Enhanced bed shear stress and mixing in the near wake of an offshore wind turbine monopile

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Abstract. Tidal flow past offshore wind farm (OWF) infrastructure generates a turbulent vortex wake that is hypothesised to enhance seabed stress and water column turbulence mixing, and thereby affect seabed mobility, water column stratification, the transport of nutrients and oxygen, and result in ecological impact. We collect novel hydrodynamic data 40 m from an OWF monopile over a spring-neap cycle, and use high frequency velocity measurements to quantify turbulence. Outside of the wake we observe a classical depth-limited boundary layer, with strong turbulence production and dissipation forced by tidal shear at the seabed. Inside the wake, turbulence production, dissipation and stress are enhanced throughout the full water column and are maximized above mid-depth where they correspond to a strong mean velocity deficit. Our results show that the seabed drag coefficient is doubled from $C_d = 3.5 \times 10^{-3}$ to $7.8 \times 10^{-3}$, suggesting greater seabed mobility, and the eddy viscosity is increased by an order of magnitude indicating enhanced water column mixing. This research provides some valuable insight as OWFs expand into deeper seasonally stratified waters using floating structures, where the addition of enhanced wake turbulence may have broad impacts as the additional mixing energy is added to regions with low rates of background mixing.

1 Introduction

There is growing interest in tidal flow past offshore wind turbine foundations and the impact of the associated wake on the environment through seabed sediment scour, water column mixing and the resultant ecological impacts (e.g., Chambel et al., 2024; Schultze et al., 2020; Dannheim et al., 2020). This is being driven by the planned massive expansion in offshore wind generation over the coming decade in the drive for Net Zero energy production. In northwest European waters (EU+UK) there were 45 GW of operational offshore wind in 2023, which is planned to increase to 110 GW by 2030 as large arrays of turbines are being installed in increasingly deep waters (TCE, 2022; European Commission, Directorate-General for Energy, 2023).

In a natural tidal flow, small-scale turbulent eddies generate strong velocity gradients (shear) close to the seabed that impart a high stress onto the bed. Moving away from the seabed, the scale of the turbulent eddies mediating the transfer of momentum increases, which reduces the velocity gradients and results in correspondingly smaller stresses; this leads to the law-of-the-wall benthic boundary layer. Turbine foundations add barotropic drag to the tidal flow, creating a deficit in the mean velocity and forming a vortex wake that generates additional turbulence at the scale of the monopile. In shallow waters the wake turbulence can directly impact the seabed and enhance the stresses, which may in turn modify seabed morphology (Couldey et al., 2020), sediment composition (McCarron et al., 2019) and impact benthic ecological communities (Damveld et al., 2018). The
persistence of the wake depends on the level of background turbulence, with wakes being efficiently eroded in highly turbulent environments (i.e. shallow and tidally energetic).

In lower energy deeper waters where stratification may occur, and particularly with the transition to deep-draft floating foundations, the combination of barotropic and baroclinic drag may significantly affect the water column by directly adding turbulent energy to the pycnocline. The addition of wake turbulence to these lower energy deeper environments will likely lead to more persistent regions of enhanced turbulent mixing (Dorrell et al., 2022); at the array scale, this may effect seasonal stratification (Schultze et al., 2020) cause cumulative ecological impacts (Isaksson et al., 2023).

The aim of this paper is to investigate how the signature of the turbulent wake from an offshore wind turbine monopile differs from that of the background flow. Specific objectives are to quantify the changes to: (1) the rate of turbulence dissipation and production measured inside and outside the wake; (2) their vertical distribution through the water column; and (3) to assess the potential impact of the wake on seabed stress and water column mixing. We use field observations in a tidally energetic well-mixed environment and through the precise deployment of instruments 40 m from a fixed seabed monopile, measure natural background flows during the flood tide but sample directly within the wake during the ebb.

2 Location and Methods

2.1 Field Site

Observations were made $x = 41$ m northwest of a $D = 4.7$ m diameter monopile of the Rhyl Flats OWF in Liverpool Bay, UK (454337.8 mE, 5915789.1 mN, UTM30U); this equates to a distance $x/D$ of 8.7 (Fig. 1). The location was selected so that during the flood tide it was upstream of the monopile and experienced natural background flows, whereas during the ebb it was downstream of the monopile within the wake. The site has a semi-diurnal macro-tidal regime and during the observations, the water depth varied between 12.5 m and 21 m on peak spring tides. The depth-averaged flow velocities confirm the rectilinear nature of the tidal flows (Fig. 1). The dominant easterly component of the flood peaked at 0.8 m s$^{-1}$; the ebb tides were weaker, reaching -0.6 m s$^{-1}$, and show greater scatter as also observed at a nearby location by Unsworth et al. (2023). The cylinder Reynolds number $Re_d$,

$$Re_d = \frac{u_∞ d}{ν}$$

where $u_∞$ is the freestream flow velocity and $ν$ the kinematic viscosity, was $O(10^4 − 10^6)$, for the range of observed depth-averaged flood tide velocities (Fig. 1; inset). The transition to the turbulent critical flow regime begins at $Re_d \gtrsim 2 × 10^5$ (equating to a minimum velocity of 0.06 m s$^{-1}$), so a turbulent Karman vortex (KV) wake was expected in the lee of the monopile for the majority of the survey. The seabed was composed of rippled sand ($d_{50} = 0.25$ mm) resulting in a roughness height $k_b = 0.122$ m.

Direct measurements of the wave field were obtained from the nearby Rhyl Flats wave buoy (459857.5 mE, 5914935.9 mN, UTM30U; Channel Coastal Observatory (2022)). The wave height and period were typically less than $H_s = 1$ m and $T_z = 4$ s, respectively, but peaked at $H_s = 1.5$ m and $T_z = 4.5$ s, during 15 – 16 Sep. In this shallow, tidally energetic, region the water
Figure 1. Field setting of the observations. (a) Bathymetry showing the Rhyl Flats OWF (UKHO, 2024). (Inset) zoomed bathymetry showing the monopile, rock scour protection, ADCP location (red triangle), and indicating the flood tide direction. (b) Depth-averaged east and north tidal current velocities (black); also plotted (grey) are velocities from 3 km to the south west (grey triangle in (a)), away from the influence of the OWF (Unsworth et al., 2023). (Inset) Histogram of cylinder Reynolds number $Re_d$, showing the transition to a turbulent boundary layer around the monopile and asymmetric KV wake (dashed), and the super-critical transition to a symmetric wake (dot-dash).
column generally remains well-mixed. No profiles of water temperatures were recorded, but time series of surface and bottom temperatures recorded nearby during 2018 indicate that thermal stratification only occurs over neap tides during Jun – Jul.

### 2.2 Observational Setup

A Nortek Signature 1000 5-beam ADCP was installed on a bed-mounted frame and profiled the water column within 44 bins of 0.5 m thickness; the centre of the lowest bin was at \( z = 0.8 \) m above the seabed. The instrument heading was 220°, with the plane of beams 2 and 4 aligned with the streamwise current; pitch and roll were -0.5° and 5.3°, respectively. The ADCP recorded along-beam velocities with a ping rate of 8 Hz and operated in burst mode collecting 2048 samples at the start of each hour. The Doppler noise level was reported as \( \sigma_N = 0.016 \) m s\(^{-1}\).

### 2.3 Turbulence Metrics

The TKE dissipation rate was estimated from the along-beam velocities of the vertical fifth beam of the ADCP \( (\varepsilon_5) \) using the Structure Function method (Wiles et al., 2006). In the presence of surface gravity waves, the vertical gradient in wave orbital velocity will bias the along-beam velocities, and we use the modified approach of Scannell et al. (2017) to remove this bias \( (A3) \).

The Reynolds stresses were estimated using the variance method (Lu and Lueck, 1999; Rippeth et al., 2003), extended by Dewey and Stringer (2007) for a five-beam ADCP and including non-zero pitch and roll. The fifth beam provides an independent measure of the vertical velocity \( w \), and allows the stress components to be estimated with a reduced bias because the approximation due to the orthogonal beam is removed. The coordinate system was rotated to provide the streamwise \( (u'w') \), cross-stream \( (v'w') \) and vertical stresses \( (w'w') \).

In a well-mixed tidally dominated environment, TKE production \( P \) is primarily through energy transfer from the mean flow to turbulence via shear at the seabed; the buoyancy term can be neglected. \( P \) was estimated from the Reynolds stresses and the mean velocity vertical shear (e.g., Rippeth et al., 2003).

### 3 Results

#### 3.1 Variation in Rates of Turbulence Dissipation and Production

The principal environmental parameters observed adjacent to the monopile are shown in Fig. 2. The profile of the mean streamwise velocity \( U_x \) (Fig. 2a) indicates that the semi-diurnal tidal wave is standing and exhibits strong semi-diurnal and spring-neap variation. The largest velocities are observed on the peak spring tides \( (\pm 0.8 \) m s\(^{-1}\)), reducing to \( \pm 0.35 \) m s\(^{-1}\) during neaps.

The TKE dissipation rate \( \varepsilon_5 \) (Fig. 2b) has both a spring-neap and a pronounced quarter diurnal variation. During the flood, maximum values of \( \varepsilon_5 \) are \(-4.5 \log_{10}(W \text{ kg}^{-1})\) during springs and \(-5 \log_{10}(W \text{ kg}^{-1})\) during neaps. In contrast, maximum \( \varepsilon_5 \)
Figure 2. Overview of observations during the survey. (a) Streamwise mean velocity $U_x$; (b) $\varepsilon$; (c) $P$; and (d) significant wave height $H_s$ (black) and period $T_z$ (red). The water surface elevation is shown by the black line in (a–c). The white band at $z < 2$ m in (b) is due to the minimum of four bins for the regression of $D(z,r)$ against $r^{2/3}$ in (A3). The horizontal black bar above each panel highlights the period shown in Fig. 3.
during the ebb increases by almost an order of magnitude during springs (-3.7 log10(W kg−1)) and half an order of magnitude during neaps. During spring tides, significant levels of ε5 is observed to occur through the full depth of the water column.

The TKE production rate P (Fig. 2c) follows a similar temporal pattern to ε5. During both phases of the tide, strong production (-4.5 log10(W kg−1)) consistent with shear at the seabed extends up to z ≈ 3 m above the bed, but during the ebb, an additional vertical band of strong P is present through the full water column. At several times throughout the survey (e.g., 15 – 19 Sep), intense regions (> -4 log10(W kg−1)) of near-surface P occur, which propagate downwards into the water column to z = 10 m. Comparing these periods to the surface waves recorded at the nearby wave buoy (Fig. 2d), steep waves (Hs = 1.5m, Tz = 4 s) are likely injecting TKE directly into the surface layers and contributing to P. This wave contamination is not observed in ε5 due to our use of the modified structure function (A3).

3.2 Wake-modified Vertical Distribution of Turbulence

To provide further insight into the distribution of turbulence in the water column and to identify the balance between seabed and water column processes, we explore three spring tidal cycles in greater detail and compare with theoretical scaling. Fig. 3(a) plots ε5 and highlights significant flood-ebb asymmetry in the strength and spatial distribution of ε5. During the upstream (flood) phase, ε5 appears to be forced at the seabed and propagates vertically toward the surface as the flow accelerates before weakening prior to high water slack. In contrast, during the downstream (ebb) phase, high ε5 persists through the full water depth with maximum values observed in the upper water column. This flood ebb asymmetry is not attributable to tidal straining or convection, because of the well-mixed nature of the environment. In Fig. 3(b) we integrate ε5 across 2 m-thick bands of the water column close to the seabed and near the sea surface, and through the full water column. All three display a quarter-diurnal variation in ε5, but contrasting behaviour is seen at the seabed and near surface during upstream and downstream phases. During the upstream phase, ε5 at the seabed exceeds that near the surface, but during the downstream phase this pattern is reversed and the difference between them is approximately twice as large. Integrating through the full depth of the water column, ε5 is approaching an order of magnitude greater during the downstream phase. We do note that ε5 is possibly under-estimated at the seabed, since due to the requirement of a minimum of four bins for the regression in (A3), the lower 2 m is excluded.

Following similarity theory, a local balance should exist between ε and P based on a constant stress relationship. This leads to a scaling factor εs = −u∗3/κz, where u∗ is the friction velocity, calculated as u∗ = (τb/ρ)1/2 for bottom shear stress τb and seawater density ρ = 1027 kg m−3; κ is the von Karman constant (= 0.41). Here we use the method of Soulsby and Clarke (2005) to compute the current only τb,c with the measured bottom roughness length-scale accounting for both bedform and skin friction roughness. During upstream phase (Fig. 3c) ε5 close to the seabed is in almost perfect balance with similarity theory, but at the surface is approximately 20% higher. During downstream conditions, ε5 is one and 1.5 orders of magnitude greater than predicted at the seabed and near-surface, respectively, and peaks prior to the occurrence of the strongest flows (mid-ebb). The similarity scaling breaks-down at slack water as ε5 is maintained despite the cessation of local production from the mean flow.

A flood-ebb asymmetry of P is clearly shown in Fig. 3(d), which shows a consistent near-bed TKE production on both upstream and downstream flow phases and a strong production throughout the full water column during the downstream phase.
Figure 3. Vertical water column distribution of turbulence dissipation and production rate. (a) dissipation rate $\varepsilon_5$; (b) seabed (black), near-surface (blue) and total (red) dissipation rate $\varepsilon_5$; (c) similarity scaling of dissipation rate $\varepsilon_5$ at seabed (black), near-surface (blue), and total observed ratio $\varepsilon_5 / P$ (red); (d) turbulence production $P$; (e) seabed (black), near-surface (blue) and total (red) turbulence production $P$; and (f) mean streamwise velocity $U_x$. Vertical dashed lines highlight equivalent mid-tide upstream (flood) and downstream (ebb) periods.
Integrating $P$ into vertical zones also shows the asymmetric flood/ebb behaviour, with greater downstream TKE production ($P = -3.5 \log_{10}(W \text{ kg}^{-1})$) compared to during upstream conditions ($P = -4.5 \log_{10}(W \text{ kg}^{-1})$). The difference between seabed and near-surface $P$ is more variable, but overall we observe a trend of greater seabed production during upstream flows and greater near-surface production during downstream flows. When integrated through the full water column, $P$ and $\varepsilon_5$ are in close agreement in magnitude and trend, and the observed budget $\varepsilon_5/P$ remains within an order of magnitude (Fig. 3(c), red line).

The mean streamwise velocity $U_x$ highlights the clear differences between the background upstream flood-tide flows and the downstream wake-effected ebb (Fig. 3(f)). During the upstream phase the characteristic tidal benthic boundary layer structure is evident with the strongest flows at the surface, which reduce towards the bed developing shear. During the downstream phase the velocity magnitude is reduced by approximately 35% with the strongest flows occurring at mid-depth and shear developing close to the bed. In the upper water column, a significant velocity deficit indicates the presence of the monopile wake and is in-phase with the peaks in $\varepsilon_5$ and $P$.

### 3.3 Enhanced Reynolds Stress, Seabed Drag and Mixing

To provide insight into the effect of the monopile wake through the water column we compute ensemble-averaged vertical profiles of mean velocity, stress and TKE dissipation rate (Fig. 4). Vertical profiles at mid-flood and mid-ebb, when flow accelerations are expected to be minimal, were extracted from the seven spring tides between 9 and 13 Sep and geometrically averaged in $z/h$-space to account for tidal changes in water depth. During the upstream phase (flood), the mean velocity profile displays the expected logarithmic form and extends the full thickness of the water column. As expected, the maximum values of the stress occur at or just above the seabed and tend towards zero at the surface (Rippeth et al., 2002). An increase in stress is observed for $z/h > 0.65$, which may be due to surface waves. Following Rippeth et al. (2003), for our observed wave amplitude and period of $\sim 0.5$ m and $\sim 4$ s, respectively, we may expect a bias in the stress term close to the surface of $\sim O(0.5)$ N m$^{-2}$ decreasing with depth to $\sim O(0.05)$ N m$^{-2}$ at the bed.

During the downstream wake-affected ebb tide, a strong velocity deficit is present above $z/h > 0.5$, indicative of the core of the wake. The stress increases from minimum values near the seabed to extreme values at the surface, but there is also a region of highly variable stress at $0.1 \leq z/h \leq 0.3$. It is noteworthy that for equivalent stages of the tide, whilst the downstream velocities are significantly weaker than during the upstream phase, the stresses are up to six times larger; this far exceeds the potential bias in the stress terms due to surface waves.

The profiles of $\varepsilon_5$ display a similar upstream-downstream asymmetry to the stresses (Fig. 4(c)). Peak $\varepsilon_5$ values occur during the downstream phase, with extreme values ($-3.5 \log_{10}(W \text{ kg}^{-1})$) at $z/h = 0.25$ and above mid-depth $z/h > 0.50$. Again, despite the stronger upstream velocities, $\varepsilon_5$ is almost an order of magnitude weaker during the upstream phase, which display maximum values close to the seabed and decrease linearly to the surface.

Stress at the seabed is often parameterised using the drag coefficient $C_d$, and the quadratic stress law $\tau_b = \rho C_d U^2$, to relate the flow speed $U$ defined at some elevation above the seabed (often $z = 1$ m for sediment transport studies) directly to the turbulent stress. We compare the total shear stress $\tau = -\rho \sqrt{u'w'^2 + v'w'^2}$, averaged over the lowest 2 m of the water column,
Figure 4. Summary of stress and drag. Peak upstream (black) and downstream (blue) ensemble-averaged (a) mean streamwise velocity profiles $\overline{U_z}$; (b) Reynolds stress $\overline{-\rho u'w'}$; and (c) dissipation rate $\varepsilon_5$. Shaded regions plot ± standard deviation. (d) Comparison of the Reynolds stress estimates with the quadratic drag law during upstream (black) and downstream (blue) periods. The Reynolds stress averaged over the four bins closest to the bed ($z = 0.8 - 2.3$ m) is plotted against $-\rho |U|U$, where $U$ is the mean current speed at $z = 1$ m, and the drag coefficient $C_d$ is evaluated by linear fitting. (e) Non-dimensional eddy viscosity $N'_z$ (where $N'_z = N_z/\kappa u_* h$) for ensemble-averaged upstream and downstream phases compared to the steady-flow model (solid line).
with the quadratic stress law evaluated at $z = 1$ m above the bed (Fig. 4(d)). Upstream (flood) and downstream (ebb) data are independently fitted to a straight line (both with $R^2 \sim 0.7$ and $\sim 270$ degrees of freedom) with significantly different slopes. This yields an downstream ebb drag coefficient of $C_{d,e} = 7.8 \times 10^{-3}$, twice that observed during the upstream flood phase ($C_{d,f} = 3.5 \times 10^{-3}$).

The eddy viscosity $N_z$ relates the vertical velocity gradients to the horizontal stress and reflects the role of turbulent eddies in mediating the transfer of momentum. If we assume a steady flow model where the velocity shear $\partial u/\partial z = u_*/\kappa z$, and the stress decreases linearly from its maximum value at the bed $\tau_b = -\rho u_*^2$, to zero at the surface, $N_z$ takes a parabolic form (Rippeth et al., 2002). We compare $N_z$ computed for the ensemble-averaged peak upstream and downstream tidal phases, and although there is some significant deviation approaching the sea surface, during the upstream phase the observations are consistent with the steady-flow model (Fig. 4(e)). During the wake-effected ebb tide, $N_z$ is approaching an order of magnitude larger and although approximating a parabolic form at $z/h < 0.5$, it rapidly increases in the upper water column where we observe the strong deficit in the mean velocity.

4 Discussion

4.1 Wake Enhanced Turbulence

The present study utilises high-frequency 5-beam ADCP data to provide turbulence metrics over multiple tidal cycles within the wake 40 m away from an offshore wind turbine monopile. Observations of the TKE dissipation rate and Reynolds stresses have been combined with the mean velocity shear to provide new insight into the changes to the vertical structure of the water column inside and outside of the wake. Upstream of the monopile, these parameters generally accord to a classical depth-limited law-of-the-wall boundary layer with peak values of mean velocity shear and stress close to the bed, and correspondingly high rates of TKE production and dissipation that are balanced at the seabed (Fig. 3). The reduction in $\varepsilon_5$ moving away from the seabed indicates that the Kolmogorov length scale ($\nu^3/\varepsilon_5)^{1/4}$, and thus the size of the energy containing eddies, is increasing as a function of $\kappa z$. Downstream of the monopile within the wake, a strong velocity deficit forms in the upper half of the water column, which is accompanied by a significant elevation in the production and dissipation of TKE (Fig. 3) that deviates from theoretical similarity scaling, and enhanced stress throughout the full depth. We have further tested the impact of these wake-generated variations on the seabed and on the water column mixing by estimating changes to the drag coefficient and the eddy viscosity, respectively.

The monopile spans the full depth of the water column and extracts momentum from the mean flow, which is transferred to TKE at a (large) scale similar to that of the monopile itself (4.7 m); this leads to the observed velocity deficit in the wake that advects downstream in a self-similar manner. In the present ebb tide data we observe that the velocity deficit is largely eliminated in the lower half of the water column ($z/h \leq 0.5$). This indicates that the high levels of shear and stress measured close to the bed, which result from the combination of natural small-scale eddy interactions and the additional TKE introduced by the monopile itself (Fig. 4), provide an important restorative mechanism for the mean flow by eroding the wake (Eames...
et al., 2011). Further support for this argument is provided by the high rate of TKE dissipation $\varepsilon_5$ also observed close to the bed.

Higher in the water column the velocity deficit is maintained due to a reduction in the efficiency of the ambient flow to erode the wake. First, the difference between the ambient flow and the velocity deficit is much greater due to the reduction in frictional drag from the seabed, and so the work required to restore the mean flow near the surface is therefore much greater. Second, we expect a decrease in the ambient shear and stress as the eddy length scale increases in proportion to $\kappa z$ to also reduce the rate at which the wake is eroded. The combination of these factors plus the continued addition of TKE from the deficit (Scott et al., 2023) leads to the maintenance of a region of elevated shear above $z/h = 0.5$ that is associated with very high stress, and $\varepsilon_5$, which is maximised at $0.5 \leq z/h \leq 0.7$.

### 4.2 Implications of Enhanced Seabed Drag

We show that the high levels of stress observed in the wake directly increase the drag coefficient at the seabed. $C_{d,f} = 3.5 \times 10^{-3}$ outside of the wake, which is comparable to standard values reported for sandy and sand-gravel seabed mixtures (e.g., Soulsby, 1998), but this more than doubled to $C_{d,e} = 7.8 \times 10^{-3}$ within the wake. Unless this wake-enhanced drag is accounted for, shelf-scale models (e.g., Telemac, FVCOM) that generally use the quadratic stress law as the default method of estimating bed shear stress will under predict seabed stress even if they include monopiles as point drag sources. The elevated $C_d$ within the wake can be directly linked to enhanced sediment transport and observations of morphological change in the lee of monopiles. Wakes can modify the seabed, flattening bedforms by forcing a change towards an upper-stage plane bed regime as observed at Rhyl Flats OWF downstream of the monopile (Fig. 1), and in extreme cases causing seabed scour, or can force a live-bed regime to transition towards one that supports bedform development (Couldrey et al., 2020). At the array-scale, wake formation will increase the spatial variability of the seabed morphology, change grain size mixtures, and likely promote greater seabed heterogeneity and impact the make-up and functionality of the benthic ecosystem (van der Kooij et al., 2008; Gates et al., 2019).

### 4.3 Implications of Enhanced Eddy Viscosity

The wake enhances water column mixing by modifying the local momentum flux, and the eddy viscosity provides a useful concept for estimating wake mixing efficiency and persistence by directly relating the mean flow gradients to the turbulent stresses. The magnitude of the eddy viscosity $N_z$ is controlled by the interplay between the mean flow shear, the rate of recovery of the velocity deficit, and the dissipation rate $\varepsilon_5$. In the present data, the ADCP is located at $x/D = 8.7$, which is sufficiently far downstream of the monopile that the velocity deficit is recovering and close to the seabed, where strong frictional drag and high $\varepsilon_5$ occur, $N_z$ is reduced. However, higher in the water column where the velocity deficit remains significant the rate of transfer of momentum to TKE remains high relative to $\varepsilon_5$, and strong Reynolds stresses are still generated maximising $N_z$ (Fig. 4). As the velocity deficit continues to weaken moving downstream we would expect $N_z$ to decrease as $\varepsilon_5$ drives the decay of the Reynolds stresses (Scott et al., 2023). The complex distribution of $N_z$ through the wake-effected water column has significant implications for the inclusion of OWF turbulent wakes in large-scale shelf-sea models. The turbulence is sub-grid
scale in these models, and the mixing processes are passed to some form of generic turbulence closure model, which attempts to balance the production and dissipation of TKE and return this as an $N_z$. In light of the many length scales introduced by the structures, robust datasets and fully resolved model simulations are first required to provide further insight into the physics of flow past structures, particularly in stratified regions.

4.4 Broader Consequences of Enhanced Mixing

The observed order of magnitude increase in mixing caused by the monopile is likely to have significant implications for the transition towards floating OWF in deeper seasonally stratified waters (Dorrell et al., 2022). In these regions, background mixing rates are low because the pycnocline isolates the surface from the bottom waters, which limits the flux of nutrients and oxygen that drive primary productivity (Sharples et al., 2001). The addition of the high level of anthropogenic mixing caused by tidal flow past OWF structures to the stratified regions will result in a large relative increase in mixing compared to the background levels, potentially affecting the timing of the onset and breakdown of seasonal stratification (Rippeth, 2005), the strength of the stratification (Schultze et al., 2020), and the mixed-layer depth (Pearson et al., 2015), combined this could result in significant ecological impacts spanning multiple trophic levels from plankton to fish to top predators (Trifonova and Scott, 2023).

5 Conclusions

High-frequency velocity measurements are used to quantify the turbulent vortex wake 40 m downstream of an OWF monopile in a tidally energetic environment. We take advantage of the rectilinear tidal flow to compare the natural background upstream flow during the flood tides with the wake-affected downstream flow during the ebb. The rates of turbulence production and dissipation are driven by tidal shear at the seabed during background flow conditions and reach $-4.5 \log_{10}(W \text{ kg}^{-1})$. Within the wake a strong mean flow velocity deficit develops, which drives enhanced dissipation and production of $-3.5 \log_{10}(W \text{ kg}^{-1})$ through the full depth of the water column. Reynolds stresses are also enhanced within the wake. This doubles the seabed drag coefficient from $C_d = 3.5 \times 10^{-3}$ to $C_d = 7.8 \times 10^{-3}$ and implies that seabed mobility will increase resulting in greater seabed heterogeneity. Enhanced stresses also increase the eddy viscosity by an order of magnitude, which will drive greater vertical water column mixing. These results provide useful insight as OWF developments progress into deeper often seasonally stratified waters, where the addition of extra turbulent energy into the water column may alter the present delicate balances and result in widespread ecosystem impact. Future work should focus on the generic parameterisation of wake turbulence into the shelf-scale numerical models required for planning and impact mitigation purposes.
Appendix A: TKE Dissipation Rate

The TKE dissipation rate $\varepsilon$ was derived from the ADCP velocity measurements using the Structure Function method (Wiles et al., 2006). Along-beam velocity components $b(z)$ from each beam are used to estimate the second-order structure function:

$$D(z, r) = \left( b'(z) - b'(z + r) \right)^2$$  \hspace{1cm} (A1)

where the overbar is the burst-average, $b' = b(z) - \overline{b}(z)$ is the fluctuating component of velocity at position $z$ along the beam and $D(z, r)$ is the mean-square of the velocity fluctuation difference between two points separated by distance $r$, based on multiples of the bin size. The maximum separation distance $r_{max}$ was set as 3 m. For isotropic turbulence, the structure function $D(z, r)$ is related to $\varepsilon$ by:

$$D(z, r) = C_2 \varepsilon^{2/3} r^{2/3},$$  \hspace{1cm} (A2)

where $C_2$ is a constant (=2.0). In the presence of surface gravity waves, the vertical gradient in wave orbital velocity will bias the along-beam velocities. We use the modified approach of Scannell et al. (2017) to remove this bias, using a least-squares fit to generate a linear model:

$$D(z, r) = a_0 + a_1 r^{2/3} + a_3 (r^{2/3})^3$$  \hspace{1cm} (A3)

where $a_3$ contains the contribution to $D(z, r)$ from the waves, $a_0 = 2\sigma^2$ provides an estimate of the instrument noise, and the gradient $a_1$ is used to derive $\varepsilon$ via:

$$\varepsilon = \left( \frac{a_1}{C_2} \right)^{2/3}. $$  \hspace{1cm} (A4)

Here, we estimate the dissipation rate from the vertical fifth beam of the ADCP ($\varepsilon_5$).

Author contributions. All authors designed the experiment. MJA and CAU performed the initial data post-processing, MJA undertook the analysis and visualisation of the data, and BJL helped with the structure function analysis. MJA prepared the initial manuscript and all authors contributed to its development.

Competing interests. The authors declare no competing interests.

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References


