An elucidatory model of oxygen's partial pressure inside substomatal cavities

Andrew S: Kowalski[1,2]

[1]Department of Applied Physics, University of Granada, Granada, 18071, Spain
[2]Andalusian Institute for Earth System Research (IISTA), Granada, 18071, Spain

Correspondence to: Andrew S: Kowalski (andyk@ugr.es)

Abstract. A parsimonious model based on Dalton's law reveals substomatal cavities to be dilute in oxygen (O_2), despite photosynthetic O_2 production. Transpiration elevates the partial pressure of water vapour but counteractively depresses those of dry air's components – proportionally including O_2 – preserving cavity pressurization that is negligible as regards air composition. Suppression of O_2 by humidification overwhelms photosynthetic enrichment, reducing the O_2 molar fraction inside cool/warm leaves by hundreds/thousands of ppm. This elucidates the mechanisms that realize O_2 transport: diffusion cannot account for up-gradient conveyance of O_2 from dilute cavities, through stomata to the more aerobic atmosphere. Rather, leaf O_2 emissions depend on non-diffusive transport via mass flow ~~in the form of "stomatal jets"~~ forced by cavity pressurization, which is not negligible in the context of ~~driving viscous flow~~dynamics. ~~Jet~~ Non-diffusive O_2 expulsion overcomes massive inward O_2 diffusion to force net O_2 emission. At very high leaf temperatures, ~~jets~~ mass flow also influence~~s~~ transport of water vapour and carbon dioxide, physically decoupling their exchanges and reducing water-use efficiency, independent of stomatal regulation.

1 Introduction

~~Plant physiological frameworks appear to have incorrectly described the partial pressures of gases within sub-stomatal cavities, where leaf photosynthesis takes place. That~~ The partial pressure of water vapour (*e*) inside sub-stomatal cavities is well known to be greatly elevated by transpiration, as reflected by the ambient vapour pressure deficit (VPD). However, both the total pressure (*p*) and partial pressures of dry air components such as oxygen (p_{O_2}) have been fixed as parameters independent of plant functioning (e.g., Farquhar and Wong,1984). This oversight~~,~~ neglect~~sing~~ the ~~consequences~~ implications of Dalton's law of partial pressures. Here, a very simple model is presented that accurately estimates p_{O_2}, offering insights into ~~with accuracy that is sufficient to elucidate~~ the mechanisms ~~relevant to~~of stomatal gas transport, which, contrary to long-standing assumption ~~are not exclusively diffusive as has long been supposed~~ (Moss and Rawlins, 1963), are not exclusively diffusive.

2 Physical Law and Theory

Dalton's law of partial pressures,

$$p = e + (p_{N_2} + p_{O_2} + p_{Ar}),\qquad(1)$$

defines p as the sum of e with the partial pressure of dry air, within the parentheses, which in turn is the sum of the partial
35 pressures of nitrogen (N_2), O_2 and argon (Ar), neglecting gases with mere trace contributions. Equation (1) can be expressed
for both the substomatal cavity interior (i),

$$p_i = e_i + (p_{i,N_2} + p_{i,O_2} + p_{i,Ar}),\qquad(2)$$

as well as for the ambient atmosphere (a) outside the leaf,

$$p_a = e_a + (p_{a,N_2} + p_{a,O_2} + p_{a,Ar}).\qquad(3)$$

40 If Δ denotes a cavity surplus versus ambient, subtracting Eq. (3) from Eq. (2) yields

$$\Delta p = \Delta e + (\Delta p_{N_2} + \Delta p_{O_2} + \Delta p_{Ar}),\qquad(4)$$

where Δe quantifies cavity humidification and reflects the ambient VPD. In the context of Eq. (4) for substomatal cavities,
water vapour's substantial surplus ($\Delta e > 0$) implies either cavity pressurization ($\Delta p > 0$), or depressed partial pressures of dry
air's components ($\Delta p_{N_2} + \Delta p_{O_2} + \Delta p_{Ar} < 0$), or a combination of both. Since cavity pressurization would drive mass flow
45 out of the aperture, theoretical considerations from micro-scale fluid dynamics can establish an upper limit for Δp.

Despite the fact that stomata are not cylindrical, the Poiseuille equation derivation (Giancoli, 1984) can be used to show that
Δp negligibly counterbalances Δe in Eq. (4). This is done below by exaggerating the parameters of cylindrical geometry to put
a bound on the Δp required to force viscous flow. The axial velocity v of a laminar flow through a cylinder of length L and
50 radius R is given as

$$v = \frac{\Delta p}{4\eta L} R^2,\qquad(5)$$

where η is air's dynamic viscosity (18 μPa s). Solving for Δp yields

$$\Delta p = \frac{4\eta L v}{R^2}.\qquad(6)$$

Here, parameters are chosen so as to maximize the Δp required to drive viscous flow:

55 • Stomatal dimensions are exaggerated based on Lawson et al. (1998):

- o   Pore depth is overestimated as $L = 10\mu m$,
- o   Stomatal aperture is underestimated using $R = 2$ μm (area ~ 13 μm^2);

- An air velocity of $v = 6$ mm s^{-1} escaping the stomatal aperture (Kowalski, 2017) represents an upper bound in the sense that ~~plant physiologists have~~traditional plant physiological models assume~~d~~ all transport to be diffusive, with no relevant role played by mass flow, effectively assuming a null value of v.

Plugging these values into Eq. (6) results in $\Delta p = 0.0011$ kPa, indicating that a very slight pressure difference is required to drive viscous flow. Given this, in the context of Eq. (4) regarding air composition and with resolution sufficient to characterize the VPD (to +/- 0.01 kPa), we can neglect substomatal pressurization in Eq. (4), taking $\Delta p = 0$. This means that any increase in the cavity's Δe forced by transpiration must be counterbalanced by a reduction in the partial pressure of dry air ($\Delta p_{N_2} + \Delta p_{O_2} + \Delta p_{Ar} < 0$).

3 The Model

With transpired water vapour supplanting substomatal dry air, the simplest model is proportional depression of the partial pressures of dry air's components. In light of the Ideal Gas Law this implies that, for every 1000 dry air molecules displaced by water vapour, we can expect N_2 : O_2 : Ar proportions of 781 : 210 : 9. Therefore O_2's partial pressure inside substomatal cavities is modelled succinctly by

$$-\Delta p_{O_2} = 0.210 \cdot \Delta e, \tag{7}$$

indicating O_2 depression (versus ambient) that is 21% of the vapour pressure surplus of the substomatal cavity, or about 21% of the environmental VPD.

4 Model Implications, ~~Uncertainties~~Accuracy, and Relevance to Other Gases

Oxygen deficits prevail within substomatal cavities because photosynthetic enrichment (μmol m^{-2} s^{-1}) of O_2 is vastly overwhelmed by O_2 dilution and displacement due to transpiration (mmol m^{-2} s^{-1}). Oxygen represents a sizeable fraction (about one-fifth) of ambient air but a far smaller fraction of leaf gas emissions, which are nearly pure water vapour and so dilute O_2 to force hypoxic conditions inside substomatal cavities. The degree of O_2 depression depends strongly on the VPD, and therefore leaf temperature (T), as illustrated by representative examples of cool and warm leaves (Table 1). Notably, even the cool leaf has a significant O_2 pressure deficit of $-\Delta p_{O_2} = 0.066$ kPa. "Near sea level" (defined hereinafter as $p = 100$ kPa), this corresponds to an O_2 molar fraction (referencing moist air) that is 660 ppm below ambient. In warm leaves O_2 depression reaches several thousand ppm, and in torrid environments it can be far greater.

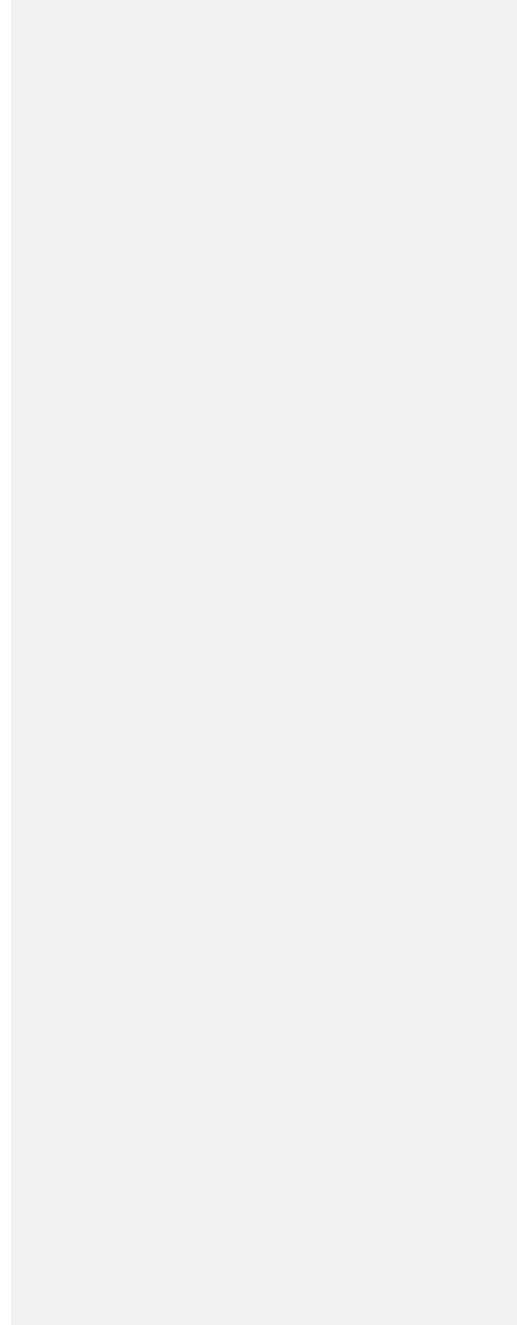
Con formato: Sin subrayado

	Cool	**Warm**
T_{leaf}	10ºC	34 ºC
T_{air}	8ºC	30 ºC
e_{leaf}	1.228 kPa	5.325 kPa
e_{air}	0.912 kPa	3.610 kPa
Δe	0.316 kPa	1.715 kPa
$-\Delta p_{O_2}$	0.066 kPa	0.359 kPa
$-\Delta \chi_{O_2}$	660 ppm	3590 ppm

Table 1: Consequences of negligible stomatal-cavity pressurization regarding air composition. Representative temperatures, water vapour pressures, stomatal cavity vapour pressure surplus (Δe), oxygen pressure deficits ($-\Delta p_{O_2}$), and oxygen concentration deficits ($-\Delta \chi_{O_2}$) for cool and warm leaves and their ambient atmospheres. Leaves are taken as saturated and ambient air at 85% relative humidity; $-\Delta p_{O_2}$ is calculated using Eq. (7); $-\Delta \chi_{O_2}$ is calculated for conditions "near sea level" ($p = 100$ kPa).

The most noteworthy inference from this Daltonian model regards the mechanisms of gas transport through stomata, since O_2 produced by photosynthesis cannot diffuse out of stomata as has been traditionally assumed (Parkhurst, 1994). Equation (7) implies that substomatal cavities are generally much more dilute in O_2 than their environments, whatever the leaf T. Although current traditional thinking in plant physiology would explain O_2 transport in terms of diffusive flows within a ternary system (Jarman, 1974; von Caemmerer and Farquhar, 1981), diffusive transport from dilute towards enriched regions is impossible – it would violate the 2nd Law of Thermodynamics. Rather, non-diffusive transport by the viscous flow – driven by pressurization that is negligible in the context of Eq. (4) but nonzero nonetheless – is required to overcome inward O_2 diffusion and drive O_2 out of substomatal cavities. Diffusion of O_2 into substomatal cavities is massive, due to concentration differences of hundreds or thousands of ppm across the leaf's pore depth. Gradients and diffusion of O_2 exceed those of CO_2 by orders of magnitude.

However simplistic, the model improves upon the accuracy of previous assumptions regarding substomatal p_{O_2} that neglected Dalton's law. These include the assumption that p_{O_2} is a fixed parameter that does not depend substantially on plant functioning (Farquhar and Wong, 1984), as well as the notion that substomatal cavities are enriched in O_2 (Parkhurst, 1994), purporting outward O_2 diffusion while overlooking the dominant effects of transpiration on O_2 abundance. The greatest inaccuracies of the Daltonian model presented here can be bounded by considering the chief processes that it does not take into account.

Adhering to the principle of parsimony, the model neglects the effects of two lesser and partially offsetting influences on p_{O_2}, neither of which can alter the above conclusion regarding O_2 transport mechanisms. Firstly, photosynthetic O_2 production must reduce the O_2 pressure deficit, increasing substomatal O_2 somewhat, but certainly not by the many hundreds of ppm (or

thousands for warm leaves) that would be required to make Δp_{O_2} positive. This seems clear when recalling the stoichiometric relation between O_2 and CO_2, and the trace amounts of the latter gas that limit the possible magnitude of photosynthetic Δp_{CO_2}. Secondly, molecular diffusion's discrimination among dry-air species must increase the O_2 deficit since N_2 (28 g mol^{-1}), representing 78.1% of atmospheric dry air molecules, diffuses upstream into substomatal cavities more rapidly than does O_2 (32 g mol^{-1}) according to Graham's law. Unaffected by these inaccuracies, the deduction that substomatal cavities generally are very dilute in O_2 is ineluctable, as is the conclusion that stomatal O_2 transport is predominantly non-diffusive. Specifically, it is due to ~~an air jet~~ a mass flow that indiscriminately pushes all gases outwards (Kowalski, 2017). Although previously couched in terms of "stomatal jets", this is a low-velocity, viscous flow (low Reynolds number) whose conveyance neither discriminates among gas species nor depends on concentration gradients, unlike diffusion. Its relevance to the transport of other gases depends on air's state conditions within stomata.

At very high leaf T, these implications from gas physics become relevant to the behaviour of CO_2 and water vapour.

Regarding CO_2, non-diffusive transport cannot be neglected universally~~, since it neither discriminates among gas species nor depends on concentration gradients, unlike diffusion~~. The p_{O_2} model presented here is not valid for estimating p_{CO_2}, whose fluctuations are principally determined by photosynthesis. However, independent of photosynthetic drawdown (well, physically independent), the assumption of proportional depression of the partial pressures of dry air's components when supplanted by water vapour seems valid. Accordingly, just as Eq. (7) apportions 21% of supplanted dry air to O_2 depression, for a CO_2 concentration of 420 ppm we can expect 0.042% of the dry-air depression described by Eq. (4) to correspond to p_{CO_2}. This influence is negligible for temperate leaves with modest VPDs. For example, for the cool leaf in Table 1, it implies CO_2 depression of ~0.0001 kPa; near sea level, this is about 1 ppm and pales in comparison to photosynthetic drawdown. By contrast, for the warm leaf also near sea level, it means substomatal CO_2 depression by over 7 ppm, which is no longer negligible and drives inward CO_2 diffusion that is not due to photosynthesis. During heat waves, with extreme values of VPD, substomatal CO_2 depression due to humidification can be much larger. Thus, at very high leaf T non-diffusive transport can appreciably suppress photosynthesis via CO_2 limitation, but it has the opposite effect on transpiration.

Water vapour is also forced out of stomata by non-discriminating ~~jets~~mass flow, with relevance that depends on water vapour abundance. Applying Newtonian physics to the momentum of air within stomata, Kowalski (2017) showed that the water vapour mass fraction, or specific humidity (q), defines the fraction of water vapour transport that is non-diffusive. Within substomatal cavities that are essentially saturated, the state variable q is largely determined by T. For the cool leaf in Table 1 ($q < 1\%$), non-diffusive transport can reasonably be neglected. But this is not so for the warm leaf ($q > 3\%$), and furthermore q increases rapidly as leaf T rises. If these increases in water vapour transport rates seem modest, versus what can be achieved

by diffusion alone, they grow in importance when considered in combination with reduced ~~jet suppression of~~ photosynthesis via suppression of sub-stomatal p_{CO_2} by Δe as described above.

The consequences of gas physics at high leaf T are disparate for water vapour and CO_2 exchanges. Ejecting all gases, ~~stomatal jets~~mass flow enhances water-vapour loss and opposes CO_2 ingress, boosting transpiration and suppressing photosynthesis versus the capabilities of diffusive transport alone. ~~They~~ It thereby reduces water-use efficiency via effects on each gas. ~~Thus far, the derivation of non-diffusive transport by stomatal jets has been little heeded by scientists who study leaf gas exchanges (De Kauwe et al., 2019; Vesala, 2024). However~~Therefore, dry-air depression and non-diffusive transport likely explain the decoupling of transpiration and photosynthesis that has been observed widely at very high leaf T (Aparecido et al., 2020; De Kauwe et al., 2019; Diao et al., 2024; Krich et al 2022; Marchin et al., 2023; Pankasem et al., 2024; Sun et al., 2024). In very hot substomatal cavities where water vapour is not a mere trace gas, ~~jet~~ transport due to mass flow casts doubt on the very meaning of stomatal conductance. And non-diffusive transport is gaining in relevance regarding leaf gas exchanges as the Earth warms and heatwaves increase in frequency and intensity (IPCC, 2021).

5 Prospects for Unveiling Stomatal Fluid Mechanics

Evaporation within a moist cavity and vapour egress through a small aperture aptly describes not only leaf gas exchanges but also a whistling tea kettle. At the boiling point, a steam jet drives out dry air (including O_2 and CO_2) and the water vapour pressure approaches the total pressure ($e \sim p$). This marks the humid extreme ($q \sim 100\%$) of a spectrum regarding fractional transport by different mechanisms, with the diffusion-only modelling framework valid at the other extreme (dry; $q \sim 0\%$). In state conditions that categorise stomatal air, q is limited to below 10% and non-diffusive transport plays a role that is secondary, although sometimes not negligible. Insight into the consequences of such mass flow might be gained by investigating gas exchanges at intermediate values of q.

Artificial experiments may be helpful in this regard and there are several strategies that can elevate q, and that can be pursued individually or in combination. Gas exchange measurements can be made at very high temperatures (exceeding 50ºC) using artificial leaves (Schymanski and Or, 2017) since they suffer no heat stress or loss of functionality under conditions that would endanger life. Evaporation from such leaves with rising q but at constant VPD is predicted to be practically constant according to stomatal conductance models, but to increase when taking non-diffusive transport into account. Similar experiments might be conducted on living leaves with hot but tolerable temperatures in conditions nearer to boiling due to reduced p, as within a hypobaric chamber. Finally, for leaves functioning in a "helox" environment (Mott and Parkhurst, 1991) – a mixture of helium and O_2 whose density (hence inertia) is just 29% that of dry air – non-diffusive transport would be elevated more than threefold

(Kowalski, 2017). Assessments of leaf functioning in such conditions should help to shed light on the implications of non-diffusive transport to stomatal gas exchanges.

~~5~~ 6 Conclusions

Water vapour's elevated partial pressure inside substomatal cavities implies depressed partial pressures of dry air components including oxygen (O_2), according to Dalton's law with negligible cavity pressurization. Substomatal cavities, not photosynthetically enriched in O_2, are dilute because of transpiration. Only non-diffusive conveyance can account for transport of O_2 from these O_2-poor cavities into the more aerobic, ambient atmosphere. Slight substomatal pressurization, however negligible in the context of Dalton's law, is sufficient to drive ~~jets~~ mass flow of air out of stomatal apertures. The relevance of ~~stomatal jets~~ mass flow to gas transport cannot be neglected universally in plant physiology, becomes important for water vapour and CO_2 in leaves at very high T, and therefore is increasing with global warming.

Competing interests

The author declares that he has no competing interests.

Acknowledgements

The author is supported by Spanish government projects PID2021-128463OB-I00 (REMEDIO), Ref: 2822/2021 (EVIDENCE), PID2020-117825GB-C21 (INTEGRATYON3), PN2021-2820s (IBERALP), and TED2021-129499A-I00 (MANAGE4FUTURE), as well as University of Granada projects PPJIB2022-08 (MODELICO) and C-EXP-366-UGR23 (MORADO) including European Union ERDF funds.

References

Aparecido, L.M.T., Woo, S., Suazo, C., Hultine, K.R. and Blonder, B., High water use in desert plants exposed to extreme heat, Ecol. Lett., 23: 1189-1200, https://doi.org/10.1111/ele.13516, 2020.

De Kauwe, M.G., Medlyn, B.E., Pitman, A. J., Drake, J. E., Ukkola, A., Griebel, A., Pendall, E., Prober, S., and Roderick, M., Examining the evidence for decoupling between photosynthesis and transpiration during heat extremes, Biogeosci., 1, 903-916. https://doi.org/10.5194/bg-16-903-2019, 2019.

Diao, H., Cernusak, L.A., Saurer, M., Gessler, A., Siegwolf, R.T.W. and Lehmann, M.M., Uncoupling of stomatal conductance and photosynthesis at high temperatures: mechanistic insights from online stable isotope techniques. New Phytol., 241: 2366-2378. https://doi.org/10.1111/nph.19558, 2024.

Farquhar, G. D. and Wong, S. C., An empirical model of stomatal conductance, Aus. J. Plant Physiol., 11, 191-210, 1984.

Giancoli D.C., General Physics, Prentice-Hall, Englewood Cliffs, 892pp, 1984.

IPCC. Climate change 2021 – the physical science basis. Cambridge University Press 43: 22–23, 2021.

Jarman, P. D. The diffusion of carbon dioxide and water vapour through stomata, J. Exp. Bot. 25, 927-936, 1974.

Kowalski, A. S., The boundary condition for vertical velocity and its interdependence with surface gas exchange, Atmos. Chem. Phys., 17, 8177-8187, https://doi.org/10.5194/acp-17-8177-2017, 2017.

Krich, C., Mahecha, M. D., Migliavacca, M. De Kauwe, M. G. Griebel, A., Runge, J. and Miralles, D. G., Decoupling between ecosystem photosynthesis and transpiration: A last resort against overheating, Env. Res. Lett., 17 (4), 044013, https://doi.org/10.1088/1748-9326/ac583e, 2022.

Lawson, T., James, W., and Weyers, J., A surrogate measure of stomatal aperture, J. Exp. Bot., 49 (325), 1397-1403, 1998.

Marchin, R., Medlyn, B 396 . E., Tjoelker, M. G. and Ellsworth, D. S., Decoupling between stomatal conductance and photosynthesis occurs under extreme heat in broadleaf tree species regardless of water access, Global Change Biol., 29, 6319-6335, https://doi.org/10.1111/gcb.16929, 2023.

Moss, D. N. and Rawlins, S. L., Concentration of carbon dioxide inside leaves, Nature, 197, 1320–1321, 1963.

Mott, K. A. and Parkhurst, D. F., Stomatal responses to humidity in air and helox, Plant Cell Environ., 14, 509–515, 1991.

Pankasem, N., Hsu, P.-K., Lopez, B.N.K., Franks, P.J. and Schroeder, J.I., Warming triggers stomatal opening by enhancement of photosynthesis and ensuing guard cell CO_2 sensing, whereas higher temperatures induce a photosynthesis-uncoupled response. New Phytol, 244, 1847-1863, https://doi.org/10.1111/nph.20121, 2024.

Parkhurst, D. F., 1994, Diffusion of CO2 and other gases inside leaves, New Phytol., 126, 449-479.

Sun, W., Maseyk, C., Lett, C., and Seibt, U., Restricted internal diffusion weakens transpiration–photosynthesis coupling during heatwaves: Evidence from leaf carbonyl sulphide exchange, Plant Cell Environ., 47, 1813-1833, 2024.

Vesala, T., Opening Pandora's box of transport phenomena. New Phytol. https://doi.org/10.1111/nph.19749, 2024.

von Caemmerer, S. and Farquhar, G.D., Some relationships between the biochemistry of photosynthesis and the gas exchange of leaves, Planta, 153, 376-387, 1981.