Sensitivity of tropical orographic precipitation to wind speed with implications for future projections

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Abstract. Some of the rainiest regions on Earth lie upstream of tropical mountains, where the interaction of prevailing winds with orography produces frequent precipitating convection. Yet, the response of tropical orographic precipitation to the large-scale wind and temperature variations induced by anthropogenic climate change remains largely unconstrained. Here, we quantify the sensitivity of tropical orographic precipitation to background cross-slope wind using theory, idealized simulations, and observations. We build on a recently developed theoretical framework that predicts enhanced seasonal-mean convective precipitation in response to cooling and moistening of the lower free-troposphere by stationary orographic gravity waves. Using this framework and convection-permitting simulations, we show that higher cross-slope wind speeds deepen the penetration of the cool and moist gravity wave perturbation upstream of orography, resulting in a mean rainfall increase of 20–30% per m s⁻¹ increase in cross-slope wind speed. Additionally, we show that orographic precipitation in five tropical regions exhibits a similar dependence on changes in cross-slope wind at both seasonal and daily timescales. Given next-century changes in large-scale winds around tropical orography projected by global climate models, this strong scaling rate implies wind-induced changes in some of Earth’s rainiest regions that are comparable with any produced directly by increases in global mean temperature and humidity.

1 Introduction

Mountains alter the distribution of rainfall in many tropical regions, including South and Southeast Asia (Shige et al., 2017; Ramesh et al., 2021), the Maritime continent (As-syakur et al., 2016), and the Central Andes (Espinoza et al., 2015). Because orographic precipitation is an essential source of freshwater for much of the tropics’ population (Viviroli et al., 2020), it is crucial to understand its interannual variability and its potential changes with anthropogenic global warming. Although such changes in seasonal-mean tropical precipitation at large spatial scales have been widely studied (e.g., Byrne et al., 2018; Wang et al., 2021), changes in low-latitude orographic rainfall have been the subject of much less investigation.

Most tropical precipitation stems from convective weather systems (Houze et al., 2015), which are influenced by mountains in two main ways (Kirshbaum et al., 2018): thermal forcing (via radiative heating of sloping terrain) and mechanical forcing (forced ascent of background flow over orography). This paper is only concerned with mechanical orographic forcing, which produces some of the most intense regions of precipitation in the tropics. Hereafter, “orographic rainfall” will be used to refer
to convective rainfall altered by mechanical orographic forcing. This type of precipitation is controlled by both thermodynamic factors (e.g., static stability and humidity) and dynamical factors. Understanding these controls, in combination with projected changes in large-scale conditions upstream of mountains, is key to anticipating future changes in rainfall hotspots and freshwater resources.

Decades of observations have facilitated progress in understanding orographic rainfall, with some studies finding purely thermodynamic controls, such as sea-surface temperature (SST) variations over the Arabian sea driving rainfall variations over India’s Western Ghats (Vecchi and Harrison, 2004; Roxy and Tanimoto, 2007). Other studies have proposed large-scale dynamical controls, such as shifts in background winds, as a cause of interannual variability (Varikoden et al., 2019; Shrivastava et al., 2017). Using a global climate model with parameterized convection, Rajendran et al. (2012) suggested a future reduction in rainfall over the Western Ghats (despite an increase in total Indian monsoon rainfall) because of weakened winds over the southern part of the region and increased static stability. However, none of these studies delineate clear mechanisms coupling orographic rainfall with large-scale temperature or wind changes. Here we aim to understand and quantify how changes in large-scale horizontal winds alter tropical orographic rainfall, recognizing that global climate change includes such wind changes together with changes in global mean temperatures and humidities (we leave the response to the large-scale thermodynamic state for future work).

While it may seem evident that orographic rainfall increases with background wind speed, the magnitude of this dependence is less obvious. A null hypothesis can be obtained using the “upslope flow” theory (Roe, 2005), which posits that precipitation is proportional to the surface vertical motion $U \partial h / \partial x$ ($U$ is background wind in the cross-slope direction $x$, and $h$ is surface height). Under this argument, considering a typical basic-state $U$ of 10 m s$^{-1}$, a 1 m s$^{-1}$ change in cross-slope wind should yield a 10% change in orographic rain. The upslope flow model turns out to be a poor descriptor of observed tropical rainfall (Nicolas and Boos, 2024), and here we strive to obtain a more reliable estimate for the sensitivity of tropical orographic rainfall to cross-slope wind by building on a recently developed theoretical framework (Nicolas and Boos, 2022). We obtain a much larger scaling rate than the above $\sim 10 \% (\text{m s}^{-1})^{-1}$, then verify this scaling rate in convection-permitting simulations and observations. We end by discussing the implications for future rainfall changes in some tropical orographic regions.

## 2 Sensitivity of tropical orographic precipitation to wind speed: theoretical basis

We present a new scaling for the sensitivity of orographic rainfall to changes in background wind, based on a recent theory that couples gravity wave dynamics with a convective closure (Nicolas and Boos, 2022). We focus on regions upstream of mountain peaks, where precipitation rates are highest. Orographic precipitation in this theory stems from the response of precipitating clouds to a stationary mountain wave (Fig. 1A). The orographic precipitation perturbation $P'$, relative to an upstream background precipitation rate $P_0$, is proportional to the mean buoyancy perturbation created by the wave’s lower-free-tropospheric perturbations of temperature and humidity (denoted $T'_L$ and $q'_L$), and a boundary layer equivalent potential

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temperature anomaly $\theta'_eB$ (Ahmed et al., 2020):

$$P' = \beta \left( \frac{\theta'_eB}{\tau_b} + \frac{q'_L}{\tau_q} - \frac{T'_L}{\tau_T} \right),$$

(1)

where $\tau_b$, $\tau_q$, and $\tau_T$ are adjustment timescales (Appendix A). Here $q$ is in temperature units (scaled by the latent heat of vaporization divided by the specific heat of dry air $L_v/c_p$), and $\beta$ is a constant converting a convective heating rate into a precipitation rate ($\beta = c_p p_T/(L_v g)$, where $p_T \simeq 800$ hPa is the tropospheric depth). Hereafter, boundary layer averages (subscript $B$) are taken between the surface and 900 hPa, and lower-free tropospheric averages (subscript $L$) from 900 hPa to 600 hPa; sensitivity of results to these choices are discussed below. (1) depends positively on $\theta'_eB$ because it increases undilute plume buoyancy, and depends positively on $q'_L$ through its effect on entrainment (the entrainment of moister free-tropospheric air is less efficient at reducing the buoyancy of ensembles of convective plumes). The negative dependence on $T'_L$ arises through its combined effect on undilute buoyancy (a colder lower-free-troposphere yields higher convective available potential energy) and on the subsaturation of the free troposphere (Ahmed et al., 2020).

Our simplest scaling further neglects variations in boundary layer equivalent potential temperature ($\theta'_eB = 0$) because it is more strongly affected by SST variations or land surface fluxes than by mechanical orographic forcing (Nicolas and Boos, 2024). This assumption is later relaxed.

The thermodynamic perturbations $T'$ and $q'$ result from the background wind, with speed $U$, being lifted by orography, as well as the convective response. For relatively low mountains with a weak convective feedback, these perturbations can be approximated by a linear, adiabatic, stationary mountain wave (nonlinear effects become important when the nondimensional mountain height $Nh_0/U \gtrsim 1$, where $N$ is the Brunt-Väisälä frequency and $h_0$ the peak mountain height). The mountain wave produces positive vertical displacement $\eta$ in the lower troposphere upstream of a ridge, resulting in a cool and moist perturbation (e.g., Fig. 1A). These adiabatic perturbations—denoted $T_{aL}$ and $q_{aL}$—produce, through (1), a precipitation perturbation

$$P_a = \beta \left( -\frac{T_{aL}}{\tau_T} + \frac{q_{aL}}{\tau_q} \right) \simeq \beta \left( \frac{1}{\tau_T} \frac{d\eta_0}{dz} - \frac{1}{\tau_q} \frac{d\eta_0}{dz} \right) \eta_L,$$

(2)

where $d\eta_0/dz$ is a lower-tropospheric moisture stratification and $d\eta_0/dz$ is a lower-tropospheric dry static energy stratification (divided by $c_p$).

Convection feeds back on these perturbations, modifying the precipitation given by (2). For example, enhanced precipitating convection upstream of orography ($P_a > 0$) heats and dries the troposphere, thereby weakening the cool and moist lower-tropospheric perturbation. The system can be closed using conservation of temperature and moisture with other constraints from tropical dynamics (Nicolas and Boos, 2022), yielding a secondary precipitation perturbation $P_m$, obeying

$$\frac{dP_m}{dx} + \frac{P_m + P_a}{L_q} = 0,$$

(3)

where $L_q$ is a length scale for the relaxation of lower-free-tropospheric moisture by convection (Appendix A). For $U = 10 \text{ m s}^{-1}$, $L_q \approx 3000 \text{ km}$, which is large compared with the horizontal length scale of the orographic forcing. Thus, we expect $P_m \ll P_a$.

For an idealized mountain of peak height 500 m, the solutions (Appendix A) feature a broad orographic enhancement of precipitation upstream of the mountain (Fig. 1A), peaking around 5 mm day$^{-1}$ on the upwind slope. The total precipitation...
Figure 1. Orographic perturbations of temperature and precipitation in linear theory and a cloud resolving model, with sensitivities to wind speed. (A) Temperature perturbation $T_a(x, p)$ in a stationary linear mountain wave with uniform static stability $N = 0.01 \, \text{s}^{-1}$ and cross-slope wind $U = 10 \, \text{m s}^{-1}$, for a 500 m mountain (color shading), precipitation perturbation $P' = \max(P_a + P_m, -P_0)$ from the linear theory (dark blue line, Eqs. 2 and 3), and the component of $P'$ due to the adiabatic mountain wave alone $P_a$ (cyan line). $P'$ in a convection-permitting simulation (see text) is shown in green. The gray line shows surface height. $T_a$ is proportional to the vertical displacement $\eta(x, p)$ in the mountain wave, with scale shown at the bottom of the colorbar. (B) Vertical structure of temperature perturbations at $x = -100 \, \text{km}$ in the theory (orange) and simulations (red), with $U = 10 \, \text{m s}^{-1}$ (solid) and 12 m s$^{-1}$ (dashed). Arrows indicate the vertical stretching of the orographic gravity wave with increased wind. (C) Fractional increase in the maximum precipitation perturbation (hatched bars) and the precipitation perturbation averaged within 30 km of the maximum (solid), in the linear theory with and without convective feedback, and in the simulations. Simulation results display a 95% confidence interval (obtained by block bootstrapping, using 20 day blocks).

Anomaly $P' = P_a + P_m$ is only about 10% smaller there than the anomaly $P_a$ that neglects convective feedback on the gravity wave, confirming the small damping effect of the feedback. A rain shadow extends downstream of the ridge, and negative precipitation values are prevented by enforcing $P' \geq -P_0$, where we take $P_0 = 4.5 \, \text{mm day}^{-1}$ to conform with simulations presented below.

The sensitivity of $P'$ to the background wind speed $U$ arises through the vertical structure of $\eta$ upstream of the mountain, which is wave-like, with wavelength $\lambda_z = 2\pi U/N$ (Fig. 1A). In the linear theory (2), $\eta$ is proportional to $-T_a$. In order to later compare results with simulations (for which temperature perturbations are more readily available than $\eta$), we thus show the vertical structure of $T_a$ in Fig. 1B (solid orange line). An increase in $U$ (dashed orange line) results in deeper penetration of the ascending region of the wave (where $T_a < 0$), which amplifies $T_{a, L}$ upstream of orography. Similarly, $q_{a, L}$ is amplified by the same amount. By (2), this produces an increase in $P_a$, and, because the convective feedback $P_m$ is modest, also in $P'$. 

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The precipitation increase produced by an increase in background wind $U$ is quantified in Fig. 1C using two metrics: maximum precipitation perturbation $P'_{\text{max}}$ and precipitation perturbation averaged within 30 km of the maximum $P'_{|x_{\text{max}}\pm30\text{ km}|}$. When $U$ increases from 10 m s$^{-1}$ to 12 m s$^{-1}$, these quantities respectively increase by 27 % (m s$^{-1}$)$^{-1}$ and 30 % (m s$^{-1}$)$^{-1}$. Most of these increases (25 % (m s$^{-1}$)$^{-1}$ and 27 % (m s$^{-1}$)$^{-1}$) are explained by changes in $P_a$. This is a large sensitivity compared with the 10 % (m s$^{-1}$)$^{-1}$ expected from simple upslope flow considerations (see Introduction). Here, the increase stems from deeper vertical penetration of orographic ascent resulting in a stronger upstream cool and moist lower-tropospheric anomaly, in turn yielding a stronger precipitation anomaly. These sensitivities exhibit little dependence on convective time scales: halving or doubling them changes the sensitivities by less than 2 percentage points. However, sensitivities vary strongly with the levels used to define the lower free troposphere: lowering its top to 650 hPa from 600 hPa changes the sensitivity of $P'_{\text{max}}$ to 19 % (m s$^{-1}$)$^{-1}$, while raising its top to 550 hPa yields 34 % (m s$^{-1}$)$^{-1}$. Using a convective closure that depends more continuously on thermodynamic perturbations at different levels (e.g., Kuang, 2010) may offer an avenue of improvement, at the expense of conceptual simplicity. Next, we use convection-permitting simulations and observations to validate these theoretical sensitivities.

3 Sensitivity in idealized simulations

3.1 Model setup

Our model setup is very similar to that used in Nicolas and Boos (2022) and is described here succinctly. We use the Weather Research and Forecasting model (WRF-ARW, version 4.1.5, Skamarock et al., 2019) to represent a doubly periodic long channel (9810 km wide in $x$ by 198 km in $y$), with a $y$-invariant 500 m-high mountain identical to that used in the theory. The 3 km horizontal grid spacing and 60 terrain-following vertical levels (spanning from the surface to 10 hPa) are used to represent deep convective clouds without a convective parameterization. The domain is ocean-covered with a fixed SST of 300 K, except over the mountain where we employ the Noah-MP land surface scheme (Niu et al., 2011; Yang et al., 2011), with a no-flux bottom boundary condition. We fix the Coriolis parameter at 20° latitude, and prescribe a constant background meridional pressure gradient which maintains a uniform background geostrophic zonal wind with speed $U$. We use a state of perpetual equinox (with a diurnal cycle), and calculate radiation interactively every hour using the RRTMG scheme (Iacono et al., 2008). Turbulent fluxes are calculated diffusively with fixed horizontal diffusion of 300 m$^{-2}$s$^{-1}$ and vertical diffusion of 100 m$^{-2}$s$^{-1}$, with the Mellor-Yamada-Janjić scheme (Mellor and Yamada, 1982; Janjić, 2002) used for boundary layer fluxes. We use the Thompson scheme for microphysics (Thompson et al., 2008).

3.2 Changes in precipitation and free-tropospheric thermodynamic perturbations

We run two simulations for 1000 days each (after discarding 250 days of spin-up), which only differ in background winds: one has $U = 10$ m s$^{-1}$, the other $U = 12$ m s$^{-1}$. In the 10 m s$^{-1}$ run, $P'$ (Fig. 1A, green line) has numerous similarities with the theory, especially the peak precipitation rate and length scale of upstream orographic enhancement. Peak rainfall in the theory
is shifted \( \sim 25 \text{ km} \) upstream compared to the simulations, a defect attributable to the convective closure: using (1) to diagnose \( P' \) with temperature and moisture perturbations from the simulations, instead of from a linear gravity wave solution, results in a similar shift (Fig. 2A). One reason for this upstream bias is the neglect of the downwind drift of hydrometeors, with a time scale of \( \mathcal{O}(1000) \) s (Smith and Barstad, 2004) that can shift the precipitation profile \( \sim 10 \text{ km} \). A second reason is the theory’s vertically uniform dependence of rainfall on \( T \) and \( q \) perturbations in the lower troposphere: giving higher weight to low levels would shift the rainfall maximum downstream because maxima in \( T \) and \( q \) perturbations shift downstream at lower levels (Fig. 1A). Stronger differences appear between the theoretical and simulated \( P' \) downstream of the mountain, which we show below is due to neglect of \( \theta_{IB} \) variations in our simplest scaling.

Both \( P'_{\text{max}} \) and \( P'_{(x = \pm 30 \text{ km})} \) increase between 20 and 30 \( \text{m s}^{-1} \) between the two simulations, commensurate with the theoretical prediction (Fig. 1C). Is this increase attributable to a deeper penetration of the stationary gravity wave cooling and moistening the lower free troposphere at higher \( U \), as our theory suggests? To assess this we evaluate \( T'(x = -100 \text{ km}, p) \) in both runs (Fig. 1B, red lines), where the reference profile is averaged over \( x \in (-4000 \text{ km}, -2500 \text{ km}) \). \( T' \) displays a gravity
wave structure in many ways similar to that of the adiabatic, linear \( T' \). With increased wind, the cool perturbation penetrates deeper (shown by black arrows in Fig. 1B), decreasing \( T'_L \). While quantitative differences with the theory’s \( T' \) arise because static stability is not vertically uniform in the simulations, the change in \( T' \) with increased wind is well captured by linear theory.

To assess whether this deepening of the \( T'_L \) structure, with the accompanying changes in \( q'_L \), can quantitatively explain the increase in \( P' \), we compute precipitation from the linear closure used in our theory: \( P'_{qT} = \beta (q'_L / \tau_q - T'_L / \tau_T) \) (Fig. 2A, blue lines). This diagnostic captures the magnitude of the simulated precipitation peak for \( U = 12 \text{ m s}^{-1} \) with a similar upstream shift as in the theory, but shows a too-weak dependence on \( U \). Specifically, the change in upstream \( P'_{qT} \) (averaged within 30 km of its maximum) between both simulations is only 7 \( \% \) (m s\(^{-1}\))\(^{-1} \) (Fig. 2D, blue bar), indicating that the increase in peak precipitation with increased wind is only partly attributable to stronger lower-tropospheric \( T \) and \( q \) perturbations.

### 3.3 Changes in boundary-layer moist entropy

We now show that this discrepancy can be resolved by considering variations in \( \theta'_{eB} \), and that these variations are controlled by the same mountain wave dynamics discussed earlier. Using \( \theta'_{eB} \) in conjunction with \( T'_L \) and \( q'_L \) (all diagnosed from simulations) in (1) generally improves comparison to the simulated \( P' \), better fitting upstream rain rates and the rain shadow (Fig. 2B, magenta lines). The value of this diagnosed precipitation, \( \beta (q'_L / \tau_q - T'_L / \tau_T + \theta'_{eB} / \tau_b) \), still averaged within 30 km of its maximum, increases by 17 \( \% \) (m s\(^{-1}\))\(^{-1} \), a value much closer to the 24 \( \% \) (m s\(^{-1}\))\(^{-1} \) change in simulated \( P' \) (95\% confidence intervals on these two values overlap; Fig. 2D). The increase in \( \theta'_{eB} \) and the decrease in \( T'_L \) contribute equally to the increase in the \( P' \) maximum, while changes in \( q'_L \) contribute negligibly (Fig. 2C). Thus, the quantitative match between theoretical and simulated precipitation changes in Fig. 1C appears in part fortuitous: the absence of free-tropospheric moistening with increased wind in simulations is compensated for by an increase in \( \theta'_{eB} \).

We now show that the increase in \( \theta'_{eB} \) with increased wind can also be attributed to the vertical stretching of the orographic ascent pattern that occurs with increasing \( U \). The difference (denoted by a \( \Delta \)) between boundary layer \( \theta'_{e} \) in the 12 m s\(^{-1} \) and 10 m s\(^{-1} \) runs is shown in Fig. 3A, with its mass-weighted vertical average \( \Delta [\theta'_{eB}] \) shown in Fig. 3B (solid black). \( \theta'_{eB} \) is about 0.3 K warmer over the upwind slope with increased wind. In order to understand this increase, we diagnose the \( \theta'_{e} \) budget over a subset of pressure levels which do not cross the topography, namely 900–950 hPa. \( \Delta [\theta'_{e}] \) averaged over these levels has a qualitatively similar structure to \( \Delta [\theta'_{eB}] \) upstream of the mountain peak (Fig. 3B), with modest variations for \( x < -100 \text{ km} \) and a sharp increase above the upwind slope.

The \( \theta'_{e} \) budget is

\[
\frac{u \partial \theta'_{e}}{\partial x} + w \frac{\partial \theta'_{e}}{\partial z} = Q_{\theta_{e}},
\]

where all quantities are time and meridional means, and \( Q_{\theta_{e}} \) is an apparent source of \( \theta_{e} \) due to transients (in the boundary layer, its main contributors are surface fluxes, turbulent mixing and penetrative downdrafts). We evaluate the two terms on the left-hand side from temporally and meridionally averaged \( u, w \) and \( \theta_{e} \) fields, and compute \( Q_{\theta_{e}} \) as a residual. Upstream of the ridge top, little accuracy is lost if we replace \( u \) by the background wind \( U \) and \( \partial \theta_{e} / \partial z \) by a constant \( \partial \theta_{e0} / \partial z \). The latter is
Figure 3. \( \theta'_e \) variations between the 10 m s\(^{-1}\) and 12 m s\(^{-1}\) simulations, and their physical drivers. Throughout the figure, \( \Delta[\cdot] \equiv [\cdot]_{12\text{m} \text{s}^{-1}} - [\cdot]_{10\text{m} \text{s}^{-1}} \). (A) \( \Delta \theta'_e \) in the boundary layer (shading). The thick gray line shows the topography. (B) \( \Delta \theta'_e \) (solid) and \( \Delta \theta'_e \) averaged between 900 hPa and 950 hPa (dashed). Note the qualitative similarity between the two profiles upstream of the mountain, with a sharp increase over the upwind slope. (C) Differential budget of \( \theta'_e \) averaged over [900 hPa, 950 hPa] between the two runs. Differences in horizontal gradients of \( \theta'_e \) (black) are balanced by differences in vertical advection (red line) and differences in diabatic sources (orange line). The residual (due to horizontal variations in \( u \) and \( \partial \theta_e / \partial p \)) is shown as a thin blue line. Note the sharp peak in the black line above the mountain’s upwind slope, mostly contributed to by changes in vertical advection. (D) Change in ascent slope \( w/U \) between the two runs, at 925 hPa, as diagnosed from simulations (red line) and from a nonlinear theory (dashed red line, see text). In panels C and D, all terms from simulations are smoothed with a Gaussian filter of standard deviation 6 km to filter out small-scale noise from finite differentiation. In all panels, vertical black lines indicate the upstream boundary and peak of the mountain, and gray shading indicates the downstream region, that is not relevant to the main discussion.

175 averaged 2000–4000 km upstream of the mountain (\( \partial \theta_{e0} / \partial z = -19.8 \text{ K km}^{-1} \) at 925 hPa). Hence, we re-write the budget as

\[
\frac{\partial \theta'_e}{\partial x} \simeq -\frac{w}{U} \frac{\partial \theta_{e0}}{\partial z} + \frac{Q_{\theta_e}}{U}.
\]

(5)

Over the ocean part of the domain (\( x < -100 \text{ km} \)), horizontal gradients in \( \theta'_e \) are constrained to be small by the uniform SST, so the two terms on the right-hand side approximately balance. Over the ridge, surface temperature is not imposed, so variation in either of the right-hand side terms can accompany variations in \( \theta_e \) gradients.
Fig. 3C shows the difference (denoted by a $\Delta$) in each of the terms in (5) between the 12 m s$^{-1}$ and 10 m s$^{-1}$ runs, averaged over 900–950 hPa. Because $\partial \theta'_e / \partial x$ is small in each run for $x < -100$ km, $\Delta [\partial \theta'_e / \partial x]$ is also small there. Over the mountain, the sharp increase in $\Delta \theta'_e$ seen in Fig. 3B translates into a large peak in $\Delta [\partial \theta'_e / \partial x]$ around $x \in (-100 \text{ km}, -50 \text{ km})$. Importantly, most of this peak is associated with the change in vertical advection (red line).

We now argue that this change in vertical advection is explained by mountain wave dynamics. Because the vertical $\theta_e$ gradient has been fixed, this increase in vertical advection is driven by an increase in the ratio of vertical to horizontal flow $w/U$. Why does this ratio increase? At the surface, where $w = U \partial h / \partial x$, it is equal to the surface slope and cannot change as $U$ is increased. Aloft, however, the ascent spreads over a deeper layer with higher $U$ (due to the vertical expansion of the mountain wave discussed in the main text), which causes an increase in $w/U$. This is illustrated in Fig. 3D, where we compare the change in $w/U$ from simulations and from mountain wave theory. We use Long’s equation (Long, 1953) to solve for the mountain wave, as the linearization of the boundary condition in classical linear mountain wave theory yields inaccuracies in the boundary layer. Neglecting damping, the vertical displacement $\eta$ satisfies

$$
\partial_z \eta + \frac{N^2}{U^2} \eta = 0, \quad \eta(z = h(x)) = h(x),
$$

with a radiation upper boundary condition. We solve (6) using an iterative procedure (Lilly and Klemp, 1979), and obtain $w$ as $U \partial \eta / \partial x$. Good agreement between the simulated and theoretical change in $w/U$ indicates that mountain wave dynamics explain the stronger boundary layer $\theta'_e$ perturbation and, ultimately, the stronger rainfall peak with increased $U$.

4 Observed sensitivity at various time scales

Do observations support the above theoretical and model-derived sensitivities? The framework developed in this work quantifies changes in the seasonal-mean orographic precipitation perturbation $P' = P - P_0$, where $P$ and $P_0$ are the total and background precipitation rates, respectively. We now aim to evaluate the observed dependence of $P'$ on variations in the background cross-slope wind $U$, recognizing that changes in $U$ may also be associated with changes in $P_0$. Yet, all the orographic regions we consider lie downstream of an ocean, over which rainfall observations at the fine spatial scales needed here are only available for the past two decades. Therefore, because $P_0$ is 3–5 times smaller than $P'$ in three of our regions, we first neglect $P_0$ and estimate the sensitivity of $P$ to interannual changes in $U$ using gauge-based rainfall observations. We then estimate the sensitivity of $P'$ to $U$ using two other products: satellite-estimated daily precipitation for 2001–2020, and reanalysis-derived seasonal-mean precipitation for 1960–2015 (Appendix B). These two approaches come with a caveat: one may question whether daily-mean $P'$ scales similarly to seasonal-mean $P'$ with changes in $U$; and reanalysis precipitation is largely produced by a model prior to 1979. However, the consistency of the estimated sensitivities across regions and time scales suggest that the result is robust.

We evaluate orographic rainfall variations in five regions of South and Southeast Asia: the west coasts of India and Myanmar, and the east coasts of Vietnam, Malaysia, and the Philippines (see Appendix B and Fig. S1 in the Supplement for details on

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1For a discussion of how the precipitation-buoyancy relationship (1) behaves at different time scales, see Ahmed et al. (2020) (their Fig. 7).
Figure 4. Evidence for large precipitation scaling rates from observational and reanalysis data at multiple time scales. (A) Observed summer mean (June-August, 1960-2015) precipitation over India and 100 m winds from reanalysis. Gray contours mark 500 m surface height. (B) Sensitivity of summer-mean precipitation to cross-slope wind speed upstream of the Western Ghats. Regions hatched in white satisfy the false discovery rate criterion (Wilks, 2016) with $\alpha = 0.1$. Winds are averaged in the blue dashed rectangle shown in A. (C) Sensitivity of orographic precipitation $P$, and precipitation perturbation $P' = P - P_0$, to upstream cross-slope wind in multiple regions and at multiple time scales. In all cases, $P$ is averaged in the peak rainfall region and $P_0$ is averaged from 200 km to 400 km upstream (respectively dashed and solid black boxes in B for the Western Ghats; see Fig. S1 in the Supplement for other regions). Light gray bars show the sensitivity of observed seasonal-mean $P$, medium gray bars the sensitivity of seasonal-mean $P'$ from a reanalysis, and dark bars the sensitivity of daily observed $P'$ over 2001-2020. A 95% confidence interval obtained by bootstrapping is shown for each estimate.

In each region, the interaction of prevailing winds with a coastal mountain range creates a precipitation maximum over and upstream of the mountains (Nicolas and Boos, 2024). In the Western Ghats, for example, precipitation rates are two to three times higher than over the core monsoon region of Central India (Fig. 4A). Seasonal-mean cross-slope wind (defined as the projection along the 70° azimuthal angle, roughly east-northeast) is averaged upstream of the Western Ghats (over the blue rectangle in Fig. 4A). This yields a 56-year time series of cross-slope wind speed, on which we regress seasonal-mean $P$ over the Indian subcontinent. The resulting regression slopes are divided by $P$ to obtain relative sensitivities, which exhibit a dipolar pattern wherein regions upstream of mountain peaks are positively associated with $U$, whereas regions in the orographic rain shadow exhibit negative sensitivity (Fig. 4B). A decrease in downstream precipitation with increased $U$ is also visible in a 300-km-wide region in the simulations (Fig. 2A). Rainfall also positively correlates with $U$ across central India, consistent with the stronger diabatic heating of increased monsoon rainfall accompanying a stronger large-scale monsoon circulation (Rodwell and Hoskins, 2001). Absolute sensitivities over Central India are, however, 2–3 times
Figure 5. Distribution of cross-slope wind changes in CMIP6 climate models under a high-emissions scenario. For each region and model, we take the difference between 10 m cross-slope wind, averaged in the same upstream region as in Fig. 4, between 2080–2099 (in the SSP5-8.5 scenario) and 1980–1999 (in the historical run). Results for 37 models are shown as histograms for each region, with the multi-model mean change $\Delta U$, standard deviation $\sigma(\Delta U)$, and mean absolute change $|\Delta U|$. weaker than in the peak rainfall region upstream of the Western Ghats (i.e., the relative sensitivities are elevated over Central India because $P$ is comparatively small there).

Although it cannot be directly compared with our theoretical and model-derived sensitivities of $P'$, we evaluate the sensitivity of spatially averaged $P$ (in the orographic precipitation band marked by a black dashed line in Fig. 4B) to interannual wind changes. It scales at 15 % (m s$^{-1}$)$^{-1}$, with local values as high as 30 % (m s$^{-1}$)$^{-1}$. Fig. 4C (light gray bars) extends this analysis to four other regions. In Myanmar and Vietnam, where $P_0$ is much smaller than $P'$, seasonal-mean $P$ exhibits a similar sensitivity to cross-slope wind as in the Ghats (around 15 % (m s$^{-1}$)$^{-1}$). Sensitivities are much lower in the Philippines and Malaysia, where increased cross-slope winds are associated with large-scale reductions in specific humidity that decrease $P_0$ (Supplement, Fig. S2).

We now estimate the observed sensitivity of $P'$, which can be directly compared with our theoretical and model estimates. Seasonal-mean $P'$ (from reanalysis) and satellite-based daily mean $P'$ are estimated as the difference between $P$ in the peak orographic rainfall region and $P$ in a region 400 km upstream (dashed and solid black rectangles in Fig. 4B for the Western Ghats; see Fig. S1 in the Supplement for other regions). These $P'$ values are regressed on upstream cross-slope wind at the corresponding seasonal or daily time scales. $P'$ is strongly sensitive to changes in $U$ at both seasonal and daily scales, with values ranging from 17 to 34 % (m s$^{-1}$)$^{-1}$ across regions (Fig. 4C, medium and dark gray bars), in line with the theoretical and numerical estimates. While this analysis controls for any variations in $P_0$, it does not control for potential changes in moisture stratification or static stability that may correlate with $U$ (although Fig. S2 in the Supplement suggests such interannual changes are modest in most regions). Differences in climatological cross-slope wind between regions may be another source of inter-regional variability. However, all five regions exhibit strong sensitivities on both time scales that quantitatively agree with the 20–30 % (m s$^{-1}$)$^{-1}$ values seen in our theoretical and model estimates.
Discussion and implication for regional rainfall change

We have presented multiple lines of evidence indicating that tropical orographic rainfall maxima increase with cross-slope wind speed at a rate of 20–30 % (m s\(^{-1}\))\(^{-1}\). This rate is physically grounded, holds in a set of convection-permitting simulations, and is observed in several regions on multiple time scales. While the fact that mechanically forced orographic rainfall increases with wind speed is not surprising, the magnitude of this sensitivity has important implications for tropical rainfall projections. Regional rainfall changes accompanying global warming have traditionally been understood from a thermodynamic standpoint, where an increase in specific humidity following the Clausius-Clapeyron (CC) rate of \(\sim 7 \text{ % K}^{-1}\) implies a similar increase in the magnitude of precipitation minus evaporation (Held and Soden, 2006). This thermodynamic increase has become a null hypothesis for regional precipitation change, with deviations from the CC rate often attributed to changes in winds. Here, we presented a mechanism by which such changes in large-scale winds can affect regional precipitation.

To evaluate whether this mechanism may appreciably strengthen or offset any thermodynamic rainfall change, we evaluate cross-slope wind changes in our five regions in 37 models from the Coupled Model Intercomparison Phase 6 (CMIP6, Eyring et al., 2016, see Table S1 in the Supplement for full list). We evaluate wind changes between the end of the 20\(^{th}\) century in historical simulations and the end of the 21\(^{st}\) century in the high-emissions SSP5-8.5 scenario\(^2\). Models agree on a weakening of \(\sim 0.5 \text{ m s}^{-1}\) in cross-slope wind upstream of the Western Ghats, consistent with a general weakening of monsoon circulations with warming (Douville et al., 2021). Given our sensitivity estimate, this weakening would yield a 10–15 % decrease in the orographic precipitation anomaly \(P'\), or a 9–13 % in total precipitation \(P\) (assuming a fixed \(P_0\) of 3 mm day\(^{-1}\)). This represents a sizeable reduction of the “null-hypothesis” 27 % increase that may result from a CC scaling, assuming a 3.5 K warming in that region (Gutiérrez et al., 2023). In Myanmar, the Philippines, and Malaysia, models disagree on the sign of cross-slope wind changes, but the multi-model mean absolute wind changes remain substantial (0.3–0.5 m s\(^{-1}\)). This implies a potential for large changes in rainfall of either sign. In Vietnam, models agree on a more modest change in winds.

A purely thermodynamic change in orographic precipitation (i.e., one produced by climate warming with fixed cross-slope winds) may be smaller than the CC rate discussed above. By (2), mechanically forced orographic precipitation is set by the background moisture stratification, static stability, and orographic vertical displacement. The first of these likely increases with warming close to the CC rate. Tropical static stability also increases with warming, which strengthens \(T_{aL}\) and thus \(P_a\); at the same time, however, this decreases vertical displacement by contracting the orographic gravity wave, weakening \(P_a\). This may imply a smaller thermodynamic increase than the CC rate, possibly even an overall stagnation or decrease in total precipitation in some regions.

It may be difficult to project future changes in tropical orographic rainfall using climate models because those models do not resolve orographic gravity waves or moist convection, two central processes in orographic precipitation. The width of the rainfall peaks in Fig. 4 is around 60 km, smaller than the grid scale of half the CMIP6 models analyzed here. We suggest that two components are in principle necessary to capture this rainfall distribution: a stationary orographic wave, and the correct sensitivity of convection to temperature and moisture perturbations. The first component can be represented by models if

\(^2\)We use the high-emissions SSP5-8.5 scenario because of its higher signal-to-noise ratio, recognizing that it may not represent the most likely future.
topography and the gravity wave structure (e.g., Fig. 1A) can be resolved, which likely requires grid scales at or below $O(10 \text{ km})$. Past work has evaluated the second component in CMIP6 models (Ahmed and Neelin, 2021), concluding that few models have adequate sensitivities. Furthermore, gravity wave parameterizations in climate models are typically used to provide drag in the upper-troposphere/stratosphere, and do not interact directly with model convection schemes. Theory, convection-permitting models, and observational analyses may thus be the primary tools with which orographic precipitation can be reliably projected.

Our analyses have several limitations. The theoretical sensitivity estimate depends on the definition of the lower-tropospheric layer used to define $T'_L$ and $q'_L$. There is uncertainty in the definition of its lower edge (the boundary layer top) and its upper boundary has been chosen somewhat arbitrarily here and in past related work (Nicolas and Boos, 2022; Ahmed et al., 2020). Using a vertically resolved sensitivity kernel (Kuang, 2010) may render the theory more robust. However, such kernels depend on the cloud-resolving model and simulation design used to derive it, and none have yet been estimated from observations. Our sensitivity estimate remains robust to changes in many other parameters of the theory.

Our simulations also have limitations, as convection-permitting models exhibit differences in emergent properties such as cloud entrainment rates and precipitation efficiencies (Wing and Singh, 2024). These might affect the sensitivity of convection to temperature and moisture perturbations, and hence the scalings derived here. Another limitation is that we only considered one SST (300 K). Although it is representative of current conditions in most of the observed regions analyzed, warmer SSTs may alter the sensitivity of convection. Finally, our idealized simulations may oversimplify the large-scale conditions of observed orographic precipitation, neglecting spatial and temporal variations in background wind and SST.

Two important unknowns preclude a projection of tropical orographic precipitation in a warmer world. First, warming-induced changes in cross-slope wind are uncertain in many regions (Fig. 5). Second, away from midlatitudes (Siler and Roe, 2014), the sensitivity of orographic precipitation to warming with fixed wind remains unknown, even though it likely is the most important factor in regions where wind changes are modest. Progress constraining either of these quantities will help in anticipating changes freshwater supplies for billions of people.

**Code and data availability.** The code used in producing the figures (including linear mountain wave and precipitation models), and processed simulation, reanalysis and observational data are archived at Zenodo (Nicolas, 2024).

**Appendix A: Linear theory for tropical orographic precipitation**

Nicolas and Boos (2022) derive an equation for orographic precipitation in one horizontal dimension (their Eq. 7) which reads

$$\frac{dP}{dx} = -\frac{P - P_0}{L_q} + \beta \frac{d}{dx} \left( \frac{q_{aL}}{\tau_q} - \frac{T_{aL}}{\tau_T} \right),$$

(A1)

after dropping the nonlinear Heaviside function (which only affects the downstream precipitation rates) and adapting units and notation to those of the present work. $L_q$ is a length scale for convective relaxation of moisture, given by $L_q = 0.6 U \tau_q / \text{NGMS}$, where NGMS is the normalized gross moist stability (Raymond et al., 2009) and is about 0.2. The factor of 0.6 converts lower-
free-tropospheric moisture perturbations into full-tropospheric moisture perturbations, assuming a fixed vertical profile of moisture variations (Ahmed et al., 2020). Using \( P_a = \beta (q_{aL}/\tau_q - T_{aL}/\tau_T) \) and \( P = P_0 + P_a + P_m \) in (A1) yields (3).

The adjustment timescales \( \tau_T, \tau_q, \) and \( \tau_b \) are derived from observations at 3-hourly resolution by Ahmed et al. (2020). For seasonal-mean precipitation rates, longer effective time scales are needed due to the inclusion of non-precipitating times. Based on the amount of non-precipitating times in simulations of orographic rainfall, Nicolas and Boos (2022) take these timescales to be 2.5 times higher than their 3-hourly values, i.e. \( \tau_T = 7.5 \) hr and \( \tau_q = \tau_b = 27.5 \) hr. These values are used throughout the paper.

The adiabatic orographic vertical displacement \( \eta \) is calculated using linear mountain wave theory (e.g., Smith, 1979). For a mountain of half-width 100 km, the waves are hydrostatic to a very good approximation. In a Boussinesq atmosphere with uniform wind \( U \), Brunt-Väisälä frequency \( N \), and no rotation, vertical displacement in a hydrostatic, stationary linear mountain wave obeys

\[
\partial_z \eta + \frac{N^2}{U^2} \eta = 0, \tag{A2}
\]

with the linearized boundary condition \( \eta(z = 0) = h \) and a condition of upward energy radiation at the top boundary. The addition of uniform Rayleigh damping (with coefficient \( \xi = 1 \) day\(^{-1} \)) in the horizontal momentum equation slightly modifies this expression, which reads in the Fourier domain

\[
\partial_z \hat{\eta} + \left(1 - \frac{i \xi}{kU}\right)^{-1} \frac{N^2}{U^2} \hat{\eta} = 0, \tag{A3}
\]

where hats denotes horizontal Fourier transforms and \( k \) is the horizontal wavenumber. The solution is given by \( \hat{\eta} = \hat{h} e^{imz} \), where \( m \) is chosen as the root of \( (1 - i \xi/kU)^{-1} (N^2/U^2) \) that satisfies upward energy radiation; one can show the relevant root is that whose real part has the same sign as \( k \). The topographic profile considered throughout this paper is

\[
h(x) = \frac{h_0}{2} \left(1 + \cos\left(\frac{\pi x}{l_0}\right)\right), \quad |x| < l_0, \tag{A4}
\]

where \( h_0 \) and \( l_0 \) are the maximum height and half-width of the mountain.

### Appendix B: Regions selected, rainfall and wind products

The regions studied here are the same as in Nicolas and Boos (2024), with the exception of Papua New Guinea, which does not have a long-term observational rainfall record. These regions were selected because they feature strong orographic rain bands, and fall clearly within the mechanically forced regime. The rainy seasons considered are June-August for the Western Ghats and Myanmar, October-December for Vietnam, and November-December for Malaysia and the Philippines. The azimuth angles used to defined cross-slope winds are respectively 70°, 50°, 240°, 225°, and 225°. Maps of mean rainfall and regressions of \( P \) and \( P' \) on \( U \) are shown in Fig. S1 of the Supplement.

Gauge-based precipitation observations are available in South and Southeast Asia for 1950-2015 (APHRODITE dataset, Yatagai et al., 2012). We take winds from the ERA5 reanalysis (Hersbach et al., 2020; Bell et al., 2021). Because the number of
assimilated observations in ERA5 is much smaller before the 1960s, we consider data from 1960 onwards. Hence, regressions of total precipitation $P$ on $U$ use a 46-year record between 1960 and 2015. The same period is used for regressions of seasonal-mean reanalyzed $P'$. Observed $P'$ at daily scales is obtained from the IMERG dataset (Huffman et al., 2019) between 2001 and 2020, with daily upstream wind taken from ERA5 over that same period.

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Competing interests. The authors declare that they have no conflict of interest.

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