



¹ Impacts from cascading multi-hazards using hypergraphs: a case ² study from the 2015 Gorkha earthquake in Nepal

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4 Alexandre Dunant^{1*}, Tom R. Robinson², Alexander L. Densmore¹, Nick J. Rosser¹, Ragindra Man Rajbhandari³, Mark
5 Kincey⁴, Sihan Li⁵, Prem Raj Awasthi³, Max Van Wyk de Vries^{6,7}, Ramesh Guragain⁸, Erin Harvey¹ and Simon Dadson⁹

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7¹ Institute of Hazard, Risk, and Resilience and Department of Geography, Durham University, Durham, UK

- 8² School of Earth and Environment, University of Canterbury, Christchurch, New Zealand
- 9³ UN Resident Coordinator's Office, Nepal
- 10⁴ School of Geography, Politics, and Sociology, Newcastle University, Newcastle, UK

11 ⁵ Department of Geography, University of Sheffield, Sheffield, UK

12 ⁶Department of Geography, University of Cambridge, Cambridge CB2 3EL, UK

13 ⁷ Department of Earth Sciences, University of Cambridge, Cambridge CB3 0EZ, UK

14 8 National Society for Earthquake Technology-Nepal (NSET), Nepal

15 9 School of Geography and the Environment, University of Oxford, UK

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- 17
- 18 * Corresponding author: alexandre.dunant@durham.ac.uk
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21 Abstract

22 This study introduces a new approach to multi-hazard risk assessment, leveraging hypergraph theory to model the 23 interconnected risks posed by cascading natural hazards. Traditional single-hazard risk models fail to account for the 24 complex interrelationships and compounding effects of multiple simultaneous or sequential hazards. By conceptualising 25 risks within a hypergraph framework, our model overcomes these limitations, enabling efficient simulation of 26 multi-hazard interactions and their impacts on infrastructure. We apply this model to the 2015 M_w 7.8 Gorkha 27 earthquake in Nepal as a case study, demonstrating its ability to simulate the primary and secondary effects of the 28 earthquake on buildings and roads across the whole earthquake-affected area. The model predicts the overall pattern of 29 earthquake-induced building damage and landslide impacts, albeit with a tendency towards over-prediction. Our 30 findings underscore the potential of the hypergraph approach for multi-hazard risk assessment, offering advances in 31 rapid computation and scenario exploration for cascading geo-hazards. This approach could provide valuable insights 32 for disaster risk reduction and humanitarian contingency planning, where anticipation of large-scale trends is often more 33 important than prediction of detailed impacts.

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35 Keywords

36 Cascading multi-hazards, multi-hazard modelling, earthquake impacts, landslides, Nepal, network modelling,37 hypergraphs





38 1. Introduction

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40 There is a growing recognition over the last 15 years that natural hazards can interact and occur in conjunction with 41 each other, leading to a potential compounding effect that is greater than the sum of the single-hazard impacts (Kappes 42 et al., 2012; Terzi et al., 2019). While the global prevalence of cascading hazards specifically is difficult to quantify 43 reliably, there are increasing calls for effective multi-hazard risk assessments (e.g., Ward et al., 2022). Multi-hazards are 44 defined by UNISDR (2016) as "events [that] may occur simultaneously, cascadingly or cumulatively over time, and 45 taking into account the potential interrelated effects". Multi-hazard approaches seek to overcome the limitations of a 46 narrower focus on single-hazard models, which are unable to account for the observed inter-relationships between 47 different hazards as well as potential compounding or cascading effects (e.g., Gill and Malamud, 2014; Tilloy et al., 48 2019; Dunant, 2021; Ming et al., 2022). Multi-hazard approaches to risk are now widely encouraged (e.g., UNISDR, 49 2005; Government Office for Science, 2012) and are increasingly integrated into risk assessment (see recent reviews by 50 Gill et al., 2022; Ward et al., 2022).

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52 There remain, however, some important challenges and limitations with multi-hazard risk assessment. Because of the 53 difficulties in recognising, understanding, and defining the inter-relationships between hazards, and the lack of data on 54 their co-dependence (Tilloy et al., 2019; Hochrainer-Stigler et al., 2023), most 'multi-hazard risk' models simply 55 overlay single hazards without considering their interactions - an approach that Gill and Malamud (2014) termed 56 'multi-layer single hazard'. Even when hazard-hazard interactions are considered in risk models, there is still a lack of 57 comprehensive approaches that capture the intricate interplay among hazards, exposure, and vulnerability beyond 58 simple spatial overlaps (Mignan et al., 2014; de Ruiter et al., 2020). These interactions are critical because of the 59 possibility that risks may be clustered in space and time or may amplify each other, as demonstrated by Mignan et al. 60 (2014). Zschau (2017) extended the ideas of Gill and Malamud (2014) to risk assessment, distinguishing between risk 61 from single hazards, risk from multi-layer single hazards, and risk from multi-hazards - the latter allowing for dynamic 62 hazard interactions, but no dynamic interactions between hazard and exposure or vulnerability). Hochrainer-Stigler et 63 al. (2023) noted that hazard-exposure relationships and changes in exposure over time, as well as vulnerability, are also 64 critical to fully characterise multi-risks. This complexity means that multi-hazard risk modelling can be both 65 computationally expensive and extremely demanding of quality input data (e.g., Kappes et al. 2012). Multi-hazard risk 66 models may also be limited by the diversity of hazard types that can be incorporated, mismatches in the appropriate 67 spatial and temporal scale of analyses, and complex data requirements (e.g., Kappes et al., 2012; Tilloy et al., 2019; 68 Dunant, 2021).

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70 A further complication is the growing need for national, regional, or even global-scale risk assessments, in order to 71 understand potential patterns of impacts, provide science-based evidence for disaster risk reduction and advocacy, and 72 allow coordinated planning (see review by Ward et al., 2020). At the same time, data are available at ever-increasing 73 spatial and temporal resolution, including information on populations, building stock, and topography, as well as 74 datasets on hazard drivers such as rainfall forecasts or observed precipitation. While these are welcome developments, 75 the combination of demands for increasing scale and increasingly-fine spatial and temporal resolution data leads to a 76 much higher computational burden. Addressing the need for both larger spatial scales and finer spatio-temporal 77 resolutions is a growing challenge for the assessment of multi-hazard risks. The distribution of risk may also be highly 78 spatially imbalanced if exposed elements are concentrated in specific areas, meaning that grid-based or GIS-based 79 approaches to risk modelling may expend much computational effort on areas where risk is low or negligible.





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81 To address these concerns, Dunant et al. (2021a) proposed a novel approach to multi-hazard risk modelling using graph 82 theory. In this framework, both the hazards and the elements at risk are modelled as a set of interconnections between 83 nodes. For example, a house can be linked to ground accelerations in an earthquake, or a hillslope to rainfall in a storm. 84 This framework can then be used to generate many disaster scenarios by cascading from node to node according to a set 85 of rules (e.g., a threshold earthquake shaking value for slope failure). The resulting network model is highly 86 computationally efficient, and the network structure is a natural fit to the simulation of coincident or cascading events 87 and their propagation through exposure networks (Dunant et al., 2021a) because network structures are purposefully 88 designed to capture the interdependencies and feedbacks among different elements. The framework is agnostic to the 89 types of objects that can be included, so it can be easily adapted to include hazard-hazard, hazard-exposure, and 90 hazard-vulnerability relationships. It is also highly flexible, so that the links between objects can be represented via 91 different interactions depending on the level of understanding and data availability, including threshold values, 92 empirical functions, fuzzy distributions, process models, or other approaches (e.g., Tilloy et al., 2019).

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94 Despite its advantages, however, the network model suffers from some important limitations. Most critically, because 95 the interactions in a network model are modelled as pairs, the computational burden grows substantially as the number 96 of components (nodes and edges) of the model increases. Prior applications focused on the epicentral area of the 2016 97 M_w 7.8 Kaikõura earthquake (Dunant et al., 2021a) and the area around Franz Josef township (Dunant et al., 2021b), 98 both in New Zealand and containing on the order of hundreds of nodes. Expanding the network model to a national 99 scale at a similar resolution would increase the model size by several orders of magnitude. Similarly, increasing the 100 number of hazards that are considered would lead to a combinatorial increase in interactions and rapid growth in 101 computation time.

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103 Here we propose a new approach to modelling the impacts of multi-hazards using hypergraphs – two-dimensional 104 surface equivalents of the pairwise links found in the graph-theory network model of Dunant et al. (2021a). The 105 hypergraph model retains the advantages of the network approach while simultaneously reducing the model complexity. 106 Below, we first present a brief review of graphs and hypergraphs and outline the benefits of using hypergraphs in a 107 multi-hazard risk modelling framework. We describe the structure of the multi-hazard impact model, including its 108 components and the interactions between nodes. We illustrate its application by simulating the impacts from the 2015 109 M_w 7.8 Gorkha earthquake in Nepal, as an exemplar of a large-scale event that had cascading effects on people and 110 infrastructure due to both primary and secondary hazards. We close by considering wider potential applications of the 111 hypergraph model, including national- or regional-scale disaster scenario ensembles and how they might be used to 112 support humanitarian contingency planning (e.g., Robinson et al., 2018).

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2. Summary of graph and hypergraph approaches

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116 A graph is essentially a mathematical representation of a network. The term was originally introduced by Sylvester 117 (1878) but graph theory had been used more than a hundred years before by Euler (1736) to solve the Seven Bridges of 118 Königsberg problem. Since then, graph theory has been used in a wide variety of fields such as geography, computer 119 science, social science, and biology (e.g., Buzna et al., 2006; Chorley & Kennedy, 1971; Dezső & Barabási, 2002; 120 Dorogovtsev & Mendes, 2003).





122 A graph comprises a set of nodes connected by edges. In the context of risks posed by environmental hazards, such
123 nodes may represent a geographical location (spatially explicit; e.g., a fault segment, or a house) or a nominal property
124 (spatially implicit; e.g., the occurrence of an earthquake) and the edges represent the relations between the nodes (e.g.,
125 earthquake shaking affecting exposed houses) (Fig. 1A).





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128 Figure 1: Graph (A) and hypergraph (B) representations of a hypothetical set of hazard and exposure interactions. The same 129 set of elements are represented in both graphical form (top) and tabular form as incidence matrices (bottom). In the tables, a 130 blank cell means no interaction between the nodes, and a value of 1 means that interactions are possible between the nodes.

132 A defining characteristic of graphs is the set of pairwise connections or edges between nodes that define the 133 relationships between these nodes. For example, we would represent earthquake shaking on a set of hillslopes as edges 134 between the earthquake and each hillslope that is affected. In tabular form, each edge is represented by a row in a 135 relational database, called an incidence matrix (Fig. 1A). The edges are directional, so a two-way relationship – for 136 example, a hillslope potentially affecting a road via landslides, and a road potentially affecting a hillslope via excavation 137 and steepening – would be represented by two separate rows.

138

139 As summarised by Dunant et al. (2021a), here we consider relationships between nodes that are observed or felt – that 140 is, via shaking, mass movement, or water flow. We also consider that nodes are connected if (1) the geographical effect 141 of one node overlaps that of another, and (2) that effect is relevant to considering impacts from hazards. For example, 142 earthquake ground shaking might affect a hillslope and trigger a new landslide or the mobilisation of loose material in a 143 debris flow; to allow for these effects, we would represent the relationship between earthquake and the hillslope as an 144 edge, and the relationship between the hillslope and any houses or road segments on it as a series of additional edges 145 (Fig. 1A). If we were to assume that the earthquake ground motion can potentially cause direct impacts on houses but 146 not roads, then the earthquake would be connected to the houses by edges but not to the road segments (Fig. 1A).

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148 In contrast, a hypergraph is a special type of graph where the edges, called hyperedges, can link one or more nodes (Fig. 149 1B). This allows us to represent interactions that extend beyond a single pair of nodes (Wolf et al., 2016). Compared to 150 pairwise edges, which only connect two nodes, hyperedges can connect multiple nodes and provide a more natural 151 representation for the spatial overlap between exposed elements, like houses, and geographical hazard footprints. 152 Hyperedges can thus represent nested information between the nodes of the system, such as their properties or locations, 153 with far fewer tabular entries (Fig. 1B). The hypergraph uses fewer edges to represent the same number of interactions 154 for a given number of nodes; this size difference (e.g., for the example in Figure 1, 11x8=88 entries for the graph 155 framework and 3x8=24 for the hypergraph framework) highlights the efficiency of the hypergraph approach.

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157 The increased efficiency enabled by hypergraphs becomes more apparent when dealing with large, interconnected 158 datasets and when iterative data manipulation is required. For example, we can run hundreds or thousands of separate 159 simulations on the same hypergraph, choosing different events or altering input parameters within a Monte Carlo 160 framework (e.g., Dunant et al., 2021a) to generate ensemble distributions of scenario outcomes (Robinson et al., 2018). 161 The improvement in computation time allows the hypergraph framework to be applied to multi-hazards risk assessment 162 over larger extents, over longer time periods, and with more complex interactions than would be feasible using a 163 GIS-based approach or standard graph framework.

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3. Methodology

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167 Below we describe the setup and operation of the multi-hazard hypergraph model and describe its application to the168 2015 Gorkha earthquake.

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170 3.1 Model overview and setup

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172 The model is based around a set of interactions between elements in Nepal that are drawn from experience in both the 173 annual monsoon (Kincey et al., 2022; Jimee et al., 2019; Goda et al., 2015; Rosser et al., 2021; Kargel et al., 2016) and 174 recent earthquakes, including the 2015 Gorkha event (e.g., Roback et al., 2018; Milledge et al., 2019; Kincey et al., 175 2021). For the simulations in this paper, the model is driven only by earthquakes (Fig. 2) and seeks to assess the risk to 176 buildings and roads at a national scale. Earthquake shaking is simulated as a spatial distribution of peak ground 177 acceleration (PGA) values; these could be derived from measurements or generated for a potential scenario earthquake 178 via a shaking model. For the experiments shown here, we use empirical PGA values estimated by the US Geological 2015 earthquake 179 Survey Shakemap for the Gorkha 180 (https://earthquake.usgs.gov/earthquakes/eventpage/us20002926/shakemap/pga). Earthquake shaking can affect 181 infrastructure either directly (described via a set of fragility functions) or by triggering landslides. Landslides, in turn, 182 may affect both buildings and roads. In this version of the model, other hazards such as rainfall and floods are not 183 considered, but they could be added via additional sets of hyperedges and interactions.







186 Figure 2: Driving stimuli and important process interactions for the area affected by the 2015 Gorkha earthquake in Nepal.187 The elements that are included in the multi-hazard impact experiments documented here are shown in **bold text**.

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189 To model coseismic landslides, we subdivide the landscape into discrete units and consider the characteristics of the 190 topography as well as the driving mechanisms within those subdivisions. Here we divide the landscape into slope units 191 that are bounded by drainages and divide lines (Alvioli et al., 2016; Woodard et al., 2024) (see Supplemental 192 Information and Fig. S1). Woodard et al. (2024) demonstrated that slope units are preferable to gridded topography 193 when representing landslide susceptibility, especially for input landslide data that are imprecise or highly spatially 194 variable in quality.

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196 The hyperedges are constructed based on the interactions in Figure 2. A hyperedge connects the earthquake node with 197 all of the slope units and buildings within the 'footprint' of the earthquake, defined by the extent of a minimum PGA (X 198 g) contour. Similarly, hyperedges connect each slope unit with the buildings and roads (divided into 100 m segments) 199 within it; we therefore assume that landslides from one slope unit cannot impact elements in another. Attributes for each 200 building, road segment, and slope unit, such as location, PGA, building type, landslide susceptibility, are stored on the 201 hyperedges and can be displayed as continuous values in a tabular form. We describe each of these attributes below.

203We use building locations and roads taken from the Humanitarian OpenStreetMap Team, covering the whole of Nepal,204andavailableat205https://data.humdata.org/dataset/hotosm_npl_buildingsand206https://data.humdata.org/dataset/hotosm_npl_roads, respectively (accessed 1 January 2021). The datasets contain c. 7.1206million building polygons and c. 3 million road segments. Because we lack specific information on the construction207type of each building to assess its fragility, we instead use exposure data from the Modeling Exposure Through Earth208ObservationRoutines (METEOR) project (https://maps.meteor-project.org/map/building-exposure-map-of-nepal)209(version 2020-02-15), which includes a list of building types and the number and value of each type within each cell of210a 90 x 90 m grid across Nepal. The PGA value of the 2015 Gorkha earthquake is extracted at the centroid of each211METEOR grid cell. To account for variability in construction detail and quality within these broad types, we adopt low,

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212 middle, and high fragility functions for the 'complete damage' state for typical building types in Nepal from the 213 METEOR dataset (Fig. 3). We take the definition of 'complete damage' from the Hazus framework of the US Federal 214 Emergency Management Agency (FEMA, 2020). We generate a weighted-average fragility function for the buildings 215 within each 90 x 90 m grid cell based on the proportion of different building types; thus, in the absence of any 216 national-scale building-specific information, all buildings within that cell are assumed to have the same average 217 fragility. We assess the likelihood of 'complete damage' because this implies loss of usability or habitability, with 218 consequences for displacement and disruption to life and livelihoods, and is typically used to estimate fatality and injury 219 rates (FEMA, 2020).







222 Figure 3: Fragility functions used in the hypergraph network modelling. Each panel shows fragility curves for a different 223 building type in the METEOR dataset, and which relate the peak ground acceleration (PGA, in g) to the probability of being 224 reduced to a complete damage state. Note that each sigmoidal fragility curve is defined by two parameters: a mean or scale 225 parameter that sets the PGA value for a 50% probability of complete damage, and a standard deviation (std) that defines the 226 spread of the curve. Parameter values and sources for the fragility curves are included in the plots.

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228 We estimate landslide susceptibility based on topographic factors alone, using a seven-parameter static susceptibility 229 model that incorporates elevation, hillslope aspect, distance to rivers, plan-view curvature, regional relief, local hillslope 230 gradient, and a terrain ruggedness index. These factors are derived from a 10 m digital elevation model (DEM) that was 231 downsampled from the 5 m Advanced Land Observing Satellite World 3D DEM 232 (https://www.aw3d.jp/en/products/standard/). We generate the susceptibility model using a gradient boosting machine 233 learning approach, XGBoost, implemented in Python. For the experiments shown here, the susceptibility model is 234 trained on the locations of coseismic landslides triggered by the 2015 Gorkha earthquake as mapped by Kincey et al. 235 (2021), yielding an area under the receiver operating characteristic (ROC) curve of 0.75 (Fig. S2). We stress that this 236 susceptibility layer is used simply as an exemplar which is optimised for the 2015 Gorkha earthquake; for other model 237 applications, susceptibility data generated with other approaches (see review in Reichenbach et al., 2018), or trained on 238 different inventories, could be substituted. Because landslide susceptibility is modelled on a 10 x 10 m grid, each slope 239 unit contains a unique distribution of cell-wise susceptibility values in the range [0,1], and each building polygon or 240 road segment overlaps with one or more cellwise susceptibility values. Importantly, because the multi-hazard model is 241 intended to simulate dynamic cascading scenarios, we choose not to include earthquake shaking as a determining factor 242 in the static landslide susceptibility model. This choice preserves independence between shaking, landslide triggering, 243 and the propagation of hazards along the hyperedges within the model.

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245 We extract the mean and standard deviation of susceptibility for each slope unit, building and road segment, although 246 other measures of the distribution could also be used. Because we lack general building or road fragility functions for 247 landslides that are comparable to those for earthquakes and that encompass the wide range of possible landslide types 248 and sizes (see Luo et al., 2023, for a recent review), we adopt a simplified binary vulnerability model, such that any 249 building or road that is affected by a landslide is considered as 'impacted'.

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251 3.2 Simulation steps

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253 In each simulation, the model works iteratively through the hyperedges that connect the driving stimulus of earthquake 254 shaking to the other elements in the model, checking against a condition to see whether that hyperedge of the network is 255 'activated' – i.e., a building is damaged by earthquake shaking, or a slope unit is affected by one or more landslides. 256 Activation of that hyperedge then allows the stimulus to propagate, and potentially to cascade along other hyperedges if 257 further conditions are met (Fig. 4). The simulation continues until all cascades stop and no further impacts are possible. 258







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260 Figure 4. Step-by-step overview of the hypergraph framework for modelling cascading multi-hazard impacts. The 261 hypergraph is represented in a simplified example on the left and the algorithm steps are specified on the right. The 262 simplified hypergraph assumes a landscape with two slope units, each of which contains two buildings and two road 263 segments. The causal cascades of the algorithm are represented in three steps; from top to bottom, these are (1) earthquake 264 shaking, (2) tests for 'activation' of a hillslope and 'triggering' of landslides, and (3) tests for impacts on structures by 265 landslides. In the simplified hypergraph, black outlines show the hyperedges where hazards occur (e.g., landslides are 266 triggered by the earthquake), and the nodes that are damaged by either shaking (step 2) or landsliding (step 3). The process is 267 embedded in an iterative Monte Carlo simulation to determine the uncertainty associated with each step, creating a series of 268 disaster scenarios that can be queried for further analysis.

269

270 In the experiments shown here, the first step is to work through the hyperedge that connects the earthquake to the 271 individual buildings to assess their damage state. For each building, we assign the PGA value at the centroid of its 90 x 272 90 m METEOR grid cell. We use the high, middle, and low weighted mean fragility functions for that grid cell to 273 determine the likelihood of that building being completely damaged – which is equivalent to the proportion of buildings 274 within that 90 x 90 m grid cell in the METEOR dataset that is completely damaged. This likelihood of complete damage 275 [0,1], reproduces the weighted mean fragility when applied over the METEOR grid cell. The low, middle, and high 276 cases provide a range of outcomes for an individual building at a specific PGA value. The per-building likelihoods of 277 complete damage under the three cases can then be summed by slope unit or administrative area to give the total 278 predicted number of completely-damaged buildings in each area.

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280 Next, we assess which slope units are 'activated' by ground shaking (Fig. 4). Activation of a slope unit means that the 281 ground accelerations are high enough to potentially trigger one or more landslides, if this is permitted by the 282 topographic conditions as represented by the landslide susceptibility. Again, this allows the stimulus to propagate within 283 the earthquake hyperedge to the slope unit, and potentially to cascade within that slope unit (and affect buildings or road 284 segments within it). In these experiments, we conduct a logistic regression between PGA and the locations of landslides 285 in the inventory of coseismic landslides triggered by the 2015 Gorkha earthquake (Kincey et al., 2021) to define the





286 regional-scale probability of landslide occurrence as a lognormal function of PGA (see Supplemental Information and 287 Fig. S3). We calculate the mean PGA value within each slope unit, and use that to determine the corresponding 288 probability of landsliding within the slope unit from the lognormal function. That probability, in turn, is compared with 289 a uniform random deviate to determine whether each slope unit is activated or not. Thus, over large numbers of 290 simulations, slope units with more observed coseismic landslides will be activated more frequently, but the exact pattern 291 of activations in each individual simulation – and thus the portion of the hypergraph network that is sampled – will vary. 292

293 For all slope units that are activated, the model proceeds to subsequent hyperedges to assess whether buildings or road 294 segments are affected by direct landslide occurrence (Fig. 4). In the experiments shown here, this is a two-step process. 295 We first check if a landslide occurred within the slope unit. Even if the shaking was strong enough to potentially trigger 296 a landslide (i.e., the slope unit was 'activated'), it might still have a low likelihood of experiencing landsliding due to 297 low susceptibility (i.e., it was not 'triggered'). Triggering in the slope unit is determined by drawing a value (A) from a 298 Gaussian distribution of landslide susceptibility with the same mean and standard deviation as the distribution of 299 susceptibility values in that slope unit, and comparing that value with a uniform random deviate (B). We employ a 300 Gaussian distribution for efficiency, as this can be calculated in advance of the simulation, and note that it provides a 301 reasonable fit to the actual distribution across a wide range of slope units (Supplemental Information, Fig. S4). If the 302 susceptibility value A is smaller than B, then no landslide has occurred in that slope unit, and propagation along that 303 hyperedge stops. If A is larger than B, then one or more landslides has occurred in that slope unit. We then check if each 304 building and road segment within the slope unit is affected by this landsliding by comparing the landslide susceptibility 305 value at the infrastructure location with another uniform random deviate. If the random deviate exceeds the landslide 306 susceptibility value, then the building or road segment remains unaffected by the landslide (in other words, even if a 307 landslide happens in the slope unit, it doesn't affect the building or road). Then, the simulation continues to evaluate 308 other buildings or roads within the same slope unit, and then moves on to other slope units activated by the earthquake. 309 If the random deviate is less than the susceptibility value, then the building or road segment is impacted by landsliding. 310 In this case, we add it to the pool of affected elements for this simulation and move to the next building or road. We 311 continue this process to search iteratively through all slope units in the network to generate a single cascading impact 312 scenario.

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314 3.3 Outputs and evaluation

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316 The iterative simulation process outlined above is repeated within a Monte Carlo framework to create an ensemble of 317 scenarios, each of which explores a different set of outcomes within the same set of hyperedges. In the experiments 318 shown here, we generate 10,000 scenarios from the initial stimulus of the 2015 Gorkha earthquake. Hence, all scenarios 319 in these experiments use the same spatial distribution of PGA values and thus the probability of an individual building 320 suffering complete damage by shaking stays the same. What differs between scenarios are the details of which slope 321 units are activated, which slope units experience landsliding, and which buildings or road segments are impacted by 322 those landslides. Thus, we take the likelihood of a structure being affected by landsliding over the whole ensemble as 323 the proportion of the 10,000 scenarios in which the structure is impacted. This leads to a shaking impact likelihood and 324 a landslide impact likelihood, both in the range [0,1], for each of the buildings and road segments in our combined 325 dataset.





327 To explore the trade-off between spatial resolution and model performance, we aggregate the structure-level results over 328 successively larger administrative units. Nepal is divided, from smallest unit to largest, into 6,743 wards, 753 urban and 329 rural municipalities, 77 districts, and 7 provinces. Aggregation across these units allows us to evaluate the performance 330 of the model against independent measures of earthquake impacts from the 2015 Gorkha earthquake at different spatial 331 resolutions. For buildings damaged by earthquake shaking, we evaluate the model in two ways. First, we sum up the 332 per-building likelihoods of complete damage in each district for the low, middle, and high fragility estimates - which 333 yields the number of completely-damaged buildings in each case - and compare those sums to incident reports 334 summarising the number of "fully damaged" buildings per district and published on the Government of Nepal's Bipad 335 Portal (http://drrportal.gov.np/ - see also Chaulagain et al., 2018) based on the Post-Disaster Damage and Needs 336 Assessment (PDNA) (National Planning Commission, 2015). This assesses the ability of the model to estimate the 337 absolute number of damaged buildings. While this data remains the most extensive for validation purpose, the PDNA 338 was done urgently after the disaster with limited systematic gathering hence it relies on judgement by the PDNA 339 participants and, therefore, carry significant uncertainty (Lallemant et al., 2017). Note that wards and municipalities 340 were defined in the federal restructuring of Nepal in 2017, and so data on damaged buildings from the 2015 earthquake 341 are not available at ward or municipality level. Second, we take the mean likelihood of complete damage in each 342 district, in the range [0,1], and compare that with the presence or absence of damaged buildings in each of the 77 343 districts. This second measure is independent of the absolute number of buildings, and gives information instead on the 344 ability of the model to anticipate the occurrence of one or more completely damaged buildings in an area. 345

346 For structures impacted by landslides, we derive similar statistical measures for model evaluation. First, we sum up the 347 per-structure likelihoods of landslide impact over successively larger areas of aggregation - ward, municipality, district, 348 and province. Because there are no systematic published data on observed landslide impacts on buildings and roads in 349 the 2015 earthquake, we generate an estimate of affected structures by overlaying the coseismic landslide polygons 350 from Kincey et al. (2021) on our building and road dataset; all structures that intersect with a mapped landslide polygon 351 are assumed to have been impacted by landsliding in the earthquake. Note that this measure of landslide impacts does 352 not consider the significant post-earthquake changes in landslide footprint and debris runout (e.g., Tian et al., 2020; 353 Kincey et al., 2022). Also, the coseismic landslides were mapped on medium-resolution satellite imagery (c. 10 m, 354 equivalent to our DEM and derived topographic metrics) and so will have omitted small landslides or rockfalls, 355 especially in areas of dense vegetation or steep topography (e.g., Williams et al., 2018); this error and the inherent 356 uncertainty in mapped landslide outlines (Kincey et al., 2021) mean that our estimate of the number of 357 landslide-affected structures is likely to represent a lower bound. We then sum the observed number of impacted 358 buildings and road segments by administrative area to compare with our modelled totals. We also compare the mean 359 likelihood of landslide impact, averaged by administrative area and ranging from [0,1], with the presence of absence of 360 landslide impacts in that area. We evaluate the relationship between these parameters with the area under the ROC 361 curve and the F1 score.

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363 4. Results

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365 4.1 Impacts from earthquake shaking

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367 We first consider modelled impacts from earthquake shaking alone. Unsurprisingly, the probability of complete damage 368 per building, or equivalently the proportion of completely-damaged buildings within each 90 x 90 m exposure grid cell,





369 closely matches the estimated PGA contours from the Gorkha earthquake (Fig. 5A). There are particularly high 370 probabilities in the hill and mountain districts, especially to the east and northeast of Kathmandu, where the values 371 exceed 0.7. Notably, these values generally increase to the north and this increase is cut off only by the lack of buildings 372 above elevations of around 3,500 m in northern Nepal (visible as the white areas in Fig. 5A). The Kathmandu Valley 373 itself yields a low proportion of completely-damaged buildings, despite moderately high PGA values, due to the 374 preponderance of less-fragile building types.

375

We convert the proportion of completely-damaged buildings per grid cell into a sum total aggregated over municipalities (Fig. 5B) and districts (Fig. 5C). These totals reflect the PGA pattern and the weighted mean fragility functions, but importantly also the number of buildings within each administrative area. When aggregated by municipality, the largest modelled totals tend to occur in the more densely-populated Middle Hills in the vicinity of kathmandu, rather than the more sparsely-populated north. There are some notable exceptions to this pattern, such as Bharatpur to the south of the earthquake epicentre (Fig. 5B), which combines a large stock of fragile building types with moderately high PGA values. When aggregated by district, the largest modelled totals are again dominated by areas with both large numbers of buildings and moderate to high PGA values (Fig. 5C). With the exception of Chitwan to the south of the epicentre, the largest totals are found in districts where PGA exceeded 0.4 g. It is instructive to compare the aggregated pattern by district to the actual numbers of completely-damaged buildings (Fig. 5D). There are broad similarities between modelled and observed totals, especially in the hill and mountain districts of Sindhupalchok, Nuwakot, and Kavrepalanchok. Notably, the model over-predicts the impacts in districts close to the epicentre, see including Gorkha and Chitwan, and under-predicts the impacts at the eastern margin of the rupture in Dolakha (Fig. SD).







392 Figure 5: Modelled building impacts from shaking in the 2015 Gorkha earthquake. In all panels, the red contours show the 393 estimated PGA values from the earthquake in g. Note that these results are derived from the middle-case fragility functions in 394 Fig. 4. A, modelled probability of complete damage for individual buildings across the country. This is equivalent to the 395 proportion of completely-damaged buildings in each 90 x 90 m grid cell in the METEOR exposure dataset. B, modelled sum 396 total of completely-damaged buildings aggregated by municipality. C, modelled sum total of completely-damaged buildings 397 aggregated by district. D, actual sum of reported "fully damaged" buildings aggregated by district. Note similar colour scales 398 in panels C and D.

399

400 To better visualise the agreement between modelled and observed totals of completely-damaged buildings, we compare 401 the observed totals for all 77 districts in Nepal with model results using the high, middle, and low fragility cases (Fig. 402 6A). For most districts with non-zero impacts, the observed totals fall within the range of model results using the 403 different fragility curves, with a slight bias toward model over-prediction (Fig. 6B). Among the top 15 districts in terms 404 of modelled impacts, observed impacts fall below that range in three districts (Chitwan, Tanahu, and Kaski; see Fig. 5C 405 for locations), within that range in 11, and above that range in only one (Dolakha). Alternatively, out of the '14 406 worst-affected districts' identified by the Government of Nepal, observed impacts fall within the range of model results 407 in thirteen districts, with Dolakha being the only outlier. The model thus appears to be somewhat conservative in that it 408 slightly over-predicts building impacts due to shaking in the 2015 earthquake. The mismatch between modelled and 409 observed totals is not clearly related to building typologies (Fig. 6C). There may be a weak correlation with shaking;





410 districts with significant over-prediction tend to be those with lower mean PGA values (typically <0.44 g) while 411 Dolakha has a larger mean PGA (0.59 g), and we explore this point in the Discussion.





413

414 Figure 6: A, comparison of modelled and observed numbers of completely-damaged buildings per district in the 2015 Gorkha 415 earthquake. Bars show the range of modelled results for each district using high and low fragility cases (see Fig. 4), with the 416 middle case shown by the black arrow. Red dots show the reported numbers of "fully damaged" buildings. Blue numbers 417 show the mean PGA for each district, in g. The inset shows the same quantities with a logarithmic y-axis scale. B, mismatch 418 between observed (D_{obs}) and modelled (D_{mod}) numbers for each district, normalised by the total number of buildings in that 419 district (N). Negative values indicate model over-prediction, while positive values indicate model under-prediction. Note that 420 impacts in most of the districts with non-zero damage values are slightly under-predicted. C, proportion of different building 421 types in each district from the METEOR exposure data set. There is no clear correlation between the residuals in panel B and 422 the dominant building types.

423

424 4.2 Impacts from coseismic landslides

425

426 As with shaking damage, the modelled probability of a building (Fig. 7A) or road segment (Fig. 7D) being impacted by 427 a coseismic landslide scales with PGA; this is simply a consequence of the assumed relationship between PGA and 428 landslide triggering (Fig. S3). Higher probability values are found in northern areas of Nepal, where landslide





429 susceptibility is elevated (Fig. S2). We aggregate these probabilities to estimate the number of impacted buildings and 430 road segments at the municipality (Fig. 7B, E) and district (Fig. 7C, F) levels. The regions experiencing the highest 431 predicted impacts closely align with those observed, notably concentrated in Sindhupalchok district, where both 432 modelled and observed landslide impacts are most prevalent (Fig. 7C, F). Again, these areas predominantly lie in 433 northern Nepal where susceptibility to landslides is greatest, contrasting somewhat with the distribution of modelled 434 shaking damage. This disparity may stem from the higher and more widely dispersed density of buildings in the 435 southern regions. Consequently, while shaking-related damage appears diffuse, landslide-related damage is more 436 focused in specific regions due to localized exposure. Importantly, the model anticipates approximately an order of 437 magnitude fewer building impacts from landslides as compared to those damaged by shaking (note the scale difference 438 between Figs. 5 and 7). We also note that, while the overall spatial patterns of modelled building and road impacts are 439 similar, the model predicts somewhat higher numbers of road impacts (by about 50%), and that this generally matches 440 the observed differences in intersections between these infrastructure types with coseismic landslides (Fig. 7). Roads are 441 typically sited along or near valley floors, thus increasing their exposure to landslides. Additionally, there is a 442 significant association between roads and landslides (e.g., Hearn and Shakya, 2017; McAdoo et al., 2018), suggesting 443 that the interaction between landslides and roads may cover a broader spatial extent compared to the relationship 444 between landslides and buildings.











447 Figure 7: Modelled structural impacts from coseismic landslides in the 2015 Gorkha earthquake. In all panels, the red 448 contours show the estimated PGA values from the earthquake in g. The red crosses show observed landslide impacts on 449 buildings (left column) and road segments (right column), derived by mapping the intersections between those structure 450 locations and the coseismic landslide inventory of Kincey et al. (2021). A, modelled probability of impact for individual 451 buildings across the country. B, sum of per-building probabilities aggregated by municipality, of which there are 753 in 452 Nepal. C, sum of per-building probabilities aggregated by district, of which there are 77 in Nepal. D, modelled probability of 453 impact for individual 100 m road segments across the country. E, sum of per-road segment probabilities aggregated by 454 municipality. F, sum of per-road segment probabilities aggregated by district.

455

456 The correlation between the modelled and observed numbers of buildings impacted by landslides depends upon the area 457 over which they are aggregated (Fig. 8). At province (n = 7) and district (n = 77) levels, there is an approximately linear 458 relationship between modelled and observed numbers of buildings, with a Pearson's correlation coefficient >0.80 (Fig. 459 8). At municipality and ward levels, however, the correlation is much weaker. Notably, modelled numbers of buildings 460 over-predict the observed totals by a factor of about 50-100, irrespective of the administrative area. Similar results are 461 seen for road segments: good linear correlations for province- and district-level aggregation, much weaker performance 462 for municipalities and wards, and over-prediction of impacts by a factor of about 20-25 (Fig. 8). 463







465 Figure 8: Comparison of modelled (x-axis) and observed (y-axis) numbers of building and road impacts from coseismic 466 landslides in the 2015 Gorkha earthquake, summed over different administrative areas. Straight lines show best-fit linear 467 regression results. Note differences in axis limits depending on the area of aggregation by province (red), district (orange), 468 municipality (green), or ward (blue).







470 Figure 9: ROC (top), F1 (lower left), and precision-recall (lower right) curves for coseismic landslide impacts of buildings and 471 road segments aggregated over province, district, municipality, ward and at the individual infrastructure scale. Numbers in 472 the top panels show the area under the ROC curves. Line colours match the symbol colours in Fig. 8.

473

474 As a more permissive test of the model's ability to anticipate landslide impacts, we also compare the mean likelihood of 475 landslide impacts, averaged by administrative area, with the presence or absence of impacts in those areas. While the 476 area under the ROC curves is high for all aggregation levels (Fig. 9), this is likely due to the strong imbalance between 477 prediction categories (i.e., there are many more non-impacted buildings than impacted buildings, so the ROC curve is 478 dominated by the large number of true negative model results). In contrast, precision-recall curves show a progressive 479 decrease in model performance at progressively smaller levels of aggregation, from province to ward, and very low 480 precision at the scale of an individual building or road segment (Fig. 9). Because F1 scores combine precision and 481 recall, they show a similar pattern (Fig. 9); across the full range of thresholds, F1 scores for both buildings and roads 482 (Fig. 9) are highest for province- and district-level aggregation and lowest for ward-level aggregation. For an optimal 483 model threshold, province-level aggregation achieves maximum F1 scores of around c. 0.8 for buildings and c. 0.65 for 484 roads. The maximum F1 scores for buildings are also around 0.8 for districts and diminish progressively to 0.55 for 485 municipalities and 0.4 for wards. For roads, the maximum F1 scores are 0.8 for districts and municipalities, and 0.55 for 486 wards. In sum, these results indicate that, while the model can reproduce the spatial pattern of landslide impacts at the 487 provincial or district scale, its predictive capability is much weaker when assessing impacts within smaller 488 administrative units like municipalities and wards, and it should not be used to predict impacts to individual buildings or 489 road segments.

490

491 5. Discussion

492

493 5.1 General observations

494

495 Overall, the hyperedge model is able to reproduce the overall spatial pattern of the impacts from the Gorkha earthquake. 496 This lends some confidence that the model framework could be adapted to estimate the potential impacts from a future 497 event, such as a large earthquake or rainstorm. While the computational efficiency of the hyperedge approach is a 498 notable strength – enabling rapid simulations involving extensive elements, such as the approximately 7.1 million 499 individual buildings and 3 million road segments in our case – its significance extends beyond speed and flexibility 500 because it fosters the generation of multi-hazard scenario ensembles, diverging from the limitation of focusing solely on 501 deterministic impact scenarios. Robinson et al. (2018) demonstrated the advantages of scenario ensembles over the 502 more common approach of single deterministic scenarios, especially as a tool for facilitating awareness of what could 503 be possible in a future event. While creation of multi-hazard scenario ensembles is our wider goal, the experiments 504 shown here focus on multiple realisations of the same past event for the purpose of evaluation.

505

506 A key finding of the experiments is the trade-off between model performance, in terms of the ability to anticipate both 507 the spatial pattern and number of impacts, and the resolution of the model outputs. Because of the probabilistic nature of 508 the model and limitations in our understanding of exposure, earthquake shaking, and landslide susceptibilities, we 509 cannot say with confidence which buildings were impacted by hazards related to the 2015 earthquake. As we aggregate 510 the model results over increasingly large areas, however, our ability to rank those areas in terms of impact, and to 511 estimate the number of structures affected, increases monotonically. While our results can therefore not be used to





512 anticipate the risk to individual households, they could be used by organisations working at a larger scale to identify 513 areas that are more or less prone to different types of hazards, and provide a relative ranking in terms of the number and 514 scale of expected impacts. Thus, the value and potential usefulness of the hypergraph approach as implemented here lies 515 more in informing planning over larger spatial scales, at which the model performs best, as opposed to rapid response to 516 a particular event where detailed spatial information would be required. There is some indication that absolute numbers 517 of affected structures could be generated for larger administrative units by extrapolating the scaling by our analysis of 518 the 2015 earthquake (see, for example, Fig. 8), but we hesitate to draw conclusions from a single earthquake without 519 further testing.

520

521 5.2 Over-prediction and relative impacts between hazards

522

523 We note that the model over-predicts the number of impacts at all levels of aggregation, and is therefore conservative in 524 terms of anticipating the scale of impacts for the 2015 earthquake. The possible reasons for this over-prediction are 525 likely to differ for shaking and landslide impacts. The mismatch in the number of buildings damaged by shaking is 526 especially notable for districts with moderate mean PGA values (typically <0.5 g; Fig. 6A). The sigmoidal fragility 527 functions used in the model are steepest at moderate PGA values (Fig. 3); for the middle case, this corresponds to PGA 528 values of ~0.2-0.5 g for the most common building types in Nepal. Thus, small uncertainties in PGA will yield large 529 differences in the likelihood of complete damage, and thus in the numbers of completely-damaged buildings in our 530 model experiments. This issue is compounded by the highly-uncertain values of ground motion in the Gorkha 531 earthquake stemming from the paucity of strong-motion recordings, as noted by Goda et al. (2015). We also note that 532 our experiments do not account for aftershocks, including the M_w 7.3 earthquake that occurred on 12 May and that 533 ruptured the eastern end of the 25 April slip patch under Dolakha district (Avouac et al., 2015). This event likely led to 534 additional building damage which was included in the observations but is not simulated here, perhaps leading to 535 under-prediction in Dolakha in particular.

536

537 Over-prediction of observed landslide impacts, in contrast, may result from a range of different factors. As noted above, 538 in the absence of an independent dataset of landslide impacts on buildings or roads in the 2015 earthquake, we have 539 generated these data by intersecting those elements at risk with the coseismic landslide inventory of Kincey et al. 540 (2021). This is likely to underpredict the actual number of impacts due to errors and limitations in landslide mapping as 541 well as the potential for buildings to be omitted from the Humanitarian OpenStreetMap database. It is also important to 542 note that our approach relies on a probabilistic sampling of an underlying landslide susceptibility dataset in order to 543 anticipate (1) the slope units in which a landslide is most likely to be triggered, and (2) the buildings and road segments 544 that were most likely to be affected. Our results are thus highly dependent upon the quality of the underlying 545 susceptibility information. In the experiments described here, susceptibility is a static quantity that depends only upon 546 local topography. Because we are focused on a single event, there is no direct provision for dynamic variation in 547 susceptibility over time or for other factors that may affect landslide occurrence, such as the presence or absence of 548 antecedent rainfall, soil moisture or other measures of ground condition, or land cover. Further applications of the 549 model could incorporate susceptibility estimates that are trained on other landslide inventories – for example, 550 time-varying susceptibility that captures the evolution of landslide hazard over time (e.g., Tian et al., 2020; Kincey et 551 al., 2021, 2022) or that depends upon other causative factors (e.g., Reichenbach et al., 2018).





553 Our model result that the number of buildings damaged by ground shaking is approximately an order of magnitude 554 greater than that impacted by landslides is difficult to test directly because of the lack of a systematic description of the 555 sources of building damage in the 2015 Gorkha earthquake. It is broadly consistent, however, with previous work on the 556 relative importance of secondary hazards - including landslides - and ground shaking in determining earthquake losses. 557 Bird and Bommer (2004) assessed the relative impacts of ground shaking and ground failure on direct and indirect 558 losses in earthquakes. They found that fatal landslides occurred in 10 of their 50 studied earthquakes and that landslides 559 could be the primary cause of building damage in affected areas, locally overshadowing ground shaking. Overall, 560 however, ground shaking was the primary cause of building damage in 88% of their studied earthquakes, and landslides 561 in only 6%. They also found that landslide-induced disruption of road or transport networks was much more common 562 than building damage, which matches our model results for the Gorkha earthquake. Daniell et al. (2017) argued that 563 ground shaking has caused 62% of total economic costs in earthquakes over the period 1900-2016, with landslides 564 responsible for 5% of total costs. Marano et al. (2010) found that 21.5% of the fatal earthquakes in the PAGER-CAT 565 database had deaths due to secondary hazards, but that these were rarely the main cause of death. Landslides were the 566 leading cause of non-shaking-related deaths if the 2004 Great Sumatra earthquake was excluded, although they 567 accounted for about an order of magnitude fewer deaths than ground shaking. In contrast, Budimir et al. (2014) 568 demonstrated that earthquakes with landslides typically cause more fatalities than those without, independent of other 569 factors such as earthquake size or affected population. Their results demonstrate the need to account for the full 570 multi-hazard cascade in anticipating losses at anything other than a simplified regional scale (e.g., Bird and Bommer, 571 2004; Daniell et al., 2017).

572

573 5.3 Limitations

574

575 While the model operates on a hyperedge that connects every structure within the dataset, there are a number of factors 576 that cannot be resolved at a building scale. Notably, PGA values were gridded at a spatial resolution of 100 by 100 m, 577 meaning that we have no information on the actual accelerations experienced by individual buildings or road segments. 578 Similarly, while landslide susceptibility was estimated using a comparatively fine-scale DEM with a grid size of 10 x 10 579 m, each individual building or road segment occupies at most a few grid cells and the susceptibility values are thus 580 highly location-dependent. It is also important to note that we do not simulate the triggering, occurrence, and runout of 581 individual landslides, nor do we 'place' landslides in the landscape as would be done for example in a landscape 582 evolution model (e.g., Croissant et al., 2017; 2019). Such a calculation would dramatically increase both the model 583 complexity, making it infeasible to construct a multi-hazard scenario ensemble at a national scale. Because of this 584 limitation, we cannot directly evaluate which elements at risk are directly impacted by landslides, nor can we anticipate 585 which elements may be affected by remobilisation and runout of landslide debris (e.g., Kincey et al., 2022). By 586 sampling the landslide susceptibility distribution for each slope unit, and the landslide susceptibility values for each 587 building, we are (over enough iterations) recovering those distributions, but we cannot overcome the inherent 588 uncertainty in susceptibility at those locations. Finally, the METEOR exposure dataset contains information on the 589 building types and numbers within each 90 x 90 m grid cell, but we have no information on the type and fragility of 590 individual buildings. Therefore, while impact likelihood is calculated at the scale of individual structures, we stress that 591 this estimate is only meaningful across the whole scenario ensemble, and should never be interpreted as a statement that 592 'building X will be affected by this earthquake'.





594 5.4 Other applications

595

596 Because of its efficiency, the framework allows exploration of other elements of model performance, including the 597 distinction between false positive and false negative errors. While performance measures such as the area under an 598 ROC or precision-recall curve can be used to define an 'optimum' model outcome, the model application and users may 599 determine which type of error is more important to minimise. For example, a humanitarian organisation may view false 600 positives as more acceptable than false negatives; the former may lead at worst to unnecessary preparations, whereas 601 the latter means that impacts are not anticipated and may delay relief and recovery efforts. By quickly generating 602 numerous multi-hazard scenarios, the framework can be run with users to explore these different outcomes, and to 603 examine the specificity of model results to the details of a particular scenario (e.g., Robinson et al., 2018). The model 604 could also be used to explore 'what-if' questions with users to examine the effects of particular interventions or 605 remediation measures. In addition, the efficiency of the framework could be used to explore the evolution of risk over 606 time, where increased simulation length or time resolution would lead to an increase in computational cost. Thus, the 607 effects of policy decisions, climate change and consequent changes in hazard occurrence, or demographic shifts on the 608 pattern of anticipated impacts could be explored (Zschau, 2017).

609

610 The flexibility of the hyperedge framework also lends itself to other types of simulation. Other elements of the 611 multi-hazard chain shown in Fig. 2 could be included; for example, susceptibility to landslide debris remobilisation and 612 runout could be included and sampled for each element at risk, allowing the model to anticipate both the direct impacts 613 within an event as well as potential longer-term impacts arising from later secondary hazards (e.g., Fan et al., 2019; 614 Kincey et al., 2022). Impacts from other types of driving events, such as monsoon rainfall, could also be explored. It 615 would be feasible, for example, to generate an ensemble of scenarios around different rainfall patterns associated with a 616 seasonal monsoon outlook, or with different iterations of shorter-term weather forecasts, to look at the pattern and 617 specificity of impacts. Such an application would be subject to the comparatively low spatial resolution of both 618 observational (e.g., Hou et al., 2014) and forecast rainfall data products, so that – just as with the earthquake scenarios 619 developed here – the impact results at the scale of an individual structure would not be meaningful. The hyperedge 620 framework would, however, allow exploration of the trade-offs between aggregation and model performance, as 621 demonstrated here, and could be useful for informing humanitarian contingency planning for annual rainfall-related 622 impacts in Nepal and other monsoon-affected countries.

623

624 6. Conclusions

625

626 Accounting for the multi-hazard aspects of risk is crucial for disaster risk reduction and humanitarian planning. 627 Traditional approaches to risk modelling tend to omit the interactions between hazards and, even when these 628 interactions are accounted for, may struggle to meet the computational demands posed by such complex scenarios. 629 Here, we demonstrate that a new model based on hypergraph theory, a type of network modelling approach, is able to 630 efficiently simulate multi-hazard risk. The model framework accounts for the interactions between a driving stimulus 631 such as an earthquake or rainstorm with processes on the landscape (such as landslides) and exposed infrastructure. 632 Beyond overcoming computational challenges, this framework can facilitate multi-hazard risk assessments by enabling 633 the generation of ensembles to explore the importance of different geophysical hazards, larger areas, longer timeframes, 634 and diverse counterfactual scenarios. This versatility enhances our understanding of complex risk landscapes and 635 empowers decision-makers with valuable insights for proactive disaster preparedness and response strategies.





636

637 We explore the capabilities of the model through a case study of the 2015 M_w 7.8 Gorkha earthquake in Nepal, which 638 caused widespread damage due to both primary shaking and secondary landslides. We find that the model can reproduce 639 the overall spatial pattern of earthquake impacts. The observed numbers of completely-damaged buildings in most 640 districts, including 13 out of the 14 worst-affected districts, fall within the range of model predictions, which depends 641 primarily on the assumed fragility functions for the typical building types found in Nepal. The model also broadly 642 reproduces the spatial patterns of structures that were damaged by coseismic landslides in the earthquake, although it 643 overestimates the absolute number of impacts. This may be due to limitations in the data used by the model to 644 determine impacts. Importantly, there is an increase in model performance when the results are aggregated over larger 645 administrative areas; the model does a reasonable job of anticipating the relative impacts at a province or district scale, 646 but performs much less well at the smaller scales of municipalities or wards. This result suggests that the hypergraph 647 framework could be usefully applied to rank administrative areas by expected impacts, for example due to a future 648 earthquake or rainstorm, to underpin pre-disaster contingency planning efforts where large-scale trends are more 649 important than detailed impact predictions. The computational efficiency of the hypergraph framework, even at the 650 scale of an entire country such as Nepal, lends itself to the generation of multiple impact scenarios and raises the 651 possibility of using an ensemble of potential scenario results rather than depending upon single-event scenarios for 652 disaster preparedness and planning.

653

654 Author contributions

655 Funding was acquired by ALD, TRR, and NJR. The study was conceived by ADu, TRR, ALD, and NJR. ADu wrote 656 the code and carried out the numerical experiments with input from TRR, ALD, NJR, RMR, and MEK. ADu and ALD 657 prepared the original draft of the manuscript and all authors contributed to review and editing.

658

659 Competing interests

660 The authors declare that they have no conflict of interest.

661

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