



1           **Impact of different solar EUV proxies and Ap index on hmF2 trend analysis**

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17

18           **Abstract**

19           Long-term trend estimation in the peak height of the F2 layer, hmF2, needs the previous  
20           filtering of much stronger natural variations such as those linked to the diurnal, seasonal, and  
21           solar activity cycles. If not filtered, they need to be included in the model used to estimate  
22           the trend. The same happens with the maximum ionospheric electron density that occurs in  
23           this layer, NmF2, usually analyzed through the F2 layer critical frequency, foF2. While  
24           diurnal and seasonal variations can be easily managed, filtering the effects of solar activity  
25           presents more challenges, as does the influence of geomagnetic activity. However, recent  
26           decades have shown that geomagnetic activity may not significantly impact trend  
27           assessments. On the other hand, the choice of solar activity proxies for filtering has been  
28           shown to influence trend values in foF2, potentially altering even the trend's sign. This study  
29           examines the impact of different solar activity proxies on hmF2 trend estimations, using data  
30           updated to 2022, including the ascending phase of solar cycle 25, and explores the effect of  
31           including the Ap index as a filtering factor. The results obtained, based on two mid-latitude  
32           stations, are also comparatively analyzed to those obtained for foF2. The main findings  
33           indicate that the squared correlation coefficient,  $r^2$ , between hmF2 and solar proxies,  
34           regardless of the model used or the inclusion of the Ap index, is consistently lower than in  
35           the corresponding foF2 cases. This lower  $r^2$  value in hmF2 suggests a greater amount of  
36           unexplained variance, indicating that there is significant room for improvement in these  
37           models. However, in terms of trend values, foF2 shows greater variability depending on the  
38           proxy used, whereas the inclusion or exclusion of the Ap index does not significantly affect  
39           these trends. This suggests that foF2 trends are more sensitive to the choice of solar activity



40 proxy. In contrast, hmF2 trends, while generally negative, exhibit greater stability than foF2  
41 trends.

## 42 **Keywords**

43 Solar activity proxy, hmF2, ionosphere long-term trends, F10.7, F30, greenhouse gas  
44 increase.

45

## 46 **Highlights**

47 1. Long-term trends in hmF2 change with the solar activity proxy used for filtering but are  
48 mostly negative.

49 2. SN yields the weakest negative hmF2 trends, which are still negative, while foF2 trends  
50 are mostly positive.

51 3. Yearly hmF2 values show a linear relationship with solar proxies but improve with the  
52 inclusion of a squared term and the Ap index.

53

## 54 **1. Introduction**

55 Long-term trends in the Earth's ionosphere expected from the increase in greenhouse gas  
56 concentration along the last decades has been a topic of growing interest since the late 1980's  
57 (Roble and Dickinson, 1989; Rishbeth, 1990) with many results already published  
58 (Laštovička et al. 2012, 2014; Laštovička 2017, 2021a). It has been mainly studied through  
59 the analyses of the critical frequency of the F2 layer, foF2, that is a measure of the ionospheric  
60 peak electron density, NmF2 ( $=1.24 \cdot 10^{10} \text{ foF2}^2$ , with foF2 in MHz and NmF2 in  $\text{m}^{-3}$ ). Even  
61 though the trends in the ionosphere linked to the greenhouse effect are expected to be more  
62 clear in the ionospheric peak height, hmF2, (Rishbeth, 1990; Rishbeth and Roble, 1992)  
63 publications analyzing foF2 trend detection are by far more numerous. One reason may be  
64 that hmF2, unlike foF2, is not directly derived from ionosonde records. It can be estimated  
65 using the Shimazaki formula (Shimazaki, 1955) based on the M(3000)F2 propagation factor,  
66 which is calculated by taking the ratio of the Maximum Usable Frequency at 3000 km  
67 (MUF(3000)) to foF2, and which dates back to the same years as foF2. However, specially  
68 during daytime hours, there are systematic differences between hmF2 derived from  
69 M(3000)F2 and the true height value. A good option is systematic hmF2 deduced by real-  
70 height analysis of automatically scaled vertical incidence digisonde ionograms but these time  
71 series are available for only a few past decades.

72 Regarding the selection of a best solar EUV proxy to estimate trends in the F2 region, it is a  
73 problem which dates back almost to the very beginning when long-term trends in the upper  
74 atmosphere became a topical issue, but has regained critical importance during the last few  
75 years. We could speak of two epochs discussing this issue, which are before and after the  
76 occurrence of the 2008 solar minimum. Papers analyzing trends based on time series not  
77 reaching this period, deal basically with the selection between two proxies: F10.7 and SN.  
78 After the 2008 minimum epoch, studies that analyzed time series that included cycle 23 with



79 its minimum in ~2008, detected that not only SN, but also F10.7 was not efficient enough for  
80 filtering solar activity. As a result, indices more directly related to UV and EUV radiation  
81 came into play, such as the core-to-wing ratio of the Mg II line, and the solar Lyman  $\alpha$   
82 irradiance (at 121.567 nm). It can be also said that 2021, with the works by Laštovička  
83 (2021b, 2021c), is the year when a variety of solar EUV proxies are formally introduced as  
84 options to filter ionospheric parameters as a previous step in trend estimations.

85 Most papers used foF2 in order to determine the effect of the different proxies over the trend  
86 values, and also to decide which of them was a best EUV indicator (de Haro Barbas et al.,  
87 2021; Zossi et al., 2023; Danilov and Konstantinova, 2023; Laštovička and Burešová, 2023;  
88 Laštovička, 2024). Laštovička (2021b) incorporated foE, and Laštovička (2021c) also global  
89 TEC.

90 Jarvis et al. (1998) were among the first to do a solar proxy selection for estimating hmF2  
91 trends. They specifically compared F10.7 and SN, choosing F10.7 due to its slightly smaller  
92 variance in trend estimates during solar cycles 23 and 24, which marked a period of  
93 significant discrepancy compared to earlier cycles, ending in 1995. Jarvis et al. (2002), added  
94 E10.7 to the solar proxies' options for hmF2 trend estimations, but its performance was  
95 almost identical to F10.7.

96 Laštovička et al. (2006), for foF2 trend analysis, compared SN to F10.7 and E10.7. They  
97 distinguished between adjusted and observed in the case of the last two proxies, with the  
98 observed F10.7 and E10.7 appearing to be the best correcting factors for filtering or modeling  
99 solar activity effects prior to trend estimation. Observed F10.7 performed the best also in the  
100 study of Ulich et al. (2007), analyzing foF2 trends as well, which is reasonable since the solar  
101 radiative energy reaching Earth is modulated by the variation in the Earth–Sun distance.

102 The idea was to provide a comprehensive overview of the evolution in the effort to select the  
103 best solar proxy for detecting long-term trends in ionospheric parameters, but the task turned  
104 out to be much larger than anticipated. This is not only due to the many years that have passed  
105 since the proxy selection issue was first identified as a conflict in the field of long-term trends,  
106 but also because the problem has become increasingly complex. On one hand, there are  
107 numerous proxies, and on the other hand, two variations in solar activity have become more  
108 apparent over the years that were not as evident with shorter data series. One is the  
109 prominence of the Gleissberg cycle in the maximum solar activity, which became clear with  
110 six complete cycles of data showing a long-term periodic modulation (~80-90 years,  
111 corresponding to the Gleissberg periodicity) and the decline of the last two minima (~2008  
112 and ~2019) compared to previous minima. These two "trends" in solar activity are not  
113 identical in every proxy. Therefore, we will end with the review of this major issue in trend  
114 estimation here, suggesting it as a future task to be carefully revisited, and proceed directly  
115 to our analysis of this conflict with hmF2 data updated to the year 2022. The issue of  
116 including or not Ap, seemed to have a weaker effect than the solar proxy selection, but was  
117 also mostly analyzed in foF2 trend studies. So, we will focus in the two problems: the solar  
118 activity proxy selection and whether accounting for geomagnetic activity makes a difference  
119 or not in trend values, making a comparison with foF2 case.



120 The next three sections outline the data sets used and methodology. The results are provided  
121 in section 5, followed by the discussion and concluding remarks in section 6.

122

## 123 **2. Data sets**

### 124 **2.1 Ionospheric data**

125 Hourly monthly medians of the ionospheric propagating factor at 3000 km of the F2 layer,  
126 identified as M(3000)F2, and foF2 from two mid-latitude ionospheric stations were analyzed  
127 for the period 1960-2022: Rome (41.5°N, 12.3°E) and Juliusruh (54.6°N, 13.4°E). Databases  
128 were obtained from the World Data Centre (WDC) for Space Weather, Australia, accessible  
129 at <https://downloads.sws.bom.gov.au/wdc/iondata/au/> and from Damboldt and Suessman  
130 database (Damboldt and Suessman, 2012) available in the same WDC  
131 (<https://downloads.sws.bom.gov.au/wdc/iondata/medians/>). In the case of Rome, to extend  
132 the dataset until 2022, additional data were incorporated from the Digital Ionogram Data  
133 Base (DIDBase) at Lowell GIRO Data Center (LGDC), (Reinisch and Galkin, 2011). A 7-  
134 year overlap (2001-2007) between the two datasets was examined to confirm series  
135 homogeneity, resulting in a reasonable agreement of over 95% between the series.

136 Autoscaled hmF2, together with M(3000)F2, for the period 2001-2022 from the LGDC were  
137 also used for Rome and Juliusruh to test the height formula chosen in this study. Data from  
138 the DIDBase at LGDC has a frequency from 5 to 30 minutes. In order to obtain the monthly  
139 medians, we first selected data with Autoscaling Confidence Score (CS) greater than 70%,  
140 and then estimated for each month the hourly medians.

141 To calculate hmF2 from M(3000)F2, the Shimazaki formula was used (Shimazaki, 1955):

$$142 \quad hmF2 = \frac{1490}{M(3000)F2} - 176 \quad (1)$$

143 Annual mean foF2 and hmF2 values were assessed for 0 LT and 12 LT.

144 While the value of hmF2 depends on the formula used, and it is closer to the "real" value for  
145 more precise ones than Equation (1), such as those given by Bradley and Dudeney (1973),  
146 Dudeney (1974), and Bilitza et al. (1979), the trend values may not differ much. In this  
147 regard, some studies suggest this is the case (Bremer, 1998), while others indicate that trends  
148 values, and even the sign, may change depending on the formula used (Ulich, 2000; Jarvis et  
149 al., 2002). We conducted a test for the two stations here analyzed described in Section 3  
150 leading us to conclude that the Shimazaki formula is reasonable and reliable for the analysis  
151 outlined in this research.

152 In the case of M(3000)F2 monthly median data for Rome, from January 1960 to December  
153 2022, there are no missing values for the selected local times. For Juliusruh there are a total  
154 of 8 missing values that correspond to the monthly medians of May 1977, September-  
155 October-November 1978, October 1983, August 2009, July 2020 and January 2022, for both  
156 local times. We considered that the mean annual values are all representative considering that



157 the worst case is 1978 with only three months missing. In the case of foF2 for both stations,  
158 at 0 and 12 LT, there are no missing data in the monthly median records.

159

## 160 **2.2 Solar EUV proxies and geomagnetic activity data**

161 The five most commonly used solar EUV radiation proxies were employed together with the  
162 geomagnetic activity Ap index. The five selected proxies are:

163 (1) Magnesium II core-to-wing ratio (MgII) (Snow et al., 2014) represents the ratio of the h  
164 and k lines of the solar Mg II emission at 280 nm to the background solar continuum near  
165 280 nm. The annual mean time series was calculated as the average of daily values from the  
166 composite extended MgII series obtained from the University of Bremen at  
167 <https://www.iup.uni-bremen.de/UVSAT/data/>.

168 (2) Hydrogen Lyman  $\alpha$  flux ( $F\alpha$ ) (Machol et al., 2019) in  $W/m^2$  units that is the full disk  
169 integrated solar irradiance over 121-122 nm, dominated by the solar HI 121.6 nm emission.  
170 The annual mean time series was estimated as the average of daily values of the composite  
171 series sourced from the LASP Interactive Solar Irradiance Data Center, University of  
172 Colorado, at <https://lasp.colorado.edu/data/timed-see/composite-lya/lyman-alpha-composite.nc>.

173 (3) The revised sunspot number (SN). The annual mean values were directly obtained from  
174 SILSO (Sunspot Index and Long-term Solar Observations - Royal Observatory of Belgium,  
175 Brussels) accessible at <http://www.sidc.be/silso/datafiles>.

176 (4) F10.7 that is the flux density of radio emissions from the Sun at 10.7 cm wavelength  
177 (2800 MHz) in  $sfu=10^{-22}Ws/m^2$ , measured at the Earth's surface. The annual time series was  
178 estimated as the average of the monthly mean series available from Space Weather Canada  
179 at <https://spaceweather.gc.ca/forecast-prevision/solar-solaire/solarflux/sx-en.php>.

180 (5) F30 that is the flux density of radio emissions from the Sun at 30 cm wavelength (1000  
181 MHz), in  $sfu=10^{-22}Ws/m^2$ , measured at the Earth's surface. The annual mean time series was  
182 estimated as the average of daily values provided by the Nobeyama Radio Polarimeters  
183 (NoRP) at <https://solar.nro.nao.ac.jp/norp/index.html>.

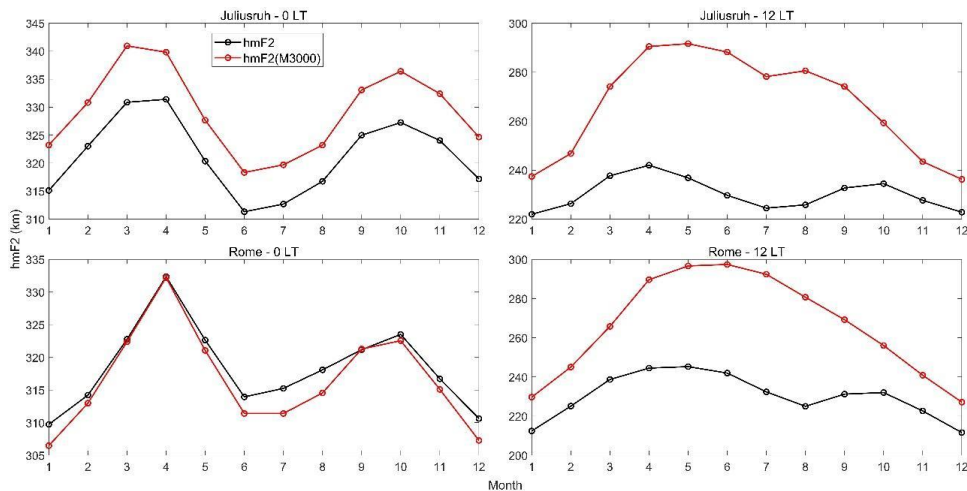
184 The geomagnetic activity index Ap annual mean series was estimated as the average of daily  
185 values supplied by the Kyoto World Data Center for Geomagnetism at  
186 <https://wdc.kugi.kyoto-u.ac.jp/index.html>.

187

## 188 **3. Testing the hmF2 Shimazaki formula for use in this analysis**

189 The Shimazaki formula to obtain hmF2 based only on M(3000)F2 is adequate at nighttime  
190 hours, when the ionization below the F2 region is weak. As this ionization begin to increase,  
191 this formula systematically overestimates hmF2. This can be seen in Figure 1 where the  
192 average of the monthly median hmF2 values along 2001-2022 is plotted in terms of month.  
193 At 0 LT a good agreement is noticed between the autoscaled and the Shimazaki heights,  
194 which declines in the case of 12 LT.

195



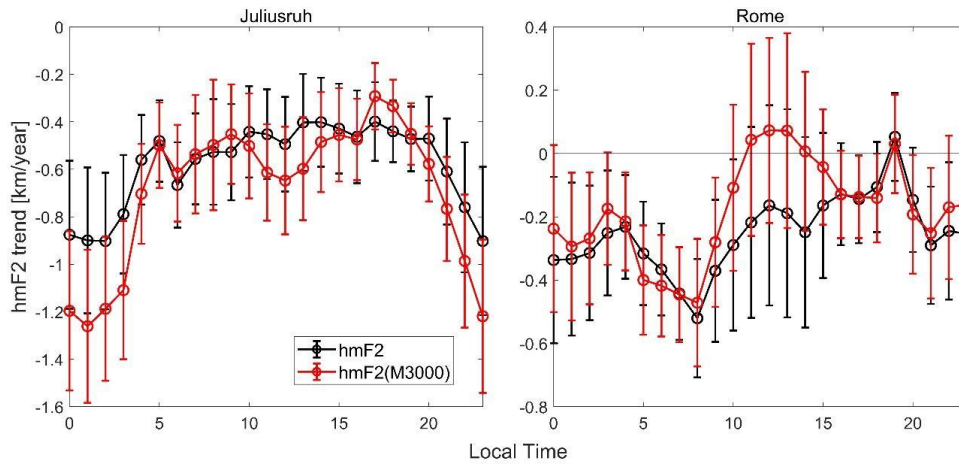
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197 **Figure 1.** hmF2 monthly median average along period 2001-2022 in terms of month, at  
198 Juliusruh (upper panels) and Rome (lower panels), at 0 LT (left panels) and 12 LT (right  
199 panels), considering autoscaled heights (black) and the values obtained using the Shimazaki  
200 formula (red).

201 However, the trend of the residuals, considering annual means for example, after filtering the  
202 solar activity effect are in good agreement for night and daytime, as can be noticed from  
203 Figure 2.

204 For this purpose, the simplest filtering was applied, that is considering the residuals of hmF2  
205 from a linear regression with MgII as the EUV solar proxy. There is a general good agreement  
206 in trend values, except in the case of Rome at noon when different signs are obtained between  
207 the autoscaled and Shimazaki hmF2 values. Despite this, we chose to carry out this study  
208 with the Shimazaki formula, given by Equation (1), considering that the errors are systematic  
209 and will not impact the results of the comparative analysis we aim to present. We further  
210 reference the findings of Scotto (2013) to support its use for trend analysis. His results were  
211 obtained for a simulation of nighttime hours with a superimposed trend of  $-14$  km/century  
212 on the hmF2 parameter, which indicate that regardless of the empirical formula used, the  
213 accuracy of hmF2 from ionosonde measurements would be adequate to detect this trend.





214

215 **Figure 2.** hmF2 trends (km/year) in terms of local time considering annual means of monthly  
 216 median autoscaled heights (black) and the values obtained using the Shimazaki formula (red),  
 217 for Juliusruh (left panel) and Rome (right panel), after filtering solar activity using a linear  
 218 regression on MgII. The error bars correspond to one standard deviation.

219

220 **4. Methodology to compare the different solar EUV proxies and Ap index roles on hmF2**  
 221 **trend analysis**

222 In order to compare the different solar EUV proxies' effects on the trend estimation process,  
 223 we repeat the filtering and trend calculations using each of the five proxies (MgII, F $\alpha$ , F10.7,  
 224 SN, and F30), which will be generically called X. The filtering, in turn, was performed  
 225 considering four models in order to analyze the effect of Ap, which are:

226 1) Linear regression on X:

227  $hmF2 = A + B X$  (2)

228 2) Second degree polynomial regression on X:

229  $hmF2 = A + B X + C X^2$  (3)

230 3) Linear regression on X and Ap:

231  $hmF2 = A + B X + D Ap$  (4)

232 4) Second degree polynomial regression on X and linear on Ap:

233  $hmF2 = A + B X + C X^2 + D Ap$  (5)

234 Thus, the regression variables in each model are: X for 1, X & X<sup>2</sup> for 2, X & Ap for 3, and  
 235 X, X<sup>2</sup> & Ap for 4.



236 The trend is estimated considering a linear regression of the residuals from these models,  
237  $\Delta hmF2$ , and time:

$$238 \quad \Delta hmF2 = [hmF2 - hmF2(\text{modeled})] = \alpha + \beta t \quad (6)$$

239 In order to determine each solar proxy and  $A_p$  suitability for the filtering process, and its  
240 effect on trend values, we considered the squared correlation coefficient,  $r^2$ , of each of the  
241 four models for each of the five solar proxies together with the values of the linear trend  
242 obtained in each case. A visual comparative analysis is made first by plotting the results  
243 obtained for each variable ( $r^2$  and trend values). This is followed by a quantitative comparison  
244 through the estimation of percentage differences considering F30 as the reference EUV solar  
245 proxy, and model 1 as the reference model.

246 The adjusted  $r^2$  value was considered because, in multiple regression, the  $r^2$  value increases  
247 as more predictors are added due to the way it is calculated. In contrast, the adjusted  $r^2$  value  
248 will decrease if the additional variables do not significantly improve the explanation of the  
249 dependent variables (foF2 and hmF2 in this case).

250 Concerning  $r^2$ , the percentage difference to compare the different solar proxies is estimated  
251 as

$$252 \quad 100 \times [r^2(X_i) - r^2(F30)] \quad (7)$$

253 where  $X_i = MgII, F\alpha, SN$  or F10.7, using only model 1; while the percentage difference to  
254 compare the different models is estimated as

$$255 \quad 100 \times [r^2(\text{model } i) - r^2(\text{model } 1)] \quad (8)$$

256 for model  $i$  from model 2 to model 4 using only F30 as the solar proxy.

257 The same applies to trend values, but relative percentage differences were assessed in this  
258 case, estimated as

$$259 \quad 100 \times [\beta(X_i) - \beta(F30)] / \beta(F30) \quad (9)$$

260 and

$$261 \quad 100 \times [\beta(\text{model } i) - \beta(\text{model } 1)] / \beta(\text{model } 1) \quad (10)$$

262 This analysis is repeated for foF2 to compare the effects of solar proxies and the inclusion of  
263  $A_p$ . Since the study is based on a similar analysis made by Laštovička (2021b, c) who  
264 considered the period 1976-2014, each calculation was also made for this period, and for  
265 1976-2022 that is Laštovička's period updated to 2022.

266

## 267 **5. Results**

268 Figures 3 and 4 present  $r^2$  for each model, at 0 and 12 LT respectively, in terms of each solar  
269 proxy, considering hmF2 and foF2 measured at Juliusruh. Figures 5 and 6 show the

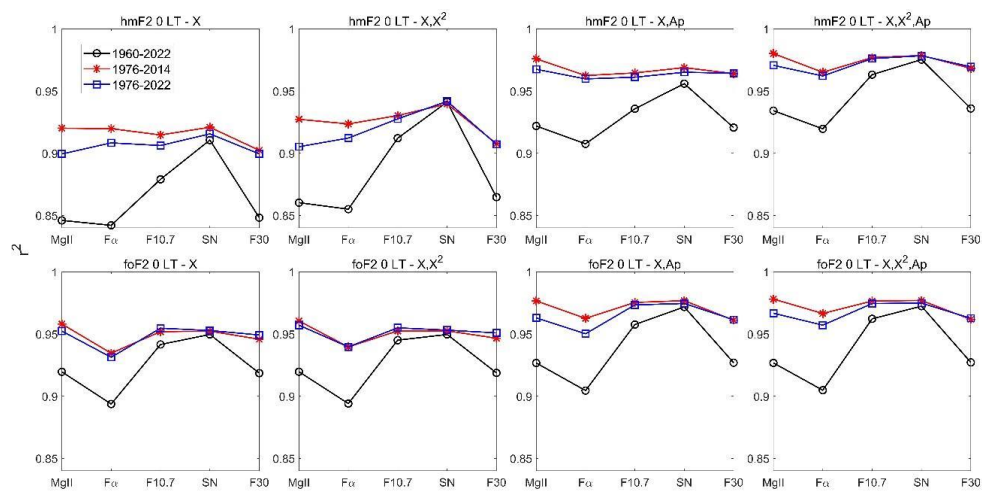




270 equivalent results for hmF2 and foF2 measured at Rome. It is easily noticed that the longest  
 271 period analyzed, 1960-2022, shows the greatest variations in  $r^2$  between each solar proxy,  
 272 with an improved correlation in the case of SN followed by F10.7 for all the models, at  
 273 midnight and noon, which nevertheless does not mean that should be considered the best  
 274 proxies (Laštovička, 2024; Zossi et al., 2024). For the shorter periods, particularly excluding  
 275 solar cycles 20 and 21, the difference in  $r^2$  values is smoothed and MgII emerge as the highest  
 276 correlated proxy for most of the cases.

277 Looking at the same figures, when comparing the different models in hmF2 case, the addition  
 278 of variables to model 1 improves the correlation, in particular when Ap is added, something  
 279 that in foF2 case is almost not noticed. We can argue that this is because there is more  
 280 potential for improvement in hmF2 compared to foF2, as the  $r^2$  value is, on average, lower  
 281 for hmF2.

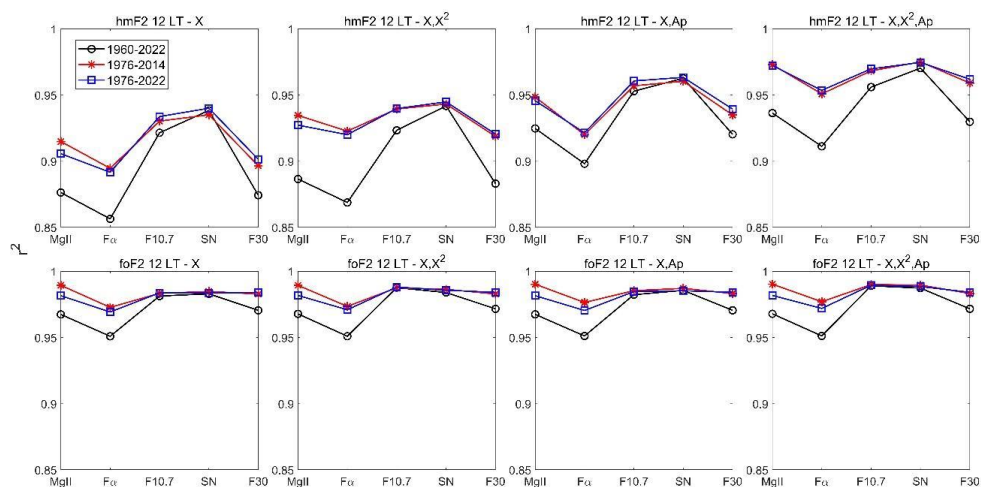
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283

284 **Figure 3.** Squared correlation coefficient,  $r^2$ , of hmF2 (upper panels) and foF2 (lower panels)  
 285 at 0 LT measured at Juliusruh, within each model (indicated at the top of each panel) in terms  
 286 of each solar proxy (MgII, F $\alpha$ , F10.7, SN and F30). Time series period: 1960-2022 (black),  
 287 1976-2014 (red), 1976-2022 (blue).

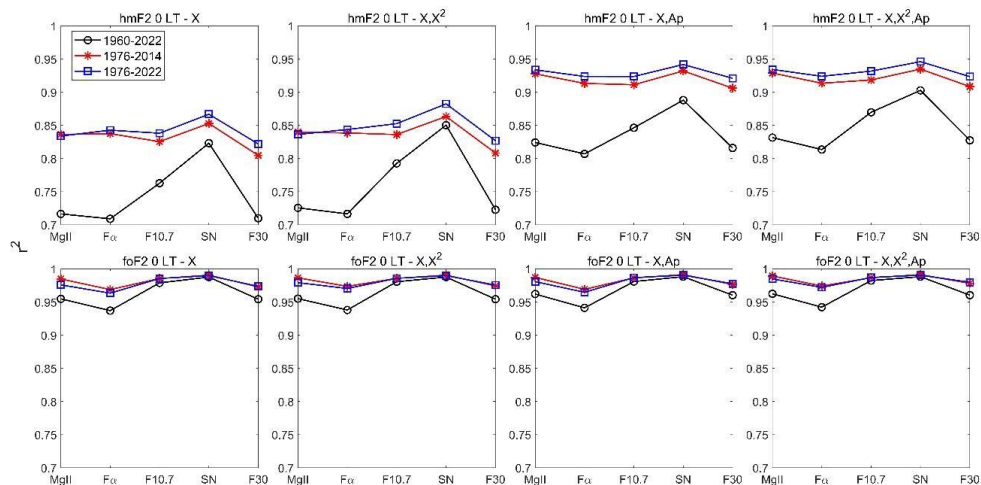
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289

290 **Figure 4.** Squared correlation coefficient,  $r^2$ , of hmF2 (upper panels) and foF2 (lower panels)  
 291 at 12 LT measured at Juliusruh, within each model (indicated at the top of each panel) in  
 292 terms of each solar proxy (MgII,  $F\alpha$ , F10.7, SN and F30). Time series period: 1960-2022  
 293 (black), 1976-2014 (red), 1976-2022 (blue).

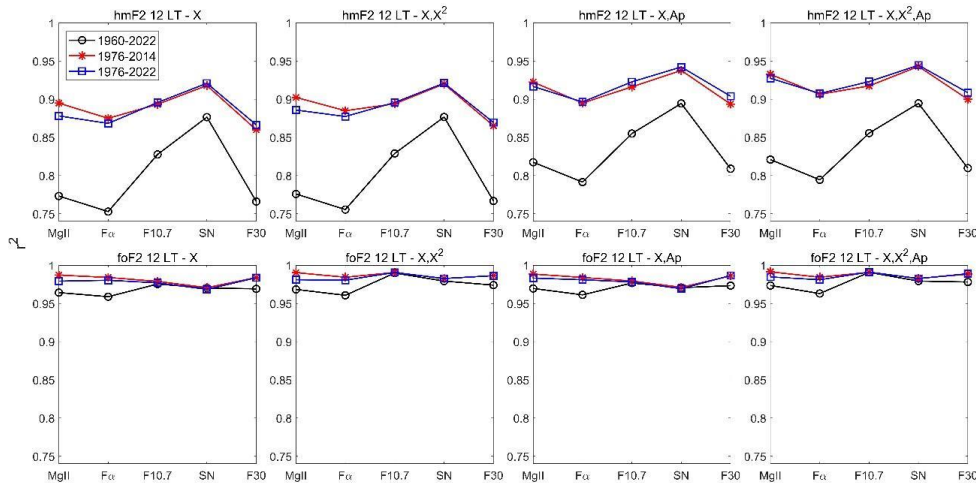
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295

296 **Figure 5.** Squared correlation coefficient,  $r^2$ , of hmF2 (upper panels) and foF2 (lower panels)  
 297 at 0 LT measured at Rome, within each model (indicated at the top of each panel) in  
 298 terms of each solar proxy (MgII,  $F\alpha$ , F10.7, SN and F30). Time series period: 1960-2022 (black),  
 299 1976-2014 (red), 1976-2022 (blue).

300



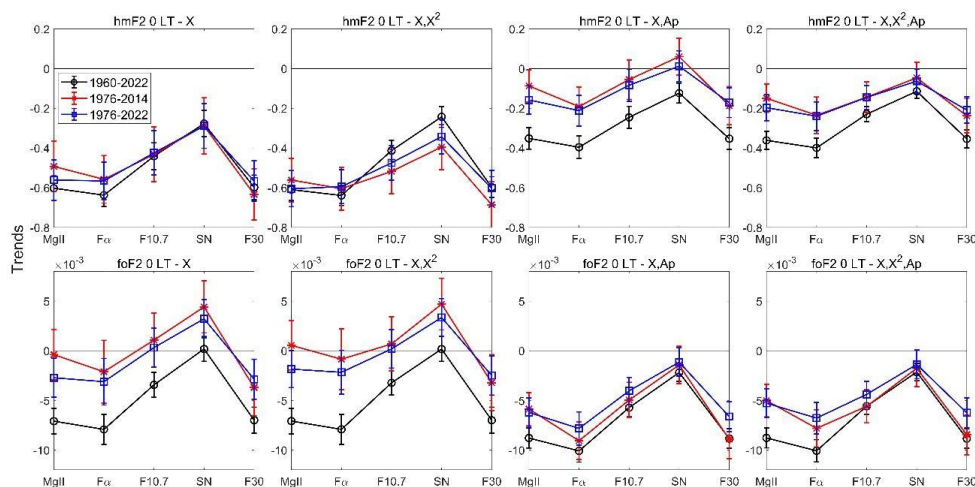
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302 **Figure 6.** Squared correlation coefficient,  $r^2$ , of hmF2 (upper panels) and foF2 (lower panels)  
 303 at 12 LT measured at Rome, within each model (indicated at the top of each panel) in terms of  
 304 each solar proxy (MgII,  $F\alpha$ , F10.7, SN and F30). Time series period: 1960-2022 (black),  
 305 1976-2014 (red), 1976-2022 (blue).

306

307 Figures 7 and 8 present trend values obtained after filtering through each of the four models,  
 308 at 0 and 12 LT respectively, in terms of each solar proxy, of hmF2 and foF2 measured at  
 309 Juliusruh. Figures 9 and 10 show the equivalent results for hmF2 and foF2 measured at Rome.  
 310 Similar to foF2 case, hmF2 trends are less negative when the solar proxy used is SN, followed  
 311 by F10.7. They are more negative when F30, MgII and  $F\alpha$  is used instead. In hmF2 case also,  
 312 the trends get less negative and closer to zero when Ap is included in the model, which is  
 313 something expected due to the increase obtained in  $r^2$ . foF2 trends are almost identical with  
 314 or without Ap included, which is in agreement with the results of other authors showing that  
 315 Ap do not make a significant difference if included in the filtering process (Laštovička,  
 316 2021a). It is worth noting that in hmF2 case there are almost no positive trends except two  
 317 exceptions: Juliusruh at 0 LT using SN as a proxy in model 3, for periods 1976-2014 and  
 318 1976-2022. While in foF2 case, positive trends are obtained for several cases all of which  
 319 use SN or F10.7 as the solar proxy.

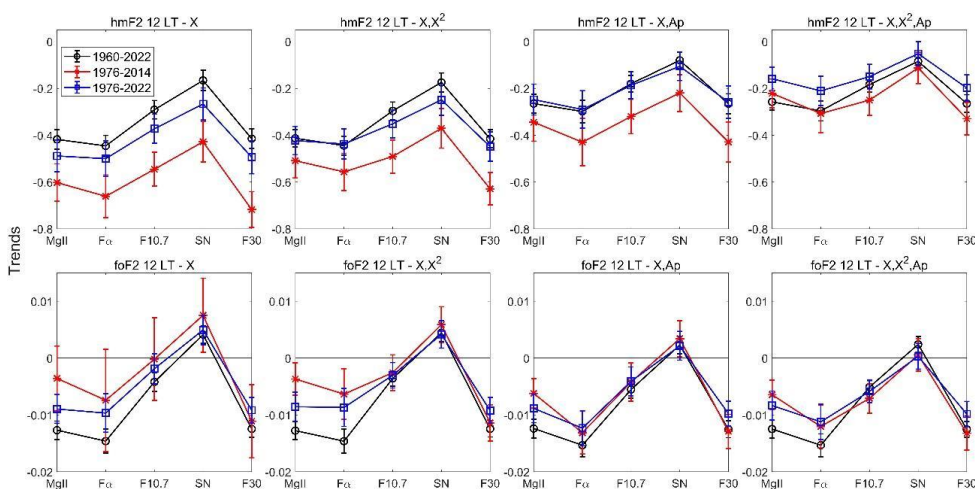
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321

322 **Figure 7.** Linear trend of hmF2 (upper panels) and foF2 (lower panels) at 0 LT measured at  
 323 Juliusruh, considering residuals filtered with each model (indicated at the top of each panel)  
 324 in terms of each solar proxy (MgII,  $F_{\alpha}$ , F10.7, SN and F30). Time series period: 1960-2022  
 325 (black), 1976-2014 (red), 1976-2022 (blue).

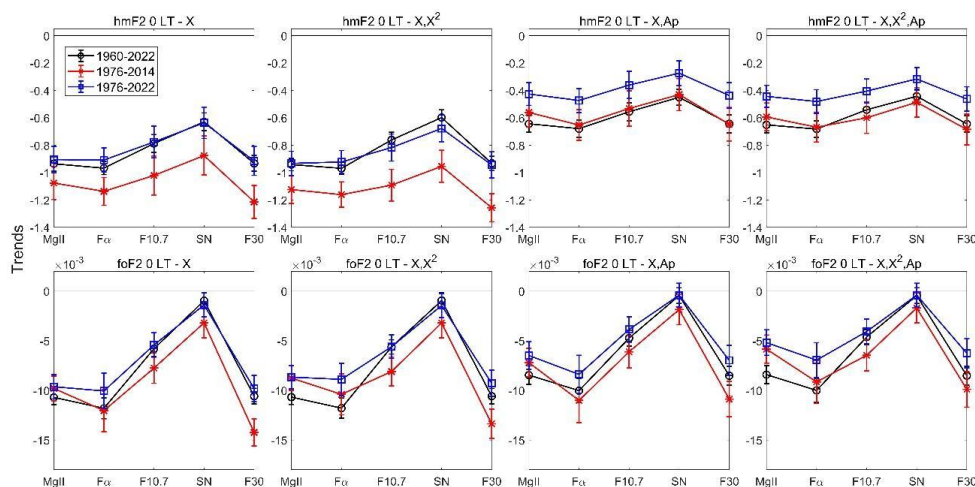
326



327

328 **Figure 8.** Linear trend of hmF2 (upper panels) and foF2 (lower panels) at 12 LT measured  
 329 at Juliusruh, considering residuals filtered with each model (indicated at the top of each  
 330 panel) in terms of each solar proxy (MgII,  $F_{\alpha}$ , F10.7, SN and F30). Time series period: 1960-  
 331 2022 (black), 1976-2014 (red), 1976-2022 (blue).

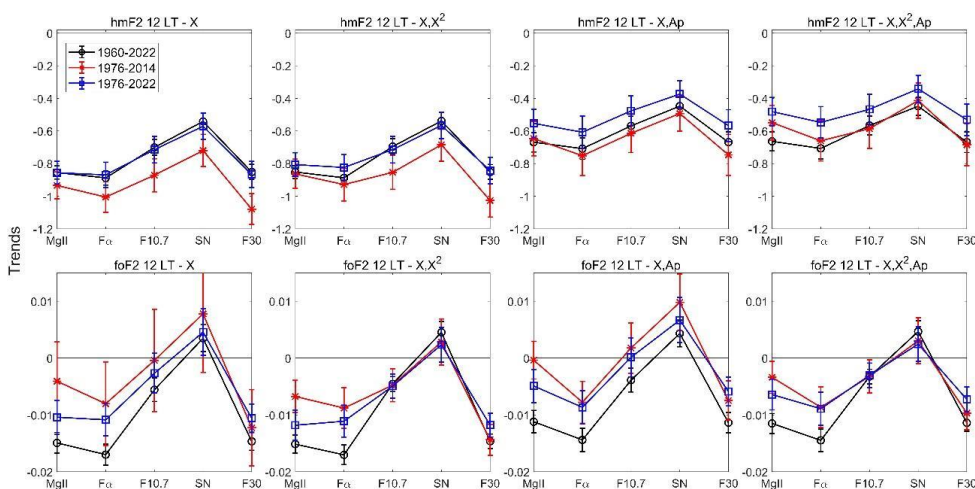
332



333

334 **Figure 9.** Linear trend of hmF2 (upper panels) and foF2 (lower panels) at 0 LT measured at  
 335 Rome, considering residuals filtered with each model (indicated at the top of each panel) in  
 336 terms of each solar proxy (MgII,  $F_{\alpha}$ , F10.7, SN and F30). Time series period: 1960-2022  
 337 (black), 1976-2014 (red), 1976-2022 (blue).

338



339

340 **Figure 10.** Linear trend of hmF2 (upper panels) and foF2 (lower panels) at 12 LT measured at  
 341 Rome, considering residuals filtered with each model (indicated at the top of each panel)  
 342 in terms of each solar proxy (MgII,  $F_{\alpha}$ , F10.7, SN and F30). Time series period: 1960-2022  
 343 (black), 1976-2014 (red), 1976-2022 (blue).

344

345 In order to have a more quantitative analysis of the differences of each solar proxy and of Ap  
 346 role on filtering we estimated  $r^2$  and trend differences with respect to proxies and also to



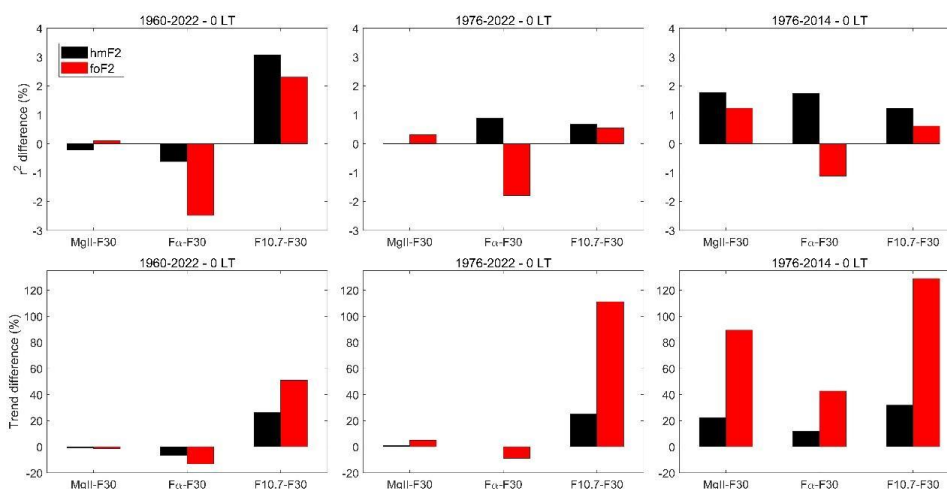
347 models as explained in Section 4. We do not show the case of SN in order to simplify the  
 348 figures, since its difference is highly notorious just from the Figures 3 to 10.

349 Figures 11 to 14 show the percentage difference in  $r^2$  together with the relative percentage  
 350 difference in trends when comparing F30 with each of the other proxies—MgII,  $F_{\alpha}$ , and  
 351 F10.7—for both hmF2 and foF2, for each station and local time.

352 In the case of  $r^2$  percentage difference, a positive value means a higher correlation, while a  
 353 negative value a lower one. In general, and leaving SN out of discussion in this point, F10.7  
 354 is the proxy that mostly improves  $r^2$  considering the two stations, both local times, and the  
 355 three periods. The are also cases of improvement when considering MgII. Again, we  
 356 highlight that this result does not imply a better performance of F10.7 and/or MgII  
 357 (Laštovička, 2024; Zossi et al., 2024).

358 In the case of the trend relative percentage differences, considering that the reference trend  
 359 is always negative, a positive value implies a less negative trend or even positive, while a  
 360 negative value indicates a more negative one. For the period 1960-2022, trend values are  
 361 similar either using F30 or MgII in hmF2 and foF2 cases, while in the shortest period 1976-  
 362 2014, F30 gives clearly the most negative trends in all the cases, with strongest effect in foF2.

363

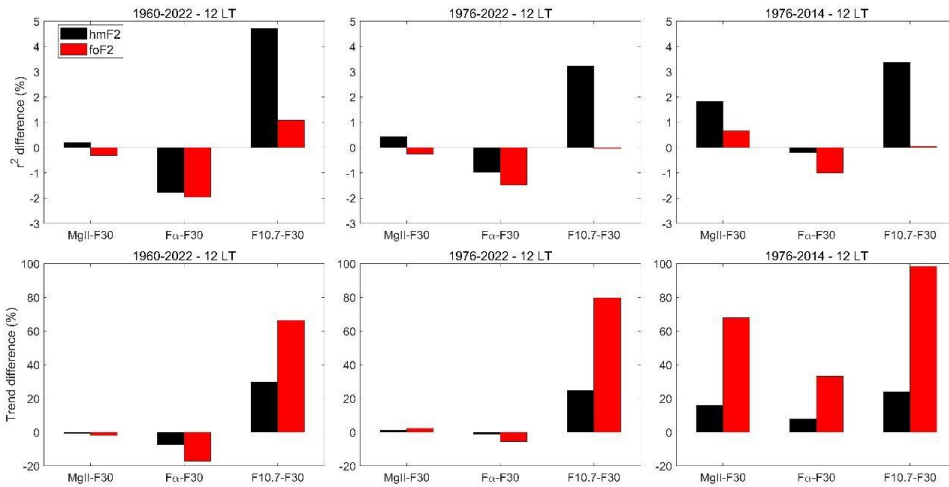


364

365 **Figure 11.**  $r^2$  percentage difference (upper panels) and trends relative percentage difference  
 366 (lower panels), using model 1, between MgII,  $F_{\alpha}$  or F10.7 and F30 for hmF2 (black bars)  
 367 and foF2 (red bars) measured at Juliusruh at 0 LT, considering periods 1960-2022, 1976-  
 368 2022, and 1976-2014, indicated at the top of each panel.

369

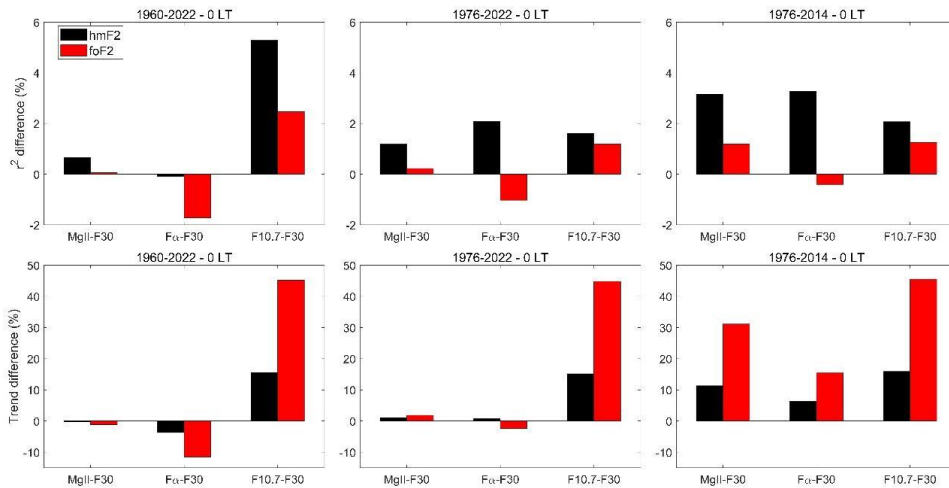




370

371 **Figure 12.**  $r^2$  percentage difference (upper panels) and trends relative percentage difference  
 372 (lower panels), using model 1, between MgII, F $\alpha$  or F10.7 and F30 for hmF2 (black bars)  
 373 and foF2 (red bars) measured at Juliusruh at 12 LT, considering periods 1960-2022, 1976-  
 374 2022, and 1976-2014, indicated at the top of each panel.

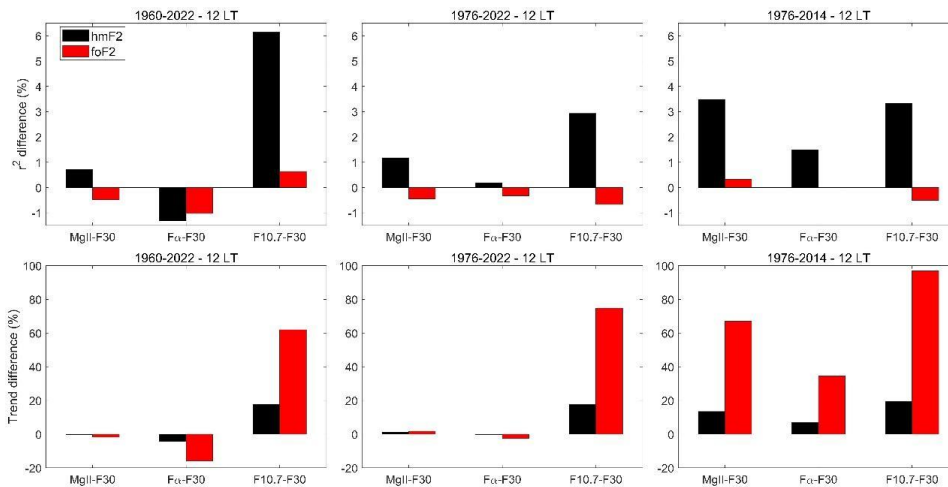
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376

377 **Figure 13.**  $r^2$  percentage difference (upper panels) and trends relative percentage difference  
 378 (lower panels), using model 1, between MgII, F $\alpha$  or F10.7 and F30 for hmF2 (black bars)  
 379 and foF2 (red bars) measured at Rome at 0 LT, considering periods 1960-2022, 1976-2022,  
 380 and 1976-2014, indicated at the top of each panel.





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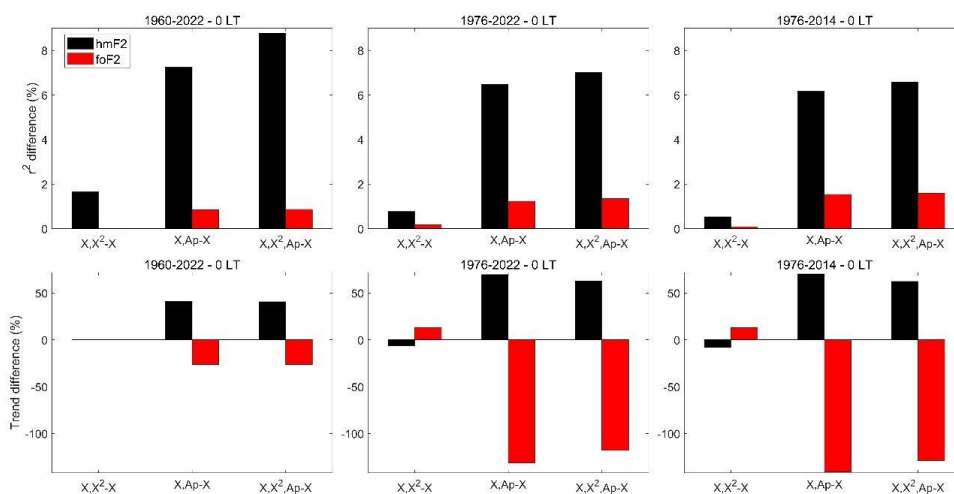
382 **Figure 14.**  $r^2$  percentage difference (upper panels) and trends relative percentage difference  
 383 (lower panels), using model 1, between MgII, F $\alpha$  or F10.7 and F30 for hmF2 (black bars)  
 384 and foF2 (red bars) measured at Rome at 12 LT, considering periods 1960-2022, 1976-2022,  
 385 and 1976-2014, indicated at the top of each panel.

386

387 Figures 15 to 18 show the percentage difference in  $r^2$  together with the relative percentage  
 388 difference in trends when comparing model 1 with each of the other models, for both hmF2  
 389 and foF2, at each station and local time.  $r^2$  differences are consistently greater for hmF2  
 390 compared to foF2 in all cases, meaning that adding the squared solar proxy term and/or the  
 391 Ap index always improve the model. Once more, this is statistically reasonable, since hmF2  
 392 has a larger margin for improvement. When a model, like that for foF2, already exhibits a  
 393 high degree of correlation, incorporating additional variables is less likely to result in  
 394 significant improvements. For example, at Juliusruh at 12 LT, neither the Ap index nor the  
 395 squared proxy term significantly enhances the foF2 model. This outcome is expected because  
 396 maximum solar activity levels typically do not surpass the saturation level, limiting  
 397 improvements in correlation for both ionospheric parameters.

398 In the case of the trend values, again the square term alone does not produce big differences,  
 399 while Ap weakens in the negative trends in all the cases except for one: foF2 at Juliusruh, 0  
 400 LT.

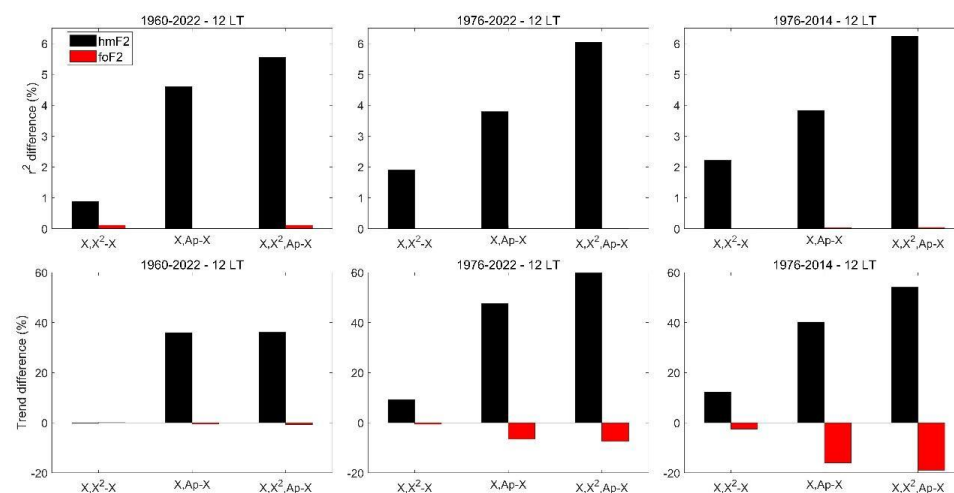
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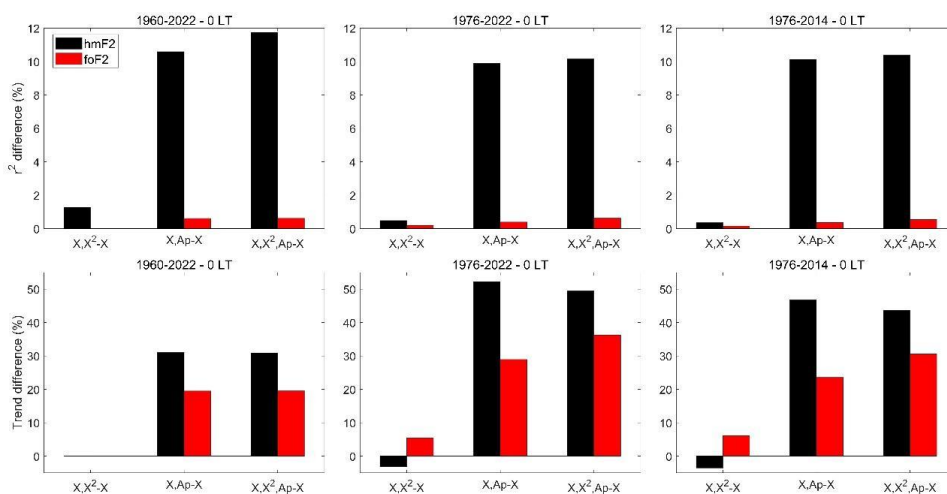
403 **Figure 15.**  $r^2$  percentage difference (upper panels) and trends relative percentage difference  
 404 (lower panels), using F30 as a solar proxy, between models 2, 3 or 4 and model 1 for hmF2  
 405 (black bars) and foF2 (red bars) measured at Juliusruh at 0 LT, considering periods 1960-  
 406 2022, 1976-2022, and 1976-2014, indicated at the top of each panel.

407



408

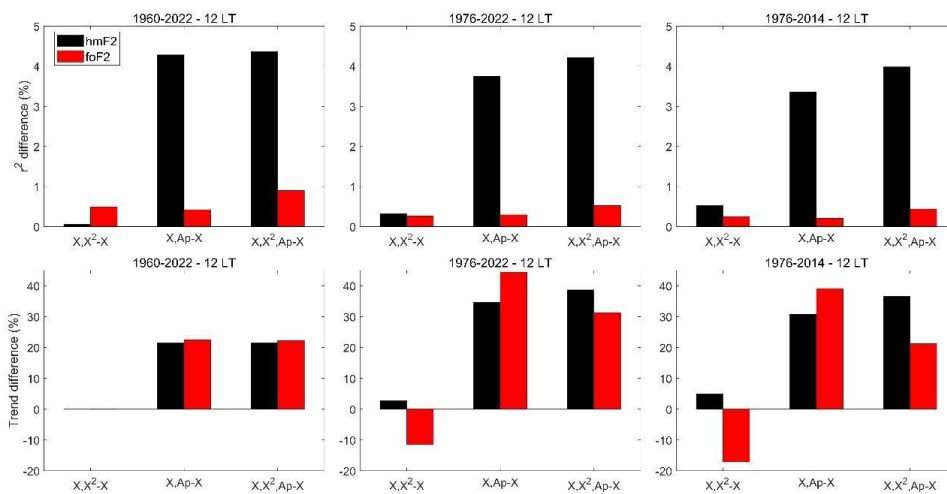
409 **Figure 16.**  $r^2$  percentage difference (upper panels) and trends relative percentage difference  
 410 (lower panels), using F30 as a solar proxy, between models 2, 3 or 4 and model 1 for hmF2  
 411 (black bars) and foF2 (red bars) measured at Juliusruh at 12 LT, considering periods 1960-  
 412 2022, 1976-2022, and 1976-2014, indicated at the top of each panel.



413

414 **Figure 17.**  $r^2$  percentage difference (upper panels) and trends relative percentage difference  
 415 (lower panels), using F30 as a solar proxy, between models 2, 3 or 4 and model 1 for hmF2  
 416 (black bars) and foF2 (red bars) measured at Rome at 0 LT, considering periods 1960-2022,  
 417 1976-2022, and 1976-2014, indicated at the top of each panel.

418



419

420 **Figure 18.**  $r^2$  percentage difference (upper panels) and trends relative percentage difference  
 421 (lower panels), using F30 as a solar proxy, between models 2, 3 or 4 and model 1 for hmF2  
 422 (black bars) and foF2 (red bars) measured at Rome at 12 LT, considering periods 1960-2022,  
 423 1976-2022, and 1976-2014, indicated at the top of each panel.

424

425

426



## 427 6. Discussion and conclusions

428 In order to analyze the effect of different solar EUV proxies on hmF2 trend estimation,  
429 following the works by Laštovička (2021b, 2021c), we implemented a similar analysis with  
430 some additions, to noon and midnight values. Noting that the correlation between hmF2 and  
431 solar EUV proxies was systematically lower than in foF2, the inclusion of Ap in the filtering  
432 process was incorporated to the analyses.

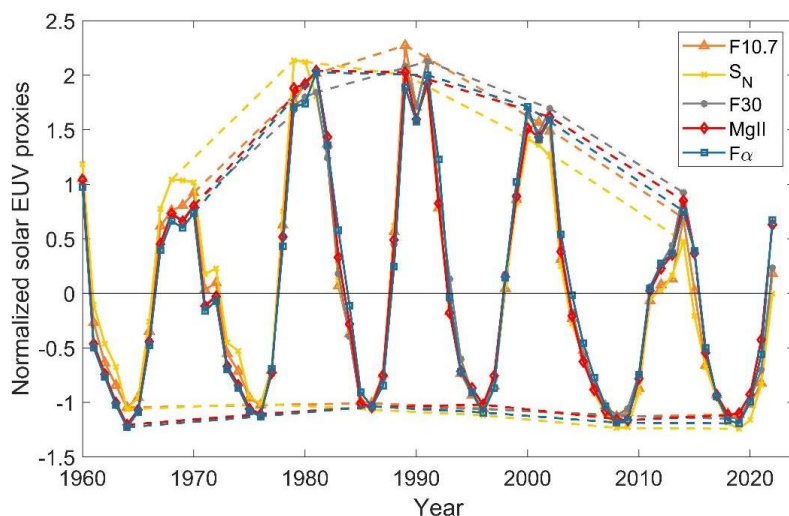
433 For both stations, both local times, and the three periods analyzed,  $r^2$  values between hmF2  
434 and the solar proxies considering different models which include or not Ap, are consistently  
435 lower compared to the corresponding foF2 cases. Thus, the variation in  $r^2$  values between  
436 different proxies, and between different models are stronger for hmF2, since there is more  
437 variance left out to be improved. In contrast, for foF2, the solar proxy linear term typically  
438 accounts for almost all the variation, leaving less than 5% of the variance unexplained.

439 However, with respect to trend values, the difference is more noticeable in foF2 case when  
440 comparing different proxies, but not when evaluating the addition or not of Ap. This suggests  
441 that foF2 trends seem more sensitive to the proxy used to filter solar activity effect. hmF2  
442 trends are also in general all negative and seem more stable than in foF2 case, probably  
443 related to the fact that the greenhouse effect is expected to be more clear in hmF2 than in  
444 foF2 (Rishbeth, 1990; Rishbeth and Roble, 1992).

445 An aspect which deserves further discussion is the comparison of our results between the  
446 three periods considered. Differences, in  $r^2$  and in trends as well, are more noticeable during  
447 the longest period: 1960-2022. This can be explained looking at the long-term variation of  
448 each solar proxy that is linked to the Gleissberg cycle, of ~80-100-year quasi-periodicity.  
449 Figure 19 highlights this more clearly by displaying the normalized annual mean values of  
450 the five proxies here considered, together with the envelope that joins the maximum and  
451 minimum values of each solar cycle in the period 1960-2022. The Gleissberg cycle is shown  
452 by the maximum values, having the most recent peak in cycle 22 (~1990). The increasing  
453 phase of this long-term cycle is clearly observed before cycle 22, followed by the beginning  
454 of the decreasing phase. While the well-known ~11-year cycle is quite similar for all the solar  
455 proxies, the Gleissberg cycle is not, being SN the index with the greatest differences. It is  
456 also clear from this figure that, while longer the period within the 1960-2022 interval, more  
457 differences are included since more maximum periods enter into the time series analyzed,  
458 and that could explain the stronger differences we found for the period 1960-2022 in  
459 comparison to the shorter ones in most of the cases.

460 A similar effect is produced by differences in the minimum epochs, but in the opposite sense.  
461 This is not supposedly part of the Gleissberg cycle, but it is clear that since the 1996 minimum  
462 epoch, the following minima present weaker indices' values in all the cases, but with different  
463 decreasing levels. Therefore, if the series starts closer to 1996, the trend will be more  
464 pronounced than if the time series begins earlier. Consequently, more significant differences  
465 should be observed in shorter periods, especially if they include one or both of the recent  
466 minima around ~2008 and ~2019.

467



468

469 **Figure 19.** MgII (red diamond), F $\alpha$  (blue square), F10.7 (orange triangle), S<sub>N</sub> (yellow cross)  
470 and F30 (gray dot) normalized annual means (period 1960-2022). Dashed lines join the  
471 maximum and minimum values of each solar cycle.

472

473 We bring back here Bremer (1992) conclusion where he mentions that an important demand  
474 is the correct filtering of the solar and geomagnetic influence on the data because it causes  
475 variations that are much larger than the trends of interest. We here emphasize this aspect of  
476 trend assessments showing once again that the problem is not yet fully resolved and deserves  
477 to be further and more deeply investigated and expanded.

478

#### 479 **Statements and Declarations**

480 The authors have no competing interests to declare that are relevant to the content of this  
481 article. Only Ana G. Elias, who is also an author of this work, is a member of the editorial  
482 board of *Annales Geophysicae*.

483

#### 484 **Acknowledgements**

485 T. Duran, Y. Melendi and F. Buezas acknowledge research project PGI 24/J089. A.G. Elias,  
486 B.S. Zossi and B.F. de Haro Barbas acknowledge research projects PIUNT E756 and PIP  
487 2957. Also, we acknowledge GIRO data resources  
488 <http://spase.info/SMWG/Observatory/GIRO>.

489

#### 490 **Data Availability**

491 Ionospheric M(3000)F2 and foF2 data for Rome and Juliusruh were obtained from the World  
492 Data Centre (WDC) for Space Weather, Australia, accessible at



493 <https://downloads.sws.bom.gov.au/wdc/iondata/au/> and from Damboldt and Suessman  
494 database available in the same WDC  
495 (<https://downloads.sws.bom.gov.au/wdc/iondata/medians/>). In the case of Rome, to extend  
496 the dataset until 2022, additional data were incorporated from the Digital Ionogram Data  
497 Base (DIDBase) at Lowell GIRO Data Center (LGDC). Juliusruh data is also available from  
498 the Leibniz-Institute of Atmospheric Physics at [https://www.ionosonde.iap-](https://www.ionosonde.iap-kborn.de/mon_fof2.htm)  
499 [kborn.de/mon\\_fof2.htm](https://www.ionosonde.iap-kborn.de/mon_fof2.htm). hmF2 autoscaled values for both stations were obtained from  
500 LGDC. MgII data is obtained from the University of Bremen at [https://www.iup.uni-](https://www.iup.uni-bremen.de/UVSAT/data/)  
501 [bremen.de/UVSAT/data/](https://www.iup.uni-bremen.de/UVSAT/data/); Hydrogen Lyman  $\alpha$  flux is accessible from the LASP Interactive  
502 Solar Irradiance Data Center, University of Colorado, at  
503 [https://lasp.colorado.edu/data/timed\\_see/composite\\_lya/lyman\\_alpha\\_composite.nc](https://lasp.colorado.edu/data/timed_see/composite_lya/lyman_alpha_composite.nc); SN  
504 annual mean values were directly obtained from SILSO (Sunspot Index and Long-term Solar  
505 Observations - Royal Observatory of Belgium, Brussels) sourced at  
506 <http://www.sidc.be/silso/datafiles>; F10.7 series are provided by Space Weather Canada at  
507 <https://spaceweather.gc.ca/forecast-prevision/solar-solaire/solarflux/sx-en.php>; F30 is  
508 available from the Nobeyama Radio Polarimeters (NoRP) at  
509 <https://solar.nro.nao.ac.jp/norp/index.html>. Ap index was obtained from the Kyoto World  
510 Data Center for Geomagnetism at <https://wdc.kugi.kyoto-u.ac.jp/index.html>.

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