Sensitivity of the tropical Atlantic to vertical mixing in two ocean models (ICON-O v2.6.6 and FESOM v2.5)

Swantje Bastin¹, Aleksei Koldunov², Florian Schütte⁴, Oliver Gutjahr¹, Marta Agnieszka Mrozowska³, Tim Fischer⁴, Radomyra Shevchenko¹, Arjun Kumar¹, Nikolay Koldunov², Helmuth Haak¹, Nils Brüggemann¹, Rebecca Hummels⁴, Mia Sophie Specht¹, Johann Jungclaus¹, Sergey Danilov², Marcus Dengler⁴, and Markus Jochum³

¹Max Planck Institute for Meteorology, Hamburg, Germany
²Alfred Wegener Institute, Bremerhaven, Germany
³Niels Bohr Institute, University of Copenhagen, Copenhagen, Denmark
⁴GEOMAR Helmholtz Centre for Ocean Research Kiel, Kiel, Germany

Correspondence: Swantje Bastin (swantje.bastin@mpimet.mpg.de)

Abstract. Ocean General Circulation Models still have large upper-ocean biases e.g. in tropical sea surface temperature, possibly connected to the representation of vertical mixing. In earlier studies, the ocean vertical mixing parameterisation has usually been tuned for a specific site or only within a specific model. We present here a systematic comparison of the effects of changes in the vertical mixing scheme in two different global ocean models, ICON-O and FESOM, run at a horizontal resolution of 10 km in the tropical Atlantic. We test two commonly used vertical mixing schemes; the K-Profile Parameterisation (KPP) and the Turbulent Kinetic Energy (TKE) scheme. Additionally, we vary tuning parameters in both schemes, and test the addition of Langmuir turbulence in the TKE scheme. We show that the biases of mean sea surface temperature, subsurface temperature, subsurface currents and mixed layer depth differ more between the two models than between runs with different mixing scheme settings within each model. For ICON-O, there is a larger difference between TKE and KPP than for FESOM. In both models, varying the tuning parameters hardly affects the pattern and magnitude of the mean state biases. For the representation of smaller scale variability like the diurnal cycle or inertial waves, the choice of the mixing scheme can matter: the diurnally enhanced penetration of equatorial turbulence below the mixed layer is only simulated with TKE, not with KPP. However, tuning of the parameters within the mixing schemes does not lead to large improvements for these processes. We conclude that a substantial part of the upper ocean tropical Atlantic biases is not sensitive to details of the vertical mixing scheme.

1 Introduction

The sea surface temperature (SST) in the tropics has a major influence on both the local and global atmospheric circulation and climate. Because it affects the location and strength of atmospheric convection, it influences large-scale tropical wind and precipitation patterns, especially over the surrounding continents (e.g. Rouault et al., 2003; Okumura and Xie, 2004; Kucharski et al., 2009; Giannini et al., 2004; Crespo et al., 2019). By controlling tropical convection, the tropical Atlantic SST can also influence extratropical climate via teleconnections (e.g. Sardeshmukh and Hoskins, 1988; Cassou et al., 2005). However,
tropical oceans are poorly represented in General Circulation Models (GCMs) (e.g. Toniazzo and Woolnough, 2014; Richter, 2015; Lübbecke et al., 2018; Richter and Tokinaga, 2020). Models usually suffer from a warm SST bias in the eastern tropical Atlantic associated with a too weak and delayed Equatorial Cold Tongue, as well as a cold SST bias in the western tropical oceans, leading to a reversed zonal SST gradient in boreal summer compared to observations (Davey et al., 2002; Richter and Xie, 2008; Richter, 2015; Richter and Tokinaga, 2020). In the atmosphere, the GCMs generally show weaker than observed trade winds, which is strongly coupled to the erroneous SST gradient through the Bjerknes feedback (e.g. Bjerknes, 1969; Keenlyside and Latif, 2007). It has been suggested that the weak trade wind bias and thus also the SST bias mostly originates from the atmospheric component of the GCMs, because the trade wind bias peak appears earlier than the peak of the zonal SST gradient bias (Richter and Xie, 2008). Additionally, atmosphere-only models also have been shown to have too weak Atlantic trade winds (e.g. Zermeño-Diaz and Zhang, 2013; Richter et al., 2014). However, uncoupled ocean general circulation models (OGCMs) generally show similar SST biases as the coupled GCMs (e.g. Song et al., 2015; Tsujino et al., 2020; Zhang et al., 2022). These studies suggest that both the oceanic and atmospheric components contribute to the strong tropical biases in the coupled models, which are then amplified by the Bjerknes feedback. Some studies have shown that tropical biases decrease in coupled models with high atmospheric resolution (e.g. Milinski et al., 2016; Harlaß et al., 2018) and high oceanic resolution (e.g. Seo et al., 2007; Small et al., 2014).

Apart from horizontal resolution, one important oceanic process that controls tropical SST is vertical turbulent mixing (e.g. Jochum and Potemra, 2008; Moum et al., 2013; Hummels et al., 2014, 2020). It affects the vertical temperature distribution by inducing down-gradient temperature (as well as other tracer and momentum) fluxes when turbulence energy is available, thus influencing e.g. the SST, air-sea heat fluxes, the thickness of the surface mixed layer, and the diapycnal heat transport across the bottom of the mixed layer. Vertical turbulent mixing is important e.g. for the seasonal cycle of the tropical Atlantic SST, namely the development of the Atlantic Cold Tongue (ACT). The ACT develops in the eastern equatorial Atlantic in boreal summer, when the trade winds intensify due to the northward shift of the Intertropical Convergence Zone (ITCZ). The stronger trade winds in turn intensify the westward-flowing surface current, which increases the shear with the underlying eastward-flowing Equatorial Undercurrent (EUC). This shear enhances vertical turbulent mixing, which cools the surface mixed layer temperature from below (Hummels et al., 2014; Lübbecke et al., 2018). Vertical turbulent mixing also plays a role for tropical Atlantic variability on smaller than seasonal time scales, for example the diurnal cycle of the near-surface temperature distribution (e.g. Smyth et al., 2013; Moum et al., 2022).

Vertical turbulent mixing is a subgrid-scale process even at high vertical resolution, and therefore needs to be parameterised in ocean models. Several parameterisations of varying complexity are available, either based on empirical considerations or attempting a statistical closure of the fluctuation correlations of the Reynolds-averaged governing equations (Burchard and Bolding, 2001). Statistical closures, in principle, consist of an infinite number of differential equations which are truncated after the first few equations for computational efficiency (Burchard and Bolding, 2001). OGCMs mostly use first order turbulence schemes because higher-order schemes are too computationally expensive. Frequently used vertical mixing schemes in OGCMs include the Richardson number dependent PP scheme (Pacanowski and Philander, 1981), the empirical K-profile
Because vertical mixing affects the SST and thus air-sea heat exchange, improvements in its representation in ocean models could contribute to a reduction of the long-standing biases in the models’ tropical SST and climate. One way to improve vertical mixing in ocean models is to tune parameters that are not well constrained by observations, another way is using a different parameterisation. Li et al. (2001) showed that the KPP scheme led to a better representation of the tropical Pacific than the PP scheme, and Blanke and Delecluse (1993) showed that the TKE scheme performs better than the PP scheme, especially for the simulation of the Equatorial Undercurrents. Concerning parameter tuning, Deppenmeier et al. (2020) for example showed that increasing the $c_k$ parameter in the TKE scheme leads to reduced SST biases in the tropical oceans, and Zhang et al. (2022) could reduce the tropical Atlantic subsurface warm bias by increasing the interior ocean background diffusivity in the KPP scheme. However, these studies only assess a specific bias, limiting their transferability. Gutjahr et al. (2021) did a broader (global) investigation of the differences between four different vertical mixing schemes: PP, KPP, TKE, and TKE+Idemix. They conclude that the optimal choice of the mixing scheme depends on the region and the variable. In their simulations, the large-scale SST bias was insensitive to changes in the vertical mixing scheme. For all of these studies, transferring their results to other models is difficult because they refer to only one particular model. Moreover, remaining biases in all studies might also be due to model errors other than the vertical mixing scheme. To alleviate this, we use here two different ocean models, FESOM and ICON-O, and perform coordinated sensitivity experiments to compare the performance of two commonly used state-of-the-art OGCM vertical mixing schemes (KPP and TKE), as well as the effect of different parameter choices for each of the two schemes.

We focus on the tropical Atlantic because there are several current observational programs with a focus on tropical Atlantic climate. Data that we use to validate the models include hydrographic measurements from Argo floats (Argo, 2022), data from the Prediction and Research Moored Array in the Tropical Atlantic (PIRATA, Bourlès et al., 2019), and data collected during multiple cruises in the tropical Atlantic.

The remainder of the manuscript is organized as follows. In Section 2, we provide a description of the two ocean models that we use for this study, followed by a description of the KPP and TKE mixing schemes in Section 3. The following sections show the results of our mixing scheme and parameter comparisons. We first assess the effect of the vertical mixing parameterisation and its parameter settings on different large-scale features of the tropical Atlantic upper ocean. Among these are the mean mixed layer depth (Section 4.1), the mean surface and vertical temperature structure as well as the seasonal evolution of the surface temperature e.g. in the Atlantic cold tongue region (Section 4.2), and the mean equatorial current systems (Section 4.3). In addition to the mean representation of the upper tropical Atlantic, we assess the representation of small-scale variability in the different model runs, including Near-Inertial Waves (Section 5.1), and the upper ocean diurnal cycle (Section 5.2). Finally, to put the sensitivity to mixing into perspective, we investigate the effect of different sets of default atmospheric forcing bulk formulae in ICON-O and FESOM (Section 6).
2 Model descriptions

We use two different ocean models, which are both part of the European Union Horizon 2020 NextGEMS project’s model development effort: the ocean component (Korn et al., 2022) of the ICON Earth System Model (Jungclaus et al., 2022) and the ocean model FESOM (Danilov et al., 2017; Scholz et al., 2019, 2022), which is coupled to the atmosphere model IFS for NextGEMS. The two ocean models will be described in the following, as well as their setup for this study.

2.1 FESOM

FESOM2 is a global unstructured-mesh ocean model developed at the Alfred Wegener Institute, Helmholtz Centre for Polar and Marine Research (AWI) in Bremerhaven (Danilov et al., 2017). It is formulated on a triangular mesh, utilizes a finite-volume dynamical core and Arbitrary Lagrangian–Eulerian (ALE) vertical coordinates (Scholz et al., 2019). The model has a computational performance comparable to structured-mesh models (Koldunov et al., 2019) and its unstructured nature enables different types of local mesh refinements (e.g. one that follows local sea surface height variability, Sein et al., 2017). FESOM2 uses the FESIM sea ice model (Danilov et al., 2015), it uses zero-layer thermodynamics (Semtner, 1976) and includes an EVP solver. For this study we use a FESOM2 mesh that has 50 km resolution over most of the globe, except for the equatorial Atlantic, where it is set to 13 km resolution. The horizontal grid is different in ICON-O, where the resolution is approximately globally uniform; however, we still argue that the two models are comparable as we only compare results from our region of interest, i.e. the tropical Atlantic. In FESOM we use a $z^*$ vertical coordinate, where the total change in SSH is distributed equally over all layers, except the layer that touches the bottom.

2.2 ICON-O

ICON-O (Korn et al., 2022) is the ocean component of the Icosahedral Nonhydrostatic Weather and Climate Model (ICON) in its Earth System Model configuration (ICON-ESM, Jungclaus et al., 2022). It is developed at the Max Planck Institute for Meteorology (MPI-M) in Hamburg. The ocean component of ICON-ESM, ICON-O, solves the hydrostatic (the “Nonhydrostatic” in the name only refers to the atmospheric component) Boussinesq equations with a free surface. These equations are solved on a triangular horizontal grid, which is generated by dividing the spherical domain into an icosahedron and subsequent division of the 12 icosahedron parts into triangles. In this study, an ICON grid with globally approximately uniform horizontal resolution of about 10km is used. In the vertical, a $z^*$ coordinate is used where model levels follow the free surface. For details on the numerics or other specifics about ICON-O, see Korn (2017) and Korn et al. (2022).

2.3 Common settings and experiment descriptions

To run the coordinated sensitivity experiments, we agreed on a common vertical axis with 128 vertical levels, with thicknesses ranging from 2 m near the surface to about 200 m near the seafloor. We also agreed to use the same vertical mixing schemes (TKE and KPP), as well as the same parameter settings. To make sure that our implementations of the TKE and KPP schemes are comparable, we use the versions provided by the CVMix (Community ocean Vertical Mixing) project, which has developed
a library of standardised vertical mixing parameterisations to be used in ocean models (Griffies et al., 2015; Van Roekel et al., 2018). In the TKE scheme, we vary the $c_k$ parameter (see Section 3.1, Eq. 2). For the KPP scheme, we run the models once with the default setting of $Ri_{crit} = 0.3$, and once with a reduced value of $Ri_{crit} = 0.27$. We do this because the best value for the critical bulk Richardson number is resolution dependent (e.g. Large et al., 1994): the finer the vertical resolution, the closer the critical bulk Richardson number should be to the theoretical critical value for the gradient Richardson number, which is 0.25. All model runs with their parameter settings are listed in Table 1.

We force all model runs with hourly ERA5 reanalysis (Hersbach et al., 2020), and run them from the end of the 5-year spinup with adjusted mixing parameter settings for two years (2014 and 2015). Of these, we analyse only the second year when the upper ocean has sufficiently adjusted to the changed mixing settings. The year 2015 was chosen because a particularly strong Near-Inertial Wave (NIW) mixing event occurred in that year and was observed during a RV Meteor cruise in the tropical North Atlantic, as described and analysed by Hummels et al. (2020). We want to compare this unique set of observations against our models to assess whether they can reproduce deep reaching NIW mixing events like the one in 2015.

Although we tried to homogenise the model settings between FESOM and ICON-O that are directly connected to the representation of vertical mixing, we left the rest of the model settings as they are commonly used in the FESOM and ICON-O communities at our institutes, i.e. partly different between the two models. This is intended and part of the reason why we do this study, to see how much of the variation between the different vertical mixing settings is model specific and how much happens similarly in both models. A relevant difference between ICON-O and FESOM is the parameterisation of the surface fluxes, for which different bulk formulae are used for the ERA5 forcing. To investigate the effect of the bulk formulae, we did an additional run with ICON-O using the standard FESOM bulk formulae. The default bulk formulae in ICON-O for the ERA5 forcing are those of Kara et al. (2002) over ocean and sea ice, with water vapor pressure and 2 m specific humidity calculated using the (modified) equations from Buck (1981) and longwave radiation calculated using Berliand (1952). FESOM instead uses bulk formulae calculated according to Large and Yeager (2009) over the ocean and with constant bulk exchange coefficients over sea ice, as described in Tsujino et al. (2018). These are also implemented in ICON-O, but usually only used together with JRA55-do forcing (Tsujino et al., 2018). For more details on ICON-O’s standard bulk formulae with ERA5-forcing, see Section A in the Appendix.

3 Description of vertical mixing schemes

3.1 TKE scheme

The TKE scheme (Gaspar et al., 1990) is a commonly used vertical mixing scheme in OGCMs. The scheme that Gaspar et al. (1990) propose is based on the turbulence closure schemes of Mellor and Yamada (1974), which requires solving a prognostic turbulent kinetic energy (TKE) equation. Gaspar et al. (1990) adapted the scheme for the ocean and used a new formulation for the mixing length which had been developed by Bougeault and André (1986) and Bougeault and Lacarrere (1989).
Table 1. Overview of model runs used in this study

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Model</th>
<th>Mixing scheme</th>
<th>Parameter settings</th>
</tr>
</thead>
<tbody>
<tr>
<td>F_TKE_01</td>
<td>FESOM</td>
<td>TKE</td>
<td>$c_k = 0.1$</td>
</tr>
<tr>
<td>F_TKE_02</td>
<td>FESOM</td>
<td>TKE</td>
<td>$c_k = 0.2$</td>
</tr>
<tr>
<td>F_TKE_03</td>
<td>FESOM</td>
<td>TKE</td>
<td>$c_k = 0.3$</td>
</tr>
<tr>
<td>F_KPP_030</td>
<td>FESOM</td>
<td>KPP</td>
<td>$R_{icrit} = 0.3$</td>
</tr>
<tr>
<td>F_KPP_027</td>
<td>FESOM</td>
<td>KPP</td>
<td>$R_{icrit} = 0.27$</td>
</tr>
<tr>
<td>I_TKE_01</td>
<td>ICON-O</td>
<td>TKE</td>
<td>$c_k = 0.1$</td>
</tr>
<tr>
<td>I_TKE_02</td>
<td>ICON-O</td>
<td>TKE</td>
<td>$c_k = 0.2$</td>
</tr>
<tr>
<td>I_TKE_03</td>
<td>ICON-O</td>
<td>TKE</td>
<td>$c_k = 0.3$</td>
</tr>
<tr>
<td>I_KPP_030</td>
<td>ICON-O</td>
<td>KPP</td>
<td>$R_{icrit} = 0.3$</td>
</tr>
<tr>
<td>I_KPP_027</td>
<td>ICON-O</td>
<td>KPP</td>
<td>$R_{icrit} = 0.27$</td>
</tr>
<tr>
<td>I_TKE_02_Langmuir</td>
<td>ICON-O</td>
<td>TKE</td>
<td>$c_k = 0.2$, additional Langmuir parameterisation (Axell, 2002)</td>
</tr>
<tr>
<td>I_TKE_02_minTKE</td>
<td>ICON-O</td>
<td>TKE</td>
<td>$c_k = 0.2$, minimum background TKE = $10^{-5}$ J/kg (default: $10^{-6}$ J/kg)</td>
</tr>
<tr>
<td>I_TKE_02_minKv</td>
<td>ICON-O</td>
<td>TKE</td>
<td>$c_k = 0.2$, minimum background diffusivity = $10^{-5}$ m$^2$/s (viscosity = $10^{-4}$ m$^2$/s)</td>
</tr>
<tr>
<td>I_TKE_02_FBF</td>
<td>ICON-O</td>
<td>TKE</td>
<td>$c_k = 0.2$, FESOM default bulk formulae</td>
</tr>
</tbody>
</table>

The TKE scheme uses the classical eddy diffusivity concept to parameterise the turbulent vertical fluxes, assuming for example for temperature:

$$-T'w' = k_v \cdot \frac{\partial T}{\partial z}$$ (1)

where $T$ denotes temperature, $w$ the vertical velocity, the overbar means a time mean and the dash means deviations from this mean as obtained by Reynolds averaging. Hence, $-T'w'$ is the turbulent vertical flux of temperature, and this is parameterised by assuming that the small scale turbulence behaves like diffusion and using the (vertical) eddy diffusivity $k_v$. The same can be done for the turbulent vertical flux of velocity $u$ using the (vertical) eddy viscosity $A_v$.

The eddy viscosity and diffusivity can be obtained from the turbulent kinetic energy (TKE) as follows:

$$A_v = c_k \cdot L_{mix} \cdot E_{tke}^{1/2}$$ (2)

and

$$k_v = A_v / Pr$$ (3)

where $c_k$ is a constant, $L_{mix}$ is the mixing length, $E_{tke}$ is the turbulent kinetic energy, and $Pr$ is the turbulent Prandtl number. It is unclear what value is best for $c_k$, and part of this study is to look at the effect of varying it. Gaspar et al. (1990) suggest a value of $c_k = 0.1$, and observational values of the mixing efficiency in the ocean which $c_k$ depends on suggest that it should not be larger than 0.3 (Deppenmeier et al., 2020). However, higher values have been tried, e.g. 0.5 by Deppenmeier et al.
The turbulent Prandtl number $Pr$ is just set to 1 in Gaspar et al. (1990), but can also be set to vary with the Richardson number $Ri$. We use the CVMix default of $Pr = 6.6Ri$. The mixing length $L_{mix}$ can be thought of as the maximum length that a particle can be moved against the stratification by the turbulent motion, and thus it depends on the kinetic energy of the turbulent motion and on the stratification of the surrounding water. The turbulent kinetic energy $E_{tke}$ is determined by the prognostic TKE equation, which is integrated by the model together with the primitive equations.

The breaking of internal waves in the ocean interior is parameterised by setting a constant minimum value of TKE. The diffusivity is then still dependent on $N^2$. We use a constant minimum TKE value of $E_{tke,min} = 10^{-6} \text{ m}^2 \text{ s}^{-2}$, as suggested in Gaspar et al. (1990). Additionally, we do a test run with an enhanced minimum TKE value of $E_{tke,min} = 10^{-5} \text{ m}^2 \text{ s}^{-2}$, as well as a different test run with a minimum background diffusivity and viscosity, which then do not depend on $N^2$. These two runs were only done with ICON-O to save computational expenses.

Another ICON-O run was done with an additional extension of the TKE scheme: the parameterisation of Langmuir turbulence (Axell, 2002). Langmuir turbulence, which is generated through the interaction of wind-driven surface currents and wind-generated surface waves, is responsible for additional turbulent energy input into the upper ocean, and it has been shown to be important over much of the global ocean area (e.g. Belcher et al., 2012). Since we do not simulate surface waves with ICON-O, the effect of the Langmuir turbulence is missing if it is not parameterised. A limitation of the Langmuir turbulence scheme used here is that the Stokes drift is estimated from the wind stress, because there are no waves in the model.

### 3.2 KPP scheme

The nonlocal K-Profile Parameterization (KPP, Large et al., 1994) is based on specifying vertical profiles of the eddy diffusivity and viscosity in the ocean boundary layer. As in the TKE scheme, the eddy diffusivity concept is applied, but the KPP scheme additionally includes a nonlocal term to parameterise e.g. convection. As in Gutjahr et al. (2021), it is assumed that the local and nonlocal eddy diffusivity are equal. The local eddy diffusivity is calculated as the product of a turbulent velocity scale $\omega$ and a non-dimensional vertical shape function $G$ which both depend on the normalised boundary layer depth $\sigma$:

$$k_{v}(\sigma) = h \omega(\sigma) G(\sigma)$$

where $\sigma = z/h$ is a dimensionless depth coordinate varying between 0 and 1 in the boundary layer, with $z$ denoting the depth below the surface and $h$ the ocean boundary layer depth.

The boundary layer depth $h$ is defined as the depth $z$ at which the bulk Richardson number becomes larger than a critical Richardson number $Ri_{crit}$. This is usually set to $Ri_{crit} = 0.3$. However, the critical bulk Richardson number below which the water column becomes unstable should be dependent on vertical resolution and approach the critical gradient Richardson number of 0.25 as the vertical resolution becomes higher. Since we run the models at relatively high vertical resolution in the upper ocean here, we did two different KPP runs with $Ri_{crit} = 0.3$ and $Ri_{crit} = 0.27$, respectively, to test the effect of a reduced Richardson number threshold.

Below the boundary layer, we use the Richardson-number dependent PP scheme (Pacanowski and Philander, 1981).
4 Large scale tropical Atlantic structure

4.1 Mean tropical mixed layer depth

An important metric to evaluate the performance of the vertical mixing parameterisation is the depth of the surface ocean mixed layer. In Figure 1, the 2015 annual mean mixed layer depth (MLD) in the tropical Atlantic is shown for ICON-O and FESOM (with TKE, $c_k = 0.2$) together with a climatology derived from Argo float observations (Argo, 2022). The MLD has been calculated from the models and all available Argo float profiles in the tropical Atlantic using a density criterion (potential density exceeds the surface density by 0.03 kg m$^{-3}$). Existing MLD climatologies normally use a density or temperature threshold compared to 10 m depth instead of the surface, and are thus unfortunately not suited for the equatorial oceans where the MLD can be very shallow (Holte et al., 2017). Both ICON-O and FESOM simulate too shallow MLDs in the equatorial Atlantic compared to the Argo float climatology. In Figure 2, the difference to the Argo MLD is shown for each of the model runs with the different vertical mixing settings. All sensitivity runs have a too shallow MLD for most parts of the tropical Atlantic as well. Interestingly, the bias pattern in the FESOM runs is quite similar for all runs, whereas for ICON-O, the difference between TKE and KPP is more pronounced, with the ICON-O KPP runs even showing a narrow region of too large MLD north of the equator. However, the parameter changes within the two mixing schemes hardly affect the MLD bias pattern in both FESOM and ICON-O.

In the TKE runs, the bias is especially large close to the equator, while it is not as pronounced for the KPP runs in either model. Figure 3 therefore shows the mean MLD along the equator (averaged between 4$°$S and 4$°$N) for the different model runs together to provide a better quantitative comparison. As seen from Figure 2, KPP is much closer to observations than TKE for both FESOM and ICON-O on the equator. A common pattern emerges from the TKE runs: with smaller $c_k$, the equatorial MLD becomes slightly deeper, i.e. more realistic, although not nearly to an extent that could remove the bias. This behavior is at first counterintuitive, because a larger $c_k$ should lead to larger viscosity and diffusivity (Eq. 2). However, the change in $c_k$ of course also leads to differences in the density and current structure, which changes the amount of TKE and can thus eventually lead to nonlinear changes in mixing. The main factor leading to a larger equatorial MLD with smaller $c_k$ is most likely the Equatorial Undercurrent, which is a source of shear instability but weakens with increasing $c_k$. We explore this process in more detail in Section 4.3. Changing the critical Richardson number in the KPP scheme has almost no effect in both models. The three additional ICON-O runs with enhanced background turbulence and Langmuir turbulence have a very similar equatorial MLD to the I_TKE_02 run (not shown).

4.2 Temperature

4.2.1 Mean surface temperature distribution

As described in the introduction, the tropical SST affects atmospheric convection, and thus can influence large-scale tropical and also extratropical wind and precipitation patterns. It is thus quite important to simulate the tropical SST distribution well in climate models. In Figure 4, the annual mean 2015 sea surface temperature in the tropical Atlantic is shown for HadISST on
In both models, a typical warm bias is evident in the upwelling regions along the African coast, which has long existed in most ocean and climate models (e.g. Farneti et al., 2022). Compared to CMIP6 models, the warm bias in the eastern upwelling regions and in the eastern equatorial region in ICON-O and FESOM is rather small of maximum 1°C compared to about 3-4°C in the CMIP6 models (e.g. Richter and Tokinaga, 2020; Farneti et al., 2022), maybe owing to the high horizontal resolution used in this study – Richter and Tokinaga (2020) and Farneti et al. (2022) find that the SST biases in HighResMIP are reduced compared to standard CMIP6. However, the largest bias in ICON-O and FESOM is not the warm bias in the east, but a very strong cold bias in the central and western tropical Atlantic, which is also a common feature of GCMs (Richter and Tokinaga, 2020). This cold bias has a similar pattern in both models, with an intensification on the equator, but is considerably stronger in ICON-O than in FESOM.

Changing the vertical mixing scheme or associated parameters has almost no effect on the mean SST bias in the tropical Atlantic, especially in FESOM. In ICON-O, changes between some of the different runs are visible, but with no effect on the large-scale bias pattern. In all cases, the western equatorial cold bias remains larger in ICON-O than in FESOM. The eastern warm bias is reduced in ICON-O when using KPP. In the west, the cold bias becomes larger in the ICON-O TKE runs when using a large value of $c_k = 0.3$.

### 4.2.2 Seasonal cycle of SST in the tropical Atlantic

The SST in the tropical Atlantic shows strong seasonal variations, especially in the eastern equatorial Atlantic. There, the Atlantic Cold Tongue (ACT) develops every year in boreal summer, when the trade winds intensify due to the northward movement of the Intertropical Convergence Zone (ITZC) and the shear between surface and subsurface currents increases and leads to vigorous turbulent mixing that cools the surface (Hummels et al., 2014). Interannual variations of this seasonal cycle are related to the Bjerknes feedback and are generally referred to as Atlantic Niño or Atlantic Zonal Mode. The ACT and Atlantic Niño are of large importance for the surface climate of the surrounding continents, but GCMs generally have difficulties with reproducing them (e.g. Lübbecke et al., 2018).

In Figure 5, the seasonal cycle of SST averaged over the ATL3 box in the eastern tropical Atlantic is shown, for HadISST in black and the different model runs in colour. The development of the ACT is visible in HadISST as a strong decline in temperature starting in April/May, with the ATL3 SST reaching a minimum in August. Both models follow this seasonal cycle with a somewhat too fast temperature decline, so that the minimum is already reached in July. The vertical mixing scheme and its parameter settings do not have a large effect on the seasonal cycle of ATL3 SST in either model. The largest differences can be seen in the minimum temperature in July and August, when the cold tongue is strongest. The KPP runs are closest to observations, while the TKE runs are slightly colder; the coldest runs are those with the smallest $c_k$ in both models.

In the western tropical Atlantic, the situation is different (Figure 6). It is noticeable that the models generally reproduce the seasonal cycle relatively well, but with a systematic offset towards colder temperatures compared to HadISST. In FESOM, the SST difference to HadISST is up to 1°C, in ICON-O about twice as large. Interestingly, the SST bias in the western Atlantic is sensitive to the vertical mixing scheme configuration in ICON-O, whereas in FESOM all the different runs are very close to
each other as it was for both models in the eastern tropical Atlantic (Figure 5). In ICON-O, the amplitude of the seasonal cycle is overestimated more when using KPP than TKE. The cold bias of the model SST is especially strong when using TKE with a high value of $c_k = 0.3$, and about 0.5°C less when using $c_k = 0.1$ instead. However, even though distinct changes between the different ICON runs are visible, they are still smaller than the differences between the models and between models and HadISST.

The seasonal cycle of ATL3 and WATL SST in the additional runs with ICON-O (with the Langmuir parameterization and an enhanced background TKE/diffusivity) looks very similar to I_TKE_02 (not shown).

### 4.2.3 Mean vertical temperature distribution

In Figures 7 and 8, vertical sections of the annual mean 2015 temperature are shown for the upper 200 m of the tropical Atlantic. The panel on the left shows a mean temperature section from Argo float data, the centre panels show the difference to Argo for ICON-O, the right panels for FESOM.

Along the equator, there is a cold bias above the thermocline and a warm bias below it in all model runs. The biases are again generally stronger in ICON-O than in FESOM, as for the mean SST. In the warm bias below the thermocline, some reactions to changes in the mixing scheme can be seen that are actually consistent between the two models: the bias becomes stronger when $c_k$ is increased in the TKE scheme, and it is also stronger in KPP than in TKE (although this is not so obvious in FESOM). As seen before, the changes between the different FESOM runs are actually not very large, while ICON-O reacts more sensitively to changes in the vertical mixing parameterization. Including the Langmuir parameterization does not have a large effect. Increasing the background TKE has a similar effect as increasing $c_k$ in the TKE scheme: both the cold bias above the thermocline and the warm bias below the thermocline increase (i.e. the thermocline becomes more diffuse). Increasing the minimum background diffusivity does not increase the bias as much.

The biases along 23°W are similar, also featuring a cold bias near the surface and a warm bias below, but the biases are generally weaker in the northern hemisphere and show more variability with latitude than with longitude. This is in accordance with the much larger zonal than meridional scales of the tropical Atlantic circulation systems. Again, there are local differences between the different mixing scheme settings, but not enough to change the large scale bias pattern. As in the sections along the equator, the difference between KPP and TKE is larger in ICON-O than in FESOM.

### 4.3 Equatorial current system

The equatorial oceans are characterized by strong zonal current systems. An important part of these is the Equatorial Undercurrent (EUC), which is one of the strongest subsurface currents in the world oceans. It transports water eastward approximately at the depth of the thermocline along the equator, and contributes to the Meridional Overturning Circulation (MOC) and the Subtropical Cells (e.g. Johns et al., 2014; Brandt et al., 2021). The EUC is not only important for horizontal water mass transport, but also for vertical mixing in the equatorial ocean: due to the shear between the mean westward surface flow of the South Equatorial Current and the eastward flow of the EUC at thermocline depth, the upper equatorial water column is permanently close to a state of marginal instability. This has some interesting consequences for the generation of turbulence in the equato-
rial oceans, which is diurnally enhanced not only in, but also below the surface mixed layer (Smyth et al., 2013; Moum et al., 2022). On the other hand, it has been shown that the EUC is notoriously hard to simulate in ocean models (e.g. Karnauskas et al., 2020; Fu et al., 2022), and that it reacts relatively sensitively to e.g. the vertical mixing parameterization (e.g. McCreary, 1981). We therefore take a closer look at how the Atlantic EUC is represented in ICON-O and FESOM and how it reacts to the different vertical mixing scheme settings.

In Figure 9, cross sections of the mean zonal velocity along 23°W are shown. The first panel shows a multi-year mean from shipboard observations during 21 cruises (available at https://doi.pangaea.de/10.1594/PANGAEA.899052, Burmeister et al., 2019). The Equatorial Undercurrent (EUC), a very strong eastward subsurface current, can be clearly seen on the equator with its core at approximately 70 m depth. In the cruise observations, it has a mean core velocity of 0.79 m s\(^{-1}\). The panels in the centre column show the same for the different ICON-O runs, the panels on the right for FESOM.

In general, the EUC is too weak as well as too deep and broad in ICON-O, whereas it is closer to the observed strength and location in FESOM. This indicates that the horizontal friction in ICON-O might be too large, making the EUC generally too weak even with the same vertical friction settings as in FESOM. In both models, increasing \(c_k\) in the TKE scheme leads to a weakening and deepening of the EUC. The weakening is likely related to an increased eddy viscosity with increased \(c_k\) (not shown). Since the EUC core depth is strongly related to the depth of the thermocline, the deepening of the EUC core is likely related to changes in the stratification with increasing \(c_k\). This is consistent with the mean temperature bias sections along the equator shown in Figure 7 where a strong influence of \(c_k\) on the vertical temperature gradient in the EUC depth range can be seen. In ICON-O, the EUC is most realistic with the smallest tested value of \(c_k = 0.1\), although it is then still a bit too weak and too deep. Since the EUC is in general stronger and shallower in FESOM, it even becomes too strong with \(c_k = 0.1\). Here, a value between 0.1 and 0.2 seems best.

Changing the vertical mixing scheme from TKE to KPP has a very different effect in ICON-O and FESOM. In ICON-O, the EUC strength reduces dramatically to below 0.3 m s\(^{-1}\). With a lower critical bulk Richardson number of \(R_{\text{icrit}} = 0.27\), the reduction is even stronger. In FESOM, the EUC core velocity with KPP remains in the range of values for the different TKE runs, and with 0.71 m s\(^{-1}\) both for \(R_{\text{icrit}} = 0.3\) and \(R_{\text{icrit}} = 0.27\) reasonably close to the observed value of 0.79 m s\(^{-1}\).

Adding the Langmuir turbulence parameterisation to the ICON-O TKE run makes the EUC slightly stronger, as does enhancing the background diffusivity. Increasing the minimum background TKE instead makes the EUC slightly weaker.

5 Representation of small scale processes in the upper ocean

One significant source of energy for the ocean system is wind energy. The way this wind energy is transferred from the atmosphere to the ocean depends on the physical setting in the upper ocean layers, e.g. stratification, which is both set by and impacts mixing. In the following, we will take a closer look at some of the processes distributing wind energy vertically in the ocean. In particular, the energy distribution within the mixed layer is crucial for modeling the energy and water cycle of the Earth’s entire climate system.
5.1 Near Inertial Waves

Near-inertial waves (NIWs) are significant contributors to wind-driven diapycnal mixing in the ocean (e.g. D'Asaro, 1985; Alford, 2003; Zhai et al., 2009). Estimates of wind work done on near-inertial motions in the global ocean range from 0.3 to 1.6 TW (Alford et al., 2016). These waves are confined to the mixed layer and oscillate horizontally with period corresponding to the local inertial frequency and speeds of up to 1 ms\(^{-1}\). At 15N, the period of NIWs is of about two days and increases toward the equator. Resonant tropical cyclonic winds induce strong near-inertial currents. Therefore, NIWs play a significant role in vertical mixing in the tropical northern Atlantic, especially during boreal autumn when the mixed layer is thinnest, and the wind speeds are highest (Foltz et al., 2020).

In Hummels et al. (2020), mixing induced by a NIW in the North Atlantic Ocean is reported and analysed. The wave cools the mixed layer at the rate of 244 Wm\(^{-2}\), deepens it and induces mixing below it. The observations of this extreme mixing event provide a unique challenge for the mixing schemes. A more extensive analysis of the NIW structure is available in Mrozowska et al. (2024). Both ICON and FESOM fail to reproduce the observed NIW amplitude. Here, we present the models’ ability to simulate the stratification changes observed as a result of NIW-induced mixing.

The site of the observations from Hummels et al. (2020) is located at 11°N, 21°W. The 25 microstructure profiles were collected over the course of 24 hours between the 13th and 14th of September, 2015, during the R/V Meteor cruise M119 (Fischer, 2020). The vertical resolution of the measurements is approximately 0.5m.

Snapshots of the buoyancy frequency (\(N^2\)) in the observations and the models are presented in Figure 10. The depth of the mixed layer in the TKE runs at the site is generally shallower than in the KPP runs. Both I_KPP and I_KPP_027 reproduce the observed \(N^2\) profiles within the mixed layer most accurately. The base of the mixed layer is highly stratified in the TKE models, with \(N^2\) values reaching three times the observed, and with diffusivity values as low as 10\(^{-7}\) m\(^2\)s\(^{-1}\). The only exceptions are the I_minTKE and I_minkv results, where minimum background TKE and diffusivity are imposed, respectively. The TKE tuning does not affect the depth of the mixed layer at the site. Significant differences between ICON-O and FESOM are noticeable: the high stratification band is weaker in FESOM TKE, and ICON-O KPP simulates a mixed layer which is twice as deep as in FESOM KPP.

The simulated \(N^2\) profile in this extreme NIW-induced mixing event is most sensitive to the mixing scheme chosen. KPP reproduces a more realistic stratification within the mixed layer. The vertical structure of the \(N^2\) profiles is not markedly affected by the tuning of TKE parameters.

5.2 Diurnal cycle of upper ocean properties

The diurnal cycle is the most dominant variability on timescales shorter than the inertial rotation of the upper ocean. It is particularly pronounced in the tropics, where a large amount of high shortwave solar radiation penetrates the upper ocean during the day, heating it up. Under low wind conditions, a stable stratification known as the diurnal warm layer (DWL) often forms in the surface layer. The depth of this DWL ranges from several centimeters to tens of meters, depending on factors such as wind conditions and incoming solar radiation. The presence of a DWL directly affects how momentum from the
wind is distributed in the upper ocean. In the following, we separate between off-equatorial regions and the equator itself for several reasons. First, the corresponding processes depend, to some extent, on the Coriolis force. Second, the equatorial region experiences considerable velocity shear due to the EUC (section 4.3), which interacts with the processes occurring on daily timescales.

### 5.2.1 Off-equatorial regions

Off the equator, the presence of a DWL directly affects how momentum from the wind is distributed in the upper ocean. When a DWL is present (resulting in strong stratification just below the ocean surface), an ocean current forms downwind, known as a diurnal jet. A significant portion of wind energy therefore remains in the uppermost layers of the ocean. In the absence of a DWL (resulting in weak stratification), no diurnal jet forms and the momentum is distributed over the entire extent of the mixed layer (ML). This diurnal jet of surface water affects the wind stress and wind power input, which in turn significantly influences how the ocean and the atmosphere exchange properties such as momentum, moisture, or heat. Air-sea fluxes depend to a large extent on the surface velocity of the ocean, which in turn depend on the stratification caused by the DWL. When the surface flow no longer matches the wind direction due to Coriolis deflection, the effect on air-sea fluxes is reduced. In the (sub-)tropics, the surface flow is usually aligned with the wind direction, making DWLs an important component of the energy/heat and freshwater input to the ocean. A high vertical resolution within the ML (at least 3-4 depth levels) is required to model these processes at all. Fig. 11 shows composites of daily temperature anomalies of the upper-ocean modelled with the different ICON-O and FESOM runs compared to temperature observations from three Slocum gliders. All data are averaged over January and February and shown for the subtropics in the western tropical Atlantic (between 12°N-14.5°N and 56.5°W-59°W). First, the diurnal temperature variations in both models align remarkably well with observations. However, subtle differences do emerge. It is noteworthy that the difference between the models is greater than that among the different mixing parametrizations. The ICON-O model represents the daily temperature cycle in the upper ocean more realistically than FESOM. In the FESOM model, the diurnal temperature variation is slightly too small (compare especially the center-top plot in Fig. 11, where the reddish lines are closer to the observations (black) than the bluish lines) and the DWL does not extend as deeply. When comparing the differences between the various runs, the diurnal temperature cycle becomes more pronounced and deeper in FESOM with increasing $c_k$. KPP behaves similarly to TKE with $c_k = 0.2$, but appears to mix the diurnal warm layer (DWL) more rapidly in the evening. This quicker mixing is more realistic compared to the observations. Among the ICON-O runs there is no distinct pattern for variations in $c_k$. However, KPP generates too little diurnal temperature variation. Over all, the ICON-O with $c_k = 0.3$ represents the observed diurnal temperature cycle in the upper ocean best.

### 5.2.2 Deep cycle turbulence on the equator (0°N, 23°W)

Deep cycle turbulence (DCT) is a complex mixing phenomenon above the EUC (section 4.3). The sheared current, wind forcing, and nighttime convection have to interact in order to cause the characteristic downward propagating turbulence patterns, which reach beyond the nighttime mixed layer base (Smyth et al., 2013). We chose the position 0°N 23°W, as DCT has been...
observed and described there from chipod measurements (Moum et al., 2022) attached to a PIRATA buoy, and data are available for the period of the model runs for comparison (https://www.pmel.noaa.gov/tao/drupal/chipod/index.html).

Timeseries of $K_v$ derived from the model runs (Fig. 12) show that KPP model runs rarely exhibit enhanced mixing below the mixed layer (ML). ICON-O TKE runs show stronger mixing below the ML during the DCT events than FESOM TKE runs. The DCT events of the ICON-O TKE runs seem to come in clusters with a longer than the observed one-day cycle, while for the FESOM TKE runs they show mostly clear diurnal cycling. The observational chipod data are more in line with the well separated diurnal events of the FESOM TKE runs. The downward propagation of the maximum diffusivity signal (Fig. 13) is most realistic for the ICON-O TKE runs. The KPP runs of both models show reasonable downward propagation over the course of the day, too. The chipod observational data have their diffusivity maxima at 8 hours local time ($\pm 1h$, at 35m), and at 10 hours local time ($\pm 2h$, at 65m); Smyth et al. (2013) report a 6m/h downward propagation speed in the Pacific.

When comparing the values of the diffusivity maxima to observations (see Figure 14), the ICON TKE runs are furthest away from the chipod observations. In the ICON TKE runs, the diffusivity maximum is overestimated. The ICON KPP runs only overestimate the maximum diffusivity a little, whereas for FESOM, both the TKE and KPP runs’ diffusivity maxima closely follow the observations.

Summarizing, only TKE runs can produce a satisfying DCT. The ICON-O TKE runs all perform better in the timing and propagation speed of the diffusivity maximum, the FESOM TKE runs in contrast better fits the observed diurnal separation of the DCT events. All FESOM runs perform much better in the simulation of the value of maximum diffusivity, which is overestimated in ICON-O. To find a configuration that can simulate all features of the equatorial Deep Cycle Turbulence, one might have to go to different higher order vertical mixing schemes.

6 Importance of forcing bulk formulae for model differences

As shown in the sections above, we generally find larger differences between the two models that we used than between different settings of the vertical mixing scheme. We were therefore interested in where the large differences between FESOM and ICON-O come from. Because of limited resources, we could test only one possible factor, and we chose the one that to us seemed to have most potential for a big impact on the mean upper ocean state: the different sets of bulk formulae in ICON-O and FESOM.

To quantify the effect of the different bulk formulae, we did an additional test run with ICON, with the same settings as in I_TKE_02, but with the bulk formulae that FESOM uses (for details see Section A). We call this run I_TKE_02_FBF. The effect that this has on the mean tropical Atlantic mixed layer depth, sea surface temperature, and Equatorial Undercurrent strength, can be seen in Figures 15, 16 and 17.

For the mixed layer depth, the two ICON-O runs look very similar. Here, the bulk formulae do not seem to make much difference, suggesting that other factors lead to the different mean MLD pattern in the model. These could include differences in lateral mixing, in the horizontal grid, or in the numerical schemes and the associated numerical mixing.
In contrast to that, the sea surface temperature and also the Equatorial Undercurrent strength react to the different bulk formulae. The SST pattern in ICON-O becomes more similar to FESOM when using the same bulk formulae, but interestingly, the entire tropical Atlantic also becomes much warmer. While ICON-O with its default bulk formulae has a much larger cold bias in the western Atlantic than FESOM, its western cold bias reduces very much and is smaller than FESOM’s when using the FESOM bulk formulae. Instead, the eastern Atlantic warm bias is then much stronger than before and also much stronger than in FESOM. For the EUC, the difference between the models reduces when using the same set of bulk formulae, i.e. the EUC in ICON-O gets stronger. However, it is still significantly weaker than in FESOM and observations.

The different bulk formulae that are by default applied in FESOM and ICON-O can explain a significant part of the models’ differences in mean tropical Atlantic SST and EUC strength, while they do not affect the mean mixed layer depth much. However, also for SST and EUC, a large unexplained difference remains such that other factors must contribute as well.

7 Discussion

Earlier studies, e.g. by Blanke and Delecluse (1993); Deppenmeier et al. (2020) and Zhang et al. (2022), have suggested that the long-standing tropical Atlantic ocean model biases can be significantly reduced by changes in the vertical mixing scheme. However, these studies focused on a specific model and usually only on a specific process or variable. Gutjahr et al. (2021) made a more comprehensive comparison of the effect of four different mixing schemes, albeit also only in one model. They found that the overall effect of the mixing scheme, e.g. on the global surface temperature bias, was rather small and at most relevant for very limited regions.

Although we can partly reproduce some of the findings of Blanke and Delecluse (1993), Deppenmeier et al. (2020) and Zhang et al. (2022), we show that overall, the large scale patterns and the magnitude of the tropical Atlantic mean state biases are not sensitive to the changes in the vertical mixing scheme settings that we tested, which is largely consistent with the conclusions of Gutjahr et al. (2021). In the cases where the biases are sensitive to the vertical mixing scheme settings, they are model dependent. The Equatorial Undercurrent (EUC), for example, is much less well reproduced in ICON-O when using KPP compared to TKE. Because we use the KPP scheme in the surface boundary layer together with the Richardson number dependent PP scheme in the deeper ocean, this is consistent with the findings of Blanke and Delecluse (1993) who found that the EUC is better reproduced when using TKE compared to PP. In contrast, the EUC is realistically simulated in FESOM with both KPP and TKE. Deppenmeier et al. (2020) claim that they can decrease the surface temperature bias in the tropical Atlantic in the NEMO ocean model by increasing $c_k$ in the TKE scheme. In their study, increasing $c_k$ from 0.1 to 0.5 leads to a surface cooling and a subsurface warming in the tropical Atlantic. This also happens in ICON-O (and the subsurface warming also in FESOM) when increasing $c_k$, however, in these two models this actually leads to a bias increase because it reinforces the original bias pattern. We can thus confirm that some sensitivity of the tropical Atlantic surface and subsurface temperature to the value of $c_k$ as described by Deppenmeier et al. (2020) is present also in ICON-O and FESOM, but whether it is beneficial to increase or decrease $c_k$ is heavily dependent on the model, and it is also not enough to induce any significant change in the temperature bias pattern in our case. Zhang et al. (2022) focus on the tropical Atlantic subsurface warm bias, which is very
similar in most Ocean Model Intercomparison Project models as in ICON-O and FESOM. They show that this warm bias can be reduced in POP2 by constraining the background diffusivity in the KPP scheme to observations, i.e. reducing it by one order of magnitude. Although we did not test this with the KPP scheme, we did similar runs with ICON-O using the TKE scheme: with the I_TKE_minKv run corresponding to the default KPP background diffusivity, and the I_TKE_02 run having up to one order of magnitude smaller diffusivities in the most parts of the interior ocean (although not in all places). We see a similar effect as Zhang et al. (2022) describe: the subsurface warm bias is increased slightly in the ICON-O TKE run with larger background diffusivity. However, the change in the subsurface temperature bias is small compared to the overall bias strength, and does not change the bias pattern.

Concerning the mixed layer depth (MLD) in the tropical Atlantic, we find that in both FESOM and ICON-O, it is generally too shallow compared to Argo float observations. This is contrary to for example Zhu et al. (2022) who, in order to reduce the overly deep penetration of boundary layer mixing in MOM5, have to reduce the strength of wind stirring in their parameter settings. For the mean mixed layer depth, we again find that ICON-O is more sensitive to a change in the vertical mixing scheme from TKE to KPP than FESOM. For ICON-O, the depth of the mixed layer near the equator becomes deeper with KPP compared to TKE, and is much closer to observations. Also in FESOM, the equatorial MLD is more realistic with KPP than with TKE, but here the effect is much smaller. Away from the equator, the MLD bias pattern is less sensitive to the vertical mixing scheme in both models.

Although it has been suggested that Langmuir turbulence is an important process for vertical mixing over much of the global ocean (Belcher et al., 2012) and that it can improve models’ representation of upper ocean mixing and mixed layer depth (e.g. Li et al., 2019), we find that including the Langmuir turbulence parameterisation from Axell (2002) in the TKE scheme in ICON-O does not really affect any of the tropical Atlantic mean state variables or small scale variability that we looked at. We especially expected it to benefit the simulation of the tropical Atlantic mixed layer depth which is too shallow in ICON-O, but the changes induced by the Langmuir turbulence scheme were in general very small or not detectable, for the MLD as well as other variables. However, the effect might be larger in the extratropics as found by e.g. Li et al. (2019).

For some specific processes and/or variables, the choice of the vertical mixing scheme can matter. As described above, the equatorial MLD is better in ICON-O with KPP. On the other hand, we find for example that the TKE scheme is much better suited for the simulation of the Atlantic EUC in ICON-O (though not in FESOM), and for the simulation of the deep diurnal cycle of equatorial turbulence. However, this clearly depends on the model and the process of interest, and the best vertical mixing scheme choice might be a different one when focusing on a different region or process. Changing tuning parameters in either the TKE or the KPP scheme has very little effect on the tropical Atlantic mean state biases in both FESOM and ICON-O. In those cases where an effect is there, it is very small compared to the magnitude of the bias, and cannot change the large scale bias pattern.

Because a large part of the tropical Atlantic biases is not sensitive to the vertical mixing scheme settings that we have tested (with the small exception of the aforementioned cases), the biases must instead be much more dependent on other specifics of the model that is being used. This is in line with the findings of Gutjahr et al. (2021) that the choice of vertical mixing scheme can matter regionally, but that the large scale bias patterns are mainly set by other factors. One other factor that we have
investigated is related to the atmospheric forcing that is used to drive the ocean model. FESOM and ICON-O use two different sets of default bulk formulae to convert ERA5 forcing fields to atmosphere-ocean fluxes. Exchanging the bulk formulae in ICON-O with those used in FESOM yielded much larger changes in the sea surface temperature field than the changes in the vertical mixing scheme. This is consistent with e.g. Zhu et al. (2022) and Zhang et al. (2022) who also found that the wind forcing has a large influence on tropical temperature biases. Unlike SST, the depth of the mixed layer is not influenced by the choice of bulk formulae. However, the bulk formulae can partly explain the difference in EUC strength between FESOM and ICON-O.

8 Conclusions

We presented coordinated sensitivity experiments with two different eddy-rich ocean models, FESOM and ICON-O, to investigate the effect of changing the vertical mixing scheme settings on biases in the tropical Atlantic. The tropical Atlantic in ocean models has long been subject to large biases in the mean state, such as sea surface temperature, which limits the ability of coupled climate models to simulate tropical and extratropical climate (e.g. Richter, 2015; Lübbecke et al., 2018; Richter and Tokinaga, 2020). Previous studies attributed an important role to the parameterisation of vertical mixing in the development of model biases of the mean state of the tropical Atlantic. Tuning of the vertical mixing scheme or a change to a different scheme thus led to a significant improvement in simulations. (e.g. Blanke and Delecluse, 1993; Deppenmeier et al., 2020; Zhang et al., 2022). However, these studies focused on a specific model and usually only on a specific process or variable.

By changing the vertical mixing schemes in two ocean models, we find that most of the long-standing biases in the large scale mean state in the tropical Atlantic Ocean are insensitive to the choice and details of the vertical mixing parameterisation. For SST, subsurface temperature, and the off-equatorial MLD, we find that the bias pattern is not affected by changing the vertical mixing scheme settings, and that there is little effect on the bias magnitude. For the MLD close to the equator as well as the EUC, the mixing scheme matters more: ICON-O has a more realistic equatorial MLD with KPP, but a more realistic EUC with TKE. These sensitivities, however, are model-dependent. In FESOM, both equatorial MLD and the EUC are not changed much by switching between TKE and KPP. For smaller scale variability like the upper ocean diurnal cycle or the representation of near-inertial waves, the choice of the vertical mixing scheme can matter as well, but the tuning of parameters within the schemes does not lead to significant improvements in diurnal cycle or near-inertial wave representation.

Our results suggest that the origin of the biases in the near-surface tropical Atlantic is complex and cannot be controlled by the ocean mixing parameterisation alone, but is likely related to biases in atmosphere-ocean interactions.

Code and data availability. The output of all model runs is provided for the upper 200m of the tropical Atlantic in the World Data Center for Climate (https://doi.org/10.26050/WDCC/nextGEMS_WP6oc, Bastin et al., 2023). The FESOM code of the version used is provided on Zenodo (https://doi.org/10.5281/zenodo.10617977, Danilov et al., 2024). The ICON-O code of the version used is provided on Edmond, the Open Research Data Repository of the Max Planck Society (https://doi.org/10.17617/3.KUFQAM, Haak and Bastin, 2024).
Appendix A: Bulk formulae

ICON-O uses two different set of bulk formulae depending on the forcing. In the case of ERA5 forcing, the bulk formulae from Kara et al. (2002) are used over the ocean and sea ice, with the water vapor pressure and 2 m specific humidity computed with (modified) equations from Buck (1981) and the longwave radiation following Berliand (1952).

Over open ocean, the turbulent heat and momentum fluxes are computed as follows. The enhancement factors (ratio of saturation vapor pressure of moist air to that of pure water vapor) at 2 m height \((f_a)\) and at the ocean surface \((f_w)\) are given by:

\[
f_a = 1.0 + A_w + p_s (B_w + C_w T_d^2)
\]

\[
f_w = 1.0 + A_w + p_s (B_w + C_w T_s^2)
\]

with \(T_d\) the dew point temperature at 2 m height (in \(^\circ\)C), \(T_s\) the sea surface temperature (in \(^\circ\)C), and the constants \(A_w = 7.2 \cdot 10^{-4}\), \(B_w = 3.20 \cdot 10^{-6}\), and \(C_w = 5.9 \cdot 10^{-10}\). Then the vapor pressure at 2 m height \((e)\) and at the water surface \(e_w\) is computed as:

\[
e = f_a a_w \exp((b_w - T_d/d_w) T_d/(T_d + c_w))
\]

\[
e_w = 0.9815 f_w a_w \exp((b_w - T_s/d_w) T_s/(T_s + c_w)),
\]

with \(a_w = 611.21\), \(b_w = 18.678\), \(c_w = 257.14\), and \(d_w = 234.5\).

The specific humidity at 2 m and at the ocean surface is then computed as:

\[
q = \alpha e/(p_s - \beta e)
\]

\[
q_w = \alpha e_w/(p_s - \beta e_w)
\]

with \(\alpha = 0.62197\) and \(\beta = 0.37803\). The relative humidity is computed as:

\[
f = 0.39 - 0.05 \sqrt{e/100}.
\]

The longwave radiation is computed following Berliand (1952). First, a factor for the effect from clouds on longwave radiation is derived:

\[
f_c = 1.0 - (0.5 + 0.4/90 \min(|\Phi|, 60)) CC^2,
\]

with \(\Phi\) the latitude and \(CC\) the cloud cover \([0,1]\). Then the net longwave radiation is computed as:

\[
LW^* = f_c f e \sigma T_{2m}^4 - 4 \epsilon \sigma T_{2m}^3 (T_s - T_{2m})
\]

with \(T_{2m}\) the 2 m temperature, \(\sigma = 5.670 \cdot 10^{-8} \text{W m}^{-2} \text{K}^{-4}\) the Stefan-Boltzman constant, \(\epsilon = 0.996\) the emissivity factor.

The net shortwave radiation is computed as:

\[
SW^* = (1 - \alpha_{vd}) f_{vd} I_0 + (1 - \alpha_{vd}) f_{vd} I_0 + (1 - \alpha_{nd}) f_{nd} I_0 + (1 - \alpha_{nd}) f_{nd} I_0
\]
the incoming shortwave radiation, the factors for visible direct and diffusive radiation $f_{vdi} = 0.28$ and $f_{vdf} = 0.24$, and factors for near-infrared direct $f_{ndi} = 0.31$ and diffusive $f_{ndf} = 0.17$ radiation. The respective albedos are $\alpha_{vdi}$, $\alpha_{vdf}$, $\alpha_{ndi}$, and $\alpha_{ndf}$.

The bulk coefficients are then computed as follows. First the air density is computed as

$$\rho_a = \frac{p_s}{(R_d T_2m (1.0 + 0.61q))},$$

(A11)

with $R_d = 287.04 \, \text{JK}^{-1} \, \text{kg}^{-1}$ the gas constant for dry air. The 10 m wind speed is bounded by

$$U_{10} = \max(2.5, \min(32.5, U_{10}))$$

(A12)

Then the bulk coefficients are computed as

$$CD_1 = 10^{-3} (-0.0154 + 0.5698/U_{10} - 0.6743/(U_{10}^2))$$

(A13)

$$CD_0 = 10^{-3} (0.8195 + 0.0506U_{10} - 0.0009U_{10}^2)$$

(A14)

The bulk coefficient for the turbulent latent heat flux is then computed as

$$CD_l = CD_0 + CD_1 (T_s - T_{2m})$$

(A15)

and bound to $CD_l = \max(0.5 \cdot 10^{-3}, \min(3.0 \cdot 10^{-3}, CD_l))$. The bulk coefficient for the turbulent sensible flux is computed as

$$CD_s = 0.95CD_l$$

(A16)

The sensible $H$ and latent $E$ heat fluxes are then derived as

$$H = \rho_a c_p CD_s U_{10} f_r (T_{2m} - T_s)$$

(A17)

$$E = \rho_a L_f CD_l U_{10} f_r (q - q_o).$$

(A18)

with $f_r = 1.1925$ an energy budget closing factor for OMIP, $L_f = 2.5008 \cdot 10^6 \, \text{Jkg}^{-1}$ the latent heat of fusion, and $c_p = 1004.64 \, \text{JK}^{-1} \, \text{kg}^{-1}$ the specific heat at constant pressure.

The turbulent momentum flux is finally computed as follows. First the drag coefficient is calculated as

$$CD_m = \min(2, \max(1.1, 0.61 + 0.063 \ast U_{10})) 10^{-3}.$$  

(A19)

Then the momentum flux is derived as

$$\tau = \rho_a CD_m U_{10} \sqrt{(u - u_o)^2 + (v - v_o)^2},$$

(A20)

with zonal and meridional wind velocity $u$ and $v$ and for the ocean $u_o$ and $v_o$, respectively.
Over sea ice a similar approach is used, by first computing the enhancement factor

\[ f_i = 1.0 + A_i + p_s(B_i + C_i T_i^2), \]  

(A21)

with \( A_i = 2.2 \times 10^{-4} \), \( B_i = 3.83 \times 10^{-6} \), \( C_i = 6.4 \times 10^{-10} \) and the ice surface temperature \( T_i \). Then the vapor pressure and specific humidity over sea ice are computed as

\[ e_i = f_i a_i \exp\left( (b_i - T_i/d_i)T_i/(T_i + c_i) \right) \]  

(A22)

\[ q_i = \alpha e_i / (p_s - \beta e_i) \]  

(A23)

with \( a_i = 611.15 \), \( b_i = 23.036 \), \( c_i = 279.82 \), and \( d_i = 333.7 \).

The bulk coefficients are then computed for the latent heat flux as

\[ CD_{li} = CD_0 + CD_1(T_i - T_{2m}) \]  

(A24)

bound to \( CD_{li} = \max(0.5 \times 10^{-3}, \min(3.0 \times 10^{-3}, CD_{li})) \), and for the sensible heat flux as

\[ CD_{si} = 0.95 CD_{li} \]  

(A25)

The turbulent fluxes for latent and sensible heat and for momentum are then derived as

\[ H_i = \rho_a c_p CD_{si} U_{10} f_r (T_{2m} - T_i) \]  

(A26)

\[ E_i = \rho_a L_f CD_{li} U_{10} f_r (q - q_i) \]  

(A27)

\[ \tau_i = \rho_a CD_{mi} U_{10} \sqrt{(u - u_i)^2 + (v - v_i)^2} \]  

(A28)

The net longwave and shortwave radiation are finally computed as

\[ LW^*_i = f_c f_s f_f c_0 T_{2m}^4 - 4 c_0 T_{2m}^3 (T_i - T_{2m}) \]  

(A29)

\[ SW^*_i = (1 - \alpha_{vd}) f_{vd} I_0 + (1 - \alpha_{vd}) f_{vd} I_0 + (1 - \alpha_{nd}) f_{nd} I_0 + (1 - \alpha_{nd}) f_{nd} I_0 \]  

(A30)

**Author contributions.** SB led the writing of the manuscript, ran the ICON-O model runs, and did the main analysis on the mean state. AK ran the FESOM model runs and wrote the parts about the FESOM model. FS analysed the diurnal cycle and wrote the corresponding text. OG implemented needed features in ICON-O and wrote the text about the bulk formulae. MAM did the analysis and wrote the parts on NIWs. TF analysed the deep cycle turbulence and wrote the corresponding text. RS contributed to analysis of the diurnal cycle. NK and HH assisted with the model runs. JJ, SD, MD and MJ conceptualised the idea and acquired funding. All authors contributed to initial analysis, planning and review of the manuscript.

**Competing interests.** The authors declare that they have no competing interests.
Acknowledgements. NextGEMS is funded through the European Union’s Horizon 2020 research and innovation programme under the grant agreement No. 101003470. The work was conceived of during a hackathon on the island of Bornoe in 2022: https://nbioccean.bitbucket.io/bornoe2022a/) Florian Schütte is funded by the Bundesministerium für Bildung und Forschung as part of the NextG-Climate Science-EUREC4A-OA project.

The vmADCP shipboard data are accessible at https://doi.pangaea.de/10.1594/PANGAEA.899052 (Burmeister et al., 2019).

The Argo float data were collected and made freely available by the International Argo Program and the national programs that contribute to it. (https://argo.ucsd.edu, https://www.ocean-ops.org). The Argo Program is part of the Global Ocean Observing System.

The authors thank the German Climate Computing Center (DKRZ) for access to their computing infrastructure.
References


Figure 1. Annual mean mixed layer depth (MLD) in the tropical Atlantic Ocean from Argo float data (Argo, 2022, mean over entire available measurement period from 2000 to 2022) and sensitivity model runs from FESOM and ICON-O (mean over second integration year 2015). The MLD has been calculated using a commonly used density threshold criterion, where the MLD is defined as the depth at which the potential density exceeds the surface density by more than 0.03 kg m\(^{-3}\).
Figure 2. Difference in annual mean mixed layer depth between FESOM and ICON-O runs and Argo float data in the tropical Atlantic Ocean.
Figure 3. Annual mean Atlantic Ocean mixed layer depth along the equator (averaged between 4°S and 4°N) from Argo float data as well as FESOM and ICON-O.
Figure 4. Annual mean 2015 Atlantic Ocean sea surface temperature from the HadISST dataset as well as FESOM and ICON-O (for the models, differences to HadISST are shown, blue colours meaning the model is colder than HadISST).
**Figure 5.** Seasonal cycle of sea surface temperature averaged over the ATL3 box (20°W-0°E, 3°S-3°N), from HadISST data as well as FESOM and ICON-O.
Figure 6. Seasonal cycle of sea surface temperature averaged over the WATL box (45°W-25°W, 3°S-3°N), from HadISST data as well as FESOM and ICON-O.
Figure 7. Vertical section along the equator of annual mean temperature from 2015, from Argo float data as well as FESOM and ICON-O.
Figure 8. Vertical section along 23°W of annual mean temperature from 2015, from Argo float data as well as FESOM and ICON-O.
Figure 9. Strength of the Equatorial Undercurrent (EUC) from cruise observations and FESOM and ICON-O model runs. Shown is a mean section of zonal velocity along 23°W, where multi-year cruise data are available. The observations are averaged over all available years, the sections from the models are annual averages over 2015.
Figure 10. Buoyancy frequency ($N^2$) in shipboard observations and the models at 11°N, 21°W between the 13th and 14th of September, 2015. The diamonds in the subfigure showing M119 observations correspond to the points in time at which the measurements were taken.
Figure 11. Composite diurnal cycle of the upper-ocean daily temperature anomaly (FESOM - left; Observations - bottom center; ICON - right). In the top center the daily anomalies at 1 m depth are shown (FESOM - blue; Observations - black; ICON - red).
Figure 12. Decadal logarithm of diffusivity in m²/s for the different model runs, at 0°N and 23°W, for days 120 to 138 of year 2014. Dashed line: nighttime mixed layer base. The model runs show different ability to represent the main characteristics of deep cycle turbulence (enhanced K below ML base; diurnal cycling)
Figure 13. Average local daytime of maximum diffusivity as function of depth for the different model runs in black, and from PIRATA chipod observations in red, at 0°N and 23°W. Uncertainty ranges are the standard deviation from all estimates in the area [0.5°S, 0.5°N, 23.5°W, 22.5°W].
Figure 14. Average maximum diffusivity as function of depth for the different model runs in black, and from PIRATA chipod observations in red, at 0°N and 23°W. Uncertainty ranges are the standard deviation from all estimates in the area [0.5°S, 0.5°N, 23.5°W, 22.5°W].
Figure 15. Effect of exchanging the forcing bulk formulae in ICON-O on the 2015 annual mean mixed layer depth.
Figure 16. Effect of exchanging the forcing bulk formulae in ICON-O on the 2015 annual mean sea surface temperature.
Figure 17. Effect of exchanging the forcing bulk formulae in ICON-O on the Atlantic Equatorial Undercurrent. Shown is the 2015 annual mean zonal velocity along 23°W.