



1 **Optimally solving topography of snow-scaped landscapes to improve snow**
2 **property retrieval from spaceborne imaging spectroscopy measurements**

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9
10 **Abstract**

11 Accurately modelling snow albedo and specific surface area (SSA) are essential for
12 monitoring the cryosphere in a changing climate and are parameters that inform hydrologic
13 and climate models. These snow surface properties can be modelled from spaceborne
14 imaging spectroscopy measurements but rely on Digital Elevation Models (DEMs) of
15 relatively coarse spatial scales (e.g. Copernicus at 30 m) degrade accuracy due to errors in
16 derived products – like aspect. In addition, snow deposition and redistribution can change the
17 apparent topography and thereby static DEMs may not be considered coincident with the
18 imaging spectroscopy dataset. Testing in three different snow climates (tundra, maritime,
19 alpine), we established a new method that simultaneously solves snow, atmospheric, and
20 terrain parameters, enabling a solution that is more unified across sensors and introduces
21 fewer sources of uncertainty. We leveraged imaging spectroscopy data from AVIRIS-NG and
22 PRISMA (collected within 1 hour) to validate this method and showed a 15% increase in



23 performance for the radiance-based method versus using the static DEM (from $r=0.52$ to
24 $r=0.60$). This concept can be implemented in future missions such as Surface Biology and
25 Geology (SBG) and Copernicus Hyperspectral Imaging Mission for the Environment
26 (CHIME).

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28 **Key Words:** Imaging Spectroscopy, Snow Properties, Topography, Snow Albedo

29

30 **1 Introduction**

31 Accurately mapping snow surface properties is essential for seasonal snow zones in a
32 changing climate especially in regions where seasonal snowpack is expected to change
33 dramatically in the coming decades (Siirila-Woodburn et al., 2021). For example, snow
34 albedo plays a crucial role in melting of the snowpack during the ablation season (Wang et
35 al., 2020) with changes in snow albedo directly affecting the amount of absorbed solar
36 radiation, and therefore the amount of snow that is melted off as liquid water. Throughout the
37 winter season, snow albedo fluctuates due in part to grain size (Seidel et al., 2016) and light
38 absorbing particles (Kaspari et al., 2015; McKenzie, 2020; Schmale et al., 2017; Skiles &
39 Painter, 2017). With limited number of *in situ* snow stations around the globe measuring
40 surface properties, and snow surfaces constantly undergoing metamorphism across space and
41 time, satellite imagery represents the best potential for spatial and temporally complete



42 mapping of snow properties. Accurately retrieving snow albedo and other snow surface
43 properties from satellite imagery is paramount, especially in a rapidly changing climate
44 (Malmros et al., 2018).

45 Retrieval of snow properties from satellite remote sensing relies on Digital Elevation
46 Models (DEMs) to correct for local terrain effects (Bair et al., 2021; Bair et al., 2022; Dozier
47 et al., 2022). In a previous study, researchers found global DEM products to have “blunders
48 and errors” when compared to airborne lidar, particularly in derived slope and aspect which
49 cause severe errors in calculated solar illumination angles (Dozier et al., 2022). Dozier et al.
50 (2022) found errors in local solar illumination angles ranging from 0.048 to 0.117 across
51 several sites for Copernicus global DEMs caused by errors in slope and aspect. The cosine of
52 the local solar illumination angle, μ_s , is a function (Eq. 1) of slope angle (S), slope aspect
53 (A), solar zenith angle (θ_0), and azimuth angle (ϕ_0) – with the last two being well
54 constrained:

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$$56 \quad \mu_s = \max[0, \cos(\theta_0) \cos(S) + \sin(\theta_0) \sin(S) \cos(\phi_0 - A)] \quad (1)$$

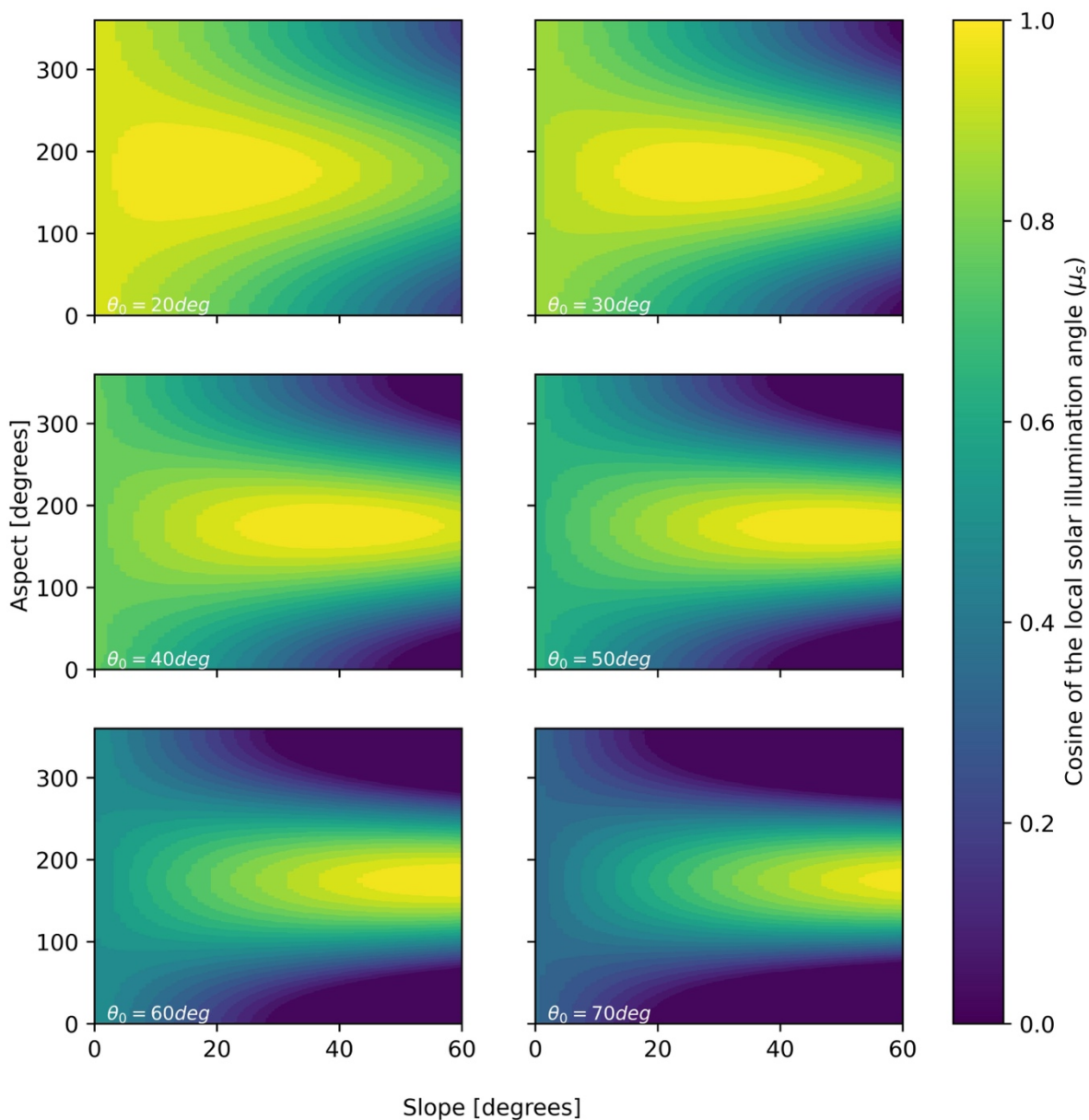
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58 Because θ_0 and ϕ_0 are calculable with low errors (less than 0.05°), the biggest contribution to
59 errors in μ_s stem from slope and aspect. Errors in μ_s increase monotonically with increasing
60 θ_0 (e.g., sun setting has high θ_0 , as does solar noon in high latitude winters). This



61 phenomenon can be explained by plotting Eq. 1 for various solar zenith angles, θ_0 , (Figure
62 1). Put simply, at higher θ_0 there is a higher standard deviation in μ_s surrounding a known
63 slope and aspect (with some temporally consistent uncertainty), increasing the probability and
64 magnitude of such an error. For example, if one were to arbitrarily choose slope and aspect
65 (with some uncertainty), and varying θ_0 (20-70°), one could find a similar range of errors as
66 presented in Dozier et al. (2022).

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68

69 **Figure 1.** Cosine of local illumination angles (μ_s) as a function of slope (x-axis) and aspect

70 (y-axis) incremented by 1° . Increasing solar zenith angles (θ_0) illustrates the problem at



71 higher latitude, and/or winter acquisitions, where variability increases with respect to slope
72 and aspect. For this illustration ϕ_0 is fixed at a value of 175° .

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74 Recent work has shown μ_s can be modelled using an optimal estimation framework
75 given the Top of Atmosphere (TOA) radiance observed from imaging spectroscopy (Carmon
76 et al., 2023). The authors solve for surface, atmospheric, and topographic state variables
77 simultaneously in their model. This works physically because the partition of direct to diffuse
78 light introduces a shape and magnitude effect on the TOA radiance spectra. However,
79 retrieving snow optical properties is sensitive to directional reflectance which is significantly
80 influenced by the viewing geometry as well, especially in steep terrain, leading to possible
81 shortcomings in this method specifically for snow covered pixels. To address this and expand
82 upon this framework, we present a new method to account for terrain in snow covered areas.
83 Our method is tested on pixels with greater than 75% snow cover in three different snow
84 climates (tundra, maritime, and alpine) with spaceborne imaging spectroscopy with the aim to
85 reduce error in derived snow properties by optimally solving for topography. The spaceborne
86 results are validated against high confidence airborne spectrometer data and further evaluated
87 with error distributions. This work directly contributes to snow property retrievals in steep
88 terrain and/or at times of high solar illumination angles for upcoming satellite missions such



89 as Surface Biology and Geology (SBG) (Cawse-Nicholson et al., 2021) and Copernicus
90 Hyperspectral Imaging Mission for the Environment (CHIME) (Celesti et al., 2022).

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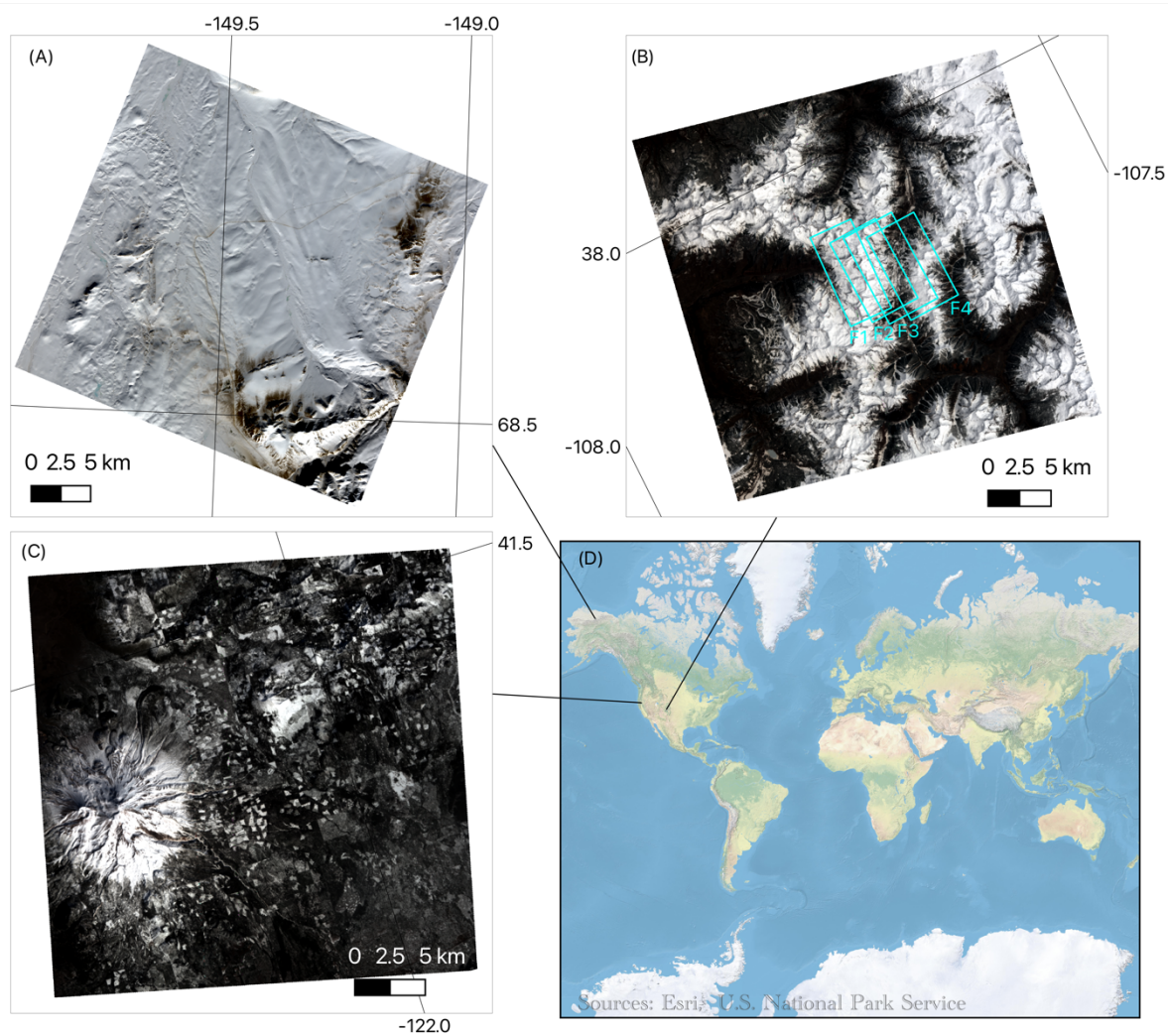
92 **2 Methods**

93 **2.1 Study area**

94 For our study, we used PRecursores IperSpettrale della Missione Applicativa
95 (PRISMA) imagery over three sites capturing different snow climates and solar zenith angles:
96 San Juan Mountains (Colorado, USA, 29 April 2021, $\theta_0=27^\circ$), Mount Shasta (California,
97 USA, 28 February 2021, $\theta_0=52^\circ$), and the Toolik area (Alaska, USA, 21 March 2021,
98 $\theta_0=68^\circ$) (Figure 2). The San Juan Mountains location is considered a high alpine site located
99 in interior continental USA with an elevation range of 2208-4129 m. The Mount Shasta site is
100 a maritime snow climate along the western coast of USA with an elevation range of 750-4232
101 m. The Toolik site (elevation range = 504-1748m) is a high-latitude tundra site, being mostly
102 flat but with steep sections along the Brooks Range (along the southern part of the image).
103 PRISMA, launched by the Italian Space Agency (ASI) and beginning operation on March 22,
104 2019, is a spaceborne imaging spectroscopy mission collecting radiance at 30 m spatial
105 resolution across 237 bands spanning 400-2500 nm at a spectral resolution of 9.24 nm and
106 9.27 nm in the visible-near and shortwave infrared, respectively (Cogliati et al., 2021).



107 To validate our method, we used four existing Airborne Visible Infrared Imaging
108 Spectrometer-Next Generation (AVIRIS-NG) flightlines over the San Juan Mountains from
109 29 April 2021 (flying 1 hour after PRISMA acquisition). AVIRIS-NG collects radiance
110 measurements at variable spatial resolution (depending on the flight altitude) across 425
111 bands spanning 380-2510 nm in 5nm intervals (Green et al., 2023). For this flight, data were
112 collected at 4 m spatial resolution. We downloaded AVIRIS-NG apparent reflectance from
113 National Snow and Ice Data Center (NSIDC) and observation geometry data from NASA
114 Search Earth Data (Skiles & Vuyovich, 2023).



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116 **Figure 2.** PRISMA true colour images for Toolik on 21 March 2021 (A), San Juan
117 Mountains on 29 April 2021 (B), and Mount Shasta on 28 February 2021 (C). Four
118 coincident AVIRIS-NG flightlines (F1-F4) are shown in cyan over the San Juan Mountains.

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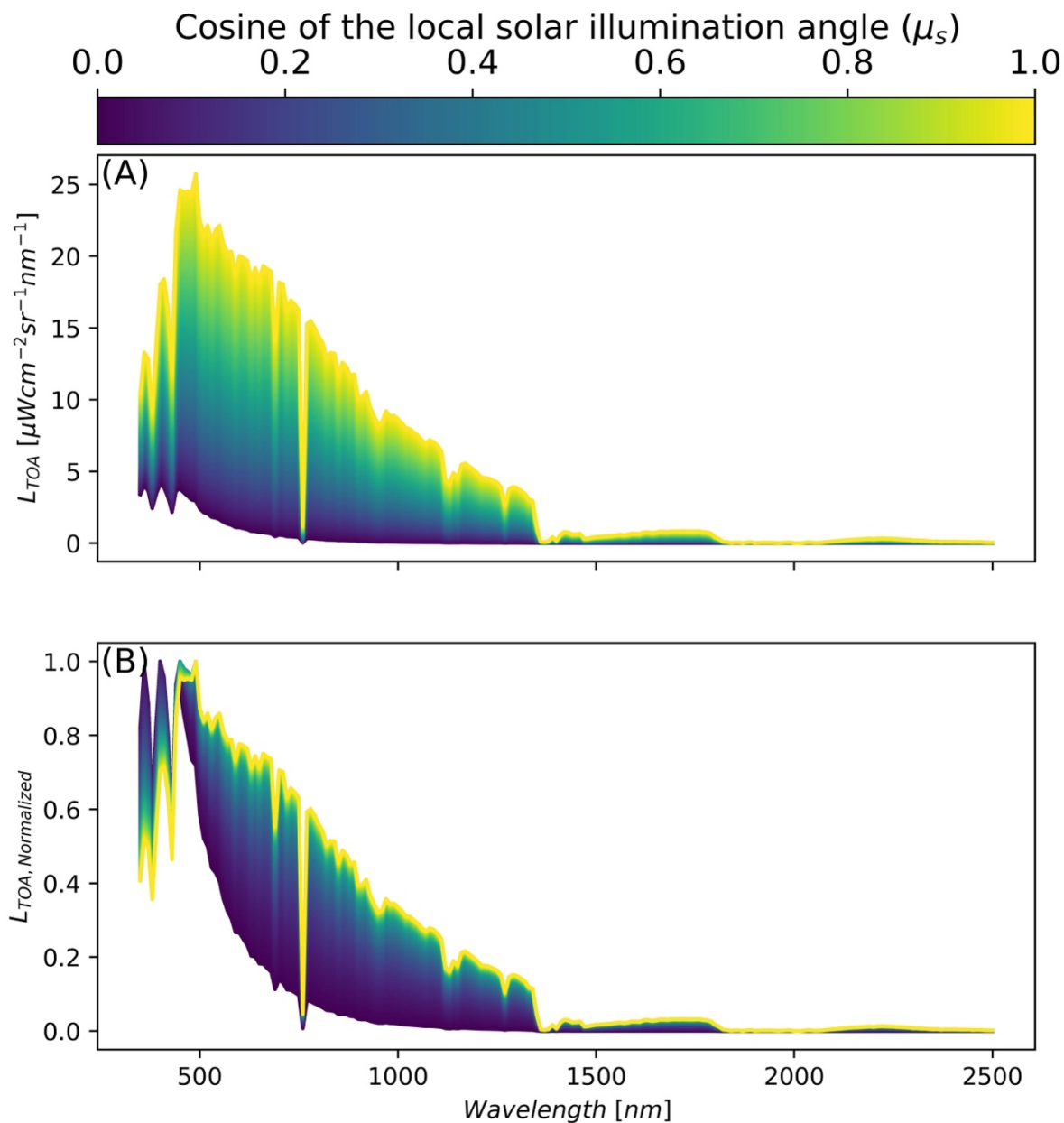
120 **2.2 Modelling surface, atmosphere, and topography from PRISMA**

121 The algorithmic improvements build off a workflow that estimates snow properties
122 given PRISMA TOA radiance, titled Global Optical Snow properties via High-speed
123 Algorithm using K-means (GOSHAWK) (Wilder et al., 2023; Wilder et al., 2024). In short,
124 GOSHAWK uses the analytic asymptotic radiative transfer model (AART) (Kokhanovsky &
125 Zege, 2004) coupled with libRadtran (Mayer & Kylling, 2005) to invert snow surface and
126 atmospheric properties (Bohn et al., 2021; Dalcin & Fang, 2021), and fractional covers of
127 mixed pixels under varied lighting conditions using non-linear numerical optimization (Bair
128 et al., 2021). The parameters solved for in the optimization routine include fractional covers,
129 specific surface area (SSA), light absorbing particle concentration (modelled as soot), liquid
130 water content (LWC) percentage, dimensionless aerosol optical depth at 550nm, and
131 columnar water vapor in the atmosphere. Here, we expand upon the GOSHAWK algorithm
132 considering recent work showing the capacity to estimate μ_s from TOA radiance (Carmon et
133 al., 2023; Bohn et al. 2024{TBD-preprint..}). This capacity is demonstrated in Figure 3 using
134 fixed snow properties via AART and fixed atmosphere properties via libRadtran across the
135 range of plausible μ_s (i.e. 0 to 1). Like the findings in Carmon et al. (2023), Figure 3 shows
136 that μ_s controls both the spectral shape and magnitude of observed TOA radiance with the
137 effect varying across wavelengths. The greatest shape effect can be seen in the visible
138 spectrum (roughly 400-700 nm) due to the magnitude of the diffuse irradiance. In



139 combination with the magnitude and shape shift, this parameter becomes solvable during
140 optimization due to its strong separability – especially when considering the entire spectrum
141 data from a hyperspectral remote sensing source such as PRISMA. It is important to note that
142 μ_s impacts both the AART estimation of snow reflectance and libRadtran estimation of
143 incoming solar irradiance.

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146 **Figure 3.** Synthetic data showing change in magnitude (A) and shape (B) of top of atmosphere

147 radiance (L_{TOA}) with respect to changing local solar illumination angle (μ_s) for fixed snow



148 surface state variables modelled with AART, and fixed atmospheric state variables modelled
149 with libRadtran (viewing geometry was fixed as well). State variables and solar/view geometry
150 were based on a PRISMA acquisition over southern Idaho on 8 December 2022. Figure (B)
151 shows normalized radiance with respect to peak TOA radiance across wavelengths to highlight
152 the change in shape.

153

154 However, if we were only to optimize μ_s , the other key terms, local viewer zenith
155 angle (μ_v) and local phase angle (ξ) in the AART formulation for bidirectional reflectance of
156 snow (Kokhanovsky & Zege, 2004) would remain constant from the available DEM (i.e.,
157 μ_s, μ_v, ξ are all derived from DEM) (Eq. 2; Wilder et al., 2024),

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$$159 \quad r_{snow}(\mu_s, \mu_v, \xi, \lambda) = r_0(\mu_s, \mu_v, \xi) \alpha_{snow}(\lambda) \quad (2)$$

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161 where r_0 represents the semi-infinite nonabsorbing snow layer, α_{snow} is the plane albedo,
162 and r_{snow} is the bidirectional reflectance of snow. Keeping other terms μ_v and ξ the same are
163 problematic because snow reflectance is poorly approximated as a non-Lambertian surface
164 (Leroux & Fily, 1988), and the outcome will be greatly influenced by μ_v and ξ . Therefore, to
165 incorporate solving for μ_s, μ_v , and ξ from TOA radiance into the GOSHAWK algorithm, we
166 instead elect to optimally solve for $\cos(\text{aspect})$ (i.e., “northness”) and $\sin(\text{aspect})$ (i.e.,



167 “eastness”) (Table 1). Aspect can be solved during optimization by using the atan2 function
168 (Van Rossum, 2020). We chose to use this method because eastness and northness are
169 continuously differentiable, and therefore, are suited for numerical optimization methods,
170 whereas aspect is circular. We then can use this optimal aspect to estimate μ_s (Eq. 1), μ_v (Eq.
171 3), and ξ (Eq. 4),

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$$173 \quad \mu_v = \max[0, \cos(\theta_v) \cos(S) + \sin(\theta_v) \sin(S) \cos(\phi_v - A)] \quad (3)$$

174

$$175 \quad \xi = \cos^{-1}(-\mu_s \mu_v + \sin(\theta_i) \sin(\theta_v) \cos(180 - (\phi_v - \phi_0))) \quad (4)$$

176

177 where ϕ_v is the viewing azimuth angle, and θ_v is the viewer zenith angle on a flat plane. This
178 directly impacts Eq. 5 and the formulation of incoming solar energy in the model,

179

$$180 \quad E(\lambda) = \psi \mu_s E(\lambda)_{dir} + V_\Omega E(\lambda)_{diff} + \left[\left(1 + \frac{\cos(S)}{2} - V_\Omega \right) r(\lambda)_{surf} (E(\lambda)_{dir} + E(\lambda)_{diff}) \right] \quad (5)$$

181

182 where E is total incoming irradiance, ψ is binary shade or no shade, E_{dir} and E_{diff} are the
183 direct and diffuse irradiance, respectively, V_Ω is the sky view factor, and r_{surf} is the reflectance
184 of nearby terrain. Explicitly within GOSHAWK the following equation is then solved using
185 non-linear numerical optimization (Wilder et al., 2024). Adding in the two extra parameters



186 in our updated optimization scheme did not change our run time significantly, which still
187 hovered around 15 minutes (depending on the image), as noted in Wilder et al. (2024). It is
188 also worth noting that while the optimal aspect cannot be solved accurately due to a non-
189 unique solution space (Figure 1), the resulting μ_s , μ_v , and ξ are unique and the solution is
190 such. Rasters of SSA and LWC at the surface were developed to verify this algorithm update.

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205 **Table 1.** Parameter space and initial vectors used in numerical optimization.

Parameter [unit]	Definition	Feasible Range	Initial State	Type
f-snow [%]	Fractional snow in the mixed pixel	[0, 100]	10	Surface
f-shade [%]	Fractional shade in the mixed pixel	[0, 100]	20	Surface
f-LC1 [%]	Fractional cover of endmember 1 (based on land cover value at pixel)	[0, 100]	50	Surface
f-LC2 [%]	Fractional cover of endmember 2 (based on land cover value at pixel)	[0, 100]	20	Surface
SSA [m ² kg ⁻¹]	Specific surface area, which is related to the optical grain size at the snow surface via the density of ice	[2, 156]	40	Surface
LAP [ng g ⁻¹]	Concentration of light absorbing particles, modelled as soot.	[0, 0.5e-5]	0	Surface
LWC [%]	Percentage of liquid water content in the snowpack.	[0, 50]	2	Surface
AOD 550 [%]	Dimensionless Aerosol Optical Depth at 550 nm	[1,100]	10	Atmospheric
H ₂ O [mm]	Columnar water vapor in the atmosphere	[1,50]	1	Atmospheric
Eastness	sin(aspect)	[-1,1]	Variable	Topographic
Northness	cos(aspect)	[-1,1]	Variable	Topographic



206

207 **2.2 Estimating snow properties from AVIRIS-NG for validation**

208 Due to the higher signal to noise ratio and the higher spatial resolution of AVIRIS-
209 NG, we treated the dataset as the ground reference. It also captured a similar spectral range to
210 PRISMA which made it a suitable comparison dataset. To select snow-covered pixels, we
211 solved for NDSI (Normalized Difference Snow Index) using bands at 600 nm and 1500 nm.
212 We limited our retrieval for NDSI greater than or equal to 0.90 (Painter et al., 2013). A
213 common approach to retrieve snow grain size from pure snow pixels is to apply the scale
214 band area algorithm (Nolin & Dozier, 2000); however, it is recognized that large presence of
215 LWC is a limitation. The maximum air temperature of 10.8° C on the day of the image at the
216 San Juan Mountains site indicated that elevated LWC at the surface was probable (Center for
217 Snow and Avalanche Studies, 2023). Additionally, reflectance spectra appeared to be shifted
218 along the x-axis (wavelength) due to the presence of LWC. Therefore, we used numerical
219 optimization to model apparent snow reflectance with AART by allowing fractional shade,
220 LWC, and SSA to vary. We did not include rock or forest endmembers in this formulation,
221 assuming the 4 m pixels are relatively homogenous. Topographic incident angles were held
222 constant based on the 4 m resolution DEM provided by AVIRIS-NG. We minimized Root
223 Mean Square Error (RMSE) between observed-apparent and modelled-apparent snow
224 reflectance from AART wavelengths greater than 900 nm and not impacted by atmospheric



225 interference and LAP (Miller et al. 2016) (901-1299 nm, 1451-1779 nm, and 1951-2449 nm).

226 The presence of LWC was included in our analysis by means of the composite refractive

227 index of water and ice (Donahue et al., 2022; Segelstein, 1981; Warren & Brandt, 2008).

228

229 **2.4 Comparing modelled snow albedo and SSA**

230 The GOSHAWK algorithm was used in two different modes: 1) static topography

231 based on the Copernicus DEM (hereon called “*static*”); and 2) solved topography based on

232 the algorithm updates (hereon called “*radiance*”). To compare the accuracy of PRISMA

233 derived SSA and LWC, we resampled the AVIRIS-NG results to match the PRISMA

234 resolution (30 m) and extents by using bilinear interpolation. Then, we sampled all valid

235 pixels where PRISMA and AVIRIS-NG had snow. We then computed r-pearson correlation

236 coefficient, Mean Bias, and RMSE for the radiance and static methods (with respect to

237 AVIRIS-NG). Finally, we used Copernicus derived slope and aspect maps to determine

238 where the largest errors were occurring on the landscape to compare with the theoretical basis

239 presented in Figure 1. We do this by using the Mean Absolute Error (MAE) with respect to

240 slope and aspect. We expected to see higher differences in north facing aspects (i.e., μ_s

241 approaches 0), and where θ_0 was higher. To test the interaction with θ_0 more fully, we

242 extended the analysis to Mount Shasta, CA, and Toolik, Alaska, where no *in situ data*



243 existed. Finally, we compared the modelled broadband albedo and SSA between the radiance
244 and static methods to assess how these assumptions propagated into outputs.

245

246 **3 Results**

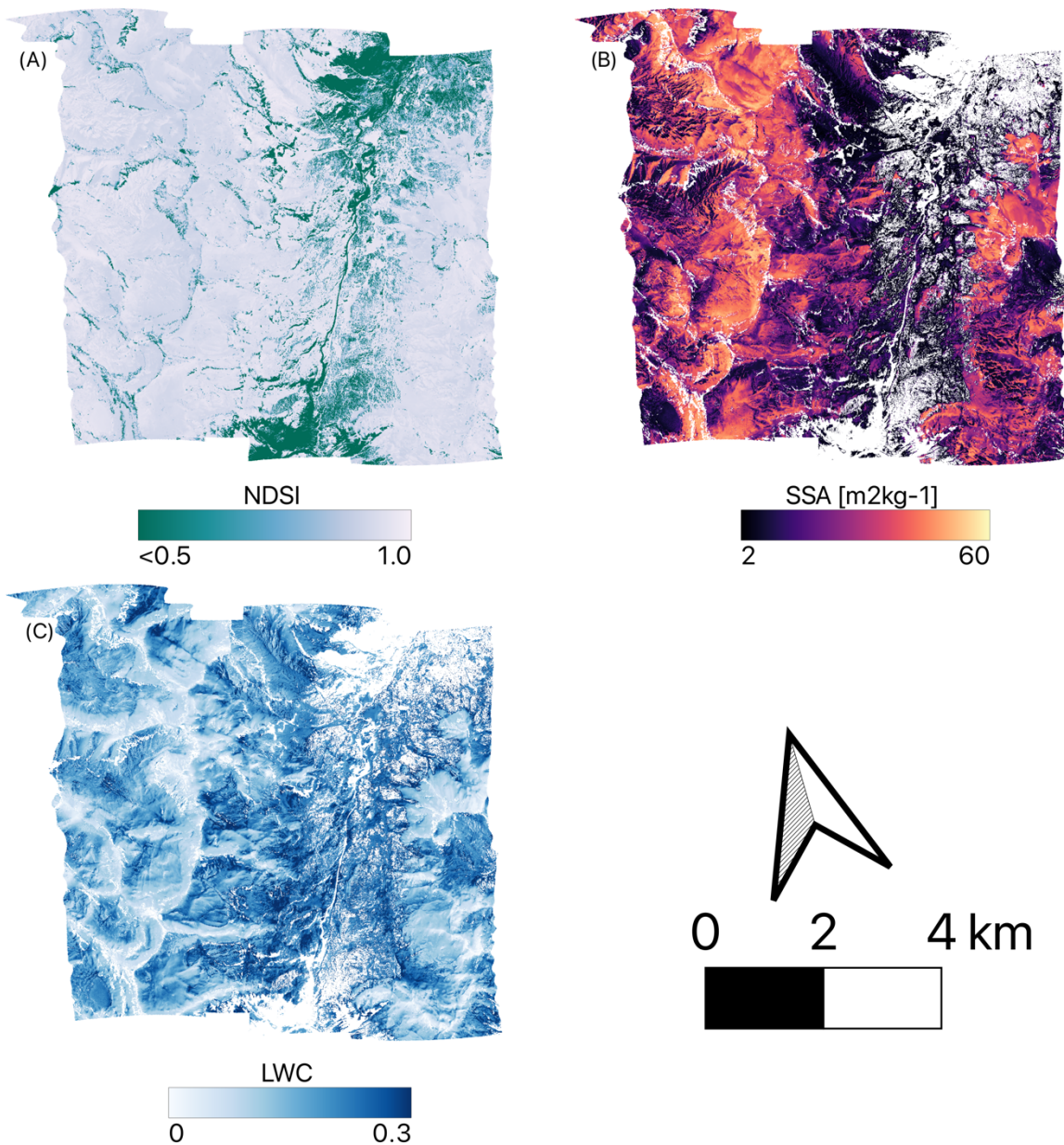
247 **3.1 Validation using AVIRIS-NG data over the San Juan Mountains**

248 When comparing the two methods over each pixel in the AVIRIS-NG flightlines
249 (Figure 4) we found that the radiance method performed better for SSA and LWC (Table 2).
250 The greatest improvement over the static DEM method was observed where average SSA was
251 highest (flightline f1), with RMSE improving from 15.58 m² kg⁻¹ to 11.12 m² kg⁻¹.
252 Interestingly, across all flightlines the radiance method had a lower range in RMSE (8.66 -
253 11.12 m² kg⁻¹) compared to the static method (RMSE was 8.99-15.58 m² kg⁻¹). Over all
254 flightlines, AVIRIS-NG estimated SSA = 23.23 +/- 13.18 m² kg⁻¹, PRISMA radiance method
255 estimated SSA = 23.67 +/- 12.45 m² kg⁻¹, and PRISMA static method estimated SSA = 25.06
256 +/- 16.06 m² kg⁻¹.

257 There was a consistent negative bias of 0.10-0.11 for LWC estimates from both static
258 and radiance when compared to AVIRIS-NG. Despite the bias, r ranged from 0.48-0.65
259 depending on the flightline and method, showing a strong signal of LWC present at the site.
260 The average LWC for the entire study area was estimated by AVIRIS-NG at 0.17 +/- 0.06,
261 PRISMA radiance method at 0.07 +/- 0.07, and PRISMA static method at 0.05 +/-0.05. As



262 previously noted, the temperatures were well above freezing during the overpass of AVIRIS-
263 NG and occurred roughly 1 hour later in the day compared to the PRISMA acquisition. This
264 most likely explains the higher LWC observed by AVIRIS-NG.





266 **Figure 4.** Snow properties computed from AVIRIS-NG (4 m spatial resolution) on 29 April
 267 2021 including NDSI (A), SSA (B), and LWC (C) for the San Juan Mountain site.

268

269 **Table 2.** Performance metrics of the static and radiance methods deriving SSA ($\text{m}^2 \text{kg}^{-1}$) and
 270 LWC from PRISMA imagery over the area of the AVIRIS-NG bounds. The two methods are
 271 compared to AVIRIS-NG derived values as ground truth.

		SSA ($\text{m}^2 \text{kg}^{-1}$)			LWC [0-1]		
AVIRIS-NG Flightline	PRISMA Method	RMSE	Average Bias	r	RMSE	Average Bias	r
f1 n=16,171	Static	15.58	0.01	0.38	0.12	-0.11	0.57
	Radiance	11.12	-1.08	0.49	0.12	-0.11	0.54
f2 n=12,930	Static	12.15	-4.33	0.57	0.12	-0.11	0.65
	Radiance	10.13	-4.00	0.66	0.11	-0.10	0.62
f3 n=5,722	Static	10.27	1.86	0.52	0.12	-0.10	0.51
	Radiance	9.12	2.33	0.57	0.12	-0.10	0.48
f4 n=8,292	Static	8.99	2.00	0.70	0.12	-0.11	0.57
	Radiance	8.66	3.10	0.73	0.11	-0.10	0.54

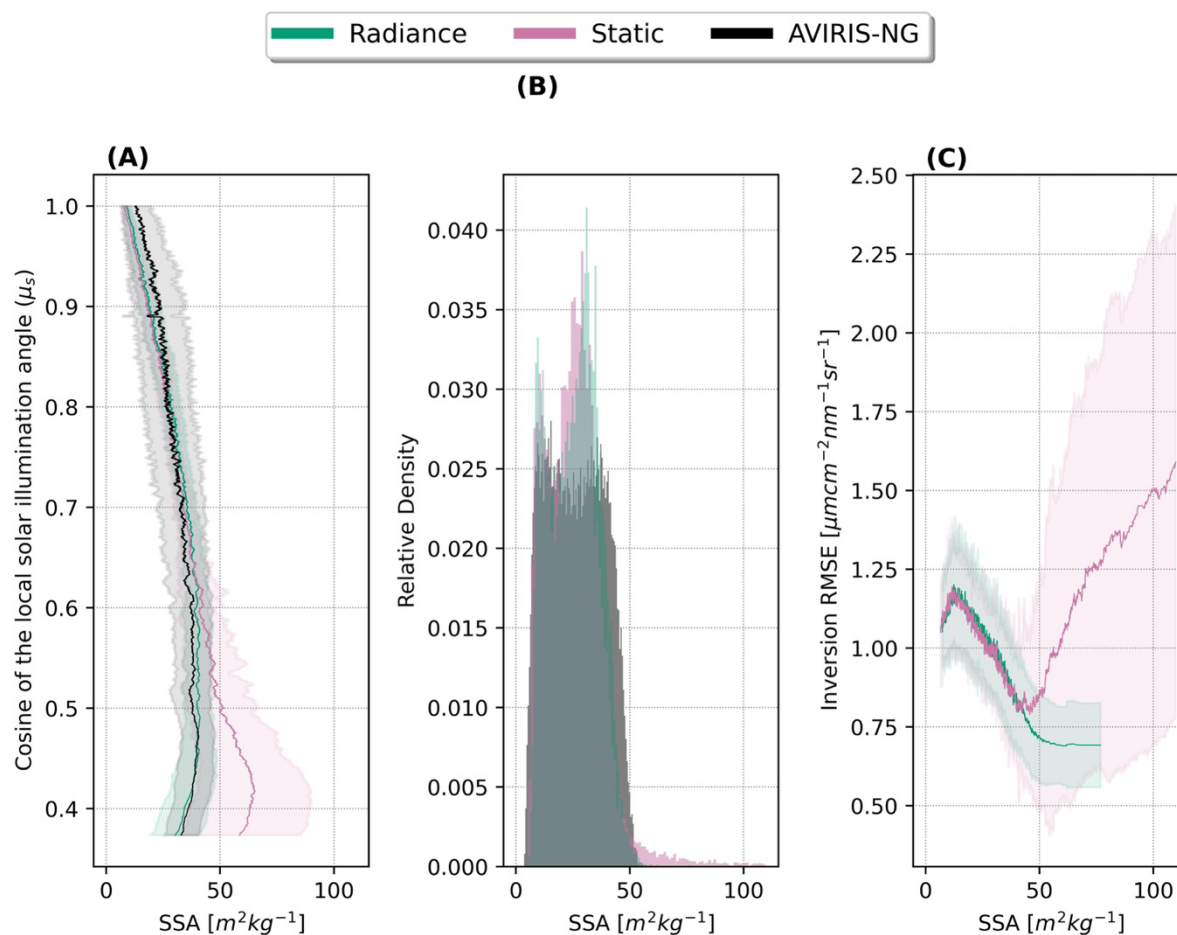


Combined f1-	Static	13.10	-0.57	0.52	0.12	-0.11	0.62
f4	Radiance	10.25	-0.67	0.60	0.12	-0.11	0.60

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274 The error analysis revealed large outliers modelled by the static method (Figure 5) when
275 compared to the reference AVIRIS-NG SSA. This can be seen in Figure 5b as a long tail of the
276 density histograms for the static method. These errors primarily occurred on steep, north facing
277 aspects (e.g., when μ_s approached 0). Using a moving average with respect to μ_s , radiance
278 derived SSA followed the general distribution of AVIRIS-NG derived SSA much better, even
279 as μ_s approached 0. This differs from the static method where the modelled SSA and resulting
280 RMSE from inversion begin to diverge as μ_s approached 0.



281

282 **Figure 5.** Modelled SSA for radiance method (green), static method (pink), and AVIRIS-NG

283 (black) with respect to μ_s (A), modelled SSA density histogram (B), and resulting RMSE from

284 the inversion from PRISMA with respect to solved SSA (C). Note that panels (A) and (C) are

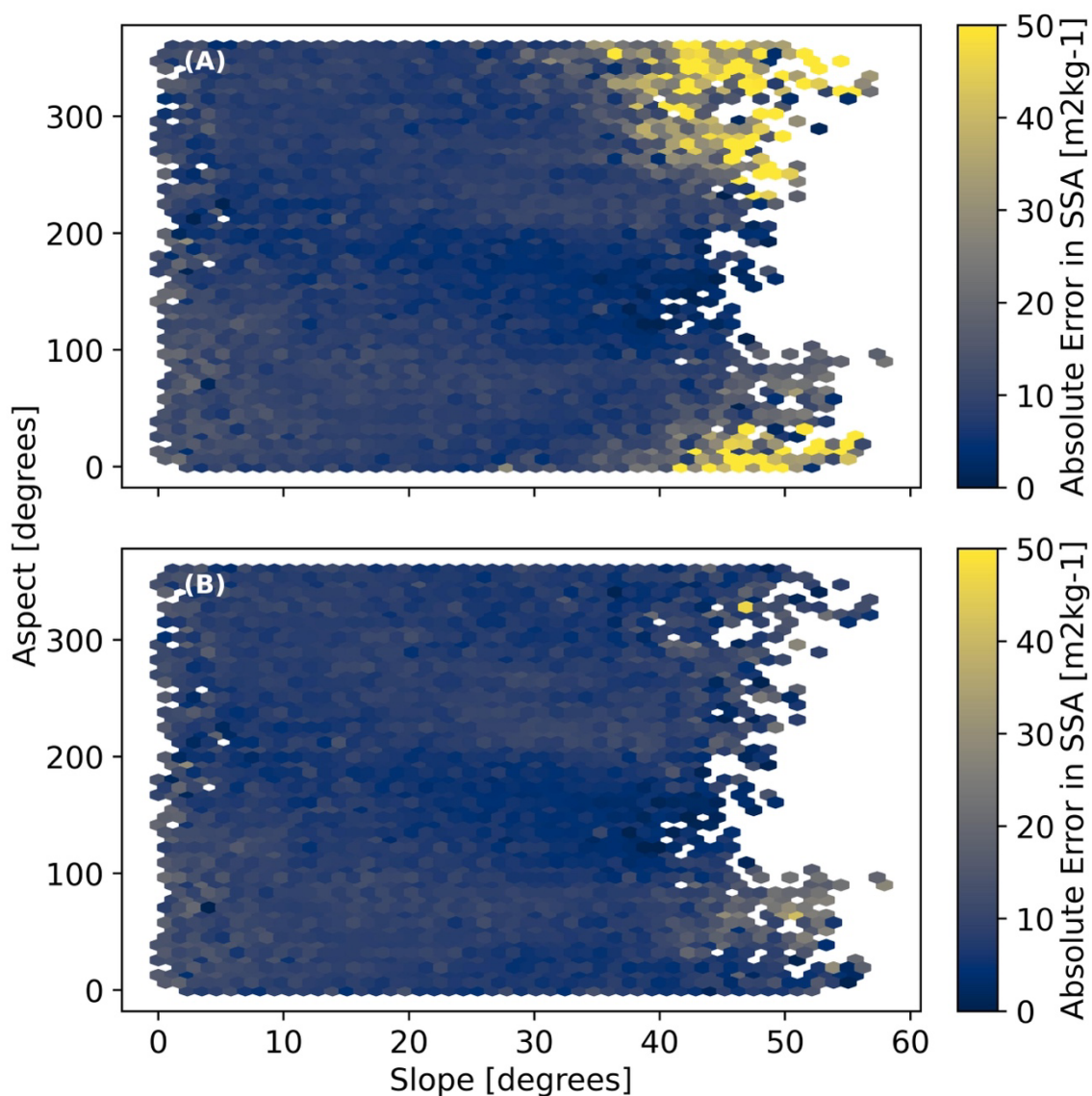
285 plotted using a moving average and binned with respect to μ_s and SSA, respectively.

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288 Next, we found the radiance method error ($MAE = 8.19 \text{ m}^2 \text{ kg}^{-1}$) was more evenly
289 distributed across the entire landscape (combined flightlines 1 through 4) (Figure 6). This is
290 unlike the static method, where symmetric zones of larger error can be seen that are similar to
291 the theoretical approach in Figure 1. Similarly, we found absolute error increased as μ_s
292 approached zero for the static method ($r = 0.27$; $p < 0.01$), while this relationship was not evident
293 for the radiance method ($r = -0.04$; $p < 0.01$).



294

295 **Figure 6.** 2D Histogram showing absolute error in SSA compared to AVIRIS-NG with respect
296 to slope and aspect across the entire dataset for PRISMA static method (A), and PRISMA
297 radiance method (B). Absolute error is calculated as $|\text{PRISMA SSA} - \text{AVIRIS-NG SSA}|$.



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299 **3.2 Comparing radiance and static methods between sites**

300 On average for the Mount Shasta site, the radiance method estimated SSA was 17.57
301 +/- 14.58 m² kg⁻¹, and static method SSA was 17.74 +/- 12.67 m² kg⁻¹ (Table 3). Notably, there
302 were more data gaps in the static method, resulting from failed inversions likely due to errors
303 in the slope and aspect. On average for the Toolik site the radiance method estimated SSA to
304 be 51.50 +/- 12.46 m² kg⁻¹, and the static method estimated 52.07 +/- 14.49 m² kg⁻¹.

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317 **Table 3.** Image-wide statistics of SSA and broadband albedo between the two methods (static
318 vs. radiance) processing the PRISMA imagery for all three sites.

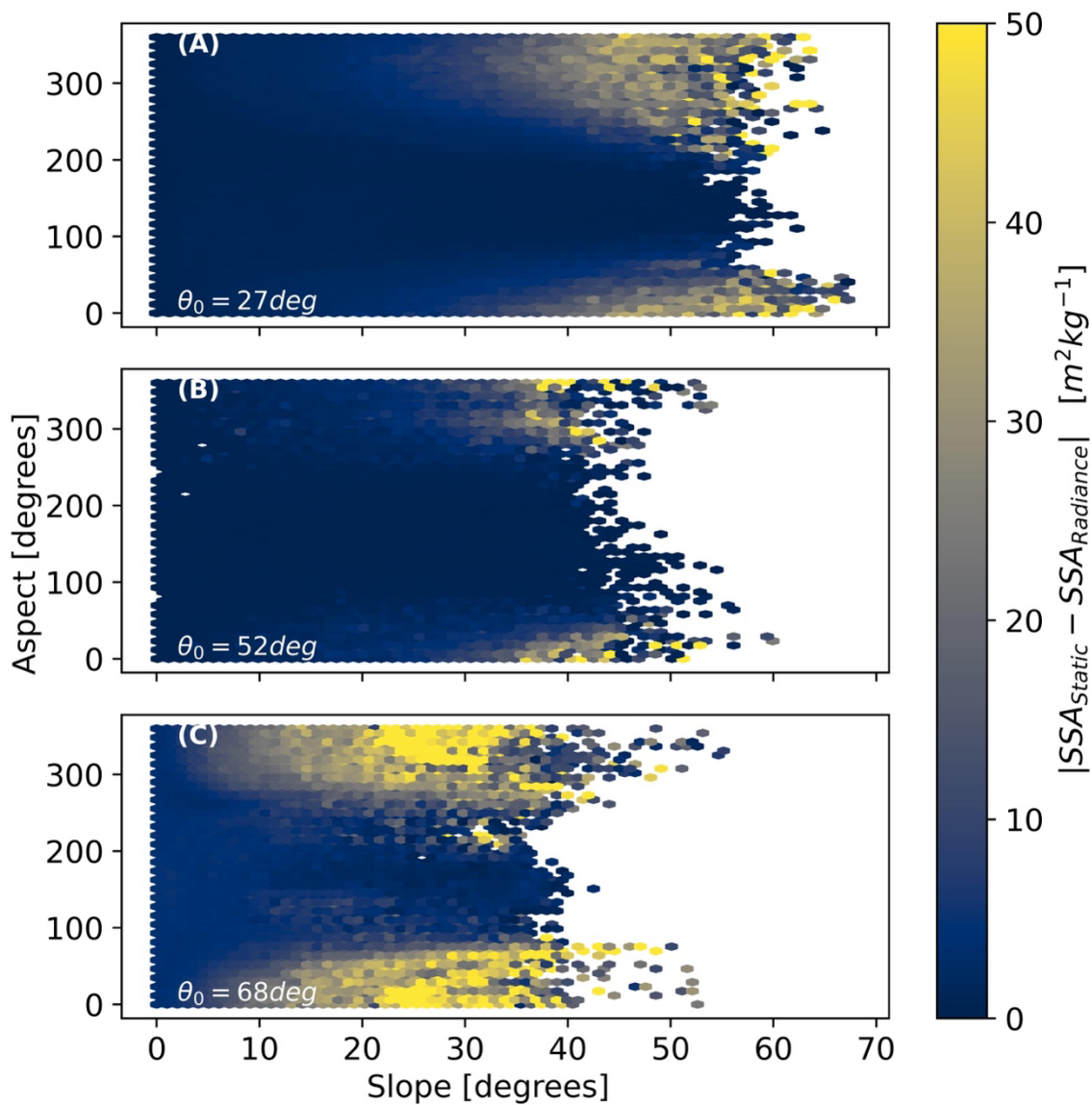
Site	PRISMA Method	Mean SSA (m ² kg ⁻¹)	Standard Deviation of SSA (m ² kg ⁻¹)	Mean Broadband Albedo	Standard Deviation of Broadband Albedo
San Juan	Static	22.14	19.40	0.79	0.03
	Radiance	21.27	15.94	0.78	0.04
Shasta	Static	17.74	12.67	0.74	0.05
	Radiance	17.57	14.58	0.72	0.06
Toolik	Static	52.07	14.49	0.82	0.03
	Radiance	51.50	12.46	0.81	0.03

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320 Additionally, we saw the highest difference between the two methods on north facing
321 aspects, where μ_s approached 0 (Figure 7). The difference in distributions matched closely to
322 the theoretical demonstration (Figure 1) and is most likely associated with the standard error
323 of slope and aspect from Copernicus DEM given the illumination conditions. This result
324 demonstrated that the difference between the two methods had the biggest impact for images
325 where θ_0 was high.



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328 **Figure 7.** 2D Histogram plot showing absolute error in SSA with respect to slope and aspect

329 across the entire dataset, treating radiance method as validation, absolute difference is

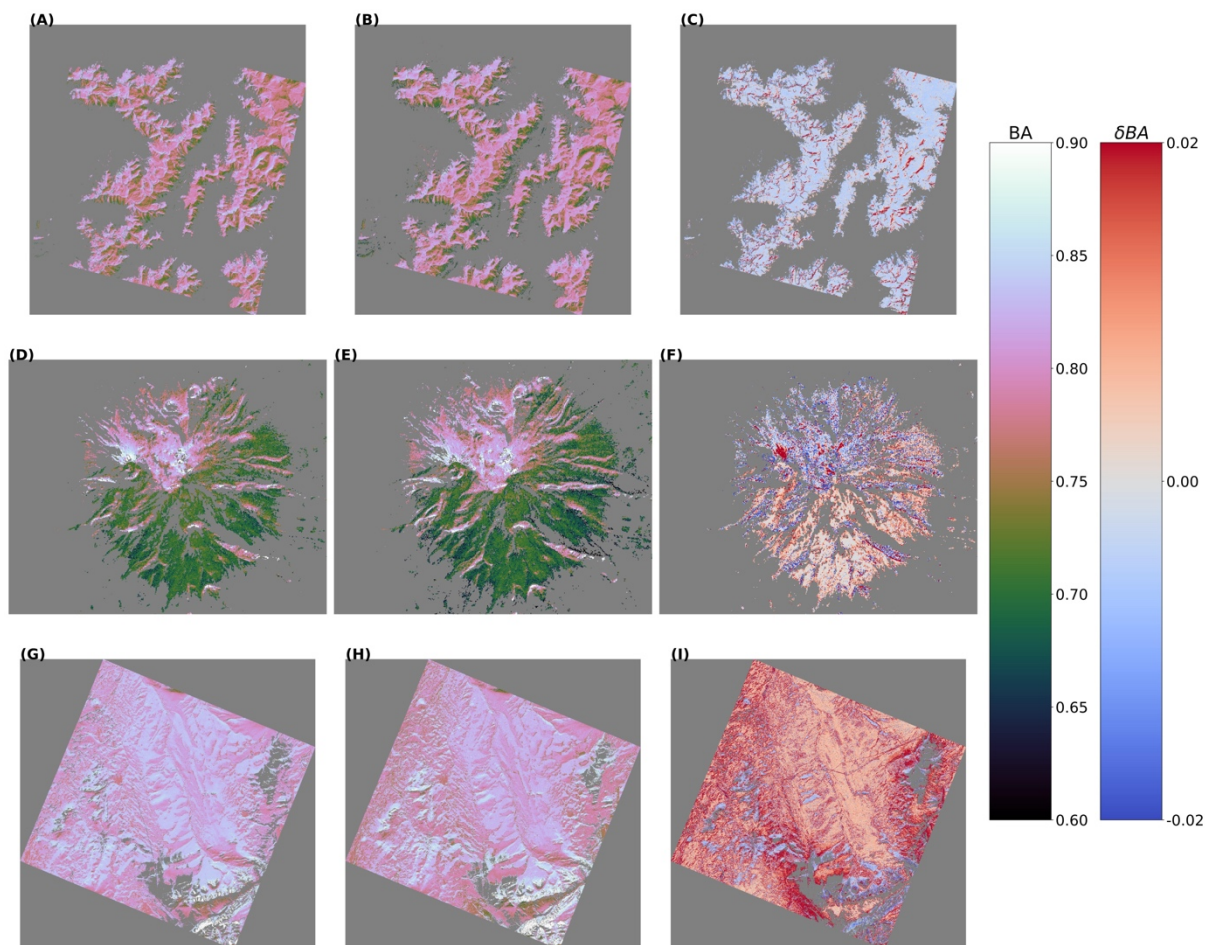


330 calculated as $|\text{Static} - \text{Radiance}|$. This is shown for the San Juan Mountains site (A), Shasta site
331 (B), and Toolik site (C). The average solar zenith angle (θ_0) is shown for reference on each
332 panel.

333

334 We observed a small but notable difference between the methods in derived snow
335 broadband albedo (BA) values (Figure 8). On average the standard deviation between $\text{BA}_{\text{Static}}$
336 $- \text{BA}_{\text{Radiance}}$ (δBA) for the San Juan Mountains site was 0.02, standard deviation for the Shasta
337 site was 0.01, and standard deviation for the Toolik site was 0.02. Generally, there was not a
338 clear bias with respect to μ_s . For the San Juan Mountains site, most of the pixels from the static
339 method showed a consistent small, negative bias of around -0.002. However, for shadier slopes
340 at this site, this bias flipped positive and was much more uncertain at around +0.02.
341 Interestingly, δBA from the Toolik site had the opposite relationship to San Juan Mountains
342 site, where δBA was more positive on sunnier slopes (μ_s approaching 1), and more negative
343 on shadier slopes (μ_s approaching 0), suggesting there could be different mechanisms for
344 which the static method may lead to inaccuracies. The result for the Toolik site confirms the
345 need to model the illumination conditions even in relatively flat terrain, because of implications
346 for net radiative forcing in the cryosphere. The Mount Shasta site δBA had no strong
347 relationship with respect to μ_s .

348



349

350 **Figure 8.** Modelled broadband snow albedo (BA) for San Juan Mountains site (A-C), Shasta
351 Mountain site (D-F), and Toolik site (G-I). Left column represents BA from static method,
352 middle column represents BA from radiance method, and right column represents difference
353 in BA (δBA), which is $BA_{Static} - BA_{Radiance}$. Dark grey colour symbolizes data that is not a
354 value.

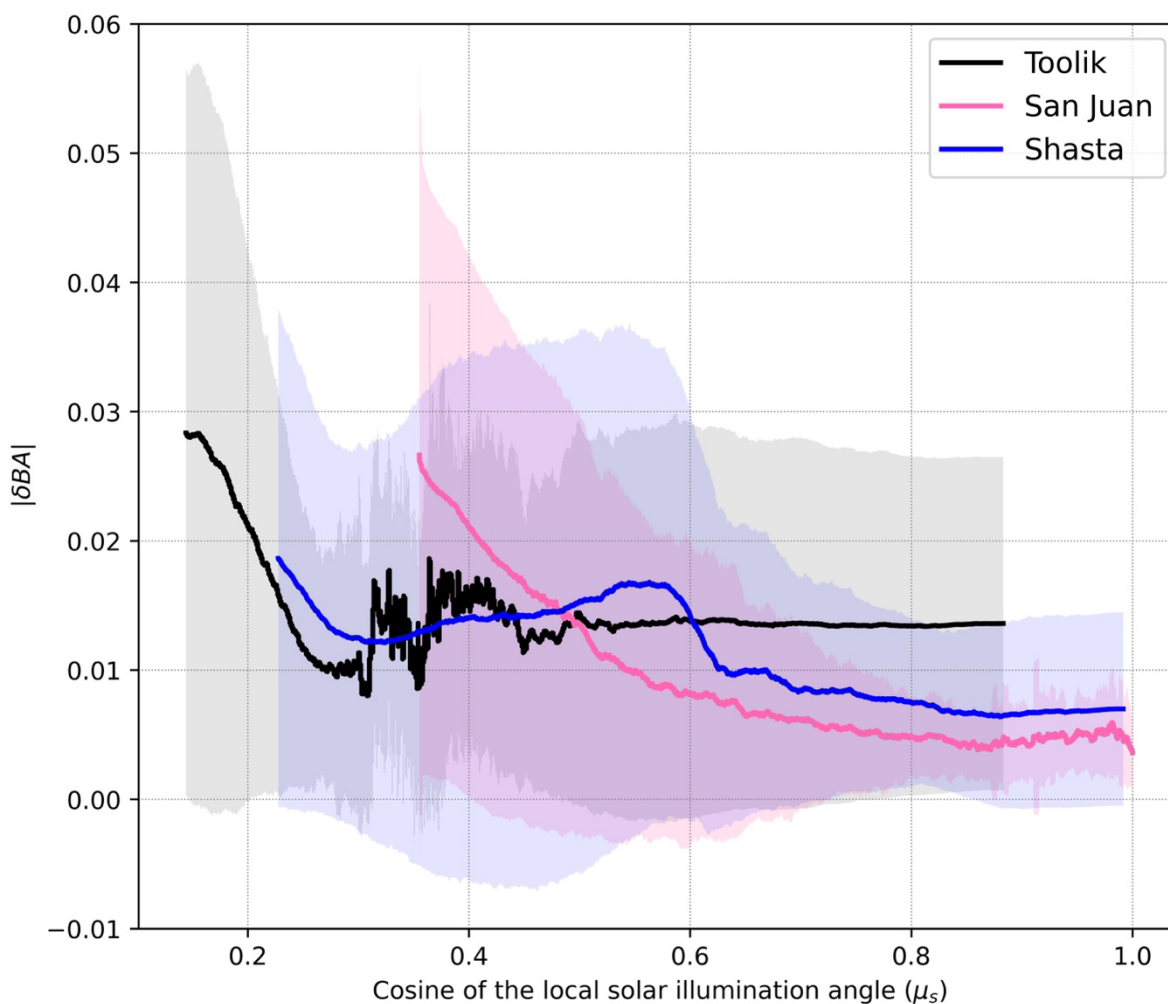
355



356 When plotting moving average of $|\delta BA|$ for all sites with respect to μ_s we found that
357 generally $|\delta BA|$ increased as μ_s approached zero (Figure 9). However, this relation appeared
358 highly non-linear and depended on the site and illumination conditions. For example,
359 standard deviation of $|\delta BA|$ (shown as the shaded regions in Figure 9) for well-lit slopes
360 ($\mu_s > 0.8$) were generally smaller for San Juan site, and conversely were higher for the
361 Toolik site. Similar to Dozier et al. (2022), one can see a monotonic relation with respect to
362 θ_0 across the three sites. This exercise demonstrates the levels of uncertainty left in for static
363 DEM methods, further showing quantitatively the improvements to broadband albedo
364 through using radiance-based approach.

365

366



367

368 **Figure 9.** Modelled absolute difference in broadband albedo ($|\delta BA| = |BA_{Static} - BA_{Radiance}|$)

369 for Toolik (black), San Juan (pink), and Shasta (blue). Note these are plotted using a moving

370 average and binned with respect to μ_s .

371

372

373



374 **4 Discussion**

375 **4.1 Implications in accounting for terrain in snow property retrieval**

376 Derivative slope and aspect maps are prone to errors at 30 m spatial resolutions
377 (Dozier et al., 2022), which become relevant for derived snow products from upcoming
378 missions such as SBG and CHIME which will rely on such topographic information to
379 calculate optical properties like snow albedo so that we can better monitor seasonal
380 snowmelt. These errors can be inherent to the DEM itself, or a product of spatial and
381 temporal misalignments (Carmon et al., 2023). To enable high quality snow products
382 regardless of illumination angles and conditions, we have demonstrated benefits of
383 computing optimal terrain using TOA radiance over snow. This new method is especially
384 useful for steep mountain terrain and/or high latitudes where illumination conditions are
385 suboptimal. The θ_0 (solar zenith angle) was relatively low for the San Juan Mountain site in
386 our study, and thus represents a lower bound of the improvement in accuracy one could
387 expect (Figure 1; Dozier et al., 2022). This disparity was demonstrated further for the Mount
388 Shasta and Toolik sites when θ_0 was larger (i.e. a greater differences in SSA due to more
389 challenging solar and sensor geometry). Even for the relatively flat Toolik site, we showed
390 that correctly accounting for incidence angels can have an impact when θ_0 is large. Our
391 modelled δ BA with respect to the non-coincident DEM was similar to work by Donahue et
392 al. (2023), who found similar uncertainties of δ BA (ranging from -10 to 10%) for their



393 investigation on Place Glacier, British Columbia, Canada. We corroborated with this research
394 showing similar ranges of δBA for our three study sites.

395 This research responds to the objectives stated in “*Thriving on our changing planet: A*
396 *decadal strategy for Earth observation from space*”, to improve biogeophysical modelling at
397 scales driven by topography (National Academies of Sciences, Engineering, & Medicine,
398 2019), enabling more accurate snow property retrievals in the cryosphere under challenging
399 illumination conditions. Our work presented on solving terrain where DEM data are not
400 available or reliable may serve to accelerate improvements to satellite remote sensing tools to
401 monitor and model at both the regional global scale (Sturm et al., 2017), at a critical juncture
402 in time where northern latitudes are changing fast under a warming climate.

403

404 **4.2 Future considerations**

405 While we solved for a few terrain parameters in this study, we did entirely remove the
406 static DEM, even from the radiance method. The elevation from a DEM has a much higher
407 confidence than its derivative products (Dozier et al., 2022). Therefore, we used these values
408 to inform our atmospheric routine, as well as our shadow casting ray tracing module in
409 GOSHAWK (Wilder et al., 2024). Additionally, as stated in Wilder et al. (2024),
410 GOSHAWK used the Dozier & Frew (1981) method for estimating the sky view factor (V_{Ω})
411 based on nearby terrain. This factor could potentially be problematic but was cited as being



412 not as important as μ_s (Dozier et al., 2022). Therefore, we elected to use V_Ω derived from the
413 static Copernicus DEM. However, this could be an area for future improvement, especially in
414 very steep terrain where V_Ω becomes small.

415 Finally, we used a static value for slope derived from Copernicus DEM. The slope
416 influences the μ_s term, but also influences the passive radiation from nearby slopes.
417 Ultimately, we concluded that aspect had the largest impact on changing μ_s (Figure 1), as
418 well as large RMSE reported in previous work (Dozier et al., 2022; Donahue et al., 2023),
419 and thus was the focus of our study. However, future work could investigate other model and
420 optimization configurations to improve upon this study. We recommend additional coincident
421 AVIRIS-NG flights with spaceborne imaging spectroscopy datasets to further this work.

422

423 **5 Conclusions**

424 In this study we have used existing PRISMA imagery to demonstrate the
425 improvements in modelling snow optical properties when explicitly modelling the terrain in
426 the inversion. This presents an interesting concept, that end users who are interested in
427 modelling snow from space, are perhaps better off working with the L1 TOA products, and
428 not using the L2 bottom of atmosphere reflectance products space agencies typically produce.
429 This would especially be true for areas where the surface undergoes rapid change, such as on
430 glaciers. A final thought to consider is the creation of snow optical mapping using a



431 combination of PRISMA, CHIME, SBG, etc. – and that in performing the operation in this
432 way you may create unified snow products that have the same terrain and atmospheric
433 uncertainties.

434

435 *Code Availability.* <https://github.com/cryogars/goshawk>

436 *Author contributions.* B.W. created the GOSHAWK algorithm and updates herein, decided
437 on experiment set-up, and performed the subsequent analysis, as well as being the main
438 article writer. J.M., J.E. and N.G. provided ideas, comments, and supervised the work.

439 *Competing interests.* The contact author has declared that neither they nor their co-authors
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445

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