

Response to Reviewer 1

This paper employed a heuristic model, which was derived from two prognostic equations (liquid water path L and cloud droplet number concentration N), to understand cloud water adjustments in stratocumulus to aerosols. The primary model parameters were chosen by matching the ensemble LES modeling of Glassmeier et al. (2021). This heuristic model successfully reproduced the inverted “v” shape relationship for L - N , which was found in LES simulations and satellite retrievals: L increases with aerosols at low N via suppressing precipitation, while L decreases with aerosols at high N through thermodynamic effects such as entrainment drying. Intriguingly, the authors found a tight relationship between adjustments at low and high N , demonstrating that entrainment effects that predominate at high N influence adjustments in precipitating clouds at low N . They also examined the sensitivity of cloud water adjustments in precipitating and non-precipitating clouds to the heuristic model’s parameters, along with external L or N perturbations.

I enjoyed reading this paper. It was very well organized and easy to follow. This study showcased a useful and effective way of applying a simple heuristic model to decipher the intricate cloud-aerosol interactions (ACI). The tight relationship between adjustments at high and low N found within this study is also beneficial in identifying potential aerosol-meteorology co-variability in the ACI study. I believe this paper will be suitable for publication in ACP if some issues outlined below are addressed.

We thank the reviewer for the support of our work and the constructive comments, which helped to clarify various aspects of our manuscript.

Major comments:

1. Lines 69-70 (or L69-70): The authors claimed that $L_{\infty,h}$ is applied to all N with *the same* $m_{\infty,h}$, because they assumed that the sensitivity of temporal change in L due to thermodynamics to N *seems* not dependent on the presence of precipitation. However, if we take a closer look at Figure S1 (or see figure below), the sensitivity of L tendency due to entrainment (see the slope of the green line) to N is found to be notably different between the precipitation period and the non-precipitation period.

We agree with this observation. However, while one can easily determine $d(dL/dt|_{\text{entrainment}})/dN$ from Fig. S1, one would have to assume a timescale to estimate $m = d\ln(L)/d\ln(N)$. And this timescale might not be constant, as indicated by τ_L in Fig. 1d. Thus, it is hard to translate any variability seen (or not seen) in Fig. S1 into cloud water adjustments. Hence, we decided to follow the established notion that cloud water adjustments can be represented by two constant slopes for low and high N , respectively.

Specifically, when precipitation occurs (or at low N), the boundary layer becomes more stable, thereby leading to a relatively small sensitivity of L tendency due to entrainment to N . Conversely, the sensitivity should be relatively large when precipitation is absent (or at high N),

as demonstrated by Figure R1. Given these facts, the authors need to clarify the rationality of assuming $m_{\infty,h}$ is independent of N and discuss the impact of this hypothesis on the main conclusion.

We would like to repeat a part of our conclusions: “This discrepancy indicates stronger thermodynamic adjustments at low N that transition into weaker thermodynamic adjustments at high N , suggesting that m_h should be a function of N .” This exactly corresponds to the reviewer’s comment above. Interestingly, the derivation of (9), i.e., our main theory, can be done for any piecewise constant $m_{\infty,h}$. Thus, our theory allows one to use different $m_{\infty,h}$ for low and high N . We have emphasized this in the conclusions: “Note that any piecewise-constant m_h obeys the aforementioned relationship with m_l , making it possible to use different m_h for low and high N in the proposed framework.”

The above sensitivity contrast also indicates weaker thermodynamic adjustments (mainly entrainment) at low N that transition into stronger thermodynamic adjustments at high N , which is, however, opposite to the authors’ discussion in L230-234. Are there any reasons for the inconsistency?

As outlined above, a weaker $d(dL/dt|_{\text{entrainment}})/dN$ at low N does not necessarily indicate weaker $m_{\infty,h}$ at low N , as we need to consider the role of an unknown timescale. In fact, a stronger $m_{\infty,h}$ at low N is a reasonable assumption as evaporating precipitation stabilizes the boundary layer and hence decreases entrainment. Thus, precipitation suppression due to an increase in N will allow turbulence to spin up and increase entrainment. We have clarified this in our conclusions: “Aerosol-meteorology co-variability could be an explanation for this N dependency. However, we would like to emphasize that this aerosol-meteorology co-variability does not have to be exogenous [e.g., differences in continental and maritime air (e.g., Brenguier et al., 2003)], but could be created by the analyzed system endogenously [e.g., the stabilizing effect of evaporating precipitation on boundary-layer dynamics and hence entrainment (e.g., Nicholls, 1984; Wood, 2007; Hoffmann et al., 2023)].”

2. In Section 5, the authors examined the susceptibility of cloud water adjustments to external perturbations in N and L . They modeled these perturbations as Bernoulli processes. The perturbation of τ , σ , and m is chosen to represent the general sensitivity of the system rather than matching a realistic case. I am curious if it is possible to perturb these parameters or impose N (L) perturbations per the influence of large-scale meteorological factors (MFs) like the moisture contrast between 1000 hPa and 700 hPa, which can alter the efficiency of entrainment drying and thus influence cloud water adjustments, especially at high N . Such a perturbation due to MFs would be more realistic and physically reasonable.

This is an important comment as it addresses the usefulness of the heuristic model to answer specific questions. Since the heuristic model does not represent entrainment explicitly, it cannot be used to answer a question on entrainment directly. Since we know that a decrease (increase) in entrainment efficiency results in an increase (decrease) in L , we can use the heuristic model to assess the influence of L perturbations, as done in Sec. 5. To address these specific questions,

especially on entrainment, more directly, we are currently developing a slightly more complex approach, in which entrainment-related processes are depicted more directly. We hope to submit the results in the coming months.

3. The paper is well-structured and concise, but in certain places, it is overly brief, particularly when introducing concepts without sufficient explanation. This brevity may stem from the text limitations imposed by the previous submission to GRL. Given that ACP does not have such restrictions, I recommend that the authors expand on and clarify specific concepts or physical mechanisms in more detail. Below, I provide some examples for the authors' consideration.

- (a) L45: The authors claimed that thermodynamic effects on L include the influence of entrainment, radiative cooling, and surface fluxes. It would be helpful if the authors could elaborate on how these three terms affect cloud water at a process level.

We slightly lengthened our descriptions of this: “The first term on the right-hand-side of $[dL/dt]$ represents a precipitation sink.” and “For a given N , this term can be a sink to the L budget due to an excess in entrainment warming and drying causing the cloud to evaporate ($L > L_{\infty,h}$), or a source driven by longwave radiative cooling leading to more condensation ($L < L_{\infty,h}$), while the effect of surface fluxes is usually small [cf. Fig. 2 in Hoffmann et al. (2020)].”

- (b) Suggest briefly explaining the concepts of “entrainment warming and drying”, “Brownian coagulation”, “Bernoulli process”, etc., and adding citations as well.

In the revised version of the manuscript, we state that “entrainment warming and drying caus[es] the cloud to evaporate.” We, however, would like to refrain from explaining established concepts in too much detail because additional explanations could affect the readability of the text. Nonetheless, to respond to the other reviewer’s comment, we slightly extended our explanation of the ‘Bernoulli process’ by “In this study, perturbations are modeled as a Bernoulli process, and are applied with the probability $\Delta t/\tau_{prt}$ evaluated for every timestep of the model. Here, τ_{prt} is the perturbation timescale, which is varied from 20 min to 2 weeks.”

4. L31: The authors mentioned the limitations of LESs in understanding cloud water adjustments due to limited spatial domains and specific initial and boundary conditions. However, the authors tuned their heuristic model parameters to match the ensemble LES modeling of Glassmeier et al. (2021). In that regard, I’d assume the heuristic model derived here is subject to LESs’ limitations. Generally, this study would be more insightful if the authors could use one paragraph or section to discuss their model's limitations and possible improvements (e.g., including a prognostic equation for cloud fraction), helping refine its applicability in future research.

This is again an important point, and we agree with it. In fact, we already discussed that the model and hence the LES data do not agree with observational data, indicating that different

$m_{\infty,h}$ need to be considered for low and high N: “This discrepancy [of the heuristic model and observations] indicates stronger thermodynamic adjustments at low N that transition into weaker thermodynamic adjustments at high N, suggesting that m_h should be a function of N.” While our conclusions section briefly addresses the LESs lack of aerosol-meteorology co-variability (“[...] this LES ensemble did not include aerosol-meteorology co-variability by design [...]”) and external perturbations (“Another explanation for the weaker observed m_h are external perturbations affecting N and L.”), this study is not the right place for a full assessment of potential shortcomings in LESs, especially the impact of numerics which could impact the representation of entrainment. Thus, we already stated in the original version of the manuscript “that this set of [LES] parameters should be seen as one potential realization of cloud water adjustments”, indicating that the parameters used here need to be adapted for any future application. Lastly, the idea of including a prognostic equation for cloud fraction is appealing, and could play an important role for the consideration of aerosol-meteorology co-variability. Thus, our manuscript states that “[q]uantifying the influence of aerosol-meteorology co-variability on the relationship between m_l and m_h constitutes an interesting way to continue this study [...]”, while not detailing how one could do so.

Minor comments:

L16: “droplet concentration” to “cloud droplet number concentration”

Done.

L33: Did you mean co-variability of aerosols and meteorology? Please be specific.

Yes. Changed to “[...] but also the inherent co-variability of aerosol and meteorology that confounds process-level understanding [...]”

L35: “letter” to “paper”

Done.

L39: “letter” to “paper”

Done.

L64: Does this source refer to cooling-induced water vapor condensation or enhanced PBL turbulent moistening?

The primary way is more condensation of water vapor due to cooler temperatures. While we agree that increased turbulence increases the surface moisture flux, its impact seems negligible for the clouds analyzed here (see Fig. S1). We clarified this as “For a given N, this term can be [...] a source driven by longwave radiative cooling leading to more condensation ($L < L_{\infty,h}$), while the effect of surface fluxes is usually small [cf. Fig. 2 in Hoffmann et al. (2020)].”

L68: Add references for “many studies”

We added a reference to Fig. 1 in Glassmeier et al. (2021), in which a selection of these studies is presented.

L72: Remove a duplicate “the”

Done.

L75: It would be helpful if the authors could provide more technical details on tuning the parameters to align with ensemble LES modeling. Additionally, including a validation figure of L evolution predicted by the heuristic model relative to LES modeling would enhance the clarity and robustness of the study.

We have added some further information: “The model parameters have been chosen to match the ensemble LES modeling of Glassmeier et al. (2021), who studied cloud water adjustments in stratocumulus clouds. They determined $\tau_t = 9$ h and $m_{\infty,h} = -0.64$ using an emulator. Based on their Fig. 3a, we selected $L_0 = 90$ g m⁻² and $N_0 = 100$ cm⁻³ to match their L_{∞} for high N , and derived $c_1 = 7600$ m⁻² kg^{-1/2} s⁻¹ to match their L_{∞} for low N .” Assessing the evolution of L is interesting but not within the scope of this study, which focuses on steady-state solutions.

L104: Please clarify how the cloud top effective droplet radius was derived and plotted in Figure 1.

Simple adiabatic considerations show that the cloud top effective radius scales with $(L/N^2)^{1/6}$, as shown in Goren et al. (2019), which is now referenced in the manuscript. We adapted the following statement: “This threshold is illustrated by the dashed black line indicating a cloud top effective droplet radius of 14 μ m that is often used to discriminate precipitating from non-precipitating clouds, and scales with $(L/N^2)^{1/6}$ (e.g., Gerber, 1996; Goren et al., 2019).”

L124: Is the threshold of 100 for N consistent with findings from LES modeling or satellite observations?

This value is not universal, but it matches the L_{∞} inflection point of this and other studies well. We added the following statement: “Note that we introduce $N \approx 100$ cm⁻³ as the boundary between the precipitation- and thermodynamics-dominated and hence low and high N parts of the phase space, as it corresponds to the L_{∞} inflection point in the heuristic model and LES ensemble data of Glassmeier et al. (2021) (Figs. 1a and b).”

L163-171: The authors highlighted some interesting values when perturbing $m_{\infty,h}$. However, I am not sure if $m_{\infty,h} = 2.0$ is physically meaningful as entrainment is supposed to dominate at high N (Figure S1), and the sinking term (entrainment) for L outweighs the source terms

(longwave radiative cooling and surface fluxes), yielding $m_{\infty,h} < 0$. It might be better to take into account some physical constraints when perturbing the parameters.

We agree that $m_{\infty,h} > 0$ is unphysical. However, we want to explore the possibilities of the phase space. Thus, we caution the reader as follows: "Nonetheless, we would like to highlight a few interesting values that $m_{\infty,h}$ may assume, even though $m_{\infty,h} > 0$ is likely unphysical due to the negative impact of increased entrainment on L at higher N ."