

# Research of mechanical model based on characteristics of fracture mechanics of ice cutting for scientific drilling in polar region

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**Abstract:** Scientific drilling in polar regions plays a crucial role in obtaining ice cores and using them to understand climate change and to study the dynamics of the polar ice sheet and its impact on global environmental changes (sea level, ocean current cycle, atmospheric circulation, etc.). Mechanical rotary cutting is a widely used drilling method that drives the cutter to rotate to cut and drill through ice layers. It is necessary to conduct in-depth research on the brittle fracture behavior of ice and mechanical model, and analyze the factors and specific mechanisms (cutter's angle, rotation speed of the drill bit, and cutting depth) affecting cutting force for the rational design of ice-core drill system, improving the efficiency of ice-core drilling, and ensuring the drilling process smoothly. Therefore, in this paper, the process of ice cutting was observed, the fracture mechanics characteristics of ice cutting process was analyzed, the formation process of ice chips was divided into three stages, and the mathematical model for the cutting force was established based on the observation results. It describes the damage conditions of ice failure and points out the influencing factors and specific influencing laws on cutting force. Furthermore, the cutting force generated under various experimental conditions was tested. Based on typical real-time data curves of cutting force, the characteristics of cutting force were analyzed during the cutting and drilling process. Based on the comparison results of the average cutting force, the influence mechanism of various parameters on the cutting force is obtained. This proves the correctness of the mathematical model of the cutting force and provides a theoretical reference for the calculation of cutting force during ice cutting and drilling in polar regions.

## 1. Introduction

30 As the largest cold source on Earth, Polar ice sheets/glaciers are an important component of the  
31 Earth's system related to the Earth's crust, glaciers, ice shelf, ocean, and atmosphere, it has a profound  
32 impact on global changes such as climate change and sea level rise et al (Lin Yang et al., 2023). Many  
33 scientific issues related to polar regions can be solved and validated by carrying out scientific drilling  
34 in ice sheets and obtaining ice cores (S.H. Faria et al., 2014; P. Talalay et al., 2015; P.L. Cao et al.,  
35 2019). Mechanical rotary drills have been widely used in the field of polar ice core drilling (Ueda and  
36 Garfield, 1968, 1969; Gundestrup et al., 1984; Kudryashov et al., 1994; Stanford, 1992; Wumkes, 1994;  
37 Shturmakov et al., 2007). The process of ice core drilling mainly consists of three steps: Cutting and  
38 drilling of the ice sheet, removal and transport of the ice chips generated at the hole bottom, and the  
39 collection of ice core and chips precipitation (Litvinenko VS and Nikolay I Vasiliev et al., 2014). These  
40 three steps are interrelated, and all of them have significant effects on the process of drilling. The  
41 cutting and drilling of the ice sheet generate a cutting force, which not only affects the selection of the  
42 motor system of the drill but also the design of the anti-torsion system, and even determines the success  
43 or failure of the cutting and drilling of the ice sheet. By conducting in-depth research on the fracture  
44 mechanics characteristics of solid ice, establishing a mechanical model for ice cutting, and determining  
45 the factors and specific mechanisms affecting cutting force, it can contribute to the rational design of  
46 the drilling tool system, the improvement of drilling efficiency, and ensure the smooth progress of  
47 drilling.

48 During ice core drilling, ice cutting is periodically carried out. At first, the moving cutters cut into  
49 the ice and compress it. When the level of stress near the edge of the cutter exceeds the cutting point, a  
50 crack is formed in the direction from the edge to the surface. This means that the horizontal force of  
51 cutting, called  $P_x$ , creates a repeated series of breaks, and its value is considered to be the mean force  
52 over the cutting length. Griffith (1920) assumed that when the energy of elastic strain exceeds the  
53 surface energy, the existing micro-crack starts to extend like an avalanche, and the materials break.  
54 Mellor and Sellman (1976) suggested that cutting force  $P_x$  can be calculated by using specific energy  
55  $E_S$  (N/m<sup>2</sup>), which is the energy consumed per unit of cutting volume:

$$56 \quad P_x = bhE_S \quad (1)$$

57 where  $b$  is the width of the cutter;  $h$  is the depth of cut.

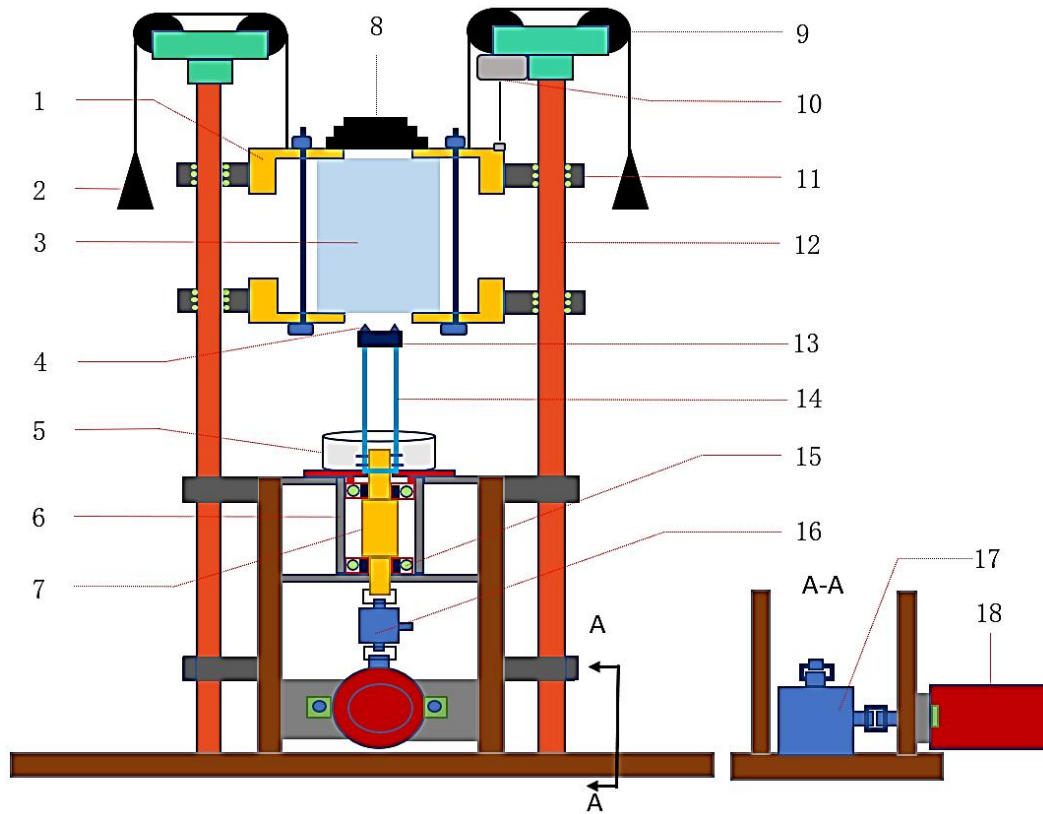
58 Using the formula (1) to calculate cutting force is difficult because specific energy is a vague  
59 concept. The formula ignores the influence of the structure of the cutter on the cutting force and lacks a  
60 certain degree of practicality. Due to the difficulty of conducting strict theoretical methods for the  
61 design of rock-cutting machines, many of the same experimental methods were developed by Mellor  
62 (1981). Maeno (1988) assumed that in any deformation process caused by compression, tension,  
63 bending, or cutting, the mechanics of ice failure are determined by the processes of inter/intragrain  
64 sliding. Taking the ideal monocrystal of ice, the theoretical stress needed for the formation of sliding  
65 zones is near 100 MPa, but for real ice, it does not exceed 0.1– 0.5 MPa (Lavrov, 1969). The  
66 contradiction is explained by the disposition theory. According to this theory, the deformation of the  
67 ice is determined by the defects which already exist in the ice crystal. The internal defects gradually  
68 expand under the action of external forces, the ice destruction occurs. Due to the non-uniformity, hard  
69 brittle, and the factors that affect cutting resistance are complex, most studies on solid ice are  
70 conducted to investigate the influence of a certain variable on cutting resistance (Chiaia, 2008; S. Hell  
71 et al., 2014; A. Chao Correias et al., 2022). The in-depth study of the cutting properties of solid ice was  
72 rarely reported.

73 In this paper, images of the cutting and drilling process of the ice under various experimental  
74 conditions were captured, the fracture mechanics characteristics of the ice cutting process were  
75 analyzed, and the formation process of ice chips was clear and divided into three stages. Based on the  
76 result, a mechanics and mathematical model of ice cutting was built, and the influencing factors and  
77 specific influencing laws on cutting force were analyzed. Finally, the influencing factors and laws were  
78 verified through experimental tests. Which provides a theoretical reference for the calculation of  
79 cutting force during ice cutting and drilling.

## 80 **2. Observation of ice fissure propagation in the process of ice cutting for ice-core drilling**

### 81 **2.1. Test stand design for study on ice cutting process**

82 To observe the cutting and drilling process of the ice under various experimental conditions, an ice  
83 cutting and drilling simulation test stand has been designed (Fig. 1).



84

85 **Figure 1.** Schematic diagram of the experimental platform: 1-ice box; 2-balance weight 1; 3-ice block; 4-cutter;  
 86 5-ice chips collector; 6-cup set; 7-stepped shaft; 8-dead weight; 9-fixed pulley; 10-draw-wire displacement sensor;  
 87 11-slider; 12- slide rail; 13-drill bit; 14- drill pipe; 15- bearing; 16-torque sensor; 17- directional converter;  
 88 18-servo motor

89 To ensure the ice cutting and drilling proceed smoothly and the WOB is constant during the drilling  
 90 process, the drilling direction is inverted upward. Therefore, the ice chips generated in the drilling  
 91 process directly fall into the ice chips collector due to gravity, there will be no adhesion or blockage on  
 92 the drill bit. During the experimental process, the ice block and ice box can slide nearly frictionless as  
 93 they are connected to two parallel slide rails through four sliders, and the slider is equipped with rolling  
 94 balls inside to ensure that the slider slides almost frictionless on the slide rail. So, during the drilling  
 95 process, constant drilling pressure can be ensured, and multiple drilling pressure tests can be achieved  
 96 by increasing or decreasing balance weight and dead weight. The drill pipe, drill bit, and cutters are  
 97 driven to rotate by the servo motor system, and its rotation speed can be adjusted arbitrarily between  
 98 0-1000rpm. In this way, the adjustment of the rotation speed of the drill bit is achieved. The cutter  
 99 equipped in the experimental test stand can be replaced arbitrarily according to the experimental

100 requirements, therefore, it is possible to conduct cutting and drilling tests on cutters with various  
101 structures.

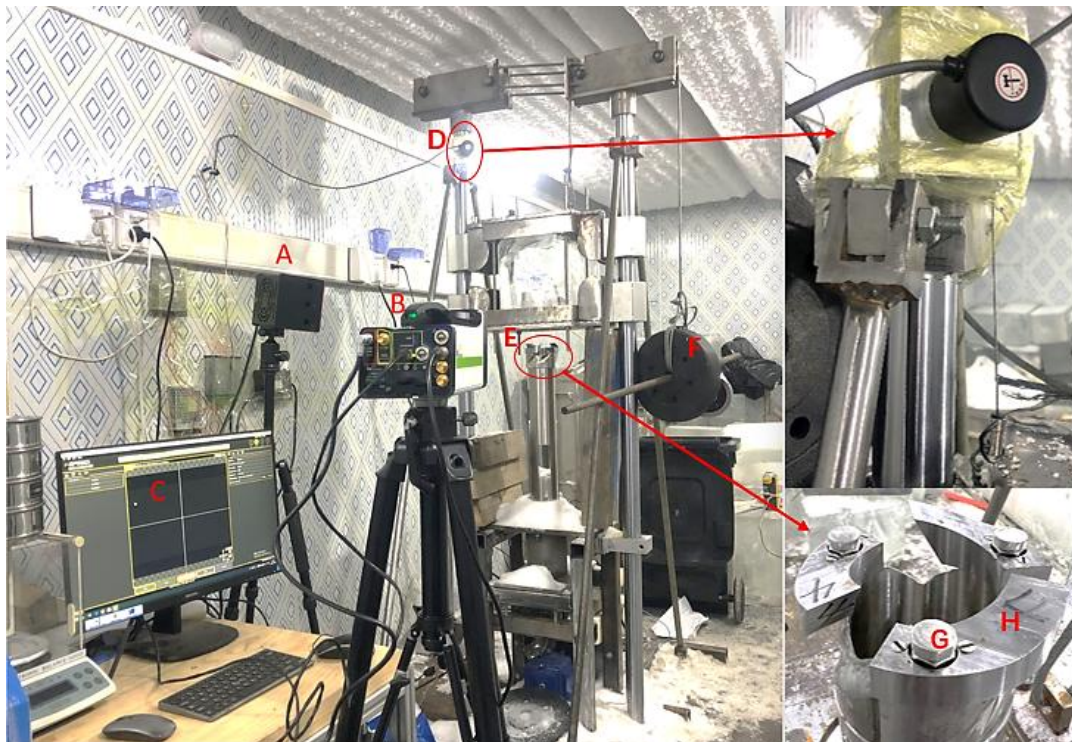
102 During the experiment, the torque generated by driving the rotation of drill pipes, step shafts, and  
103 other components, as well as the cutting torque generated by ice cutting is measured by the torque  
104 sensor. Before conducting the cutting and drilling experiment, adjust the rotation speed of the drill bit  
105 to the rotation speed for the next experiment, and let the drill bit and other components blank run. After  
106 the torque measured by the torque sensor stabilizes, the torque is recorded as  $T_1$ . Next, perform cutting  
107 and drilling. After the cutting and drilling process stabilizes, the recording of cutting torque begins.  
108 after the drilling process, the average cutting torque during this period is recorded as  $T_2$ . So, the torque  
109 for ice blocks cutting  $T_c$  can be calculated according to the following formula (2).

110 
$$T_c = T_2 - T_1 \quad (2)$$

111 The drilling depth and time are measured by the Draw-wire displacement sensor. The formation  
112 process of ice chips is captured by a high-speed camera.

## 113 2.2. Test stand building and observation of ice fissure propagation during ice-core drilling testing

114 Based on the above working principle, the ice core drilling test stand has been established (Fig. 2).



115

116 **Figure 2.** Test stand: A-light source; B-high speed camera; C-image display computer; D-draw-wire  
 117 displacement sensor; E-drill bit; F-counterweight block; G-drill bit shoe; H-cutter

118 The specific parameters of the main equipment in the test stand are shown in Table 1.

119 **Table 1.** Main parameters of equipment

equipment and sensor	Model	Main parameters
		Drive voltage: 130-220VAC
Driver	3DM2080-DSP	Pulse mode: Mono pulse
		Adjustment range: 0-1000rpm
Servo motor system	Motor 130BYG350D	Maximum output torque: 60N.M
		Step angle: 1.2°
		Rated voltage and current: 220V and 8.5A
Pulse generator	CS10-3	Output mode: Steering + pulse
		Adjustment range: 0-1000rpm
		Output signal voltage: 5V; Power range:9-30V
Torque sensor	LLBLS-I	Measuring range: 60N.M: Overall accuracy:0.3%
		Maximum speed: 6000rpm
Draw-wire displacement sensor	MPS-M	Measuring distance:0-1500mm
		Resolving power:0.01mm;
		Pulling force of stay wire:4N
Slide rail and slider system	Ø50; SK50	Friction coefficient: 0.0010-0.0015
		Technology: CMOS active pixel
		Resolution: 2048×1536
High-speed camera	Ispeed-7	Frames per second: 1000000fps
		Shutter: 1us
		Lens options: F mount/G mount/C mount

120 Before the experiment, the cutters (Fig.2.H) made from tool steel (W18Cr4V) shall be installed on  
 121 the drill bit (Fig.2.E) through bolts and pins (Fig.2.H) that also serve as the shoes with adjustable height.  
 122 The height of the bolts is lower than the height of the cutter's tip when the ice block slides into contact  
 123 with the shoes, the cutters have been cut into the ice block at the designed depth. Thus, the cutting and  
 124 drilling at the designed cutting depth is realized and the cutting depth has been accurately controlled.

125 Aiming the high-speed camera (Fig.2.B) at the cutting edge of the cutter, adjusting the frame number  
 126 of the high-speed camera to 100,000, meanwhile, supplementing the light on the object with the light  
 127 source (Fig.2.A), until the image displayed in the computer (Fig.2.C) is clear. After the experiment, the  
 128 images of the formation process of ice chips are captured and saved in a high-speed camera. The  
 129 observation experiment of the cutting and drilling process is conducted under various experimental

130 conditions (multiple cutter angles, cutting depths, and rotation speed of drill bit). The specific  
 131 parameters of experimental conditions are shown in Table 2. [The cutter used in the experimental](#)  
 132 [process are processed with wire cut technology. Before the experimental, to prevent the impact of](#)  
 133 [surface burrs, slag, and surface roughness on the test results, sandpapers with 1000 mesh, 1500 mesh,](#)  
 134 [and 2000 mesh were selected respectively to manually polish the surface of the cutter until it was](#)  
 135 [smooth. After each test, the surface and cutting edge of the cutter are observed, if there is wear or](#)  
 136 [damage, the cutter is polished or replaced directly.](#) The cutters\_ tested in the experiment are shown in  
 137 Fig. 3.

138 **Table 2.** The specific parameters of experimental conditions

Structure of cutter						
Width (mm)	Rake angle (°)	Relief angle (°)	Cutting depth (mm)	Rotation speed (rpm)	Ice sample dimension (mm)	Ice core diameter (mm)
25	20	5	1	50	~250×250×450	60
	30	10	2	100		
	40	15	3	150		



139  
 140 **Figure 3.** Multi-group structure cutters

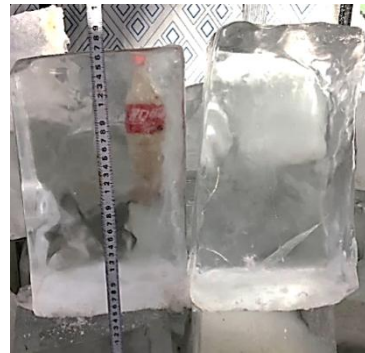
141 This study mainly focuses on the establishment of mechanical model during the ice cutting and  
 142 drilling process. And, studies have shown that the crystal orientation, the crystal size and the density of  
 143 ice samples in NGRIP boreholes in Greenland are similar to naturally formed and artificially frozen ice  
 144 samples (Center for Ice and Climate, 2023). Moreover, many scholars have conducted experiments on  
 145 artificially prepared or naturally formed ice samples, and have ultimately obtained convincing  
 146 experimental data and conclusions, providing valuable references for research in the polar field  
 147 (Talalay, 2003; Hong et al.,2015; Wang et al, 2024). In order to better observe the formation process of

148 ice chip, at present stage, this study selected transparent ice and explored the fracture process and  
149 cutting force generated by this type of ice. The ice with variety properties belongs to brittle materials,  
150 and there will be similarities in the fracture process. In the future, the cutting and drilling experiments  
151 with different ice sample properties to explores the effect of ice properties against the cutting force will  
152 be carried out. The ice blocks used in this experiment are frozen by an ice-making machine (Fig.4),  
153 which can produce transparent ice samples without bubbles. Then, we divided these blocks into  
154 experimental ice blocks with uniform dimensions (Fig.5) of  $\sim 250 \times 250 \times 450$  mm. and all tests were  
155 carried out in the refrigerated container with a constant temperature of  $-15^{\circ}\text{C}$ .



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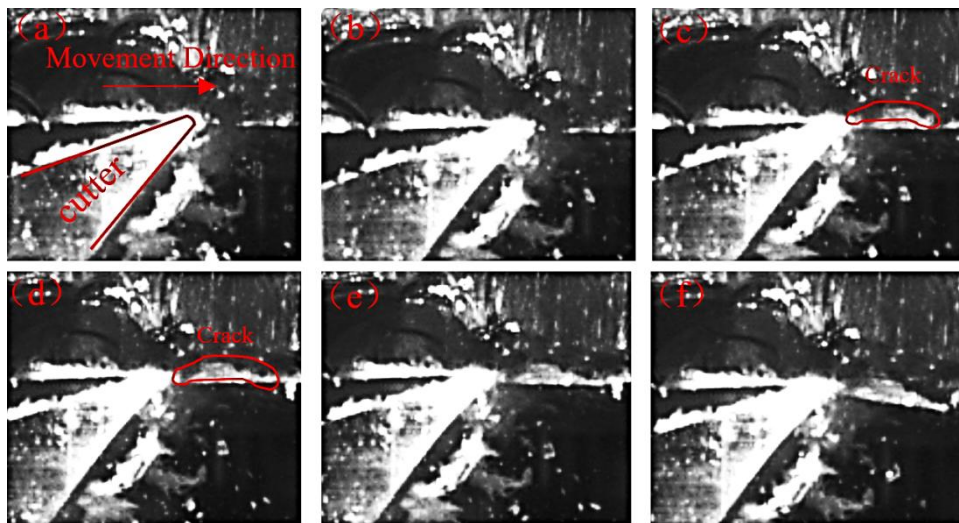
157 **Figure 4.** Ice-making machine



158 **Figure 5.** Experimental ice samples

### 159 **3. Analysis of characteristics of ice fracture mechanics in the process of ice cutting**

160 It is preliminary observed after the mechanical testing of ice under the special experimental  
161 condition. The actual ice-cutting process captured by a high-speed camera is shown in Fig. 6.



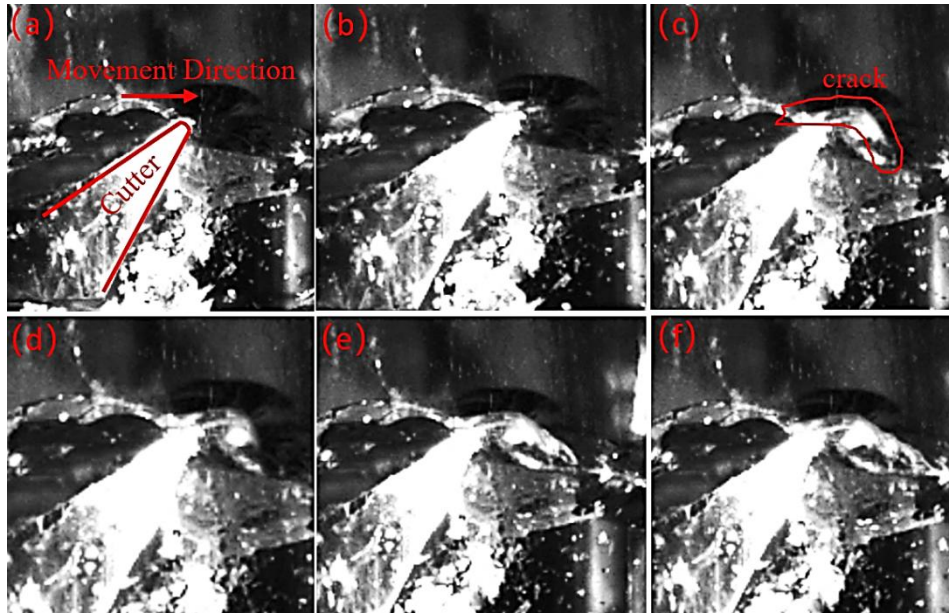
161

162 A (rake angle is  $40^{\circ}$ , relief angle is  $15^{\circ}$ , cutting depth is 1 mm and the rotation speed of the drill bit is

163

100 rpm)





164

165

B (rake angle is  $30^\circ$ , relief angle is  $25^\circ$ , cutting depth is 2 mm and the rotation speed of the drill bit is

166

100 rpm)

167

**Figure 6.** Cutting process captured by high-speed video camera

168

Compared with the cutting and drilling process at a cutting depth of 1mm, when cutting and drilling at a cutting depth of 2mm, the depth of the cutter inserted into the ice sample increases resulting in more small particle ice chips. The particle size of the ice chips formed by major fracture increases, and the surface after cutting becomes more uneven.

172

Under various experimental conditions, the ice cutting process is similar. In the cutting process, the cutting of the ice is constantly repeated, the main damaged form of ice is a brittle fracture, the chips show wedge block with no significantly deform, and wedge-shaped ice chips with different particle sizes are constantly formed under variety experimental conditions. The formation process of a single large particle of ice chips can be divided into three stages. In the first stage, the cutter invades the ice, and the ice is compressed by the rake and relief surfaces of the cutter, resulting in ice crushing and smaller ice chip formation (Fig. 6. a, b). In the second stage, with the rotation of the drill bit, cracks appeared in the ice, and the cracks began to expand along a direction that approximately presented an angle of  $45^\circ$  with the horizontal direction (Fig. 6. c, d). However, there were no gaps or separations between the ice and cutters on both sides of the cracks. In the third stage, the cutter moved forward, the crack expanded to form ice chips with large particle size that slid forward, and finally detached from

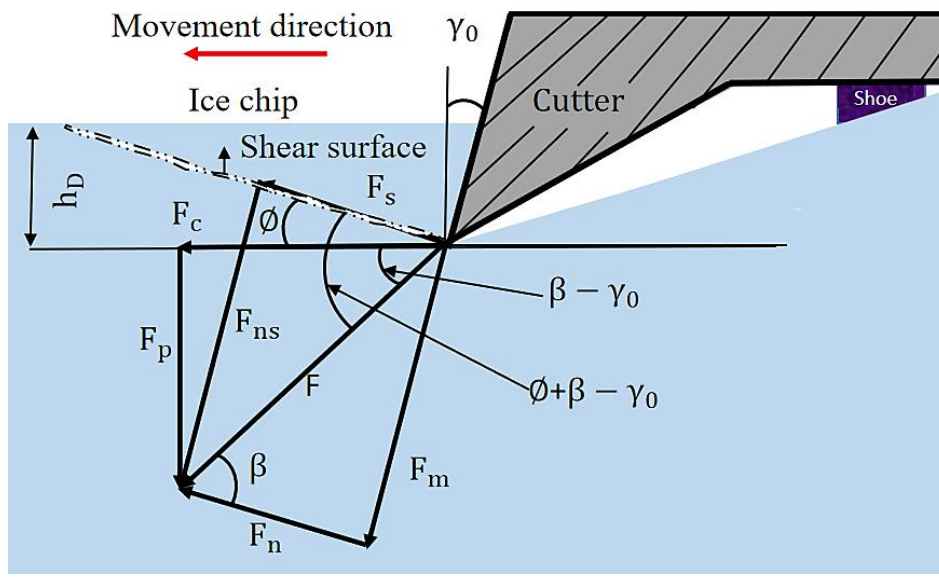
182

183 the ice. At the same time, ice chips with small particle sizes were also generated on the sliding surface  
 184 (Fig. 6. e, f).

#### 185 4. Study on a mechanical model of ice cutting process

##### 186 4.1. Mechanical model building based on the characteristics of ice fracture mechanics

187 According to the observation results of the ice cutting, it can be considered that the damage of the ice  
 188 is the result of shear slip failure caused by the compression effect of the cutter. In this process, the force  
 189 exerted on the ice chips mainly includes the squeezing force  $F_n$  towards the ice, and along the normal  
 190 direction of the cutter's rake face. The frictional force  $F_m$  exerted by the cutter when the ice chips  
 191 flow out; At the same time, the shear surface of the ice will also be subjected to normal pressure  $F_{ns}$   
 192 and shear force  $F_s$ . Before the cutting of the ice, these two pairs of forces are in equilibrium. The  
 193 relationships between these forces are analyzed in front of the cutting edge (Fig. 7).



194  
 195 **Figure 7.** Relationship between force and angle

196 Where  $F$  is the combined force of  $F_m$  and  $F_n$ ,  $\phi$  is the shear angle,  $\beta$  (Friction angle) is the angle  
 197 between  $F_n$  and  $F$ ,  $\gamma_0$  is the rake angle of the cutter,  $F_p$  is the component force perpendicular to the  
 198 movement direction of the cutter, which is applied to the cutter and mainly provided by the weight on  
 199 drill bit during the ice layer cutting and drilling, causing the cutter to cut into the ice to a certain depth.  
 200 During the cutting and drilling process, the cutter comes into contact with the ice sample before the  
 201 shoes. Only when the cutter is inserted into the ice layer with designed cutting depth, the shoes will  
 202 fully contact the bottom of the borehole. Prior to this, there will be continuous  $F_p$  on the cutter. As the

203 drill bit rotates, the cutter always inserts the ice sample before the shoe, and the  $F_p$  on the cutter will  
 204 continue to exist. Where  $F_c$  is the component force acting on the ice layer, and during the ice layer  
 205 cutting and drilling process, this force is mainly provided by the motor, which is called the cutting  
 206 force.  $h_D$  is the cutting thickness. If the cutting width is represented by  $b_D$ , The cutting width  
 207 represents the width of the annular gap between the ice core and the hole wall in the process of ice  
 208 drilling (cutting width, width of the cutter), The area of the nominal cross-section of the cutting layer is  
 209 represented by  $A_D$  ( $A_D = h_D b_D$ ), The area of shear surface is represented by  $A_s$  ( $A_s = A_D / \sin \phi$ ), the  
 210 shear stress on the shear plane is represented by  $\tau$ , then

$$211 \quad F_s = \tau A_s = \frac{\tau A_D}{\sin \phi} \quad (3)$$

212 According to Fig. 7, it can be concluded that:

$$213 \quad F_s = F \cos (\phi + \beta - \gamma_0) \quad (4)$$

214 According to the relationship between various forces, it can be concluded that:

$$215 \quad F = \frac{F_s}{\cos (\phi + \beta - \gamma_0)} = \frac{\tau A_D}{\sin \phi \cos (\phi + \beta - \gamma_0)} \quad (5)$$

$$216 \quad F_p = F \sin (\beta - \gamma_0) = \frac{\tau A_D \sin (\beta - \gamma_0)}{\sin \phi \cos (\phi + \beta - \gamma_0)} \quad (6)$$

$$217 \quad F_c = F \cos (\beta - \gamma_0) = \frac{\tau A_D \cos (\beta - \gamma_0)}{\sin \phi \cos (\phi + \beta - \gamma_0)} \quad (7)$$

#### 218 4.2. Analysis of factors influencing cutting forces via the mechanical model

219 According to Fig. 7, there is no shear stress in the plane perpendicular to the combined force  $F$ , so  
 220 the main stress is completely determined by the  $F$ . The material is in the state of plane stress, and the  
 221 included angle between the direction of the maximum shear stress and the direction of the maximum  
 222 principal stress is  $45^\circ$ , the included angle between the maximum principal stress and the  $F$  is  $45^\circ$ , then  
 223 there is:

$$224 \quad \phi + \beta - \gamma_0 = \frac{\pi}{4} \quad (8)$$

225 So:

$$226 \quad \phi = \frac{\pi}{4} - \beta + \gamma_0 \quad (9)$$

227 The shear angle  $\phi$  is affected by the rake angle of the cutter  $\gamma_0$  and friction angle  $\beta$ . As the rake  
 228 angle of the cutter  $\gamma_0$  increases, the shear angle  $\phi$  increases; as the friction angle  $\beta$  increases,  $\phi$   
 229 decreases.

230 The area of the nominal cross-section of the cutting layer is represented by  $A_D$  ( $A_D = h_D b_D$ ), The  
 231 area of the shear surface is represented by  $A_s$  ( $A_s = A_D / \sin \phi$ ), the shear stress on the shear plane is  
 232 represented by  $\tau$ , then, according to equation (5) and the relationship between the nominal  
 233 cross-section and the shear plane, it can be obtained that:

$$234 \quad F_c = \frac{\tau A_D \cos(\beta - \gamma_0)}{\sin \phi \cos(\phi + \beta - \gamma_0)} \quad (10)$$

235 When the ice is about to break, the shear stress on the shear plane reaches its maximum value. This  
 236 value is determined by the properties of the ice and will not change as the drilling conditions. Therefore,  
 237 the cutting force is influenced by the cutting width of the cutter and the cutting depth. The cutting force  
 238 shows a linear increasing trend with the increase of the cutting width and the cutting depth. In addition,  
 239 the cutting force is also affected by the shear angle  $\phi$ , friction angle  $\beta$ , and cutter's rake angle  $\gamma_0$ . The  
 240 friction angle  $\beta$  is a certain value as the properties of the ice and cutter's material. The shear angle  $\phi$  is  
 241 determined by the friction angle and the cutter's rake angle as shown in formula (9). Substituting  
 242 equation (9) into (10) and solving for the combined cutting force  $F_c$ , the following equation can be  
 243 given:

$$244 \quad F_c = \frac{\tau h_D b_D \cos(\beta - \gamma_0)}{\sin(\frac{\pi}{4} - \beta + \gamma_0) \cos(\frac{\pi}{4})} \quad (11)$$

245 After simplifying the above equation, it can be obtained that:

$$246 \quad F_c = \frac{2\tau h_D b_D}{1 - \tan(\beta - \gamma_0)} \quad (12)$$

247 It can be seen from the formula (12) that the factors affecting the cutting force mainly consist of four  
 248 sides: The first aspect, it related to the shear strength of the ice, with the increase of shear strength, the  
 249 cutting force increases gradually. The second aspect, it influenced by the cutting depth, with the  
 250 increase of cutting depth, the cutting force increases gradually. The third aspect, it affected by the  
 251 cutting width, with the increase of cutting width, the cutting force increases gradually. Finally, the rake  
 252 angle of the cutter also has an impact on the cutting force. Formula (12) shows that: within the  $\beta -$   
 253  $\gamma_0 \leq \frac{\pi}{2}$  range, as the rake angle of the cutter  $\gamma_0$  increases,  $\beta - \gamma_0$  gradually decreases, and the  
 254  $\tan(\beta - \gamma_0)$  decreases,  $1 - \tan(\beta - \gamma_0)$  increases,  $F_c$  decreases.

255 **5. Test on the characteristics of cutting force and its influencing factors for verifying the**  
 256 **mechanical model**

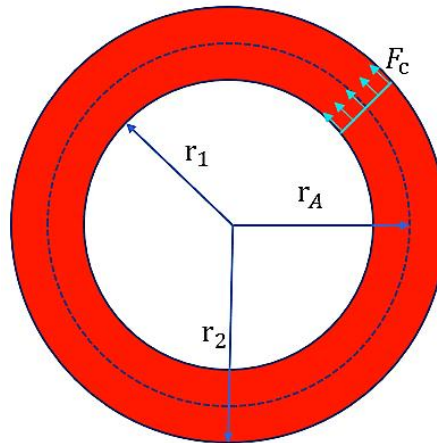
257 **5.1 Analysis of the characteristics of cutting force**

258 To verify the theoretical analysis results of the factors affecting cutting force, the cutting torque  
259 collected by the torque sensor under various cutter angles, rotation speed of the drill bit, and cutting  
260 depth conditions were measured.

261 After the experiment, the torque for ice cutting and drilling can be obtained through formula (2). The  
262 schematic diagram of the torque and cutting force generated during the ice cutting drilling process is  
263 shown in Figure 8, The relationship between the cutting force  $F_c$  generated by cutting the area of the  
264 circular ring and the torque  $T_c$  measured by the torque sensor is as follow.

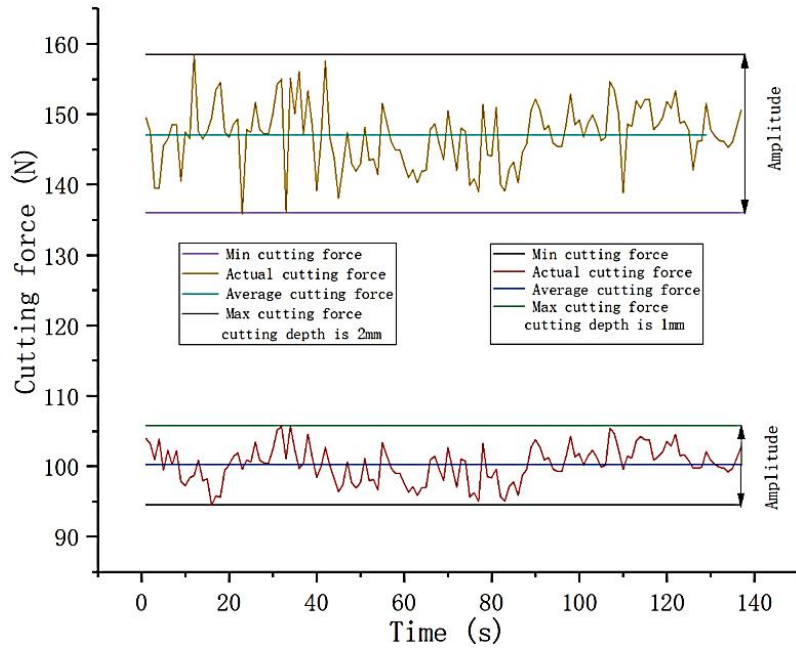
265 
$$T_c = F_c r_A \quad (13)$$

266 Where  $r_A$  is the average radius of the circular ring.



267  
268 **Figure 8.** The schematic diagram of the torque and cutting force

269 By processing the data collected by the torque sensor, the cutting force generated by one cutter  
270 during the ice block cutting and drilling is obtained. The typical cutting force trace generated during the  
271 ice cutting process is shown in Fig. 9.



272

273 **Figure 9.** Typical cutting force trace (Cutting depth is 1 mm and 2 mm; Rotation speed of drill bit is 50rpm; Rake  
 274 angle is 30°; Relief angle is 5°)

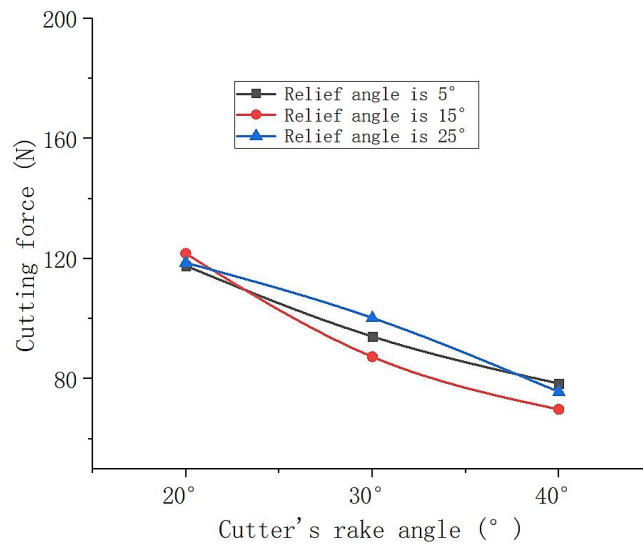
275 Fig. 9 shows the cutting force trace generated during two cutting and drilling process, which were  
 276 carried out under the same conditions except for cutting depth, both cutting force traces oscillate at a  
 277 certain frequency within a certain range, and the oscillation consists primarily of two frequencies, in  
 278 addition the oscillation frequencies of two cutting force trace are similar. The higher frequency is  
 279 related to the resolution of the sensor. The sensor outputs data at a certain interval during the recording  
 280 process, the output data is not continuous, resulting in fluctuations in the trace. The lower frequency is  
 281 related to the formation of large particle ice chips. Unlike ductile materials, where the chips produced  
 282 by a shearing action are continuous and the forces appeared relatively constant, chips from brittle  
 283 materials are produced by a repeated series of breaks. When the cutter is pressed into the ice, the  
 284 cutting force begins to rise and elastic energy is stored in the cutter assembly, some of the energy is  
 285 expended in local crushing, the ice layer undergoes shear-slip deformation. As the cutting force reaches  
 286 a magnitude necessary to induce a major fracture, a crack propagates into the ice, releasing the cutter  
 287 elastic energy and dislodging a major chip, the force than suddenly decreases. Therefore, during the  
 288 cutting and drilling process in the ice layer, the cutting force trace exhibits an oscillating state, the  
 289 amplitude of the oscillation is related to the cutting depth. During the process of the cutting depth  
 290 increase, the degree of rapid increase and decrease in cutting force will be more severe. As show in Fig.

291 9, when drilling with a cutting depth of 2 mm, the oscillation amplitude of cutting force is greater than  
292 that of drilling with a cutting depth of 1 mm.

293 As the cutting depth increases, the degree of crack propagation into the ice will also increase. When  
294 the crack extends into the ice core, it will cause a decrease in the surface quality of the ice core. It is  
295 necessary to control the cutting depth reasonably during the cutting process to ensure the quality of the  
296 ice core. Moreover, the study results on mechanical models of ice cutting process indicated that:  
297 “within the range of  $\beta - \gamma_0 \leq \frac{\pi}{2}$ , the cutting force gradually decreases with the increase of the rake  
298 angle”. The rake angle can be appropriately increases within this range to reduce the oscillation.

### 299 5.2. Test of the factors influencing cutting force

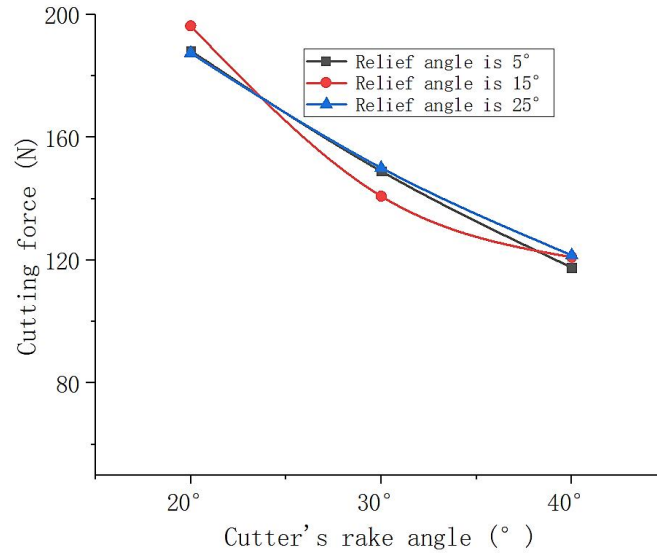
300 After the cutting and drilling experiments, the average cutting force was obtained under each  
301 experimental condition. Plots of the average cutting force versus the cutter’s rake angle are shown in  
302 Fig. 10.



303

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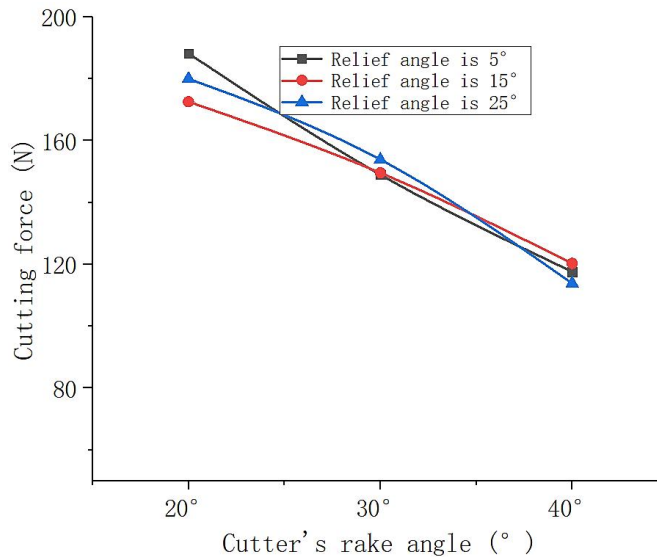
(a) The cutting depth is 1 mm, and the rotation speed of the drill bit is 100rpm



305

306

(b) The cutting depth is 2 mm, and the rotation speed of the drill bit is 100rpm



307

308

(c) The cutting depth is 2 mm, and the rotation speed of the drill bit is 50rpm

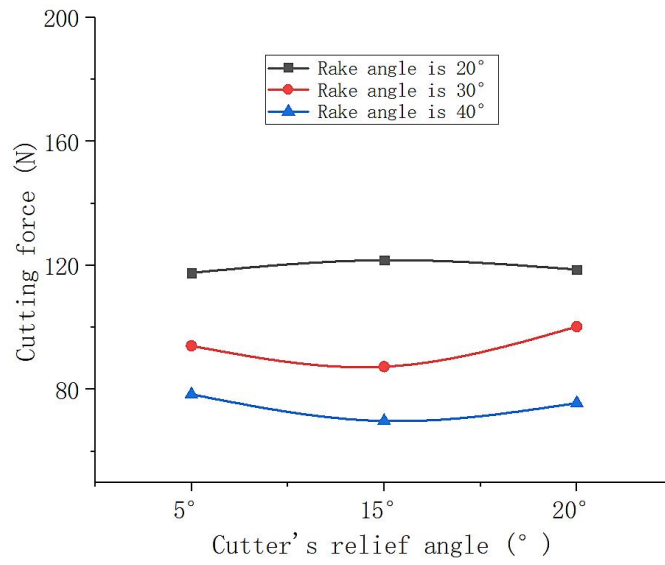
309 **Figure 10.** Cutting force versus cutter's rake angle

310 As shown in Fig. 10, when the cutting depth is 2mm, the rotation speed of the drill bit is 100 rpm,  
 311 and the rake angle of the cutter is 20 °, the cutting force reaches the maximum value of 196.3451N.

312 When the cutting depth is 1mm, the rotation speed of the drill bit is 100 rpm, and the rake angle of the  
 313 cutter is 40 °, the cutting force reaches the minimum value of 69.83529N. The cutting force varies  
 314 within this range under the other experimental conditions. That is, under various cutting depths and  
 315 drill speed conditions, the cutting force gradually decreases with the increase of the cutter's rake angle.

316 Plots of the average cutting force versus the cutter's relief angle are shown in Fig. 11.

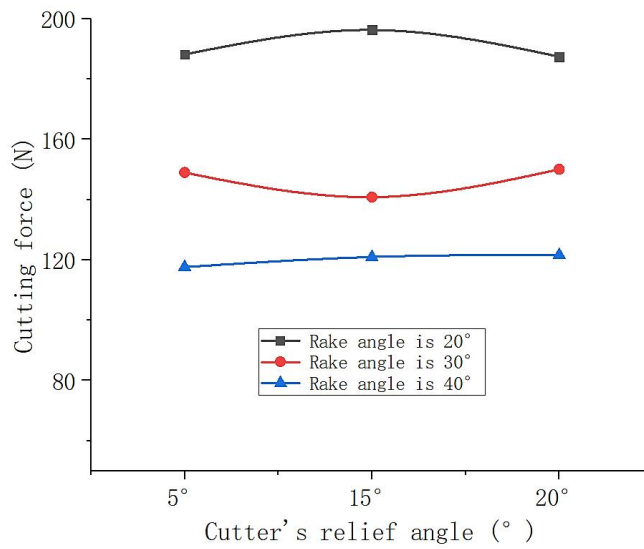




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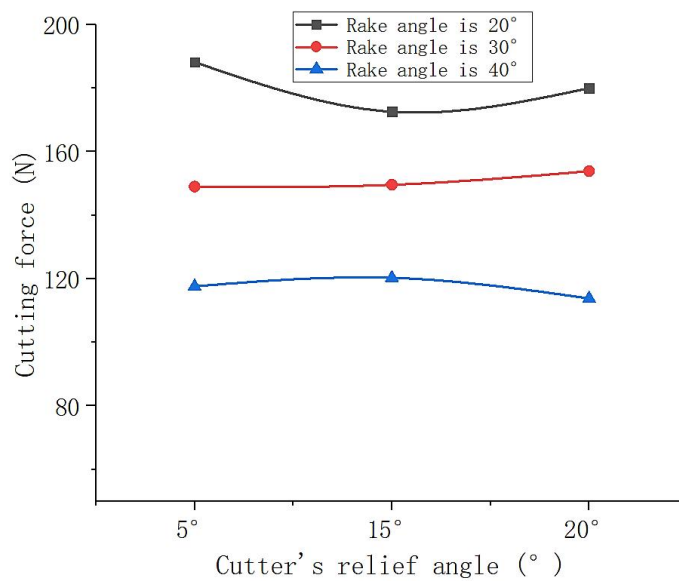
(a) The cutting depth is 1 mm, and the rotation speed of the drill bit is 100rpm



319

320

(b) The cutting depth is 2 mm, and the rotation speed of the drill bit is 100rpm



321

322

(c) The cutting depth is 2 mm, and the rotation speed of the drill bit is 50rpm

323

**Figure 11.** Cutting force versus cutter's relief angle

324

Under various experimental conditions, the relief angle of the cutter changes, and the cutting force

325

only changes slightly. Moreover, with the change of the relief angle of the cutter, the cutting force does

326

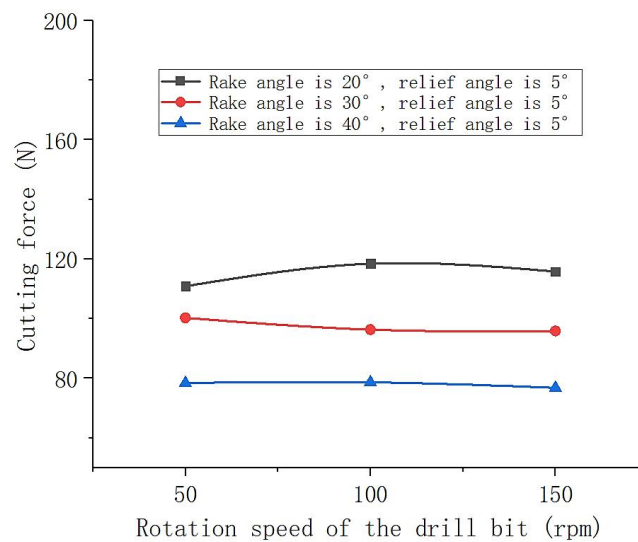
not show a clear and consistent change pattern. Therefore, it can be inferred that the relief angle of the

327

cutter has no clear effect on the cutting force.

328

Plots of the average cutting force versus the rotation speed of the drill bit are shown in Fig. 12.

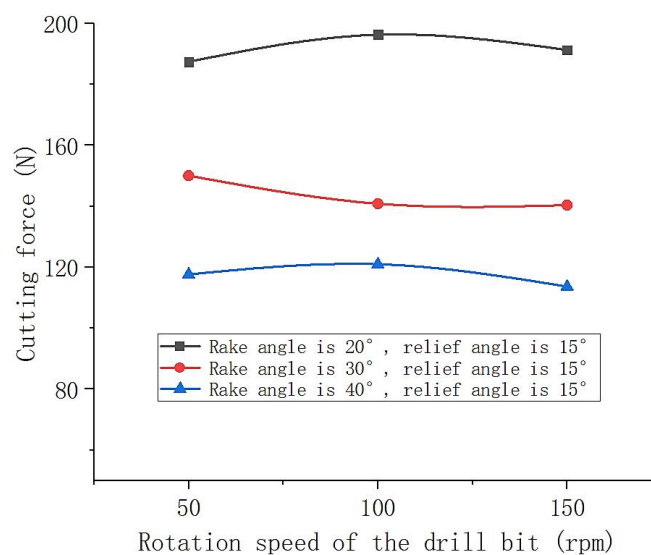


329

Rotation speed of the drill bit (rpm)

330

(a) The cutting depth is 1mm

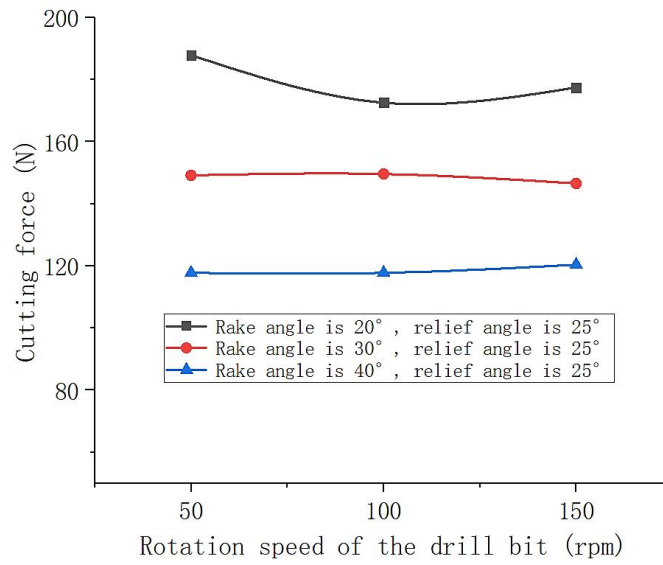


331

Rotation speed of the drill bit (rpm)

332

(b) The cutting depth is 2mm



(c) The cutting depth is 2mm

333

334

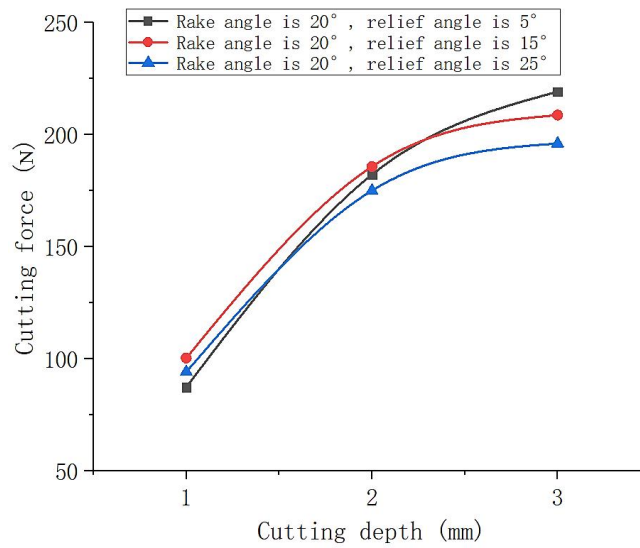
335 **Figure 12.** Cutting force versus rotation speed of the drill bit

336 Under various experimental conditions, there is only a slight change in cutting force during the process of the

337 rotation speed changing, and there is no clear pattern of change. The rotation speed of the drill bit does not affect

338 the cutting force.

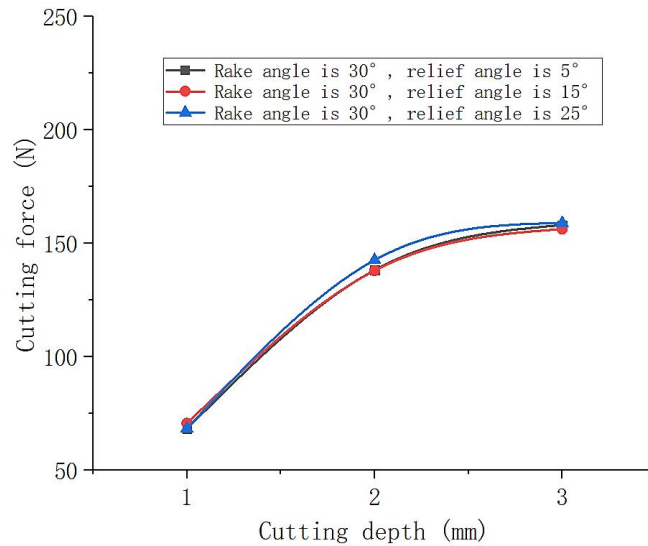
339 Plots of the average cutting force versus cutting depth are shown in Fig. 13.



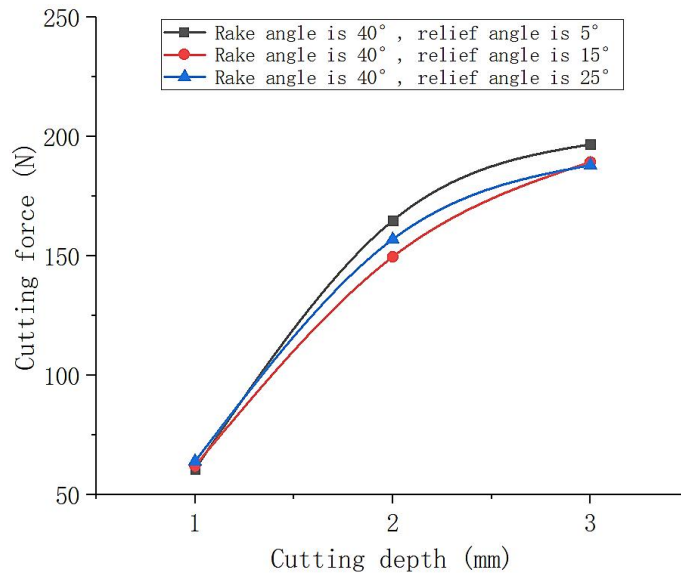
(a) The rotation speed of the drill bit is 50 rpm

340

341



(b) The rotation speed of the drill bit is 100 rpm



(c) The rotation speed of the drill bit is 100 rpm

**Figure 13.** Cutting force versus cutting depth

Under all experimental conditions, as the cutting depth increases, the cutting force shows a gradually increasing trend. When the cutting depth is 3mm, the maximum cutting force reaches 219.13725N. And, under the same experimental condition, the cutting depth increasing from 1 mm to 2 mm results in an approximate doubling of the cutting force. As the depth of penetration increases, the cutting force continues to increase, but the increasing trend gradually weakens.

## 6. Conclusions

354 It is preliminarily observed after the mechanical testing of ice, that the main damage form of ice is a  
355 brittle fracture in the cutting process. During this process, the cutters press into the ice to a certain  
356 depth and rotate, the ice withstands a squeezing effect from the rake face of the cutter and the shear slip  
357 deformation occurs. When the shear slip deformation reaches a certain degree, the ice undergoes shear  
358 failure and then forms ice chips. This process is constantly repeated throughout the cutting and drilling  
359 of the ice.

360 Based on the characteristics of ice cutting and the stress characteristics during the ice cutting and  
361 drilling process, a mechanical model of ice cutting was established. The mechanical model shows that  
362 the cutting force is not only affected by the mechanical properties of ice but also by the cutting width,  
363 cutting depth, and the rake angle of the cutter. As the cutting width and cutting depth increase, the  
364 cutting force increases; as the increase of rake angle of the cutter, the cutting force decreases.  
365 Additionally, the characteristics of cutting force were analyzed through experimental methods. The  
366 experimental results show that the cutting force traces oscillated within a certain range, the oscillation  
367 consists primarily of two frequencies. The higher frequency is related to the resolution of the sensor,  
368 the lower frequency is related to the formation of large particle ice chips. the oscillation amplitude of  
369 the cutting force traces is related to the cutting depth, as the cutting depth increases, the oscillation  
370 amplitude of the trajectory will also increase. In addition, the oscillation amplitude will also affect the  
371 quality of the core, as the amplitude increases, the possibility of the ice core breaking will also increase,  
372 and the quality of the ice core will also increase accordingly. It is necessary to control the cutting depth  
373 reasonably during the cutting process to ensure the quality of the ice core. Finally, the influencing  
374 factors and laws of cutting force were verified by analyzing the cutting force generated under various  
375 experimental conditions.

376

377 *Date availability.* No data sets were used in this article

378

379 *Author contribution.* Xinyu Lv: Conceptualization, Methodology, Writing – original draft; Zhihao Cui:  
380 Methodology, Validation, Formal analysis, Visualization; Ting Wang: Methodology, Validation,  
381 Formal analysis, Visualization; Yumin Wen: Conceptualization, Writing – review & editing,

382 Methodology, Validation; An Liu: Methodology, Validation, Formal analysis, Visualization; Rusheng  
383 Wang: Methodology, Formal analysis, Supervision, Project administration, Funding acquisition.

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