Responses of Pine Island and Thwaites Glaciers to Melt and Sliding Parameterizations

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Abstract. Pine Island and Thwaites glaciers are the two largest contributors to sea level rise from Antarctica. Here we examine the influence of basal friction and ice-shelf basal melt in determining projected losses. We examine both Weertman and Coulomb friction laws with explicit weakening as the ice thins to flotation, which many friction laws include implicitly via the

- 10 effective pressure. We find relatively small differences with the choice of friction law (Weertman or Coulomb) but find losses are highly sensitive to the rate at which the basal traction is reduced as the area upstream of the grounding line thins. Consistent with earlier work on Pine Island Glacier, we find sea-level contributions from both glaciers vary linearly with the melt volume averaged over time and space, with little influence from the spatial or temporal distribution of melt. Based on recent estimates of melt from other studies, our simulations suggest that the combined, melt-driven sea-level-rise contribution from both
- 15 glaciers may not exceed 10 cm by 2200, though the uncertainty in model parameters allows for larger increases. We do not include other factors, such as ice shelf breakup that might increase loss, nor factors such as increased accumulation and isostatic uplift that may mitigate loss.

1 Introduction

Most of Antarctica's contribution to sea level originates from West Antarctica (Otosaka et al., 2023), where ice loss occurs predominately from Pine Island and Thwaites glaciers (Rignot et al., 2019). These losses are a response to increased ocean melting of the glaciers' buttressing ice shelves (Payne et al., 2004; Shepherd et al., 2004; Rignot and Jacobs, 2002). This enhanced melt is caused by increased transport of warm circumpolar deep water (CDW) to the glaciers' deep grounding lines (Thoma et al., 2008; Dutrieux et al., 2014; Jenkins et al., 2016), potentially in response to atmospheric forcing originating in equatorial regions (Dutrieux et al., 2014; Holland et al., 2019; Naughten et al., 2022).

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Many numerical modelling studies reveal that these glaciers will lose mass over the coming decades to centuries in response to continued ocean forcing (Joughin et al., 2010, 2014; Seroussi et al., 2017, 2020; Favier et al., 2014) in the form of ice-shelf basal melt (hereon referred to as simply "melt"). For Pine Island Glacier (PIG) at least, the amount of future ice loss appears

to be a linear function of the spatio-temporally averaged sub-shelf melt rate (Joughin et al., 2021b), which is consistent with

- 30 the results from a large suite of models forced with the Coupled Model Intercomparison 6 (CMIP6) output for the Ice Sheet Model Intercomparison for CMIP6 (ISMIP6) exercise (Seroussi et al., 2020). If further work continues to find that ice loss from well-buttressed glaciers is almost completely determined by average melt rates, it will support a linear-response approach to projecting sea-level rise (Levermann et al., 2019).
- An important control on modelled ice stream dynamics is the basal friction law, which relates basal shear stress to the speed at which the ice slides over its bed. Early work suggested linear viscous behaviour for soft (weak till) beds (Blankenship et al., 1987) and Weertman sliding (power law with an exponent of ~3) over a hard bed (Weertman, 1957). Later work showed that weak till beds are far better approximated as Coulomb-plastic behaviour (Kamb, 1991; Zoet and Iverson, 2020). Moreover, when cavitation effects are incorporated in sliding models, Coulomb-like conditions should occur for fast basal sliding over
- 40 hard beds (Gagliardini et al., 2007; Schoof, 2005). Thus, both hard and soft beds may be well represented by a Coulomb model, at least at fast sliding speeds (Minchew and Joughin, 2020). Historically, models used to project ice-sheet loss over the next few centuries use basal-friction parameterizations ranging from linear-viscous to Coulomb plastic, or some hybrid combination (Asay-Davis et al., 2016). While the sliding coefficient for such parameterizations typically can be solved for with inverse methods (MacAyeal, 1993), other factors such as the exponent and the treatment of effective pressure are less well constrained.

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Here we examine the sensitivity of the responses of Pine Island and Thwaites glaciers to a) various parameterizations of the friction law, and b) the mean aggregate basal melt for their respective ice shelves. In particular, we focus on a regularized Coulomb friction (RCF) law that prior work indicates best replicates recent observations of Pine Island Glacier (PIG) (Joughin et al., 2019).

50 2. Basal Friction Overview

A major focus of this paper is to try and systematically separate how ice loss is affected by the speed-dependence in the friction law from how it is affected by weakening of the bed as the area near the grounding line approaches flotation. As a result, here we include a review of various commonly used sliding laws and examine their respective sensitivities to changes in flow speed and thinning induced changes in effective pressure.

One of the more widely used forms of the friction law to relate basal shear stress, τ_b , to the sliding speed, u_b , is the power-law relation

$$\boldsymbol{\tau}_{\boldsymbol{b}} = \beta_m^2 |\boldsymbol{u}_{\boldsymbol{b}}|^{\frac{1}{m}} \frac{\boldsymbol{u}_{\boldsymbol{b}}}{|\boldsymbol{u}_{\boldsymbol{b}}|'} \tag{1}$$

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which is often used with a value of m=3 to produce Weertman sliding (Weertman, 1957). As *m* becomes very large this relation tends toward Coulomb basal friction, which can be expressed as

$$\mathbf{\tau}_{\boldsymbol{b}} = \beta^2 \frac{u_b}{|u_b|}.\tag{2}$$

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Following the convention of MacAyeal (1993), the friction coefficient in these equations is expressed as β^2 to ensure a positive value is determined when using inverse methods.

Work by Schoof (2005) and Gagliardini et al. (2007) indicates that while Weertman conditions can occur at slow speeds, at
high speeds water-filled cavities form in the lee of basal bumps, causing more Coulomb-like or even velocity-weakening
behaviour. Based on this work, large-scale ice-sheet-modelling studies often use a basal friction law with the form (Asay-Davis et al., 2016)

$$\boldsymbol{\tau}_{\boldsymbol{b}} = \frac{\beta^2 |\boldsymbol{u}_{\boldsymbol{b}}|^{\frac{1}{m}\alpha^2 N}}{(\beta^{2m} |\boldsymbol{u}_{\boldsymbol{b}}| + (\alpha^2 N)^m)^{\frac{1}{m}} |\boldsymbol{u}_{\boldsymbol{b}}|},\tag{3}$$

where α^2 is the Coulomb friction coefficient (typically 0.5; e.g., Asay-Davis et al., 2016), and *N* is the effective pressure, 75 which is the difference between the overburden and basal-water pressures. Tsai *et al.* (2017) developed an alternative expression to combine Weertman and Coulomb behaviour as

$$\boldsymbol{\tau}_{\boldsymbol{b}} = \min(\alpha^2 N, \beta^2 |\boldsymbol{u}_{\boldsymbol{b}}|^{\frac{1}{m}}) \frac{\boldsymbol{u}_{\boldsymbol{b}}}{|\boldsymbol{u}_{\boldsymbol{b}}|}. \tag{4}$$

80 Equations (3) and (4) both depend on the effective pressure, N. An often-used convention is to assume a perfect hydrological connection to the grounding line so that the basal water pressure equals the ocean pressure (e.g., Asay-Davis et al., 2016). In this case, the effective pressure is given by

$$N = \rho_i g(h - h_f), \tag{5}$$

where ρ_i is the density of ice, *g* is the acceleration due to gravity, *h* is the ice elevation, and h_f is the flotation height (the elevation at which ice begins to float).

Figure 1 illustrates the sensitivity of these friction laws to speed for parameters meant to represent the strong area upstream of the grounding line, central trunk, and outlying tributaries of PIG (see basal shear stress map in Figure 2a). In these examples,

90 Weertman conditions occur for all cases except for the case where Equation (3) is plotted using a height above flotation $(h - h_f)$ of 45 m (transition to Coulomb) and 40 m (nearly full Coulomb; Figure 1a).

The reason why these plots largely reflect Weertman sliding is that the transition from Coulomb to Weertman conditions in Equation (4) occurs at $h - h_f = \frac{\tau_b}{\alpha^2 \rho_{ig}}$, with Equation (3) producing a less abrupt transition at a similar value. Thus, if we assume ~300 kPa as the maximum expected value for τ_b with Coulomb friction, then the transition to Weertman sliding takes

place at locations where the elevation is less than ~67 m above flotation for $\alpha^2=0.5$. To illustrate the extent of the region where Coulomb conditions occur with these models, Figure 2 shows contours of $h - h_f$ plotted over values of τ_b inferred as described in the Methods Section. These contours indicate that Coulomb conditions only occur within about 10 km of the grounding line, which is consistent with the distances over which the assumption of perfect hydrological connectivity is likely

100 valid (Asay-Davis et al., 2016).

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Numerous boreholes indicate water pressures close to flotation, and thus, low (<400 kPa) effective pressure (Luthi et al., 2002; Kamb, 2001) well away from the grounding line. The widespread presence of active subglacial lakes also suggests that low effective pressures are prevalent (Gray et al., 2005; Smith et al., 2009; Fricker et al., 2007; Bell, 2008). Recent hydrological

105 models also support the presence of widespread areas of low effective pressure in the PIG and Thwaites Glacier basins (Dow, 2022; Hager et al., 2022). If this is the case, then Equations (3) and (4) indicate Coulomb conditions occur over a much broader area than that obtained by assuming basal water pressure equals ocean pressure.

Weertman sliding can also include an effective-pressure dependence. Initially based on laboratory measurements by Budd et
 al. (1979) and later modified by Fowler (1987), a modification of Weertman sliding that adds an explicit effective pressure dependence is given by

$$\boldsymbol{\tau}_{\boldsymbol{b}} = \beta_m^2 N^{\frac{q}{m}} |\boldsymbol{u}_{\boldsymbol{b}}|^{\frac{1}{m}} \frac{\boldsymbol{u}_{\boldsymbol{b}}}{|\boldsymbol{u}_{\boldsymbol{b}}|}.$$
 (6)

This equation is often applied with the effective pressure as given by Equation (5), even at large distances from the grounding line where the assumption is likely not valid (Yu et al., 2018). For the remainder of this manuscript, we refer to Equation (6) as Budd friction and Equation (3) as Weertman sliding (or friction).

We know of no basal hydrological models for N that have been demonstrated to have sufficient accuracy with which to determine basal shear stress, leading to the often-used assumption given in Equation (5). An alternate approach is to assume

120 that effective pressures are low enough in regions of fast flow to produce Coulomb conditions. In this case, the observed speeds are assumed to determine the extent and type of basal friction with the transition from Weertman to Coulomb behaviour occurring at some critical speed, u_o . By subsuming the effective pressure into the sliding coefficient (β^2), the form of the equation given by Schoof (2005) can be rewritten (Joughin et al., 2019) as

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$$\mathbf{\tau}_{\boldsymbol{b}} = \beta^2 \left(\frac{|\mathbf{u}|}{|\mathbf{u}|+\mathbf{u}_0}\right)^{\frac{1}{m}} \frac{\boldsymbol{u}_{\boldsymbol{b}}}{|\boldsymbol{u}_{\boldsymbol{b}}|}, \quad (7)$$

which we refer to as regularized Coulomb friction (RCF). In this case, the influence of *N* is determined implicitly in the solution for β^2 . Although this expression was derived for sliding-induced cavitation on hard beds (Schoof, 2005; Gagliardini et al., 2007), laboratory studies show this form also applies to soft, deforming beds (Zoet and Iverson, 2020), albeit with a potentially different exponent. Thus, it may be reasonable to model friction with a single friction law (Minchew and Joughin, 2020).

- 130 When modified as described below to allow near grounding-line weakening and included in a model forced with observed elevation change, this friction model with m=3 most accurately reproduced the observed speedup of PIG over nearly two decades (Joughin et al., 2019). As indicated in Figure 1, this equation produces Coulomb-like friction in regions of fast flow $(|u| > u_o)$ and Weertman-like conditions in areas of slower flow $((|u| < u_o; Figure 1c))$. Another study indicated that PIG conditions are reproduced better with a power law using values of *m* in the range of 10–20, which produces a sensitivity of τ_b
- 135 to speed that more closely resembles that of Equation (7) than that of Weertman sliding (Gillet-Chaulet et al., 2016).

In addition to determining the transition from Weertman to Coulomb conditions, the sensitivity to $h - h_f$ for the assumed form of N used in Equations (3) and (4) causes the bed to weaken as the ice approaches flotation. This is a desirable effect since it is unlikely that the basal traction goes from full strength to nothing precisely as the ice base goes from grounded to floating. To illustrate this point, Figure 2c shows the cumulative distribution functions (CDFs) for values of τ_b inferred as described

- 140 To illustrate this point, Figure 2c shows the cumulative distribution functions (CDFs) for values of τ_b inferred as described below for height-above-flotation-determined bands near the grounding line. The results show that in the band closest to the grounding line $(h - h_f < 41 \text{ m}) \log \tau_b$ values (median 66 kPa) are far more likely than ~5–15 km farther inland (41 < $h - h_f$ < 176 m) where higher values of τ_b (medians of 97 and 125 kPa) are more prevalent. This characteristic is consistent with observations of a break in slope near the grounding line, indicating reduced driving and basal-shear stresses (Fricker and
- 145 Padman, 2006). These observations suggest that as the grounding line (zone) recedes inland to presently high-friction areas some reduction in basal traction occurs.

Figure 3 shows the weakening as the surface elevation approaches flotation for Equations (3) and (4). The difference in these two formulations is that Equation (3) combines Weertman and Coulomb basal resistance in parallel (Gudmundsson et al., 2023), which provides a smoother transition between the two friction types than does the more abrupt transition when using

Equation (4).

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The Weertman and RCF models as parameterized above have no such weakening. To include this effect, Joughin et al. (2010) included a linear weakening of the bed that initiates once the height above flotation falls below some threshold, h_T , which can be expressed as

$$\lambda(\mathbf{h}) = \begin{cases} 1 & (h - h_f) > h_T \\ \frac{(h - h_f)}{\min(h_T, h_0 - h_f)} & (h - h_f) \le h_T, \end{cases}$$
(8)

where h_o is the elevation at the start of the simulation. When used to scale Equations (1) or (7) (e.g., $\tau_b(h) = \lambda(h)\tau_b$), this function produces linear weakening as the surface elevation evolves time similar to Equation (4) as shown in Figure 3. (Note strengthening can occur in the rare instances where thickening occurs.) There is a critical difference, however, in that h_T in Equation (8) is fixed for all values of τ_b , whereas the elevation-dependent weakening in Equations (3) and (4) occurs with a spatially varying threshold determined by τ_b . The former assumes some critical threshold for effective pressure, which applies to a range of bed conditions. That latter assumes an effective pressure limit that depends on how much shear stress the bed can support. Each represents imperfect assumptions, and it's not clear which model is preferable in the absence of a better solution.

Earlier work suggested that a value of h_T =41–46 m best reproduces PIG's response over the last two decades (Joughin et al., 2019, 2021a) for the RCF model (Weertman sliding with m=3 produced best results with h_T = 122–123 m). Figure 2, however, suggests the weakening may occur over a broader zone (see Figure 2c). As a result, a major goal of the work presented here is to investigate the sensitivity of losses projected over centuries to this parameter. Here we perform experiments using Equation

(8) because it allows us to vary the amount of weakening so that we can study the resulting impact on ice loss. It also lets us separate the weakening behaviour from the friction model. Thus, many of the experiments described below are aimed at understanding the sensitivity of ice loss to the choice of h_T .

3 Methods

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175 Our numerical experiments are all conducted using a finite element modelling package called *icepack* (Shapero et al., 2021). The remainder of this section describes the setup and initialization used to conduct the experiments described below.

3.1 Model

Our results are based on simulations using a basin-scale model of a coupled ice-sheet/shelf system that was developed for earlier studies of PIG (Joughin et al., 2021a, b). The ice-sheet modelling package, *icepack* (Shapero et al., 2021), used to construct this model is built around the finite-element analysis library, Firedrake (Rathgeber et al., 2016), which includes an embedded symbolic language for specifying the differential equations to be solved. Both *icepack* and Firedrake are fully open

The model solves the shallow-shelf equations (MacAyeal, 1989) on an unstructured finite-element mesh with triangular elements. The domain extent is fixed and the ice-shelf front does not move, but the grounding line evolves freely. The mesh

source and are available through GitHub as is the basin-scale model used for the work described here.

spacing is variable, with resolutions of a few hundred meters near the grounding lines and several kilometres in the deep interior (Figure S1). The model does not account for glacial isostatic adjustment since this effect should be small at the 200-year time scales examined here (Larour et al., 2019). A typical 200-year simulation for the combined basins of Pine Island and Thwaites glaciers takes a few days on a single CPU core with first-order elements and a time step of 0.01 years. Since

190 everything is single-threaded, we can run ensembles in parallel on a multi-core machine over the same period.

Rather than using Equation (7) to implement RCF, within *icepack*, it is numerically easier to solve for a different expression given by (Shapero et al., 2021)

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$$\mathbf{\tau}_{b} = \frac{\beta^{2} |u_{b}|^{\frac{1}{m}}}{\left(u_{o}^{\frac{1}{m}+1} + |u_{b}|^{\frac{1}{m}+1}\right)^{\frac{1}{m+1}} |u_{b}|}.$$
(9)

We refer to the icepack version of regularized Coulomb friction as RCFi. Although Equations (7) and (9) appear substantially different in form, by adjusting the values of u_o , they can produce nearly equivalent responses, as demonstrated in Figure 1 (compare RCF and RCFi with values of u_o equal to 200 and 300 m yr⁻¹ in Figure 1, respectively). For both the RCFi and Weertman (Equation 1 with m = 3), we scale the basal shear stress by $\lambda(h)$, using a range of h_T .

We initialize the model by inverting for the basal friction law parameters (β^2 for Weertman or RCFi as appropriate) using standard methods implemented in *icepack*, with the amount of regularization determined through L-curve analysis (Hansen and OLeary, 1993). The inversion procedure also solves for the Glen's flow law parameter, *A*, on the floating ice (Joughin et

al., 2021b). For the grounded ice the model determines *A* based on its temperature dependence (Cuffey and Paterson, 2010) using an earlier simulation for internal temperature (Joughin et al., 2009). Both *A* and β^2 remain constant with time throughout each simulation.

For most of the experiments, we use a randomly generated ensemble of 30 melt distributions applied to the floating nodes (Joughin et al., 2021b), which are used to force 30 independent simulations. Unless otherwise noted, we present the results as the ensemble averages of these simulations. The melt distributions are selected such that approximately half produce peak melt at the grounding line while the other half produce peak melt higher in the water column (see example profiles in Joughin et al., 2021b). At each time step (0.01 years), each melt distribution is re-normalized to produce a specified level of melt (e.g., 57 Gt/yr). By contrast, many studies use a melt function parameterized by depth (e.g., Joughin et al., 2014; Gudmundsson et

al., 2023; Jourdain et al., 2020; Yu et al., 2018; Barnes and Gudmundsson, 2022). In addition to our melt ensembles, we also conducted simulations with depth-parameterized melt rates used in other recent studies (Gudmundsson et al., 2023; Yu et al., 2018; Barnes and Gudmundsson, 2022).

3.2 Initialization Data Sets

Our study area is the combined basins of PIG and Thwaites Glacier. Note that we treat Haynes Glacier as a branch of Thwaites

- 220 Glacier so that all references hereafter to Thwaites apply to both glaciers. For the surface and bed elevations and thickness, we used the BedMachine Version 3 data set (Morlighem et al., 2020). We modified the bed elevations slightly to make them consistent with other data. First, we reduced bed elevations along some areas of the ice front to ensure they were floating, consistent with the assumed boundary condition. Second, we raised elevations for a few pockets in the interior to ensure that they were grounded. Finally, we reduced elevations downstream of the grounding line position of PIG that we inferred from
- 225 2014 TerraSAR-X speckled-tracked offsets (Joughin et al., 2016), which agrees well with the MEaSUREs Version 2 grounding line (Rignot et al., 2014).

To invert for the friction coefficient, we used a velocity map assembled from three sources. First, we produced a map by processing all the Sentinel 1A/B data for the region collected from January 2019 to December 2020, which covered most of the model domain north of 78.7°S. Next, we filled gaps using data from the MEaSUREs Phase-Based Velocity (Version 1) map (Mouginot et al., 2019). Finally, for some of the slower, southernmost regions where there were gaps or excessive noise in the MEaSUREs data, we used balance velocity data computed with a well-established algorithm (LeBrocq et al., 2006) constrained by RACMO 2.3 (Wessem et al., 2014) surface mass balance (SMB) data averaged from 1979-2022. Because most of the fast-moving areas are covered by the Sentinel-1 data, the final map is representative of the mean flow for 2019-2020.

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For the surface mass balance (SMB), consistent with earlier studies (Joughin et al., 2021b, 2014), we used a map of SMB derived from airborne radar and ice cores (Medley et al., 2014), which does not vary with time. Using this SMB and initializing the model with the observed velocities, the combined system initially loses ice at a rate of 0.33 mm yr⁻¹ sea level equivalent (sle), with PIG and Thwaite Glacier losing 0.17 and 0.16 mm yr⁻¹ sle, respectively. Note all values presented here are computed on a polar stereographic grid, which introduces area distortion. As a result, our estimated losses are biased low by ~2.5%.

4.0 Results

Earlier work simulated the response of PIG to melt rate using h_T =41 m (Joughin et al., 2021b), which is our preferred value since it provides the best match to PIG's recent behaviour using RCFi (Joughin et al., 2019). The PIG record is short (<2 decades), however, relative to the periods over which sea-level projections are required (centuries). To examine the sensitivity

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of simulated losses to the choice of h_T and melt rate, we conducted further simulations with an expanded domain that also includes Thwaites Glacier.

Figure 4 shows the volume above flotation (VAF) losses for 200-year simulations with RCFi and our preferred value of h_T (41 m) and for melt rates of 57, 75, 100, and 125 Gt yr⁻¹ applied to each ice shelf (i.e., total melt for the domain is twice these

- 250 values). For PIG the results agree well with those from earlier work (Joughin et al., 2021b), with small differences due to differences in the initial conditions and interactions with the adjacent Thwaites basin. Thwaites Glacier and PIG produce similar losses throughout these simulations when forced with the same melt levels. Also shown are the combined VAF losses that would occur if the current rates are linearly extrapolated. The combined 200-year VAF losses are 73% and 85% of extrapolated current rates for melt rates of 57 and 75 Gt yr⁻¹, respectively. With the higher melt rates, losses exceed the present
- 255 rates by 7–28%. As with the rest of the simulations described here, the results represent an average of 30 randomly selected melt profiles, each normalized to produce the prescribed amount of melt as described above.

Figure 5 shows combined losses for both glaciers for the four values of h_T that correspond to the height-above-flotation contours shown in Figure 2. The simulations were conducted using both RCFi and Weertman sliding. For both types of friction,

- the VAF loss is strongly sensitive to the choice of h_T . For the least melt (57 Gt yr⁻¹), the largest value (h_T =172 m) produces 260 ~40% more loss than the smallest value (h_T =1 m). At the highest melt rate (125 Gt yr⁻¹), the corresponding difference is more than a factor of 2. The behaviour is similar for the Weertman cases, except that the sensitivity to h_T is substantially lower at the lower end of the melt range. At the two lowest melt rates, nearly all the simulations produce less loss than extrapolation of the current rate. By contrast, the simulated losses exceed the extrapolated current rate with the two highest melt rates for all 265
- but some of the cases with $h_T=1$ m.

Figure 6 shows the annual loss rates for each glacier from the RCFi simulations. These results are averages of 30 simulations with differing melt distributions, so they tend to smooth out the variability of individual ensemble members as the grounding line retreats off basal highs (Joughin et al., 2021b). After a brief initial transient as the system equilibrates to the imposed melt,

270 the VAF losses occur at relatively steady rates throughout most of the simulations. For Thwaites Glacier with the larger h_T values, however, the annual rates of loss tend to increase substantially ($\sim 2-3x$) throughout the simulation. At the most extreme $(h_r=172 \text{ m and } 125 \text{ Gt yr}^{-1} \text{ melt})$, the end-of-simulation loss rate for Thwaites Glacier is more than 5 times the present rate and more than twice the rate for PIG. As a result, much of the sensitivity to h_T for the combined losses shown in Figure 5 is attributable to Thwaites Glacier.

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To examine the sensitivity to melt, Figure 7 shows the 200-year losses as a function of the melt rate for the combined and individual glacier basins. To illustrate the sensitivity to the different spatial distributions of melt, this figure also shows the individual melt-distribution ensemble members for the RCFi simulations. Linear fits to raw ensemble data (120 points for each fit) for both friction models are also shown. For the combined basin, the regressions show that the melt rate accounts for most of the variance (88–94%), with the remaining variance due to the spatial distribution. The corresponding ranges are 81–97%

and 62–92% for PIG and Thwaites Glacier, respectively. The sensitivity to melt increases with h_T as indicated by the slopes for the combined RCFi responses, which vary from -0.21 to -0.61 mm Gt⁻¹ yr sle over the range h_T values. The corresponding range of sensitivity is -0.24 to -0.51 mm Gt⁻¹ yr sle for PIG and -0.18 to -0.71 mm Gt⁻¹ yr sle for Thwaites Glacier. The results are similar for the Weertman cases, except that the sensitivity to h_T is somewhat greater for PIG (-0.21 to -0.7 mm Gt⁻¹ yr sle).

285 This increase in slope is largely due to the substantially lower losses for Weertman sliding at the lower end of the melt range.

To demonstrate their spatial distribution, Figure 8 shows the VAF loss averaged over all 30 ensemble members at each level of melt for both the RCFi and Weertman simulations with h_T =41 m. All the simulations have some thickening in the upper basin, which is likely due to the poorer quality of the velocity used to initialize the model there (i.e., speeds that are too slow).

290 At the lower elevations, there is strong thinning of up to a few hundred m that increases with melt level. At the higher melt values, the results from RCFi and Weertman are similar. At the lower melt levels, Weertman cases show some slight thickening near the PIG grounding line and less overall thinning, consistent with the results shown in Figure 7. These results show PIG grounding line advance for the low melt Weertman cases where thickening also occurred.

5.0 Discussion

Our simulations of Pine Island and Thwaites glaciers reveal several important aspects of how projected contributions to sea level are influenced by the friction model, loss of traction upstream of the grounding line as ice thins (h_T) , and the melt rate.

5.1 Sensitivity to Friction Law

Overall, our results indicate the choice of friction law yields relatively minor differences to the projected VAF losses (Figure 7), except for the PIG cases with low melt. These differences are consistent with the PIG re-grounding seen in the low melt simulations with Weertman sliding (Figure 9e&f). As noted above, there are limited areas $(h_o < h_T)$ where the bed can strengthen if thickening rather than thinning occurs. Such thickening rarely occurs because the region near the grounding line tends to nearly always thin. For some Weertman cases, however, thickening and advance do occur for sufficiently low melt, which should be reinforced by thickening-induced strengthening of the bed near the grounding line. This would explain why the losses decline as h_T increases for the low melt Weertman cases on PIG, since the area subject to this type of strengthening 305 expands. Whether this should remain a feature of our model is a subject for future research.

(Joughin et al., 2019)On Thwaites Glacier, all the simulations result in retreat and the RCFi and Weertman simulations produce roughly similar results in terms of grounding-line retreat (Figure 9) and VAF loss (Figures 7–8). Overall, the grounding line retreat is more variable for Thwaites Glacier (blue-green areas in Figure 9). This variability likely occurs because

310 approximately half the ensemble members tend to produce shallower melt distributions that shift a larger portion of the melt to the eastern shelf, which should enhance retreat along the eastern portion of the grounding line. Thus, while the choice of the form of the frictional law makes a relatively small difference (< 20%) in general, the friction models cannot be treated interchangeably since in some circumstances the differences can be large (>50%) and unpredictable, as in the low-melt PIG simulations. Since RCFi is better able to reproduce recent behaviour on PIG and because Weertman friction can cause 315 grounding-line advance (Figure 9) that is inconsistent with current observations, RCFi seems preferred for studies where only one type of friction is used.

Several studies have compared Weertman sliding with the friction laws expressed in Equations (3) and (4) (Gudmundsson et al., 2023; Barnes and Gudmundsson, 2022; Nias et al., 2016). Comparisons of our work with those studies are hindered by the fact that while the friction laws represented by these equations are often referred to as regularized Coulomb friction, they produce Coulomb friction for only a small fraction of the bed (<1% of the domain) near the grounding line $(h - h_f < ~86 \text{ m} \text{ in Figure 2})$ so that the vast majority of the basin is subject to Weertman sliding. By contrast, RCFi applies Coulomb conditions to the full extent of the fast-moving regions (~11% of the domain). A further complicating factor is the extent to which Equations (3) and (4) differ from Weertman due to Coulomb behaviour (i.e., the dependence of τ_b on speed) versus their dependence on effective pressure (i.e., reduction in traction as flotation is approached). Moreover, such an effective-pressure

dependent reduction is not limited to Coulomb friction and such a dependence can be included in a Weertman model as is the case for Equation (6).

An advantage of our approach is that we can evaluate how the friction law and the weakening above the grounding line 330 individually affect ice loss. As the latter appears to play a larger role, we defer further comparison to the discussion below where we examine the sensitivity of our results to h_T .

5.2 Sensitivity to Weakening as Ice Approaches Flotation

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Figure 2c indicates that the area near the grounding line $(h - h_f < 41 \text{ m})$ is substantially weaker than the area immediately above it $(h - h_f > 41 \text{ m})$, which suggests the need for a mechanism to reduce basal traction as the ice column evolves toward flotation. This reduction can be accomplished either explicitly through Equation (8) or implicitly through the dependence on effective pressure in Equations (3) and (4). All of our simulations use the explicit approach.

The results shown in Figures 5–7 indicate a strong sensitivity to the rate at which traction above the grounding line is reduced in our simulations as parameterized via h_T . Larger values of h_T tend to produce more loss at the same melt level due to the

- additional loss of basal traction as the ice thins. An exception occurs for PIG with RCFi where, at low melt values, the losses are nearly the same across the full range of h_T . An earlier analysis of PIG indicated that while loss of traction acts to speed the glacier up, much of this effect is counterbalanced by the evolution of the surface, which reduces the driving stress near the grounding line (Joughin et al., 2019). In most cases the loss of basal traction appears to prevail, leading to an overall speedup. At low melt rates on PIG, however, these two competing effects appear to roughly balance each other over the full range of
- 345 h_T . Thwaites Glacier losses are far more sensitive to h_T , with the min and max values producing differences of ~60% at the low end of the melt range up to a factor of 2.8 at the upper end of the range. This enhanced sensitivity is likely due to its weak

shelf, which is less able to produce additional buttressing as it speeds up to help compensate for the greater loss of basal traction due to high melt with a large value of h_T .

As Figure 3 indicates, the loss of traction near the grounding line as the ice approaches flotation is similar in form for Equations (3), (4), and (8). The key difference is that for our simulations, the linear reduction in traction is determined by a spatially invariant threshold (h_T). The way Equations (3) and (4) are formulated means that they effectively have similar thresholds, except that they vary spatially based on the basal shear stress at each point. These differences tend to make direct comparisons difficult. One way to obtain a rough equivalency is to determine the value of h_T that yields equivalent area-integrated traction subject to reduction via the effective pressure dependency in Equation (4) for a given value of α^2 .

Barnes and Gudmundsson (2022) conducted simulations using α^2 values of 0.25, 0.5, and 0.75 in Equation (3), which roughly translates to h_T values of 57, 27, and 17 m, respectively, using the method just described. These values bracket our preferred value of 41 m, which indicates this choice of h_T is consistent with the range of values they used as well as values used for other studies. They conducted several 120-year simulations for a domain that also included Smith, Pope, and Kohler glaciers. When they used the friction model described by Equation (3), the results were 20 and 38% greater relative to Weertman sliding $(\alpha^2 \rightarrow \infty)$ for α^2 values of 0.5 ($h_T \sim 27$ m) and 0.25 ($h_T \sim 57$ m), respectively. Over the same period using Weertman sliding scaled by $\lambda(h_T)$ with h_T =41 m, we obtained results that were 23% greater than with h_T =1 m (Weertman with effectively no weakening). Given the differences in the models and domains, our results are in good agreement with theirs, suggesting that

365 most of the additional losses in the Barnes and Gudmundsson (2022) results are due to the reduction in basal traction as the effective pressure declines rather than the transition to Coulomb conditions in the region near the grounding line.

The fact that our empirically-derived value of h_T agrees well with roughly equivalent values determined from consideration of effective pressure suggests that both types of models tend to reduce basal traction at rates that are approximately the right magnitude. While we cannot completely discount the results from the larger values of h_T used in our simulations, they likely

produce losses that are larger than can be expected.

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Consistent with the other work cited above, the results presented here suggest that models should include some type of reduction in basal traction as flotation is approached, irrespective of the actual friction type (e.g., Weertman or Coulomb). Less

375 clear is how such weakening should be applied. While empirical in nature, Equation (8) has demonstrated a reasonable ability to reproduce observed behaviour (Joughin et al., 2019). There is no reason, however, that α^2 in Equations (3) and (4) cannot be selected through a procedure like that used to derive our preferred value of h_T . On the other hand, Equation (8) can easily be modified to have a spatial variable h_T that depends on effective pressure in a similar manner to Equations (3) and (4), which

would allow the traction reduction to be decoupled from the form of the basal friction law. The best combination of these 380 concepts is a subject for future research.

Our best estimate for h_T is based solely on the response of PIG over a decade and half. While it is likely that other glaciers can be modelled well with a value of h_T of similar magnitude, further work is needed to establish the best value for other regions. Our results, however, do establish that the choice of h_T can have a substantial effect on projected losses as is the case for α^2

385 (Barnes and Gudmundsson, 2022).

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As the ice evolves in areas away from the grounding line, the driving stress increases in some areas and decreases in others. It is unclear the extent to which the friction law parameters are static, as is often assumed, or whether they should instead coevolve with the driving stress or other changes in the ice-sheet geometry that influence effective pressure. Lacking a good model to vary the friction as the surface evolves, except near the grounding line, many models, including ours, only allow basal traction in the interior to respond to variations in speed (e.g., Seroussi et al., 2020). Budd friction with effective pressure determined by Equation (6) is an exception in that the basal traction is reduced over the entire model domain in direct response to thinning. When using this type of friction, projected losses can more than double (Yu et al., 2018; Barnes and Gudmundsson, 2022). With q=3 and m=3 in Equation (6), the result is equivalent to Weertman friction with unbounded h_T (i.e., basal traction

- declines linearly with reductions in $h h_f$). The assumption, however, that a hydrologic connection to the ocean exists over the full domain such that the water pressure is equal to ocean pressure is not well supported by borehole observations of water pressure (Luthi et al., 2002; Kamb, 2001) and the widespread presence of subglacial lakes (Gray et al., 2005; Smith et al., 2009; Fricker et al., 2007; Bell, 2008) and models (Dow, 2022; Hager et al., 2022). We suggest that any law that relies solely on the local height above flotation to govern changes in effective pressure (e.g., Equation 6), and thus, basal friction over the
- 400 entire domain is likely oversimplified and incorrect. Other factors, such as the surface slope, should influence the basal hydrological system that determines effective pressure. As a result, care should be taken in interpreting results that employ Budd friction (Equation 7) in the absence of a more accurate way of determining the effective pressure.

5.3 Sensitivity to Melt

- 405 Our results indicate that the combined and individual losses for PIG and Thwaites Glacier increase linearly with melt (Figure 7), consistent with similar work for just PIG (Joughin et al., 2021b). For PIG, the linear fits to the 120 ensemble members for each friction model (30 melt distributions for each of 4 melt levels) indicate that the spatiotemporal averaged melt has a far greater effect on ice loss (r^2 =0.86–0.97) than does either the spatial or temporal variation of the melt, consistent with an earlier study that simulated just the PIG basin (Joughin et al., 2021b). The PIG ice shelf provides substantial back stress
- 410 (Gudmundsson et al., 2023). As a result, increasing the discharge to the shelf provides more backstress (faster flow and thicker ice), which acts as a negative feedback on the speed. Greater melting weakens this response, allowing greater discharge. For

Thwaites Glacier, the sensitivity to melt is weaker for lower values of h_T with less of the variance being explained by the trend ($r^2=0.6-0.69$). Thwaites Glacier is not nearly as well buttressed by its ice shelf as PIG (Gudmundsson et al., 2023), so the flow is less sensitive to melt-induced thinning of the shelf at low values of h_T , consistent with an earlier sensitivity study (Nias

- 415 et al., 2016). Moreover, Thwaites Glacier feeds a broad weak shelf with a shallow draft and narrow, deep pockets that provide some buttressing (Gudmundsson et al., 2023). As mentioned above some of the shallower melt distributions will concentrate more of the melt on the eastern shelf to yield more variable results.
- We used a fixed melt level throughout each simulation. In other work on PIG, however, similar simulations with periodic melt
 forcing (periods of decades to centuries), linear melt trends, and steady melt all produced virtually the same losses in cases where the long-term average melt was the same (Joughin et al., 2021b). This finding might appear to contradict other work suggesting melt rate variability about a constant long-term average rate can affect overall VAF loss (Robel et al., 2019; Hoffman et al., 2019). These studies, however, examine fluctuations in melt rate rather the volume, which is a function of both the melt rate and the shelf geometry. For example, a constant melt rate will lead to an increasing melt volume as the shelf area
 expands with ungrounding. Thus, we speculate that if these earlier results were recast as functions of melt volume, then they would exhibit a similar linearity with melt volume as do our results. While we are not well positioned to repeat these prior experiments, we can examine whether such linearity holds for melt volume that freely evolves when driven by fixed depth-dependent melt-rate parameterizations. To do so, we conducted additional experiments using the depth-parameterized functions used in other studies (Barnes and Gudmundsson, 2022; Gudmundsson et al., 2023; Yu et al., 2018), which allow the
- originating in a warm bottom layer (<500–1000 m) with high melt rates (40-160m yr⁻¹) that rises through a linear melt gradient approximating the thermocline at middle-depths, above which the plume loses all ability to melt ice.

Figure 10 shows the results using these 10 depth-parameterized melt rates, which produce average melt per glacier ranging

- 435 from 36 to 389 Gt yr⁻¹, with melt on Thwaites Glacier of up to 549 Gt yr⁻¹. Linear regressions to the results from these simulations produce r^2 values of 0.96 or greater, except for one case on Thwaites Glacier ($r^2=0.9$ for $h_T=1$). The independently determined regressions from our constant-melt ensembles all fit nearly as well ($r_{const.melt}^2 = 0.77-0.98$). These results indicate that the linear increases with steady melt evident in Figure 7 also apply when the melt freely evolves with the shelf geometry. We note that the regressions to the depth-parameterized melt rates typically yield higher r^2 values (Figure 10)
- 440 than do the regressions to the constant-melt ensemble data (Figure 7), which may be a statistical quirk. The better fits for the depth-parameterized functions, however, may reflect the fact that our melt ensembles employ a wider range of depth variation. For example, all the depth-parametrized melt functions produce maximum melt in the bottom part of the water column near the grounding line. By contrast, half of the ensemble distributions produce maximum melt higher in the water column as some models suggest should be the case (Favier et al., 2019)

Both our ensembles and the depth-parameterized melt simulations reveal that ice losses increase linearly with melt. Although we used a single model, the ISMIP6 suite of models yields similar results (Seroussi et al., 2020) with a linear regression of sea level rise on melt yielding r^2 =0.93 for the Amundsen Sea Embayment (Joughin et al., 2021b). Based on a similar assumption of linearity, Leverman *et al.* (2019) characterized sea-level uncertainty from Antarctica by generating large ensemble estimates

450 based on a more limited number of runs from ISMIP6. The linear response to melt shown in Figures 7 and 10 supports the use of their approach, which may help limit the computational burden for large ensemble projections.

Given that shelf-wide total melt is a robust predictor of sea level rise contributions, future studies should include total melt values in addition to other descriptors of melt (e.g., average melt rates or melt parameterizations) to facilitate comparison with other studies as discussed above. For example, plotting results from multiple studies as shown in Figure 10 would help differentiate the cases where different models produce results consistent with the level of melt forcing (e.g., the results lie along a linear regression line with high r^2 near 1) from those where the differences are due to some other aspect of the model (e.g., results are not explained well by a linear regression to melt). For example, the fact that melt is a strong predictor of loss in the Amundsen Sea Embayment for the suite of ISMIP6 models (Seroussi et al., 2020), suggests that much of the difference 460 between models in this region may be due to how they treat melt, as opposed to differences in their treatment of ice dynamics.

Our use of prescribed, rather than freely evolving, melt rates does not necessarily emulate natural processes. It does, however, provide a controlled way to evaluate the response of a coupled ice-sheet/ice-shelf system to melt forcing. The resulting regressions reliably predict the VAF loss in cases where the total melt can be determined (e.g., dashed curves in Figure 10).

465 While we used a constant melt forcing, a melt history supplied by any methods that can estimate total melt for a given cavity geometry (e.g., offline ocean model) could be used. Removing the details of the spatial distribution of melt may allow the use of simpler, more loosely coupled models that only need to determine the total melt at infrequent intervals so long as they track the long-term melt trend.

5.4 PIG and Thwaites Glacier Outlook

- 470 Our simulations are not projections since they are not tied to climate forcings. Nor do they include factors not related to ocean melt such as increased accumulation as atmospheric temperatures rise (Donat-Magnin et al., 2021), loss of ice shelf area, or glacial isostatic adjustment (Larour et al., 2019). Nonetheless, they do provide some sense of how much these glaciers will contribute to sea level rise over the next two centuries in response to basal melt.
- 475 Prior estimates for PIG melt range from 76 to 101 Gt/yr (Rignot et al., 2013; Depoorter et al., 2013; Shean et al., 2019; Adusumilli et al., 2020) but these estimates cover an area substantially larger than our domain. A recent melt estimate from remote sensing that covers an area similar to our model domain is 67 Gt yr⁻¹ with substantial interannual variability (Joughin et al., 2021b). This value lies between our 57 and 75 Gt yr⁻¹ simulations both of which produce future losses less than the

present rate. The current rates, however, include speedup due to recent ice-shelf loss, which is expected to decline as the system

480 adjusts to the new geometry. Our 100 and 125 Gt yr⁻¹ simulations produce long-term average losses greater than present for PIG with $h_T \ge 41$ m.

Recent simulations of water temperatures with regional-scale ocean models forced with climate model output indicate that melt rates on PIG will increase by \sim 5–8 m/yr (Jourdain et al., 2022), which is equivalent to 21 Gt yr⁻¹ by 2100 for the current ice-shelf geometry. If there is a similar increase for the next century, then our 125 Gt/yr estimate would still exceed the two-

century average. This analysis, however, does not allow for increases in ice-shelf area (Figure 9), which also influence the melt rate. Neglecting the expansion of the ice shelf may not have a big impact on results for PIG. A coupled ice-ocean model produces a relatively steady melt rate of ~150 Gt/yr for warm conditions (base of thermocline at 600 m) through a 120-year simulation in which the glacier has a total VAF loss of 50 mm sle (Bett et al., 2023). Our simulations with depth-parameterized

- 490 melt rates do allow the melt to increase as the ice shelf area expands though not necessarily in a way that realistically accounts for ocean circulation. The most aggressive melt parameterization (see 160_700 in Figure S2) for PIG yielded an average melt rate of 182 Gt yr⁻¹. If we take the corresponding VAF loss as an upper bound, then the maximum 2-century melt-driven VAF loss from PIG is 63 mm sle (Figure 10; h_T =41 m), 24 mm sle of which occurs over the first century of the simulation.
- 495 The evolution of the Thwaites Ice Shelf's cavity is more complex because, in advanced stages of grounding-line retreat, it broadens and deepens, providing a much greater area exposed to high melt rates at depth. Based on an ocean model with warm conditions used by Bett et al. (2023), melt increases from ~46 Gt/yr for the current geometry to ~220 Gt yr⁻¹ when the VAF loss reaches ~40 mm sle. Although their model loses mass much faster than ours due to its treatment of the ice dynamics, the melt rates the ocean model produces at a particular VAF loss should not depend heavily on the time it took to reach that state
- 500 if the temperature forcing is steady as in this case. Assuming a linear increase, these rates imply an average melt rate of ~133 Gt yr⁻¹. For comparison, our 125 Gt yr⁻¹ melt rate produces a VAF loss of 39 mm sle (*h_T*=41 m). Thus, for the warm conditions they used, our simulation suggests losses of ~40 mm sle over the next 200 years. As the cavity beneath the Thwaites Ice Shelf increases in response to greater losses, the melt rates could eventually reach 600 Gt yr⁻¹ (Bett et al., 2023), indicating much larger losses may be likely in the 23rd Century and beyond. For comparison, the most aggressive parameterized melt rate 505 function for Thwaites Ice Shelf produces an average melt rate of 151 Gt yr⁻¹ (*h_T*=41 m; see B&G in Figure 10c), which yields a VAF loss of 46 mm sle (Figure 10). (Note while 160_700 yields less melt, it produces a slightly large loss for Thwaites Glacier.) Thus, melt-driven losses for Thwaites Glacier are likely to remain relatively moderate (< 50 mm sle) over the next two centuries with our preferred value of *h_T* (41 m), which is comparable to PIG. After 200 years, however, as melt rates increase, losses should accelerate rapidly (Joughin et al., 2014). If it turns out that the larger values of *h_T* should be used in
- 510 place of our preferred value, then the period of rapid losses for Thwaites Glacier could occur earlier and could greatly exceed those from PIG (Figure 10).

6. Conclusions

We have conducted several numerical simulations for Pine Island and Thwaites Glacier to understand how their projected contributions to sea level over the next two centuries are affected by the amount of melt and the choice of friction law. For

- 515 most cases, the choice of friction law makes little difference if the same loss of basal traction occurs as the region near the grounding line approaches flotation. Our preferred value (h_T =41 m) produces ~20% more loss than the cases when there is an abrupt transition from full friction to no friction as the ice column goes afloat (h_T =1 m). The value of h_T =41 m is roughly consistent with the degree of weakening introduced by other regularized Coulomb friction laws. Our results indicate, however, that the weakening itself introduced by these friction laws is a far more significant effect than the introduction of Coulomb
- 520 rather than Weertman conditions over a small (<1%) fraction of the domain. The possibility remains that sea level contributions could be much larger (>2x) if a value of h_T substantially larger than our preferred value is found to be more appropriate.

Our results indicate that irrespective of the choice of h_T , losses are a linear function of the total melt averaged over the full simulation period. This linearity holds for simulations with both constant melt and freely evolving depth-parameterized melt.

- 525 The spatial distribution of the melt has little effect on overall VAF loss. Each glacier, however, has a different sensitivity to melt. With its more well-buttressed ice shelf, PIG yields about 50% more VAF loss for each incremental increase in the melt than does Thwaites Glacier. Thus, despite the complexity of the non-linear system, 200-year simulated losses from the glaciers are reliably predicted solely by the spatiotemporally-averaged melt rate.
- 530 While we can't account for other factors that might increase ice loss, such as full ice shelf breakup (MacAyeal et al., 2003) or partial shelf loss (Joughin et al., 2021a), our results suggest melt-driven losses from PIG and Thwaites Glacier over the next two centuries may not exceed 10 cm. Two centuries out, however, both glaciers will have lost a substantial amount of ice and will be primed for much more rapid loss if melt rates don't subside.

Code and data availability

535 The original BedMachine bed and surface elevations and thickness data (DOI: 10.5067/FPSU0V1MWUB6) MeASUREs Phase-Based Antarctica Ice Velocity Map V001 (DOI: 10.5067/9T4EPQXTJYW9) is available at NSIDC. To allow for any updates that may occur during the revision process, we defer the permanent archiving of all other data used to constrain the model until final acceptance. All data and model inputs are freely available at Dyad (https://datadryad.org/stash/dataset/doi:10.5061/dryad.7sqv9s50x).

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Icepack is available at <u>https://icepack.github.io</u> (commit 0c17259979b1e595fdfcccb53bdc6f3d033755c4). The basin-scale model and supporting code are available at <u>https://github.com/fastice/icesheetModels</u> (commit 5c94064) and https://github.com/fastice/modelfunc (commit 904c8a9).

Author contributions

545 IJ conceived the ideas with support from PD. The basin scale model was written by IJ and he performed the model runs and analysis of the results with input from PD and DS. DS wrote the icepack modelling package and provided guidance on its use. All authors contributed to the production of the final manuscript.

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Figure 1. Basal shear stress (τ_b) as a function of speed for conditions representative of flow a) for the strong area upsteam of the grounding line, b) on the weak main trunk farther inland, and c) slow inland tributary flow. In each case, the sliding coefficients have been selected to produce the same speed basal resistance at a nominal reference speed. For the near-grounding-line case, the transition to full Coulomb friction begins at $h - h_f \approx 40$ m (red dotted curve) with mixed conditions occurring at $h - h_f = 45$ (red dot-dashed line).



Figure 2. Height above flotation $(h - h_f)$ contours plotted over inferred basal shear stress (τ_b from RCFi inversion) for (a) Pine Island and (b) Thwaites glaciers. (c) Cumulative distribution functions for τ_b for bands defined by $h - h_f$. Note the contour values correspond to the value of h_T used in our simulations.



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Figure 3. Example of the decrease in basal resistance as ice approaches flotation for the different friction laws described in the text.



810 Figure 4. Cumulative volume above flotation (VAF) losses for PIG and Thwaites Glacier simulated using RCFi for melt rates applied to each glacier's ice shelf of a) 57 Gt yr⁻¹, b) 75 Gt yr⁻¹, c) 100 Gt yr⁻¹, and d) 125 Gt yr⁻¹. All simulations h_T =41 m. Also shown is the initial combined VAF loss rate based on observed velocity linear extrapolated over 200 years. All losses are subject to mapprojection-related biases of a few percent.



815 Figure 5. Cumulative VAF loss for both glaciers simulated using both RCFi and Weertman sliding for several values of h_T for melt applied to each glacier's ice shelf of a) 57 Gt yr⁻¹, b) 75 Gt yr⁻¹, c) 100 Gt yr⁻¹, and d) 125 Gt yr⁻¹. All losses are subject to mapprojection-related biases of a few percent.



820 Figure 6. Annual VAF loss for PIG and Thwaites Glacier simulated using RCFi with melt applied to each glacier's ice shelf of a) 57 Gt yr⁻¹, b) 75 Gt yr⁻¹, c) 100 Gt yr⁻¹, and d) 125 Gt yr⁻¹. The current rates based on velocities used to initialize the model are also shown. All losses are subject to map-projection-related biases of a few percent.



Figure 7. Simulated 200-year VAF losses as a function of melt for a) both glaciers, b) PIG, and c) Thwaites Glacier. Results are shown for several values of h_T and both RCFi and Weertman sliding. Each result represents the average of an ensemble of 30 simulations with randomly generated melt distributions, which are shown only for the RCFi simulations. The lines show linear regressions to the ensemble data (4x30 points), with the corresponding slopes given in each legend. As such, the r² values in the legend represent the proportion of the variance caused by the melt forcing.



Figure 8. Simulated 200-year VAF loss/gain for h_T =41 m averaged over 30 ensemble members for RCFi with melt applied to each glacier of a) 57 Gt/yr, b) 75 Gt/yr, c) 100 Gt/yr, and d) 125 Gt/yr, and for Weertman sliding with melt of e) 57 Gt/yr, f) 75 Gt/yr, g)

835 glacier of a) 57 Gt/yr, b) 75 Gt/yr, c) 100 Gt/yr, and d) 125 Gt/yr, and for Weertman sliding with melt of e) 57 Gt/yr, f) 75 Gt/yr, g) 100 Gt/yr, and h) 125 Gt/yr. Speed at 1000 m/yr intervals are shown in black and basin boundaries are shown in blue. The magenta box in panel a indicates the area shown in more detail in Figure 9.



Figure 9. The number of ensemble members (colour) h_T =41 m simulations at each point that are floating after 200 years simulated with RCFi for melt per glacier of a) 57 Gt/yr, b) 75 Gt/yr, c) 100 Gt/yr, and d) 125 Gt/yr, and with Weertman sliding for melt of e) 57 Gt/yr, f) 75 Gt/yr, g) 100 Gt/yr, and h) 125 Gt/yr. The speed at 1000 m/yr intervals is shown in black.



Figure 10. Simulated 200-year VAF losses as a function using depth-parameterized melt functions for a) both glaciers, b) PIG, and c) Thwaites Glacier with RCFi. Results are shown for several values of h_T . The solid lines show the linear regressions to the plotted points, and the dashed lines are those computed from the RCFi ensemble data shown in Figure 7. The $r_{const.melt}^2$ values show the fraction of variance that the constant melt regression parameters explain for the depth-parameterized melt function simulations.