

Design Study for an Airborne N₂O Lidar

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Abstract. Nitrous oxide (N₂O) is the third most important greenhouse gas modified by human activities after carbon dioxide and methane. This study examines the feasibility of airborne differential absorption lidar to measure N₂O concentration enhancements over agricultural, fossil fuel combustion, industrial and biomass burning sources. The mid-infrared spectral region, where suitably strong N₂O absorption lines exist, challenges passive remote sensing by means of spectroscopy due to both low solar radiation and thermal emission. Lidar remote sensing is principally possible thanks to the laser as independent radiation source, but has not yet been realized due to technological challenges. Mid-infrared N₂O absorption bands suitable for remote sensing are investigated. Simulations show that a spectral trough position between two strong N₂O lines in the 4.5 μm band is the favored option. A second option exists in the 3.9 μm band at the cost of higher laser frequency stability constraints and less measurement sensitivity. Both options fulfill the N₂O measurement requirements for agricultural areal or point source emission quantification (0.5 % measurement precision, 500 m spatial resolution) with technically realizable and affordable transmitter (100 mW average laser power) and receiver (20 cm telescope) characteristics for integrated-path differential absorption lidar that measures the column concentration beneath the aircraft. The development of an airborne N₂O lidar is feasible yet would benefit from progress in infrared laser transmitter and low-noise detection technology. It will also serve as a precursor to space versions which are still out of reach due to the lack of space technology.

20 **1 Introduction**

The average concentration of nitrous oxide (N₂O) amounts to only 337 ppb yet its global warming potential is nearly 300 times that of CO₂ on a 100-year span (Arias et al., 2021). This makes N₂O the third most important greenhouse gas contributing to human-induced global warming after carbon dioxide and methane. The major anthropogenic source is nitrogen fertilization on arable land. Further N₂O sources are processes in the chemical industry and combustion processes. According to current knowledge, anthropogenic sources contribute ~36 % to total global N₂O emissions (Tian et al., 2024). Emissions from natural soils and oceans constitute the major natural sources. Agricultural N₂O emissions are increasing due to interactions between nitrogen inputs and global warming, constituting an emerging positive N₂O-climate feedback. The recent increase in global N₂O emissions exceeds even the most pessimistic emission trend scenarios developed by the IPCC, underscoring the urgency to mitigate N₂O emissions (Tian et al., 2024). Estimating N₂O emissions from agriculture is inherently complex and comes with a high degree of uncertainty, due to variability in weather and soil characteristics, in

agricultural management options and in the interaction of field management with environmental variables (Eckl et al., 2021). Moreover, N₂O measurements are sparse. Consequently, more comprehensive N₂O concentration measurements are needed, particularly by means of remote sensing. Recently, the World Meteorological Organization has launched the Global Greenhouse Gas Watch (G3W) initiative to endorse, among others, this need (WMO, 2024).

35 The mid-infrared (mid-IR) spectral region, where suitably strong N₂O absorption lines exist, challenges passive remote sensing by means of spectroscopy due to both low solar radiation and thermal emission from Earth's surface (e.g., Ricaud et al., 2021; Vandenbussche et al., 2022). Lidar remote sensing is principally possible thanks to the laser as independent radiation source, but has not yet been realized due to technological challenges. While mid-IR lidars are employed for ground-based pollution detection (e.g., Robinson et al., 2011; Gong et al., 2020), to our knowledge, neither an airborne N₂O
40 lidar has been realized yet, nor has passive remote sensing by means of spectroscopy been used to measure N₂O concentrations in the lower troposphere.

Airborne N₂O lidar remote sensing has the potential to combine the advantages of high measurement accuracy, large-area coverage and dawn/dusk or nighttime measurement capability to study diurnal concentration variations. Initial studies have shown that Integrated-Path Differential-Absorption (IPDA) lidar from an airborne or even a satellite platform has the
45 potential to measure N₂O with high precision and low bias (Ehret and Kiemle, 2005; Ehret et al., 2008). It uses the Earth surface backscatter signal at an "online" laser wavelength tuned to a N₂O absorption line to obtain column concentrations of N₂O (Ehret et al., 2008; Amediek et al., 2017). A parallel reference measurement at the non-absorbed "offline" wavelength avoids biases generated by albedo variations or aerosol layers within the light path. In comparison to conventional lidar using backscatter from atmospheric molecules and aerosol, IPDA lidar yields high signal to noise ratio at comparatively low
50 instrument size since the surface backscatter is about 100 times stronger than the atmospheric backscatter in terms of laser energy per range gate. Still, accurate ranging by means of short laser pulses is important for precise measurements of the individual column length. First airborne systems for CO₂ and CH₄ have demonstrated high measurement accuracy and the capability to measure in broken cloud environments (Amediek et al., 2017; Sun et al., 2021; Barton-Grimley et al., 2022; Mao et al., 2024).

55 The objective to quantify agricultural areal or point source emissions requires obtaining N₂O column concentration gradients along the flight track between background levels outside the emission regions and the N₂O source regions, cultivated soils or exhaust plumes from, e.g., fertilizer production sites. The airborne lidar should point downward from a flight altitude of about 5 km, well above the boundary layer in which N₂O surface emissions disperse vertically by turbulence. Gradients over agricultural regions measured by airborne in-situ instruments (Eckl et al., 2021; Waldmann et al., 2024) suggest that the
60 maximum uncertainty of the N₂O column measurement should be 0.5 % and that an along-track horizontal measurement resolution of 500 m is sufficient. Consequently, the measurement instability due to instrumental drifts or changing biases should remain below 0.5 %. Experience from airborne lidar campaigns shows that long-term stability can be controlled by executing repeated flight legs over the same tracks, and over background concentrations in case those can be assumed

constant. To detect smaller but denser N₂O emission plumes from industrial production sites the horizontal resolution can be improved at the cost of precision. Lidar allows such tradeoffs to adapt to the measurement objectives. This study first investigates the N₂O spectroscopy to find suitable absorption lines. The chosen wavelength has consequences for the surface reflectance, the atmospheric absorption, the solar and thermal background radiation, as well as transmitter and detector options. All relevant environment, instrument and spectroscopic constraints are implemented into a lidar simulation model to design the instrument in order to meet the above measurement requirements. Finally, although beyond the scope of this study, concepts for suitable lidar transmitter and detector technologies are briefly discussed.

2 N₂O Spectroscopy

Up-to-date spectroscopic data retrieved with the HITRAN (high resolution transmission molecular absorption database) Application Programming Interface (HAPI) are used to find suitable absorption lines in the four major rotational-vibrational N₂O bands located at 2.9, 3.9, 4.5 and 7.8 μm (Nemtchinov et al., 2004; Loos et al., 2015; Kochanov et al., 2016; Gordon et al., 2022). Molecular absorption cross sections are calculated line-by-line with a resolution of 0.001 cm⁻¹ with the Hartmann-Tran scheme (Ngo et al., 2013) using standard atmosphere profiles of pressure, temperature and trace gas concentrations within the lowest 5 km, below the foreseen flight altitude. The vertically integrated product of the absorption cross section σ and the trace gas molecule number density n , both varying with altitude z between the surface sfc and the flight height flh, is the optical depth od:

$$od_{gas}(\lambda) = \int_{sfc}^{flh} \sigma_{gas}(z, \lambda) \cdot n_{gas}(z) dz \quad (1)$$

It is related to atmospheric transmission and represents the spectroscopic determining parameter for IPDA lidar column measurements. The IPDA technique is well described in e.g. Ehret et al. (2008) and Amediek et al. (2017). Criteria for line selection are (a) trace gas molecule number density, (b) appropriate line strength, related to the optimal optical depth, (c) low temperature sensitivity and (d) minimal influence by other gases. The optimal line strength or optical depth is a compromise between too weak absorption and saturation. The optimal optical depth typically lies between 0.5 and 1.2 and depends on column height and instrument noise (Ehret et al., 2008). Temperature sensitivity is determined using an atmospheric temperature profile shifted by 1 K and evaluating the difference in optical depth between the reference and the temperature-shifted optical depth.

The N₂O bands at 2.9 and 3.9 μm contain absorption lines of comparable strength, yet the entire 2.9 μm N₂O band is dominated by water vapor absorption lines whose wings are without exception stronger than the N₂O lines within the lowest 5 km, hence the 2.9 μm band is not shown here. The 3.9 μm N₂O band is illustrated in Fig. 1 showing the one-way column optical depth of the lowermost 5 km as function of vacuum wavenumber and wavelength. The 3.9 μm band is composed of

relatively weak lines suitable for satellite lidar (Ehret and Kiemle, 2005; Ehret et al., 2008) yet suboptimal for lower tropospheric concentration measurements. One of the strongest absorption lines, situated at 2576.54 cm^{-1} , is selected here (red line), characterized by both low influence of other absorbing gases and low temperature sensitivity. The offline reference wavenumber is set to a neighboring minimum absorption and temperature sensitivity position.

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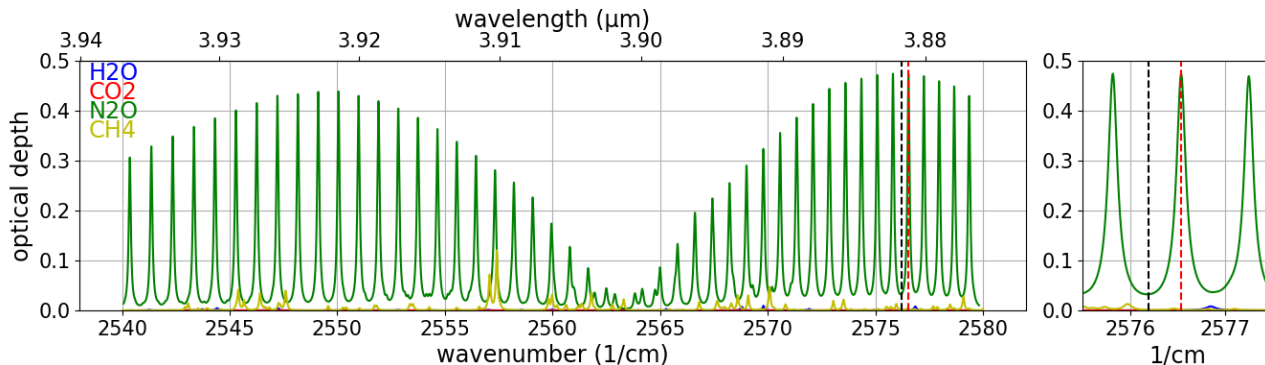


Figure 1: *Optical depth spectrum of trace gases in the $3.9 \mu\text{m}$ N_2O band in a standard atmosphere vertical column covering the lowest 5 km. The selected online (offline) position is highlighted in red (black) and within a close-up (right). Absorption lines of N_2O (green), water (blue), CO_2 (red) and CH_4 (yellow) need to be considered in this spectral region.*

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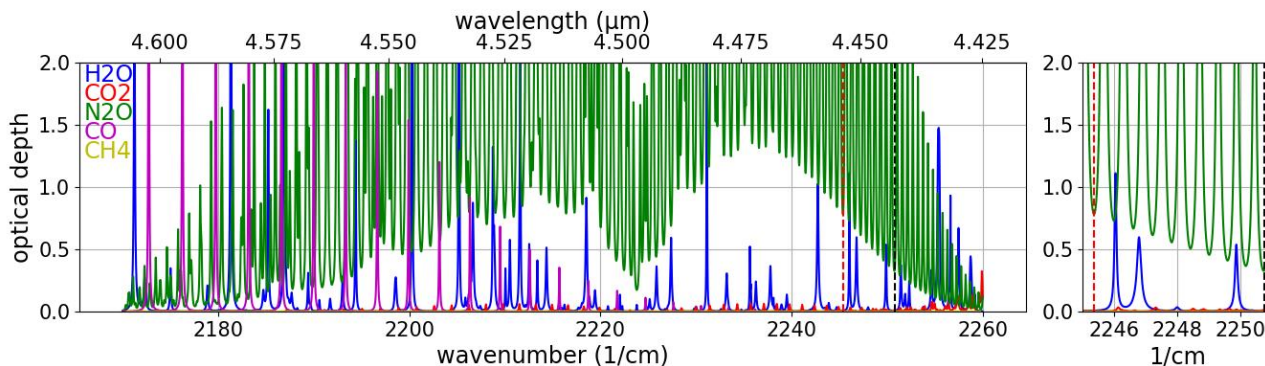


Figure 2: *Optical depth spectrum of trace gases in the $4.5 \mu\text{m}$ N_2O band in a standard atmosphere vertical column covering the lowest 5 km. The selected online (offline) position is highlighted in red (black) and within a close-up (right). Absorption lines of CO have to be considered in addition (magenta).*

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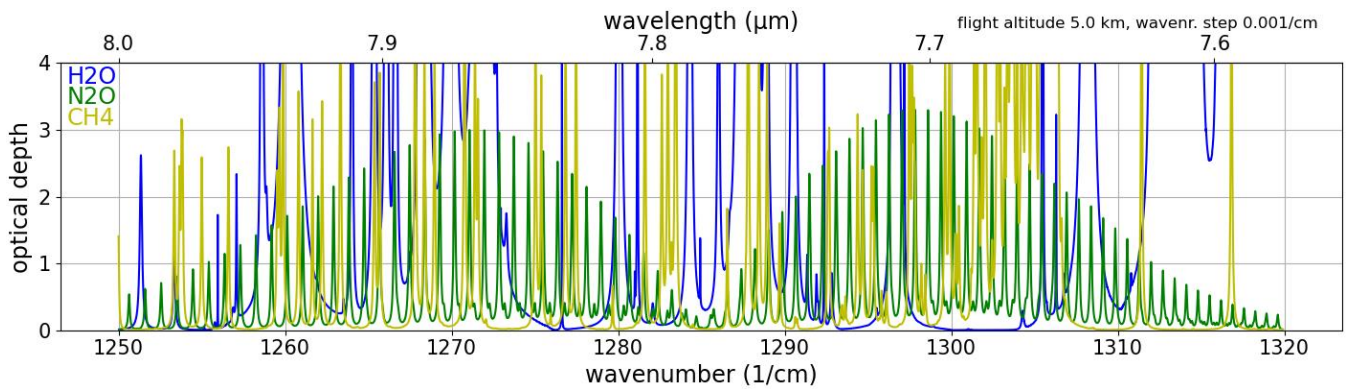


Figure 3: Optical depth spectrum of trace gases in the 7.8 μm N_2O band, as is Figures 1 and 2. The atmospheric window ends at 1310 cm^{-1} where a large water vapor absorption band begins.

115 The 4.5 μm band contains much stronger N_2O lines (Fig. 2). N_2O lines with suitable strength exist at both edges of the band, around 2180 and 2255 cm^{-1} , as well as in the center of the band. However, all of those reveal inappropriate due to overlapping water lines and high temperature sensitivity in the center of the band. Finally, Figure 3 illustrates the 7.8 μm band which is so densely populated with strong water and methane lines that no suitable N_2O line candidate is found. Water vapor is difficult to correct due to its high variability in the lower troposphere. Consequently, we restrict this study to the 3.9 and 4.5 μm N_2O bands. In the 4.5 μm band, trough positions at minimum optical depth in between two strong lines can be selected for both on- and offline, as used for CH_4 lidar and foreseen for MERLIN, the Remote Sensing Methane Lidar Mission (Kiemle et al., 2011; Amediek et al., 2017). A trough position has two advantages. First, it relaxes the laser frequency stability requirement due to a relatively flat optical depth in the center of the trough. More quantitatively, the derivative of optical depth with respect to wavenumber around the minimum of the trough is a factor fifty to hundred lower than outside the trough in the steep flank of a line (Kiemle et al., 2011). Second, the measurement sensitivity at low altitudes, i.e. near the surface where the N_2O sources are located, is improved thanks to pressure broadening of both lines surrounding the trough (Ehret et al., 2008). Figure 4 illustrates the differences in sensitivity between line center, wing and trough (i.e. far wing) positions. Within the lowest 1 km a spectral position in the center of the trough is found to increase the near-surface sensitivity to N_2O by about a factor of 1.5 ($= 1.4\% / 0.92\%$) in comparison to a line center position.

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Therefore, in the 4.5 μm band we select a trough position at the high-wavenumber side of the band at 2245.35 cm^{-1} because it is less influenced by other gases than the low-wavenumber side (Fig. 2). The closest possible offline position is at 2250.75 cm^{-1} . The 10.7 nm distance from the online position may require separate lasers for the generation of the on- and offline wavelengths and may lead to uncertainties estimated to $< 1\%$ if surface albedo or aerosol extinction are wavelength dependent (Amediek et al., 2009). Table 1 summarizes the spectroscopic characteristics of the candidate lines in both bands. The temperature sensitivity is sufficiently low, especially at the online positions. The additional optical depth by line wings

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of other gases is insignificant at 3.9 μm and ~ 0.01 at 4.5 μm . In the event of a 50 % concentration change possible for H_2O yet very unlikely for CO_2 , the impact on the total optical depth at 4.5 μm would be $0.005/0.79 \approx 0.6\%$ for the online and $0.005/0.34 \approx 1.5\%$ for the offline, which we consider uncritical. Note that our line selection is provisional as new spectroscopic data may lead to better options.

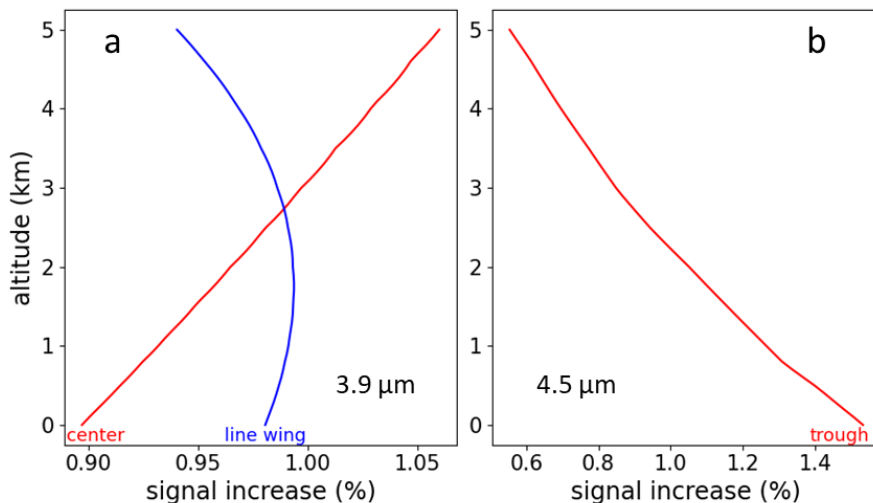


Figure 4: N_2O measurement sensitivity expressed as online optical depth (signal) increase under the assumption of a hypothetical 50 % N_2O concentration increase within a 100 m thick layer, as function of the altitude of this layer. (a) 3.9 μm line center (red) position of Fig. 1 in comparison with an online line wing (blue) position at 2576.57 cm^{-1} (very close to the line center; not further discussed). (b) 4.5 μm online trough position of Fig. 2.

Line selection	wavenumber cm^{-1}	N_2O opt. depth (0-5 km)	temperature sensitivity	opt. depth of other gases (0-5 km)
3.9 μm online, line center	2576.54	0.47	- 0.01 % / K	0.002 (CH_4)
3.9 μm offline	2576.20	0.03	0.43 % / K	0.001 (CH_4)
4.5 μm online, trough	2245.35	0.78	0.06 % / K	0.008 (H_2O)
4.5 μm offline	2250.75	0.33	- 0.31 % / K	0.008 (H_2O), 0.010 (CO_2)

Table 1: Selected online and offline spectral positions in the 3.9 and 4.5 μm N_2O absorption bands with corresponding N_2O optical depth for a vertical standard atmosphere column in the lowest 5 km, relative N_2O optical depth change per Kelvin temperature change, and optical depth of other trace gases.

3 Mid-IR Surface Albedo, Aerosol Influence and Background Radiation

The albedo is key for IPDA lidar which relies on surface backscatter intensity. It is generally low in the IR, compared to the near-IR and visible spectral ranges. Ehret and Kiemle (2005) and Ehret et al. (2008) used a value of 0.02 (2 %) for land surfaces. The Ecosystem Spaceborne Thermal Radiometer Experiment on Space Station (ECOSTRESS) spectral library contains a limited set of mid-IR reflectance data (Baldrige et al., 2009; Meerdink et al., 2019). Table 2 lists their agriculturally relevant values. We keep the small value of 2 % from our initial studies for the present simulation which can be considered a safe worst case. Over agricultural soils, extinction by rural aerosol within the boundary layer is expected. Based on IR lidar measurements by Vaughan et al. (1995 and 1998) and scaled to 3.9 and 4.5 μm using an Angström exponent of 1, we assume a worst-case maximum aerosol optical depth of 0.2 across the lowest 5 km. The Rayleigh optical depth due to air molecular extinction amounts to $\sim 2 \cdot 10^{-5}$ at around 4 μm in the lowest 5 km and is therefore negligible. Photons from solar scattered and thermal emitted radiation cause noisy background signals in the detector. The mid-IR radiation emitted from earth's surface is calculated with Planck's law (Stull, 2017) assuming a blackbody with albedo zero, at 288 K temperature and without atmosphere. According to Kirchhoff's law this represents the worst-case maximum thermal emission, also because the atmosphere is mostly colder than earth's surface. The solar radiation is calculated with Planck's law assuming an albedo of 0.4, a sun in the zenith and no atmosphere, which also represents a maximum-radiation worst case. Table 2 summarizes the environmental boundary conditions for the lidar simulation. The low total radiation, close to the spectral minimum of the sum of thermal emitted and solar scattered radiation represents a challenge for passive remote sensing in the mid-IR.

	N₂O band	3.9 μm	4.5 μm	unit	remarks
Albedo		0.03-0.04	0.02 -0.03	-	over grain or grass
		0.23-0.32	0.13-0.35		over soil
Aerosol optical depth, od_a		0.2	0.2	-	0 - 5 km
Earth emission		0.4	1.0	W / ($\text{m}^2 \mu\text{m sr}$)	albedo 0.0 and 288 K assumed
Solar backscatter		1.2	0.8	W / ($\text{m}^2 \mu\text{m sr}$)	albedo 0.4 assumed
Total background radiation		1.6	1.8	W / ($\text{m}^2 \mu\text{m sr}$)	sum of thermal emitted and solar scattered radiation
N ₂ O $od_{on} - od_{off}$		0.44	0.45	-	see Eqs. (1) and (3)

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Table 2: Mid-IR albedo, aerosol optical depth and background radiation used for the N₂O lidar simulation. The minimum albedo of 0.02 (bold) is selected as a worst case for the simulation. Soil has about ten times higher albedo than grain or grass. The differential absorption optical depth is about equal in both N₂O bands.

4 N₂O Lidar Simulation

185 The airborne lidar performance is assessed by implementing the measurement requirements together with environmental, instrumental and spectroscopic constraints into a lidar noise propagation model developed for earlier studies (Kiemle et al., 2011 and 2017). Atmospheric transmission and surface scattering are evaluated to compute the backscattered signal power as function of emitted laser power P_L , surface reflectance ρ (= albedo / π), receiver optical efficiency η , telescope area A , and range R (= 5 km) for the on- and offline wavelengths in the IPDA lidar equation:

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$$P_{on,off} = P_{L,on,off} \rho \eta A R^{-2} \exp^{-2(od_a + od_{on,off})} \quad (2)$$

According to the Beer-Lambert law the exponential term represents the atmospheric transmission along the vertical path, lowered by the aerosol optical depth od_a and the N₂O on- and offline optical depths. Solving Eq. (2) for the respective on- and offline optical depths, and assuming constant surface albedo, optical efficiency, and aerosol optical depth for both on- and offline wavelengths, we obtain the differential absorption optical depth DAOD from subtracting the offline solution of Eq. (2) from the online solution:

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$$DAOD = od_{on} - od_{off} = \frac{1}{2} \ln \left(\frac{E_{L,off}/E_{ref,off}}{E_{L,on}/E_{ref,on}} \right), \quad (3)$$

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where $E_{L,on,off}$ are the received on-/offline laser pulse energies, and $E_{ref,on,off}$ are energy reference measurements accounting for variations of the emitted pulse power P_L . After Eq. (1) the DAOD is proportional to the N₂O column concentration weighted with the absorption cross section. Table 2 lists the DAOD values expected in a reference atmosphere.

205 Table 3 lists the major instrument parameters. The larger the average laser power, surface reflectance (albedo), and telescope size, the stronger the received signal power and consequently the signal-to-noise ratio (SNR). Further parameters influencing the SNR are the flight altitude, the horizontal resolution, the laser pulse repetition rate, the receiver field-of-view and several detector parameters. Parametric analyses allow to finetune the instrument with the aim to optimize efficiency or flexibility. Parameters can depend on each other, such as the aircraft velocity, the horizontal resolution, the repetition rate, and the number of averaged pulses. Likewise, for the laser, repetition rate, pulse energy and average laser power are related. Finally, the telescope field-of-view is related to its diameter, its focal ratio, and the detector size. Equations implement all relevant dependencies in the model. For more details we refer to our former studies (Ehret et al., 2008; Kiemle et al., 2011 and 2017).

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Simulation parameter	value	reference
Requirements: flight altitude	5 km	Eq. (2): R
horizontal along-track resolution	500 m	
aircraft velocity	150 m/s	
Laser: average IR online and offline power	100 mW	Eq. (2): $P_{L,on,off}$
pulse energy	0.5 mJ	
pulse energy reference measurement precision	1 %	Eq. (3): $E_{ref_on,off}$; Ehret et al. (2008)
double pulse (online, offline) repetition rate	100 Hz	
number of averaged double pulses	333	
pulse length	15 ns	Ehret et al. (2008)
beam divergence, full angle	0.6 mrad	
spectral line width	30 MHz	Ehret et al. (2008)
frequency stability at 3.9 μm	~ 1 MHz	Ehret et al. (2008)
frequency stability at 4.5 μm	~ 100 MHz	Kiemle et al. (2011)
Receiver: telescope area	0.03 m²	Eq. (2): A (20 cm diam.)
telescope focal ratio, 1/f	1.25	
optical efficiency	0.65	Eq. (2): η ; Kiemle et al. (2011)
optical narrow-band filter	1 nm	Ehret et al. (2008)
field-of-view, full-angle	0.8 mrad	
footprint size at surface	4 m	
Detector: MCT APD, NEP	0.1 pW/Hz^{0.5}	e.g., Sun et al. (2017)
diameter	200 μm	e.g., Martyniuk et al. (2023)
bandwidth	3 MHz	Ehret et al. (2008)
Surface albedo	0.02	Eq. (2): $\rho\pi$; Ehret et al. (2008)

Table 3: N_2O lidar instrument parameters assumed for the simulation, partly adopted from earlier studies and regarded as achievable. Parameters of first importance to the performance are in bold.

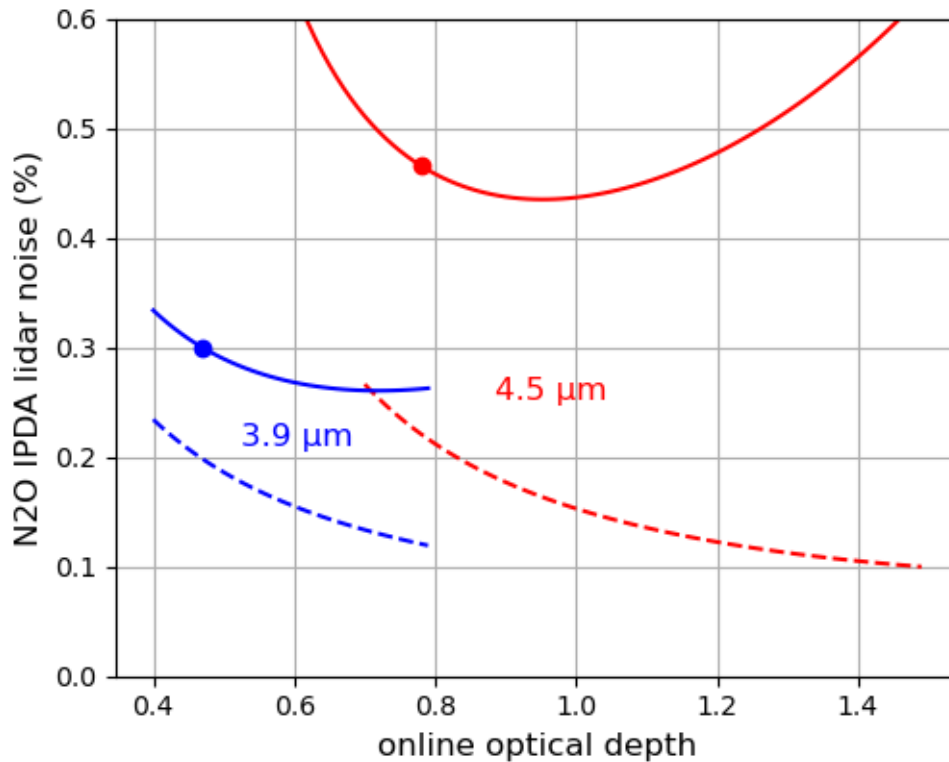


Figure 5: Simulated N_2O lidar measurement precision at 3.9 (blue) and 4.5 μm (red) as function of online optical depth under the conditions of Tables 2 and 3. The dots indicate the selections of Table 1 and the dashed lines represent an ideal noise-free detector for comparison. The absence of strong lines in the 3.9 μm band limits the 3.9 μm online optical depth range.

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The simulation is run with the environment conditions of Table 2 and the instrument parameters of Table 3. All noise contributors, Poisson noise from laser photons and background radiation, detector noise, laser speckle noise within the field of view, and energy reference measurement noise are considered. Speckle noise can be more significant for laser measurements in the mid-IR since the speckle cell sizes are larger and there are fewer “speckles” (regions of constructive interference) on the detector surface. This effect is compensated by a larger telescope field-of-view and laser beam divergence, compared to near-IR applications. As all noise sources are basically uncorrelated, error propagation on the basis of Eqs. (2) and (3) provides the overall one-sigma precision of the N_2O measurements as function of the prescribed online optical depth for both N_2O bands (Fig. 5). The offline optical depth is kept at a constant level of 0.03 (0.33) at 3.9 (4.5) μm . At 3.9 μm this level corresponds to a representative minimum optical depth within the band (Fig. 1), while at 4.5 μm the offline from Table 1 may serve several neighboring online trough options (Fig. 2). The dashed lines show the performance of an ideal noise-free detector for comparison. While the detector noise is assumed zero, all other noise contributors remain: Poisson / shot noise, speckle noise, and energy measurement noise. Their minima are right-shifted because the optimum

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online optical depth is larger under low-noise conditions (Ehret et al., 2008). The curves are flatter since a low-noise instrument is more tolerant with respect to suboptimal spectroscopic settings.

240 Assuming, as a provisional proxy, a mercury cadmium telluride (MCT) avalanche photodiode (APD) detector with a noise
equivalent power (NEP) of $0.1 \text{ pW/Hz}^{1/2}$, the optimum online optical depth for minimum noise is around 0.7 (0.9) for 3.9
(4.5) μm . Due to the lack of more comprehensive mid-IR detector data the NEP is estimated on the basis of near-IR
realizations and mid-IR prototypes (Sun et al., 2017; Martyniuk et al., 2023) using large security margins, likely representing
a worst case. The absence of strong lines in the 3.9 μm band (Fig. 1) prevents an optimum online setting yet the low offline
245 optical depth of 0.03 provides satisfying low-noise levels (Fig. 5). At 4.5 μm , a trough nearby the optimum optical depth
could be selected (Fig. 2). Stronger neighboring troughs that would fit the optimum suffer from overlapping water line wings
and larger temperature sensitivity. The 4.5 μm selection also allows for a measurement precision fulfilling the initial
requirement of 0.5 %, although at a higher noise level, primarily due to the relatively high offline optical depth of 0.33.
Away from the optimum, noise increases towards lower optical depths because of a smaller DAOD (Eq. 3), and towards
250 higher optical depths because of online signal attenuation.

In addition to uncorrelated random noise which averages out over longer data accumulation lengths, persisting systematic
uncertainties (biases) may arise from errors in the spectroscopic parameters. The HITRAN database specifies the N_2O line
intensity uncertainties to within 2 and 5 %. This does not threaten the objectives to quantify agricultural areal or point source
emissions since those are derived from relative column gradients between sources and background rather than from absolute
255 measurements. In addition, spectroscopy errors can be corrected by comparing the lidar columns against collocated profiles
from high accuracy aircraft in-situ sensors (Amediek et al., 2017; Mao et al., 2024). Biases may also arise from variability in
the actual aerosol, temperature and pressure profiles within the columns. Experience and simulation (Ehret et al., 2008;
Kiemle et al., 2011; Amediek et al., 2017) shows that these usually remain below 1 %. Finally, albedo variations cause
measurement uncertainties if the on- and offline surface laser spots are not fully overlapping, which is generally the case.
260 Those however tend to behave like random deviations leading to slightly increased noise levels (Amediek et al., 2009).

5 Technology Options and Readiness

IR lidar transmitters that can be considered for the described purpose are (a) tunable solid-state lasers such as transition-
metal (TM)-doped II-VI chalcogenide lasers, for example Fe:ZnS or Fe:ZnSe lasers, (b) optical parametric oscillators (OPO)
and amplifiers, and (c) laser sources based on nonlinear difference frequency generation (DFG) or Raman shifting.
265 Comprehensive overviews on recent advances in those laser-based mid-infrared sources are given in Vodopyanov (2020)
and Ren et al. (2021). Using OPOs, wavelengths in the 3.9 to 4.5- μm range are readily accessible. When pumping with the
ubiquitous Nd:YAG laser at 1.064 μm , the corresponding signal wavelengths that lead to an idler wavelength at 3.9 or 4.5
 μm are ~ 1.46 or $1.39 \mu\text{m}$, respectively. This requires suitable nonlinear crystals with transparency at all these wavelengths.
But, other pump laser sources at longer wavelength such as 2.05 μm (e.g. Medina et al., 2021), cascaded OPOs or DFG

270 sources are also options (e.g. DFG of 1.064 μm with 1.46 μm results in 3.9 μm and mixing 1.064 μm with 1.39 μm results in 4.5 μm , respectively). Using DFG, lidar measurements of species such as hydrocarbons in the wavelength range around 3.4 μm have been performed (Robinson et al., 2011; Gardiner et al., 2017).

Low-noise and high-bandwidth radiation detection is a challenge in the mid-IR. Prototype MCT APDs can achieve very low excess noise in the mid-IR, yet cooling down to at least 200 K is required to reduce dark currents. Sun et al. (2017 and 2021) report a detector linear analog output with a dynamic range of 2-3 orders of magnitude at a fixed APD gain for MCT material that has a cut-off at 4.3 μm . These detectors work well at 3.9 μm yet have little response at 4.5 μm . Generally, developments are ongoing but manufacturability is considered low (Chen et al., 2021; Martyniuk et al., 2023). In addition, the literature reveals that efforts go into the development of imaging sensors, while lidar requires a single sensor with a large photosensitive area in order to satisfy optical constraints (cf. Table 3). Due to the lack of data we used in our study a conservative approach for the simulation, with a large security margin for the detector noise on the basis of data from near-IR realizations and mid-IR prototypes. An alternative to MCT is indium antimonide (InSb), yet mid-IR InSb APDs apparently have more noise and less bandwidth (Abautret et al., 2015; Alimi et al., 2020). Besides APD detectors, up-conversion detectors (UCD; Hoegstedt et al., 2016; Meng et al., 2018) or superconducting nanowire single-photon detectors (SNSPD) could offer high-efficiency, low-noise signal detection, yet SNSPDs require operating temperatures below 3 K which is challenging onboard aircraft. A single-photon response was reported up to 25 K at 1.5 μm (Charaev et al., 2023), unfortunately not much less challenging. Also, in this area, developments are underway.

Concerning methodical alternatives for active remote sensing, the more common differential absorption lidar (DIAL) technique exploits atmospheric instead of surface backscatter with the advantage of providing vertical profiles of trace gases instead of column concentrations. A dedicated simulation using the same lidar simulator shows that this is at the expense of a 100 times larger laser power and telescope aperture product ($P_L \cdot A = 0.3 \text{ W m}^2$ instead of 0.003 W m^2 from Table 3) to compensate for the roughly 100 times weaker atmospheric backscatter signals (in terms of laser photons per range gate), even within a boundary layer with rural aerosol. A low-power alternative is IPDA or DIAL with heterodyne instead of direct signal detection. It requires a diffraction-limited optical setup and laser pulse repetition rates in the kHz range to manage speckle-induced noise. So far, ground-based profiling systems (Koch et al., 2008; Yu et al., 2024) and an airborne realization (Spiers et al., 2011; Jacob et al., 2019) for CO_2 have been reported, yet only in the near-IR. Another low-power option for IPDA is (modulated) continuous-wave (cw) laser operation instead of emitting short pulsed signals (e.g., Campbell et al., 2020). For measurements with a precision requirement below 1 % however, the length of the atmospheric column must be known to an accuracy of better than 3 m which is only practicable with short laser pulses in combination with a sufficiently large detection bandwidth (Table 3; Ehret et al., 2008). Alternatively, a precision range finder had to be added which annihilates the cost benefit of cw lidar. We conclude that methodical alternatives for N_2O active remote sensing are either too expensive, or their maturity for airborne operation lags behind that of direct detection pulsed IPDA.

6 Conclusion

With a resulting noise level of $< 0.5\%$ an airborne IPDA lidar provides important new capabilities for N_2O regional gradient or hot spot detection with technically realizable and affordable transmitter (100 mW average laser power) and receiver (20 cm telescope, MCT APD) characteristics. Using an MCT APD detector that requires cooling to 200 K the system could fit into a small- to mid-size research aircraft. The simulation results show better performance at $3.9\ \mu\text{m}$ in terms of the noise level. On the other hand, the trough position at $4.5\ \mu\text{m}$ yields higher measurement sensitivity at low altitudes and considerably relaxes the laser frequency stability requirement. Which option is finally preferred will depend on many factors including several aspects of laser technology such as availability, complexity, linewidth, frequency locking performance, as well as detector availability, costs, aircraft suitability, etc. The simulation tool will be applied to trade off various instrument options as technology is developing. Better low-noise IR detectors will be particularly beneficial. While a satellite implementation is not impossible, but still far away because of lacking space-proof technology, the development of an airborne N_2O lidar at 3.9 or $4.5\ \mu\text{m}$ is recommended given the technical feasibility and the scientific-societal need.

315 Code/Data availability

Code and data can be provided by the first author on request.

Author contribution

CK developed the model code, performed the simulations, and prepared the manuscript with contributions from all co-authors. AF, CF, GE and MW contributed information on available laser and detector technology.

Competing interests

The authors declare that they have no conflict of interest. CK is member of the editorial board of AMT.

References

- 325 Abautret, J., Perez, J. P., Evirgen, A., Rothman, J., Cordat, A., Christol, P.: Characterization of midwave infrared InSb avalanche photodiode. *J. Appl. Phys.*, 117 (24): 244502, doi:[10.1063/1.4922977](https://doi.org/10.1063/1.4922977), 2015.
- Alimi, Y., Pusino, V., Steer, M. J., and Cumming, D. R. S.: InSb Avalanche Photodiodes on GaAs Substrates for Mid-Infrared Detection, *IEEE Transactions on Electron Devices*, 67, 1, 179-184, doi: 10.1109/TED.2019.2956283, 2020.
- Amediek, A., Fix, A., Ehret, G., Caron, J., and Durand, Y.: Airborne lidar reflectance measurements at $1.57\ \mu\text{m}$ in support of the A-SCOPE mission for atmospheric CO_2 , *Atmos. Meas. Tech.*, 2, 755–772, doi:[10.5194/amt-2-755-2009](https://doi.org/10.5194/amt-2-755-2009), 2009.
- 330 Amediek, A., Ehret, G., Fix, A., Wirth, M., Büdenbender, C., Quatrevalet, M., Kiemle, C., and Gerbig, C.: CHARM-F - a new airborne integrated-path differential-absorption lidar for carbon dioxide and methane observations: measurement

- performance and quantification of strong point source emissions, *Applied Optics*, 56 (18), 5182-5197, doi: 10.1364/AO.56.005182, 2017.
- 335 Arias, P.A. et al.: Technical Summary. In *Climate Change 2021: The Physical Science Basis. Contribution of Working Group I to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change*, Cambridge University Press, Cambridge, United Kingdom and New York, USA, pp. 33–144. doi:10.1017/9781009157896.002, 2021.
- Baldridge, A. M., Hook, S. J., Grove, C. I. and Rivera, G.: The ASTER Spectral Library Version 2.0, *Remote Sensing of Environment*, 113, 711-715, 2009.
- 340 Barton-Grimley, R. A., Nehrir, A. R., Kooi, S. A., Collins, J. E., Harper, D. B., Notari, A., Lee, J., DiGangi, J. P., Choi, Y., and Davis, K. J.: Evaluation of the High Altitude Lidar Observatory (HALO) methane retrievals during the summer 2019 ACT-America campaign, *Atmos. Meas. Tech.*, 15, 4623–4650, doi:10.5194/amt-15-4623-2022, 2022.
- Campbell, J. F., Lin, B., Dobler, J., Pal, S., Davis, K., Obland, M. D., et al.: Field evaluation of column CO₂ retrievals from intensity-modulated continuous-wave differential absorption lidar measurements during the ACT-America campaign. *Earth and Space Science*, 7, e2019EA000847. <https://doi.org/10.1029/2019EA000847>, 2020.
- 345 Charaev, I., Bandurin, D. A., Bollinger, A. T., Phinney, I. Y., Drozdov, I., Colangelo, M., Butters, B. A., Taniguchi, T., Watanabe, K., He, X., Medeiros, O., Božović, I., Jarillo-Herrero, P., and Berggren, K. K.: Single-photon detection using high-temperature superconductors, *Nature Nanotechnol.* 18, 343-349, 2023.
- Chen, J., Chen, J., Li, X. et al. High-performance HgCdTe avalanche photodetector enabled with suppression of band-to-band tunneling effect in mid-wavelength infrared, *Nature npj Quantum Mater.* 6, 103, [doi:10.1038/s41535-021-00409-3](https://doi.org/10.1038/s41535-021-00409-3), 2021.
- 350 Eckl, M., Roiger, A., Kostinek, J., Fiehn, A., Huntrieser, H., Knote, C., Barkley, Z. R., Ogle, S., Baier, B. C. Sweeney, C. and Davis, K. J.: Quantifying nitrous oxide emissions in the U.S. Midwest - A top-down study using high resolution airborne in situ observations, *Geophys. Res. Lett.*, 48 (5), doi: 10.1029/2020GL091266, 2021.
- 355 Ehret, G. and Kiemle, C.: Requirements Definition for Future DIAL Instruments, ESA Study Final Report, ESA-CR(P)-4513, ESA Contract no. 10880/03/NL/FF, 2005.
- Ehret, G., Kiemle, C., Wirth, M., Amediek, A., Fix, A., and Houweling, S.: Space-borne remote sensing of CO₂, CH₄, and N₂O by integrated path differential absorption lidar: a sensitivity analysis, *Appl. Phys. B* 90, 593-608, 2008.
- Gardiner, T., Helmore, J., Innocenti, F., Robinson, R.: Field Validation of Remote Sensing Methane Emission Measurements. *Remote Sens.*, 9, 956, <https://doi.org/10.3390/rs9090956>, 2017.
- 360 Gong, Y., Bu, L., Yang, B., Mustafa, F.: High Repetition Rate Mid-Infrared Differential Absorption Lidar for Atmospheric Pollution Detection, *Sensors*, 20, 2211, doi:[10.3390/s20082211](https://doi.org/10.3390/s20082211), 2020.
- Gordon, I. E., Rothman, L. S., Hargreaves, R. J., Hashemi, R., Karlovets, E. V., Skinner, F. M., et al.: The HITRAN2020 molecular spectroscopic database, *J. Quant. Spectrosc. Radiat. Transfer*, 277, 107949, doi:10.1016/j.jqsrt.2021.107949, 2022.
- 365

- Hoegstedt, L., Fix, A., Wirth, M., Pedersen, C., and Tidemand-Lichtenberg, P.: Upconversion-based lidar measurements of atmospheric CO₂, *Optics Express* 24, 5, doi:10.1364/OE.24.005152, 2016.
- Jacob, J. C., Menzies, R. T. and Spiers G. D.: Data Processing and Analysis Approach to Retrieve Carbon Dioxide Weighted-Column Mixing Ratio and 2- μ m Reflectance With an Airborne Laser Absorption Spectrometer, *IEEE Transactions on Geoscience and Remote Sensing*, 57, 2, 958-971, doi:10.1109/TGRS.2018.2863711, 2019.
- 370 Kiemle, C., Quatrevalet, M., Ehret, G., Amediek, A., Fix, A., and Wirth, M.: Sensitivity studies for a space-based methane lidar mission, *Atmos. Meas. Tech.*, 4, 2195-2211, doi:10.5194/amt-4-2195-2011, 2011.
- Kiemle, C., Ehret, G., Amediek, A., Fix, A., Quatrevalet, M., and Wirth, M.: Potential of Spaceborne Lidar Measurements of Carbon Dioxide and Methane Emissions from Strong Point Sources, *Remote Sens.* 9, 1137, doi:10.3390/rs9111137, 2017.
- 375 Koch, G. J., Beyon, J. Y., Gibert, F., Barnes, B. W., Ismail, S., Petros, M., Petzar, P. J., Yu, J., Modlin, E. A., Davis, K. J., and Singh, U. N.: Side-line tunable laser transmitter for differential absorption lidar measurements of CO₂: design and application to atmospheric measurements, *Appl. Opt.* 47, 944-956, 2008.
- Kochanov, R.V., Gordon, I.E., Rothman, L.S., Wcislo, P., Hill, C., and Wilzewski, J.S.: HITRAN Application Programming Interface (HAPI): A comprehensive approach to working with spectroscopic data, *J. Quant. Spectrosc. Radiat. Transfer*, 177, 380 15-30, 2016.
- Loos, J., Birk, M., Wagner, G.: Pressure broadening, -shift, speed dependence and line mixing in the ν_3 rovibrational band of N₂O, *J. Quant. Spectrosc. Radiat. Transfer* 150, 300-309, 2015.
- Mao, J., Abshire, J. B., Kawa, S. R., Sun, X., and Riris, H.: Airborne lidar measurements of atmospheric CO₂ column concentrations to cloud tops made during the 2017 ASCENDS/ABoVE campaign, *Atmos. Meas. Tech.*, 17, 1061–1074, 385 doi:10.5194/amt-17-1061-2024, 2024.
- Martyniuk, P., Wang, P., Rogalski, A., Gu, Y., Jiang, R., Wang, F., Hu, W.: Infrared avalanche photodiodes from bulk to 2D materials, *Light: Science & Applications* 12:212, doi:[10.1038/s41377-023-01259-3](https://doi.org/10.1038/s41377-023-01259-3), 2023.
- Meng, L., Fix, A., Wirth, M., Hoegstedt, L., Tidemand-Lichtenberg, P., Pedersen, C., and Rodrigo, P. J.: Upconversion detector for range-resolved DIAL measurement of atmospheric CH₄, *Optics Express* 26, 4, 2018.
- 390 Meerdink, S. K., Hook, S. J., Roberts, D. A., and Abbott, E. A.: The ECOSTRESS spectral library version 1.0, *Remote Sensing of Environment*, 230, 111196, 2019.
- Medina, M. A., Piotrowski, M., Schellhorn, M., Wagner, F. R., Berrou, A., and Hildenbrand-Dhollande, A.: Beam quality and efficiency of ns-pulsed high-power mid-IR ZGP OPOs compared in linear and non-planar ring resonators. *Opt. Express* 29(14), 21727–21737, <https://doi.org/10.1364/OE.487887>, 2021.
- 395 Nemtchinov, V., Sun, C., Varanasi, P.: Measurements of Line Intensities and Line Widths in the ν_3 -fundamental Band of Nitrous Oxide at Atmospheric Temperatures, *J. Quant. Spectrosc. Radiat. Transfer* 83, 267-284, 2004.
- Ngo, N.H., Lisak, D., Tran, H., and Hartmann, J.-M.: An isolated line-shape model to go beyond the Voigt profile in spectroscopic databases and radiative transfer codes, *J. Quant. Spectrosc. Radiat. Transfer*, 129, 89–100, [doi:10.1016/j.jqsrt.2013.05.034](https://doi.org/10.1016/j.jqsrt.2013.05.034), 2013.

- 400 Ren, T., Wu, C., Yu, Y., Dai, T., Chen, F., Pan, Q.: Development Progress of 3–5 μm Mid-Infrared Lasers: OPO, Solid-State and Fiber Laser. *Appl. Sci.*, 11, 11451. <https://doi.org/10.3390/app112311451>, 2021.
- Ricaud, P., et al.: The Monitoring Nitrous Oxide Sources (MIN2OS) satellite project. *Remote Sensing of Environment*, 266, 112688, <https://doi.org/10.1016/j.rse.2021.112688>, 2021.
- Robinson, R., Gardiner, T., Innocenti, F., Woods, P., and Coleman, M.: Infrared differential absorption Lidar (DIAL) measurements of hydrocarbon emissions, *J. Environ. Monit.*, 13, 2213–2220, doi:10.1039/C0EM00312C, 2011.
- 405 Spiers, G. D., Menzies, R. T., Jacob, J., Christensen, L. E., Phillips, M. W., Choi, Y., and Browell, E. V.: Atmospheric CO₂ measurements with a 2 μm airborne laser absorption spectrometer employing coherent detection, *Appl. Opt.* 50, 2098–2111, doi: 10.1364/AO.50.002098, 2011.
- Stull, R.: *Practical Meteorology: An Algebra-based Survey of Atmospheric Science*, version 1.02b, Univ. of British Columbia, 940 pages, ISBN 978-0-88865-283-6, 2017.
- 410 Sun, X., Abshire, J. B., Beck, J. D., Mitra, P., Reiff, K., and Yang, G.: HgCdTe avalanche photodiode detectors for airborne and spaceborne lidar at infrared wavelengths, *Opt. Express* 25, 16589–16602, doi:[10.1364/OE.25.016589](https://doi.org/10.1364/OE.25.016589), 2017.
- Sun, X., Abshire, J. B., Ramanathan, A., Kawa, S. R., and Mao, J.: Retrieval algorithm for the column CO₂ mixing ratio from pulsed multi-wavelength lidar measurements, *Atmos. Meas. Tech.*, 14, 3909–3922, [https://doi.org/10.5194/amt-14-](https://doi.org/10.5194/amt-14-3909-2021)
- 415 [3909-2021](https://doi.org/10.5194/amt-14-3909-2021), 2021.
- Tian, H., et al.: Global nitrous oxide budget 1980–2020, *Earth System Science Data*, doi:[10.5194/essd-2023-401](https://doi.org/10.5194/essd-2023-401), 2024.
- Vandenbussche, S., Langerock, B., Vigouroux, C., Buschmann, M., Deutscher, N. M., Feist, D. G., García, O., Hannigan, J. W., Hase, F., Kivi, R., et al.: Nitrous Oxide Profiling from Infrared Radiances (NOPIR): Algorithm Description, Application to 10 Years of IASI Observations and Quality Assessment. *Remote Sensing*, 14(8):1810.
- 420 <https://doi.org/10.3390/rs14081810>, 2022.
- Vaughan, J. M., Brown, D. W., Nash, C., Alejandro, S. B., and Koenig, G. G.: Atlantic Atmospheric Aerosol Studies: 2. Compendium of Airborne Backscatter Measurements at 10.6 μm , *J. Geophys. Res. - Atm.*, 100 (D1), 1043–1065, doi 10.1029/94JD01817, 1995.
- Vaughan, J. M., Geddes, N. J., Flamant P. H., and Flesia, C.: Establishment of a backscatter coefficient and atmospheric database, DERA Report for ESA Contract no. 12510/97/NL/RE, DERA/EL/ISET/CR980139/1.0, 1998.
- 425 Vodopyanov, Konstantin L.: *Laser-Based Mid-infrared Sources and Applications*. Print ISBN:9781118301814, Online ISBN:9781119074557, DOI:10.1002/9781119074557, John Wiley & Sons, Incorporated, 2020.
- Waldmann, P., et al.: Quantifying agricultural CH₄ and N₂O emissions of the Netherlands using a novel airborne eddy-covariance measurements system: First results of the GHGMon campaign in June 2023, EGU24-19467 General Assembly of the European Geosciences Union, Vienna, April 2024.
- 430 WMO, 2024: <https://wmo.int/activities/global-greenhouse-gas-watch-g3w>
- Yu, S., Guo, K., Li, S., Han, H., Zhang, Z., and Xia, H.: Three-dimensional detection of CO₂ and wind using a 1.57 μm coherent differential absorption lidar, *Opt. Express* 32, 21134–21148, <https://doi.org/10.1364/OE.523904>, 2024.