



1                   **RELATIONSHIP BETWEEN INTRASEASONAL OSCILLATIONS AND**  
2                   **ABNORMAL RAINFALL IN VIETNAM**

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### Abstract

19 Vietnam's summer monsoon season are characterised by intense rainfall, driven by dynamic  
20 intraseasonal oscillations such as the Madden-Julian Oscillation (MJO) and the Boreal Summer  
21 Intraseasonal Oscillation (BSISO). Located near the equator with diverse terrain, the country  
22 presents a unique case for studying how these atmospheric mechanisms interact with local  
23 geography, influencing both the timing and spatial distribution of extreme rainfall events.  
24 Despite this, gaps remain in understanding the detailed coupled impact mechanisms that hinder  
25 the accurate prediction of abnormal rainfall over the region. This study pioneers an exploration  
26 into the interconnected dynamics of abnormal rainfall occurrences and coupled activities of  
27 BSISO and MJO in Vietnam. Using association analysis of abnormal events, detected from  
28 remote sensing gridded rainfall database, within conditional probability analysis framework,  
29 our findings reveal distinct seasonal patterns: during summer, North and South Vietnam  
30 experience primary impacts, whereas Central Vietnam becomes more susceptible during  
31 autumn. Notably, BSISO phases 3 and 5 dominate the summer landscape, while MJO phases  
32 exhibit balanced occurrence frequencies throughout the season. Probability assessments  
33 highlight phase 7 of BSISO in July and phases 6-7 in August as periods of heightened extreme  
34 rainfall probability in North and South Vietnam, contrasting with phases 5-8 in Central  
35 Vietnam. Additionally, MJO phase 5 emerges as a focal point for intensified extreme rainfall  
36 in October, alongside notable increases in phases 3-4 during September. This comprehensive  
37 analysis enhances our understanding of the complex interactions shaping Vietnam's monsoonal  
38 rainfall dynamics, offering valuable insights for future studies leveraging the two intraseasonal  
39 oscillations mechanisms to explain and predict abnormal heavy rainfall in Vietnam.

40

41 **Keywords:** BSISO, MJO, CMORPH, heavy rainfall, intraseasonal oscillations, monsoon  
42 rainfall

43



44 **1. Introduction**

45 Vietnam, located in the Asian summer monsoon belt, exhibits a distinct climate marked  
46 by significant regional variation caused by multiple-scale atmospheric dynamics mechanisms  
47 interacting with the country's elongated north-south mountainous terrain. The rainy season in  
48 the North and South Vietnam is associated with the development of the tropical westerly winds,  
49 beginning around mid-May and ending around September (Nguyen and Nguyen 2004; Nguyen  
50 et al. 2014; Nguyen-Le et al. 2014). In contrast, due to the Foehn effect induced by the Truong  
51 Son mountain range, the Central Vietnam experiences oppositely dry season during the summer  
52 months (Nguyen-Le et al. 2014). The rainy season in the Central typically starts from August  
53 to September and ends around December, related to the development of the northeast monsoon  
54 and the strong activity of the tropical disturbances (Yokoi and Matsumoto 2007; Tuan 2019;  
55 Nguyen et al. 2023). Recent study (Nguyen et al. 2022) pointed out that North Vietnam  
56 experiences early rainfall in spring due to the influence of cold fronts.

57 Rainfall in Vietnam exhibits clear oscillations on an intraseasonal scale, including two  
58 main modes: 10–20 days and 30–60 days (Tuan 2019; Truong and Tuan 2018; 2019). The 10–  
59 20-day oscillations are caused by the southward movement of pressure anomalies from the  
60 extratropical region, interacting with the westward movement of tropical disturbances. The  
61 movements of these pressure anomalies are directed by developments of upper-level wavetrain  
62 along jet stream (Tuan 2019). On the other hand, the 30–60-day oscillations are primarily  
63 induced by the Madden-Julian Oscillation (MJO) and the Northern Hemisphere summer  
64 monsoon (BSISO). While the MJO typically appears apparently in the late summer and  
65 autumn, moving from west to east, the BSISO occurs frequently in summer and propagates  
66 northeastward (Madden and Julian 1972; Lee et al. 2012).

67 Heavy rainfall induces serious consequences for socioeconomic activities causing  
68 flooding and land slides. Accurate predicting these occurrences or probability of occurrences in  
69 intraseasonal context is crucial for mitigating associated risks across multiple societal sectors.  
70 Initial studies on the heavy rainfall occurrences in Vietnam were based on analyzing a large  
71 number of their related synoptic patterns which were mainly conducted by experienced  
72 forecasters and researchers in National Center for Hydrometeorological Forecasting (Khanh  
73 1993; 1998a, 1998b, Lanh 2012). These studies identified various synoptic patterns  
74 contributing to the occurrence of the heavy rainfall, varying with climatic subregion. Keys  
75 patterns include tropical cyclones, interactions between cold surge and tropical disturbances,  
76 the arrival of tropical convergence zones (ITCZ) and deepening of monsoon trough, and the



77 intensification of high-level troughs associated with cold surge. However, these insights rely  
78 on forecasters experiences, there are lack of robust statistics relationship have provided.

79 On the other hand, mechanisms of heavy rainfall were also investigated for individual  
80 heavy rainfall events. Wu et al. (2011) pointed out that the heavy rainfall in Hanoi in October  
81 2008 was caused by the interaction between cold surges and tropical disturbances. This  
82 disturbance was part of a synoptic-scale tropical wave developing from the warm Pacific Ocean  
83 to the East Sea. Van de Linden et al. (2016) demonstrated that the heavy rainfall in northern  
84 Vietnam in August 2015 was caused by a westward movement of a low-pressure system over  
85 the northern region combined with the strong activity of the southwest monsoon. The  
86 movement of the low-pressure system was associated with the westward movement of a high-  
87 level trough in the extratropical region. In another study, Chen et al. (2012) indicated that the  
88 heavy rainfall in Hanoi in 2008 was caused by the interaction of multiple processes at different  
89 scales, including 5-day oscillations, 12–24-day oscillations, and the MJO. In more spatially  
90 specific studies focusing the Central Vietnam, heavy rainfall is primarily attributed to  
91 interactions between cold surges, tropical disturbances, and topography (Yokoi and Matsumoto  
92 2007; Yen et al. 2011; Chen et al. 2012). Meanwhile, in the Central Highlands and South  
93 Vietnam, the heavy rainfall be less frequent and less studied. Van de Linden et al. (2016)  
94 pointed out that heavy rainfall in this area often occurs more frequently during the activity  
95 phases of the MJO and tropical waves. Based on the analysis of large-scale synoptic patterns  
96 related to the historical heavy rainfall event in the subregion in August 2019, Wu et al. (2021)  
97 showed that this heavy rainfall event was caused by multi-scale interaction between the 10–  
98 60-day frequency oscillations and the 6–10-day frequency oscillations.

99 While these studies offer valuable insights into potential atmospheric mechanisms  
100 influencing the intraseasonal oscillations in local extreme events, there are lack of studies  
101 explicitly climatological relationships between these multiple oscillations – such as MJO or  
102 BSISO and these coupled effects – and abnormal rainfall occurrences in across subregions in  
103 Vietnam. Understanding how different subregions respond differently to these oscillations  
104 remains an important area for further investigation. Our study focus on understanding the  
105 influence of intraseasonal oscillations on the probability of abnormal rainfall occurrences  
106 across different regions of Vietnam. We aim to uncover how varying local terrains and  
107 geographical conditions responds differently with large-scale atmospheric oscillations, leading  
108 to diverse rainfall patterns throughout Vietnam.



109 This paper is organized as following; the Section 2 presents the data and methodology  
110 used in the study. Section 3 presents the results of the analysis of the relationship between  
111 BSISO and MJO heavy rainfall in Vietnam. The conclusion and discussion are presented in  
112 Section 4.

## 113 **2. Data and methodology**

### 114 *2.1. Data*

115 In this study, high-resolution satellite rainfall data (CMORPH) are utilized to calculate  
116 the linkage of heavy rainfall occurrence over the Vietnam region. These data are provided at a  
117 spatial resolution of 8 km x 8 km and a temporal resolution of 3 hours. This dataset is estimated  
118 based on microwave observations from remote sensing satellites and employs the rainfall  
119 estimation algorithm developed by Ferraro (1997). To identify the activities of the BSISO and  
120 MJO, the BSISO and MJO index provided by the Asia-Pacific Economic Cooperation Climate  
121 Center (APCC) were employed. These indexes were constructed based on the analysis of the  
122 natural orthogonal functions of various atmospheric variables (Wheeler and Hendon 2004; Lee  
123 et al. 2013). Since the calculation of these indexes does not requires bandpass filtering, it can  
124 be applied to real-time forecast data to support forecasting.

### 125 *2.2. Methodology*

126 Since extreme rainfall exhibits seasonal variation (Tuan 2019), the extreme event  
127 thresholds were calculated for each month. In this study, a rainfall event is identified based on  
128 the 90th percentile of days with rainfall exceeding 0.3 mm in each respective month. This  
129 identification of rainfall events is conducted across all grid points from May to November,  
130 which is considered the rainy season in North and South Vietnam. The period from December  
131 to April is considered dry season in Vietnam (Nguyen-Le et al. 2014); therefore, it is excluded  
132 from our analysis.

133 Using 21 years of the BSISO, MJO and CMORPH rainfall data from 2000 to 2020, the  
134 empirical probability of extreme heavy rainfall occurrence in each phase of BSISO, MJO is  
135 calculated using the following formula:

$$136 \quad P - \text{dependent Pr}_O(\%) = P(\text{Ext} / \text{BSISO}_{XZ}),$$

137 In which, Pr<sub>O</sub> represents the probability of heavy rainfall occurrence based on the  
138 BSISO index, P(BSISO<sub>XZ</sub>) is the probability of phase X of BSISO occurring in month Z,  
139 and P(Ext | BSISO<sub>XZ</sub>) is the conditional probability of extreme rainfall events given that the  
140 phase of BSISO is X in month Z. To focus on the effects of BSISO amplitude on occurrence  
141 of the extreme heavy rainfall, the BSISO index was categorized into four groups based on its



142 amplitude, namely  $(PC1^2 + PC1^2)^{1/2} \geq 1$ ,  $(PC1^2 + PC1^2)^{1/2} < 1$ ,  $(PC2^2 + PC4^2)^{1/2} \geq 1$ ,  $(PC3^2 +$   
143  $PC4^2)^{1/2} < 1$

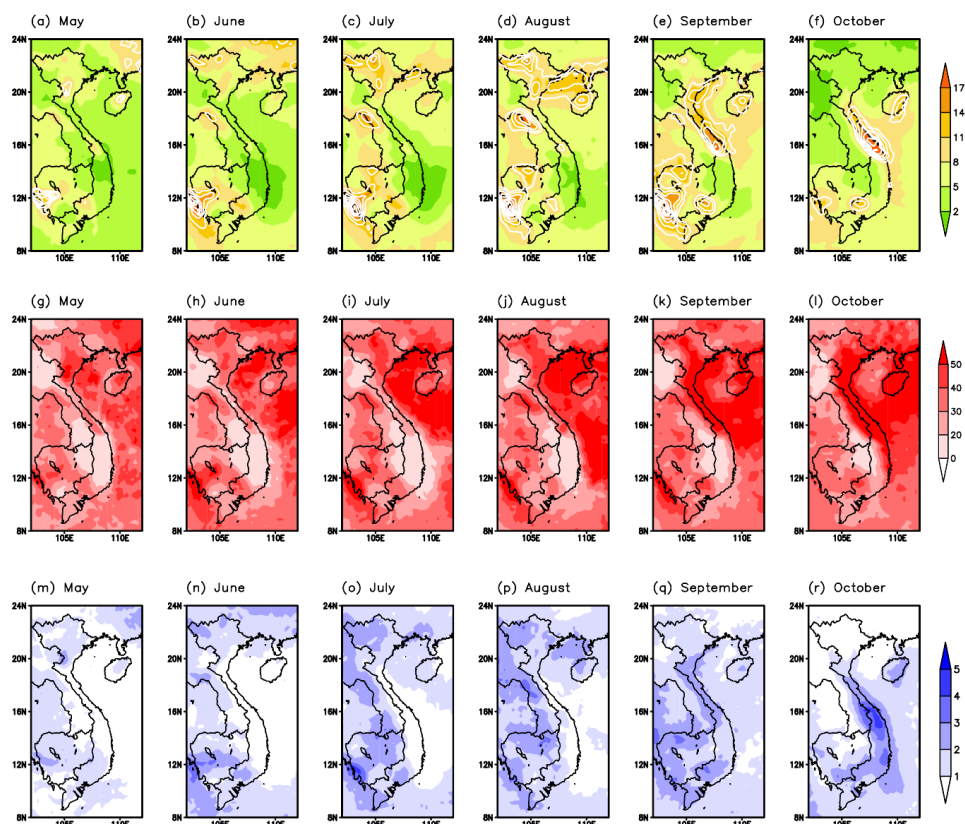
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$$PA - \text{dependent Pr}_O(\%) = P(\text{Ext} / \text{BSISO}_{XYZ}),$$

145 where  $P(\text{BSISO}_{XYZ})$  is the propability that BSISO phase X which amplitude greater  
146 than Y, in month Z.

### 147 **3. Results and discussions**

#### 148 *3.1. Characteristics extreme rainfall in summer in Vietnam*

149 Figure 1 illustrates the characteristics of the rainfall and extreme rainfall events in  
150 Vietnam during the rainy season. Rainfall primarily occurs in North and South Vietnam in  
151 summer while it starts to occur in Central Vietnam much latter, from September to October.  
152 While the monsoon westerlies bring a large amount of moisture to support for the development  
153 of deep convection, the Truong Son mountain runing along the country play a role as a nature  
154 barrier that prevents the low-level flow from developing to the east. Therefore, summer is dry  
155 season in Central Vietnam (Nguyen-Le et al. 2014). It is importat to note that, although the  
156 timing of rainy season onset is similar between the North and South Vietnam, the rainfall  
157 amount in the former is significantly higher than that in the later. This difference in rainfall  
158 amount is primarily caused by the extratropical factors effecting the North Vietnam in summer  
159 (Tuan et al. 2019). Additionally, the highest amount of the summer rainfall is observed in the  
160 high and steep mountainous terrain in northwestern region, especially in Lai Chau and Bac  
161 Quang, implying the rainfall is significantly affected by topography. In the Central Highlands  
162 and South Vietnam, rainfall mostly concentrates in the western sides of the highlands, which  
163 may also result from the interaction of the southwest monsoon winds and terrain. In another  
164 hand, heavy rainfall only begins to appear in Central Vietnam in September which is related to  
165 the intensification of cold surge, activities of tropical disturbances and orographic effects  
166 (Yokoi and Matsumoto 2007).



167

168 *Figure 1: Top panel: climatological rainfall (color) and its standard deviation of daily*  
 169 *rainfall (white lines) from May to October over 21 years (2000-2020); Middle panel: 90th*  
 170 *percentile rainfall values for each month (mm/day); Bottom panel: Number of extreme rainfall*  
 171 *days.*

172 Similar to the distribution of climatological mean of the rainfall, the 90<sup>th</sup> percentile of  
 173 rainfall also shows significant differences among the subregions. In the North Vietnam region,  
 174 the 90<sup>th</sup> percentile of rainfall ranges from 30–60 mm per day, with highest values in the Red  
 175 River Delta. These rainfall values gradually increases as autumn approaches. Meanwhile, in  
 176 South Vietnam, the 90<sup>th</sup> percentile of rainfall does not vary much throughout the year, which  
 177 oscillates in a lower range, from 20–40 mm per day. The 90<sup>th</sup> percentile of rainfall in the Central  
 178 Highlands displays the lowest values, only below 20 mm per day. Conversely, the 90<sup>th</sup>  
 179 percentile of rainfall is also small over Central Vietnam in summer months, that is consistent  
 180 with the fact that summer is dry season in the subregions. The rainfall abruptly increases in  
 181 September, and then reaches over 60 mm per day in October.

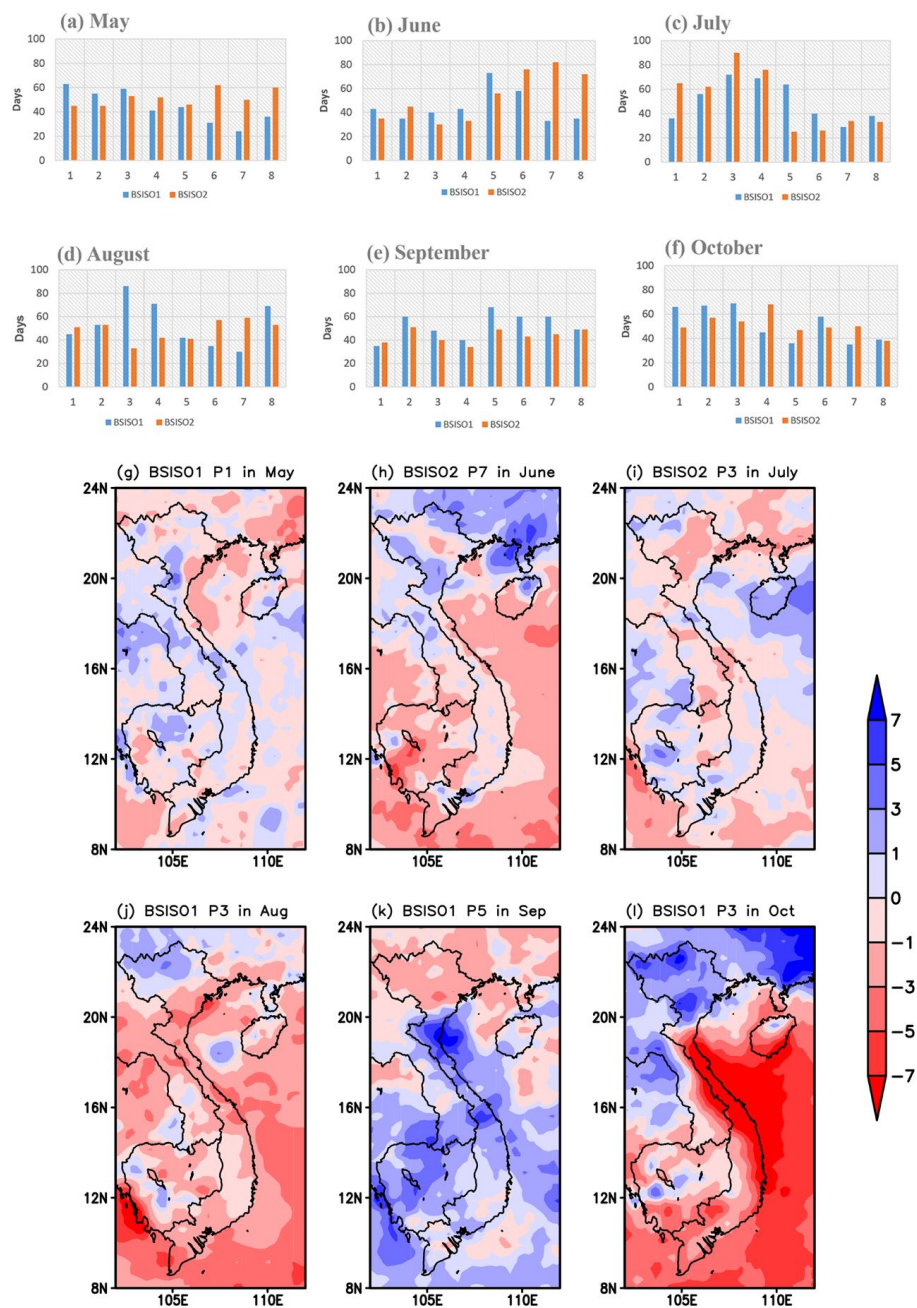


182           The number of extreme rainfall days also varies significantly among the climatic  
183 subregions. The number of extreme rainfall days in North Vietnam increases gradually from  
184 May, reaches a peak around July, then gradually decreases in September. Meanwhile, the  
185 number of extreme rainfall days in the Central Highlands and South Vietnam peaks later,  
186 around September. Lastly, the number of extreme rainfall days in Central Vietnam reaches its  
187 peak in October-November, corresponding to the increase of rainfall in the subregion in the  
188 period. This extreme rainfall patterns once again indicates the complex characteristics of  
189 extreme rainfall in Vietnam due to influences of multiple weather systems.

### 190           3.2. Evolution of the BSISO and the linkage with rainfall

191           Figure 2 illustrates the frequencies of the individual BSISO phases during the summer  
192 months. The anomalous rainfall associated with the highest frequency phase is also plotted.  
193 Although the difference in the frequencies among the phases is not too large, the highest  
194 frequency phase can be noted. In May, phase 1 of the BSISO-1 shows the highest frequency  
195 (approximately 120 days), followed by phases 2 and 3 (around 100 days). This phase is related  
196 to the decrease of rainfall in almost all Vietnam subregions, except for small areas in the North  
197 and Central Vietnam (Fig 2g). In June and July, phase 5 and phase 3 of the BSISO-2 exhibit  
198 the highest frequencies, respectively; however, the anomalous rainfall patterns is nearly  
199 uniform in entire Vietnam, indicating the insignificant contributions of these phases to the  
200 variation of the rainfall. The most important signals are only noticed in September and October.  
201 In September, phase 5 of the BSISO-1 shows the highest frequency, associated with a clear  
202 increase of rainfall in Central Vietnam and decrease of rainfall in North Vietnam. In contrast,  
203 in October, phase 3 displays the highest frequency, simultaneous with the outburst increase of  
204 rainfall in North Vietnam.





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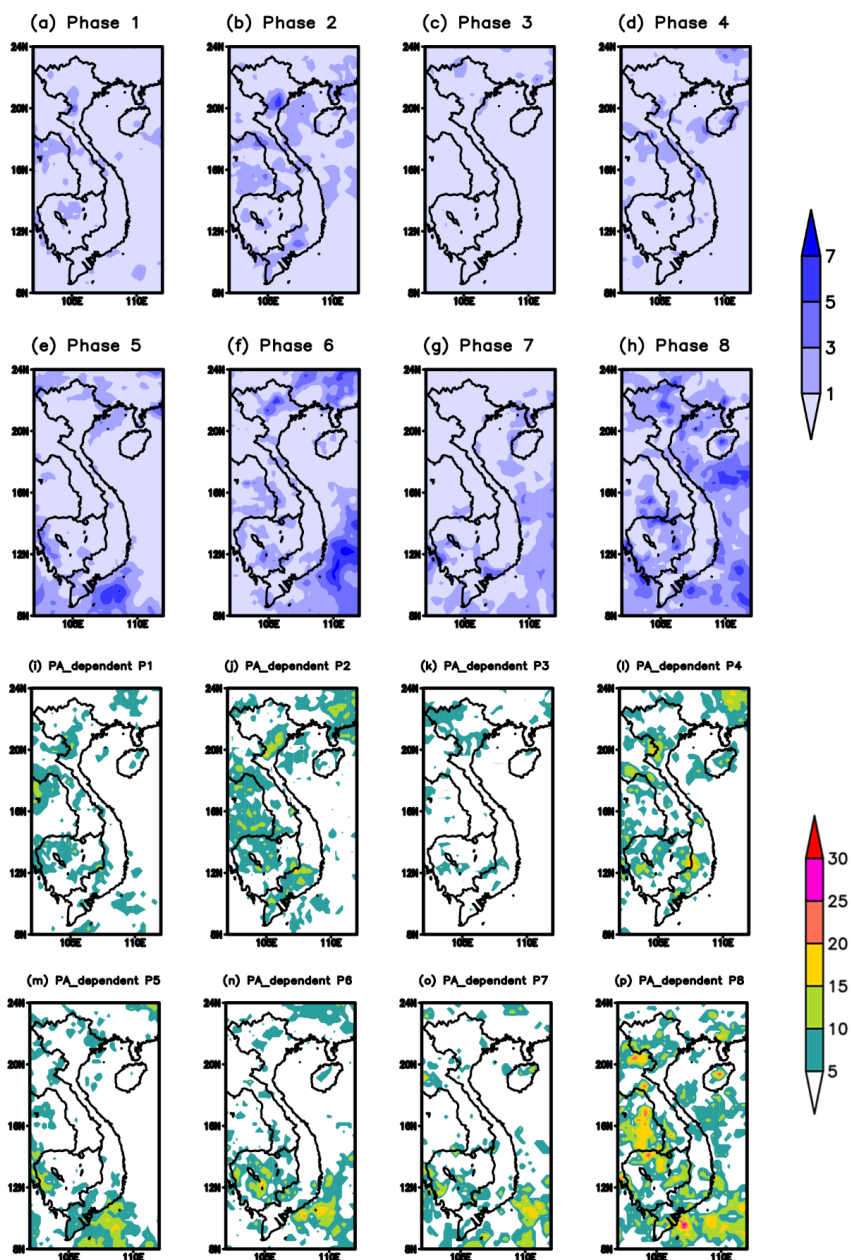
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*Figure 2. (a-f) Frequency of each BSISO1 and BSISO2 phase in May, June, July, August, September, October from 2000 to 2020. Figure (g-l) represents the corresponding anomalous rainfall associated with the phases of BSISO of highest frequency.*



209

210 Further investigation on the linkages between the BSISO variations of rainfall in Vietnam  
211 is displayed in Figure 3. The anomalous rainfall values in each BSISO-1 phase (Fig 3a-h) and  
212 probability of extreme rainfall occurrence in the phases which their amplitude greater than 1  
213 (Fig 3i-p) are plotted. It can be seen that, although the anomalous rainfall are nearly uniform  
214 in many BSISO-1 phases, the increase rainfall is clearly observed in North Vietnam in the  
215 phases 2, 4 and 8. This result indicates the insignificant influences of the BSISO-1 activities  
216 on rainfall in Vietnam. Similarly, in the phase 2, 4 and 8, the anomalous and extreme rainfall  
217 are also enhanced over the North Vietnam and the southern of Central Highland. Therefore,  
218 the BSISO might also contribute to the occurrence of extreme rainfall in the country in some  
219 specific months. Note that, the anomalous rainfall and probability of extreme rainfall is  
220 calculated in all day that the phase occurs, the signal of rainfall variations might not be clear.  
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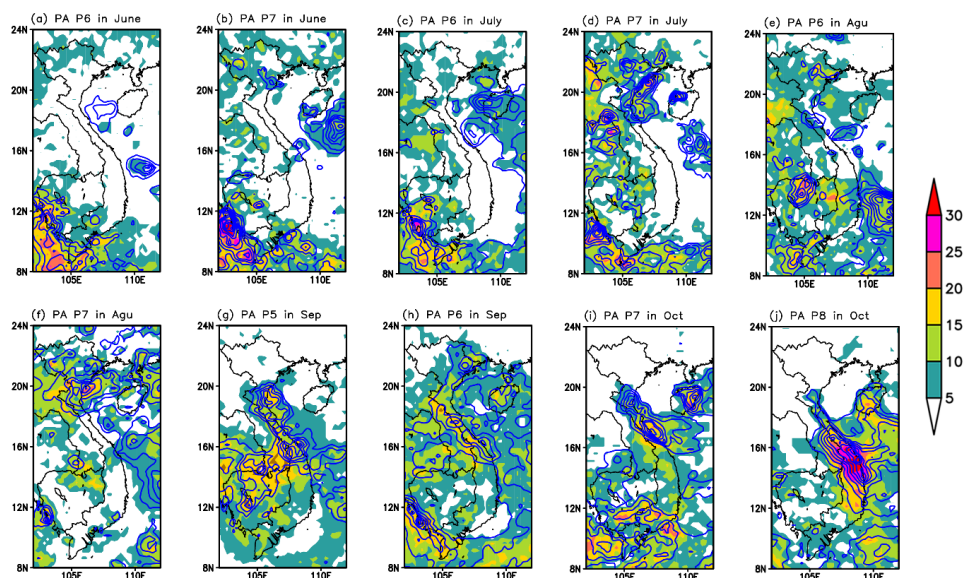
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Figure 3. Anomalous rainfall and probability of extreme rainfall occurrence in BSISO-1 phases.



226 Since the extreme rainfall has significant seasonal variability, the probability of extreme  
227 rainfall in each BSISO-1 phases in specific month are plotted (Fig. 4). To highlight the effect  
228 of of the BSISO-1 intensity on rainfall, only the phases which the BSISO-1 amplitude greater  
229 than 1 are plotted. This approach might help to better recognize the linkage between the  
230 BSISO-1 and the extreme rainfall in Vietnam. In June, the phase 6 and phase 7 of the BSISO-  
231 1 play the most important role in modulating the extreme rainfall, with the high probability of  
232 extreme rainfall observed in North and Southern Vietnam (Fig. 4a-b). From July to August,  
233 these two phases still the controlling factors of the extreme rainfall. The high probability of  
234 extreme rainfall values are not only observed over the North and South Vietnam, it also  
235 expands to Central Highlands. From September to October, there are additional contributions  
236 of phase 5 and phase 8 on the frequency of extreme rainfall. While the probability of extreme  
237 rainfall tends to decrease over the North Vietnam, it is rapidly intensified significantly in the  
238 North Central and South Vietnam, consistent with the development of cold surge and activities  
239 of tropical disturbances during this period.



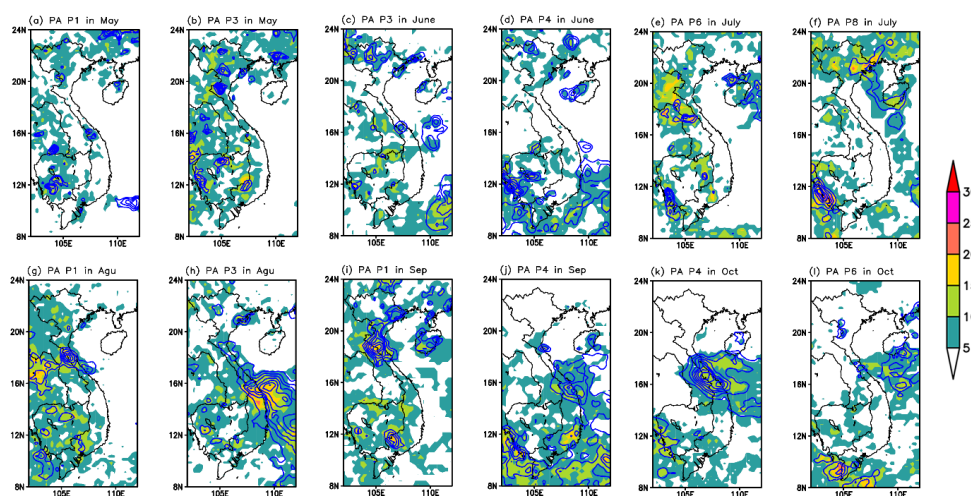
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241 *Figure 4. Probability of extreme rainfall occurrence in the BSISO-1 phases in specific*  
242 *month*

243 Similar to Figure 4, Figure 5 illustrates the probability of extreme rainfall caused by each  
244 the BSISO-2 phases in specific months. From May to July, the phase 1, 3, 6 and 8 display the  
245 closest linkage with the extreme rainfall, with the highest probability of extreme rainfall is



246 observed in North Vietnam (Fig. 5a, e, f, g) and Central Highlands (Fig. 5b, g). However, from  
 247 August the phase 3, 1, 4 and 6 play the most important role in modulating the occurrence of  
 248 extreme rainfall. The high probabilities of extreme rainfall tend to occurs in North Vietnam in  
 249 September and then propagate southward to Central Highland and Southern Vietnam in  
 250 October. Therefore, although the BSISO-2 has different period compared to the BSISO-1, it  
 251 also related to the southward propagation of extreme rainfall in Vietnam from summer to  
 252 autumn.



253

254 *Figure 5. Same as Fig. 4, except for the BSISO-2 phases*

255

### 256 3.3. Linkages of MJO and the occurrence of extreme rainfall

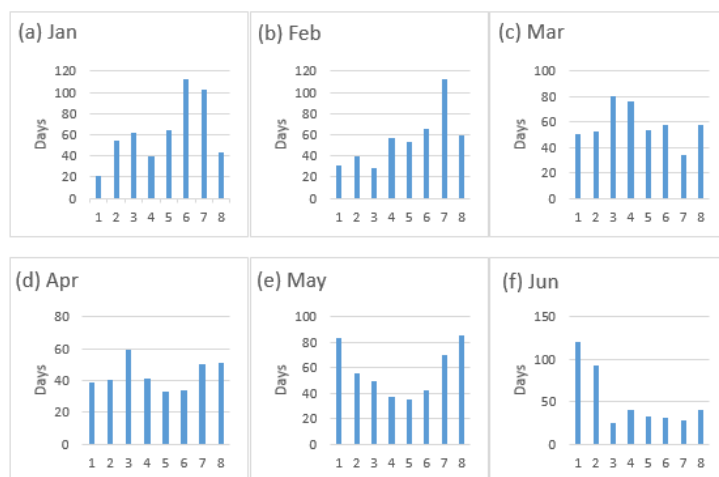
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258 Figures 6 and 7 depict the frequency of occurrence of MJO phases and the corresponding  
 259 anomalous rainfall associated with the most frequent MJO phase. It can be seen that in certain  
 260 months, some MJO phases tend to occur more frequently than others, although the difference  
 261 in frequency between phases is not significant. In January, phases 6 and 7 exhibit higher  
 262 frequencies (112 and 103 days, respectively) compared to other phases. Moving to February,  
 263 phase 7 has the highest occurrence frequency (112 days) while from March to April, it is  
 264 replaced by phase 3. From May to July, phases 1 has the highest occurrence frequencies,  
 265 followed by Phase 2 in August. From September to October, phase 5 occurs the most  
 266 frequently, that then replaced by phase 4 in November. Finally, in December, phase 5 once  
 267 again is the most frequent phase among these others. While anomalous rainfall displays  
 268 negative values in almost phase in summer months, it is significantly increased in Central and  
 North Vietnam in phase 5, from September to October. This result indicates that, the activities

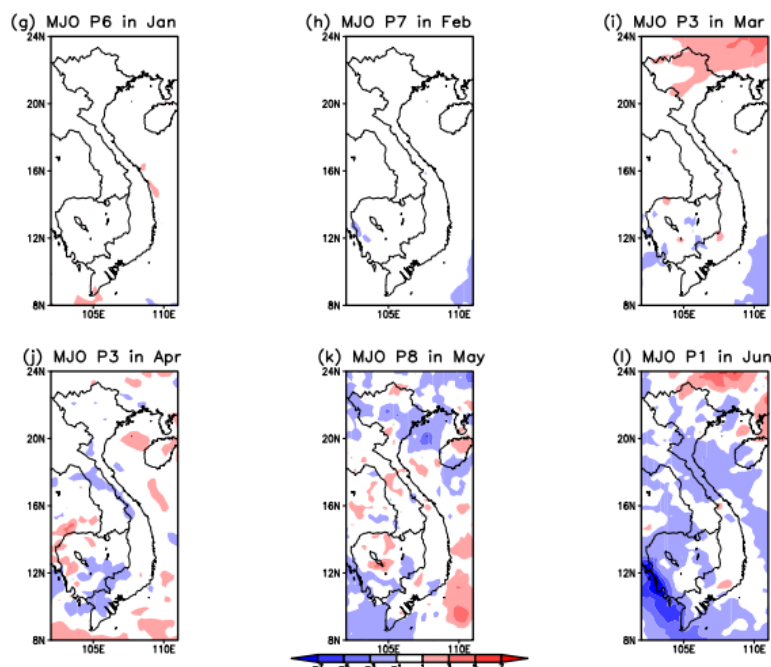




269 of MJO primarily inhibit the rainfall in Vietnam in summer while they intensify the rainfall  
270 from late summer to early autumn.



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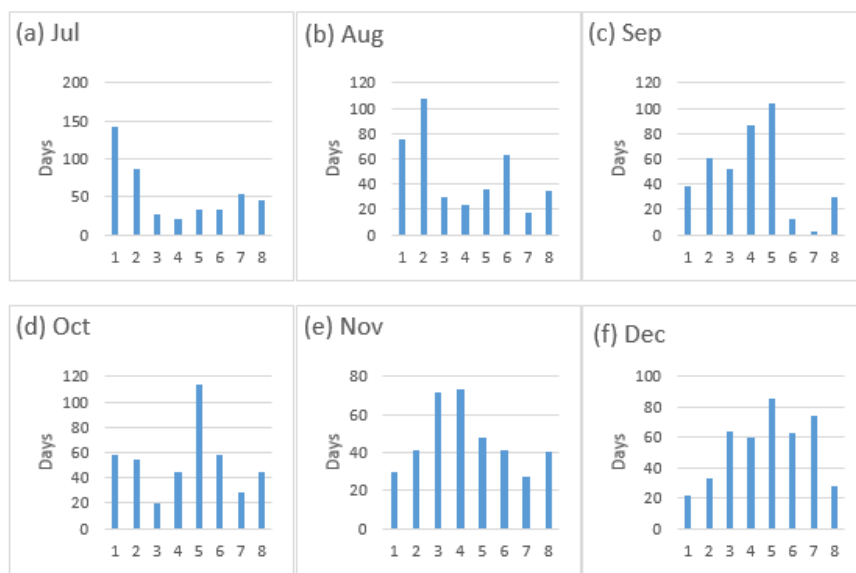


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273 *Figure 6. Same as Fig. 2, except for the MJO*

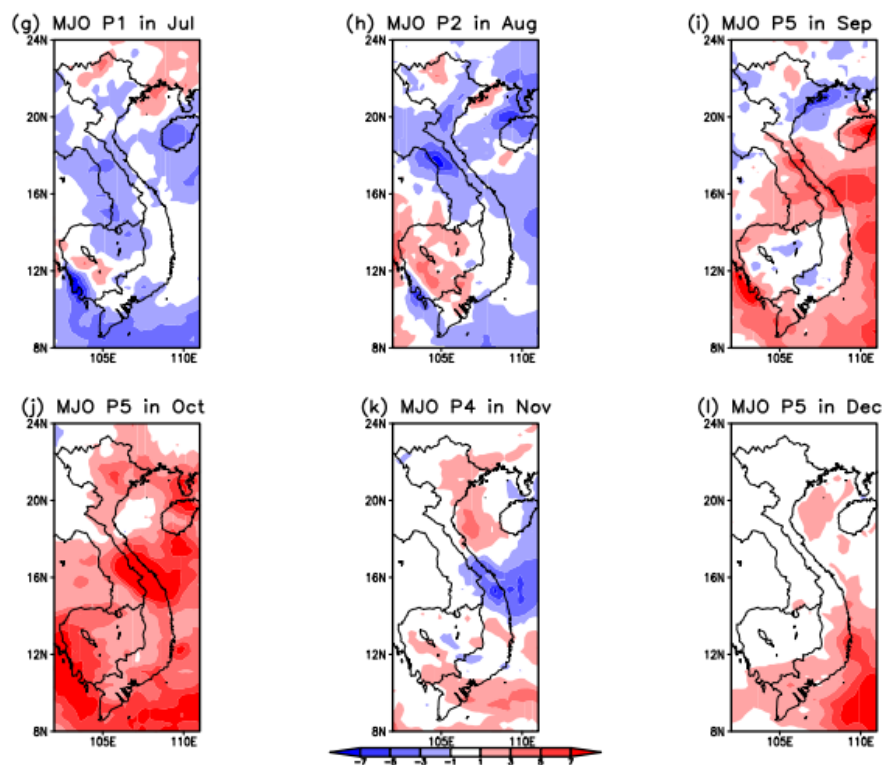


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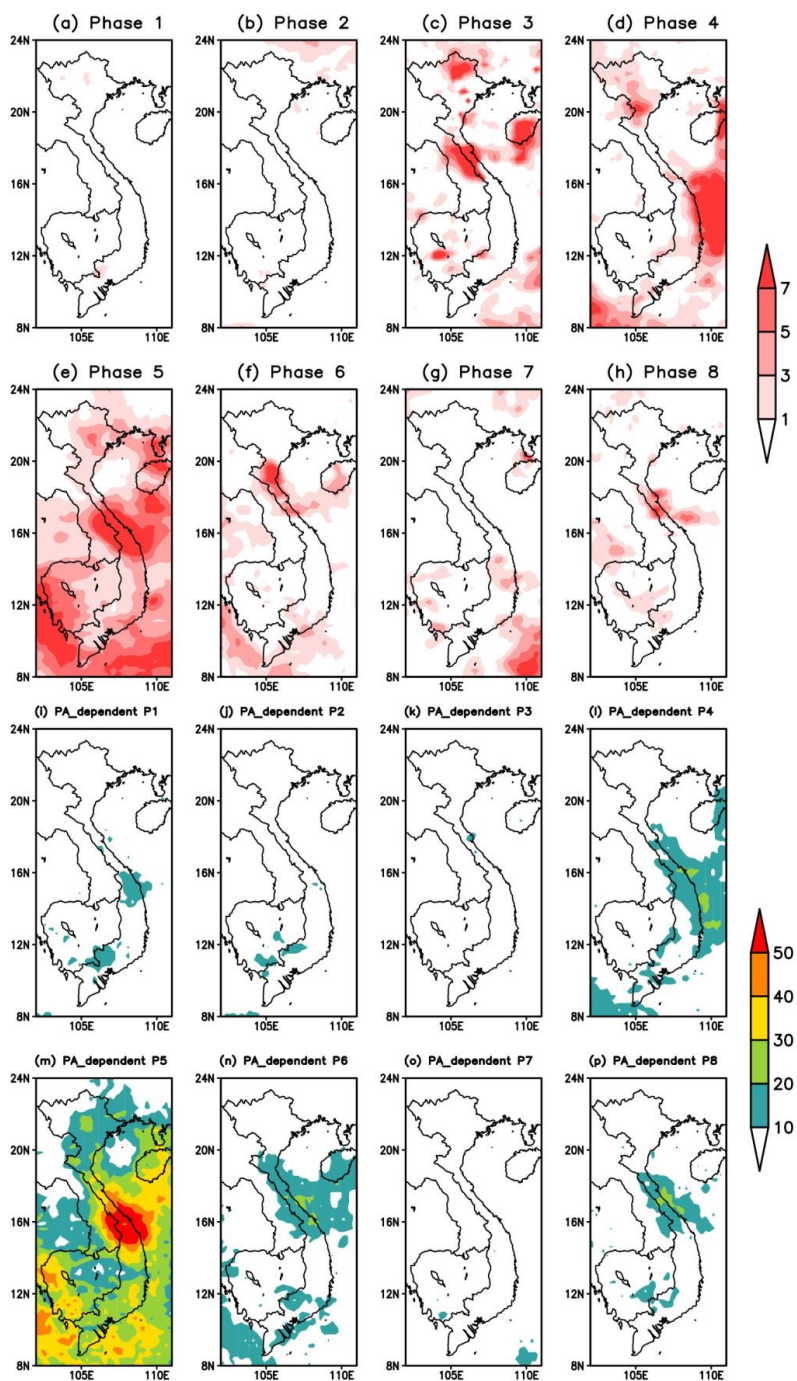
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279 *Figure 7 Same as Fig. 2, except for the MJO*

280 From January to April, while the MJO displays high frequency, the anomalous rainfall is  
281 very small in Vietnam, indicating the insignificant relationship of the MJO with rainfall in the  
282 country (Fig. 6g–k). These patterns are consistent with the fact that this period is dry season in  
283 Vietnam. The domination of cold surge setups a stable condition that prevent the formation of  
284 deep convection. In summer months, from May to August, the phase 1, 2 and 8 display highest  
285 relationship with the anomalous rainfall, which is characterized by decrease of rainfall in North  
286 Central. In contrast, from September to October, the phase 5 is the most important phase  
287 modulating anomalous rainfall in Vietnam, with an high positive anomalous rainfall values in  
288 North Central. In the following months, there is additional contribution of phase 4 on the  
289 variation of rainfall; however, positive anomalous rainfall tend to diminish and propagate  
290 southward as winter approaches.

291 Figure 8 depicts the anomalous rainfall and the probability of extreme rainfall occur in  
292 each MJO phase in October. It can be seen that, while the signal of rainfall is insignificant in  
293 phase 1, 2, 7 and 8, consistent with the fact that deep convection in the Western North Pacific  
294 is suppressed in these MJO phases. In contrast, the anomalous rainfall and extreme rainfall  
295 display great values in the phases from 3 to 6, especially over North Central since these phase  
296 favor for the development of deep convection. Note that, the highest anomalous values are  
297 observed in phase 5, indicating the closest relationship of this MJO phase and rainfall in Central  
298 Vietnam.





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*Figure 8: Anomalous rainfall and the probability of extreme rainfall occur in each MJO phase in October*

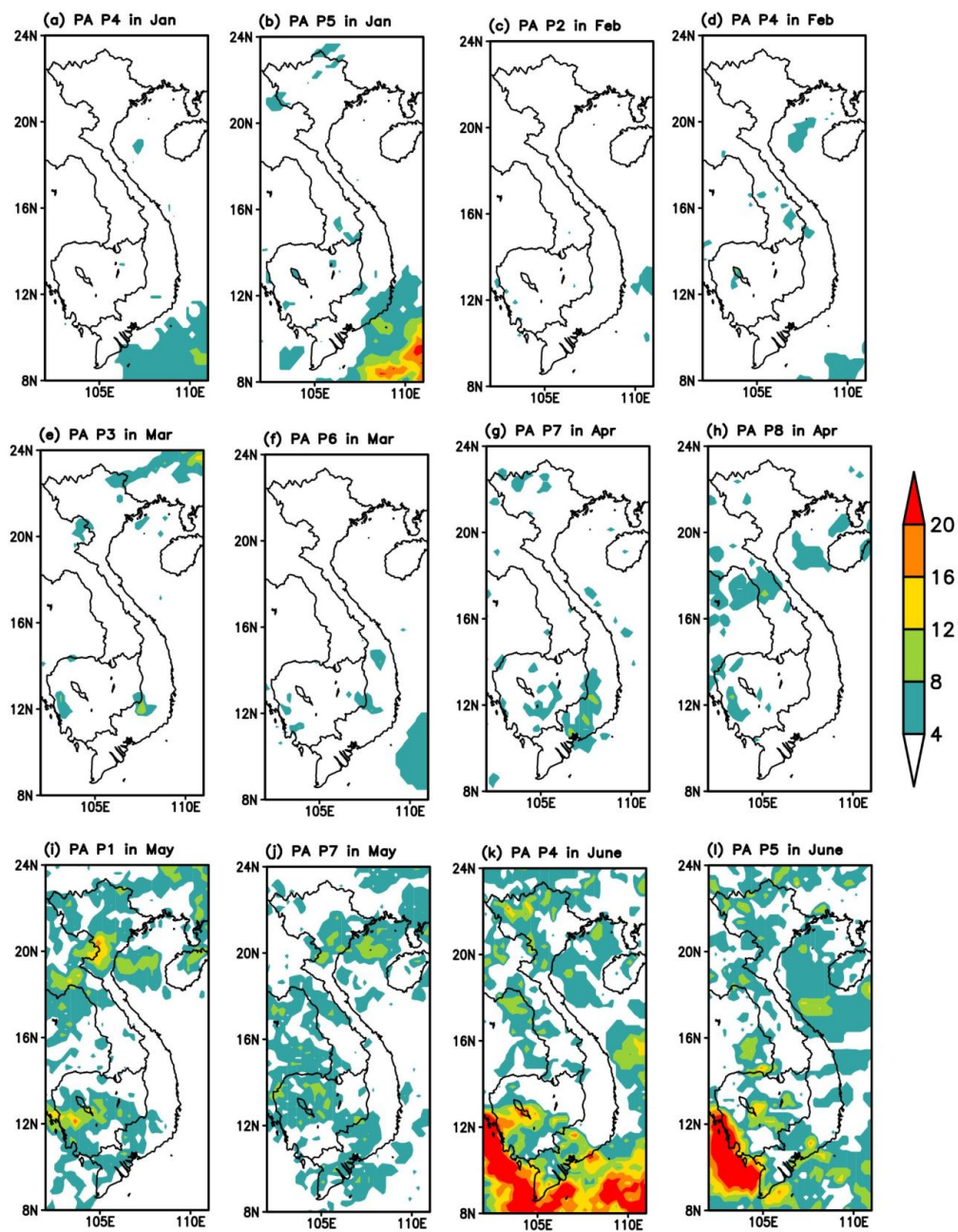


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303           The probability of extreme rainfall events in individual MJO phase in certain months are  
304 plotted in Fig. 9. It can be seen that, from January to April, signal of extreme rainfall is  
305 insignificant, consistent with the dry season in the country. The probability of extreme rainfall  
306 events starts increasing in May, with the most pronounced values are observed in North and  
307 South Vietnam. These values range from 4–20 percentage, occurring in the phase 1 and 7 in  
308 May and phase 4 and 5 in June. This increment of the probability of extreme rainfall is due to  
309 the fact that, summer is rainy season in Vietnam. Similar to Figure 9, Figure 10 illustrates the  
310 probability of extreme rainfall caused by each phase in specific months. In July, the probability  
311 of extreme rainfall is nearly negligible; however, it increases significantly in phase 6 in August.  
312 Moving to September, the probability of extreme rainfall is continuously intensified in the  
313 Central and Southern regions during phases 3 and 4. In October, the highest frequency of  
314 extreme rainfall is found in the middle of Central Vietnam during phase 5 while it shows small  
315 values in the Northern Central during phase 6. In the following months, the probability of  
316 extreme rainfall diminishes rapidly, that is consistent with the withdrawal of rainy season in  
317 Vietnam. The probability of extreme rainfall is nearly zero in December, and the signal of the  
318 high probability is only observed in the oceanic regions to the south of the Bien Dong.

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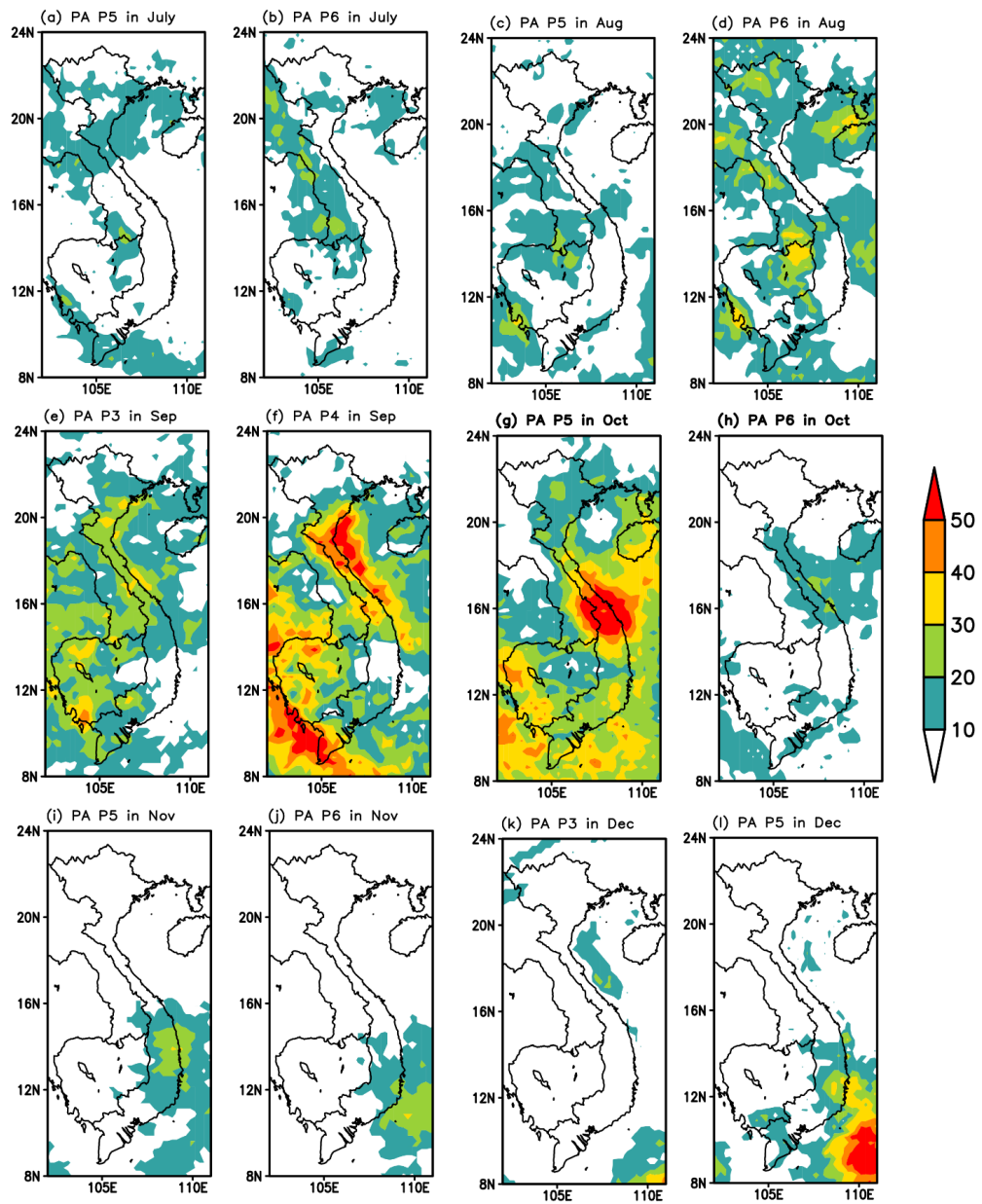
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*Figure 9 illustrates some conditional probabilities (PA) of extreme rainfall events occurring with various phases in months 1-6 of the MJO*

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328 *Figure 10. Same as Fig. 9, except for other months*



329 **4. Conclusion**

330 In this study, the linkage between the activities of the BSISO and MJO and extreme  
331 rainfall events in Vietnam were explored using high-resolution satellite rainfall data  
332 (CMORPH) and BSISO and MJO indexes. The results can be summarized as below:

333 The BSISO is most active in summer, that primarily influence the variation of rainfall in  
334 North and South Vietnam. The phase 6 and phase 7 of BSISO-1 appear to be the two most  
335 important phases contributing to the increase of the probability of extreme rainfall in North and  
336 South Vietnam in summer. As autumn approaches, there are additional contributions of phase  
337 5 and phase 8 on the occurrence of the extreme rainfall. Note that, the extreme rainfall display  
338 a southward propagation, from North to Central Vietnam in autumn. On the other hand, the  
339 phase 3, 6 and 8 of BSISO-2 has most important influence on the probability of extreme rainfall  
340 in summer and the phase 1, 3 and 4 play the most important role in modulating extreme rainfall  
341 in autumn.

342 In a different manner, the MJO is most active in autumn, that primarily influences the  
343 rainfall variations in Central Vietnam. In summer, the relationship of MJO and rainfall in  
344 Vietnam is not as clear, although decrease of rainfall is observed over North Central in some  
345 phase. The relationship become more dominant as autumn approaches. While the phase 1, 2, 7  
346 and 8 are associated with dry condition in Vietnam, the propability of the extreme rainfall tends  
347 to increase in phase 3 to 6. Especially in phase 5, the propability display the highest values,  
348 indicating the close relationship between the MJO and extreme rainfall in Vietnam.

349

350 **Competing interests**

351 The authors declare that they have no conflict of interest

352

353 **Acknowledgment**

354 This research is funded by the Ministry of Natural Resources and Environment in project code  
355 2022.06.07 entitled “Research and develop technology for intraseasonal forecasting (10 to 45  
356 days) to predict severe rainfall and prevent natural disasters”

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