

Dynamical MJO forecasts using an ensemble subseasonal-to-seasonal forecast system of the IAP-CAS model

Yangke Liu^{1,6}, Qing Bao^{*1}, Bian He¹, Xiaofei Wu², Jing Yang³, Yimin Liu¹, Guoxiong Wu¹, Tao Zhu¹, Siyuan Zhou¹, Yao Tang^{1,6}, Ankang Qu^{1,7}, Yalan Fan³, Anling Liu³, Dandan Chen^{1,6}, Zhaoming Luo^{1,7}, Xing Hu⁴, Tongwen Wu⁵

¹State Key Laboratory of Numerical Modeling for Atmospheric Sciences and Geophysical Fluid Dynamics (LASG), Institute of Atmospheric Physics, Chinese Academy of Sciences, Beijing 100029, China

²School of Atmospheric Sciences/Plateau Atmosphere and Environment Key Laboratory of Sichuan Province, Chengdu University of Information Technology, Chengdu 610225, China

³Faculty of Geographical Science, Beijing Normal University, Beijing 100875, China

⁴National Meteorological Information Center, China Meteorological Administration, Beijing 100081, China

⁵Center for Earth System Modeling and Prediction, China Meteorological Administration, Beijing 100081, China

⁶College of Earth and Planetary Sciences, University of Chinese Academy of Science, Beijing 100049, China

⁷School of Emergency Management Science and Engineering, University of Chinese Academy of Science, Beijing 100049, China

Correspondence to: Qing Bao (baoqing@mail.iap.ac.cn)

17 **Abstract.** The Madden-Julian Oscillation (MJO) is a crucial predictability source on a sub-seasonal to seasonal (S2S) timescale.
18 Therefore, the models participating in the WWRP/WCRP S2S prediction project focus on accurately predicting and analyzing
19 the MJO. This study provided a detailed description of the configuration within the IAP-CAS S2S forecast system. We assessed
20 the accuracy of the IAP-CAS model's MJO forecast using traditional RMM analysis and cluster analysis. Then, we explained
21 the reasons behind any bias observed in the MJO forecast. Comparing the 20-year hindcast with observations, we found that
22 the IAP-CAS ensemble mean has a skill of 24 days. However, the ensemble spread still has potential for improvement. To
23 examine the MJO structure in detail, we used cluster analysis to classify the MJO events during boreal winter into four types:
24 fast-propagating, slow-propagating, standing, and jumping patterns of MJO. The model exhibits biases of overestimated
25 amplitude and faster propagation speed in the propagating MJO events. Upon further analysis, it was found that the model
26 forecasted a wetter background state. This leads to stronger forecasted convection and coupled waves, especially in the fast
27 MJO events. The overestimation of the strength and length of MJO-coupled waves results in a faster MJO mode and quicker
28 dissipation in the IAP-CAS model. These findings show that the IAP-CAS skilfully forecasts signals of MJO and its
29 propagation, and they also provide valuable guidance for improving the current MJO forecast by developing the ensemble
30 system and moisture forecast.

31 **Keywords:** MJO prediction, S2S, IAP-CAS, FGOALS-f2, Cluster Analysis

32 **1 Introduction**

33 With the increasing occurrence of metrological disasters in recent years, there has been growing attention toward S2S forecast,
34 as it bridges the gap between weather and climate forecasts and reduces disaster risks through early warnings. In November
35 2013, the WWRP/WCRP S2S prediction project (Phase 1) was launched, with the principal objectives of enhancing S2S
36 forecast accuracy and advancing our comprehension of its dynamics and climate drivers. Then, work on the S2S research
37 continued in Phase 2, from 2018 to 2023. The whole project has made a significant contribution to the development of S2S
38 prediction.

39 MJO (Madden and Julian, 1971) is a crucial predictability source of S2S forecasts. It is a significant tropical oscillation with
40 a period of 30-60 days, characterized by expansive cloud masses and precipitation systems that propagate eastward along the
41 equatorial regions. Accurate S2S prediction requires a good representation of MJO. Many studies have clarified the relationship
42 between the MJO and global weather and climate, such as monsoons (Goswami, 2012; Hsu, 2012; Lau and Chan, 1986;
43 Wheeler et al., 2009; Liu et al., 2022), tropical cyclones (Bessafi and Wheeler, 2006; Ferreira et al., 1996; Hall et al., 2001)
44 and El Niño-Southern Oscillation (ENSO; Lau et al., 2005; Zhang, 2005). The convective and circulation anomalies associated
45 with MJO establish intricate connections across global weather and climate systems on the S2S timescale. Being able to
46 accurately forecast the MJO can have a positive impact on the forecast of other related systems (Cassou, 2008; Vitart and
47 Molteni, 2010; Wu et al., 2007). Achieving an accurate forecast of MJO becomes a primary objective in the field of S2S
48 forecasts.

49 With an enhanced comprehension of the underlying physical mechanisms governing the MJO and the continuous improvement
50 of numerical models, remarkable advancements have been achieved in the MJO forecast. In Coupled Model Intercomparison
51 Project Phase 6 (CMIP6), models that exhibited lower forecast skills (Hung et al., 2013) in Coupled Model Intercomparison
52 Project Phase 5 (CMIP5) have demonstrated noteworthy improvements in the simulation of MJO (Chen et al., 2022). Generally,
53 the models in CMIP6 simulate more realistic eastward propagation and precipitation over the Maritime Continent (MC) region
54 (Ahn et al., 2019; Ahn et al., 2020).

55 However, for S2S forecasts, the improvement of model physics is one aspect of advancing S2S forecasts, as various factors
56 impact MJO forecast skills, such as initialization and ensemble generation (Kim et al., 2018). The forecast skills of the MJO
57 in most models is typically 3-4 weeks (Vitart, 2017), while the estimate of predictability of MJO is approximately 5-7 weeks
58 (Waliser et al., 2003; Neena et al., 2014). These facts underscore the persisting challenges in the S2S forecasts.

59 The realistic forecast of MJO eastward propagation is one of the challenges repeatedly mentioned in recent years (Jiang, 2017;
60 Kim, 2019; Lim et al., 2018; Wang and Lee, 2017). The MJO propagation skill is closely related to the forecast of the state in
61 the Maritime Continent (MC) region (Gonzalez and Jiang, 2017). Many studies have pointed out the "MC barrier" (Hendon
62 and Salby, 1994; Rui and Wang, 1990a; Vitart et al., 2017) during the MJO's propagation through the MC region. The "MC

63 barrier" refers to a notable deterioration of the MJO signal when it traverses the MC area, but this phenomenon is usually
64 amplified in the climate models (Kim et al., 2014b; Neena et al., 2014; Xiang et al., 2022, 2015), showing the model's limitation
65 in preserving MJO propagation within the MC region. The moisture mode theory (Raymond and Fuchs, 2009) has been
66 proposed to explain this phenomenon. It suggests that the advection of seasonal mean moisture by the MJO-related circulation
67 anomalies in the lower troposphere is crucial to MJO's propagation through the MC region (Jiang, 2017; Kim, 2019). In models
68 that are hard to capture the realistic propagation of MJO, the mean low-troposphere moisture amplitude over the MC is
69 underestimated, resulting in a weakened horizontal moisture gradient (Gonzalez and Jiang, 2017; Kim, 2017). This discrepancy
70 in moisture advection hinders MJO propagation.

71 The Institute of Atmospheric Physics at the Chinese Academy of Sciences (IAP-CAS) has been actively involved in climate
72 model development and applications since the CMIP1 in the 1990s. As for the IAP-CAS model, it has already shown a
73 significant enhancement in MJO simulation in CMIP6 compared to CMIP5 (Chen et al., 2022), but the performance of the
74 S2S system in IAP-CAS remains uncertain and requires comprehensive evaluation. Therefore, the objectives of this article are
75 fourfold: Firstly, the aim is to introduce the S2S forecast system of the IAP-CAS model. Secondly, to evaluate the forecast
76 skills of the IAP-CAS in the MJO forecast. Thirdly, the aim is to analyze the evaluation results to identify the sources of
77 forecast errors. This will facilitate further improvements in the MJO forecast. At last, we hope that the verification and analysis
78 process can provide some valuable insights for other models.

79 The structure of the paper is as follows. A thorough review of the IAP-CAS model and S2S ensemble forecast system is
80 introduced in Section 2. Section 3 describes the observation data and primary methodology utilized in the article. Section 4
81 assesses the overall MJO forecast skills in IAP-CAS. Section 5 focuses on analyzing the propagation details of the fast-
82 propagating and slow-propagating MJO. After that, in Section 6, we discuss the potential causes of any bias observed in the
83 MJO forecast. In Section 7, we summarize our findings and have a discussion.

84 **2 The global S2S ensemble forecast system of IAP-CAS**

85 The architecture of the IAP-CAS S2S ensemble forecast system is depicted in Figure 1. In this section, we will give a thorough
86 description of the S2S system, covering the model, initialization methods, ensemble generation approaches, and the resulting
87 datasets.

88 **2.1 Configuration of IAP-CAS model**

89 The climate system model CAS FGOALS-f2 (The Flexible Global Ocean-Atmosphere-Land System model Finite Volume
90 version 2, Chinese Academy of Sciences; Bao 2019; Bao et al. 2020) is the core of the IAP-CAS S2S ensemble forecast system.
91 It is developed by the State Key Laboratory of Numerical Modeling for Atmospheric Sciences and Geophysical Fluid

92 Dynamics (LASG) at the Institute of Atmospheric Physics (IAP), Chinese Academy of Sciences (CAS). We utilize the
93 institution name, IAP-CAS, as a proxy for the model.

94 FGOALS-f2 is a fully coupled model that encompasses four components: atmospheric, land, oceanic, and sea ice models, with
95 its configuration detailed in Table 1. The atmospheric component is version 2 of the Finite-volume Atmospheric Model
96 (FAMIL2; Li et al. 2019), with a standard horizontal resolution of C96, which means 96×96 grid points in each tile of the
97 cube sphere, roughly equivalent to 1-degree resolution. Vertically, it features 32 hybrid sigma-pressure levels, with the
98 uppermost level situated at 1 hPa (The Hybrid coefficients are listed in Table A1). The land surface component used in
99 FGOALS-f2 is version 4 of the Community Land Model (CLM4.0; Oleson et al. 2010; Lawrence et al. 2011), featuring a
100 horizontal resolution nearly at 1-degree resolution. The oceanic component is Parallel Ocean Program version 2 (POP2;
101 Kerbyson and Jones 2005), which utilizes a displaced-pole grid with the North Pole shifted to Greenland. This grid has a
102 resolution of gx1v6, approximately equivalent to a 1-degree horizontal resolution, and includes 60 vertical layers. The sea ice
103 component is the Los Alamos Sea Ice Model version 4.0 (CICE4; Hunke et al. 2010), sharing the exact horizontal resolution
104 as the ocean model. These four components are coupled via the coupler version 7 in the Community Earth System Model
105 (CESM; Craig et al. 2012).

106 It is worth noting that FAMIL2, the latest generation atmospheric model from LASG, has adopted the Finite-Volume Cubed-
107 Sphere Dynamical Core (FV3; Lin 2004; Putman and Lin 2007; Harris et al., 2020) as its dynamical core. FV3 solves the fully
108 compressible Euler equations on the gnomonic cubed-sphere grid and a Lagrangian vertical coordinate. The hydrostatic solver
109 of FV3 is used in our model. This enhancement of the atmospheric component results in improved computational efficiency
110 and accuracy. Besides, the key parameterization in FAMIL2 is a Resolved Convection Precipitation scheme (RCP), which is
111 independently developed to calculate the microphysics processes in the convective precipitation for both deep and shallow
112 convection (Bao and Li, 2020). Due to the rapid phase changes occurring within the convective cloud, a sub-time step of 150
113 seconds is employed for the calculation of microphysical processes within a physical timestep of 30 minutes. FAMIL2 has
114 also implemented the University of Washington Moist Turbulence parameterization scheme (UWMT, Park and Bretherton
115 2009) as its boundary layer scheme. The microphysical parameterization used in FAMIL2 is the revised Lin scheme, which is
116 a single-moment scheme (Zhou et al., 2019).

117 **2.2 Initialization scheme of the S2S forecast system**

118 The S2S forecast system of the IAP-CAS model adopts a Newtonian nudging method with time-varying treatment (Jeuken et
119 al., 1996) to complete the initialization of the atmosphere and ocean. The reanalysis nudging and the forecast nudging are the
120 two components that make up the initialization process, which is seen in Figure 2. Table A2 provides a summary of the detailed
121 technical specifics for these two nudging processes.

122 The reanalysis nudging initializes the atmospheric variables, including temperature, surface pressure, sea level pressure, and
 123 surface wind from the NCEP Final Operational Global Analysis datasets (FNL, <http://rda.ucar.edu/datasets/ds083.2>,
 124 ds083.2|DOI: 10.5065/D6M043C6). The oceanic variable of potential temperature from the National Oceanic and Atmospheric
 125 Administration (NOAA) Optimum Interpolation Sea Surface Temperature (OISST) reanalysis data (Reynolds et al., 2007) is
 126 also included. These reanalysis data serve as observations in the eq. (1) to diminish errors in the initial condition:

$$127 \quad x(t) = x_{model}(t) + N_{rea}(t)[x_{obs}(t) - x_{model}(t)] \quad (1)$$

128 where t is the time, $x(t)$ is the field after nudging process, $x_{model}(t)$ represents the model forcing, $x_{obs}(t)$ represents the
 129 “truth” value, and $N_{rea}(t)$ is a relaxation coefficient that varies over time, which constantly adjusts the model results during
 130 the integration process, making it approximate to the observed values while being constrained by the dynamical constraints of
 131 the physical model. The calculation process for $N_{rea}(t)$ is as follows:

$$132 \quad N_{rea}(t) = \frac{\Delta t}{\frac{T}{1 + \cos(2\pi \frac{t\%T}{T})} + \Delta t} \quad (2)$$

133 Δt is the time step in FAMIL2, which is 0.5h for C96 resolution (approximately 1-degree resolution). T represents the time
 134 window with a value of 6 hours. As depicted in Figure 2a, the relaxation coefficient varies as a cosine function. It is large at
 135 the beginning and end of the temporal window, thereby facilitating accelerated convergence of the model results toward
 136 observations. While in the middle of the time window, N_{rea} becomes smaller and even drops to zero, which indicates the
 137 reliability of the reanalysis data decreases. The reason is that the reanalysis data within the time window is obtained through
 138 interpolation between its start and end values.

139 In the forecast nudging, the initialization process adheres to a similar nudging algorithm at 6-h intervals, as shown in eq. (3).

$$140 \quad x(t) = x_{model}(t) + N_{fcst}(t)[x_{fcst}(t) - x_{model}(t)] \quad (3)$$

141 Nevertheless, the atmospheric variables assimilated into the S2S system are sourced from the GFS weather forecast, denoted
 142 as $x_{fcst}(t)$. The relaxation coefficient $N_{fcst}(t)$ is as follows:

$$143 \quad N_{fcst}(t) = \frac{\Delta t}{\frac{T}{1 + \cos(2\pi \frac{t\%T}{T})} + \Delta t} \cdot \cos\left(\frac{\pi}{2} \cdot \frac{(t-t\%T)}{4mT}\right) \quad (4)$$

144 Compared to N_{rea} , N_{fcst} is multiplied by a decay factor, which also varies in accordance with the cosine function. In this
 145 context, the number of days for forecast nudging is denoted by m , and the system is configured with a 10-day forecast nudging
 146 period. Figure 2b illustrates the variation of N_{fcst} , which decreases as the reliability of weather forecast data diminishes over
 147 time, ultimately reaching zero by the 10th day.

148 In forecast nudging, we used 10 days of GFS weather forecast data for nudging. One purpose of this approach is to avoid
 149 coupling shock at initialization. Additionally, we aim to enhance the quality of initial forecasts in S2S by nudging GFS weather
 150 forecast data to ultimately improve S2S prediction accuracy, as the skill of weather forecasts is higher than that of S2S forecasts
 151 during the initial period.

152 Summarily, the S2S forecast system commences its daily forecast from the initial condition derived via reanalysis nudging. It
153 then fine-tunes the forecasts with weather prediction data through the forecast nudging process. This initialization system
154 effectively reduces system errors in the model and augments forecast accuracy.

155 **2.3 Time-lagged method for ensemble generation**

156 The value of ensemble forecasts in medium to long-term forecasts has been repeatedly emphasized (Liu, 2003; Vitart and
157 Molteni, 2009). In addition to improving the physical scheme of the model, devising an effective approach for ensemble
158 generation might have a considerable impact on the MJO forecast. The IAP-CAS S2S ensemble forecast system utilizes the
159 time-lagged method (Hoffman and Kalnay, 1983) to generate ensemble members.

160 A schematic diagram of the time-lagged method is depicted in Figure 2b. During the initial day of the forecast nudging, the
161 S2S system issues forecasts from 00Z, 06Z, 12Z, and 18Z, resulting in the generation of 4 ensemble members. The core idea
162 behind this approach is to introduce perturbations by leveraging lagged initialization times.

163 **2.4 Hindcast experiment and real-time forecast**

164 The S2S ensemble forecast system provides daily forecasts, forecasting weather and climate conditions for the upcoming 65
165 days. Out of the 65 days, 5 days are reserved for extending the ensemble members by using the time-lagged method, ensuring
166 a complete forecast for at least 60 days. Since June 1st, 2019, the IAP-CAS S2S system has been operating 16 ensemble
167 members daily for real-time forecasts. So far, approximately 8.2TB of real-time data has been uploaded to the S2S website.
168 For hindcast experiments from 1999 to 2018, the system has run 4 ensemble members daily, generating a dataset of
169 approximately 11TB. Our subsequent research is based on the 20-year hindcast experiment.

170 In 2021, the IAP-CAS model participated in phase II of the S2S Project (Vitart et al., 2017) successfully, providing the 20-
171 year hindcast and real-time forecast data generated by the S2S ensemble forecast system. Detailed information regarding the
172 data is listed in Table A3, and Table A4 shows the list of output variables. The output data is interpolated to a standardized
173 horizontal resolution of $1.5^{\circ} \times 1.5^{\circ}$, following the S2S's requirements, and is stored in version 2 of General Regularly-distributed
174 Information in Binary (GRIB2) format. The output data of the S2S system is publicly available on three S2S Data Portals
175 (ECMWF, CMA, and IRI).

176 **3 Datasets and methods**

177 **3.1 datasets**

178 The observational datasets used for the MJO verification include the NOAA daily outgoing longwave radiation (OLR;
179 Liebmann and Smith 1996), daily wind from the National Centers for Environmental Prediction (NCEP)/Department of Energy
180 (DOE) Reanalysis 2 dataset (Kanamitsu et al., 2002), daily specific humidity from ECMWF Reanalysis version 5 (ERA5;

181 ERA 2017), and the precipitation product from the Global Precipitation Climatology Project (GPCP; Adler et al. 2003). To
 182 facilitate computation and meaningful comparisons, both observation and hindcast datasets have been uniformly interpolated
 183 to a horizontal resolution of $2.5^\circ \times 2.5^\circ$. Seven pressure levels (1000, 925, 850, 700, 500, 300, and 200hPa) of wind and specific
 184 humidity are extracted for analysis.

185 3.2 MJO RMM index

186 To conduct a quantitative assessment of MJO, we have employed the widely used Real-time Multivariate MJO (RMM) index
 187 (Wheeler and Hendon, 2004a) to extract the MJO signal. This index consists of two components, RMM1 and RMM2, which
 188 are the first and second principal components of the combined empirical orthogonal functions (EOFs) of multiple variables,
 189 including OLR, 200hPa zonal wind (U200), and 850hPa zonal wind (U850). It serves as a tool for tracking the location and
 190 amplitude characteristics of MJO.

191 The calculation of the RMM index refers to the method described in Gottschalck et al. (2010). Detailed calculation steps are
 192 as follows:

- 193 1) Remove the 0-3 waves of the climatology and low-frequency variability of the U200, U850, and OLR variables from both
 194 the observation and hindcast data. It is noteworthy that removing low-frequency variability is to subtract the mean of the
 195 past 120 days from the anomalies. For model forecast, this is the mean model anomalies of the previous forecast days,
 196 plus the mean observed anomalies of the remaining days.
- 197 2) Average the anomalies between 15° S and 15° N and normalize the three variables, using the pre-computed coefficients
 198 as in Gottschalck et al. (2010).
- 199 3) Project the anomalies onto the observed combined EOF eigenvectors from Wheeler and Hendon (2004b) to get RMM1
 200 and RMM2.

201 Bivariate anomaly correlation coefficient (ACC) and bivariate root mean square error (RMSE) are calculated using the
 202 observed and hindcast RMM indices to represent the forecast skills of the IAP-CAS model as

$$203 \text{ACC}(\tau) = \frac{\sum_{t=1}^N [a_1(t)b_1(t,\tau) + a_2(t)b_2(t,\tau)]}{\sqrt{\sum_{t=1}^N [a_1^2(t) + a_2^2(t)]} \sqrt{\sum_{t=1}^N [b_1^2(t,\tau) + b_2^2(t,\tau)]}}, \text{ and} \quad (5)$$

$$204 \text{RMSE}(\tau) = \sqrt{\frac{1}{N} \sum_{t=1}^N [(a_1(t) - b_1(t,\tau))^2 + (a_2(t) - b_2(t,\tau))^2]} \quad (6)$$

205 Here $a_1(t)$ and $a_2(t)$ are the observation RMM1 and RMM2 at time t ; $b_1(t)$ and $b_2(t)$ are the forecasting RMM1 and
 206 RMM2 at time t for lead τ days; N is the total number of times. It is commonly accepted that days with ACC above 0.5 are
 207 considered to have valid forecasts. Therefore, the forecast skill of a model is quantitatively defined as the maximum lead time
 208 exceeding 0.5, which approximately corresponds to the day when RMSE reaches $\sqrt{2}$.

209 RMM index can also be adapted to quantitatively evaluate the forecasted intensity and velocity through the calculation of the
 210 error of amplitude ($ERR_{amp}(\tau)$) and phase ($ERR_{phase}(\tau)$) as a function of lead time τ :

$$211 \text{ERR}_{amp}(\tau) = \frac{1}{N} \sum [AMP_b(t,\tau) - AMP_a(t)], \text{ and} \quad (7)$$

$$ERR_{phase}(\tau) = \frac{1}{N} \sum \tan^{-1} \left[\frac{a_1(t)b_2(t,\tau) - a_2(t)b_1(t,\tau)}{a_1(t)b_1(t,\tau) + a_2(t)b_2(t,\tau)} \right] \quad (8)$$

Negative (positive) $ERR_{amp}(\tau)$ indicates weaker (stronger) amplitude in forecasts. Similarly, Negative (positive)

$ERR_{phase}(\tau)$ indicates slower (faster) propagation in forecasts. Here the MJO amplitude for observation ($AMP_a(t)$) and forecast ($AMP_b(t)$) is defined as

$$AMP_a(t) = \sqrt{a_1(t)^2 + a_2(t)^2}, \text{ and} \quad (9)$$

$$AMP_b(t, \tau) = \sqrt{b_1(t, \tau)^2 + b_2(t, \tau)^2}. \quad (10)$$

3.3 Cluster analysis of MJO events

Another crucial method used in this research is cluster analysis. In Section 5, we select the representative MJO events and classify them following the work Wang et al. (2019) did. This facilitates a more focused and targeted investigation into the forecast bias of MJO in the IAP-CAS model.

An MJO event was chosen if the regional average of OLR, spanning from 10° S to 10° N and 75° E to 95° E, remained below one standard deviation for a consecutive period of 5 days during the boreal winter (November–April). Subsequently, the K-means cluster analysis is employed to categorize the chosen MJO events based on the propagation patterns from day -10 to 20 (day 0 is the day with the peak MJO in the Indian Ocean). At last, we use silhouette clustering evaluation criteria (Rousseeuw, 1987) to identify and eliminate poorly classified MJO events.

Finally, a total of 50 MJO events were selected from 1999 to 2018 winter and four types of MJO events were identified, namely the fast-propagating (10 cases), slow-propagating (16 cases), standing (12 cases), and jumping (12 cases) patterns of MJO (Fig. 5).

The fast-propagating MJO and slow-propagating MJO belong to the propagating type of MJO, characterized by their consecutive eastward propagation across the Indian Ocean to the Pacific Ocean region. On the other hand, the standing and jumping MJO represent relatively non-propagating types, where the convection remains relatively fixed or exhibits discontinuous movement. Wang et al. (2019) believe that propagating MJO events are often associated with strong and tightly coupled Kelvin waves, especially for fast-propagating MJO. This is the biggest difference between propagating MJO and non-propagating MJO.

4 Evaluation of MJO forecast skill from the IAP-CAS model

The evaluation in this section was conducted for the annual MJO events. Figure 3 demonstrates the overall MJO forecast skill in the IAP-CAS model and the improvement brought by the time-lagged ensemble method. Figure 3a shows the forecast skill of the ensemble mean is 24 days with the criterion of ACC exceeding 0.5, while the skill of individual members is about 21-22 days. Meanwhile, the ensemble mean RMSE reaches $\sqrt{2}$ at 21 days and the individual members exhibit larger RMSE,

241 reaching $\sqrt{2}$ at 16 days (Fig. 3b). The solid blue line in Figure 3b represents the ensemble spread (Leutbecher and Palmer,
242 2008) of IAP-CAS. When this ensemble spread approaches the RMSE of the ensemble mean (solid red line), it indicates that
243 the ensemble members are sufficiently dispersive. Figure 3b illustrates that the ensemble exhibits an underdispersive
244 characteristic in the early stage of the forecast. We have also observed similar issues of "underdispersive" in many other
245 models (Rashid et al., 2011; Neena et al., 2014; Kim et al., 2014b; Xiang et al., 2015), and addressing this aspect may be a
246 focal point for future model enhancements.

247 Increasing the number of ensemble members within a certain range proves effective in forecasting the uncertainty of weather
248 and climate (Hou et al. 2001). We employed the time-lagged ensemble method to further augment the ensemble members. The
249 time-lagged ensemble includes the ensemble members generated on the forecast day and from lag times. For instance, by
250 incorporating ensemble members with a lag of i ($i = 0, 1, 2, \dots$) days, the total number of members becomes $4 * (i + 1)$.
251 Upon examining the relationship between lag i days and forecast skill, it was found that the skill increases as i increases at
252 first, but then it reaches a plateau when $i > 3$ (see Fig. A2). This suggests that the forecast skill of the 16 members may
253 represent the limit of the time-lagged ensemble method in IAP-CAS. Figure 3d shows the ensemble of 16 members is more
254 dispersive than 4 members, which is illustrated by less distinction between RMSE and Spread in the 16-member system. The
255 ensemble mean of 16 members achieves a skill of 26 days, surpassing the skill of 4 members by two days (Fig. 3c).

256 Numerous prior investigations have demonstrated that MJO forecast skill is sensitive to the MJO amplitude in many models
257 (Lin et al., 2008; Rashid et al., 2011; Wang et al., 2014; Xiang et al., 2022), and this characteristic is also evident in the IAP-
258 CAS model. We classify an MJO case as an initial (target) strong case if its initial (target) amplitude is greater than 1, while
259 an event with an initial (target) amplitude less than 1 is classified as an initial (target) weak case. Figures 4a-b show that in the
260 IAP-CAS model, the forecast skills of strong MJO cases are generally higher than weak cases, especially in the target strong
261 (weak) cases.

262 The amplitude and phase of MJO serve as additional indicators for a detailed assessment of MJO forecast performance. For
263 initially strong MJO cases, we analyze the MJO amplitude and forecasted phase angle error (Figs. 4b-c). The individual
264 member has a stronger amplitude than observation, which leads to a relatively strong amplitude in the ensemble mean during
265 the initial 40 days. However, as the noise rapidly increases, the phase error of the individual members also escalates (as shown
266 in Fig. 4c). The phase error results in a mutual cancellation in positive and negative phases of MJO among ensemble members,
267 leading to a rapid weakening of the amplitude in the ensemble mean. In Figure 4d, the phase error of the ensemble mean
268 indicates that the speed of forecasted MJO tends to decrease at first and then start increasing around the 10th day. A more
269 detailed investigation into the speed of propagating MJO events will be described in Section 5.

270 **5 The forecast of MJO propagation**

271 We present a qualitative diagnostic of a 20-year hindcast experiment to evaluate the overall forecast skills of IAP-CAS in
272 Section 4. This analysis provides us with preliminary insights into the performance and biases of the system. Given that the
273 MJO is more pronounced during boreal winter, our focus is concentrated from November to the following April. Based on
274 Wang et al. (2019), we aim to conduct further investigations into different types of boreal winter MJO events to explore the
275 physical explanation of system biases.

276 In Section 3, we have already described the methodology for classifying MJO events and results. Figure 5 compares the
277 composited propagation patterns of precipitation and U850 between observation and forecast for four different MJO types. In
278 observations, the fast-propagating (Fig. 5a) and slow-propagating (Fig. 5b) MJO exhibit a consecutive eastward propagation
279 structure from the Indian Ocean across the MC region to the Pacific Ocean. The primary distinction between the two types lies
280 in their propagation speed. The fast-propagating MJO demonstrates a faster speed, with a velocity of 4.58 m/s, compared to
281 the slow-propagating type, which moves at 4 m/s. The standing MJO (Fig. 5c) remains relatively stationary over the Indian
282 Ocean and does not continue to propagate eastward. The jumping MJO (Fig. 5d) shows a convective system that bypasses the
283 MC region and directly jumps from the Indian Ocean to the Pacific Ocean. Here, fast MJO and slow MJO are considered
284 propagating MJO events, while the latter two types are regarded as non-propagating MJO events.

285 The observed U850 displays a coupled structure characterized by equatorial westerly anomalies of the Kelvin wave component
286 located west of the convection, and easterly anomalies of the Rossby wave component located east of the convection (Rui and
287 Wang, 1990b; Adames and Wallace, 2014; Wang and Lee, 2017). As illustrated in Figure 5, a distinct contrast between
288 propagating MJO and non-propagating MJO can be found in the circulation at the low level: in the propagating MJO events,
289 the Kelvin wave response is strong and tightly coupled with the center of convection, which is shown in the stronger and
290 eastward-extending easterly wind component, particularly prominent in fast MJO events. Many previous studies (Benedict
291 and Randall, 2007; Hsu and Li, 2012; Wang and Lee, 2017) have also indicated that the presence of low-level easterly winds
292 is a key signal that contributes to the eastward propagation of MJO by inducing low-level convergence and premoistening to
293 the east of the major convection. In the non-propagating MJO events, the easterly wind is weak and tends to decouple from
294 the major convection.

295 The model accurately reproduces the propagating morphology of the MJO and exhibits coupled signals of Kelvin and Rossby
296 waves (Figs 5e and 5f). However, a noticeable acceleration in speed is evident, particularly in the case of fast MJO, reaching
297 speeds of 6 m/s, while the simulated slow MJO moves at 5 m/s. Figure 5g also shows that the forecast for standing MJO
298 remains somewhat imprecise. This aspect is also evident in the MJO forecast skill depicted in Figure 6, where the standing
299 MJO has the lowest skill (13 days). For each MJO type, we consider the skill as the ACC of the cases initiated from day -20

300 to day 15 (Xiang et al., 2015). Figure 6 displays that the fast MJO achieves the highest skill at 32 days, while the jumping MJO
301 and slow MJO exhibit skills of 23 and 21 days, respectively.

302 Additionally, from the Hovmöller diagram of observed propagating MJO (Figs. 5a and 5b), a significant change in convection
303 is observed after crossing the MC region, which is marked by a decrease in intensity and a slower propagation speed. This
304 change is roughly delineated by the 135° E, which is commonly referred to as the “MC barrier”. As mentioned above, the “MC
305 barrier” effect is usually amplified in the climate models. In the IAP-CAS model, the forecasted convective signal of slow
306 MJO appears to halt after crossing the MC region. Could this indicate an amplification of the "MC barrier" issue in the IAP-
307 CAS model? However, this phenomenon is less pronounced in the simulation of fast MJO. Due to the zonal averaging in the
308 Hovmöller diagram, some information may be obscured. Further investigation is required to determine the detailed
309 characteristics of the propagating MJO simulated by the model.

310 Figure 7 presents the evolution patterns of propagating MJO. In the first 10 days, it is noticeable that the forecasted precipitation
311 intensity of propagating MJO is significantly higher than observed, especially in the case of fast MJO. Coupled winds in 850
312 hPa also exhibit stronger magnitudes, with a larger zonal scale. The forecasted location of the major convection is relatively
313 biased towards the east, which further confirms that there is an overestimation of the propagation speed. On the 15th day, the
314 MJO convective system crosses the MC region and reaches the eastern Pacific. It is worth noting that the forecasted negative
315 phase of MJO exhibits a significant development, with an accelerated speed, gradually intruding into the positive phase (Figs.
316 7b and 7d). By the 20th day, the development of the negative phase has further intensified, extending its influence into the
317 tropical eastern Pacific region, while in the observation, the negative phase remains east of the MC region. In the later stages,
318 as the negative phase intrudes, the forecasted convective signal in the positive phase is almost absent due to the inherently
319 weaker convection in slow MJO. The disappearance of the slow MJO signal observed in the Hovmöller diagram after crossing
320 the MC region may stem from the intrusion of the negative phase. This might differ from the commonly defined issue of "MC
321 barrier" amplification observed in many models.

322 In Figure A3, simulations show that both standing and Jumping MJO also exhibit overall enhanced convective intensity.
323 However, they accurately capture the non-propagating characteristics of the observed MJO, such as the weak coupling of
324 Kelvin waves and the strong coupling of Rossby waves.

325 **6 The possible physical explanation for the forecast biases**

326 Section 5 highlights some biases observed in the forecast of propagating MJO, which includes stronger amplitude and faster
327 propagation speed in the IAP-CAS model. These biases are also mentioned in Section 4. In this section, we aim to unravel the
328 physical mechanisms underlying these biases.

329 As a large-scale convective system, MJO's genesis, evolution, and dissipation are intricately linked to atmospheric moisture
 330 (Wang, 1988; Kemball-Cook and Weare, 2001; Maloney, 2002; Wang and Lee, 2017). Given that the model forecasts exhibit
 331 a systematic bias of stronger amplitude, we start with the diagnosis of the background state in moisture. Figure 8 shows the
 332 winter mean specific humidity averaged over 10° S–10° N. A clear positive bias of the background moisture state in the IAP-
 333 CAS model is observed (Fig. 8c), which can enhance the convection in the MJO. However, the distribution of this moisture
 334 bias is non-uniform. Figure 8c illustrates that the positive moisture bias is more pronounced towards the western Indian Ocean
 335 and the central-eastern Pacific, and this bias gradually spreads to the upper levels. However, in the MC region, the positive
 336 moisture bias is smaller and primarily concentrated in the low level. We speculate that higher evaporation fluxes in the model
 337 may be the reason for the positive moisture bias. Therefore, the reduction in oceanic surface area within the MC region
 338 contributes to a decrease in this positive bias.

339 Figure 9 displays the precipitation-induced condensational heating (Q_2) during fast MJO and slow MJO events. The
 340 condensational heating serves as a proxy for the distribution of convection, which was estimated by the moisture sink defined
 341 as

$$342 \quad Q_2 = -L_v \left(\frac{\partial q}{\partial t} + \vec{V} \cdot \nabla q + \omega \frac{\partial q}{\partial p} \right), \quad (11)$$

343 where q is the specific humidity, \vec{V} is the horizontal circulation, ω is vertical pressure velocity, and L_v is the latent heat
 344 at condensation, which is a constant here. The vertical distribution of Q_2 reveals that both fast MJO and slow MJO events in
 345 the model forecasts trigger stronger convection, particularly in the fast MJO events. Furthermore, the enhanced convective
 346 heating leads to a strong response in the coupled MJO-related circulation (Fig. 9). From the 1st day to the 10th day, there is a
 347 gradual strengthening process observed in the simulated convection, particularly pronounced in fast MJO, with its intensity
 348 peaking on the tenth day.

349 To further understand the propagation and intensity variations of MJO in the IAP-CAS model, it is necessary to comprehend
 350 the underlying physical processes associated with it. Under the framework of “moisture mode”, Jiang (2017) performed a
 351 moisture budget analysis on the latest generation of general circulation models (GCMs) and identified the key processes for
 352 the eastward propagation of MJO. This research revealed that the advection ($\vec{V}' \cdot \nabla \bar{Q}$) of the seasonal mean moisture (\bar{Q}) by
 353 the MJO anomalous circulations (\vec{V}') plays a crucial role in the propagation of MJO. By increasing moisture eastward and
 354 decreasing it westward of the MJO convection, the advection regulates the propagation. (Kim et al., 2014a; Adames and Kim,
 355 2016; Jiang et al., 2018). Among the two determining factors (\vec{V}' and \bar{Q}), the role of the moisture gradient term is further
 356 emphasized. Many studies (Gonzalez and Jiang, 2017; DeMott et al., 2018; Ahn et al., 2020) have demonstrated that the mean
 357 moisture's horizontal gradient plays a crucial role in determining the propagation of MJO (Fig. 10a). It is well-forecasted in
 358 the models that simulate MJO well, leading to realistic horizontal mean moisture gradients and, thus, well-forecasted horizontal
 359 moisture advection associated with the MJO (Hsu and Li, 2012; Kim et al., 2014a; Nasuno et al., 2015; Adames and Wallace,

2015; Gonzalez and Jiang, 2017). The IAP-CAS model is capable of reproducing this gradient, although there is an overall stronger moisture bias (Fig. 10b). Here, the \bar{Q} presented is the winter mean specific humidity at 850 hPa (\bar{Q}_{850}). Research has indicated that the \bar{Q}_{850} is representative (Kim, 2019), and subsequent analysis also focuses on the 850 hPa level.

Figure 11 shows the composite equatorial U850 anomalies averaged over the 15° S-15° N for fast MJO and slow MJO respectively. It depicts the transition from westerly to easterly winds in the MC region (as enclosed by the two blue dashed lines), leading to the change from positive advection to negative advection. On the 1st and 5th days, the MC region is predominantly occupied by easterly winds, while from the 10th to the 20th day, the region is primarily characterized by westerly winds in both fast MJO and slow MJO. However, the forecasted amplitude of low-level wind is significantly stronger, which can be caused by the enhanced MJO convection as explained earlier.

The MJO anomalous circulation patterns in the MC region result in a positive moisture advection on the eastern part of the MJO during the early stages of MJO's development, which facilitates the propagation of convection in the positive phase. We refer to this process as the "developing phase". Figure 12 provides a detailed illustration of this process. Conversely, during the later stages, there is a negative moisture advection on the western side of the MJO, which leads to the propagation of convection in the negative phase and promotes the dissipation of the MJO. We refer to this process as the "decaying phase" (Fig. 12). Compared to the observation, the stronger amplitude of the low-level moisture advection ($\bar{\mathbf{V}}' \cdot \nabla \bar{Q}$) in the model explains the gradual enhancement of convective moist phases during the early stages and the amplification of convective dry phases during the later stages (Fig. 13). The model's moist environment leads to intensified convection, triggering the strengthening of coupled wind fields, which in turn enhances the moist phase in the early stage and the dry phase in the later stage of convection. Consequently, during the development phase of the MJO, its amplitude gradually strengthens. Conversely, during the decaying phase of the MJO, the intensity of the dry phase also progressively increases.

As the simulated propagating MJO gradually intensifies, we observe an enhancement of easterly winds on the east of the convective center, accompanied by an overestimation in zonal scale, indicating the triggering of stronger Kelvin waves (Figs 7b and 7d). According to Wang et al. (2019), MJO with a larger zonal scale will experience an increased eastward propagation speed since the phase speed is inversely proportional to the wave number. This phenomenon is also observed in observation, where the Kelvin wave response to fast MJO exhibits a larger zonal scale compared to slow MJO. Subsequently, during the decay phase of the propagating MJO, the model exhibits a pronounced Rossby wave response triggered by the MJO, leading to the intrusion of convective negative phases and facilitating the dissipation of the MJO.

In addition to examine the winter mean moisture state (\bar{Q}), we have analyzed MJO-related moisture anomalies (Q') as well (Fig. 14). By comparing the evolution pattern of moisture anomalies between slow MJO and fast MJO, it is found that the moisture anomalies in the eastern part of fast MJO are more intense compared to the slow MJO. This results in stronger low-level moisture transport towards the convective region, thereby also facilitating the intensification and acceleration of the MJO. Moreover, there is a significant distinction in the spatial correlation between fast and slow MJO and it happens as early as the

392 1st day. As the forecast lead time progresses, the accuracy of the moisture forecast deteriorates, while fast MJO events display
393 comparatively better performance. The disparity in moisture anomalies is possibly a pivotal factor contributing to differences
394 in forecast skills between the fast (32 days) and the slow MJO (21 days). This underscores the significance of improving
395 moisture forecast in the MJO forecast.

396 **7 Summary and discussion**

397 **7.1 Summary**

398 The graphical abstract presents a workflow for this paper, outlining the structure of this work. This study introduces a newly
399 developed S2S ensemble forecast system of the IAP-CAS model. The introduction primarily focuses on the numerical model,
400 initialization, ensemble generation, and post-processing aspects of the S2S system. Then we aim to identify potential
401 possibilities for developing this S2S system through a comprehensive assessment of its forecast skills. Based on the 20-year
402 hindcast experiment, the IAP-CAS model shows comparable skill (24 days) to other S2S models. However, the ensemble
403 forecast for MJO has been demonstrated to be underdispersive. A detailed examination of the propagating MJO forecasted in
404 the IAP-CAS model reveals that the amplitude of the convection is overestimated with an increasing propagation speed,
405 particularly in the fast MJO events. These biases are accompanied by a faster dissipation of the MJO.

406 The root cause of these biases lies in the model's wetter environment, which leads to enhanced convection and strengthened
407 circulation coupled with convection. This, in turn, further amplifies convection during the development of propagating MJO.
408 The gradual intensification of MJO strength and coupled Kelvin waves is mainly associated with the stronger amplitude of the
409 low-level moisture advection ($\vec{V}' \cdot \nabla \bar{Q}$) in the forecast. The overestimate in the zonal scale of Kelvin waves accelerates the
410 propagation of the propagating MJO in the model. Similarly, the strengthening of Rossby waves also hastens the dissipation
411 of the MJO. Moreover, the differences in forecast skills between the fast MJO and the slow MJO may be attributed to
412 discrepancies in moisture anomalies (Q') forecast. This further underscores the significance of accurate moisture forecasts.

413 **7.2 Discussion**

414 In Figure A4, we compare the forecast skill of the IAP-CAS model with 11 other S2S models. The MJO index of 12 S2S
415 models and ERA-Interim from the S2S website (<http://www.s2sprediction.net/>) is used for evaluation during the standard
416 hindcast period 2001-2010. In Figure A4, we observe improved forecast skill in ensemble forecasts compared to deterministic
417 forecasts. Among the 12 S2S models, the IAP-CAS model exhibits MJO skill above the mean skill level, while the ECMWF
418 model stands out as the highest-performing model. Figure A5a shows that the skill of individual members in ECMWF is
419 approximately 17-18 days, whereas the ensemble mean demonstrates an extended skill of up to 30 days. This phenomenon
420 may be attributed to the ECMWF model's considerable dispersion (Fig. A5b), which once again underscores the critical role
421 of ensemble dispersion in forecasting uncertainties of weather and climate.

422 Therefore, the forthcoming phase in our model's development plan encompasses increasing model dispersion through
423 improved ensemble perturbation methods, with the ultimate goal of improving model forecast skills. The method of orthogonal
424 conditional nonlinear optimal perturbations (CNOPs, Mu et al. 2003) and the second-order exact sampling (Pham, 2001) are
425 both promising approaches for generating initial perturbations in the model. This method allows the generation of a set of
426 initial perturbations in different orthogonal perturbation subspaces, each with the maximum potential for nonlinear
427 development. When applied to ensemble forecast using a simple Lorenz-96 model, the CNOPs method has demonstrated
428 higher forecast skill compared to the commonly used linear Singular Vectors (SVs) method (Lorenz, 1996). Furthermore,
429 PDAF (Parallel Data Assimilation Framework, Nerger et al., 2020) provides an efficient method known as second-order exact
430 sampling, which uses the long-time variability of the model dynamics to estimate the uncertainty. Evidence has already
431 suggested that the use of second-order exact sampling can greatly improve the skill in sea ice extent throughout the Arctic and
432 along the Northern Sea Route (Yang et al., 2020). We plan to explore the application of CNOPs and second-order exact
433 sampling in the IAP-CAS model in the future and eagerly anticipate the potentially significant results it may yield. Additionally,
434 using machine learning to improve the skill of ensemble forecast is also a viable way to enhance the ensemble forecast of our
435 model.

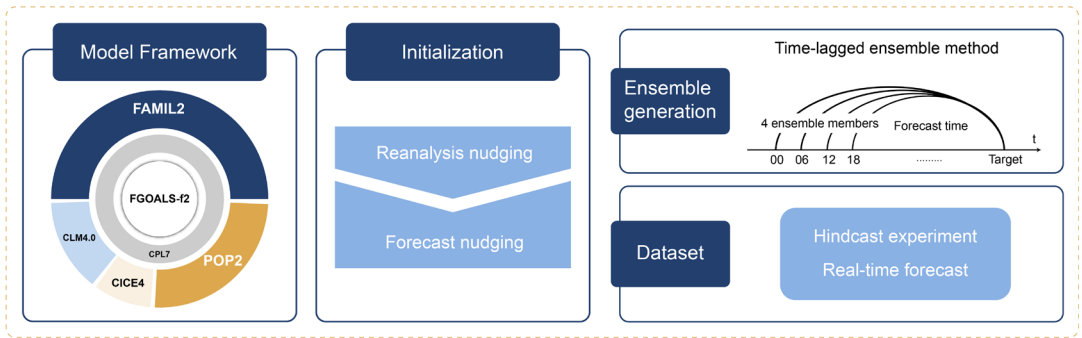
436 In addition to exploring ensemble perturbations, we also intend to enhance the initialization system of the model. Recognizing
437 the moisture is crucial in the forecast of MJO and acknowledging the issue of moisture bias in the IAP-CAS model, it is
438 essential to take measures to ameliorate moisture forecast in our model. The recent research by Zeng (Zeng et al., 2023)
439 provides convincing evidence that humidity initialization can indeed significantly enhance MJO forecast in the IAP-CAS S2S
440 forecast system, especially in the 2 and 3 phase of MJO propagation. However, it is worth noting that changes in the mean
441 state have a significant impact on MJO development (Hannah et al., 2015; Kim, 2019), we must pay attention to the influence
442 of moisture initialization on the mean state. Moreover, the current S2S system's initialization process uses the nudging method,
443 and it is worthwhile to explore more efficient methods to enhance the initialization process.

444 We are also considering increasing the resolution of the model to C384 (25 km) globally. A High-resolution coupled model
445 could better represent the MJO (Crueger et al., 2013). This improvement could be attributed to the enhanced resolution, which
446 better captures the ocean-atmosphere interaction – a critical factor for MJO convection. Increasing the resolution is also
447 meaningful for enhancing forecasts in the MC region by accurately depicting terrain distortion (Hsu and Lee, 2005; Inness and
448 Slingo, 2006; Wu and Hsu, 2009). Further optimizing the model's physical processes and dynamic-physical coupling is also
449 believed to enhance the forecast of the MJO (Zhou and Harris, 2022). As the foreseeable resolution and complexity of the
450 model increase in the future, the issue of power consumption on X86 architecture processors for handling the growing amount
451 of data will become more pronounced. We have plans to port the model to the computing platform based on ARM architecture
452 to address the challenges posed by the explosive growth of data.

Component	Model name	Horizontal Resolution	Vertical levels	Reference
Atmosphere	FAMIL2	Cubed Sphere Grid (C96, $\sim 1^\circ \times 1^\circ$)	32 in the hybrid levels	Li et al. 2019
Land	CLM4.0	Nested subgrid hierarchy (f09, $\sim 1^\circ \times 1^\circ$)	15 soil levels and 3 snow levels	Oleson et al. 2010; Lawrence et al. 2011
Ocean	POP2	Displaced-pole grid (gx1v6, $\sim 1^\circ \times 1^\circ$)	60 levels	Kerbyson and Jones 2005
Sea ice	CICE4	Displaced-pole grid (gx1v6, $\sim 1^\circ \times 1^\circ$)	5 levels	Hunke et al. 2010

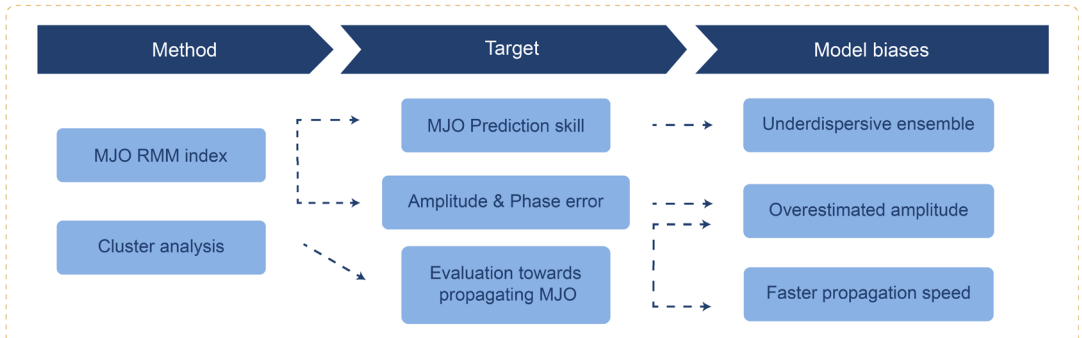
1 An overview of IAP-CAS S2S ensemble forecast system

EXPECTED: Readers can acquire a thorough and organized comprehension of this system



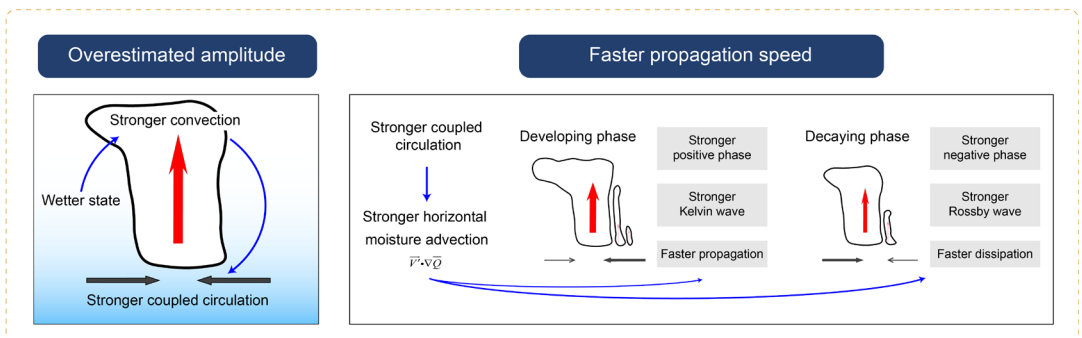
2 Evaluation of MJO forecast in IAP-CAS S2S system

EXPECTED: Gain insights into the S2S system's performance in S2S forecast



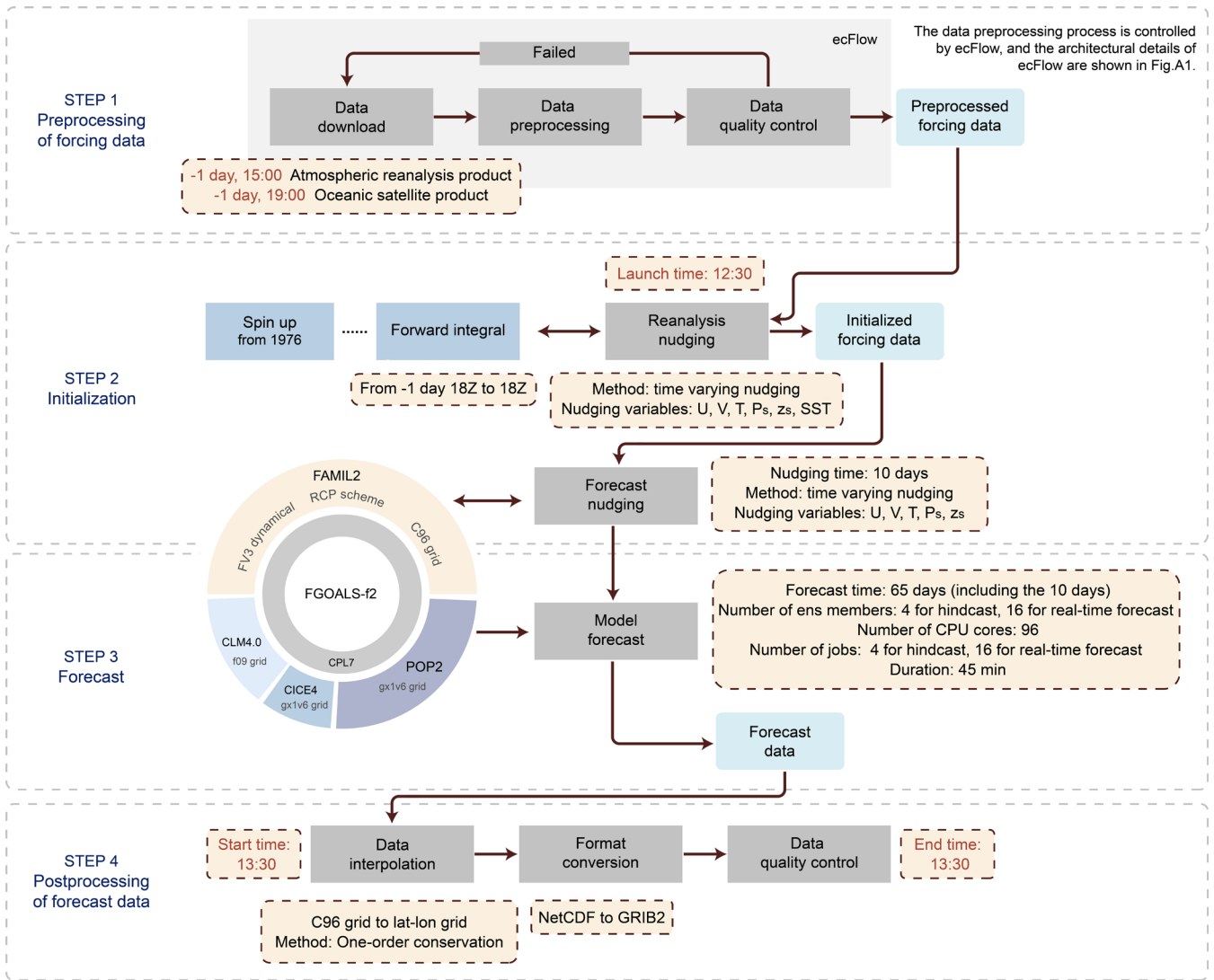
3 The possible explanation about the prediction biases

EXPECTED: Identify the sources of system errors for further improvements



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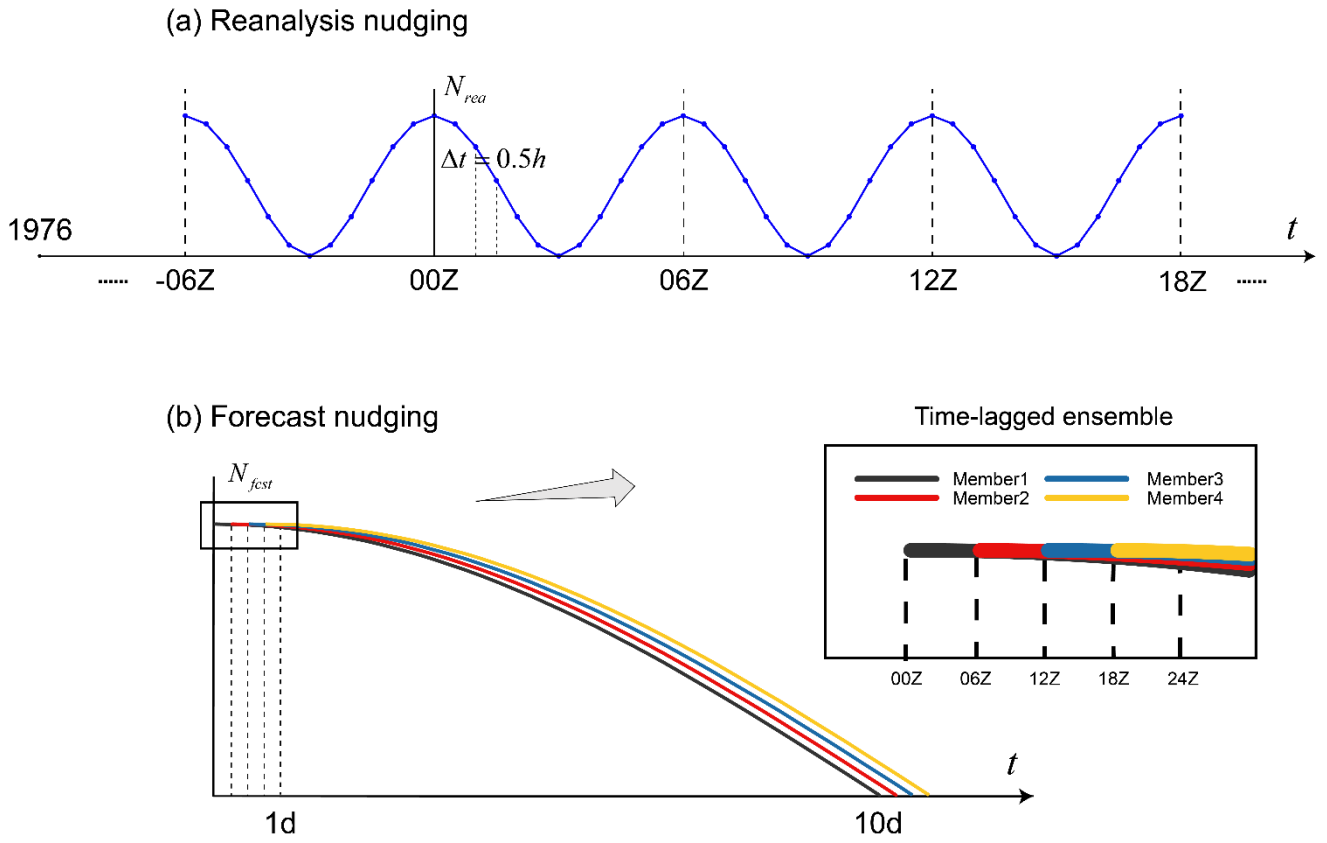
455 **The graphical abstract**



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The time marked in red here is local time (beijing time)

Figure 1. The structure of the IAP-CAS S2S ensemble forecast system



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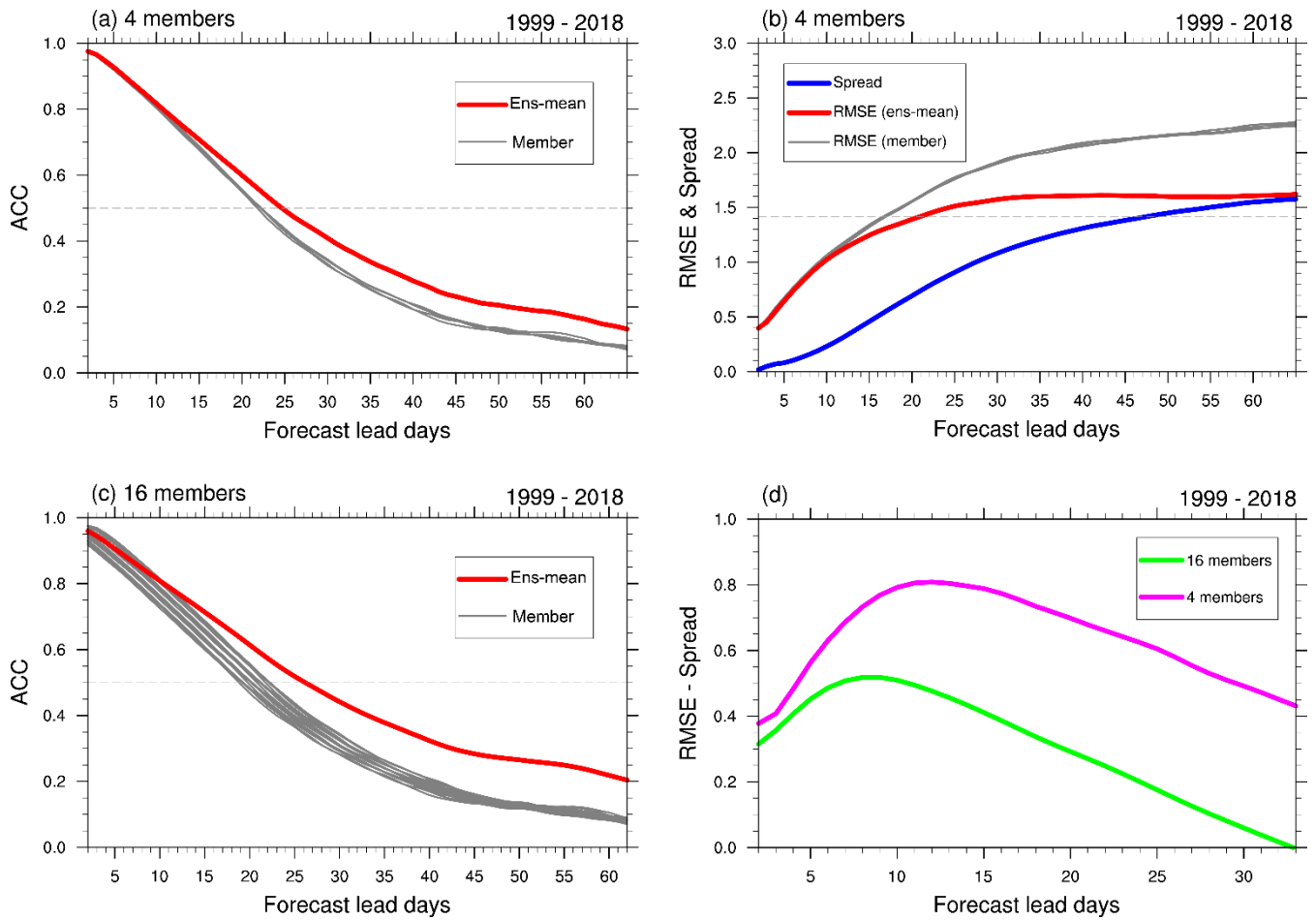
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Figure 2. The initialization scheme of the S2S ensemble forecast system in the IAP-CAS model. The relaxation coefficient (N) as a function of time (t) in (a) the reanalysis nudging and (b) the forecast nudging. In (a), The reanalysis nudging begins on January 1, 1976. The dots indicate the nudging process every 30 minutes. In (b), the solid lines of 4 colors represent the 4 ensemble members with their generation facilitated through the application of the time-lagged method.



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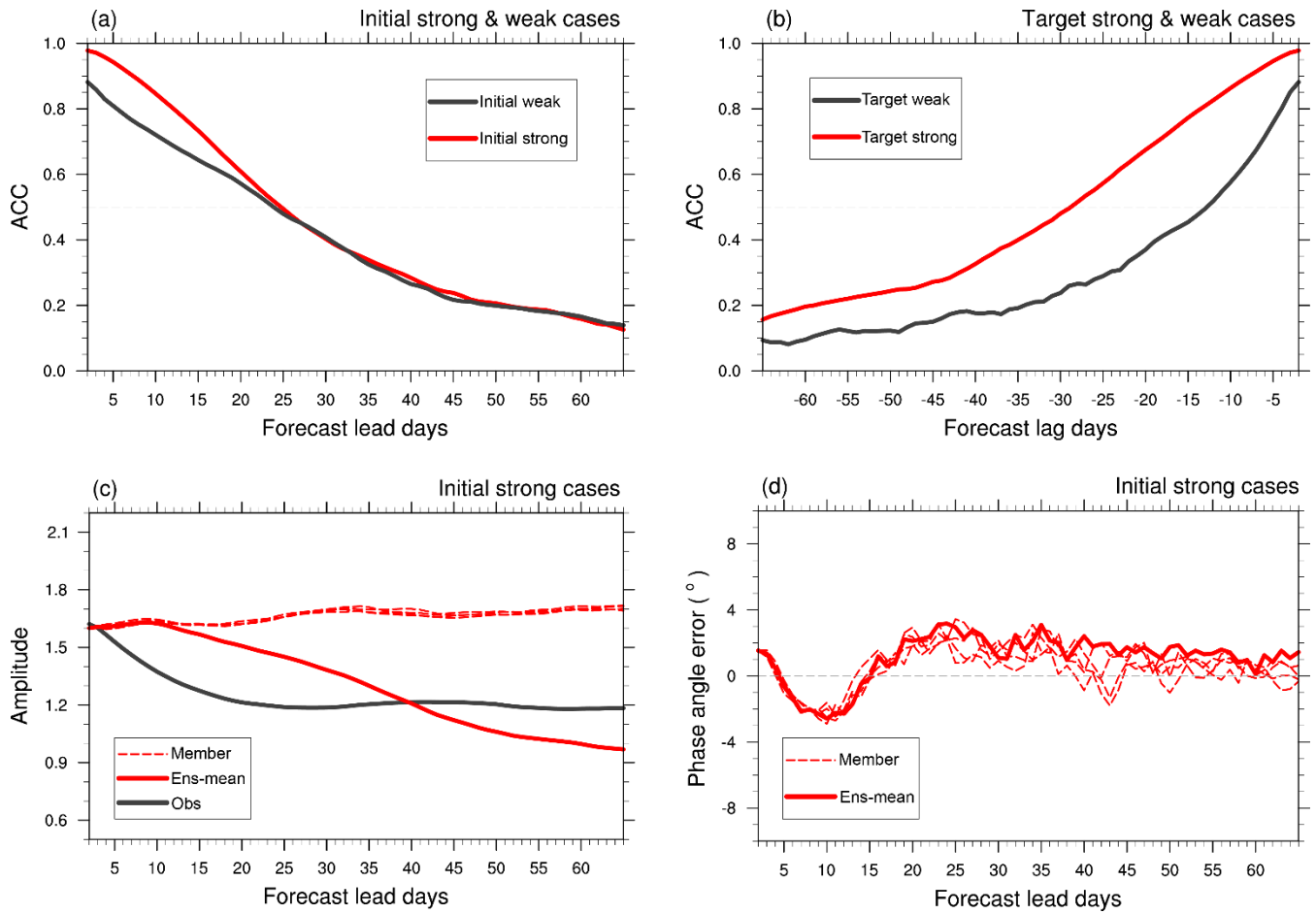
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Figure 3. MJO forecast skill of IAP-CAS for the annual MJO events over 20 years (1999-2018) re-forecast data. (a) The bivariate anomalous correlation coefficient (ACC) and (b) The Root Mean Squared Error (RMSE) varied with forecast lead days for individual members (gray solid line) and ensemble mean (red solid line). The blue solid line denotes the ensemble spread. (c) The ACC of individual members and ensemble mean, as generated by the time-lag method resulting in 16 ensemble members. The dashed line in (a) and (c) has the values of 0.5, and it represents 1.414 in (b). (d) The difference between RMSE and Spread of 4-member ensemble mean (purple solid line) and 16-member ensemble mean (green solid line).



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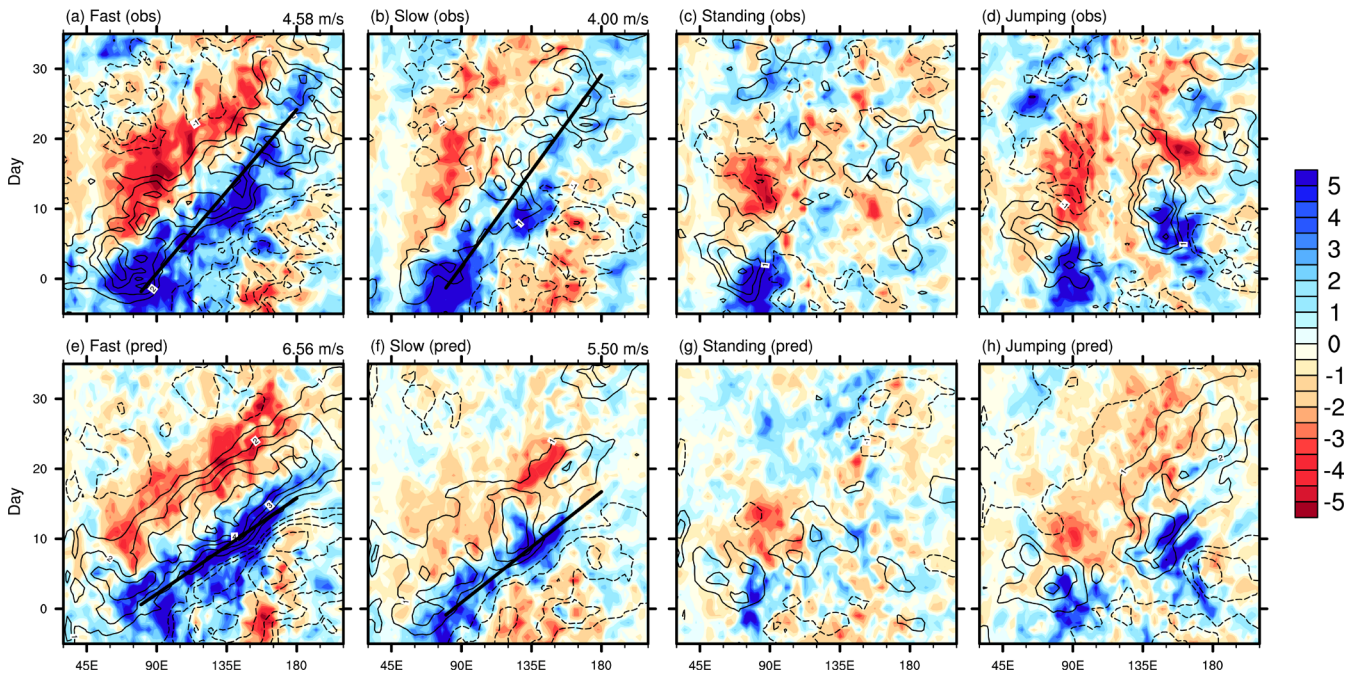
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Figure 4. The ACC (a) varied with forecast lead days for initially strong (red) and weak (black) cases and (b) varied with forecast lag days for target strong (red) and weak (black) cases from the ensemble mean. The dashed lines in (a) and (b) have the values of 0.5. (c) The forecast of MJO amplitude varied with forecast lead days for initially strong cases from observation (black solid line), individual ensemble members of the model (red dashed line) and their ensemble mean (red solid line). (d) The forecast of MJO phase angle error (°) for initially strong cases (black solid line). The dashed line in (d) is the reference line with the values of 0.



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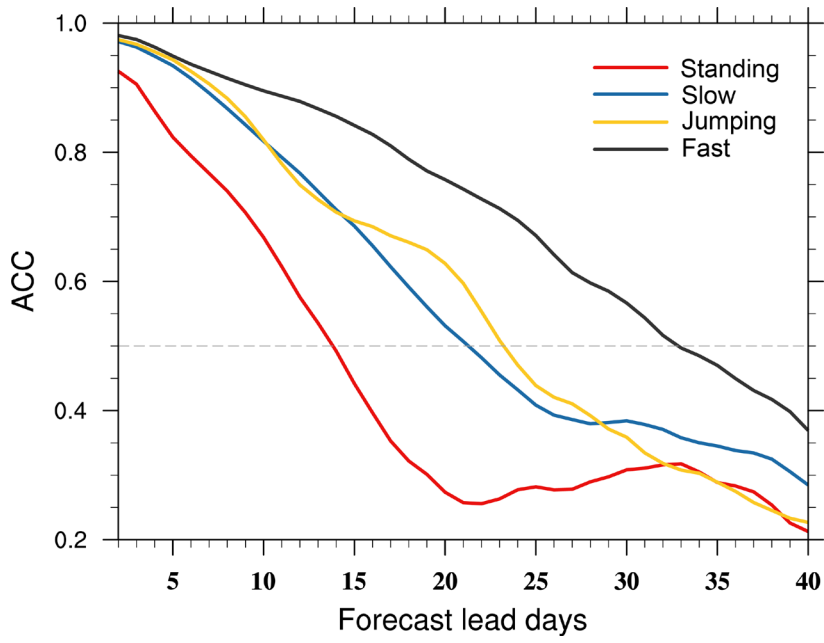
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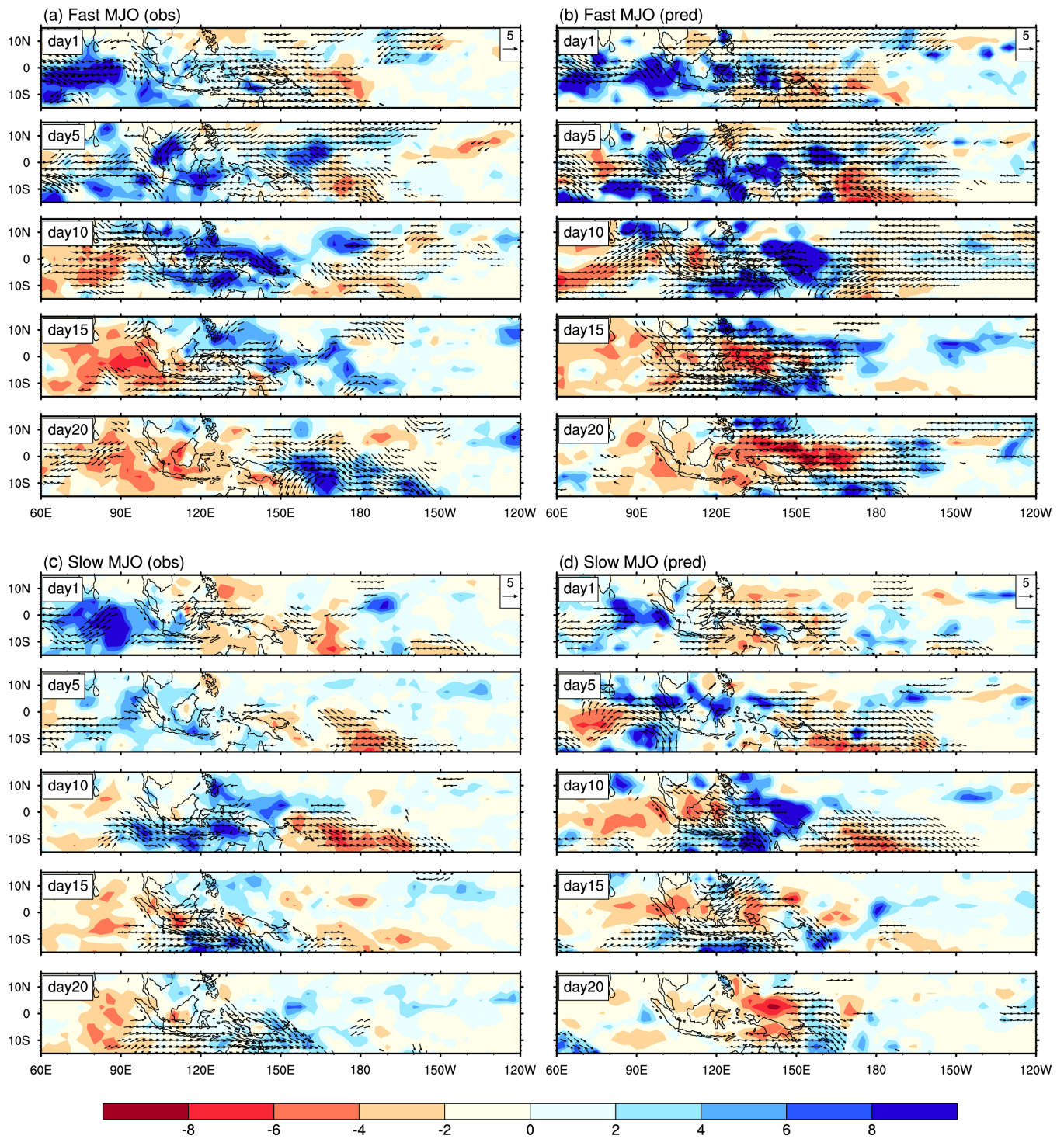
Figure 5. 10° S– 10° N averaged Precipitation anomalies (shading; mm day^{-1}) and 850-hPa zonal winds anomalies (contours with an interval of 1 m s^{-1}) varied with longitude (x-axis) and time lag (y-axis; days) composited for four types of the boreal winter MJO. The top row is for observation (NCEP winds and GPCP precipitation), and the bottom row is for model forecasts. The thin solid black lines represent positive values and the dashed lines represent negative values. The thick solid black line represents the propagation trajectory of the MJO, derived via least squares regression. The propagation speed of the propagating MJO is annotated in the top right corner of the panels.



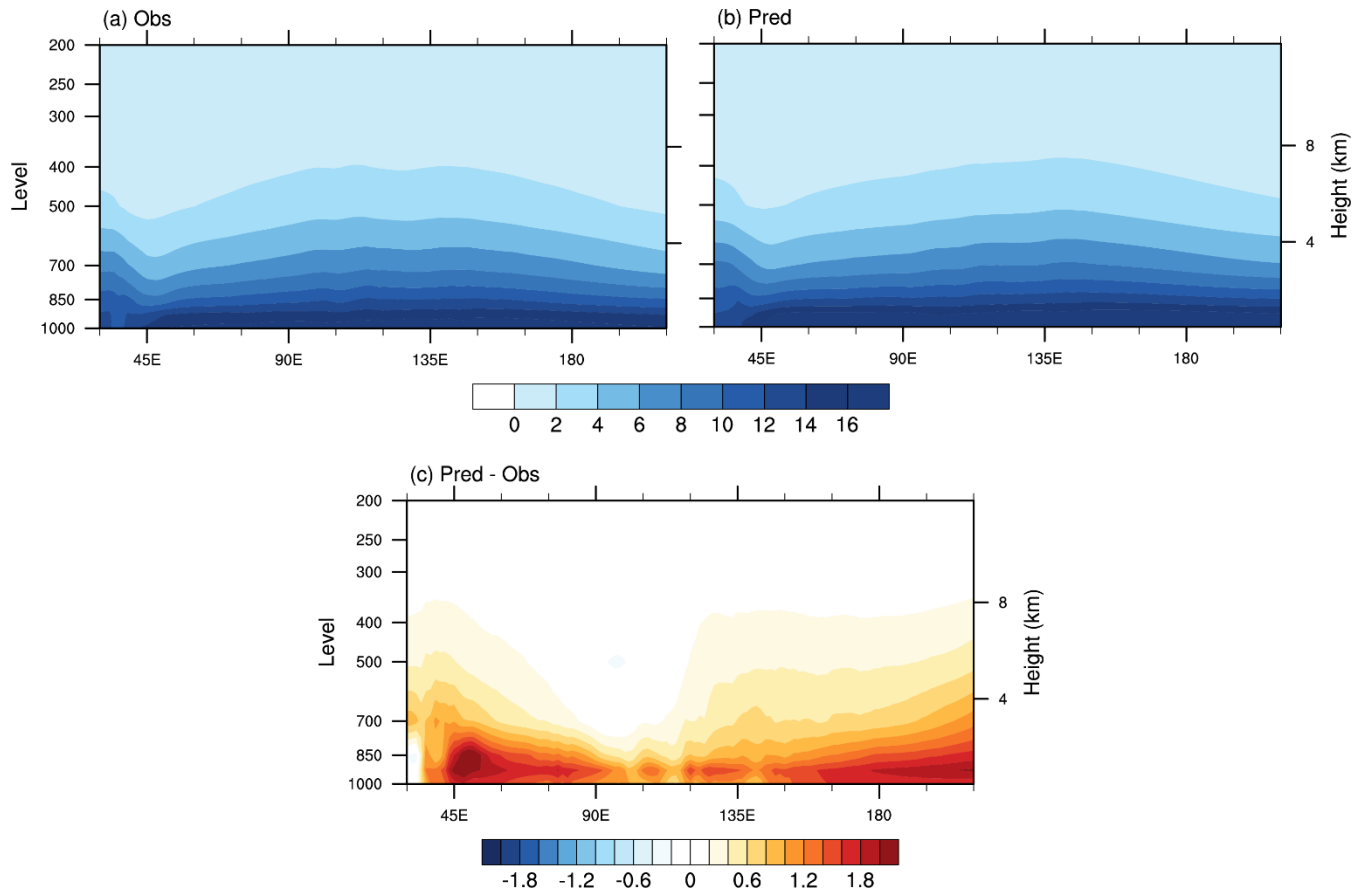
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484 **Figure 6. The bivariate ACC as a function of forecast lead days for fast, slow, jumping, and standing MJO events. The dashed line**
485 **has a value of 0.5.**

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487
 488 **Figure 7. Evolution patterns of the composite precipitation (shading; mm day⁻¹) and 850-hPa winds (vectors; m s⁻¹) anomalies**
 489 **(exceeding 2 m/s) for day 1, day 5, day10, day15 and day 20 in (a) observed fast MJO, (b) simulated fast MJO, (c) observed slow**
 490 **MJO and (d) simulated slow MJO.**

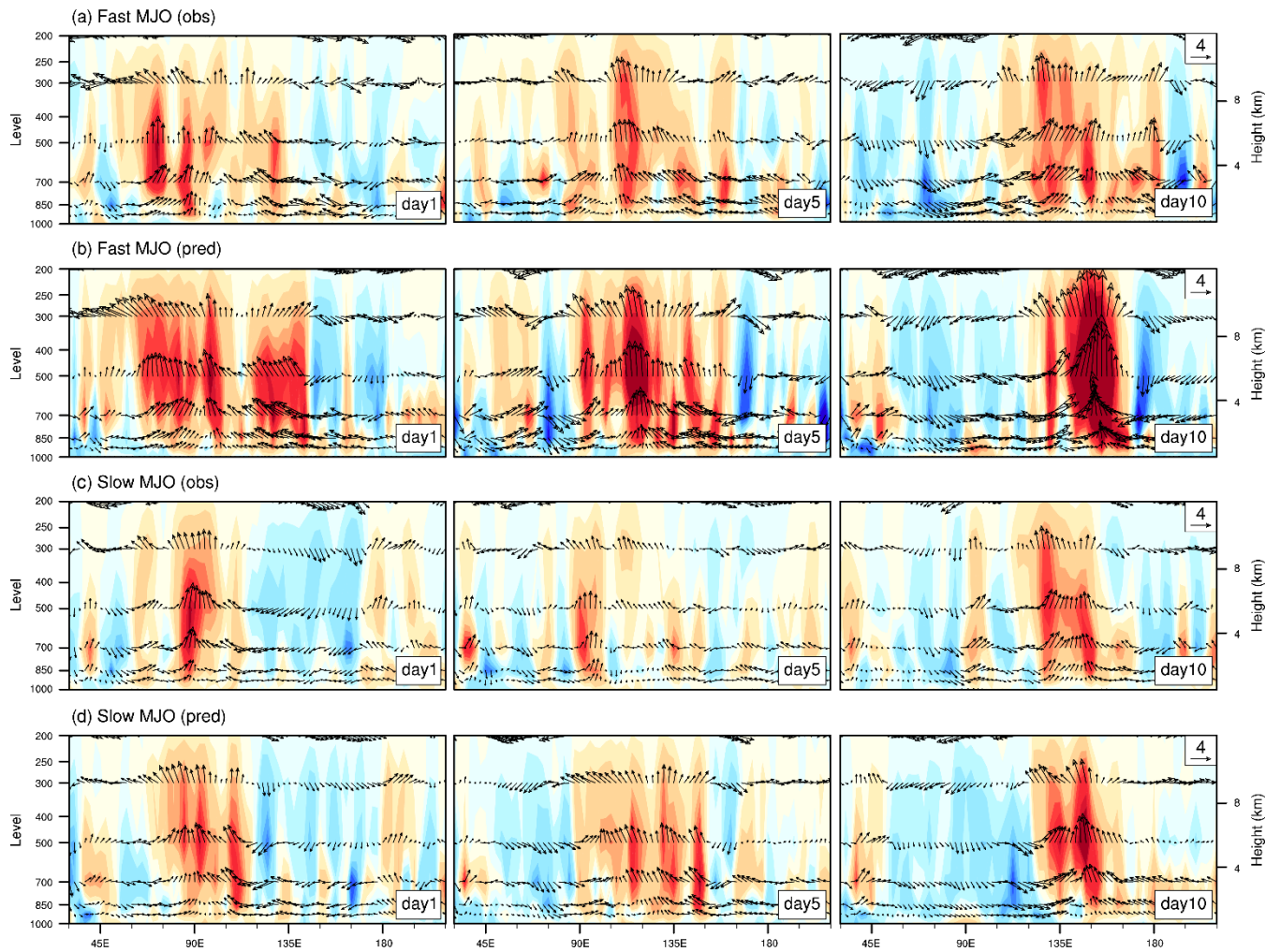


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Figure 8. The longitude-vertical profiles of winter (November–April) mean specific humidity (g kg^{-1}) averaged over 10°S – 10°N for (a) observation, (b) IAP-CAS model, and (c) the difference between IAP-CAS model and observation.



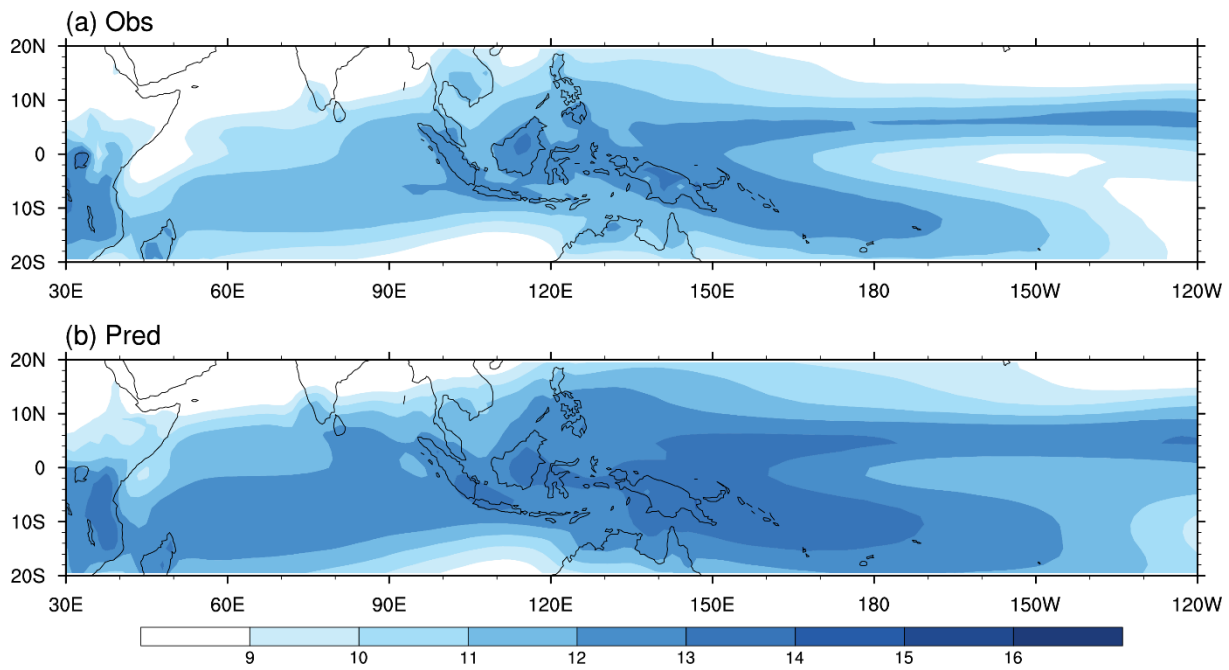
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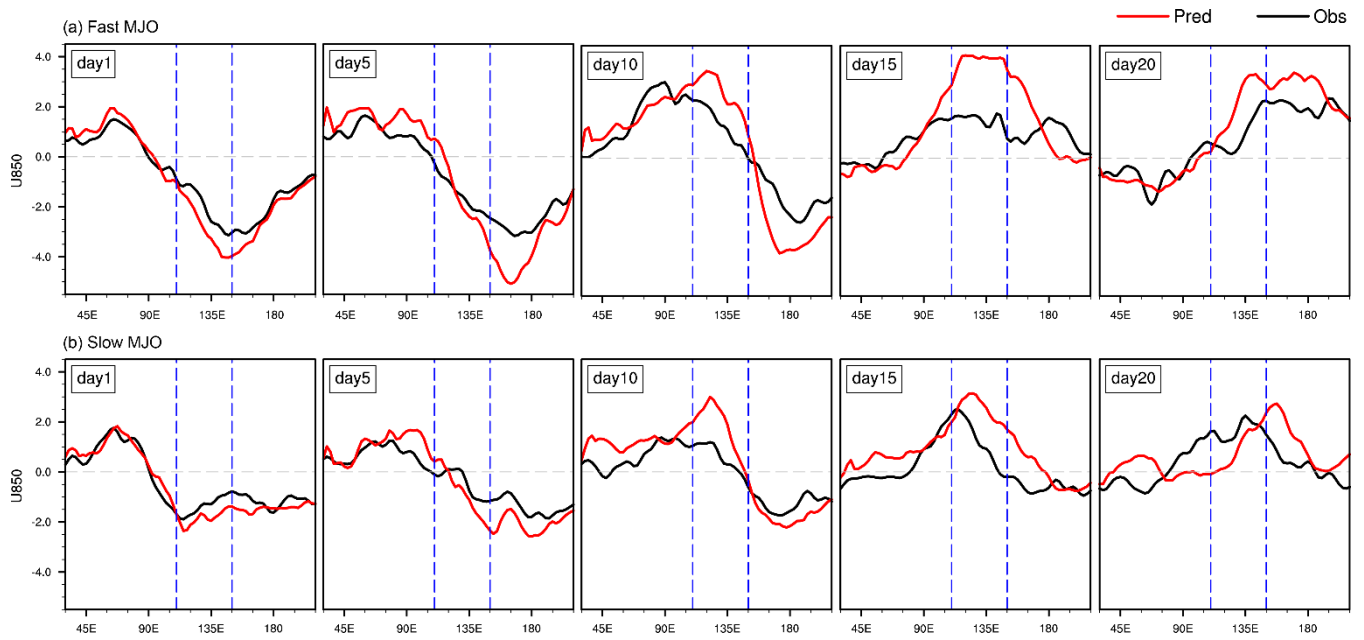
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Figure 9. The composited longitude-vertical structure of precipitation heating (contours; $1 \times 10^{-2} \text{ J kg}^{-1} \text{ s}^{-1}$) and zonal and vertical winds anomalies (vectors; units are m/s for zonal winds and 0.01 Pa s^{-1} for vertical winds) averaged over $10^\circ \text{ S} - 10^\circ \text{ N}$ for day 1, day 5, day 10 in (a) observed fast MJO, (b) simulated fast MJO, (c) observed slow MJO and (d) simulated slow MJO.



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Figure 10. The winter (November–April) mean specific humidity (g kg^{-1}) on 850hPa for (a) observation and (b) IAP-CAS model.



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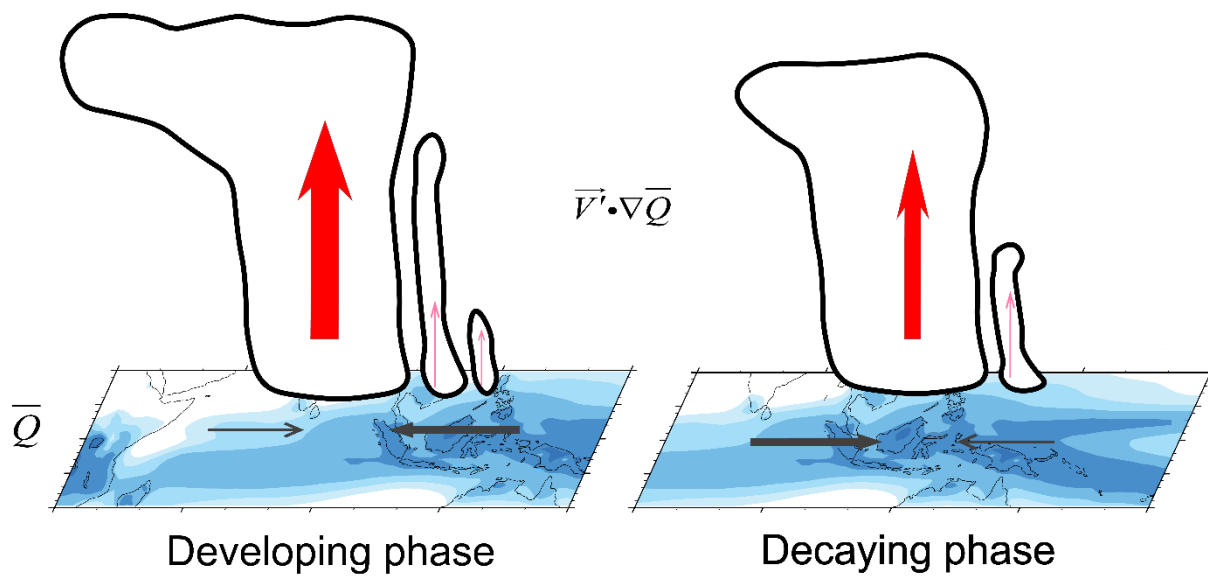
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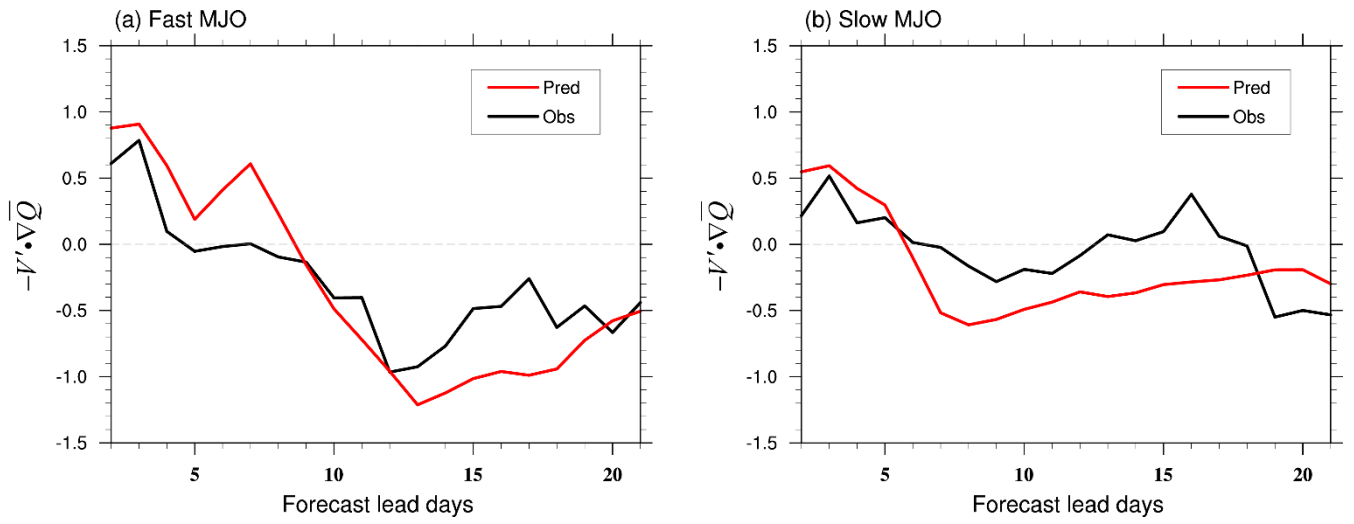
Figure 11. The composited longitudinal structure of the 850hPa zonal wind anomalies (m s^{-1}) averaged over 15°S – 15°N for day 1, day 5, day10, day15 and day 20 from observation (black solid line) and IAP-CAS model (red solid line) in fast and slow MJO events. The gray dashed line is the reference line with the values of 0. The two blue dashed lines are 110°E and 150°E respectively, which denote the extension of the MC region.



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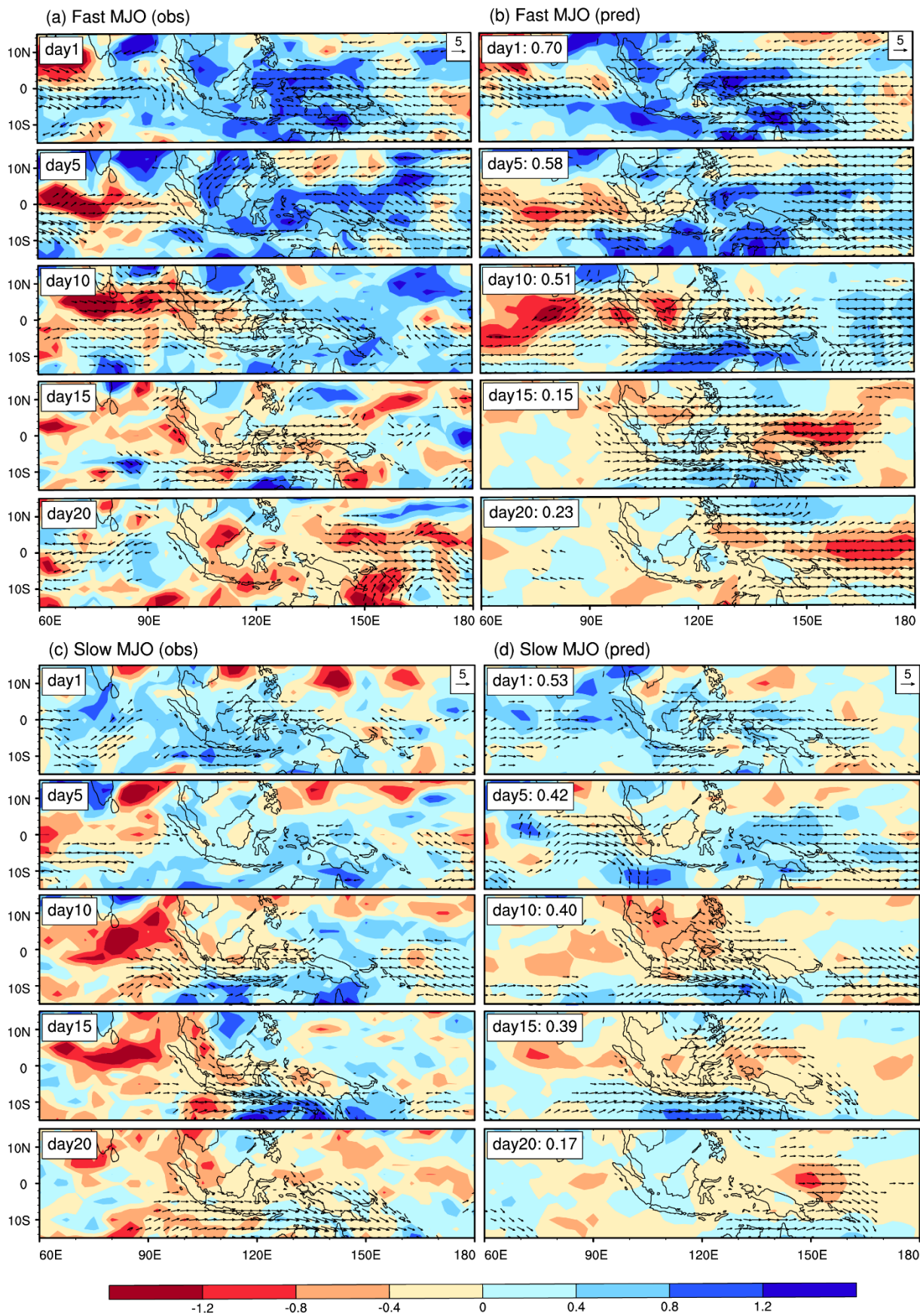
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Figure 12. Schematic diagrams illustrating the moisture mode theory on MJO propagation in the MC region.



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508 **Figure 13.** The composited $-V' \cdot \nabla \bar{Q}$ ($\text{g kg}^{-1} \text{s}^{-1}$) averaged over the MC region (15° S - 15° N , 110° E - 150° E) as a function of forecast
 509 lead days from observation (black solid line) and IAP-CAS model (red solid line) in (a) fast MJO and (b) slow MJO events. The gray
 510 dashed line is the reference line with the values of 0.



511
 512 **Figure 14. Evolution patterns of the composite specific humidity anomalies (g kg^{-1}) and winds (vectors; m s^{-1}) anomalies (exceeding**
 513 **2 m/s) on 850hPa for day 1, day 5, day10, day15 and day 20 (a) observed fast MJO, (b) simulated fast MJO, (c) observed slow MJO**
 514 **and (b) simulated slow MJO. The spatial correlation coefficient between simulated and observed moisture anomalies is shown to the**
 515 **right of panels (b) and (c).**

517 **Table A1 Hybrid coefficient of hybrid sigma-pressure coordinates at layer interfaces in CAS FGOALS-f2**

Layer	Coefficient of pressure coordinates	The coefficient of sigma coordinates	Layer	Coefficient of pressure coordinates	The coefficient of sigma coordinates
1	100.00	0.00	18	27131.33	0.23
2	400.00	0.00	19	24406.11	0.32
3	818.60	0.00	20	21326.05	0.42
4	1378.89	0.00	21	18221.18	0.51
5	2091.80	0.00	22	15275.15	0.59
6	2983.64	0.00	23	12581.68	0.67
7	4121.79	0.00	24	10181.43	0.73
8	5579.22	0.00	25	8081.90	0.79
9	7419.79	0.00	26	6270.87	0.83
10	9704.83	0.00	27	4725.35	0.87
11	12496.34	0.00	28	3417.39	0.91
12	15855.26	0.00	29	2317.75	0.93
13	19839.62	0.00	30	1398.09	0.96
14	24502.73	0.00	31	632.50	0.98
15	28177.10	0.02	32	0.00	0.99
16	29525.28	0.06	33	0.00	1.00
17	29016.34	0.14			

518 **Table A2 Initialization information of the S2S ensemble forecast system**

Nudging type	Data Assimilation	Variable	Data	Frequency
Reanalysis nudging	Time-Lagged Nudging (Hoffman and Kalnay, 1983; Jeuken et al., 1996)	U, V, T, P _s , z _s ^a SST	FNL (http://rda.ucar.edu/datasets/ds083.2 , ds083.2 DOI: 10.5065/D6M043C6) NOAA OISST (Reynolds et al., 2007)	6h
Forecast nudging		U, V, T, P _s , z _s	GFS weather forecast	6h

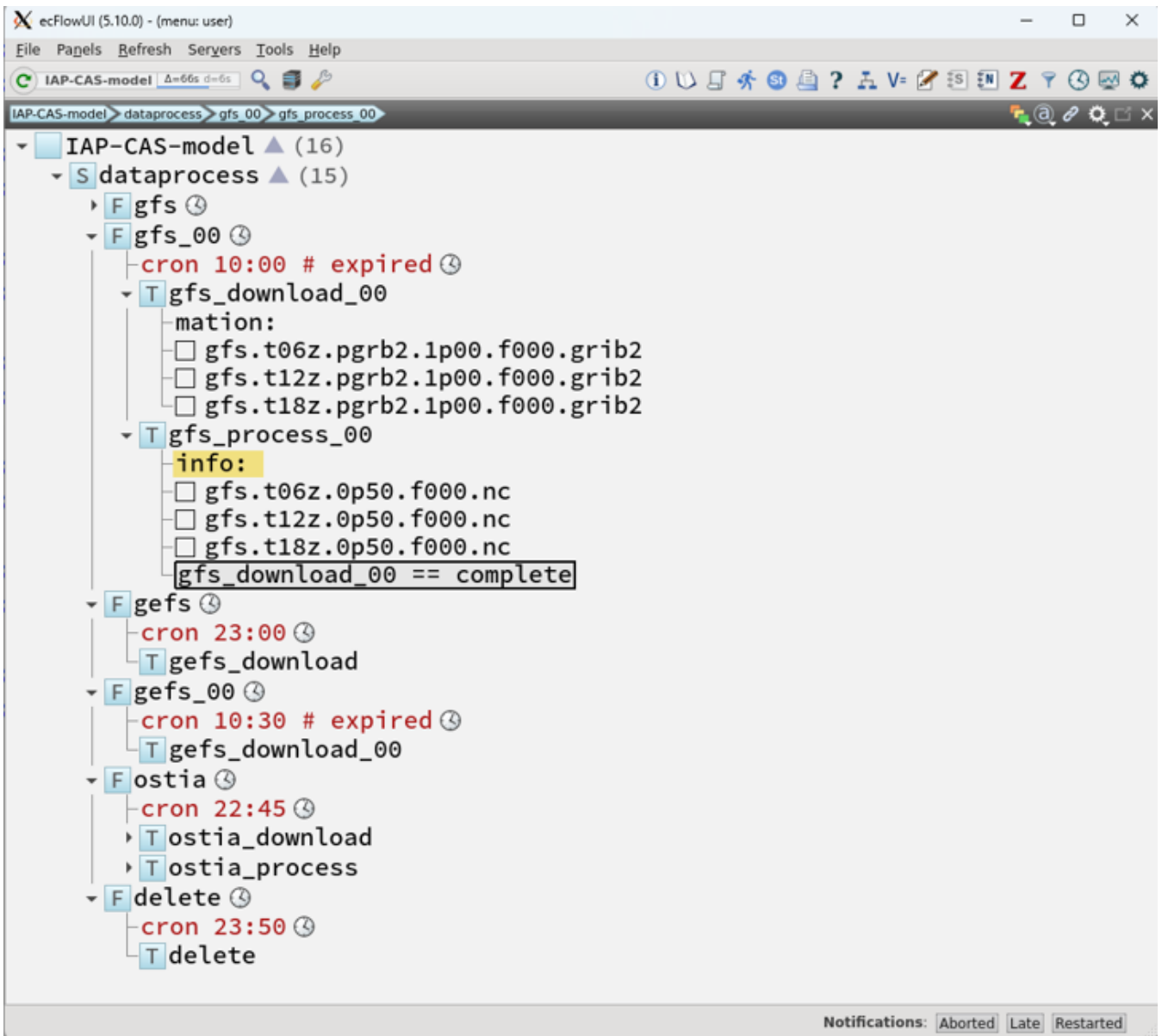
519 ^a Table notes: U represents zonal wind, V represents meridional wind, T represents temperature, P_s represents surface pressure,
520 z_s represents surface geopotential height, and SST represents sea surface temperature.

521 **Table A3 Introduction to the output data of the S2S ensemble forecast system**

Experiment	Ensemble members	Time range	Frequency	Forecast time	Variable	Resolution	Interpolation method
Hindcast	4	1999-2018	Daily	65 days	25 variables	Horizontal:1.5°	One-order
Real-time forecast	16	2019			(A detailed list of variables is shown in TableA4)	×1.5° Vertical:7 levels (1000, 925, 850, 700, 500, 300, and 200hPa)	conservation

Statistical process	Level(s)	Short name	Standard name	Unit	
Instantaneous value/24h	The variables are located on 10 pressure layers (1000, 925, 850, 700, 500, 300, 200, 100, 50, 10 hPa)	gh	Geopotential height	gpm	
		t	Temperature	K	
		u	U-velocity	m s ⁻¹	
		v	V-velocity	m s ⁻¹	
		w	Vertical velocity	pa s ⁻¹	
	The variable is located on 7 pressure layers (1000, 925, 850, 700, 500, 300, 200 hPa)	q	Specific humidity	kg kg ⁻¹	
		2-dimensional variables	w	Vertical velocity	pa s ⁻¹
			sp	Surface pressure	Pa
			lsm	Land sea mask	Proportion of land
			orog	Orography	gpm
Daily average value		tcc	Total cloud cover	%	
		skt	Skin temperature	K	
		2t	Surface air temperature	K	
		2d	Surface air dewpoint temperature	2d	
		wtmp	Sea surface temperature	K	
		ci	Sea ice cover	proportion	

24-hour accumulated value	sf	Snow fall water equivalent	kg m ⁻²
	ttr	Time-integrated top net thermal radiation	W m ⁻² s
	ssr	Time-integrated surface net solar radiation	W m ⁻² s
	str	Time-integrated surface net thermal radiation	W m ⁻² s
	ssrd	Time-integrated surface solar radiation downwards	W m ⁻² s
	strd	Time-integrated surface thermal radiation downwards	W m ⁻² s
Instantaneous value/6h	mx2t6	Surface air maximum temperature	K
	mn2t6	Surface air minimum temperature	K
	10u	10 metre u-velocity	m s ⁻¹
	10v	10 metre v-velocity	m s ⁻¹
6-hour accumulated value	tp	Total precipitation	kg m ⁻²



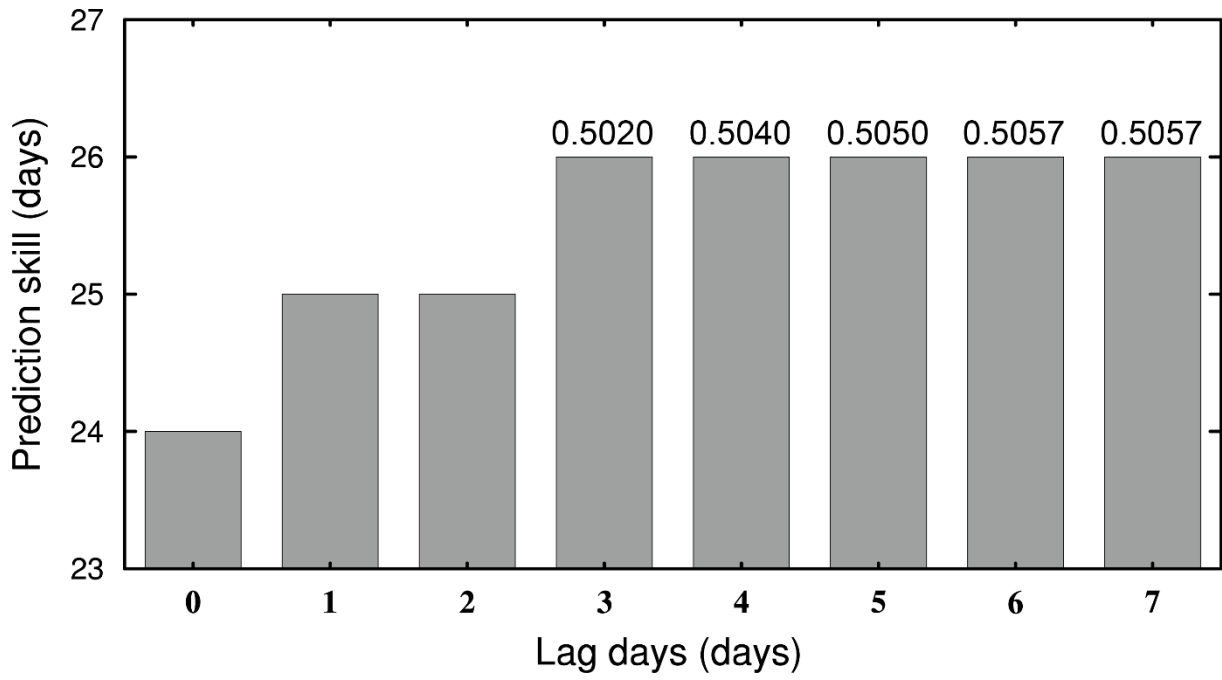
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Figure A1. The structure of ecFlow (ECMWF Workflow). EcFlow, developed and maintained by the ECMWF, is a client/server workflow package designed to facilitate the execution of a substantial number of programs within a controlled environment. It is used in the IAP-CAS model to accomplish the download and preprocessing of the forcing data.



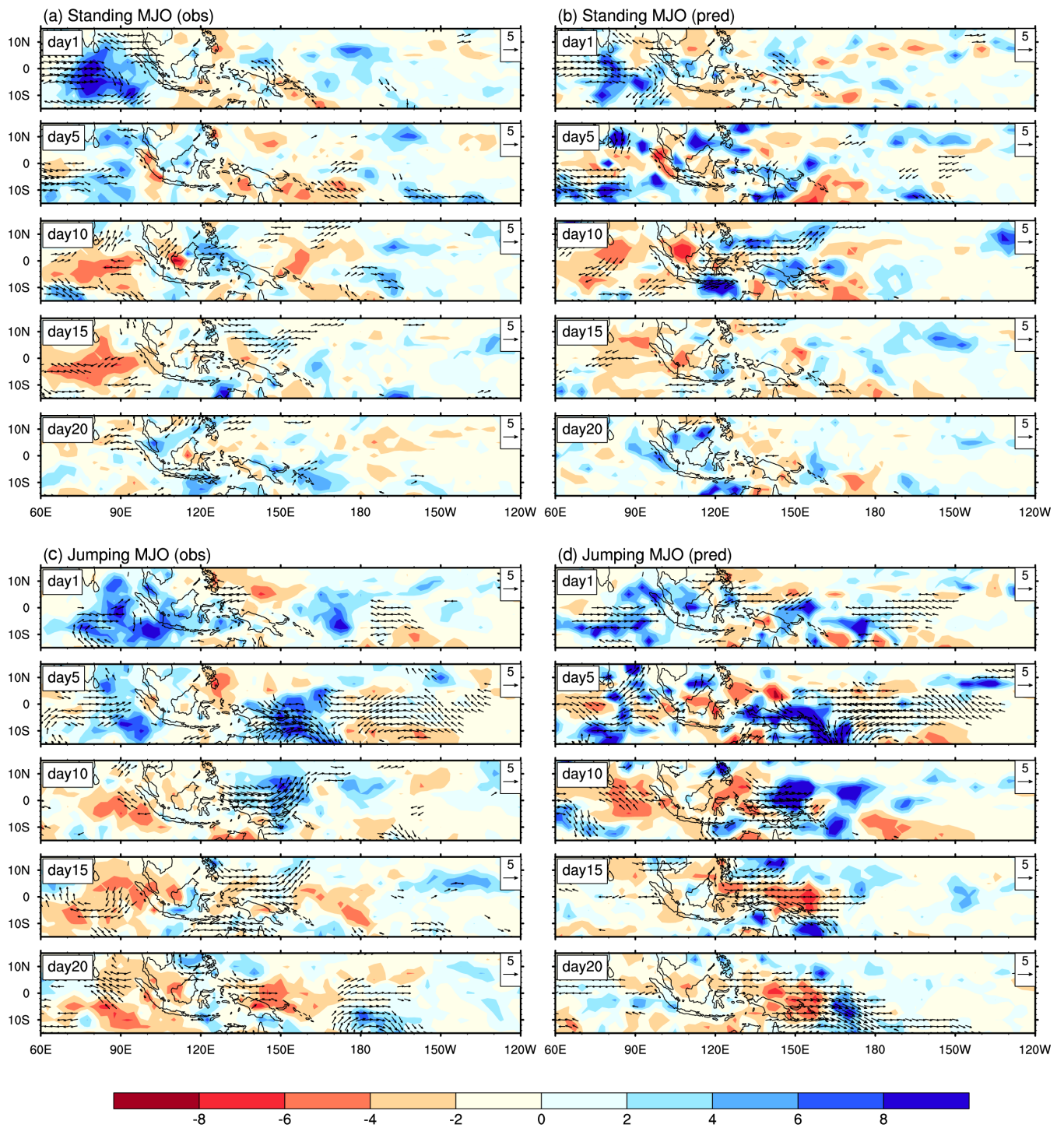
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Figure A2. MJO forecast skill of the ensemble mean of time-lagged members as a function of lag days. The values on the bars represent the ACC on day 26.

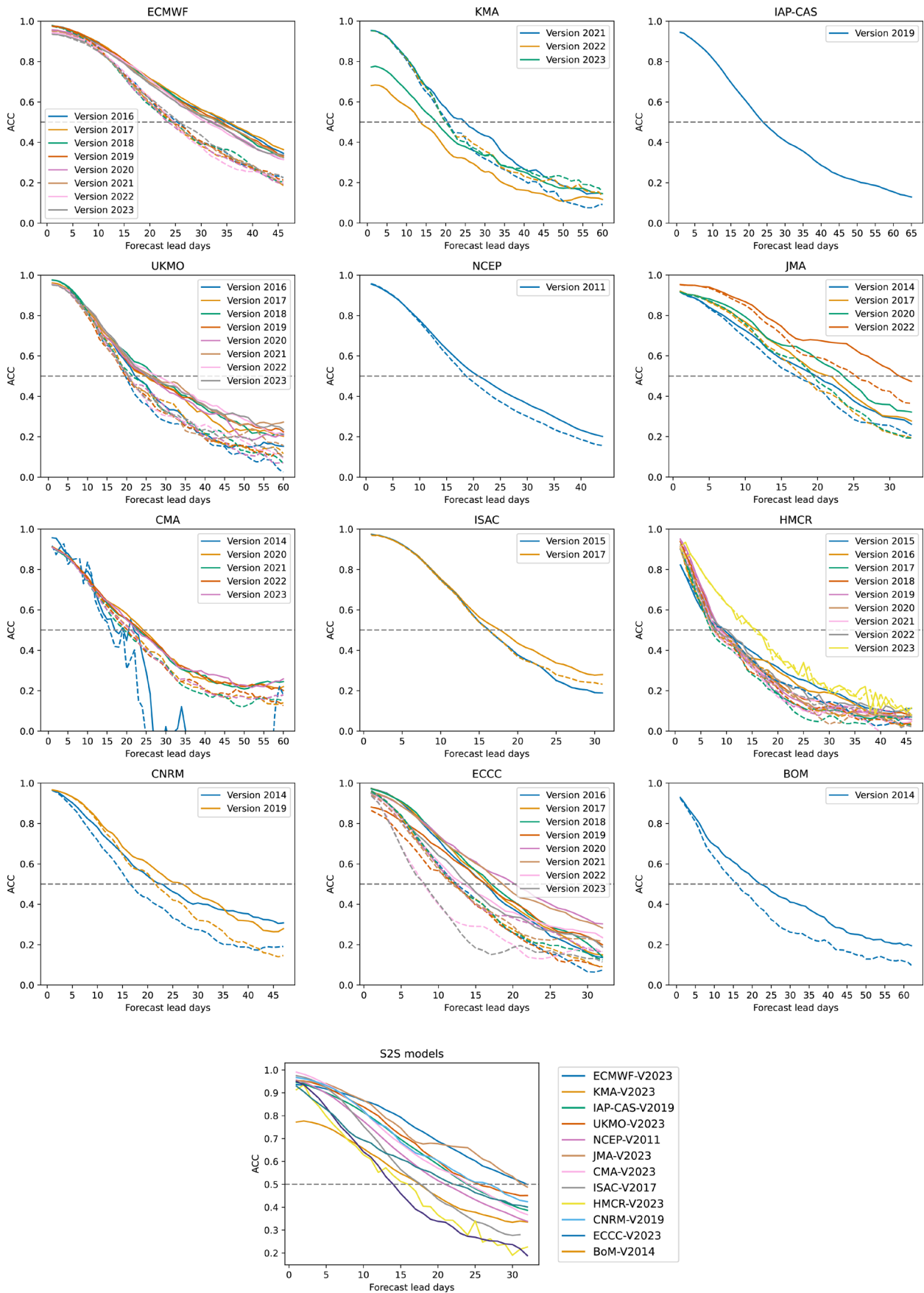
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533 **Figure A3. Evolution patterns of the composite precipitation (shading; mm day⁻¹) and 850-hPa winds (vectors; m s⁻¹) anomalies**
 534 **(exceeding 2 m/s) for day 1, day 5, day10, day15 and day 20 in (a) observed standing MJO, (b) simulated standing MJO, (c) observed**
 535 **Jumping MJO and (d) simulated Jumping MJO.**



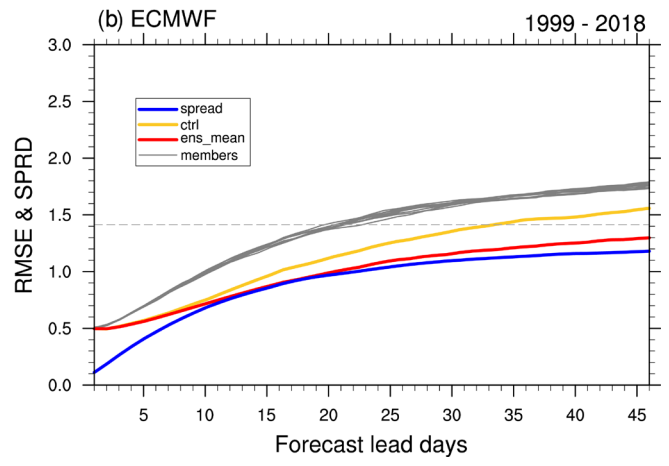
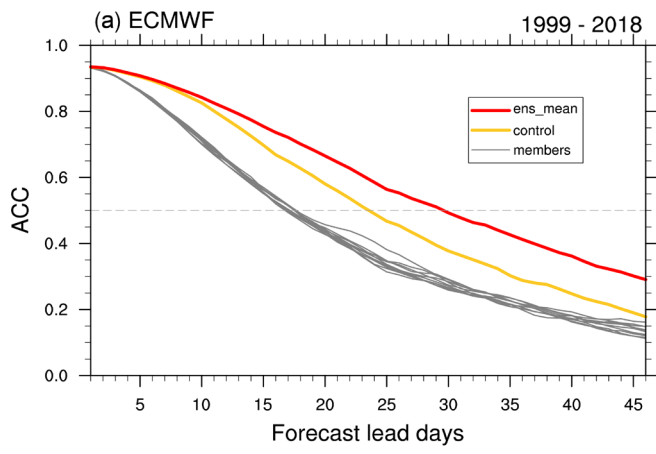
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Figure A4. The MJO forecast skill of 12 S2S models, providing comparisons between various model versions over the years, and the latest versions of 12 models. The evaluation covers the period from 2001 to 2010, except for CMA, which spans from 2008 to 2013. The solid lines represent the skill of ensemble mean forecasts, while the dashed lines represent the skill of deterministic forecasts.



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Figure A5. The ACC (a) and the RMSE (b) of ECMWF (2019 version) from individual members (gray solid line), ensemble ctrl (yellow solid line), and 10-member ensemble mean (red solid line) as a function of forecast lead days. The blue solid line denotes the ensemble spread. The dashed line in (a) has a value of 0.5, and it represents 1.414 in (b).

545 **Code availability**

546 The code of the IAP-CAS model is archived on Zenodo (<https://doi.org/10.5281/zenodo.10791355>). The code used to
547 reproduce the figures in this work can be obtained from <https://doi.org/10.5281/zenodo.10817813>.

548 **Data availability**

549 The boundary conditions and input data are available at <https://doi.org/10.5281/zenodo.10820243>. The data for initial
550 ization in the IAP-CAS S2S system is available at <http://rda.ucar.edu/datasets/ds083.2>, ds083.2|DOI: 10.5065/D6M043-
551 C6 (FNL), <https://www.ncei.noaa.gov/products/optimum-interpolation-sst> (NOAA OISST) and [https://www.ncei.noaa.gov-](https://www.ncei.noaa.gov/products/weather-climate-models/global-forecast)
552 [v/products/weather-climate-models/global-forecast](https://www.ncei.noaa.gov/products/weather-climate-models/global-forecast) (GFS weather forecast). The hindcast dataset of the IAP-CAS S2S
553 system used in the article is publicly available on the three S2S Data Portals (ECMWF: [https://apps.ecmwf.int/data-](https://apps.ecmwf.int/datasets/)
554 [sets/](https://apps.ecmwf.int/datasets/); CMA: <http://s2s.cma.cn/index>; IRI: [https://iridl.ldeo.columb-ia.edu/SOURCES/ECMWF/S2S/](https://iridl.ldeo.columbia.edu/SOURCES/ECMWF/S2S/)). All the validation
555 data are available to download from the cited references or data links shown in Section 3.1.

556 **Author contribution**

557 Q.B. led the IAP-CAS model development. All other co-authors contributed to it. B.H. and X.F.W. designed the experiments
558 and carried them out. Y.K.L. utilized the dataset to assess the performance of the IAP-CAS S2S system and wrote the final
559 document with contributions from all other authors. Q.B. reviewed and edited the manuscript. G.X.W., Y.M.L., and J.Y.
560 supervised and supported this research and gave important opinions.

561 **Competing interests**

562 The authors declare no conflict of interest.

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