field data rather than the randomness of the inversion algorithm. In particular, HCRF measurements are not strictly equivalent
 to hemispherical spectral albedo modelled by the RTM due to reflectance anisotropy (Cook et al., 2017), but no anisotropy
 correction exists for the type of wet, rough, aged and heterogeneous snow surface targeted by this study. The anisotropy of
 snow is more pronounced beyond 1.4 μm (Aoki et al., 2000) and its effect is lower for measurements taken at nadir view and
 incident angles below 60 ° (Dumont et al., 2010). Sensitivity analyses indicate that the effect of anisotropy on the retrievals

235 was different for each type of LAP and that this effect can be positive or negative depending on the LAP concentration and
the incident angle (Fig. A2). The algal concentrations were the least affected by the anisotropy correction (Fig. A2). Beyond
anisotropy, the slope of the surface can have a significant effect on snow albedo and corrections exist if the spectral diffuse
and direct partitioning of the incoming irradiance as well as the slope inclination and aspect have been measured (Picard et al.,
2020). Future work could therefore include measurements of the slope and roughness of the surfaces, along with the LAPs
240 concentrations, to distinguish between the error related to the LAPs abundance and the geometry of the surface. In this study,
given the variability in the effect of anisotropy, the effort to select flat and homogeneous surfaces during sampling and keep
the solar zenith angle below 60° , the nadir viewing, and the fact that our sample surfaces had varying physical configurations
that would require specific ARFs, HCRF measurements are considered to be equivalent to hemispherical albedo for BBA and
radiative forcing calculations presented herein.

245 The BBA reduction of LAPs ranged from 0.04 to 0.25 for the 180 data points, equivalent to a daily radiative forcing (RF)
of $7\text{--}44\text{ W m}^{-2}$ for the average daily summer illumination conditions at the field site (Fig. 3a), and $15\text{--}83\text{ W m}^{-2}$ for the
sunniest day of the season. These values cover the range of reported values for the maximum daily radiative forcing of LAPs
in Europe and North America (Skiles et al., 2018), and compare well with the recent estimation of 58 W m^{-2} reported in Col
du Lautaret, France (Tuzet et al., 2020). Red algal blooms alone reduced the albedo by up to 0.13 (mean: 0.05), dust reduced
250 the albedo by up to 0.21 (mean: 0.02), and dark particles reduced the albedo by up to 0.25 (mean: 0.03). The albedo-reducing
effect of each LAP was lower than if it was present alone, because the darkening caused by the presence of a LAP is lower
when the background surface is also darkened by other LAPs. In this case, the impact of algal blooms, dust and dark particles
were on average 39, 62 and 45% lower, and up to 2.8, 3.2 and 2.6 times lower, than if each type of LAP had been present alone.
These results align with previous observations for dust and black carbon (Skiles and Painter, 2018; Kaspari et al., 2014) and
255 emphasise the need to study LAPs concomitantly.

The daily average RF caused by dust, red algae and dark particles were respectively up to 36 W m^{-2} (mean: 4.0 W m^{-2}),
 22 W m^{-2} (mean: 9.0 W m^{-2}) and 44 W m^{-2} (mean: 6.1 W m^{-2}) and reached up to 72 W m^{-2} , 44 W m^{-2} and 87 W m^{-2}
 m^{-2} during the sunniest day. In comparison, the dust-specific daily RF estimates from surfaces in the Upper Colorado River
Basin were of the same order of magnitude, although higher as the surfaces were visibly more dust-loaded there (Skiles and
260 Painter, 2018), and the red algal-specific daily RF was comparable to the effect of red blooms in Antarctica (13 W m^{-2} ; Khan
et al. (2021)). The maximum instantaneous radiative forcing (IRF) due to LAPs for the entire dataset was 337 W m^{-2} . The
maximum dust IRF was 277 W m^{-2} , which is of the same order of magnitude to those reported in the Alps (up to 154 W m^{-2} ;
Di Mauro et al. (2015)) and in the Upper Colorado River Basin (525 W m^{-2} ; Skiles and Painter (2018)). In comparison, the
maximum algal IRF was 169 W m^{-2} , which closely matched the values reported for Alaska (up to 175 W m^{-2} ; Ganey et al.
265 (2017)), and the North Cascades at the end of July (156.9 W m^{-2} ; Healy and Khan (2023)), but was lower than those reported
in British Columbia at the end of July (up to 295 W m^{-2} ; Engstrom et al. (2022)) and in the North Cascades at the beginning
of July (359.95 W m^{-2} ; Healy and Khan (2023)). Differences in maximum IRF for a given LAP can be due to a different LAP
abundance, the presence of other LAPs at the surface, a different surface distribution, and/or a higher maximum irradiance.
Finally, the 180 data points presented here are representative of small footprints of $\sim 0.1\text{ m}^2$ and were not specifically collected

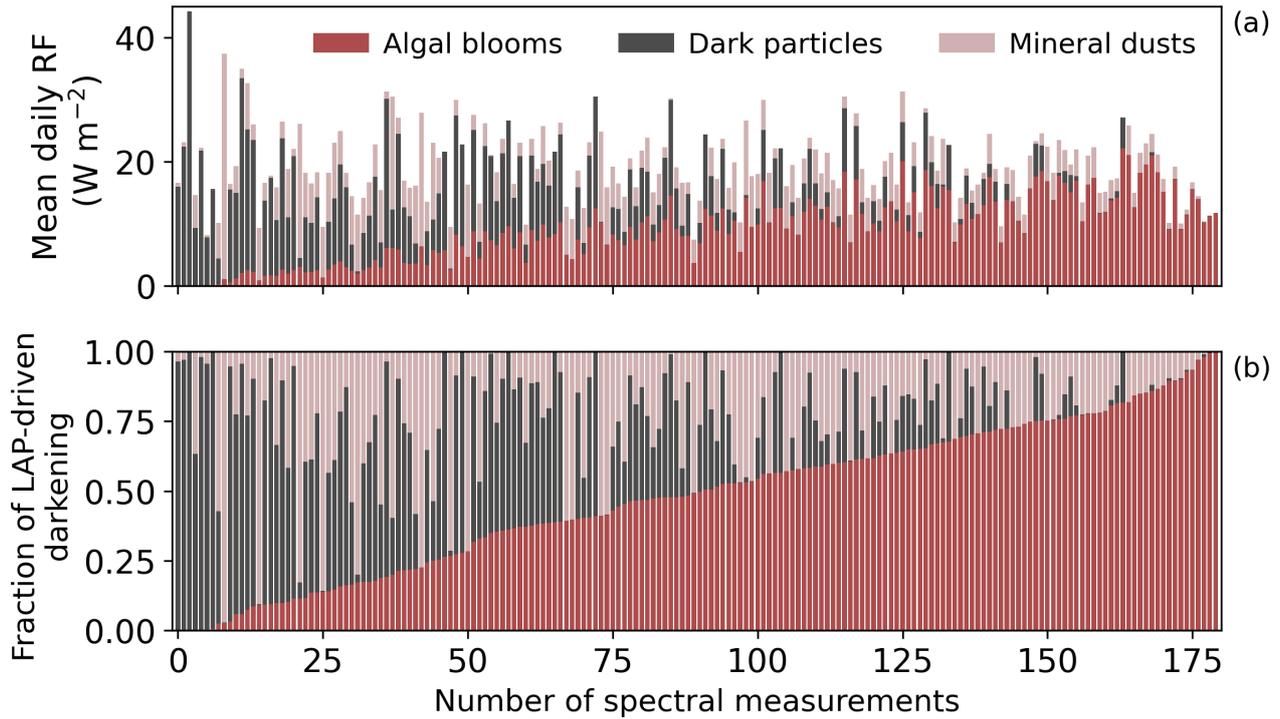


Figure 3. Radiative forcing (a) and contribution to LAP-driven albedo reduction (b) associated with the presence of each LAP for the 180 spectra analysed.

270 to be representative of larger surface areas, yet they serve as an illustration of the range of impact and relative contribution that LAPs can have. Indeed, the new method employed here enables the retrieval of surface properties that are otherwise not accessible, such as the separate impact of each type of light absorbing particle. This dataset therefore demonstrates the high variability of LAPs impact, emphasising the need to study them both separately and concomitantly, and highlighting the important role of biotic LAPs in snow surface albedo reduction (Fig. 3b). Eventually, other LAPs could be integrated in the
 275 model for it to be applicable to other locations where ashes, brown carbon, green algae or different types of dust are present on the snow surfaces.

4 Conclusions

Light absorbing particles have varying apparent optical properties, challenging the quantification of their albedo reducing effect using forward modeling and making inverse methods relevant for their detection. Here we present an efficient, robust and
 280 portable method aimed at simultaneously retrieving the abundance of LAPs and their albedo-reducing effect on snow surfaces from spectral albedo measurements. It consists of a neural network emulating a radiative transfer model, and an inversion algorithm. We found that the neural network added negligible error compared to using the full RTM and ran significantly

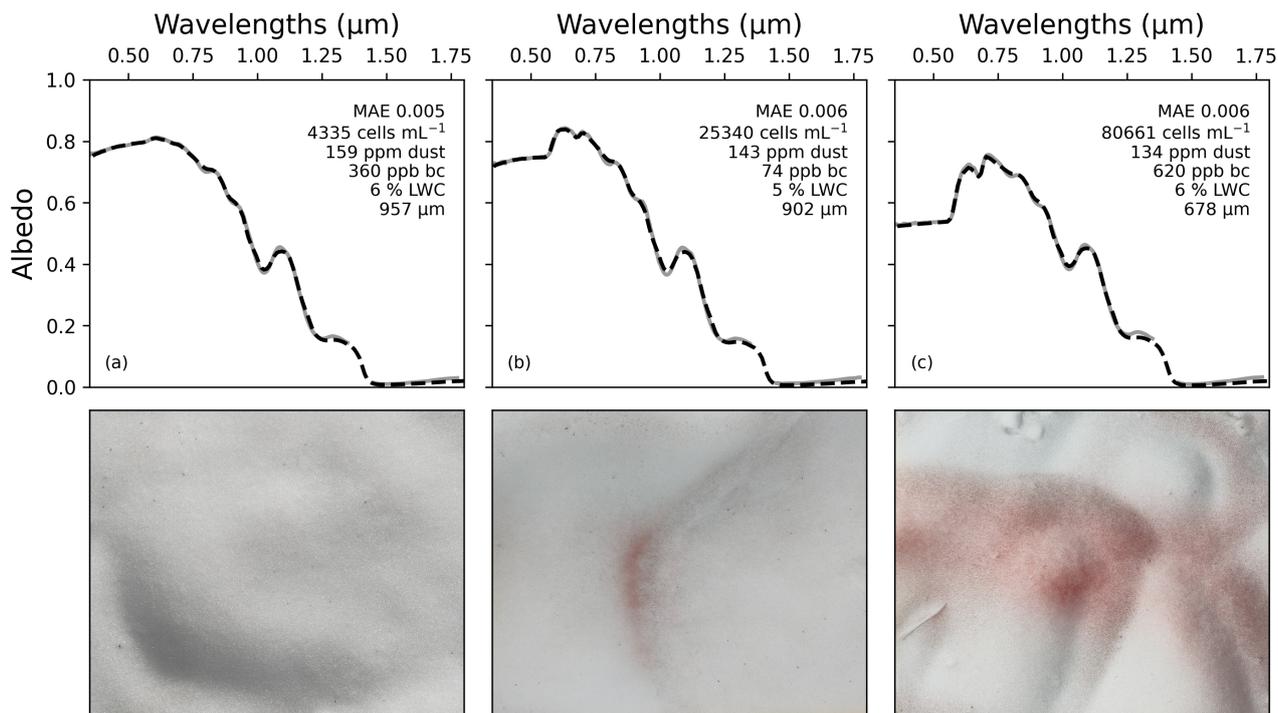


Figure A1. Field reflectances (gray) vs retrieved spectral albedos (dashed black) and associated surface properties for three surfaces visibly more and more red. The scale of the images at the bottom is approximately 45x45 cm and is centered on the middle point of the footprint of the reflectance measurements.

faster. We used the neural network in inverse mode to retrieve the surface properties that best explain observed field spectra and calculate how much albedo change and radiative forcing can be attributed to red algae, dust or dark particles. The results highlight a wide range, magnitude, and co-dependency of LAP impacts, illustrating the subsequent need to study LAPs both separately and concomitantly. The high and stable performance of this inversion algorithm on field spectra indicates that it could also be applied to imagery obtained from drones or satellites to improve the diversity of information captured from regional scale mapping of snow. To facilitate future usage and development of the method, the full code running the model and the inversion was made available into an open-source Python package. Ongoing developments currently focus on making the inversion algorithm resolution-agnostic and hence adaptable to several remote sensing products, as well as adding the possibility to prescribe sensor-specific spectral responses. The application of the method to new areas using remotely sensed imagery will present additional challenges to consider, such as (i) the variability in mineral dust optical properties that may require new mineral mixtures in the model, (ii) the presence of shallow snowpacks of which signature could be confounded with that of black carbon (Warren, 2013), or (ii) the variability in spectral resolution between sensors, where lower resolution imagery may require stronger constraints on the inverse problem.

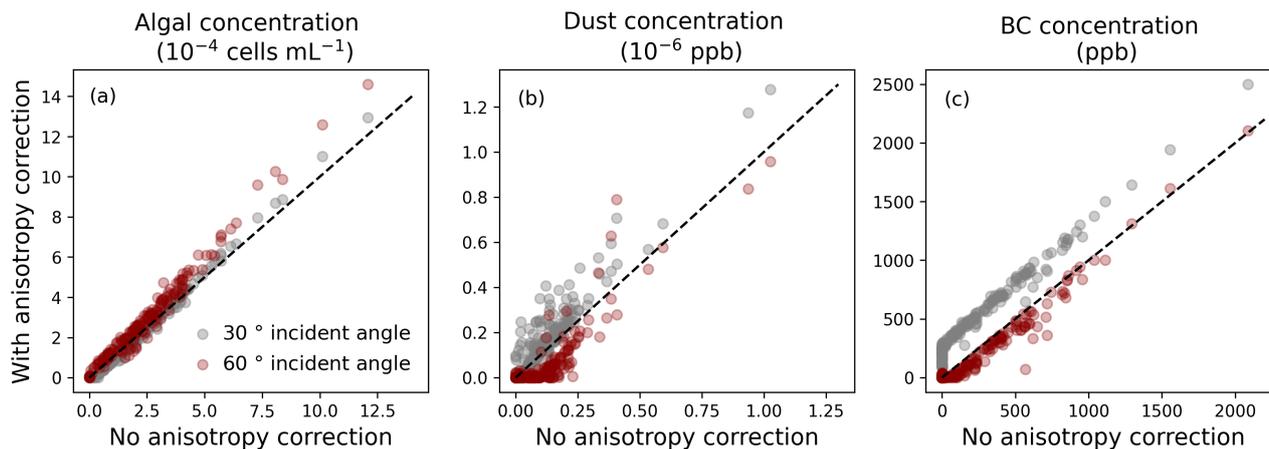


Figure A2. Sensitivity tests to evaluate the potential effect of snow anisotropy on the retrievals of (a) algal, (b) dust and (c) black carbon concentrations with the inversion algorithm. The retrievals of the inversions on LAPs concentrations are compared to the retrievals when applying ARFs from Dumont et al. (2010), measured over a flat snow surface with impurities at an incident angle of 30 ° and 60 °.

Code and data availability. The inversion framework developed in this study is available as the Python package snowlaps online on GitHub at <https://github.com/openosmia/snowlaps>. The version 0.1.0 used in this study is stored in a Zenodo repository at <https://doi.org/10.5281/zenodo.14639602>. The BioSNICAR model version 2.1 is available at <https://github.com/jmcook1186/biosnicar-py>.

Author contributions. Conceptualisation: LC, AW; Data collection: LC, AW, NP; Data curation: LC, AW, NP; Algorithm development: LC, AW; BioSNICAR maintenance: LC, JC; Visualisation: LC, AW; Writing - original draft preparation: LC; Funding acquisition: LGB, AMA, MT; Writing - review and editing: All authors.

Competing interests. The authors declare that they have no conflict of interest.

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310 (Harris et al., 2020), pandas (pandas development team, 2024; Wes McKinney, 2010), tensorflow (Developers, 2024), keras (Chollet et al., 2015), matplotlib (Hunter, 2007), scipy (Virtanen et al., 2020), and scikit-learn (Pedregosa et al., 2011).

References

- Aoki, T., Aoki, T., Fukabori, M., Hachikubo, A., Tachibana, Y., and Nishio, F.: Effects of snow physical parameters on spectral albedo and bidirectional reflectance of snow surface, *Journal of Geophysical Research: Atmospheres*, 105, 10 219–10 236, 2000.
- 315 Bohn, N., Painter, T. H., Thompson, D. R., Carmon, N., Susiluoto, J., Turmon, M. J., Helmlinger, M. C., Green, R. O., Cook, J. M., and Guanter, L.: Optimal estimation of snow and ice surface parameters from imaging spectroscopy measurements, *Remote Sensing of Environment*, 264, 112 613, 2021.
- Bond, T. C., Doherty, S. J., Fahey, D. W., Forster, P. M., Berntsen, T., DeAngelo, B. J., Flanner, M. G., Ghan, S., Kärcher, B., Koch, D., et al.: Bounding the role of black carbon in the climate system: A scientific assessment, *Journal of geophysical research: Atmospheres*, 320 118, 5380–5552, 2013.
- Chevrollier, L.-A., Cook, J. M., Halbach, L., Jakobsen, H., Benning, L. G., Anesio, A. M., and Tranter, M.: Light absorption and albedo reduction by pigmented microalgae on snow and ice, *Journal of Glaciology*, 69, 333–341, 2023.
- Chollet, F. et al.: Keras, <https://keras.io>, 2015.
- Cook, J. M., Hodson, A. J., Gardner, A. S., Flanner, M., Tedstone, A. J., Williamson, C., Irvine-Fynn, T. D., Nilsson, J., Bryant, R., and 325 Tranter, M.: Quantifying bioalbedo: a new physically based model and discussion of empirical methods for characterising biological influence on ice and snow albedo, *The Cryosphere*, 11, 2611–2632, 2017.
- Cook, J. M., Tedstone, A. J., Williamson, C., McCutcheon, J., Hodson, A. J., Dayal, A., Skiles, M., Hofer, S., Bryant, R., McAree, O., et al.: Glacier algae accelerate melt rates on the south-western Greenland Ice Sheet, *The Cryosphere*, 14, 309–330, 2020.
- Dauchet, J., Blanco, S., Cornet, J.-F., and Fournier, R.: Calculation of the radiative properties of photosynthetic microorganisms, *Journal of* 330 *Quantitative Spectroscopy and Radiative Transfer*, 161, 60–84, 2015.
- Developers, T.: TensorFlow, <https://doi.org/10.5281/zenodo.12726004>, 2024.
- Di Mauro, B., Fava, F., Ferrero, L., Garzonio, R., Baccolo, G., Delmonte, B., and Colombo, R.: Mineral dust impact on snow radiative properties in the European Alps combining ground, UAV, and satellite observations, *Journal of Geophysical Research: Atmospheres*, 120, 6080–6097, <https://doi.org/10.1002/2015jd023287>, 2015.
- 335 Donahue, C., Skiles, S. M., and Hammonds, K.: Mapping liquid water content in snow at the millimeter scale: an intercomparison of mixed-phase optical property models using hyperspectral imaging and in situ measurements, *The Cryosphere*, 16, 43–59, 2022.
- Donahue, C. P., Menounos, B., Viner, N., Skiles, S. M., Beffort, S., Denouden, T., Arriola, S. G., White, R., and Heathfield, D.: Bridging the gap between airborne and spaceborne imaging spectroscopy for mountain glacier surface property retrievals, *Remote Sensing of Environment*, 299, 113 849, 2023.
- 340 Dumont, M. and Tuzet, F.: Light-absorbing Particles in Snow and Climate, in: *Chemistry in the Cryosphere (In 2 Parts)*, pp. 795–830, World Scientific, 2022.
- Dumont, M., Brissaud, O., Picard, G., Schmitt, B., Gallet, J.-C., and Arnaud, Y.: High-accuracy measurements of snow Bidirectional Reflectance Distribution Function at visible and NIR wavelengths—comparison with modelling results, *Atmospheric Chemistry and Physics*, 10, 2507–2520, 2010.
- 345 Dumont, M., Arnaud, L., Picard, G., Libois, Q., Lejeune, Y., Nabat, P., Voisin, D., and Morin, S.: In situ continuous visible and near-infrared spectroscopy of an alpine snowpack, *The Cryosphere*, 11, 1091–1110, 2017.
- Engstrom, C. B., Williamson, S. N., Gamon, J. A., and Quarmby, L. M.: Seasonal development and radiative forcing of red snow algal blooms on two glaciers in British Columbia, Canada, summer 2020, *Remote Sensing of Environment*, 280, 113 164, 2022.

- Flanner, M., Liu, X., Zhou, C., Penner, J. E., and Jiao, C.: Enhanced solar energy absorption by internally-mixed black carbon in snow grains, *Atmospheric Chemistry and Physics*, 12, 4699–4721, 2012.
- Flanner, M. G., Shell, K. M., Barlage, M., Perovich, D. K., and Tschudi, M.: Radiative forcing and albedo feedback from the Northern Hemisphere cryosphere between 1979 and 2008, *Nature Geoscience*, 4, 151–155, 2011.
- Flanner, M. G., Arnheim, J. B., Cook, J. M., Dang, C., He, C., Huang, X., Singh, D., Skiles, S. M., Whicker, C. A., and Zender, C. S.: SNICAR-ADv3: a community tool for modeling spectral snow albedo, *Geoscientific Model Development*, 14, 7673–7704, 2021.
- Ganey, G. Q., Loso, M. G., Burgess, A. B., and Dial, R. J.: The role of microbes in snowmelt and radiative forcing on an Alaskan icefield, *Nature Geoscience*, 10, 754–759, <https://doi.org/10.1038/ngeo3027>, 2017.
- Gardner, A. S. and Sharp, M. J.: A review of snow and ice albedo and the development of a new physically based broadband albedo parameterization, *Journal of Geophysical Research: Earth Surface*, 115, 2010.
- Harris, C. R., Millman, K. J., van der Walt, S. J., Gommers, R., Virtanen, P., Cournapeau, D., Wieser, E., Taylor, J., Berg, S., Smith, N. J., Kern, R., Picus, M., Hoyer, S., van Kerkwijk, M. H., Brett, M., Haldane, A., del Río, J. F., Wiebe, M., Peterson, P., Gérard-Marchant, P., Sheppard, K., Reddy, T., Weckesser, W., Abbasi, H., Gohlke, C., and Oliphant, T. E.: Array programming with NumPy, *Nature*, 585, 357–362, <https://doi.org/10.1038/s41586-020-2649-2>, 2020.
- Harrold, Z. R., Hausrath, E. M., Garcia, A., Murray, A. E., Tschauer, O., Raymond, J. A., and Huang, S.: Bioavailability of mineral-bound iron to a snow algal-bacterial coculture and implications for albedo-altering snow algal blooms, *Applied and Environmental Microbiology*, 84, e02322–17, 2018.
- He, C.: Modelling light-absorbing particle–snow–radiation interactions and impacts on snow albedo: fundamentals, recent advances and future directions, *Environmental Chemistry*, 19, 296–311, 2022.
- Healy, S. M. and Khan, A. L.: Albedo change from snow algae blooms can contribute substantially to snow melt in the North Cascades, USA, *Communications Earth & Environment*, 4, 142, 2023.
- Hunter, J. D.: Matplotlib: A 2D graphics environment, *Computing in Science & Engineering*, 9, 90–95, <https://doi.org/10.1109/MCSE.2007.55>, 2007.
- Jouvet, G., Cordonnier, G., Kim, B., Lüthi, M., Vieli, A., and Aschwanden, A.: Deep learning speeds up ice flow modelling by several orders of magnitude, *Journal of Glaciology*, 68, 651–664, <https://doi.org/10.1017/jog.2021.120>, 2021.
- Kandilian, R., Soulies, A., Pruvost, J., Rousseau, B., Legrand, J., and Pilon, L.: Simple method for measuring the spectral absorption cross-section of microalgae, *Chemical Engineering Science*, 146, 357–368, 2016.
- Kaspari, S., Painter, T. H., Gysel, M., Skiles, S., and Schwikowski, M.: Seasonal and elevational variations of black carbon and dust in snow and ice in the Solu-Khumbu, Nepal and estimated radiative forcings, *Atmospheric chemistry and physics*, 14, 8089–8103, 2014.
- Khan, A. L., Dierssen, H. M., Scambos, T. A., Höfer, J., and Cordero, R. R.: Spectral characterization, radiative forcing and pigment content of coastal Antarctic snow algae: approaches to spectrally discriminate red and green communities and their impact on snowmelt, *The Cryosphere*, 15, 133–148, <https://doi.org/10.5194/tc-15-133-2021>, 2021.
- Kokhanovsky, A., Di Mauro, B., Garzonio, R., and Colombo, R.: Retrieval of dust properties from spectral snow reflectance measurements, *Frontiers in Environmental Science*, 9, 644551, 2021.
- Lutz, S., Anesio, A. M., Raiswell, R., Edwards, A., Newton, R. J., Gill, F., and Benning, L. G.: The biogeography of red snow microbiomes and their role in melting arctic glaciers, *Nature communications*, 7, 11968, 2016.
- Malinka, A.: Stereological approach to radiative transfer in porous materials. Application to the optics of snow, *Journal of Quantitative Spectroscopy and Radiative Transfer*, 295, 108410, 2023.

- McCutcheon, J., Lutz, S., Williamson, C., Cook, J. M., Tedstone, A. J., Vanderstraeten, A., Wilson, S., Stockdale, A., Bonneville, S., Anesio, A. M., et al.: Mineral phosphorus drives glacier algal blooms on the Greenland Ice Sheet, *Nature Communications*, 12, 570, 2021.
- Painter, T. H.: Comment on Singh and others, 'Hyperspectral analysis of snow reflectance to understand the effects of contamination and grain size', *Journal of Glaciology*, 57, 183–185, 2011.
- 390 pandas development team, T.: pandas-dev/pandas: Pandas, <https://doi.org/10.5281/zenodo.10957263>, 2024.
- Pedregosa, F., Varoquaux, G., Gramfort, A., Michel, V., Thirion, B., Grisel, O., Blondel, M., Prettenhofer, P., Weiss, R., Dubourg, V., Vanderplas, J., Passos, A., Cournapeau, D., Brucher, M., Perrot, M., and Duchesnay, E.: Scikit-learn: Machine Learning in Python, *Journal of Machine Learning Research*, 12, 2825–2830, 2011.
- 395 Picard, G. and Libois, Q.: Simulation of snow albedo and solar irradiance profile with the Two-streAm Radiative TransfER in Snow (TARTES) v2.0 model, *Geoscientific Model Development*, 17, 8927–8953, 2024.
- Picard, G., Libois, Q., and Arnaud, L.: Refinement of the ice absorption spectrum in the visible using radiance profile measurements in Antarctic snow, *The Cryosphere*, 10, 2655–2672, 2016.
- Picard, G., Dumont, M., Lamare, M., Tuzet, F., Larue, F., Pirazzini, R., and Arnaud, L.: Spectral albedo measurements over snow-covered slopes: theory and slope effect corrections, *The Cryosphere*, 14, 1497–1517, <https://doi.org/10.5194/tc-14-1497-2020>, 2020.
- 400 Pirk, N., Aalstad, K., Yilmaz, Y. A., Vatne, A., Popp, A. L., Horvath, P., Bryn, A., Vollsnes, A. V., Westermann, S., Berntsen, T. K., Stordal, F., and Tallaksen, L. M.: Snow–vegetation–atmosphere interactions in alpine tundra, *Biogeosciences*, 20, 2031–2047, <https://doi.org/10.5194/bg-20-2031-2023>, 2023.
- Prahl, S.: miepython: Pure python implementation of Mie scattering, <https://doi.org/10.5281/zenodo.8023972>, 2023.
- 405 Robledano, A., Picard, G., Dumont, M., Flin, F., Arnaud, L., and Libois, Q.: Unraveling the optical shape of snow, *Nature Communications*, 14, 3955, 2023.
- Rowe, P., Fergoda, M., and Neshyba, S.: Temperature-dependent optical properties of liquid water from 240 to 298 K, *Journal of Geophysical Research: Atmospheres*, 125, e2020JD032 624, 2020.
- Segelstein, D. J.: The complex refractive index of water, Ph.D. thesis, University of Missouri–Kansas City, 1981.
- 410 Skiles, S. M. and Painter, T. H.: Assessment of radiative forcing by light-absorbing particles in snow from in situ observations with radiative transfer modeling, *Journal of Hydrometeorology*, 19, 1397–1409, 2018.
- Skiles, S. M., Painter, T., and Okin, G. S.: A method to retrieve the spectral complex refractive index and single scattering optical properties of dust deposited in mountain snow, *Journal of Glaciology*, 63, 133–147, 2017.
- Skiles, S. M., Flanner, M., Cook, J. M., Dumont, M., and Painter, T. H.: Radiative forcing by light-absorbing particles in snow, *Nature*
- 415 *Climate Change*, 8, 964–971, 2018.
- Stafford, B., Louis, R., Wilson, R., Rejeté, F., Steinmetz, F., Borsetti, M., Bachmann, A., Aronovitch, A., Blennerhassett, E., Hardy, W., steelman, Kiselev, A., Firing, E., Semeniuc, E., Kundert, P., Arron-Walker, T., McNaughton, W., solarjoe, Wallace, A., bfrobin446, Luiten, C., Rackwitz, C., Sharma, D., Maliarik, D., Hasan, Deane, J., van Haarst, J., Heikkilä, J., Maron, J., and Contreras, J. L. L.: pingswept/pysolar: 0.11, <https://doi.org/10.5281/zenodo.8184359>, 2023.
- 420 Stramski, D., Reynolds, R. A., Kaczmarek, S., Uitz, J., and Zheng, G.: Correction of pathlength amplification in the filter-pad technique for measurements of particulate absorption coefficient in the visible spectral region, *Applied Optics*, 54, 6763–6782, 2015.
- Tuzet, F., Dumont, M., Picard, G., Lamare, M., Voisin, D., Nabat, P., Lafaysse, M., Larue, F., Revuelto, J., and Arnaud, L.: Quantification of the radiative impact of light-absorbing particles during two contrasted snow seasons at Col du Lautaret (2058 m asl, French Alps), *The Cryosphere*, 14, 4553–4579, 2020.

- 425 Virtanen, P., Gommers, R., Oliphant, T. E., Haberland, M., Reddy, T., Cournapeau, D., Burovski, E., Peterson, P., Weckesser, W., Bright, J., van der Walt, S. J., Brett, M., Wilson, J., Millman, K. J., Mayorov, N., Nelson, A. R. J., Jones, E., Kern, R., Larson, E., Carey, C. J., Polat, İ., Feng, Y., Moore, E. W., VanderPlas, J., Laxalde, D., Perktold, J., Cimrman, R., Henriksen, I., Quintero, E. A., Harris, C. R., Archibald, A. M., Ribeiro, A. H., Pedregosa, F., van Mulbregt, P., and SciPy 1.0 Contributors: SciPy 1.0: Fundamental Algorithms for Scientific Computing in Python, *Nature Methods*, 17, 261–272, <https://doi.org/10.1038/s41592-019-0686-2>, 2020.
- 430 Warren, S. G.: Optical properties of snow, *Reviews of Geophysics*, 20, 67–89, 1982.
- Warren, S. G.: Can black carbon in snow be detected by remote sensing?, *Journal of Geophysical Research: Atmospheres*, 118, 779–786, 2013.
- Warren, S. G. and Brandt, R. E.: Optical constants of ice from the ultraviolet to the microwave: A revised compilation, *Journal of Geophysical Research: Atmospheres*, 113, 2008.
- 435 Wes McKinney: Data Structures for Statistical Computing in Python, in: *Proceedings of the 9th Python in Science Conference*, edited by Stéfan van der Walt and Jarrod Millman, pp. 56 – 61, <https://doi.org/10.25080/Majora-92bf1922-00a>, 2010.
- Whicker, C. A., Flanner, M. G., Dang, C., Zender, C. S., Cook, J. M., and Gardner, A. S.: SNICAR-ADv4: a physically based radiative transfer model to represent the spectral albedo of glacier ice, *The Cryosphere*, 16, 1197–1220, 2022.
- Wiscombe, W. J. and Warren, S. G.: A model for the spectral albedo of snow. I: Pure snow, *Journal of the Atmospheric Sciences*, 37, 440 2712–2733, 1980.