



# 1 Variations in the microstructure of saline ice during its growth and 2 decay: Evidences from an experimental study

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8 **Abstract.** Ice physics are highly sensitive to the ice temperature and are primarily determined by the distribution of  
9 inclusions such as gas bubbles and brine pockets within ice. However, a detailed understanding of their distributions and  
10 evolution patterns during ice freezing and melting is lacking. To address this issue, in situ experiments were conducted to  
11 collect detailed information on the variations in the microstructure of ice using continuous sampling and a high-resolution  
12 imaging system. The results revealed a 5- to 10-fold increase in the volume fraction and a 2-fold increase in the size of gas  
13 bubbles during the melting phase of ice. Moreover, the size of brine pockets in the ice surface, middle, and bottom layers  
14 clearly increased for different reasons. The nearly 30% increase in gas bubbles observed in the middle layer was thermally  
15 driven, while the increase in the surface layer was influenced by the net shortwave radiation. Additionally, the variation in  
16 the inclusion size distribution was attributed to the merging process, most of which occurred among smaller inclusions rather  
17 than among larger inclusions. The changing ice temperature is a significant factor in the merging process of the middle layer  
18 but not for the surface or bottom layers. This study could enhance the understanding of the effect of the transfer of energy  
19 between the atmosphere and water beneath ice on the ice microstructure.

## 20 1 Introduction

21 Ice is a multiphase material comprising ice crystals, gas bubbles, and impurities (Hruba and Kletetschka, 2018; Hunke et al.,  
22 2011; Petrich and Eicken, 2017). Saline ice also contains brine pockets or salt precipitates (Light et al., 2003; Notz and  
23 Worster, 2008). The proportions of these components vary with the ice formation, freezing, and melting phases (Eicken,  
24 2003; Frantz et al., 2019; Light et al., 2003; Perovich and Gow, 1996). Therefore, the properties of bulk ice, including  
25 thermal, optical, electromagnetic, and mechanical properties, exhibit significant variability in both time and space (Light et  
26 al., 2008; Pringle et al., 2009; Wang et al., 2020). As a result, ice plays a crucial role in the transfer of heat, salt, gases, and  
27 radiation between subglacial water and the atmosphere (Corkill et al., 2023; Crabeck et al., 2014; Light et al., 2004; Trodahl  
28 et al., 2001; Vancoppenolle et al., 2010), rendering it a key element of the Earth's climate system.

29 Variations in the inclusions within natural ice depend on two main factors: the meteorological environment and the  
30 hydrographic boundary conditions (Eicken, 2003). The content of newly formed brine pockets in ice can be quantified by an



31 effective segregation coefficient and the salinity of the underlying water (Cox and Weeks, 1988). Moreover, the formation of  
32 gas bubbles in ice is related to many factors (Tsurikov, 1979). During the initial freezing phase, gases are released from the  
33 solution and trapped in the initial ice cover, referred to as inactive bubbles by Light et al. (2004). Additionally, as the ice  
34 temperature changes, the volume of brine pockets and gas bubbles changes as a result of phase variations to maintain gas–  
35 brine equilibrium (Crabeck et al., 2019). For example, voids form due to the partial evaporation of ice or brine during  
36 internal melting. Notably, Light et al. (2004) defined these bubbles affected by the melting process as active bubbles.  
37 A statistical description of how the volume of inclusions changes is needed to better understand how the physical properties  
38 of ice change. Based on ice phase diagrams (Cox and Weeks, 1983; Leppäranta and Manninen, 1988), the seasonal and  
39 annual variations in bubbles and brine volumes in ice can be obtained. The results indicate a significant increase in ice  
40 porosity during the melting season (Salganik et al., 2023; Wang et al., 2020). The latest mushy layer theory was employed as  
41 the physical basis for brine exchange processes in ice and could be used to simulate the changing  $V_b$  value of ice (Bailey et  
42 al., 2020; Hunke et al., 2011; Turner and Hunke, 2015). The variations in the  $V_b$  profile were clearly impacted by ice surface  
43 radiation (Vancoppenolle et al., 2007). During the Multidisciplinary drifting Observatory for the Study of the Arctic Climate  
44 expedition (MOSAiC), Macfarlane et al. (2023) reported the seasonal variation in the specific surface area of the ice surface  
45 scattering layer.

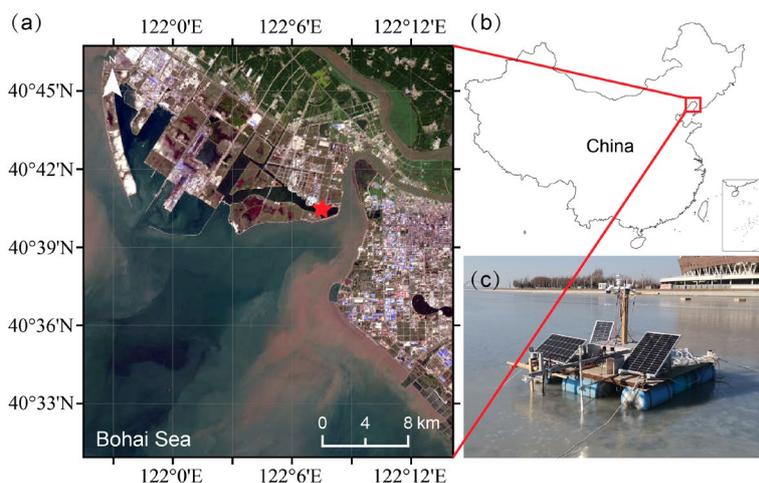
46 The morphology of ice inclusions is another significant property that should be observed. Grenfell (1983) and Perovich and  
47 Gow (1996) reported the size and distribution of gas bubbles in sea ice. Cole and Shapiro (1998) recorded detailed  
48 information on the size and shape of brine inclusions. Recent studies on the inclusion morphology have largely focused on  
49 their connection with ice physical changes, providing useful information. For example, studies have shown that the size of  
50 inclusions increases in the melting process due to the aqueous–gaseous equilibrium (Frantz et al., 2019; Light et al., 2003),  
51 while the number of inclusions decreases (Salomon et al., 2022). Additionally, the ice texture (granular or columnar) is an  
52 important factor controlling the gas size distribution (Crabeck et al., 2016; Oggier and Eicken, 2022).

53 Although previous observations have provided a general understanding of the ice microstructure, there is limited available  
54 information on the exact seasonal variation in inclusions. Some studies on changes in the inclusion size distribution mainly  
55 rely on laboratory cooling or heating processes (Crabeck et al., 2019; Light et al., 2003), which may not accurately represent  
56 the physics of natural ice changes with radiation and other meteorological factors. Due to the lack of seasonal variations in  
57 ice inclusions, it remains challenging to precisely obtain variations in ice physical properties. This inevitability introduces  
58 inaccuracies into ice models in response to varying circumstances. In this study, for the first time, high-resolution imagery  
59 was used to observe the microstructure of natural saline ice throughout the winter season together with its physical properties.  
60 The temporal variations and vertical distributions of the size and volume fractions of inclusions were investigated, while the  
61 factors driving these variations were also explored.



## 62 2 Fieldwork and methods

63 Field observations were conducted in Lake Hanzhang, which is a brackish water body that originates from the Bohai Sea  
64 (Figure 1a, b), from December 1, 2022, to February 23, 2023. The lake water salinity ranged from approximately 5–7‰. The  
65 freezing period typically lasts for 3–4 months, from early December to mid-March. A floating remote observation system  
66 (Figure 1c) was deployed prior to ice formation and recovered after complete ice melting at the site (Xie et al., 2022). Then,  
67 the ice properties, meteorological data, and water properties under the overall seasonal variations in ice could be measured.  
68 Ice cores were obtained near the floating platform approximately once a week to analyse the ice density, salinity, and  
69 microstructure when the ice thickness was large enough. A total of 7 samples were collected during the observation, and the  
70 distance between the sampling sites was no more than 20 cm to avoid the effects of spatial differences.



71  
72 **Figure 1: (a, b) Fieldwork site (shown as a red star) and (c) the floating remote observation system. The base map in (a) is imagery**  
73 **satellite from TerraColor NextGen obtained on January 11, 2023.**

74

### 75 2.1 Ice physics

76 The ice thickness was measured using an ultrasonic sensor (PA500, Tritech, Westhill, UK), with a measuring range of 0.1 to  
77 10 m, a 1-mm resolution, and a 2.5-mm accuracy. The ultrasound sensor was affixed onto the floating platform and  
78 maintained upright in water. The ice thickness was then calculated by subtracting the distance between the ice bottom and  
79 the sensor from the known distance between the ice surface and the sensor. The ice surface height was monitored using a  
80 downward ultrasonic sensor (SR50A, Campbell Scientific, Logan, UT, USA), with a measuring range of 0.5–10 m and an  
81 accuracy of 1 cm.

82 Platinum resistance sensors (PTWD, Sunshine Meteorological Technology (Jinzhou) Ltd., Jinzhou, China) were employed to  
83 measure the vertical temperature profiles of ice and water. The available temperature measurement range is from –40°C to



84 +150°C, with a precision of 0.04°C. The sensors were calibrated using an ice/distilled water mixture at 0°C prior to the  
85 experiment. A wooden frame was used to fix the probes at 3-cm intervals on ice. As wood exhibits a lower thermal  
86 conductivity than ice (Hruba and Kletetschka, 2018), the impact of the frame on our observations was neglected. The  
87 temperature of the ice surface was measured using an infrared temperature sensor (SI-411, Apogee Instruments, Logan, UT,  
88 USA), with an accuracy of 0.2°C.

89 After extracting ice samples at each sampling site, a portion of each sample was immediately cut into 5-cm sections and  
90 stored in sealed plastic containers to thaw. The bulk salinity of the meltwater was obtained using a salinometer, with an  
91 accuracy of 0.1‰. The other sample portion was used to measure the ice density according to Archimedes' law, which  
92 exhibits a lower measurement uncertainty than the most common mass/volume method (Pustogvar and Kulyakhtin, 2016).  
93 The sample mass was measured both while floating on and while submerged in cold antifreeze liquid to prevent the ice from  
94 melting during the measurement. Then, the ice density ( $\rho_{ice}$ ) can be derived as follows:

$$95 \rho_{ice} = \frac{M_2 - M_1}{M_3 - M_1} \rho_1 \quad (1)$$

96 where  $M_1$  is the total mass of the container and the contained liquid,  $M_2$  is the total mass of the container when the ice sample  
97 floats on the liquid,  $M_3$  is the total mass of the container when the ice sample is immersed in the liquid, and  $\rho_1$  is the known  
98 density of the antifreeze liquid. In the following analysis, the first 5-cm layer of ice was defined as the surface layer, and the  
99 last 5-cm layer was defined as the bottom layer. The remaining section was defined as the middle layer.

## 100 2.2 Meteorological conditions

101 The meteorological conditions were monitored on an hourly basis using a compact weather station (MaxiMet GMX 501, Gill  
102 Instruments Ltd., Lymington, UK). The available parameters included the shortwave solar radiation, air temperature, relative  
103 humidity, wind speed and direction, with corresponding accuracies of 1 W m<sup>-2</sup>, 0.3°C, 2%, 3%, and 3°, respectively.

104 The incident shortwave radiation can be obtained from weather stations. Another global radiometer (TBQ-2, Sunshine  
105 Meteorological Technology (Jinzhou) Ltd., Jinzhou, China) was arranged above the ice surface to monitor the total reflected  
106 shortwave radiation. The radiometer was placed on an extension rod away from the floating platform to prevent any possible  
107 influence of platform shadows.

108 The net longwave radiation ( $Q_{ln}$ ) is the difference between the downwelling longwave radiation ( $Q_{ld}$ ) and upwelling  
109 longwave radiation ( $Q_{lu}$ ), which can be obtained as follows:

$$110 Q_{ln} = Q_{ld} - Q_{lu} = \varepsilon_a \sigma T_a^4 - \varepsilon \sigma T_0^4 \quad (2)$$

111 where  $\sigma$  is the Stefan–Boltzmann constant ( $5.67 \times 10^{-8}$  W m<sup>-2</sup> K<sup>-1</sup>),  $T_a$  and  $T_0$  are the air temperature and ice surface  
112 temperature, respectively,  $\varepsilon$  is the ice surface emissivity (0.98), and  $\varepsilon_a$  is the effective atmospheric emissivity, which depends  
113 on the humidity and cloudiness (Efimova, 1961):

$$114 \varepsilon_a = (A + B \cdot e)(1 + C \cdot N^2) \quad (3)$$



115 where  $A$  and  $B$  are clear sky parameters ( $A = 0.746$  and  $B = 0.0066$ ),  $e$  is the water vapor pressure, which is a function of the  
116 temperature,  $C$  is the cloudiness coefficient (0.26), and  $N$  is the cloudiness, which can be estimated by the difference  
117 between the theoretical clear sky irradiance (Meyers and Dale, 1983) and the measured irradiance (Crawford and Duchon,  
118 1999). This parameterization agrees well with the observed results (Duarte et al., 2006).

## 119 2.3 Ice microstructure

### 120 2.3.1 Volume fraction of inclusions

121 In this study,  $V_a$  and  $V_b$  of ice were calculated according to phase diagrams (Cox and Weeks, 1983; Leppäranta and  
122 Manninen, 1988) using in situ ice temperature ( $T$ ), bulk ice salinity ( $S$ ), and bulk ice density ( $\rho_{ice}$ ) measurements of the ice  
123 samples:

$$124 \quad V_a = 1 - \frac{\rho_{ice}}{\rho_i} + \rho S \frac{F_2}{F_1} \quad (4)$$

$$125 \quad V_b = \frac{\rho_{ice} S}{F_1} \quad (5)$$

126 where  $\rho_i$  is the density of pure ice (Cox and Weeks, 1983):

$$127 \quad \rho_i = 0.917 - 1.403 \times 10^{-4} \times T \quad (6)$$

128  $F_1$  and  $F_2$  are also functions of the ice temperature. Here,  $T$  was obtained from the vertical temperature profile (Section 2.1).  
129 The temperature profile of the original ice was interpolated from 3- to 1-cm intervals. This allowed for calculating the mean  
130 ice temperature for each 5-cm layer.

### 131 2.3.2 Size of inclusions

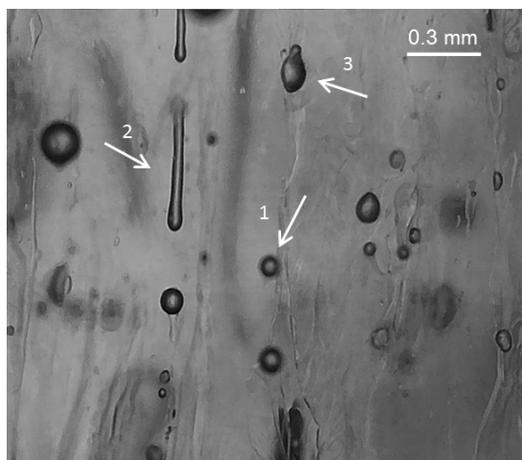
132 The ice samples were processed into vertical thin sections with a thickness of  $\sim 5$  mm to observe their microstructure. This  
133 thickness was chosen to ensure that the individual inclusions were entirely visible and not obscured by others. Subsequently,  
134 the thin ice sections were imaged in a cold laboratory ( $-10^\circ\text{C}$ ) for inclusion observation. To enhance the visibility of gas  
135 bubbles and brine pockets and to facilitate image processing, the thin sections were imaged under diffuse light. Each typical  
136 image covers an area of approximately  $2 \times 3$  mm. Notably, the true length of a pixel is approximately 0.002 mm, while  
137 higher-resolution images were obtained at a resolution of 0.001 mm per pixel. Approximately 30–70 images were recorded  
138 for each thin section within  $\sim 5$  min. In total, more than 1800 images were recorded covering all ice samples. The potential  
139 effect of the low temperature in the cold laboratory on the ice microstructure during imaging is described in Section 4.1.

140 After obtaining thin section photographs, they were analyzed using ImageJ software (rsb.info.nih.gov/ij/). The first step  
141 involved image filtering by applying a Gaussian blur filter (standard deviation 100) to obtain a background image. The  
142 background image was then subtracted from the original image to eliminate the effect of unfocused inclusions. Next, image  
143 segmentation was performed by exploiting the grey level differences between ice and inclusions. Many automated



144 segmentation algorithms have been adopted in related studies. The Otsu algorithm (Otsu, 1979) was used by Maus et al.  
145 (2021). Crabeck et al. (2021) employed the Ridler method (Ridler and Calvard, 1978) to separate background and inclusion  
146 pixels. Several segmentation methods were assessed on our ice image sets to ensure a stable algorithm response. Then, the  
147 results of each segmentation method were visually evaluated by comparing the raw and segmented images. The  
148 segmentation threshold produced by the Ridler method facilitated the accurate identification of inclusions in all images while  
149 introducing minimal noise in the segmented image. Moreover, the batch-segmented images were manually verified. Several  
150 images were randomly selected, and the background and inclusions were manually separated. The obtained batch-segmented  
151 inclusions were slightly larger than the manually segmented inclusions, with a mean difference of 5 pixels, equivalent to  
152 approximately 0.008 mm.

153 Following image partitioning, the inclusions were categorized as either gas bubbles or brine pockets. The observation of  
154 Perovich and Gow (1996) regard all inclusions in first-year ice are brine pockets, whereas all inclusions in multiyear ice are  
155 gas bubbles. Light et al. (2003) empirically classified inclusions based on their shape. Notably, brine pockets are trapped  
156 between ice platelets, and they move and become elongated as ice grows and melts (Petrich and Eicken, 2017). The shape of  
157 most brine pockets is heterogeneous, but most gas bubbles are nearly spherical (Crabeck et al., 2019; Light et al., 2003).  
158 Therefore, gas bubbles and brine pockets were classified based on the circularity ( $4\pi \times \frac{\text{area}}{\text{perimeter}^2}$ ) of the inclusions (Figure  
159 2). Several circularity thresholds were tested for our ice image sets, and inclusions with a circularity greater than 0.75 were  
160 regarded as gas bubbles. The Spearman correlation coefficient between  $V_a$  derived from the images and that calculated from  
161 the phase diagrams was 0.78 ( $p < 0.001$ ), which indicates that the tendencies of  $V_a$  obtained from the two methods were  
162 significantly related. Note that the transparent portions of thin sections devoid of inclusions were discarded during imaging.  
163 Therefore, the  $V_a$  values derived from the images were greater than the real values. Therefore,  $V_a$  calculated from the images  
164 was not employed in this study.



165

166 **Figure 2: Image of a vertical thin section of ice. The arrows indicate examples of (1) gas bubbles and (2, 3) brine pockets.**

167



168 Following Grenfell (1983) and Light et al. (2003), the size distribution function of the inclusions was defined as the number  
169 of inclusions per  $\text{mm}^3$  per unit length. Unless otherwise specified, the bubble size in this study refers to the diameter, while  
170 the brine pocket size refers to the length, i.e., the maximum caliper length. The raw inclusion size data were binned by size,  
171 with bin widths of 0.01 mm for gas bubbles and 0.05 mm for brine pockets. The mean number of gas bubble bins was 70,  
172 while the mean value of brine pocket bins was 50. These data were sufficient for analysing the inclusion size distribution,  
173 and outliers could be avoided.

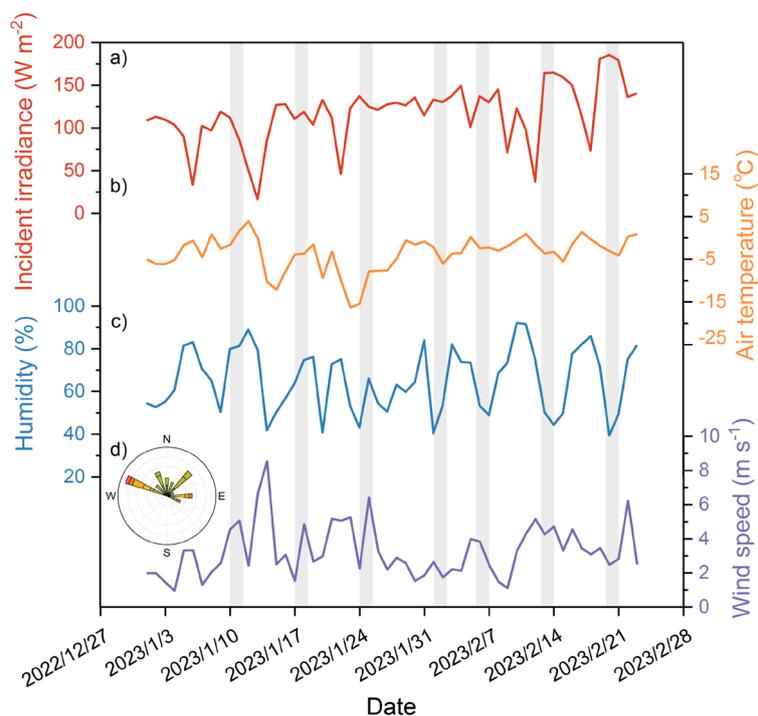
## 174 **3 Results**

### 175 **3.1 General conditions during the ice season**

#### 176 **3.1.1 Weather conditions**

177 Figure 3 shows the weather conditions during the observation period, with the grey columns indicating the sampling dates.  
178 Here, the period from January 1 to February 23 was emphasized because the unshown and sampling dates greatly differed.  
179 The weather conditions throughout the whole ice season are shown in Figure S1. Throughout the observation period, there  
180 were no snowfall or rainfall events. Additionally, there was an increasing trend in the incident shortwave irradiance (Pearson  
181 correlation coefficient  $r = 0.65$ ,  $p < 0.001$ ). During the later phase of the observation period, the downwelling shortwave  
182 irradiance reached  $180 \text{ W m}^{-2}$ . The ambient air temperature varied between 0 and  $-16^\circ\text{C}$ , with an average temperature of -  
183  $3.7^\circ\text{C}$ . Figure 3b shows the minimum air temperature on January 23. Subsequently, the air temperature gradually increased  
184 until the end of the observation period ( $r = 0.53$ ,  $p < 0.005$ ). The humidity during the observed period was  $65.3 \pm 14.8\%$ ,  
185 without a clear trend. Additionally, no clear wind speed or direction trends were observed. On most observation dates, the  
186 speed was lower than 3 m/s, and the corresponding wind direction remained relatively steady.

187



188

189 **Figure 3: a) Incident irradiance, b) air temperature, c) humidity, d) wind speed and direction during the observation period from**  
 190 **January 1 to February 23. The grey columns denote the ice sampling dates.**

191

### 192 3.1.2 Ice thickness

193 The first time when the ultrasonic sensor detected ice formation was December 8, 2022 (Figure S1). Over the following 20  
 194 days, the ice thickness rapidly increased at a rate of  $1.2 \text{ cm day}^{-1}$  ( $r = 0.99$ ,  $p < 0.001$ ). By December 28, the ice thickness  
 195 had reached 22.8 cm. Then, the growth rate decreased to  $0.17 \text{ cm day}^{-1}$  ( $r = 0.85$ ,  $p < 0.001$ ) from December 28, 2022, to  
 196 January 31, 2023 (Figure 4). In February 2023, the ice thickness began to decrease. During the first two weeks, the melting  
 197 rate reached  $0.25 \text{ cm day}^{-1}$  ( $r = -0.92$ ,  $p < 0.001$ ). Then, the rate increased to  $3.3 \text{ cm day}^{-1}$  ( $r = -0.94$ ,  $p < 0.001$ ) over the  
 198 following days.

199 The variation in the ice surface elevation obtained from the downward ultrasonic sensor was not significant ( $-0.08 \pm 0.5 \text{ cm}$ ,  
 200 not shown in the figure), indicating that the ice surface did not move appreciably during the observation period. This could  
 201 be attributed to the absence of snowfall or rainfall during the experiment, as well as unclear melting of the ice surface. As  
 202 shown in Figure 4, the thickness of the ice samples agreed well with the ultrasonic sensor data ( $r = 0.96$ ,  $p < 0.001$ ). The  
 203 mean difference was 1.1 cm, indicating that the ice surrounding the floating platform remained relatively level with no  
 204 notable spatial variations. Therefore, the data obtained from the floating platform could be used in ice sample analysis.

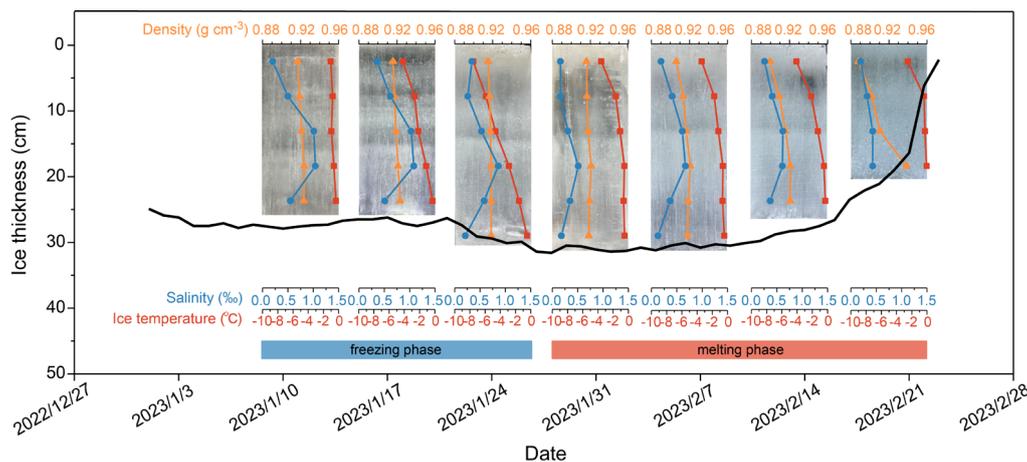
205



206 **3.1.3 Ice physics**

207 The ice temperature of the ice samples varied between  $-7.5$  and  $-0.06^{\circ}\text{C}$ . The bulk temperature of the ice sampled on January  
 208 11 was  $-0.8^{\circ}\text{C}$ , and it decreased to  $-3.8^{\circ}\text{C}$  on January 25. The bulk temperature of the following three ice samples reached  $-$   
 209  $1.4^{\circ}\text{C}$ , with no clear changes. The ice sample collected on February 20 notably melted, with a bulk temperature of  $-0.8^{\circ}\text{C}$ .  
 210 All ice temperature profiles decreased from the surface to the bottom. The surface layer temperature showed similar  
 211 temporal variations to those in the bulk temperature ( $r = 0.96, p < 0.001$ ) and was significantly correlated with the air  
 212 temperature ( $r = 0.95, p < 0.001$ ). Moreover, the temperature of the bottom layer remained relatively stable ( $-0.4^{\circ}\text{C}$ ), except  
 213 for the sample obtained on February 20 ( $-0.06^{\circ}\text{C}$ ). According to the variations in the ice temperature and thickness, the first  
 214 three samples were considered to occur during the freezing phase, while the latter four samples were considered to occur  
 215 during the melting phase (Figure 4).

216 The bulk salinity of the ice sample differed between the freezing and melting phases. The values were  $0.61\text{‰}$  and  $0.37\text{‰}$ ,  
 217 respectively. All seven samples exhibited a nearly fresh surface layer. Most samples exhibited a maximum salinity in the  
 218 middle layer, but the maximum salinity occurred in the bottom layer of the sample collected on February 20. Furthermore,  
 219 the maximum salinity of each ice sample decreased ( $r = -0.89, p < 0.01$ ). The bulk ice density ranged from  $0.90$  to  $0.92 \text{ g cm}^{-3}$ .  
 220  $^3$ . The value remained nearly constant ( $0.91 \text{ g cm}^{-3}$ ) during the freezing phase and clearly decreased during the melting phase.  
 221 On February 20, a significant melting event caused a high density ( $0.94 \text{ g cm}^{-3}$ ) in the bottom layer of ice, which was visibly  
 222 saturated with water during sampling.



223  
 224 **Figure 4: Observed variations in the ice thickness and sampled ice images overlain by the ice temperature, salinity, and density.**  
 225 **Seven ice samples were sorted into the freezing and melting phases according to their temperature and thickness changes. The**  
 226 **dates on the horizontal axis are formatted as year/month/day.**

227



## 228 3.2 Ice microstructure

### 229 3.2.1 Variations in the volume fraction of inclusions

230 The volume fraction of gas bubbles ( $V_a$ ) ranged from 0.1% to 3.3%. The brine pocket volume fraction ( $V_b$ ) ranged from  
231 0.3%–39.9%. Figure 5a shows that  $V_a$  during the freezing phase remained relatively stable. The mean  $V_a$  values for the  
232 surface, middle and bottom layers during the freezing phase were 0.3%, 0.1% and 0.05%, respectively. Subsequently,  $V_a$   
233 clearly increased during the following melting phase. On February 20, there was a more than tenfold increase in  $V_a$  for the  
234 surface and middle layers compared to those of the ice sample collected on February 1. Additionally, the bottom layer  
235 experienced a fivefold increase.

236 In contrast, the observed  $V_b$  trends differed. Notably,  $V_b$  decreased in all three layers during the freezing phase and increased  
237 during the melting phase (Figure 5a). Among the three layers, the surface layer experienced the smallest decrease in  $V_b$   
238 during the freezing phase. For the middle layer, the  $V_b$  value on January 25 was  $\sim 1/5$  of that on January 11. A similar trend  
239 was also observed for the bottom layer. During the melting phase, the bottom layer showed the clearest increase in  $V_b$ ,  
240 increasing from 1.8% on February 1 to 39.9% on February 20. The corresponding increase in the middle layer ranged from  
241 2.3% to 5.9%. In summary,  $V_b$  of the middle and bottom layers was more sensitive to the freezing/melting phase than was  
242 that of the surface layer.

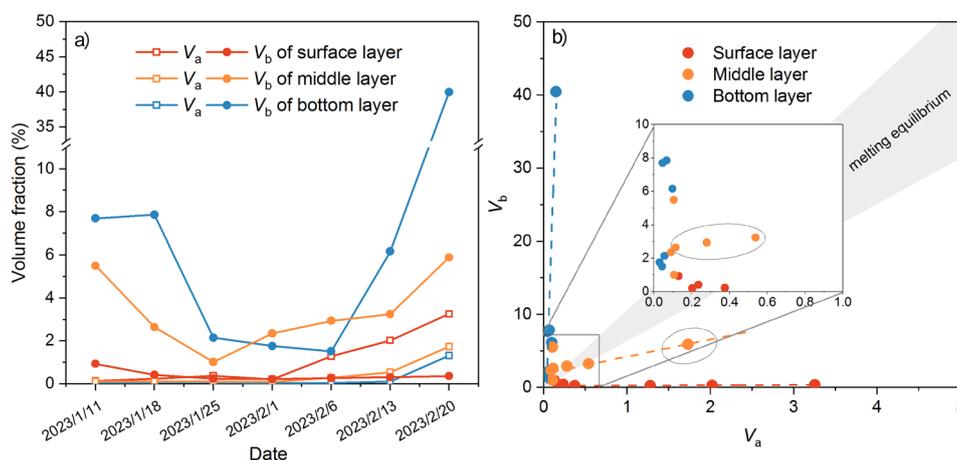
243 As ice melts, in a closed system, some of the pure ice surrounding each brine inclusion melts and becomes brine. Due to the  
244 greater density of brine than that of pure ice, gas bubbles expand to fill the volume difference. Therefore, changes in  $V_a$  are  
245 likely related to changes in  $V_b$  (Light et al., 2004). This relationship can be expressed as the melting equilibrium relationship  
246 (Cox and Weeks, 1983):  $\Delta V_a = \Delta V_b (\rho_s / \rho_i - 1)$ , where  $\rho_i$  is the density of pure ice (Equation 6), and  $\rho_s$  is the density of brine,  
247 which can be obtained according to the method of Maykut and Light (1995). According to the ice temperature during the  
248 observation period, the corresponding melting equilibrium is shown as a grey shaded area in Figure 5b.

249 The relationships between  $V_a$  and  $V_b$  for the different ice layers varied (Figure 5b). For the ice surface layer,  $V_a$  clearly  
250 increased with a low variation in  $V_b$ , resulting in a slope of the fitting line that was much lower than that of the melting  
251 equilibrium curve. This reveals that these newly formed gas bubbles did not result from the thermodynamic melting of pure  
252 ice. In contrast, for the bottom layer, there was high variation in  $V_b$ , but  $V_a$  remained relatively constant. The fitting line is  
253 distant from the melting equilibrium curve. From February 13 to 20, the increase in  $V_b$  was expected to result in a 3.1%  
254 increase in  $V_a$ . However, this phenomenon was not observed.

255 The general trend in  $V_b/V_a$  of the middle layer was more closely related to the melting equilibrium than that of the surface  
256 and bottom layers. During the melting phase of the middle layer (marked as ellipses in Figure 5b), the slope of  $V_b/V_a$  was  
257 2.12 ( $r = 0.93$ ,  $p < 0.01$ ), which is lower than the thermodynamic equilibrium value. This indicates that  $\sim 30\%$  of the increase  
258 in  $V_a$  could be explained by the change in  $V_b$ . The results for the middle layer during the freezing phase differed from those  
259 during the melting phase but were more similar to those for the bottom layer. The decrease in  $V_b$  from 5.5% on January 11 to  
260 1.0% on January 25 did not result in clear  $V_a$  changes.



261



262

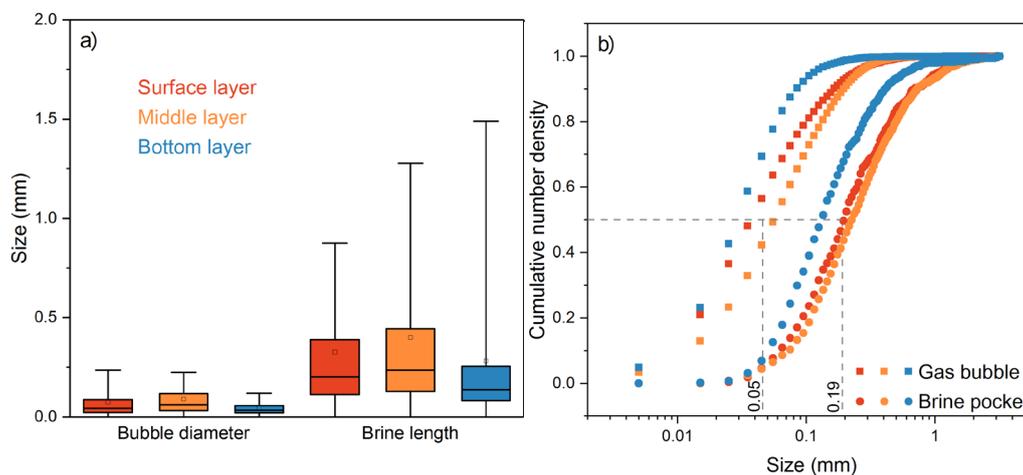
263 **Figure 5: a) Temporal variations in the volume fractions of gas bubbles and brine pockets. b) Relationship between the brine and**  
 264 **gas bubble volume fractions. The grey shaded area denotes the melting equilibrium relationships of Cox and Weeks (1983). The**  
 265 **ellipses denote the results for the middle layer during the melting phase.**

266

### 267 3.2.2 Variations in the size of inclusions

268 Figure 6a shows the interquartile range (IQR) box plot of the inclusion size for the different ice layers. The brine pockets  
 269 were larger than the gas bubbles, while the brine pocket size range was also greater. The mean size of the gas bubbles in the  
 270 surface layer was 0.07 mm, while in the middle and bottom layers, the corresponding values were 0.09 and 0.05 mm,  
 271 respectively. Moreover, the mean sizes of the brine pockets in the surface, middle, and bottom layers were 0.33, 0.40, and  
 272 0.28 mm, respectively. The medians of the inclusion sizes were smaller than the corresponding means, except the brine  
 273 pocket size in the bottom layer, where the median reached 0.5 times the mean. For the other layers, the median was ~0.6  
 274 times the corresponding mean. This indicates that most inclusion sizes were relatively small.

275 Figure 6b shows the cumulative number density of inclusions of different sizes in the different ice layers. The median sizes  
 276 of the gas bubbles and brine pockets are shown as grey lines. Hereinafter, the inclusions with sizes smaller (larger)  
 277 than their median were defined as small (large) inclusions. The size of the gas bubbles ranged from 0.002–3.17 mm, with half of the  
 278 bubbles smaller than 0.05 mm. For the surface layer, 19% of the bubbles were larger than 0.1 mm. The corresponding  
 279 proportions for the middle and bottom layers were 27% and 6%, respectively. This explains why the mean bubble size of the  
 280 middle layer was larger than that of the surface and bottom layers (Figure 6a). A similar phenomenon was also observed for  
 281 the brine pockets. The proportion of large brine pockets in the middle layer was greater than that in the surface and bottom  
 282 layers.



283

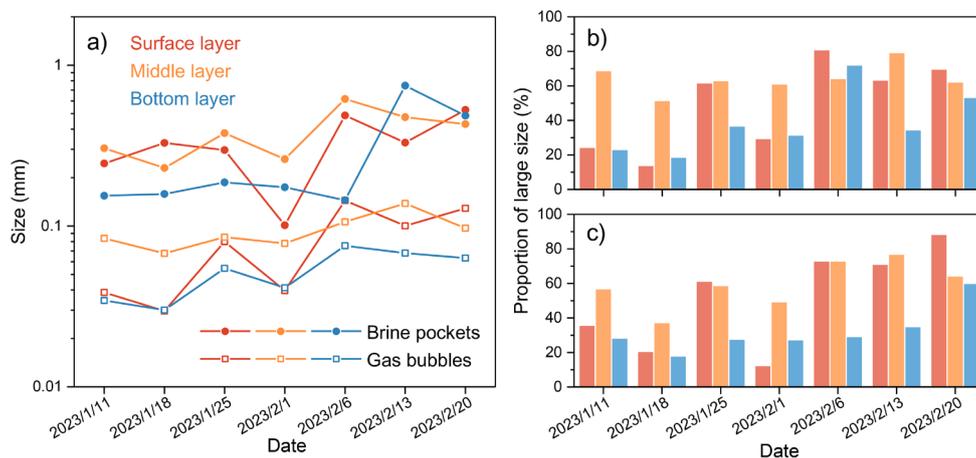
284 **Figure 6: a) IQR box plot showing the distribution of the bubble diameter and brine pocket length. The box is defined by the first**  
 285 **and third quartiles of the distribution. The line in the box is the median, and the square denotes the mean. b) Cumulative number**  
 286 **density of the inclusions in the different ice layers. The grey lines denote the median of each inclusion size class.**

287

288 Figure 7 shows the temporal variations in the inclusion sizes for the different ice layers and the proportion of large inclusions  
 289 on each sampling date. There was a general increasing trend in the gas bubble size. Among the three ice layers, the increase  
 290 rate of the surface layer was the highest, at approximately 0.017 mm per week ( $r = 0.79, p < 0.05$ ). The corresponding values  
 291 were 0.007 mm per week for the middle layer ( $r = 0.67, p < 0.1$ ) and bottom layer ( $r = 0.81, p < 0.05$ ). Notably, the increase  
 292 rate of the surface layer was ~2.4 times that of the middle and bottom layers. Moreover, the mean size of the gas bubbles in  
 293 the middle layer did not significantly change during the freezing phase, while the sizes of the gas bubbles in the surface and  
 294 bottom layers notably increased.

295 The proportions of large bubbles in the three layers varied to different degrees (Figure 7b). The proportion in the surface  
 296 layer generally increase during the observation period, at a rate of 9.1% per week ( $r = 0.76, p < 0.05$ ). Similarly, the bottom  
 297 layer exhibited an increasing trend, with a rate of 5.6% per week ( $r = 0.66, p < 0.1$ ). In contrast, the trends observed for the  
 298 middle layer differed. There was a consistent proportion of large gas bubbles, at  $63.7 \pm 7.7\%$ , with no significant trend.  
 299 However, the mean size significantly increased. This may result from the merging of bubbles. This process exerted a greater  
 300 impact on the mean bubble size than on the number of bubbles.

301



302

303 **Figure 7: a) Temporal variations in the sizes of gas bubbles and brine pockets in the different ice layers. b) Variation in the**  
 304 **proportion of large inclusions on each sampling date. A large inclusion was defined as an inclusion with a size larger than the**  
 305 **median value.**

306

307 Generally, there were increasing trends in the size of brine pockets in the three ice layers (Figure 7a). Furthermore, the  
 308 increasing speeds were greater than those in the gas bubble size. From January 11 to February 20, the brine pocket size in the  
 309 surface and middle layers increased nearly twofold, while that in the bottom layer increased nearly fourfold. Notably, this  
 310 finding differed from the gas bubble observations. The differences in the brine pocket size between the surface and bottom  
 311 layers were greater during the melting phase than during the freezing phase. In particular, the brine pocket size in the bottom  
 312 layer remained almost constant during the freezing phase but rapidly increased during the melting phase.

313 The proportions of large brine pockets in the three layers typically increased during the observation period (Figure 6c). On  
 314 January 11, the proportion of large brine pockets did not exceed 40%, and it increased to ~70% on February 20. Among the  
 315 three layers, the increase rate of the surface layer was the greatest, at approximately 9.7% per week ( $r = 0.72, p < 0.1$ ). The  
 316 increase rates of the middle and bottom layers were 4.1% per week ( $r = 0.66, p = 0.1$ ) and 4.7% per week ( $r = 0.76, p < 0.05$ ),  
 317 respectively. Although the proportions of large brine pockets in the bottom layer on February 13 and during the period from  
 318 January 11 to February 6 were similar, the mean sizes differed. This was due to the maximum size of the brine pockets on  
 319 February 13 greatly exceeding (~4 mm) that on the previous day (<1 mm) as a result of merging.

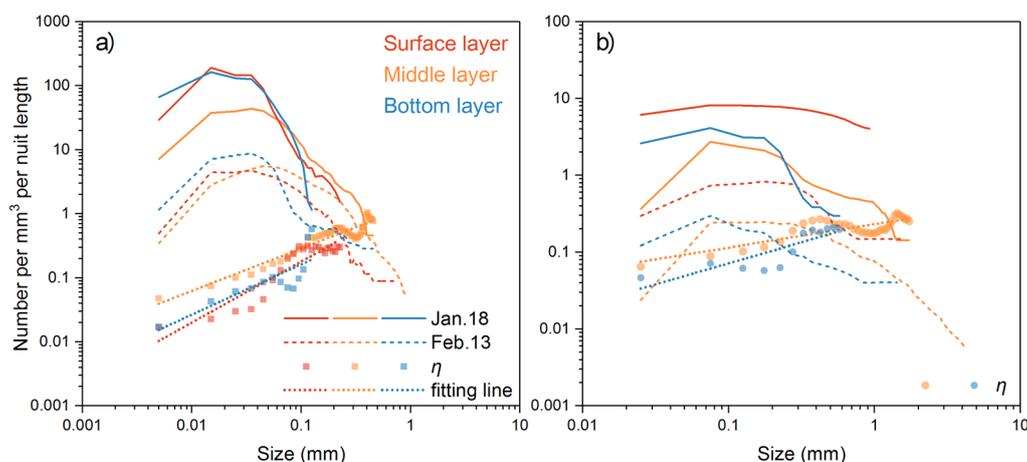
### 320 3.2.3 Merging of inclusions

321 Inclusions often merged with neighboring inclusions as they expanded, resulting in a decrease in the number density of  
 322 inclusions of each size. Following Light et al. (2004), the merging factor ( $\eta =$  number density distribution after  
 323 merging/original distribution) was used to quantify this process. Figure 8 shows the size distribution of gas bubbles and brine  
 324 pockets on January 18 and February 13 as a function of the inclusion size and the corresponding  $\eta$  value. Note that the  
 325 distributions were normalized according to their volume fraction. This indicates that the volume fractions of the inclusions



326 shown as solid lines in Figure 8 are identical, and the variation in  $\eta$  resulting from inclusion volume change was removed.  
 327 These two dates were chosen because the difference in the proportion of large inclusions was significant (Figure 7b, c). The  
 328  $\eta$  values corresponding to other dates can be found in the following section.  
 329 Notably, the size distribution of gas bubbles on February 13 differed from that on January 18 (Figure 8a). On the one hand,  
 330 the number of gas bubbles of each size decreased to different degrees. On the other hand, the maximum size of the gas  
 331 bubbles clearly increased. There was also a common phenomenon between the bubble size distributions on the two dates.  
 332 Although the number of gas bubbles of each size decreased, the size with the peak number density did not notably change.  
 333 The corresponding size for the different ice layers was  $\sim 0.02$  mm. The abovementioned differences and similarities reveal  
 334 that the variations in the gas bubble size distribution from January 18 to February 13 did not result from the increase in  
 335 bubbles of a single size class but rather from the merging of inclusions. Otherwise, the density number function would shift  
 336 toward larger sizes and not notably decrease, as shown in Figure 8.  
 337 The  $\eta$  values of the gas bubbles in the three ice layers increased linearly ( $r > 0.9$ ,  $p < 0.001$ ) in the  $\log(\text{size})$ – $\log(\text{number})$   
 338 space (Figure 8a). For gas bubbles with a size smaller than 0.01 mm, the number density decreased by more than 95% from  
 339 January 18 to February 13. The decrease rate of gas bubbles larger than 0.2 mm reached  $\sim 40\%$ . Notably, most merging  
 340 occurred among the smaller bubbles. Among the three ice layers, the  $\eta$  value of the middle layer was the largest, while that  
 341 of the surface layer was the smallest. This reveals that the merging rate of the gas bubbles in the middle layer was lower than  
 342 that in the surface layer. This finding partially explains why the mean bubble size increased at a lower rate in the middle  
 343 layer than in the surface layer (Figure 7a).

344



345 **Figure 8: Size distribution of the a) gas bubbles and b) brine inclusions on January 18 and February 13 as a function of the**  
 346 **inclusion size. The merging factors ( $\eta$ ) of the gas bubbles and brine pockets between two dates are shown as squares and dots,**  
 347 **respectively, and both are fitted by dotted lines.**  
 348

349

350 Figure 8b shows the size distribution of brine pockets in the three ice layers on January 18 and February 13, along with the  
 351 corresponding  $\eta$  value. Note that the  $\eta$  value of the surface layer is not shown here due to the insufficient number of brine



352 pockets observed in the ice surface layer, which resulted in a statistically nonsignificant fitting line of  $\eta$ . In general, the size  
353 distribution of the brine pockets varied similarly that of the gas bubbles, as did the  $\eta$  values of the brine pockets between the  
354 two dates. The  $\eta$  value for each brine pocket size was more similar than that for the gas bubbles. This suggests that brine  
355 pockets in ice are more diverse than gas bubbles, as the probability of merging brine pockets of the same size was greater  
356 than that of merging gas bubbles. This explains the greater increase in the brine pocket size than that in the gas bubble size  
357 (Figure 7a).

### 358 3.3 Drivers of the change in the microstructure of ice

359 The surface layer exhibited clearer variation in  $V_a$  than did the middle and bottom layers (Figure 5a). To analyze the  
360 mechanism underlying this variation, the potential influencing factors are shown in Figure 9a. The net shortwave radiation  
361 and surface ice temperature were observed (Sections 2.1 and 2.2), and the net longwave radiation was simulated (Section  
362 2.2). The reason that the influencing factor of  $V_b$  was not analysed is that this parameter is directly controlled by the ice  
363 temperature and salinity. Therefore,  $V_b$  can be estimated using an ice thermodynamic model (Vancoppenolle et al., 2010).  
364 However, estimating the variation in  $V_a$  remains challenging due to a lack of information on its influencing factors.

365 There was no clear correlation between the net longwave radiation and  $V_a$  of the surface layer (Figure 9a), which was also  
366 observed for the surface temperature. However, a significant positive correlation was observed between the net shortwave  
367 radiation and  $V_a$  of the surface layer ( $r = 0.81$ ,  $p < 0.05$ ). With increasing net shortwave radiation,  $V_a$  of the surface layer  
368 gradually increased, with no clear surface temperature or surface elevation changes. This reveals that the increasing  
369 shortwave radiation absorbed by the ice surface was entirely used for phase changes. This process partially explains the  
370 formation of a porous sea ice surface layer (Macfarlane et al., 2023; Smith et al., 2022).

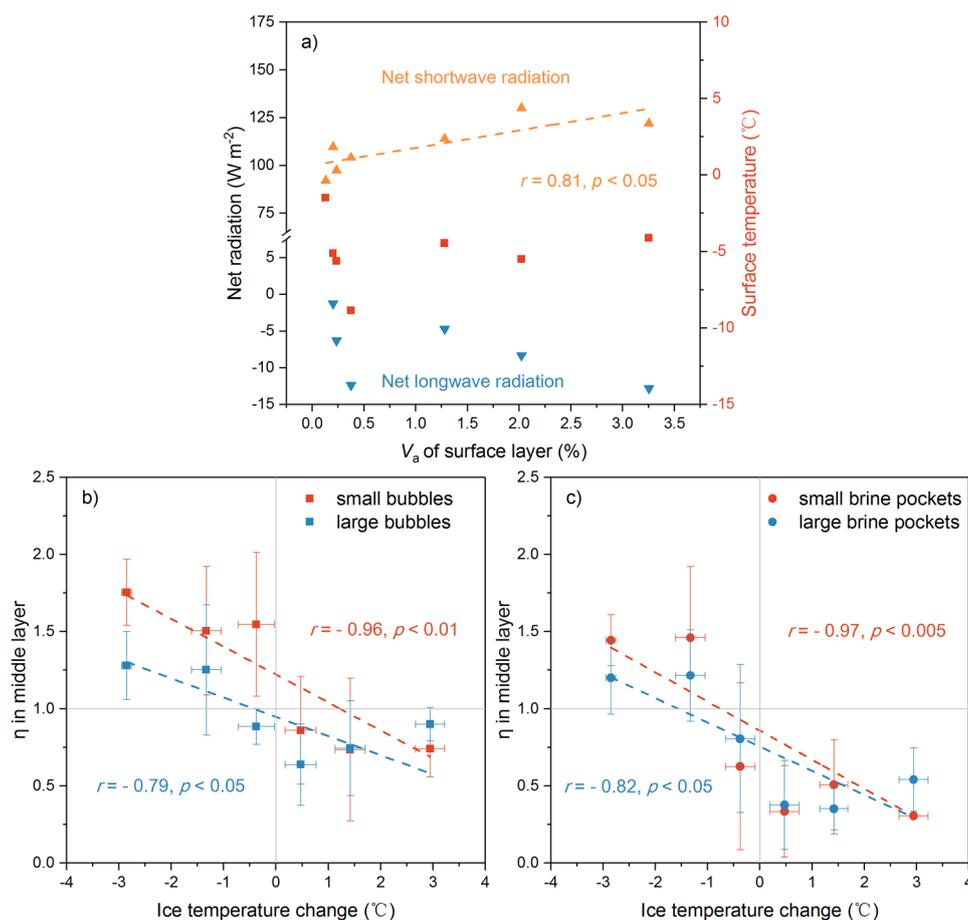
371 Figure 9b shows the variations in  $\eta$  of the gas bubbles in the middle layer with ice temperature change. Adopting an ice  
372 sample as the original condition, the ice temperature change between the other samples and the original sample could be  
373 obtained, as well as the corresponding  $\eta$  value. All the data were binned by ice temperature change. Significant relationships  
374 were found between the ice temperature changes and  $\eta$  of the middle layer for both small bubbles ( $r = -0.96$ ,  $p < 0.01$ ) and  
375 large bubbles ( $r = -0.79$ ,  $p < 0.05$ ). Notably,  $\eta$  decreased with increasing ice temperature. When the ice temperature was  
376 greater than  $0^\circ\text{C}$ ,  $\eta$  was less than 1, indicating that the number density of gas bubbles decreased due to merging as the ice  
377 warmed. During the cooling phase, the number density of gas bubbles generally increased. This may have resulted from the  
378 newly formed bubbles separating from the solution.

379 Different phenomena were observed for the brine pockets (Figure 9c). The  $\eta$  values of the small and large brine pockets in  
380 the middle layer were significantly related to ice temperature changes ( $r = -0.97$ ,  $p < 0.01$  and  $r = -0.82$ ,  $p < 0.05$ ,  
381 respectively). Notably,  $\eta$  of the brine pockets was smaller than that of the gas bubbles for the same ice temperature changes.  
382 This reveals that the decreasing rate of the number density of brine pockets was greater than that of the gas bubbles during  
383 the warming phase. Moreover, the increasing rate of the number density during the cooling phase was lower. The former is



384 expected because brine pockets in ice are more varied than are gas bubbles (Figure 8). The latter may occur because the  
 385 formation rate of new gas bubbles was greater than the dividing speed of brine pockets during the cooling phase.  
 386 No significant relationships were found between  $\eta$  of the inclusions in the surface or bottom layers and ice temperature  
 387 changes (not shown here). The range of ice temperature changes in the bottom ice layer was smaller (-1 to 1°C) than that in  
 388 the middle layer (-3 to 3°C), while the range in the surface layer was larger (-5 to 5°C). Therefore, the limitations of the  
 389 observed temperature could be eliminated. This reveals that the changes or merging of inclusions in the surface and bottom  
 390 layers mainly resulted from nonthermodynamic processes, such as those related to energy exchange with the atmosphere or  
 391 ocean.  
 392

393



394

395 **Figure 9: a) Relationships between  $V_a$  of the surface layer and the surface ice temperature, net longwave radiation, and net**  
 396 **shortwave radiation. The variations in  $\eta$  of b) gas bubbles and c) brine pockets in the middle layer with ice temperature change.**

397



## 398 4 Discussion

### 399 4.1 Uncertainties

#### 400 4.1.1 Estimations of $V_a$ and $V_b$

401 The uncertainties in  $V_a$  and  $V_b$  resulted from uncertainties in measuring  $T$ ,  $S$ , and  $\rho_{ice}$  (Cox and Weeks, 1983; Leppäranta and  
402 Manninen, 1988). The uncertainties in  $T$  and  $S$  are known (Section 2.1). Therefore, to quantify the uncertainties in  $V_a$  and  $V_b$ ,  
403 the uncertainty in  $\rho_{ice}$  was first evaluated. The focus here is on inherent uncertainties: the limiting measurement uncertainty  
404 and the errors related to brine loss.

405 The limiting measurement uncertainty in  $\rho_{ice}$  is defined as the sum of the maximum positive errors of all measurements. In  
406 this method (Equation 1), the limiting measurement uncertainty can be expressed as:

$$407 \Delta\rho_{ice} = \left| \frac{\partial\rho_{ice}}{\partial M_1} \right| \Delta M_1 + \left| \frac{\partial\rho_{ice}}{\partial M_2} \right| \Delta M_2 + \left| \frac{\partial\rho_{ice}}{\partial M_3} \right| \Delta M_3 \quad (7)$$

$$408 \frac{\Delta\rho_{ice}}{\rho_{ice}} = \left| \frac{(M_2 - M_3)}{(M_2 - M_1)(M_3 - M_1)} \right| \Delta M_1 + \left| \frac{1}{M_2 - M_1} \right| \Delta M_2 + \left| \frac{-1}{M_3 - M_1} \right| \Delta M_3 \quad (8)$$

409 where  $\Delta M_1$ ,  $\Delta M_2$ , and  $\Delta M_3$  of the present balance are 0.01 g. After inputting the means  $M_1$ ,  $M_2$ , and  $M_3$ , the measurement  
410 uncertainty in the ice density can be obtained as 0.71%.

411 Brine loss during sampling is another significant factor contributing to uncertainty in ice density measurements. When an ice  
412 sample is removed from water, the brine in open channels is replaced by gas, which inevitably causes an increase in the gas  
413 content. This effect is particularly pronounced in the lower part of an ice core with high permeability. To accurately measure  
414 the ice density, it is important to account for brine channels that were drained during sampling. These channels are filled  
415 with liquid during submersion, and their volume should therefore be excluded from the measurements.

416 The mean  $V_b$  during the observation period was 3.8%. According to the relationship between the volume fraction of open  
417 brine and total brine from Maus et al. (2021), the open brine porosity of the present ice is 1.72%. Moreover,  $\rho_{ice}$  can be  
418 expressed as  $(1 - V_a - V_b) \rho_i + V_b \rho_b$ , where  $\rho_i$  is the density of pure ice (Cox and Weeks, 1983) and  $\rho_b$  is the density of brine  
419 (Equation 6). After inputting the mean  $V_a$  and ice temperature,  $\rho_{ice}$  without drainage was  $0.917 \text{ g cm}^{-3}$ . The  $\rho_{ice}$  value with  
420 drainage was  $0.915 \text{ g cm}^{-3}$ . Notably, the uncertainty due to drainage reached 0.203%. According to the propagation law of  
421 errors, the total uncertainty in  $\rho_{ice}$  was 0.74% (approximately  $6.8 \times 10^{-3} \text{ g cm}^{-3}$ ). This value agrees well with the reported  
422 uncertainty range for the hydrostatic weighing method (Pustogvar and Kulyakhtin, 2016).

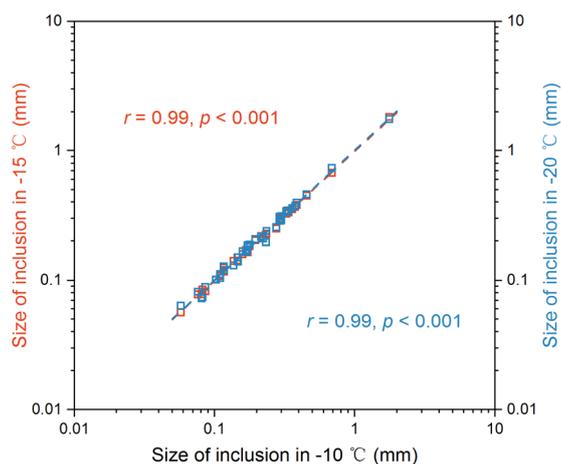
423 As introduced in Section 2, the precision of the platinum resistance sensors employed in this observation study is  $0.04^\circ\text{C}$ .  
424 The uncertainty in the salinometer is 0.1%. According to the phase diagrams (Cox and Weeks, 1983; Leppäranta and  
425 Manninen, 1988), the maximum absolute uncertainties in  $V_a$  and  $V_b$  reached 0.77% and 0.23%, respectively.



426 **4.1.2 Effects of a changing temperature during imaging**

427 The thin ice sections were imaged in a cold laboratory (-10°C) to observe their inclusions. This temperature is lower than the  
 428 ice temperature (Figure 4). Experiments were designed by Light et al. (2003) to determine the thermal evolution of the ice  
 429 microstructure over a wide range of temperatures. Their results showed that each inclusion decreased in size during the ice-  
 430 cooling phase. In the experiment conducted by Light et al. (2003), the ice samples were maintained at each temperature for a  
 431 minimum of 24 hours before photographs were obtained. In this study, ice sections were imaged after ice density  
 432 measurement. The imaging time ranged from 15–25 min. Although the difference in time at low temperature is large, it is  
 433 still necessary to analyze whether the low temperature during imaging affects the inclusion size.

434



435

436 **Figure 10: Comparison of inclusion sizes at different observed temperatures. The observed temperature was lowered by 5°C every**  
 437 **half hour.**

438

439 A sensitivity study was conducted to investigate whether inclusion size changes occur during short-term cooling. Thin ice  
 440 sections were repeatedly imaged at -10°C, -15°C and -20°C. Each ice section was maintained at each temperature for 30 min  
 441 before imaging. The measured inclusion sizes at each temperature are shown in Figure 10. There were significant linear  
 442 relationships between the measured inclusion sizes ( $r = 0.99, p < 0.001$ ), which revealed that short-term cooling did not  
 443 clearly affect the inclusion size. The observed sizes at -10°C and -15°C differed by  $2.5\% \pm 1.9\%$ , while the difference  
 444 reached  $4.5\% \pm 3.4\%$  between -10°C and -20°C. The corresponding lengths were  $0.006 \pm 0.008$  mm and  $0.009 \pm 0.008$  mm,  
 445 respectively. These results indicated that short-term cooling does affect the inclusion size, with a greater effect observed  
 446 under larger temperature differences. However, the effect is minimal and does not significantly impact the statistical results.

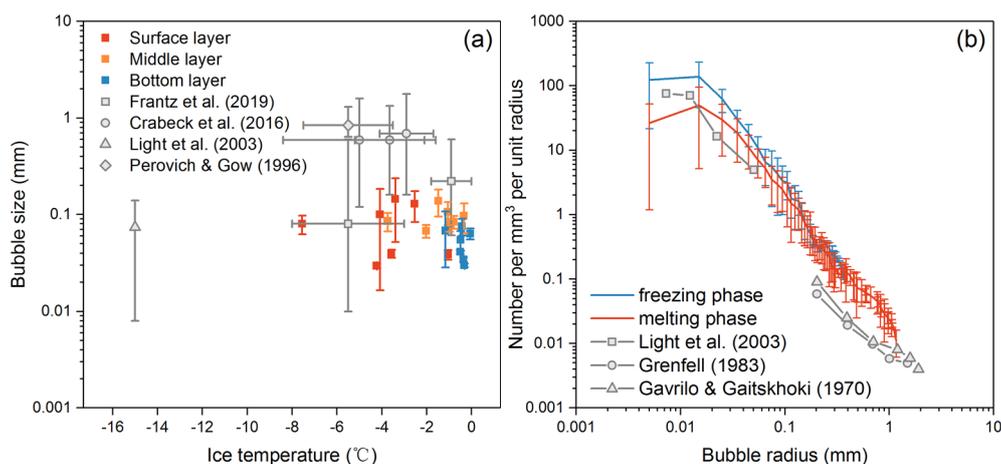


447 **4.2 Comparison with other observations**

448 This section provides a comparison of the inclusion sizes observed in this study with previous results. These earlier  
 449 observations were conducted of Arctic sea ice and saline ice grown in artificial pools. It is challenging to consider all the  
 450 potential influencing factors because the ice microstructure variations remain unclear. Figure 11a shows a comparison of the  
 451 gas bubble size in this study with that in other studies as a function of the ice temperature. In comparison, the ice  
 452 microstructure data of Light et al. (2003) and Perovich and Gow (2003) were obtained from first-year Arctic sea ice. Frantz  
 453 et al. (2019) observed the microstructure of melting Arctic ice by computed tomography (CT). In Crabeck et al. (2016), ice  
 454 was formed by freezing Arctic seawater in an in-ground concrete pool.

455 The bubble sizes in this study (0.003–3.2 mm) were consistent with previous results. The mean bubble sizes were close to  
 456 those reported by Light et al. (2003), slightly smaller than those reported by Frantz et al. (2019), and smaller than those  
 457 reported by Crabeck et al. (2016) and Perovich and Gow (1996). This study revealed more small bubbles than did previous  
 458 studies, which could be attributed to differences in the observation resolution. Frantz et al. (2019) and Crabeck et al. (2016)  
 459 obtained observations using CT. The resolution in the former study was 0.142 mm, while the resolution in the latter was  
 460 0.098 mm. Furthermore, the latter study observed a significant amount of snowice, which contained numerous large bubbles.  
 461 The gas bubbles in Light et al. (2003) and Perovich and Gow (1996) were observed in images at resolutions of 0.002–0.003  
 462 and 0.03 mm, respectively. The resolution in this study ranged from 0.001–0.002 mm. At a low resolution, small bubbles  
 463 may not be visible, yielding a larger mean size.

464



465

466 **Figure 11: Comparison of the a) size and b) size distribution of gas bubbles between this study and related studies.**

467

468 The bubble size distributions in this study suitably agreed with those in other studies (Figure 11b). The resolution of the gas  
 469 bubble size distributions of freezing lead ice in Grenfell (1996) was 0.1 mm, while no small bubbles were detected. The  
 470 mean  $V_a$  value in this ice (Section 3.2.1) is similar to the result (<1%) reported by Light et al. (2003). Therefore, the



471 comparison here is valid. Note that the horizontal axis in Figure 11 is the gas bubble radius and not the most commonly used  
472 diameter (e.g., Figure 8). In previous studies, the size distribution function of inclusions was consistently fitted by a power  
473 law, indicating that the number of inclusions increases with decreasing size. However, in this study, the minimum number of  
474 bubbles was small (Figure 8; Figure 11). This may be due to two reasons. First, small bubbles could not be fully observed,  
475 which causes a decrease in the number of minimum bubbles. The other reason is that the power law distribution is not  
476 appropriate. It is counterintuitive that the number of newly formed small bubbles is infinite. A Gaussian distribution may be  
477 more suitable for the size distribution, but this requires more accurate observations for confirmation.

478 The size of the brine pockets in this study ranged from 0.01–13 mm. Arcone et al. (1986) studied the microstructure of saline  
479 ice grown in an outdoor pool and obtained brine pocket sizes ranging from 0.04–1.68 mm (-30°C). Light et al. (2003) and  
480 Cole and Shapiro (1998) observed first-year Arctic ice, reporting brine pocket sizes of 0.01–8 mm at -15°C and  $2.4 \pm 2.5$   
481 mm at -14°C, respectively. Note that the smallest brine pocket measured by Cole and Shapiro (1998) was 0.1 mm. It is  
482 reasonable that the brine pocket size in this study is larger than that in other studies due to warmer ice (Section 3.1.3). In  
483 addition, the method in this study for identifying brine pockets (Section 2.3) may result in the classification of some small (<  
484 0.02 mm) and round brine pockets as gas bubbles, resulting in underestimation of the number of small brine pockets. The  
485 bubble distribution in this study suitably agrees with that reported by Light et al. (2003) (Figure 11b). That's to say, the  
486 number of small gas bubbles was not notably overestimated. Therefore, it could be concluded that the methods used for  
487 classifying small inclusions in different works do not considerably affect the overall statistical results.

#### 488 **4.3 Mechanism of variations in ice inclusions**

489 In this section, the mechanism of the variations in inclusions of different origins is examined according to the observations.  
490 The experiments were limited by the ice type. Although the salinity of saline ice in this study is less than that of typical sea  
491 ice, it is comparable to that of some estuaries along the coast and to that of sea ice in the Baltic Sea. Furthermore, the  
492 structural characteristics of ice closely resemble those of sea ice (Section 4.2). Therefore, the following discussion focuses  
493 not only on the present experimental results but also provides insights into the potential applications of sea ice.

##### 494 **4.3.1 Variations in the inclusion volume of the different layers**

495 There was a significant increase in  $V_a$  of the surface layer during the melting phase (Figure 5a). Furthermore, this melting  
496 process occurred only on a microscopic scale and did not affect the ice surface elevation. As shown in Figure 5b, the  
497 equilibrium melting process could result in an increase in  $V_a$  smaller than 0.02%, which is considerably less than the actual  
498 increase in  $V_a$  (~3%). Although the observed ice surface temperature and porosity did not fully meet the commonly used  
499 empirical values (Eicken et al., 2004; Vancoppenolle et al., 2007), these newly formed bubbles likely resulted from flushing  
500 or similar processes. Figure 9a further shows the relationship between the net shortwave radiation and the flushing process.  
501 This figure partially justifies the assumption regarding the formation of a porous sea ice surface layer (Macfarlane et al.,  
502 2023; Smith et al., 2022).



503 The general trend in  $V_b/V_a$  of the middle layer closely approached the melting equilibrium trend (Figure 5b), indicating that  
504 the new bubbles in the middle layer were partially thermally driven. It is expected that other newly formed gas bubbles were  
505 driven by convection from the bottom layer given a sufficient ice porosity. During the melting phase, the increase in  $V_a$  of  
506 the bottom layer was only approximately 2% less than the thermally driven value. These bubbles partly accumulate in the  
507 middle layer as a result of their buoyancy, while others escape from the ice bottom. Moreover, it was found that for  $V_a < 0.1\%$ ,  
508  $V_b$  hardly affected  $V_a$  (refer to the enlarged part of Figure 5b). On the one hand, the ice temperature decreased from -0.8 to -  
509 4°C, and  $V_b$  decreased from 5.5 to 1.0% during this period. A decrease in the temperature could cause an increase in  $V_a$  by  
510 0.5% due to gas release from cooled brine (Garcia and Gordon, 1992; Hamme and Emerson, 2004). Moreover, the latter  
511 could cause a decrease in  $V_a$  by 0.6% due to phase equilibrium. The two processes jointly result in a nearly constant bubble  
512 volume. On the other hand, it is also expected that some inactive gas bubbles occur in ice that are insensitive to  $V_b$  of ice.

### 513 4.3.2 Merging processes of inclusions

514 The variations in the inclusion volume in the middle layer are thermally driven, and the inclusion merging process is also  
515 thermally driven. Figure 9 shows significant relationships between the ice temperature difference and  $\eta$  of the middle layer.  
516 With ice warming, the number of inclusions decreases, and the size increases due to merging (Figure 7; Figure 8). However,  
517 there was no correlation between the ice surface temperature difference and the inclusion size distribution. Similarly, for the  
518 ice temperature and size distribution of bottom layer. These phenomena agree well with the results shown in Figure 5. The  
519 fitting relationship depicted in Figure 9 could be readily incorporated into the ice thermodynamic model. Other mechanisms  
520 remain needed to explain the merging of inclusions in the surface and bottom layers.

521 The merging equation obtained in this study differed from that used by Light et al. (2004). In their study,  $\eta$  was assumed to  
522 vary linearly in the log(volume) and log(number) spaces, which is supported by our observations (Figure 8). Furthermore, in  
523 their parameterization,  $\eta$  was set to 1 for the smallest inclusions, and the most merging was predicted to occur among larger  
524 inclusions. However, in this study, the merging of small inclusions was more notable than that of large inclusions (Figure 8).  
525 Currently, it is unclear whether this difference is the result of differences in ice types. Our findings conform with intuition, as  
526 the number of small inclusions exceeded that of larger inclusions, and the likelihood of additional nearby inclusions was  
527 greater.

528 The sensitivity of  $\eta$  to the ice temperature also differed between this study and that of Light et al. (2004). In their study,  $\eta$   
529 was 1 at -14°C and 0.1 at -1°C, with a decrease of 0.07 per °C. The minimum observed ice temperature in this study was -  
530 7.5°C. Therefore, it is unclear whether merging will stop at lower ice temperatures. The observed decreasing rates of  $\eta$  for  
531 small and large gas bubbles were 0.18 and 0.12 per °C, respectively. The corresponding values for small and large brine  
532 pockets were 0.19 and 0.16 per °C, respectively. Notably, the merging rate in this study was much greater than that reported  
533 by Light et al. (2004), although the salinity was much lower. Furthermore, the variations in the inclusion volume were  
534 eliminated herein. If the increase in the inclusion volume were considered, the merging rate would be even greater.



### 535 4.3.3 Variations in inclusions of different sizes

536 Although small inclusions exhibit a greater probability of merging than do large inclusions (Figure 8), the merging of large  
537 inclusions more notably impacts the mean inclusion size. For example, the merging of two 0.01-mm inclusions into one  
538 0.02-mm inclusion imposes a negligible effect on the mean size compared to the merging of two 1-mm inclusions into one 2-  
539 mm inclusion. This occurs because the effects on the number of inclusions are identical. The number of large gas bubbles in  
540 the middle layer is greater than that in the surface and bottom layers (Figure 6b). That is, the probability of gas bubbles  
541 merging in the middle layer is lower than that in the other layers. Consequently, the change in the size distribution in the  
542 middle layer is smaller than that in the other layers (Figure 8a), but the change in the mean size remains notable (Figure 7a).  
543 This explains why the proportion of large bubbles in the middle layer remains relatively constant, while the mean size  
544 continues to increase (Figure 7a, b).

545 In summary, the merging of large inclusions imposes a smaller influence on the size distribution but more notably influences  
546 the mean size than small inclusions. This partly explains why Light et al. (2004) only considered the merging of large  
547 inclusions but were still able to accurately estimate the reduced ice scattering coefficient due to merging. In addition, it is  
548 expected that large inclusions formed during freezing will maintain their relatively large sizes in the subsequent melting  
549 process. In other words, the banding features associated with microstructural gas and brine porosity variations (Cole et al.,  
550 2004) can hardly be easily altered during ice melting.

## 551 5 Summary and conclusions

552 The field work was designed to obtain information for providing a fundamental understanding of the variations in the size  
553 distribution of ice inclusions during the ice freezing or melting phase. Ice cores sampled from a saline lake adjacent to the  
554 Bohai Sea were analyzed weekly to study the ice microstructure and physical properties. High-resolution imagery was used  
555 to quantify the size and distribution of inclusions within ice.

556 The microstructure of ice continuously changes during both the growth and melting phases. Notably,  $V_a$  of ice remained  
557 relatively constant during the freezing phase but significantly increased during the melting phase. Similarly,  $V_b$  of ice  
558 significantly increased during the melting phase but decreased during the freezing phase. The general trend in  $V_b/V_a$  of the  
559 middle layer was much closer to melting equilibrium trend, which revealed that the newly formed bubbles in the middle  
560 layer were partly thermally driven. For the ice surface layer,  $V_a$  notably increased, with only a slight variation in  $V_b$ . A  
561 significant relationship between the net shortwave radiation and  $V_a$  of the surface layer was observed. It is suggested that the  
562 newly formed bubbles were a result of flushing or a similar process.

563 There was a general increasing trend in the inclusion size during the ice melting phase because of the increased proportion of  
564 large inclusions. The changes in the brine pocket size during the freezing phase were not as notable as those during the  
565 melting phase. Therefore, the gas bubble size in the middle layer decreased. Moreover, the gas bubble size in the surface and  
566 bottom layers clearly increased during the freezing phase. These changes were the result of merging. The merging factor  $\eta$  of



567 the inclusions linearly increased in the  $\log(\text{size})$ – $\log(\text{number})$  space. Notably, most merging occurred among smaller  
568 inclusions. Furthermore,  $\eta$  of the middle layer was significantly affected by the ice temperature difference. With the warming  
569 of ice, the number density of inclusions generally decreased due to merging. The  $\eta$  value of inclusions in the surface or  
570 bottom layers are insensitive to ice temperature differences, which reveals that other mechanisms control their merging  
571 processes.

572 This study provided new insights into microstructural changes during ice growth and decay, which represent the microscale  
573 effects of varying circumstances on ice. However, additional processes that require further investigation, such as the  
574 relationship between newly formed inclusions and the gas saturation level or growth velocity. They are needed to better  
575 understand ice microstructural changes and their subsequent effects on other optical and thermodynamic properties of ice.

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