Polar Mesospheric Summer Echo (PMSE) Multilayer Properties During Solar Maximum and Solar Minimum

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Abstract.

Polar Mesospheric Summer Echoes (PMSE) are radar echoes that are measured in the upper atmosphere during the summer months and that can occur in several layers. In this study, we aimed to investigate the relationship between PMSE layers ranging from 80 to 90 km altitude, and the solar cycle. We investigated 230 hours of observations from the EISCAT VHF radar located near Tromsø, Norway, from the years 2013, 2014 and 2015, during solar maximum and the years 2019 and 2020 during solar minimum and applied a previously developed classification model to identify PMSE layers. Our analysis focused on parameters such as the altitude, thickness, and echo power in the PMSE layers, as well as the number of layers present. Our results indicate that the average altitude of PMSE, the echo power in the PMSE and the thickness of the layers is on average higher during solar maximum than during solar minimum. In the considered observations, the electron density at 92 km altitude and the echo power in the PMSE are positively correlated with the thickness of the layers, except for four multi layers at solar minimum. We infer that higher electron densities at ionospheric altitudes might be necessary to observe multi-layered PMSE. We observe that the thickness decreases as the number of multi-layers increase. We compare our results with previous studies and find that similar results regarding layer altitudes were found in earlier observations with other VHF radars. We also observed that the bottom layer in in the different sets of multilayers almost always aligned with the Noctilucent Clouds (NLC) altitude reported by previous studies of 83.3 km altitude. Also, an interesting parallel is seen between the thickness of NLC multi layers and PMSE multi layers, where both NLC and PMSE have a similar distribution of layers greater than 1 km in thickness. Future studies that include observations over longer periods would make it possible to distinguish the influence of the solar cycle from possible other long-term trends.

1 Introduction

During the summer months, radars can measure a phenomenon in the upper atmosphere called Polar Mesospheric Summer
Echoes (PMSE). PMSE are strong radar echoes that ~~are linked to~~ typically form at heights between 80 and 90 kilometers and
in regions of extremely cold temperatures~~, and they have a characteristic wavy pattern of~~. They are observed at mid and high
latitudes and their height and thickness ~~variation over time~~varies over time, (Rapp and Lübken, 2004). Figure 1 shows a typical
example of a PMSE ~~occurrence, where it is possible to notice the variation of altitude an thickness of the PMSE over time.~~
~~These echoes occur between 80 and 90 kilometers (km) altitude. Their formation requires~~ event where these variations can be
seen. The PMSE formation is linked to the presence of turbulence, free electrons, and charged aerosols. The charged aerosols
contain water ice, which requires the presence of low temperatures, sufficient water vapor, and nucleation centers to fos-
ter heterogeneous condensation, ~~Latteck et al. (2021), Cho and Röttger (1997), Rapp and Lübken (2004)~~(Latteck et al., 2021),
(Cho and Röttger, 1997), (Rapp and Lübken, 2004). The mesopause, which marks the boundary between the mesosphere and
the thermosphere, is characterized by the lowest temperatures in the atmosphere. Such low temperatures at PMSE altitudes
are conducive to ice formation. Meteor Smoke Particles (MSP), produced by meteor ablation and recondensation have been
proposed as ~~the likely condensation nuclei , formed through meteor ablation and recondensation~~potential condensation nuclei
along with several other potential nuclei, (Rapp and Thomas, 2006). In addition to ~~MSP~~nucleation centers, the presence ~~of cold~~
~~temperatures and water vapor at~~ water vapor and the low temperatures at the mid and high ~~latitudes at the~~latitude mesopause
during the summer months ~~creates~~ create conditions favorable for ice particle formation~~Avaste (1993)~~, (Avaste, 1993). Cold
temperatures and ~~MSPs~~water ice are known to be at the origin of another phenomenon called Noctilucent Clouds (NLC)~~Latteck et al. (2021~~
~~. The combination of neutral air turbulence and negatively charged ice particles results in irregularities in electron density,~~
~~generating the observed radar echoes or PMSE, at the Bragg wavelength, as described in Latteck et al. (2021)~~, (Schäfer et al., 2020)
, that are due to light scattered at the ice particles observed from the ground. More general, and when observed from space, the
clouds of ice particles are denoted as polar mesospheric clouds, (Fritts et al., 2019).

The PMSE are formed through a process that involves the electrical charging of the ice particles and is for instance
discussed by Rapp and Lübken (2004) and Latteck et al. (2021). They are strong radar echoes, and they result from reflections
at inhomogeneities in the electron density when their spatial scales are of sizes comparable to half the radar wavelength.
Constructive interferences of the reflections result in high backscattered power and narrowly peaked power spectra. Such
strong echoes are typically from turbulence in the partially ionized upper atmosphere. The PMSE are in addition influenced by
the presence of charged ice particles. The ice particles are spatially structured by the turbulence and as the ice particles collect
ambient electrons when they are charged, they cause electron gradients to last longer and to form on smaller scales. The radar
echoes in PMSE are stronger compared to normal incoherent scattering. The neutral atmospheric motion and dissipation of
gravity waves at these altitudes are causes for the turbulence.

The EISCAT VHF radar used in our study is designed to measure the incoherent scatter, which comes from the small scale
fluctuations of electrons in the ionospheric plasma. As the ionospheric electrons are exposed to the electromagnetic wave
transmitted by the radar, the Thomson scattering scatters a small fraction back. The back scattered power is proportional to the

electron density and the electron oscillations which in turn are influenced by ion interactions. As a result, the spectra measured from incoherent scatter allow one to derive from the observed signal the electron density, and electron and ion temperatures, (Beynon and Williams, 1978). In their study, Rapp and Lübken (2004) elucidate the difference to PMSE, where PMSE are typically stronger than incoherent scatter located at the same altitude, and their spectrum is more narrow. The PMSE have different spectral characteristics from the incoherent scattering. Observations with radars that also detect incoherent scatter offer the opportunity to measure the electron density in the vicinity of the PMSE.
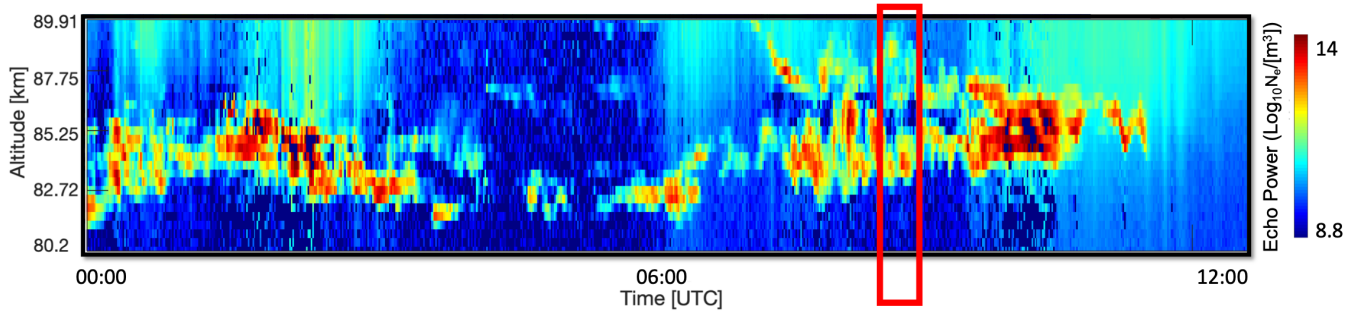
Figure 1. Data from EISCAT VHF from 16 July 2015 from 00:00 to 12:00, showing an example of a PMSE event that contains 3 multi-layers in the red frame.

Multi-layered ~~Polar Mesospheric Summer Echoes (PMSE) have been the focus of several investigations. An example of a PMSE occurrence with three distinct layers is depicted in Figure 1, inside of the red frame. Hoffmann et al. (2005) examined the occurrence and mean altitude of PMSE layers, and performed microphysical model simulations. They proposed that the observed multiple PMSE layer structures are mainly caused by the layering of ice particles due to subsequent nucleation cycles. Li et al. (2016) developed a two-dimensional model to explore the creation process of PMSE. They developed a model able to simulate the presence of gravity waves by assigning both vertical and horizontal wavelengths. They found that increasing the vertical wavelength led to a decrease in the number of layers, while the thickness of the layers increased. Li et al. (2016) also observed that multi-layer formations in their model had preferred altitudes, which were dependent on the size of the ice particles. Additionally, larger particles led to a more rapid decrease in layer altitude and a slower formation.~~

~~Some research has also been done on Noctilucent Clouds (NLC), and NLC multilayers. Despite being distinct phenomena, PMSE and NLC have an overlap in the ice particle population that contributes to their formation mechanisms. Lübken et al. (2009) found that NLCs have higher brightness at lower altitudes, while Schäfer et al. (2020) analyzed 182 hours of LIDAR data and found that NLCs occur most of the time in thick layers of more than 1 km. Additionally, they classified the NLCs they observed into 10 subcategories and found that the most frequently occurring subcategory consist of thick layers composed of multiple multi-layers. They report that each of the multi layers move in parallel with each other. This implies that there is a similar movement in the vertical displacement of the multi layers .~~

Polar Mesospheric Summer Echoes have been the focus of several investigations, (Hoffmann et al., 2005), (Li et al., 2016) , (Shucan et al., 2019). To simplify the exploration of PMSE multilayers, Jozwicki et al. (2021) conducted a preliminary study

demonstrating the feasibility of distinguishing between images containing PMSE and those that do not, employing Linear Discriminant Analysis (LDA). Subsequently, in Jozwicki et al. (2022), a model built on random forests was employed to segment the PMSE signal from the incoherent scatter signal based on the power return in altitude. This model is utilized in the current paper for the pre-selection of data. An example of a PMSE occurrence with three distinct layers is depicted in Figure 1, inside of the red frame. Given the significance of electron density in PMSE formation, it is reasonable to expect a potential influence of the solar cycle in it. Limited research has been conducted to examine the connection between multi-layered PMSE and the solar cycle. Zhao et al. (2020) reported a positive correlation between the temperature of the mesopause and the solar flux at 10.7 cm wavelength (F10.7 flux), and found that the height of the mesopause is decreasing with time at polar latitudes. The mesopause, which marks the boundary between the mesosphere and the thermosphere, is characterized by the lowest temperatures in the atmosphere. Such low temperatures at PMSE altitudes are conducive to ice formation, and PMSE are known to be influenced by ice formation through the slowing of diffusion processes. The F10.7 flux is often used as a proxy for the level of solar activity and, more specifically, the amount of ultraviolet radiation that reaches the Earth's upper atmosphere. Shucan et al. (2019) found that PMSE mono, double, and triple layer occurrence ratios are positively correlated with the K index, which corresponds to geomagnetic activity and potential particle precipitation. Also, Shucan et al. (2019) mentions that the PMSE triple layer occurrence ratio shows a negative correlation with F10.7. Narayanan et al. (2022) investigated the effects of particle precipitation on PMSE formation using electron densities from 90 to 95 km, and found that the sudden increase in electron densities due to particle precipitation amplifies the PMSE structures, resulting in an increase in the strength of the backscattered signal.

Understanding the trend of winds and gravity waves at PMSE altitudes is fundamental in comprehending the formation of PMSE. Neutral wind shears generate turbulence which is a key factor in PMSE measurements. Singer et al. (2012) found that westward winds are increasing below an altitude of about 85 km, while eastward winds are increasing above 85 km, particularly during summer. They also found that at an altitude of about 75 km, the long-term trend of zonal winds corresponds to increased activity of gravity waves with periods of 3 to 6 hours at altitudes between 80 km and 88 km. Severe solar proton events cause eastward winds to increase above an altitude of about 85 km. This behavior of winds and gravity waves at PMSE altitudes may be key to better understanding the turbulence at those altitudes leading to the formation of multi-layered PMSE.

We investigate PMSE observations with EISCAT VHF during the recent years. Our objective is to analyze the number of PMSE layers, their thickness, altitude, and general behavior during solar maximum and minimum, and to determine possible correlations between these variables and the electron density at ionospheric heights above PMSE. The study is organized as follows: In Sect. 2, we describe the methods and theories related to the pre-selection of the PMSE data, as well as the correlation coefficients employed to assess the significance of our results. In Section 3, we present and discuss the obtained results. Finally, in Sect. 4, we summarize the conclusions drawn from this study.

2   Methods and Theory

In this section, we will ~~provide an overview of the theoretical background behind the formation of PMSE. We will then~~ describe our methodology for data selection, including the tools utilized. Furthermore, we will present the criteria used for identifying the different PMSE layers and the metrics employed for analyzing the collected data.

2.1   ~~Theory behind the formation of PMSE~~

In this study, we use recorded data from the EISCAT VHF radar located in Tromsø that operates at 224 MHz. ~~EISCAT VHF measures the small scale fluctuations of electrons in the ionospheric plasma. When an electromagnetic wave from EISCAT VHF is transmitted into a portion of the ionosphere, the electric field of the wave causes ionospheric electrons to begin oscillating. The electrons scatter the electromagnetic wave with the same frequency as the incoming wave. This is Thomson scattering. The distribution of the electron velocities results in the Doppler spectrum observed. This process, called incoherent scatter depends on ionospheric plasma parameters, and one can derive from the observed signal the electron density, and electron and ion temperatures Beynon and Williams (1978). In their study, Rapp and Lübken (2004) elucidate the difference to PMSE, where PMSE are typically stronger than incoherent scatter located at the same altitude, and their spectrum is more narrow.~~

~~The PMSE have different spectral characteristics, and they arise due to the combination of several different processes. Gravity waves propagate through the atmosphere and break around the altitude where PMSE form. When these waves break, they create various areas of turbulence, among which some areas would be larger, and some would be smaller. The turbulence structures the present electron content in those areas, as the electrons are coupled to the larger ions in the region that are influenced by the neutral atmospheric motion and turbulence. The radar signal measures the turbulence occurring at scales of half the radar wavelength, Rapp and Lübken (2004). When this happens, the oscillating electrons, governed by the turbulence present in the area, will scatter electromagnetic waves in a similar direction. Constructive interferences will happen, resulting in an amplified backscattered power and a narrower peak in the power spectrum compared to a case without PMSE. Of course, in the case of a portion or ionosphere with PMSE, the resulting power spectrum can have both spectral signatures discussed above: the regular incoherent scatter signal which is broader, as well as the signal that comes from the coherent interferences that would be more narrow~~The geographical coordinates of the EISCAT VHF radar are 69°35′N and 19°14′E; its geomagnetic latitude and longitude are respectively 66.73° and 102.18°.

2.1   Data selection

The Grand Unified Incoherent Scatter Design and Analysis Package (GUISDAP) is a software package used for processing and analyzing data from the EISCAT VHF incoherent scatter radar, ~~Lehtinen and Huuskonen (1996)~~(Lehtinen and Huuskonen, 1996). GUISDAP analysis fits the observed frequency spectrum received from each height with an incoherent scatter profile. The analysis returns the electron density based on the backscattered power, independently from the scattering process. The electron density parameter given by the analysis is proportional to the received echo power and therefore the strength of the PMSE.

Table 1. Data-set used for this study. The upper part of the table displays the dates and times selected for the solar maximum, and the lower part of the table is dedicated to the solar minimum. For each date, the corresponding sunspot number and the F10.7 cm flux is displayed. The F10.7cm solar flux is given in $W.m^{-2}.Hz^{-1}$. The date and time format are given respectively by the dd/mm/yyyy and the ...h...m format.

	F10.7 cm Flux	Sunspot Number	Year	Date	Start time	End time	Observation Hours per Day	Observation Hours per Year	Observation Hours per Solar Max. or Min.	Total of Observation Hours
Solar Maximum	9.95000e-21	90.9	2013	27/06/2013	07h02m	10h58m	03h56m	57h52m	130h18m	230h32m
	1.01000e-20	90.9		28/06/2013	07h02m	12h58m	05h56m			
	1.19900e-20	94.6		09/07/2013	00h00m	00h00m	24h00m			
	1.17900e-20	94.6		10/07/2013	00h00m	00h00m	24h00m			
	9.91000e-21	112.6	2014	23/07/2014	00h00m	09h26m	09h26m	09h26m		
	1.01000e-20	68.3	2015	15/07/2015	08h00m	00h00m	16h00m	63h00m		
	9.96000e-21	68.3		16/07/2015	00h00m	00h00m	24h00m			
	9.74000e-21	68.3		17/07/2015	00h00m	23h00m	23h00m			
Solar Minimum	6.70000e-21	3.7	2019	18/06/2019	06h59m	00h00m	17h00m	59h13m	100h14m	
	6.80000e-21	3.7		19/06/2019	00h00m	12h59m	12h59m			
	6.80000e-21	3.5		04/07/2019	07h07m	12h21m	05h14m			
	6.70000e-21	3.4		20/08/2019	00h00m	00h00m	24h00m			
	6.90000e-21	9.0	2020	06/07/2020	07h58m	09h08m	01h06m	41h01m		
	6.80000e-21	9.0		07/07/2020	00h00m	11h59m	11h59m			
	6.70000e-21	9.0		08/07/2020	00h00m	11h59m	11h59m			
	6.90000e-21	9.0		09/07/2020	00h00m	11h58m	11h58m			
	6.90000e-21	9.0		10/07/2020	08h00m	11h59m	03h59m			

We downloaded over 230 hours of recorded data via the ~~Magridal~~ Madrigal website. This corresponds to 17930 data points, with the details provided in Table 1. The EISCAT VHF radar utilizes ~~multiple~~ many different experimental modes to collect data. The utilized pulse coding for the PMSE measurements we analyzed is referred to as 'Manda'. Some parameters of the EISCAT VHF radar using the 'Manda' experiment are listed in Table 2. Detailed information regarding this experiment can be found on the EISCAT website (https://eiscat.se/scientist/document/experiments/). For this study, we specifically analyzed data obtained using the ~~manda code, which~~ 'Manda' experiment, because it is designed to detect low-altitude signals and ~~provides spectral measurements at mesospheric altitudes~~ layers in the mesosphere. We chose a time resolution of 60 seconds and a height resolution of 0.360 km.

We employed EISCAT VHF frequencies over UHF frequencies due to the latter exhibiting a lower recorded amount of PMSE compared to VHF frequencies. As the Heating experiment is known to influence the back-scattered power (also known as echo power) of the PMSE, ~~Belova et al. (2003)~~ (Belova et al., 2003), we carefully selected data from the days when the Heating experiment was not performed. This enabled us to compare electron densities at 92 km altitude alongside echo power at PMSE altitudes.

Table 2. Some parameters of the EISCAT VHF radar, the source of data for this paper. More information about the EISCAT documentation and radar system parameters can be found at: https://eiscat.se/scientist/document/experiments/.

EISCAT VHF parameters	
Frequency	223.4 MHz
Wavelength	1.34 m
Bragg scale	0.67 m
Peak power	1.2 MW
Transmitted pulse scheme	Manda v 4.0
Interpulse period	1.5 ms
Time resolution	4.8 s
Range resolution	360 m
Spectral resolution	2.6 Hz
Antenna Elevation	90 deg, zenith

The data was carefully selected to encompass the solar maximum and solar minimum phases of the solar cycle. For the purpose of this study, we do not require an absolute value of PMSE strength, thus, we do not perform all the steps that would be necessary to obtain the absolute radar reflectivity as per the study by Hocking et al. (1986).

To investigate the behaviour of the ionosphere in relation to PMSE, we compared the echo power for PMSE altitudes between 80 and 90 km, with the electron density at 92 km ionospheric altitude. We used the electron density at 92 km altitude as a reference as it was the closest to the PMSE altitudes and the results were similar for altitudes of 92, 95, and 100 km.

2.2 Data processing

In this paper, we consider two variables: echo power and electron density. Both are measured in base 10 logarithmic units of the number of electrons per cubic meter. The number of electrons per cubic meter is proportional to the back-scattered power for incoherent scatter, where the back-scattered power is defined as the amount of power in the scattered signal received by the antenna. We define the back-scattered power at 92 km altitude as electron density. The back-scattered power at PMSE altitudes, between 80 and 90 km altitude, is defined as echo power.

We selected the PMSE data between 80 and 90 km altitude by using a segmentation model from the study by Jozwicki et al. (2022). The segmentation model used random forests on a set of hand-crafted features to segment the PMSE data from the background. Random forests is a machine learning algorithm used for both classification and regression. In this algorithm, a number of decision trees are used during training phase to make predictions. On the output from the segmentation model, we applied a threshold to ensure that only PMSE data were retained for further analysis. This thresholding technique was also employed in the study by Shucan et al. (2019), where they used an echo power threshold $N_e > 2.6 \times 10^{11} m^{-3}$, and in the study by Rauf et al. (2018b), where the authors used a threshold $N_e > 5.0 \times 10^{10} m^{-3}$. We were able to use a lower threshold

175 of $N_e > 3.2 \times 10^{10} m^{-3}$ (which is equivalent to 10.5 in base 10 logarithmic units of the number of electrons per cubic meter) as the segmentation model from the study by Jozwicki et al. (2022) had successfully removed almost all non-PMSE data. This enabled us to retain a large amount of PMSE data per number of hours of observation, in comparison to the findings of Shucan et al. (2019) and Rauf et al. (2018b).

2.3 Detection of PMSE multi-layers

180 After processing the data at PMSE altitudes as described in Sect. 2.2, we aimed to detect the start and end of each PMSE layer in altitude. To achieve this, we utilized a method used in the study by Hoffmann et al. (2005) and Shucan et al. (2019). This method involves defining the start of a layer each time the threshold for echo power is exceeded, and the end of the layer when the echo power falls below the given threshold. The time intervals and the corresponding altitude intervals associated with the start and end of each layer were recorded. During solar maximum conditions, we observed a maximum of six layers.

185 In this study, we decided to ignore multi layers with more than 4 layers, as their occurrence rates were low. For instance, we observed 13 occurrences of 5 multi layers in the whole data-set, and 2 occurrences of 6 multi layers. In Table 3, we show the occurrences of monolayer and multilayer PMSE events, observed during the solar minimum and solar maximum phases, with each occurrence corresponding to a 1-minute interval.

2.4 Data analysis

190 In this study, we perform comparisons between the different mono and multi layers of PMSE by using a number of parameters. The parameters included the starting and ending altitude intervals of the layer, the layer thickness (calculated as the difference between the start and end altitude interval), the mean altitude interval that corresponds to the middle of the layer, the echo power in the mean altitude interval inside the PMSE, the altitude of the mean altitude interval, the layer's time interval, the UTC time associated with the time interval, the number of layers present in the time interval, and the electron density at 92 km

195 altitude.

In order to investigate different PMSE properties, we use the Pearson correlation coefficient and the Spearman's rank correlation coefficient to calculate the correlations between the different parameters, (Wilks, 1995), (Myers and Well, 2003). The Pearson correlation coefficient is used to measure how strong and in what direction two variables are related in a linear way Wilks (1995), (Wilks, 1995). For two random variables X and Y, the Pearson correlation coefficient is defined as fol-

200 lows Wilks (1995), (Wilks, 1995):

$$r_{Pearson}(X,Y) = \frac{cov(X,Y)}{\sigma_X \sigma_Y} \tag{1}$$

Where σ_X and σ_Y are the respective standard deviations of X and Y, and cov is the covariance.

The Spearman's rank correlation coefficient is a measure of the strength and direction of the relationship between two variables. It is similar to the Pearson correlation, but instead of measuring the linear relationship between two variables, it

205 measures the monotonic relationship between them. The Spearman's rank correlation coefficient is obtained by calculating the
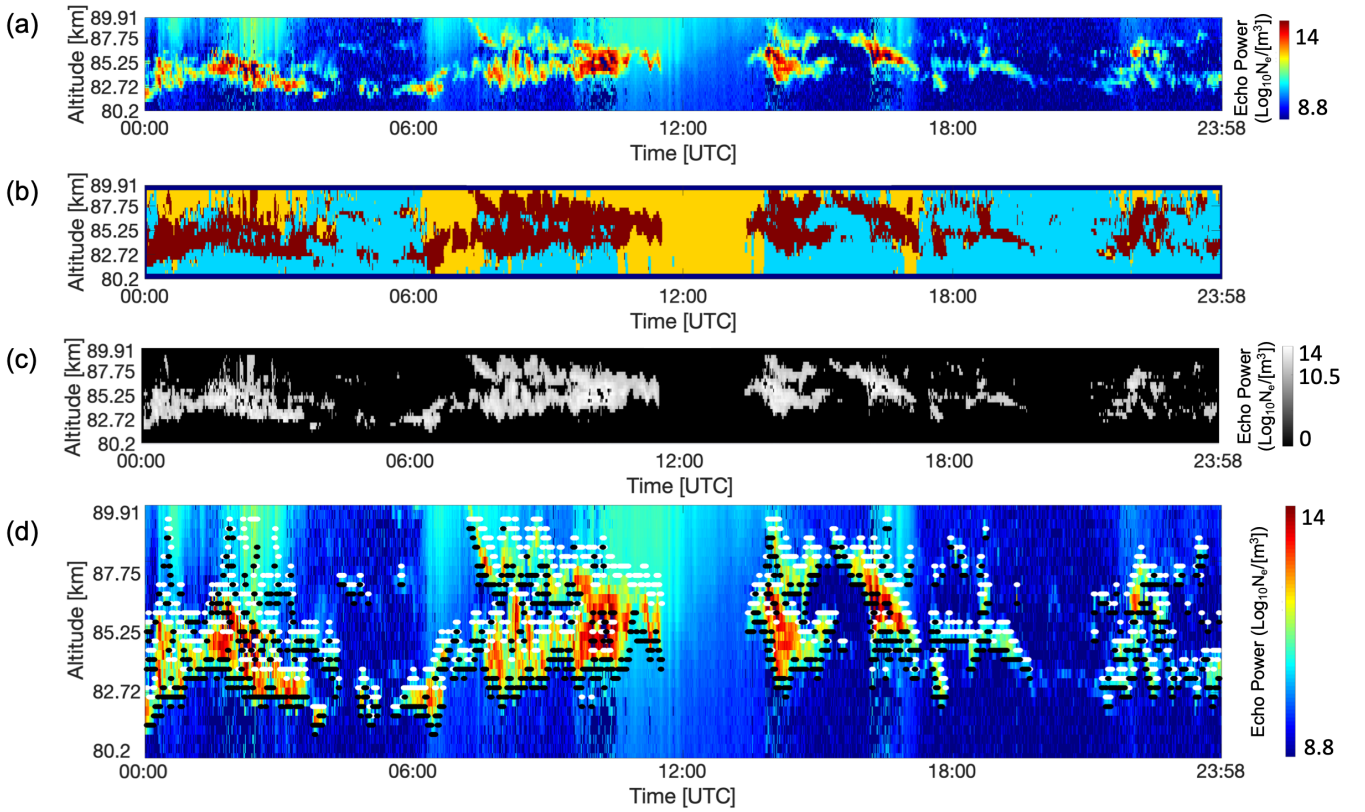
Figure 2. Figure illustrating the process of the layer detection. **(a)** shows the original data for the 16 July 2015 between 00:00 and 23:58. **(b)** shows the output from the classification model used from Jozwicki et al. (2022). Dark red represents areas labeled as PMSE, cyan represents areas of the data labeled as background noise and yellow represents areas labeled as ionospheric background. **(c)** represents the data labeled as PMSE in dark red from sub Fig. 2(b), onto which we applied the threshold described in Sect. 2.2 to make sure we have only PMSE data left. Finally, **(d)** represents the detected beginning and end of layers respectively represented with white and black points, overlayed on the original data.

Pearson correlation between the ranked values of the variables~~(Myers and Well, 2003)~~, (Myers and Well, 2003). To compute the Spearman correlation coefficient, for a sample size n, the raw scores Xi and Yi are converted into their rank values rg_X and rg_Y. After that, the Spearman correlation coefficient is then computed as follows:

$$r_{Spearman} = \frac{cov(rg_X, rg_Y)}{\sigma_{rg_X} \sigma_{rg_Y}} \tag{2}$$

210   Where σ_{rg_X} and σ_{rg_Y} are the standard deviations of the rank variables, and cov(rg_X, rg_Y) is the covariance of those rank variables.

In this analysis, we calculated the statistical significance of our results using the p-value (t-test), which are listed in Tables B2, B4 and B3 in the Appendix. P-values are used to determine whether the obtained results are different enough to be judged

Table 3. This table displays the number of occurrences and approximate percentage of occurrence for each of the mono and multi layers in our data-set. The data is separated by solar maximum and solar minimum. For both solar maximum and solar minimum, the approximate percentage of occurrence for 5 multi layers or more is below one percent. Therefore, the analysis in this study is limited to PMSEs with up to four multi-layers.

		Number of Occurrences	Total Number of Occurences per Sol Max. or Min.	Approximate Pencentage of Occurence
Solar Maximum	Mono Layers	3077		51
	2 Multi Layers	2233		37
	3 Multi Layers	597		10
	4 Multi Layers	81	5996	1
	5 Multi Layers	6		<1
	6 Multi Layers	2		<1
	7 Multi Layers	0		0
Solar Minimum	Mono Layers	1399		51
	2 Multi Layers	935		34
	3 Multi Layers	328		12
	4 Multi Layers	67	2736	2
	5 Multi Layers	7		<1
	6 Multi Layers	0		0
	7 Multi Layers	0		0

statistically significant or not, using the means, variances, and populations of the given variables. If the p-value falls below the significance level (alpha), the given result is considered to be statistically significant. Testing the statistical significance of results comes with various confidence levels (90%, 95%, and 99%), which depend on the chosen significance level (with corresponding significance levels of 0.1, 0.05, and 0.01). It is commonly accepted that a p-value below $\alpha = 0.05$ is indicative of statistical significance. However in this study, we are analyzing a multi parameter dataset, which is why we chose a lower threshold of $\alpha = 0.0001$, which is two orders of magnitude more selective.

3 Results and Discussion

In this section, we will discuss our results which are organized into multiple parts. Firstly, we will discuss the distributions of a few variables, which will be presented using histograms. Subsequently, we will analyze the correlation coefficients that we have computed for the different variables.

3.1 Height distribution of PMSE layers

225 ~~The average altitude of all layers together~~ Our study focuses on observations from the summer mesopause during solar maximum in years 2013 to 2015, and solar minimum in years 2020 and 2021. The average peak altitude of PMSE height distribution, considering all PMSE detections, is higher during solar maximum than during solar minimum ~~as illustrated in~~ (see Fig. 3 ~~. There is a slight increase in altitude with increasing number of~~). The averaged mean altitude values of all the separate layers in the ~~case of solar maximum seen~~ different sets of 2 multilayers, 3 multilayers and 4 multilayers, are shown in

230 the Appendix section, in Fig.A1 ~~, but not in the case of solar minimum seen~~ and Fig.A2.

When considering the mean altitude values of individual layers within the sets of 2, 3, and 4 multilayers, a trend is seen in Fig. 4 and Fig. 5. In these figures, the color scheme has the red distribution representing the highest-altitude layer (the topmost layer), followed by the green distribution for the second highest layer, the blue distribution for the third highest layer, and the magenta distribution for the fourth highest layer. Additionally, when two layers' altitude distributions overlap, an intermediate

235 color arises to represent this overlap. The p-values for all possible combinations of these individual layers, as shown in Fig. ~~A2.~~ 4 and Fig. 5, can be found in Table B1 in the Appendix. Upon decomposing the multilayer sets into individual layers, one can see that in both solar maximum and solar minimum conditions, the altitude of the top layer increases as the number of multilayers increases. This pattern holds true for the second and third highest layers as well.

Our study confirms the findings of Hoffmann et al. (2005) regarding the altitude of the observed mono ~~layers.~~ and multiple

240 layers. Hoffmann et al. (2005) examined the occurrence and mean altitude of PMSE layers, and performed microphysical model simulations. They proposed that the observed multiple PMSE layer structures are mainly caused by the layering of ice particles due to subsequent nucleation cycles. They reported that mono layers occurred at an average altitude of 84.8 km, and our results show that the mean altitude of mono layers was 85.21 km for solar maximum and 84.46 km for solar minimum. Our mean altitude of 84.83 km is consistent with the results of Hoffmann et al. (2005). ~~They~~ Furthermore, they observed that

245 in a set of two multilayers, the lower layer occurs at a mean altitude of 83.4 km, and the upper layers occurs at a mean height of about 86.3 km, which is consistent with our findings. In fact, we found that in a set of two multilayers, the lower layer happens at a mean altitude of 83.74 km for solar maximum and 82.90 km for solar minimum, which results in an average of 83.32 km. Additionally, the upper layer occurs at an average altitude of 86.71 km for solar maximum and 85.97 km for solar minimum, which results in an average altitude of 86.34 km over the whole solar cycle. For this reason, we can note a similar

250 observation as Hoffmann et al. (2005) did in their study, that the altitude of the lower layer is in good agreement with the mean altitude of NLC from lidar observations made by Fiedler et al. (2003) at ALOMAR (at 69°16'42.0"N 16°00'29.0"E, i.e. close to EISCAT), where the mean altitude of NLC was found to be of about 83.3km. When examining the lowest layer in various multilayer sets in Fig. 4 and Fig. 5 (not limited to a set of just two multilayers, as discussed earlier), one can notice that the lowest layer almost always aligns with the NLC altitude as reported by Fiedler et al. (2003). Finally, Hoffmann et al. (2005)

255 observed that mono layers occurred 50.1%, double layers 36.6%, and multi layers with more than 2 layers 13.3%, during both solar maximum and minimum periods. Our study indicates that mono layers were observed at a rate of 51% in both solar maximum and minimum, while double layers occurred at a rate of 37% in solar maximum and 34% in solar minimum. Furthermore,

we found that the occurrence rate for multi layers with 3 and 4 layers combined was more than 11% in solar maximum and
more than 14% in solar minimum. ~~Therefore, our results are consistent with those of Hoffmann et al. (2005) concerning the~~

260 ~~occurrence rate of mono and multi layers too.~~

~~An unexpected result is that during solar maximum , the average altitude of PMSEs is higher than during solar minimum .~~
~~This is counter-intuitive, as one might expect that during solar maximum, the higher energy of incoming particles from the Sun~~
~~would result in a lower altitude of PMSEs due to their ability to penetrate further into the atmosphere~~The solar maximum phase
is characterized by an increased number of sunspots and higher levels of ultraviolet radiation compared to the solar minimum

265 phase. The F10.7 flux is often used as a proxy for the level of solar activity and, more specifically, the amount of ultraviolet
radiation. Shucan et al. (2019) found that PMSE mono, double, and triple layer occurrence ratios are positively correlated
with the K index, which corresponds to geomagnetic activity and potential particle precipitation. Also, Shucan et al. (2019)
mentions that the PMSE triple layer occurrence ratio shows a negative correlation with F10.7. Zhao et al. (2020) reported a
positive correlation between the temperature of the mesopause and the solar flux at 10.7 cm wavelength (F10.7 flux). They

270 found that the temperature of the mesopause is decreasing with time over 18 year long investigation (from 0 to -0.14 K/year),
which could affect the formation of PMSE. They also found that the height of the mesopause is decreasing with time at polar
latitudes, which could potentially impact the height of PMSE.

Lübken et al. (2021) show in their study that over time the ice particles are increasing in size. In Fig. 3, we can see that the
altitude of the PMSE layers is on average lower for solar minimum compared to solar maximum. This could be due to the fact

275 that the ice particle sizes increase over time, and our selected date for the solar maximum are anterior to the selected dates for
the solar minimum. Considering these findings, the small difference in the altitude of the layers that we noted may be due to
trends not related to solar cycle effects. Therefore, it appears that factors other than the sole influence from the solar cycle play
a significant role in the altitude of PMSE.

~~Zhao et al. (2020) found that the height of the mesopause is decreasing with time at polar latitudes over their 18 year long~~

280 ~~investigation time. Our study focuses on observations from the summer mesopause during solar maximum in years 2013~~
Finally, further investigations, comparing the next solar maximum to ~~2015, and solar minimum in years 2020 and 2021. We~~
~~could hypothesize that in the latter years corresponding to solar minimum,~~ the previous one, might bring more clarity in ~~the~~
~~mesopause was lower than during the previous years corresponding to solar maximum . This could have potentially made it~~
~~possible for PMSE to appear over a wider altitude range during solar minimum, and therefore at lower altitudes. We indeed~~

285 ~~notice in Fig. 3 that the average altitude of PMSE is slightly lower during solar mimimum, and that the calculated standard~~
~~deviation is higher during solar minimum compared to solar maximum, which means that the PMSE would indeed be able to~~
~~form over a wider altitude interval~~understanding of the influence from the solar cycle alone.

3.2 Distribution of the electron density

In the next step, we investigate how the distribution of the PMSE layers ~~varies with the ionizationobserved at the same~~

290 ~~time~~changes with ionization. We consider the electron densities observed above the PMSE and ignore specific causes of
ionization in this study. All the observed ~~electrons~~ electron densities are summarized in Fig. 6; they range from 8.9 to 11.7
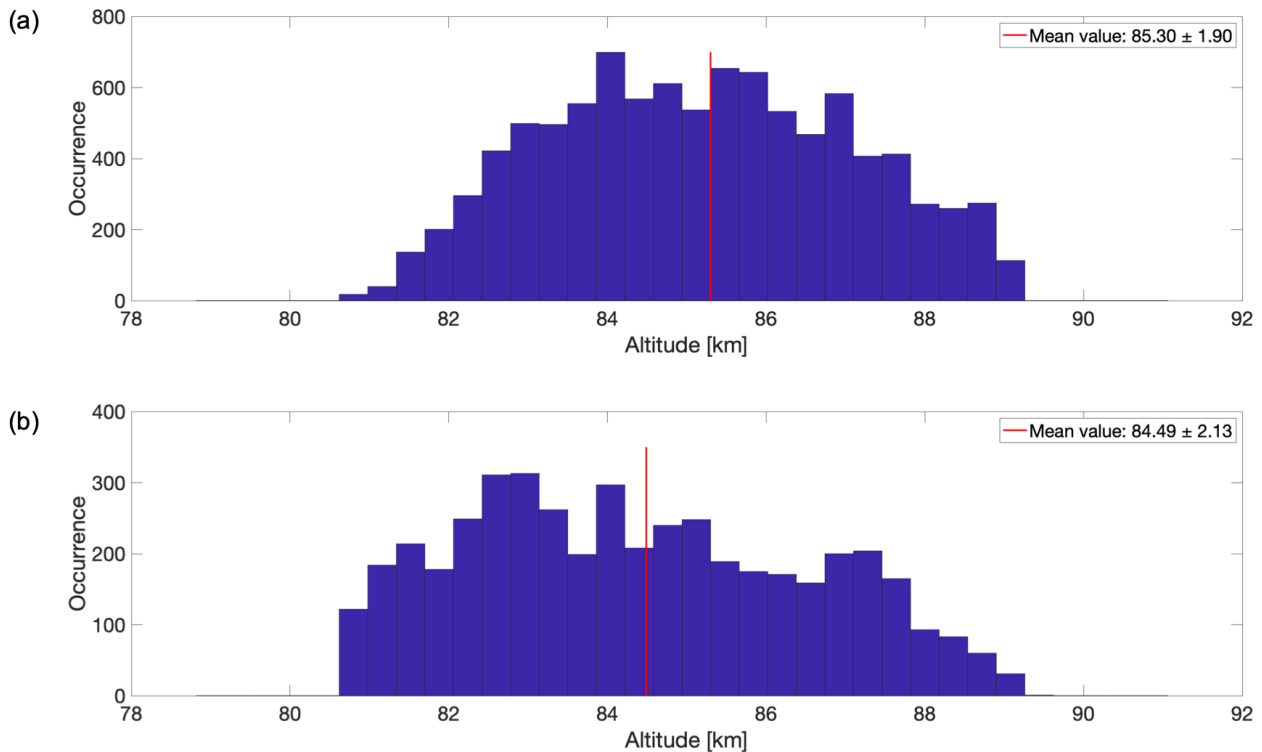
Figure 3. Altitude distribution of the data for the **(a)** solar maximum and **(b)** solar minimum. Each subplot was its respective mean altitude represented with a red line on the graph, and specified in the legend together with one standard deviation.

electrons per cubic meter in base 10 logarithmic unit during solar maximum and their mean value is slightly higher during solar maximum. Specifically, multi-layer PMSEs with 2 layers exhibit the highest average corresponding electron density, reaching 10.47 electrons per cubic meter in base 10 logarithmic unit as one can see from Fig. 7. In contrast, the mono layers during solar minimum have the lowest average corresponding electron density, with a value of 10.15 electrons per cubic meter in base 10 logarithmic unit, as displayed in Fig. 8. It is worth noting that, for both solar maximum and solar minimum periods, the mono layers corresponded to the lowest average electron density of their respective seasons. However, it is important to bear in mind that this trend is weak and that ~~the standard deviations are quite large~~some P-values corresponding to the different combinations of layers in Fig. 7 and Fig. 8 are greater than 0.05, as shown in Table B2. A plausible argument could be made that higher electron densities at ionospheric altitudes might be necessary to observe multi-layered PMSEs.

During solar maximum, we observe a wider range of electron densities compared to solar minimum when PMSE are present, particularly at higher electron densities. This variation in electron densities may explain why the mean electron density at an altitude of 92 km is higher during solar maximum than solar minimum during PMSE events. Additionally, our analysis reveals that the standard deviation of electron densities decreases with increasing number of layers, with mono layers exhibiting
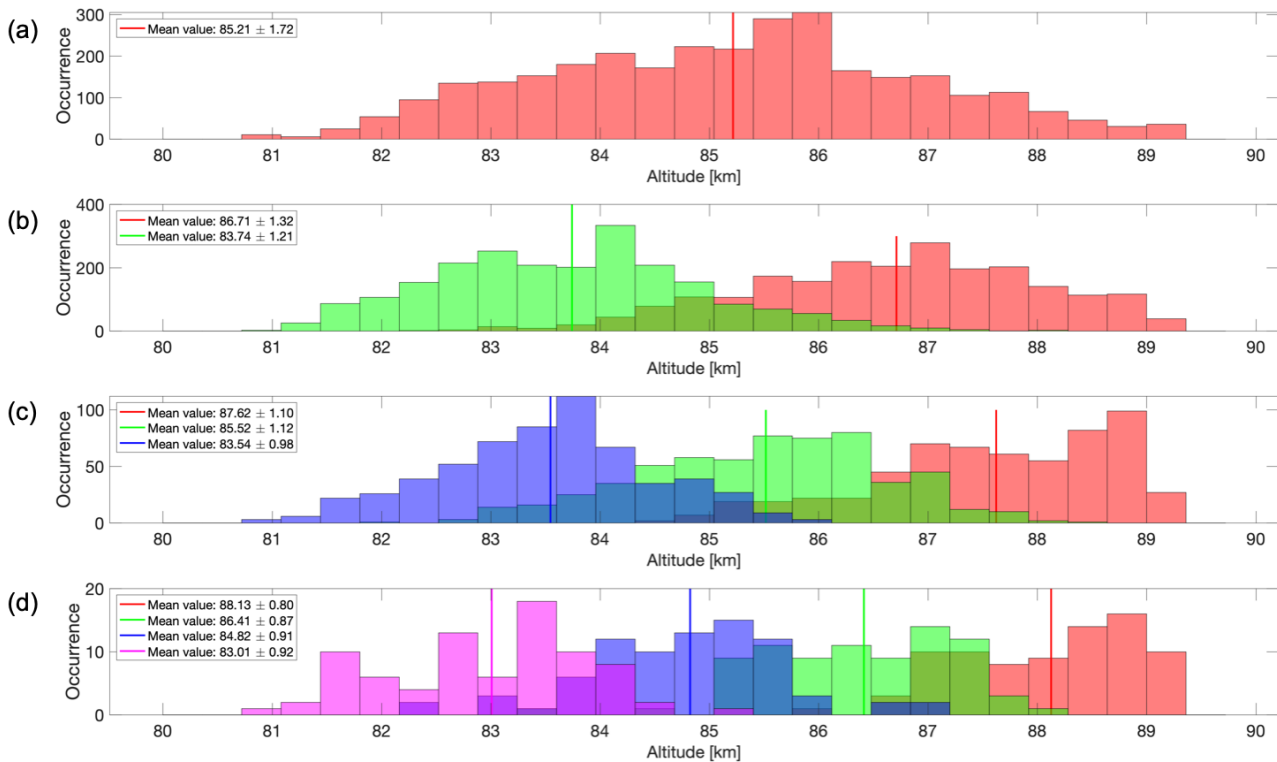
Figure 4. Altitude distribution of the data during solar maximum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. ~~Each subplot was its respective mean~~ In each figure, the color scheme of the distributions indicates altitude ~~represented with a~~ order: red ~~line on~~ for the ~~graph~~highest layer, green for the second highest, blue for the third highest, and ~~specified in~~ magenta for the fourth highest. Intermediate colors represent overlapping altitude distributions. The legend ~~together with~~ displays the mean value and one standard deviation for each distribution.

305   the largest standard deviations and 4-layer systems exhibiting the smallest standard deviations, for both solar maximum and minimum conditions.

3.3   Distribution of the echo power

As discussed in Sect. 2.2 we classified the data using the classification model of Jozwicki et al. (2022) and applied a threshold to identify PMSE. Specifically, we considered all echo power values above a threshold of 10.5 electrons per cubic meter in

310   base 10 logarithmic unit as PMSE. This explains the absence of values below 10.5 on the horizontal axis of Fig. 9, Fig. 10 and Fig. 11. Figures have been generated to visualize individual layers within the various sets of 2, 3, and 4 multi-layers seen in Fig. 10 and Fig. 11. This approach mirrors the technique employed in Fig. 4 and Fig. 5. However, since the separation of layers did not yield additional information, we have chosen to retain the averaged representations of all multi-layers combined, as depicted in Fig. 10 and Fig. 11.
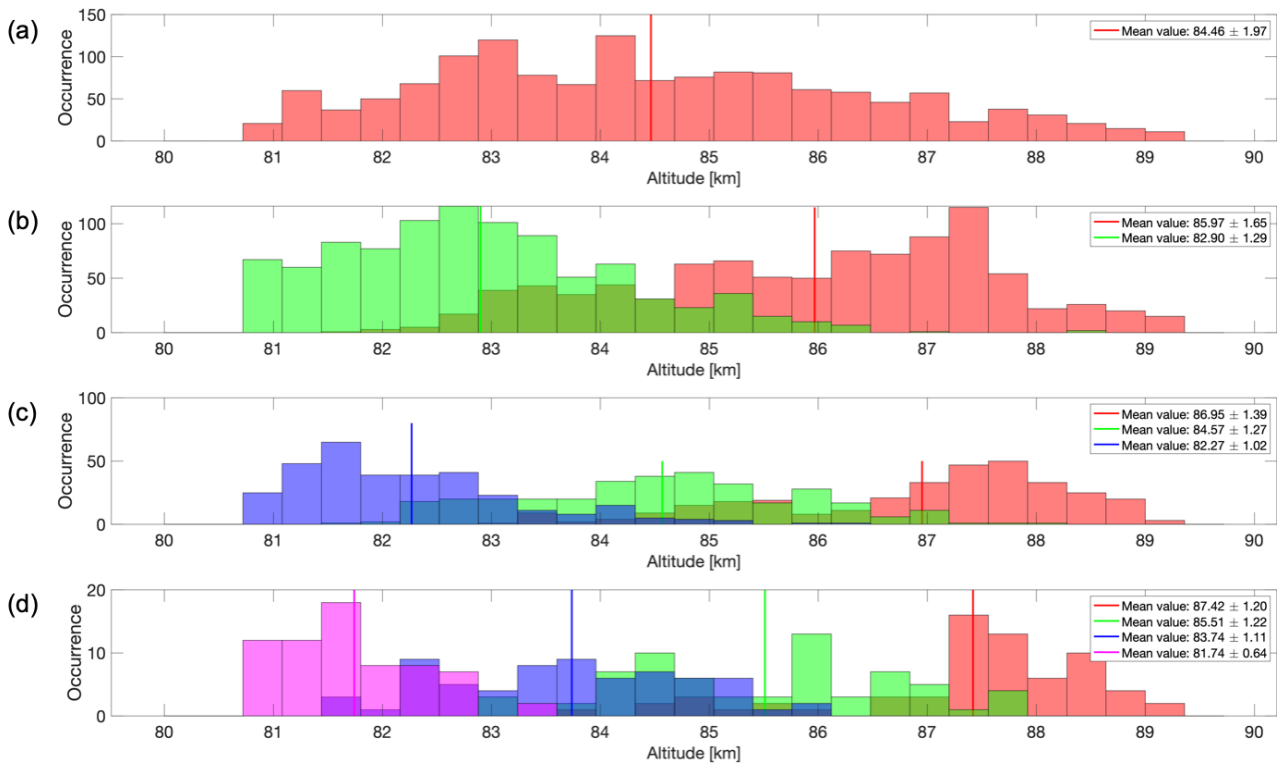
Figure 5. Altitude distribution of the data during solar minimum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. ~~Each subplot was its respective mean~~ In each figure, the color scheme of the distributions indicates altitude ~~represented with a~~ order: red ~~line on~~ for the ~~graph~~highest layer, green for the second highest, blue for the third highest, and ~~specified in~~ magenta for the fourth highest. Intermediate colors represent overlapping altitude distributions. The legend ~~together with~~ displays the mean value and one standard deviation for each distribution.

In Fig. 9, it is evident that the average echo power in PMSE is higher during solar maximum than solar minimum. We noticed a greater distribution of higher values of echo power during solar maximum as compared to solar minimum, which leads to higher mean value during the solar maximum. Further, in Fig. 10, we observe that the average echo power decreases as the number of multi-layers increase for solar maximum and the individual layers considered. This indicates that a single mono-layer has a higher echo power than the individual layers of two multi-layers, which in turn have a higher echo power than the individual layers of three multi-layers, and so on. However, during solar minimum as shown in Fig. 11, this trend is less evident, and we do not see a clear decrease in echo power with increasing number of layers.

3.4 Distribution of the thickness

In our study, we determined the thickness of the PMSE layers based on the number of neighboring data points, or altitude channels exceeding the echo power threshold described in Sect. 2.2. Each data point or altitude channel corresponds to a
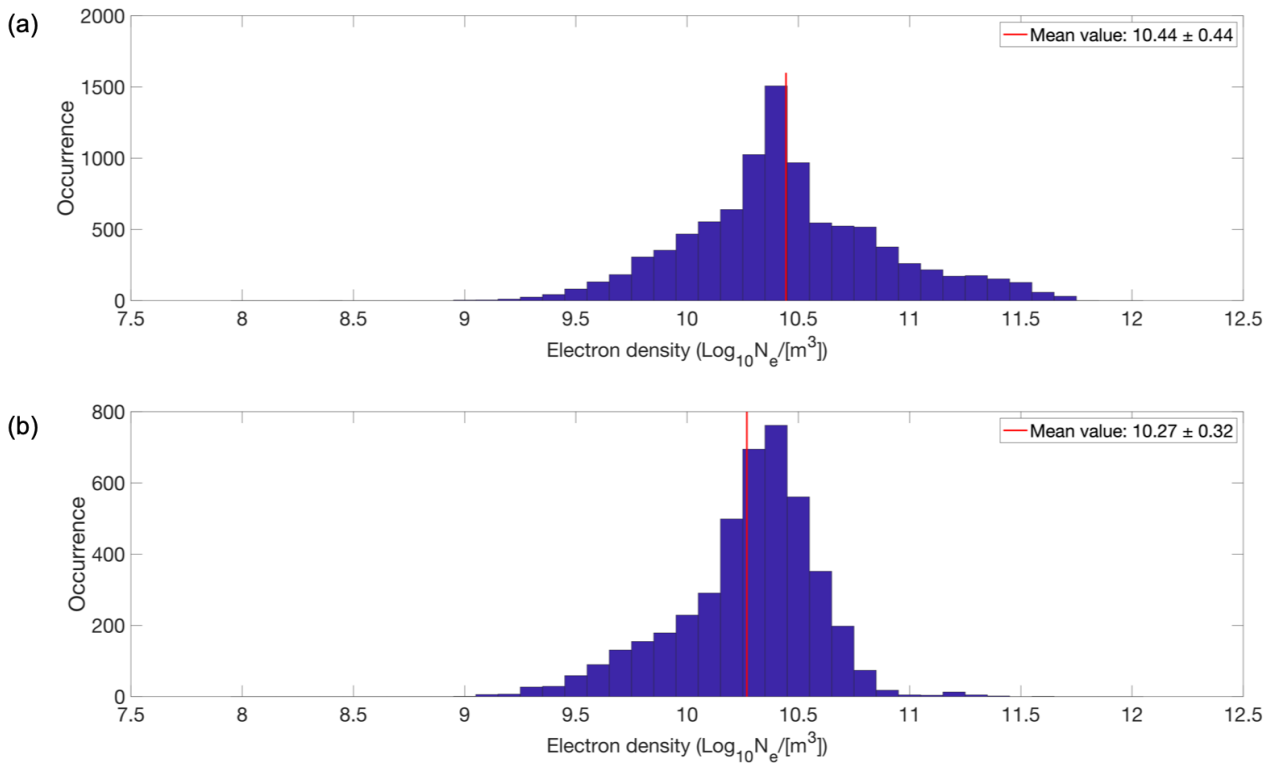
Figure 6. Electron densities at 92 km altitude for all layers during **(a)** solar maximum and **(b)** solar minimum. Each subplot was its respective mean electron density represented with a red line on the graph, and specified in the legend together with one standard deviation.

distance of 360m. As shown in Fig. 12, the average thickness of the layers is higher during solar maximum, with an average of ~~4.42 altitude intervals (1591m)~~1.59 km, compared to solar minimum, where the average thickness is ~~3.67 altitude intervals (1321m)~~1.32 km. When we examine the mono and multi-layer cases in more detail, as shown in Fig. 13 and Fig. 14, we observe that the average thickness decreases as the number of layers increases. This means that a mono-layer will be thicker than a layer belonging to a set of 2 multi-layers, which in turn will be thicker than a layer in a 3 multi-layer case, and so on. Figures have been generated to visualize individual layers within the various sets of 2, 3, and 4 multi-layers seen in Fig. 13 and Fig. 14. This approach mirrors the technique employed in Fig. 4 and Fig. 5. However, since the separation of layers did not yield additional information, we have chosen to retain the averaged representations of all multi-layers combined, as depicted in Fig. 13 and Fig. 14. The highest average layer thickness is obtained during solar maximum for mono-layers with an average of ~~5.98 data points (2153m)~~2.15 km, while the lowest average of ~~2.41 data points (868m)~~0.87 km is obtained during solar minimum, for 4 multi-layers.

A ~~compelling~~ comparison can be drawn between the thickness of NLCs and PMSEs. Although the formation mechanisms of these two phenomena differ, there is a shared population of ice particles that contribute to both. Therefore, it is worthwhile to explore the potential similarities and differences between them. Lübken et al. (2009) found that NLCs have higher brightness
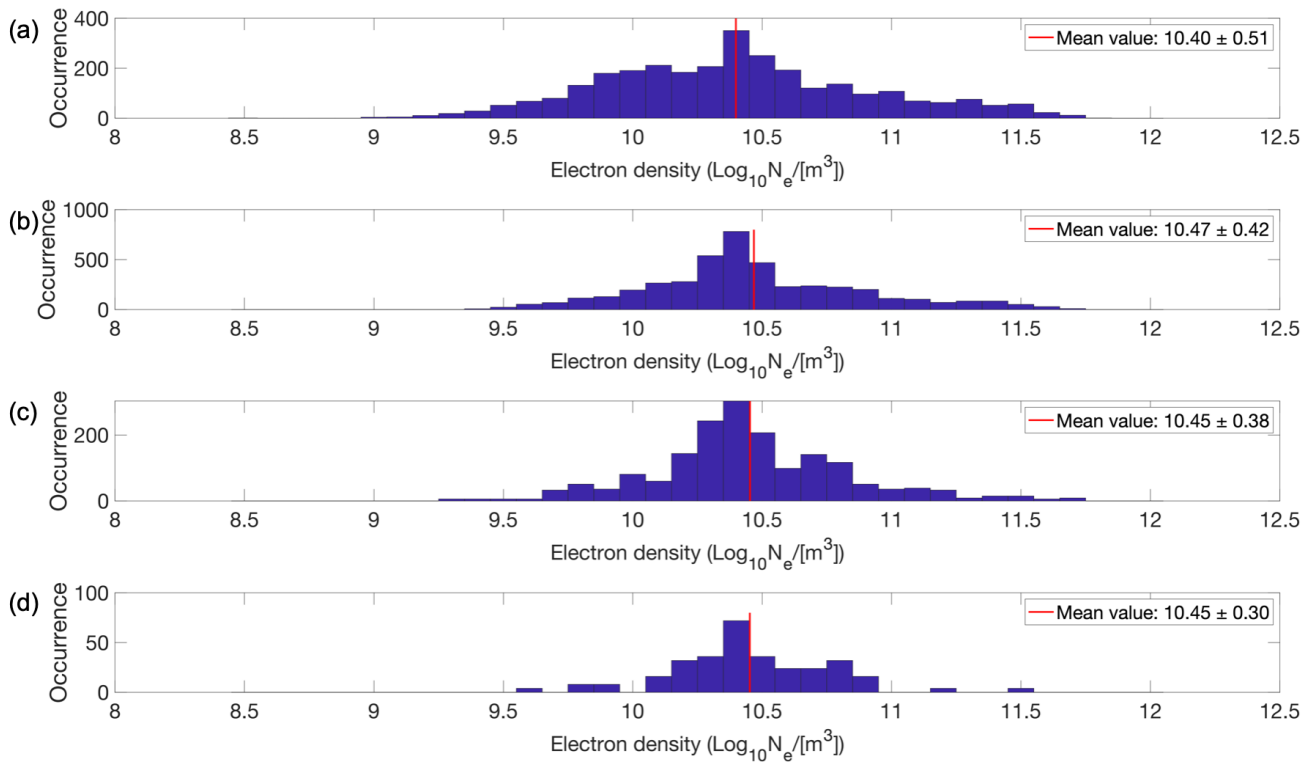
Figure 7. Electron density at 92 km altitude during solar maximum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. Each subplot was its respective mean electron density represented with a red line on the graph, and specified in the legend together with one standard deviation.

at lower altitudes, while Schäfer et al. (2020) analyzed 182 hours of LIDAR data and found that NLCs occur more than half of
340   the time (57.2%), in thick layers of more than 1 km. In our study, we analyzed 7790 instances of PMSEs with 3 or more altitude channels. Knowing that one altitude channel corresponds to 360m, 3 altitude channels or more indicate a PMSE thickness of at least ~~1080m~~1.08 km. Our findings show that 54.64 percent of PMSE occurrences resulted in thick layers of ~~1080m~~1.08 km or more. These results are consistent with those of Schäfer et al. (2020), where they reported that 57.2 percent of NLC occurrences were observed in thick layers of ~~1km~~1 km or more. Additionally, Schäfer et al. (2020) classified the NLCs they
345   observed into 10 subcategories and found that the most frequently occurring subcategory consists of thick layers composed of multiple multi-layers, with an occurrence rate of 20.5%. They report that each of the multi layers move in parallel with each other. This implies that there is a similar movement in the vertical displacement of the multi layers. If we consider all types of multi layers, mentioned by Schäfer et al. (2020), this percentage increases up to 27.6%. In our study, multi layers happen half of the time, with an approximate occurrence rate of 49%. Therefore our results differ from the ones of Schäfer et al. (2020)
350   when it comes to the occurrence rate of multi layers, which may be explained by some of the differences in the formation and measurement of the two phenomena.
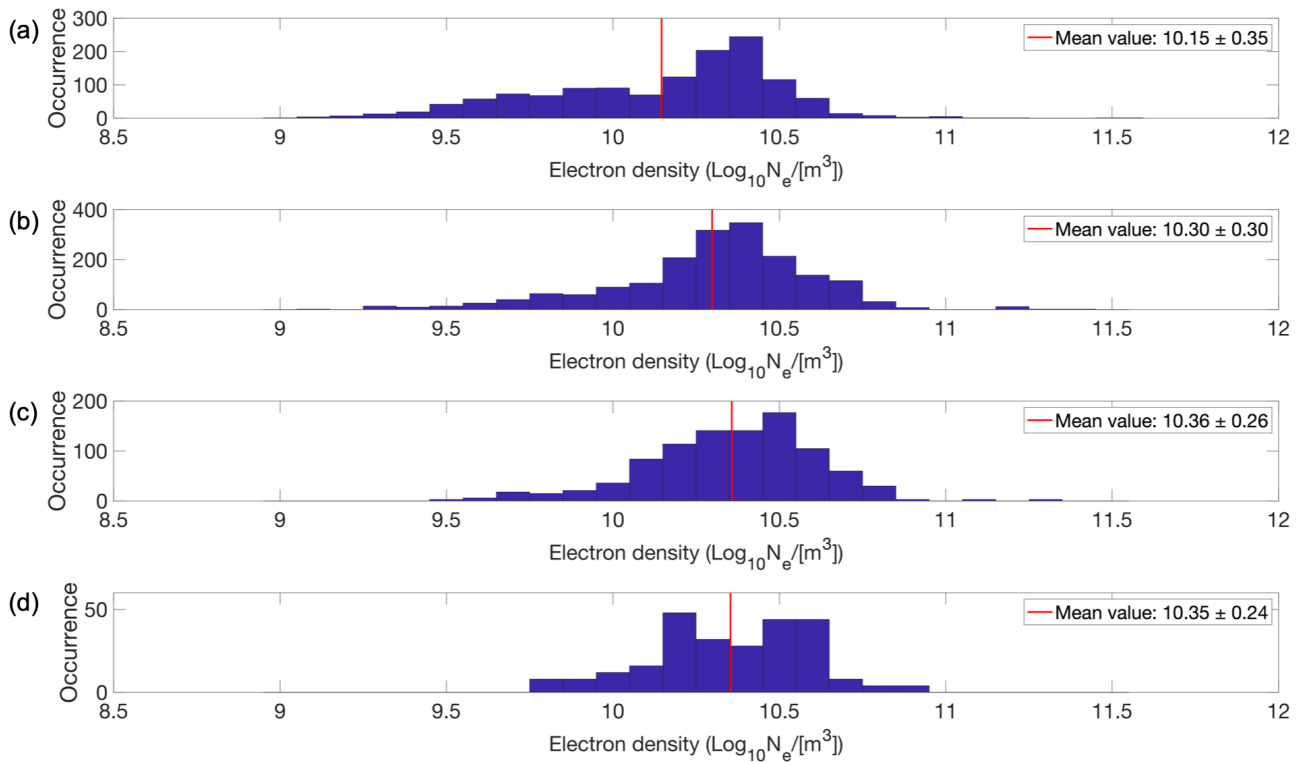
Figure 8. Electron density at 92 km altitude during solar minimum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. Each subplot was its respective mean electron density represented with a red line on the graph, and specified in the legend together with one standard deviation.

Gravity waves are thought to play a ~~significant~~ role in the formation of PMSE by generating neutral turbulence in the mesosphere. The ~~neutral turbulence caused by~~ complex dynamics and structuring because of shear instabilities and breaking of the gravity waves are derived, for example, from polar mesospheric cloud observations, and can generate turbulence at

355   PMSE altitudes, (Fritts et al., 2019). This turbulence can lead to small-scale variations in the electron density, which can create the conditions necessary for PMSE to form, ~~Rapp and Lübken (2004)~~(Rapp and Lübken, 2004). Therefore, understanding the characteristics of gravity waves and their effects on the neutral atmosphere is essential for understanding the formation of PMSE.

Li et al. (2016) developed a ~~2D~~ two-dimensional theoretical model to explore the creation process of multi layered PMSE.

360   The aim of the proposed model was to consider how gravity waves could cause movement of ice particles through collisions with the neutral atmosphere. Their model was able to simulate the presence of gravity waves by assigning both vertical and horizontal wavelengths. The ice particles are considered to be spherical, and their size does not vary during the simulations. This means that processes such as growth, sedimentation or sublimation are not taken into account in ~~this~~ their model. In their first experiment, Li et al. (2016) fixed the particle size at 10 ~~nanometers (nm)~~ nm and varied the vertical wavelength of gravity
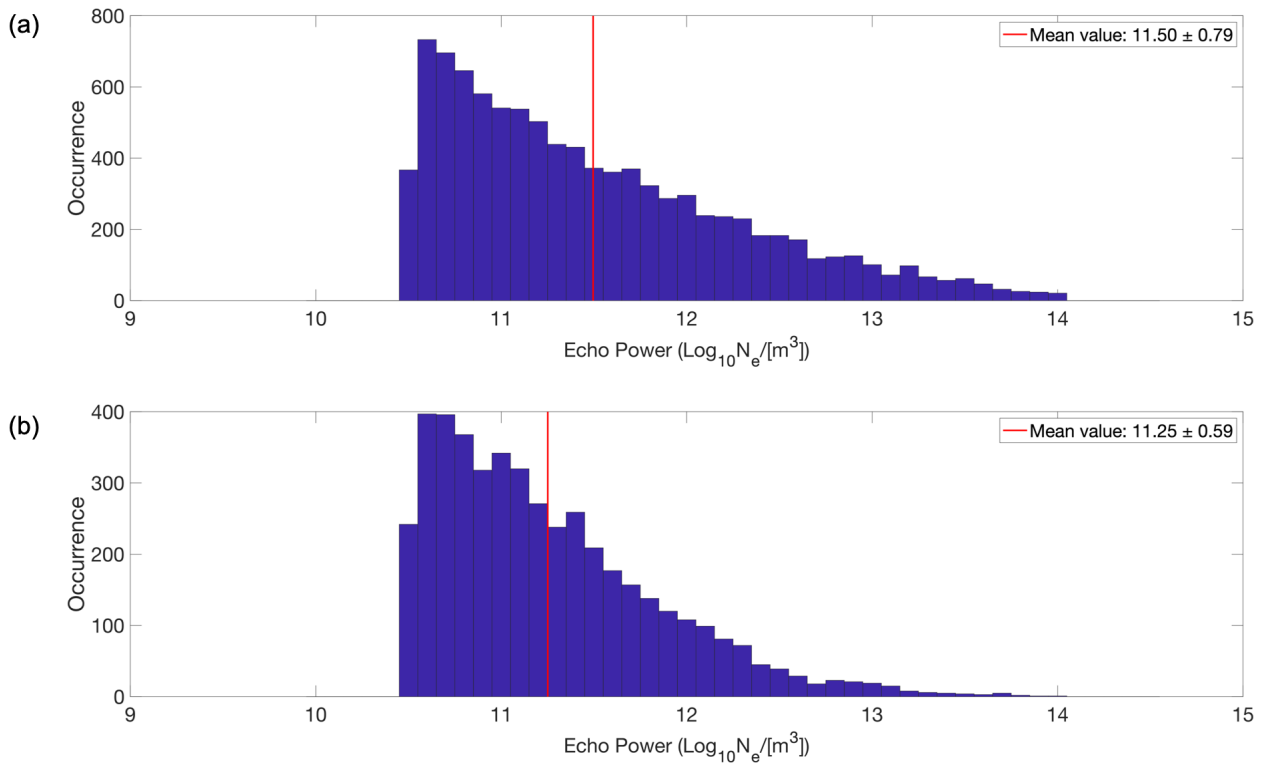
Figure 9. Echo power in the PMSE for all layers during **(a)** solar maximum and **(b)** solar minimum. Each subplot has its respective mean echo power represented with a red line on the graph, and specified in the legend together with one standard deviation.

365   waves to ~~3km, 4km, and 5km~~3 km, 4 km, and 5 km. Only one wavelength was considered at a time, when varying the vertical wavelength. They observed a decrease in the number of layers as the vertical wavelength increased. Also, the thickness of the layers increased as the number of layers decreased. Our results on thickness distribution as shown in Fig. 12, Fig. 13 and Fig. 14 show similar trends. We found that the average thickness of mono layers was higher than that of multi layers, and the thickness decreased with an increasing number of multi layers. One possible hypothesis that can be drawn is that the thickness

370   of the layers could be related to the vertical wavelength of gravity waves, with higher wavelengths producing thicker layers.

~~Li et al. (2016) reported the observation of preferred altitudes for each multi layer formation, which depended on the size of the ice particles. One might expect to observe distinct peaks in the distribution of multi layers for each size range. A plausible hypothesis is that if such peaks are not observed, and instead a more uniform distribution is seen, this could be due to the presence of ice particles of various sizes that create peaks at different altitudes, resulting in a smoothed-out distribution. In~~

375   ~~Fig. A2, which shows the altitude distribution for mono and multi layers during solar minimum, the distributions appear less smooth than those in Fig. A1. This observation could support the hypothesis that the range of size distributions of ice particles is smaller during solar minimum as compared to solar maximum. Potential mechanisms for ice formation at upper mesospheric altitudes that could be affected by the solar cycle are unknown to the authors, but this is something to investigate in a future~~
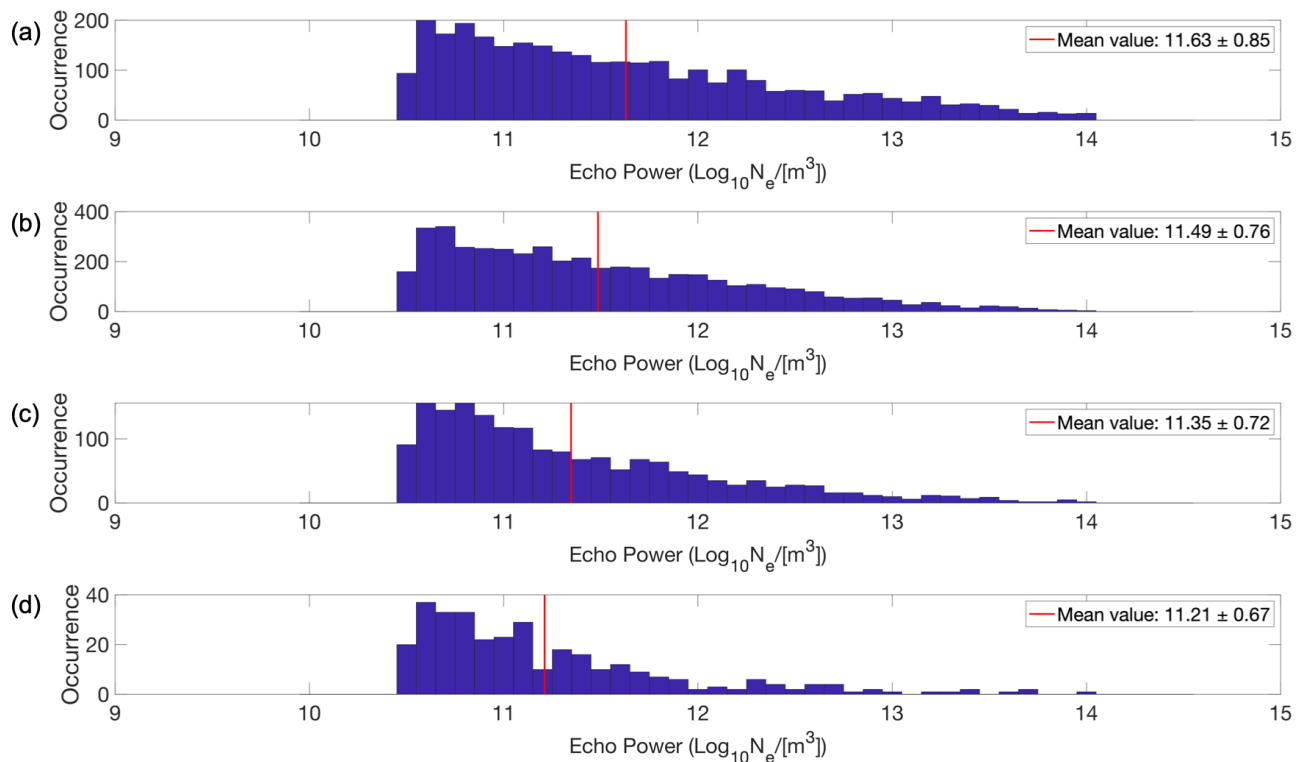
Figure 10. Echo power in the PMSE during solar maximum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. Each subplot has its respective mean echo power represented with a red line on the graph, and specified in the legend together with one standard deviation.

~~study.~~ In another experiment in Li et al. (2016) study investigated the effect of varying ice particle size while fixing the vertical

380 wavelength of gravity waves at 4km. They used particle sizes of ~~10nm, 20nm, and 30nm~~ 10 nm, 20 nm, and 30 nm and found that the altitude of the layers decreased more rapidly and their formation became more challenging with increasing particle size. Also, once the turbulence stopped, the larger ice particles took longer to go back to a neutral homogeneous state. It is worth noting that their model does not consider the growth, sedimentation, and sublimation processes, so these findings should be considered as preliminary hypotheses. Li et al. (2016) also reported the observation of preferred altitudes for each multi

385 layer formation, which depended on the size of the ice particles. Potential mechanisms for ice formation at upper mesospheric altitudes that could be affected by the solar cycle are unknown to the authors, but this is something to investigate in a future study.

~~In their study, Singer et al. (2012) observed the intensification of westward winds below~~ Neutral air turbulence which is a key factor in PMSE formation can be generated by wind shears. Singer et al. (2012) found that westward winds are increasing

390 below an altitude of about 85 km~~and eastward winds~~, while eastward winds are increasing above 85 km~~during the summerseason~~, particularly during summer. They also ~~noted that~~ found that at an altitude of about 75 km, the long-term trend of zonal winds
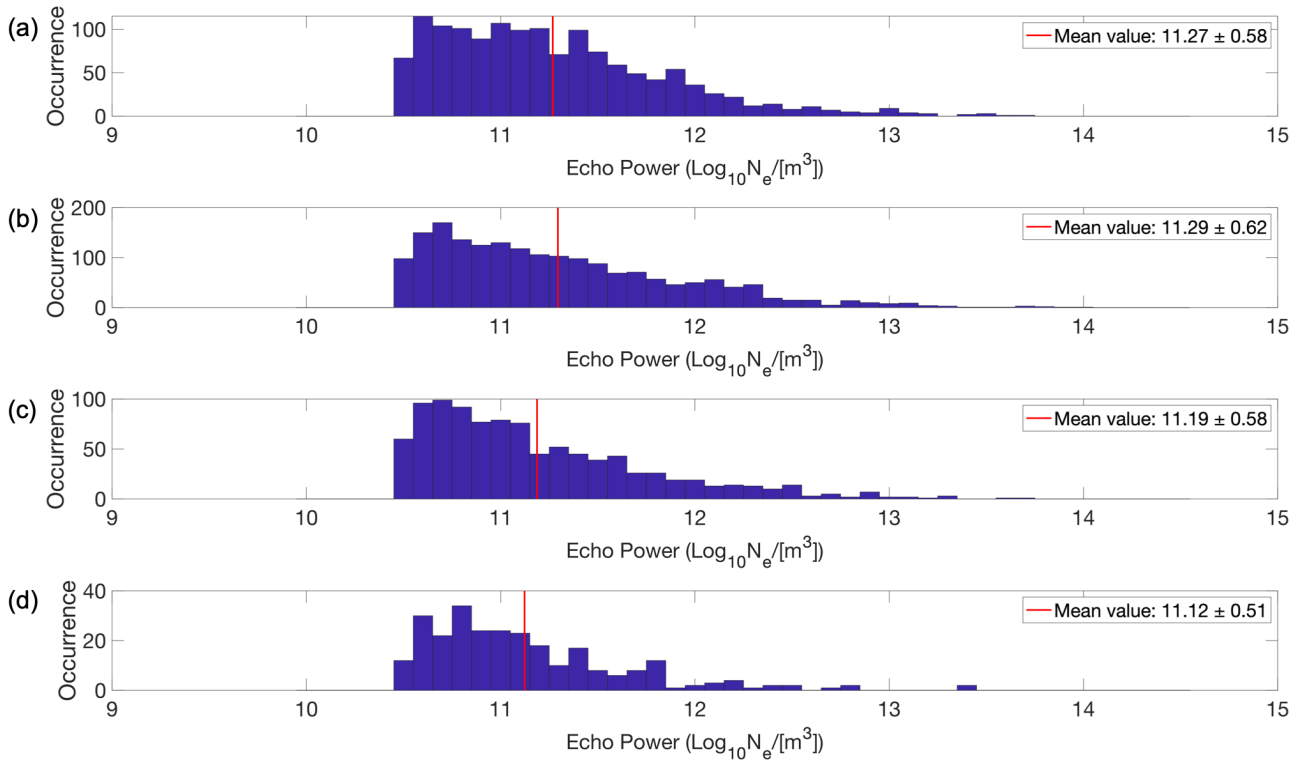
Figure 11. Echo power in the PMSE during solar minimum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. Each subplot has its respective mean echo power represented with a red line on the graph, and specified in the legend together with one standard deviation.

corresponds to increased activity of gravity waves with periods of 3 to 6 hours ~~, at altitudes~~ between 80 km and 88 km~~, are more active at an altitude of about 75 km. Additionally, they found that severe~~ . Severe solar proton events ~~result in an increase in eastward winds above~~ cause eastward winds to increase above an altitude of about 85 km. ~~These wind and gravity wave~~

395   ~~behaviors~~ This behavior of winds and their effects at PMSE altitudes ~~might be the key factors in understanding the turbulence leading to~~ may be another key to a better understanding of the formation of multi-layered PMSE~~formation~~.

3.5 Correlations

In this section, we will analyze the correlation between several parameters, namely electron density, echo power, thickness, and altitude. Table 4 shows both correlation coefficients for all layers together, for the solar maximum on the lower portion of

400   the table, and for the solar minimum on the upper portion of the table. Table 5(a) shows the results of the Pearson correlation coefficient only, for mono and multi layers separately, and for solar maximum and minimum. Table 5(b) shows the results of the Spearman's rank correlation coefficient only, for mono and multi layers separately, and for solar maximum and minimum. For simplicity, in all the mentioned above tables, the notation "r_p" is chosen to represent Pearson correlation coefficients, and
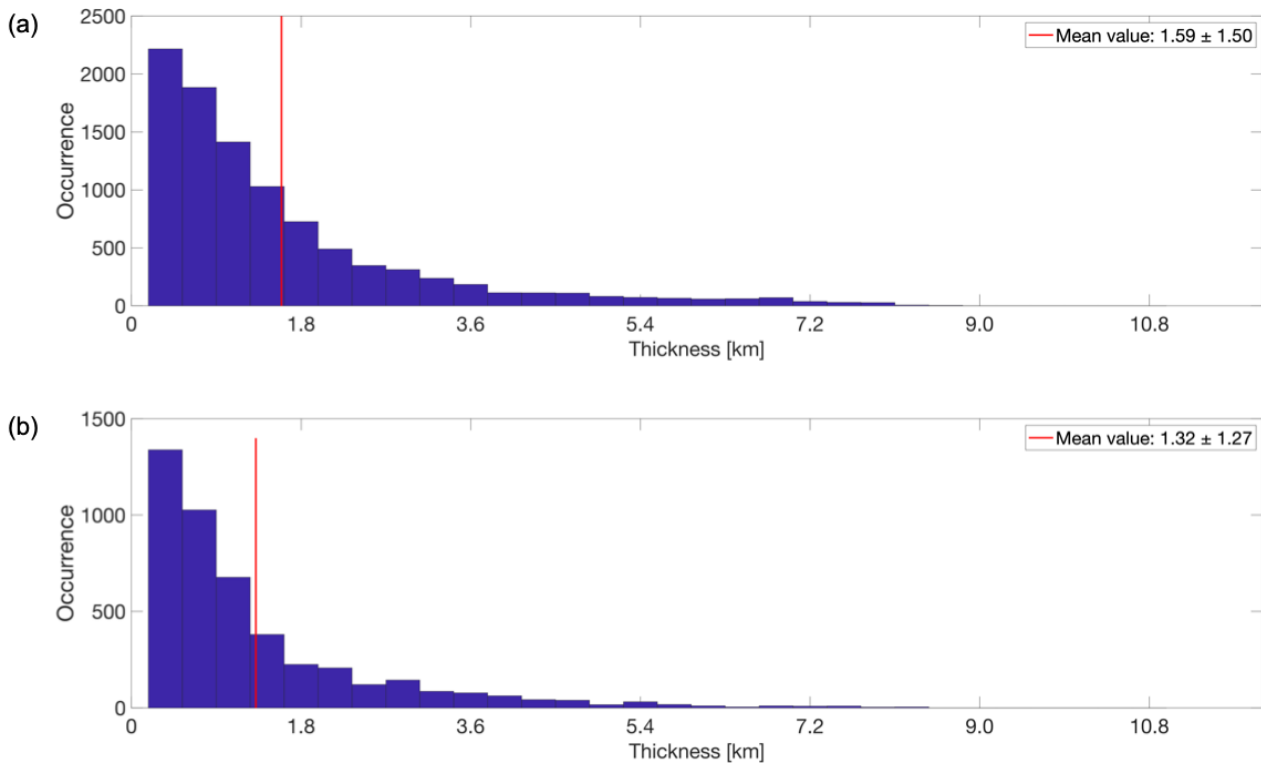
Figure 12. Thickness distribution of the layers for all layers combined during **(a)** solar maximum and **(b)** solar minimum. Each subplot was its respective mean thickness represented with a red line on the graph, and specified in the legend together with one standard deviation.

the notation "r_s" is chosen to represent Spearman's rank correlation coefficients. In Tables 5(a) and 5(b), the notations "r_{p1}",
405 "r_{p2}", "r_{p3}" and "r_{p4}" denote the Pearson correlation coefficients for mono layers, double layers, triple layers, and quadruple layers respectively. In a similar manner, the Spearman's rank correlation coefficient notations are "r_{s1}", "r_{s2}", "r_{s3}" and "r_{s4}".

In Table 4, it is observed that the electron density at 92 km altitude and the echo power are positively correlated with the thickness of all the layers for both solar maximum and solar minimum. This is also the case for Tables 5(a), and 5(b). During solar maximum, the positive correlation between electron density and thickness is greater than during solar minimum, but
410 this is not observed between echo power and thickness. In Tables 4, the Pearson correlation coefficient of 0.480 for solar maximum suggests a moderate positive linear relationship between electron density and thickness, while the Spearman's rank correlation coefficient of 0.392 indicates a moderate positive monotonic relationship between the variables for the same case. Since the two values are similar, it suggests that during solar maximum there is a consistent association between electron density and thickness. In Tables 5(a), and 5(b), we observe that the Pearson correlation coefficient and Spearman's rank correlation
415 coefficient between electron density and thickness decrease as the number of multi layers increases. Specifically, in both cases the highest correlation is observed for solar maximum and mono layers, with a Pearson coefficient of 0.695 and a Spearman's rank coefficient of 0.668. This could possibly indicate that at higher ionization levels at this altitude, the PMSE mono layers
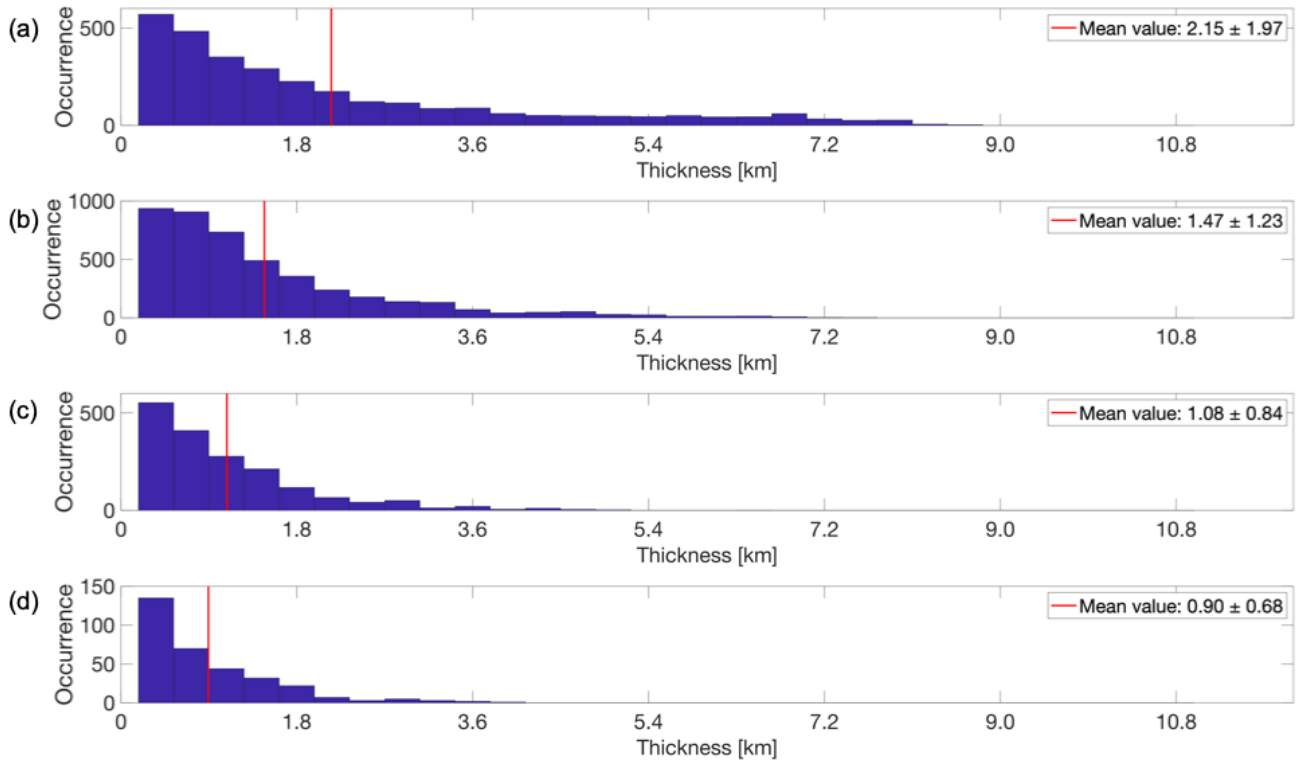
Figure 13. Thickness distribution during solar maximum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. Each subplot was its respective mean thickness represented with a red line on the graph, and specified in the legend together with one standard deviation.

Table 4. Pearson and Spearman's rank correlation coefficients for all layers together, for solar maximum and solar minimum.

<table>
<tr><td colspan="2" rowspan="2"></td><td colspan="4">Solar minimum</td></tr>
<tr><td>Electron density</td><td>Echo power</td><td>Thickness</td><td>Altitude</td></tr>
<tr><td rowspan="8">Solar maximum</td><td rowspan="2">Electron density</td><td rowspan="2"></td><td>$r_p = 0.213$</td><td>$r_p = 0.251$</td><td>$r_p = -0.079$</td></tr>
<tr><td>$r_s = 0.163$</td><td>$r_s = 0.232$</td><td>$r_s = -0.058$</td></tr>
<tr><td rowspan="2">Echo power</td><td>$r_p = 0.338$</td><td rowspan="2"></td><td>$r_p = 0.521$</td><td>$r_p = -0.165$</td></tr>
<tr><td>$r_s = 0.305$</td><td>$r_s = 0.631$</td><td>$r_s = -0.162$</td></tr>
<tr><td rowspan="2">Thickness</td><td>$r_p = 0.480$</td><td>$r_p = 0.510$</td><td rowspan="2"></td><td>$r_p = -0.153$</td></tr>
<tr><td>$r_s = 0.392$</td><td>$r_s = 0.631$</td><td>$r_s = -0.169$</td></tr>
<tr><td rowspan="2">Altitude</td><td>$r_p = 0.011$</td><td>$r_p = -0.034$</td><td>$r_p = 0.039$</td><td rowspan="2"></td></tr>
<tr><td>$r_s = 0.003$</td><td>$r_s = -0.031$</td><td>$r_s = 0.024$</td></tr>
</table>

Table 5. (a) Pearson correlation coefficients for mono and multi layers separately, for solar maximum and solar minimum. **(b)** Spearman's rank correlation coefficients for mono and multi layers separately, for solar maximum and solar minimum.

(a)		Solar minimum			
		Electron density	Echo power	Thickness	Altitude
Solar maximum	Electron density		$r_{p1} = 0.270$ $r_{p2} = 0.247$ $r_{p3} = 0.163$ $r_{p4} = 0.199$	$r_{p1} = 0.376$ $r_{p2} = 0.273$ $r_{p3} = 0.226$ $r_{p4} = 0.168$	$r_{p1} = -0.339$ $r_{p2} = 0.010$ $r_{p3} = 0.048$ $r_{p4} = 0.054$
	Echo power	$r_{p1} = 0.501$ $r_{p2} = 0.259$ $r_{p3} = 0.224$ $r_{p4} = 0.306$		$r_{p1} = 0.455$ $r_{p2} = 0.574$ $r_{p3} = 0.608$ $r_{p4} = 0.514$	$r_{p1} = -0.071$ $r_{p2} = -0.186$ $r_{p3} = -0.228$ $r_{p4} = -0.210$
	Thickness	$r_{p1} = 0.695$ $r_{p2} = 0.393$ $r_{p3} = 0.246$ $r_{p4} = 0.264$	$r_{p1} = 0.534$ $r_{p2} = 0.482$ $r_{p3} = 0.508$ $r_{p4} = 0.541$		$r_{p1} = -0.110$ $r_{p2} = -0.199$ $r_{p3} = -0.167$ $r_{p4} = -0.161$
	Altitude	$r_{p1} = 0.091$ $r_{p2} = -0.079$ $r_{p3} = -0.046$ $r_{p4} = 0.030$	$r_{p1} = 0.087$ $r_{p2} = -0.052$ $r_{p3} = -0.118$ $r_{p4} = -0.184$	$r_{p1} = 0.131$ $r_{p2} = 0.031$ $r_{p3} = -0.040$ $r_{p4} = -0.113$	

(b)		Solar minimum			
		Electron density	Echo power	Thickness	Altitude
Solar maximum	Electron density		$r_{s1} = 0.245$ $r_{s2} = 0.179$ $r_{s3} = 0.178$ $r_{s4} = 0.123$	$r_{s1} = 0.428$ $r_{s2} = 0.215$ $r_{s3} = 0.178$ $r_{s4} = 0.173$	$r_{s1} = -0.292$ $r_{s2} = 0.006$ $r_{s3} = 0.045$ $r_{s4} = 0.047$
	Echo power	$r_{s1} = 0.494$ $r_{s2} = 0.239$ $r_{s3} = 0.202$ $r_{s4} = 0.232$		$r_{s1} = 0.603$ $r_{s2} = 0.643$ $r_{s3} = 0.635$ $r_{s4} = 0.542$	$r_{s1} = -0.047$ $r_{s2} = -0.188$ $r_{s3} = -0.240$ $r_{s4} = -0.208$
	Thickness	$r_{s1} = 0.668$ $r_{s2} = 0.311$ $r_{s3} = 0.202$ $r_{s4} = 0.230$	$r_{s1} = 0.615$ $r_{s2} = 0.621$ $r_{s3} = 0.637$ $r_{s4} = 0.595$		$r_{s1} = -0.168$ $r_{s2} = -0.185$ $r_{s3} = -0.141$ $r_{s4} = -0.124$
	Altitude	$r_{s1} = 0.095$ $r_{s2} = -0.052$ $r_{s3} = -0.031$ $r_{s4} = 0.058$	$r_{s1} = 0.111$ $r_{s2} = -0.051$ $r_{s3} = -0.107$ $r_{s4} = -0.190$	$r_{s1} = 0.161$ $r_{s2} = 0.008$ $r_{s3} = -0.052$ $r_{s4} = -0.076$	
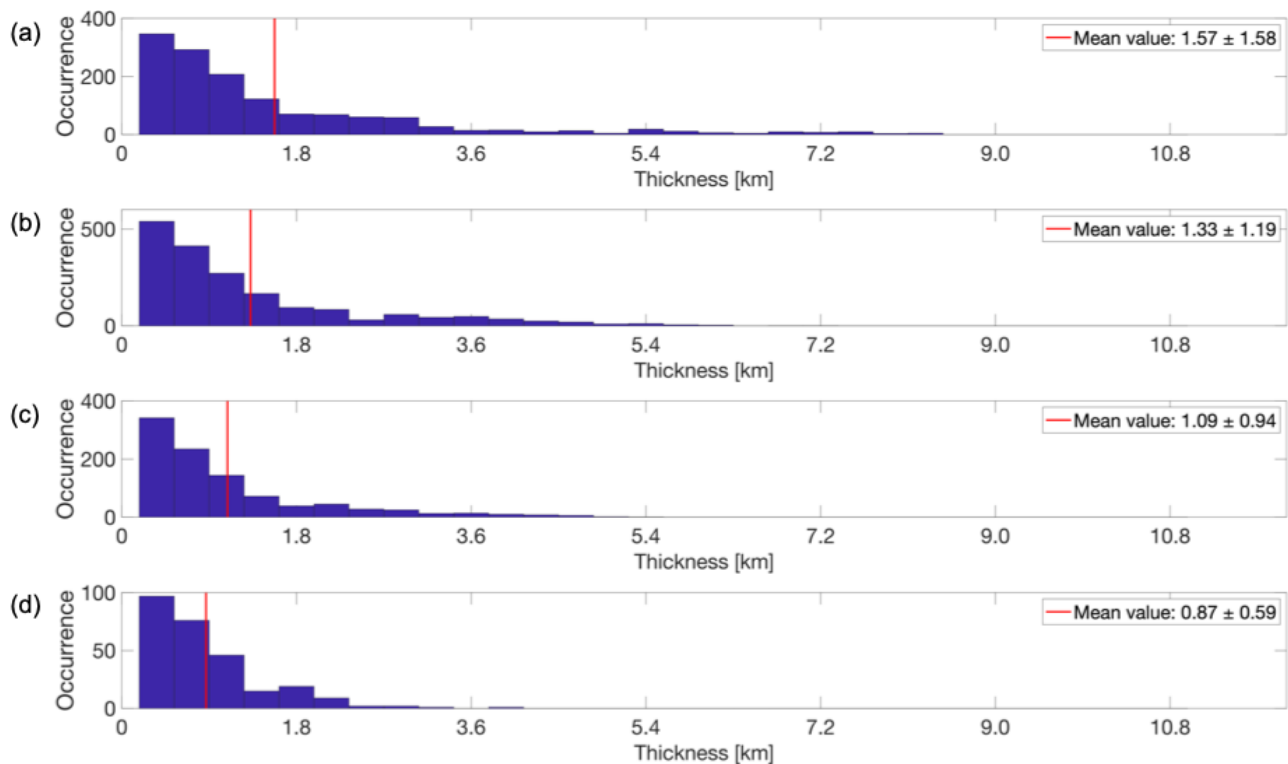
Figure 14. Thickness distribution during solar minimum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. Each subplot was its respective mean thickness represented with a red line on the graph, and specified in the legend together with one standard deviation.

are thicker. Conversely, the lowest correlations were obtained for solar minimum and the largest number of multi layers, which is 4, with a Pearson coefficient of 0.168 and a Spearman's rank coefficient of 0.173.

420   From Tables 4, 5(a), and 5(b) we notice a weak negative correlation between the echo power in the PMSE and altitude for all layers during both solar maximum and solar minimum. The strongest negative correlation is found for 3 multi layers, with a Pearson coefficient of -0.228 and a Spearman's rank coefficient of -0.240. Notably, altitude appears to be uncorrelated with the other variables, implying that additional factors may be influencing the formation of PMSE at specific altitudes. For example, this could be attributed to mesopause conditions, gravity wave wavelength and ice particle size.

425   From Tables 4, 5(a), and 5(b) we notice overall the positive correlation between the electron density at 92 km altitude and the echo power in the PMSE for all the layers and for both solar maximum and solar minimum. For Tables 5(a) and 5(b), we note that the highest Pearson correlation coefficient and Spearman's rank correlation coefficient are obtained for mono layers. Specifically for solar maximum, the Pearson coefficient is 0.501 and the Spearman's rank coefficient is 0.494, while for solar minimum, the Pearson coefficient is 0.270 and the Spearman's rank coefficient is 0.245. These results can possibly suggest that

430   at higher ionization levels at 92 km altitude, the PMSE have a higher intensity, indicated by a higher echo power, particularly

in the case of mono layers during solar maximum. On the other hand, the lowest correlations were found for multi layers containing three layers, with a Pearson coefficient of 0.224 and a Spearman's rank coefficient of 0.202 for solar maximum and a Pearson coefficient of 0.306 and a Spearman's rank coefficient of 0.232 for solar minimum.

~~In their study, Narayanan et al. (2022) found that there was~~ Narayanan et al. (2022) investigated the effects of particle precipitation on PMSE formation using electron densities from 90 to 95 km. They found a clear response in the power of the PMSE echoes during particle precipitation events: in all their cases, an increase in PMSE power was observed in association with particle precipitations. However, Narayanan et al. (2022) say that the particle precipitation does not seem to be related to the very existence of PMSE, and that there seem to be no linear relationship between both, which is consistent with the results of our study. Specifically, we observe weak Pearson correlation coefficients during the solar minimum, as reported in Table 5(a), consistent with the findings of Narayanan et al. (2022) who analyzed EISCAT VHF observations from 2019, a period corresponding to the solar minimum. However, our results indicate slightly higher Pearson correlation coefficients during solar maximum, particularly for mono layers. It would be worthwhile to conduct a similar investigation as Narayanan et al. (2022) during the solar maximum phase of a solar cycle. These findings should be interpreted with care, considering that our study differs from that of Narayanan et al. (2022) in several ways. Specifically, our data selection process did not require the simultaneous presence of PMSE and particle precipitation.

From Table 4, one can notice that for the combination of echo power and electron density during solar maximum, the obtained Pearson correlation coefficient is 0.338 and the Spearman's rank correlation coefficient is 0.305. In their study, Rauf et al. (2018a) used EISCAT VHF data to investigate the correlation between PMSE strength and particle precipitation, over a dataset of 111 hours, or 5 days of observation. However in their case, they derived the Pearson and Spearman correlation coefficients between their PMSE proxy which is equivalent to our use of the term "echo power", and the electron density at 90 km altitude instead of 92 km for us. Nevertheless, it is interesting to note that they also found a positive correlation between echo power and electron density with 0.15 for the Pearson correlation coefficient, and 0.24 for the Spearman correlation coefficient. It is important to note that during their analysis, Rauf et al. (2018a) only selected data from 8 to 12 July 2013, when PMSE and particle precipitation were occurring simultaneously. ~~The year 2013 is included in our study in the solar maximum data, therefore we compare Rauf et al. (2018a) correlation coefficients with our correlation coefficients for solar maximum.~~ In our study, we included data from the year 2013 in the solar maximum period. Hence, we compare the correlation coefficients from Rauf et al. (2018a) with our own coefficients for the solar maximum. While both studies discovered a positive correlation, our findings had higher correlation coefficients than Rauf et al. (2018a) study. One factor which could explain this difference might be the fact that in Rauf et al. (2018a) data, PMSE and particle precipitation was always occurring simultaneously, while in our analysis, data was selected solely based on the presence of PMSE, without any filtering based on the occurrence of particle precipitation. It should be noted that while PMSE was present in all of our cases, there may have been instances where particle precipitation was present and instances where it was not. Another factor might be that we used a lower threshold for PMSE detection than Rauf et al. (2018a), due to the fact that we used a classification model on the data before hand. We used the threshold $N_e > 3.2 \times 10^{10} m^{-3}$ while Rauf et al. (2018a) used $N_e > 4.6 \times 10^{11} m^{-3}$.

4 Conclusions

The ~~results from our study indicate that the~~ altitude, the echo power and the thickness of layers in PMSE have on average higher values during solar maximum than during solar minimum. ~~As~~ During the PMSE occurrence, as expected, the electron density at 92 km is on average higher during solar maximum than solar minimum. ~~Based on our investigation, we have found that the electron density at 92 km altitude and the echo power are positively correlated with the thickness for all the layers and for both solar maximum and solar minimum. The echo power and electron density are positively correlated, especially for mono layers and solar maximum. This can possibly suggest that under those conditions and at higher ionization levels at 92 km altitude, the PMSE are stronger, indicated by a higher echo power. For~~ Taking into account the findings presented by Lübken et al. (2021) that show an increase in ice particle size over time in conjunction with these results, it is difficult to isolate the exact mechanisms by which the PMSE properties are affected. None the less, breaking down the multilayer sets into individual layers reveals a consistent trend: in both solar maximum and solar minimum ~~periods, the mono layers attained the lowest average electron density of their respective seasons, though the trend was relatively weak. A plausible argument could be made that higher electron densities at ionospheric altitudes might be necessary to generate multi-layered PMSEs. The electron density was also highly correlated with the thickness of~~ cases, the altitude of the ~~layers especially for solar maximum and mono layers, which indicates that at higher ionization levels at 92km altitude, the PMSE mono layers are commonly thicker.~~ top layer tends to rise with an increasing number of multilayers. This tendency extends to the second and third highest layers as well. Our findings support the conclusions drawn by Hoffmann et al. (2005) regarding the altitude and occurrence rate of both mono and multiple layers. Additionally, when examining the lowest layer in various multilayer sets, the lowest layer almost always aligns with the NLC altitude as reported by Fiedler et al. (2003) of 83.3 km.

~~The echo power was found to decrease with increasing multi layers, but only in the case of solar maximum. Furthermore, we~~ We have observed that the thickness of the layers decreases as the number of multi-layers increases, indicating that a single mono-layer will be thicker than the separate layers of a set of two multi-layers, which in turn will be thicker than the separate layers of three multi-layers, and so on. This is mostly the case for layers one to three and for both solar maximum and solar minimum. Furthermore, the echo power was found to decrease with increasing multi layers, but only in the case of solar maximum, and mostly for layers one to three. This suggests that there may be a relationship between the number of layers, echo power, and thickness. Our study is consistent with the findings of ~~Li et al. (2016)~~ Li et al. (2016) where they found that the thickness of multi layers decreases with increasing number of ~~multi layers~~ multilayers.

Based on our investigation, we have found that the electron density at 92 km altitude and the echo power are positively correlated with the thickness for all the layers and for both solar maximum and solar minimum, except for four multi layers at solar minimum. We also found similar results as Rauf et al. (2018a), discovering a positive correlation between electron density and echo power, especially for mono layers and during solar maximum. This can possibly suggest that under those conditions and at higher ionization levels at 92 km altitude, the PMSE are stronger, indicated by a higher echo power. The electron density was highly correlated with the thickness of the layers, except for solar minimum and 4 multilayers. The correlation is the strongest especially for solar maximum and mono layers, which indicates that at higher ionization levels at 92km altitude, the

PMSE mono layers are commonly thicker. Comparing our results with ~~Li et al. (2016)~~ Li et al. (2016) led us to hypothesize that the thickness of the layers could be related to the vertical wavelength of gravity waves, with larger wavelengths producing thicker layers. Further investigations could explore this hypothesis, potentially providing a means to infer the wavelength of gravity waves through PMSE observations at these altitudes.

~~Our study is consistent with previous research from Hoffmann et al. (2005) regarding the altitude of the observed mono layers and the occurence rate of PMSE mono and multi layers . We also found similar results as Rauf et al. (2018a), discovering a positive correlation between electron density and echo power. Taking into account the findings presented by Lübken et al. (2021) that show an increase in ice particle size over time, and in conjunction with our own results, it is possible to hypothesize that factors other than the sole influence from the solar cycle might play a significant role in the altitude of PMSEs. An interesting parallel could~~ For both solar maximum and solar minimum periods, the mono layers attained the lowest average electron density of their respective seasons, though the trend was relatively weak. An argument could be made that higher electron densities at ionospheric altitudes might be necessary to generate multi-layered PMSEs, though this requires more investigation.

A parallel can be drawn with the findings of ~~Schäfer et al. (2020)~~ Schäfer et al. (2020) regarding multi layered NLC, where both our studies found a similar occurrence rate for thick layer formation above 1 km thickness. In light of the similarities in multi-layer formation between PMSE and NLC, future studies may be able to utilize findings from NLC research to gain insights into PMSE dynamics.

~~The altitude region where PMSE form is a site of significant activity and dynamics. As we discussed in the previous section, other factors besides the sole influence of the solar cycle play an important role in multi-layer PMSE formation. Singer et al. (2012) study highlights the significant activity that occurs within the PMSE height range. As a suggestion for future research, it would be worth investigating the connections between multi-layered PMSE formation and winds and gravity waves rather than solely focusing on the solar cycle.~~

In conclusion, the mechanism of the formation PMSE might be presently well understood, however the exact conditions leading to multi-layered PMSE formation remains unclear, and further investigation is required. For example, future research should include further investigating the connections between multi-layered PMSE formation and winds and gravity waves. Understanding the complex interplay of the factors involving the formation of PMSE is crucial to gain insights into the thermodynamic and fluid dynamic processes occurring at altitudes between 80 to 90 km. ~~We have provided evidence of PMSE properties being potentially related to gravity wave vertical wavelength, ice particle size, and electron density~~ While differences between the results from observations during solar maximum and during solar minimum considering all the layers together are statistically significant, the cause for the differences needs to be confirmed by future studies.

Data availability. EISCAT VHF data are available under https://madrigal.eiscat.se/madrigal/ (accessed on 15 January 2023).

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Competing interests. The authors declare no conflict of interest. The funders had no role in the design of the study; in the collection, analyses, or interpretation of data; in the writing of the manuscript, or in the decision to publish the results.

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Appendix A: Figures

Appendix B: Tables

Table B1. P-values for all combinations of layers shown in Fig. 4 and Fig. 5.

P-Values		Solar Minimum									
		Mono Layers	Layers 1 of 2	Layers 2 of 2	Layers 1 of 3	Layers 2 of 3	Layers 3 of 3	Layers 1 of 4	Layers 2 of 4	Layers 3 of 4	Layers 4 of 4
Solar Maximum	Mono Layers		P <0.0001	P <0.0001	P <0.0001	0.3618	P <0.0001	P <0.0001	P <0.0001	0.0027	P <0.0001
	Layers 1 of 2	P <0.0001		P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	0.0268	P <0.0001	P <0.0001
	Layers 2 of 2	P <0.0001	P <0.0001		P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001
	Layers 1 of 3	P <0.0001	P <0.0001	P <0.0001		P <0.0001	P <0.0001	0.0106	P <0.0001	P <0.0001	P <0.0001
	Layers 2 of 3	P <0.0001	P <0.0001	P <0.0001	P <0.0001		P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001
	Layers 3 of 3	P <0.0001	P <0.0001	0.0002	P <0.0001	P <0.0001		P <0.0001	P <0.0001	P <0.0001	0.0001
	Layers 1 of 4	P <0.0001	P <0.0001	P <0.0001	0.0001	P <0.0001	P <0.0001		P <0.0001	P <0.0001	P <0.0001
	Layers 2 of 4	P <0.0001	0.0448	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001		P <0.0001	P <0.0001
	Layers 3 of 4	0.0411	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001		P <0.0001
	Layers 4 of 4	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	P <0.0001	

Table B2. P-values for all combinations of layers and parameters shown in Fig. 3, Fig. A1, Fig. A2, Fig. 6, Fig. 7, Fig. 8, Fig. 9, Fig. 10, Fig. 11, Fig. 12, Fig. 13, and Fig. 14.

		Altitude	Electron Density	Echo Power	Thickness
Solar Maximum	Layers 1-2	P = 0.6462	P <0.0001	P <0.0001	P <0.0001
	Layers 1-3	P <0.0001	P = 0.0003	P <0.0001	P <0.0001
	Layers 1-4	P = 0.0002	P = 0.0831	P <0.0001	P <0.0001
	Layers 2-3	P <0.0001	P = 0.0804	P <0.0001	P <0.0001
	Layers 2-4	P = 0.0014	P = 0.4000	P <0.0001	P <0.0001
	Layers 3-4	P = 0.8035	P = 1.0000	P = 0.0012	P = 0.0002
Solar Minimum	Layers 1-2	P = 0.6808	P <0.0001	P = 0.3483	P <0.0001
	Layers 1-3	P = 0.1098	P <0.0001	P = 0.0009	P <0.0001
	Layers 1-4	P = 0.3030	P <0.0001	P = 0.0001	P <0.0001
	Layers 2-3	P = 0.0481	P <0.0001	P <0.0001	P <0.0001
	Layers 2-4	P = 0.2284	P = 0.0091	P <0.0001	P <0.0001
	Layers 3-4	P = 1.0000	P = 0.5707	P = 0.0728	P = 0.0002
Sol Max. - Min.		P <0.0001	P <0.0001	P <0.0001	P <0.0001

Table B3. P-values for the correlation coefficients for all layers together during solar maximum and solar minimum shown in Table 4.

P-Values		Solar minimum			
		Electron density	Echo power	Thickness	Altitude
Solar Max.	Electron density		1.53E-27	1.38E-54	1.06E-04
	Echo power	1.02E-203		0	2.51E-28
	Thickness	0	0		1.94E-30
	Altitude	0.772	2.24E-03	0.0175	

Table B4. P-values for the correlation coefficients for the mono and multi layers separately, during solar maximum and solar minimum shown in Table 5 b).

P-Values		Solar minimum			
		Electron density	Echo power	Thickness	Altitude
Solar Maximum	Electron density		Layer1 = 1.86E-19 Layer2 = 1.49E-14 Layer3 = 4.17E-04 Layer4 = 0.0489	Layer1 = 1.02E-59 Layer2 = 2.84E-08 Layer3 = 4.17E-04 Layer4 = 0.00542	Layer1 = 2.08E-27 Layer2 = 0.800 Layer3 = 0.165 Layer4 = 0.455
	Echo power	Layer1 = 4.06E-183 Layer2 = 5.68E-58 Layer3 = 4.29E-12 Layer4 = 3.19E-05		Layer1 = 3.58E-139 Layer2 = 5.62E-112 Layer3 = 4.17E-04 Layer4 = 6.96E-22	Layer1 = 0.0760 Layer2 = 2.30E-16 Layer3 = 2.51E-14 Layer4 = 5.92E-04
	Thickness	Layer1 = 0 Layer2 = 9.23E-99 Layer3 = 1.65E-17 Layer4 = 3.60E-05	Layer1 = 4.186E-319 Layer2 = 0 Layer3 = 8.51E-205 Layer4 = 1.89E-32		Layer1 = 2.87E-10 Layer2 = 8.82E-06 Layer3 = 4.17E-04 Layer4 = 0.0418
	Altitude	Layer1 = 1.80E-07 Layer2 = 5.19E-04 Layer3 = 0.194 Layer4 = 0.305	Layer1 = 6.87E-10 Layer2 = 5.85E-04 Layer3 = 5.32E-06 Layer4 = 6.02E-04	Layer1 = 2.93E-19 Layer2 = 0.592 Layer3 = 0.0288 Layer4 = 0.174	
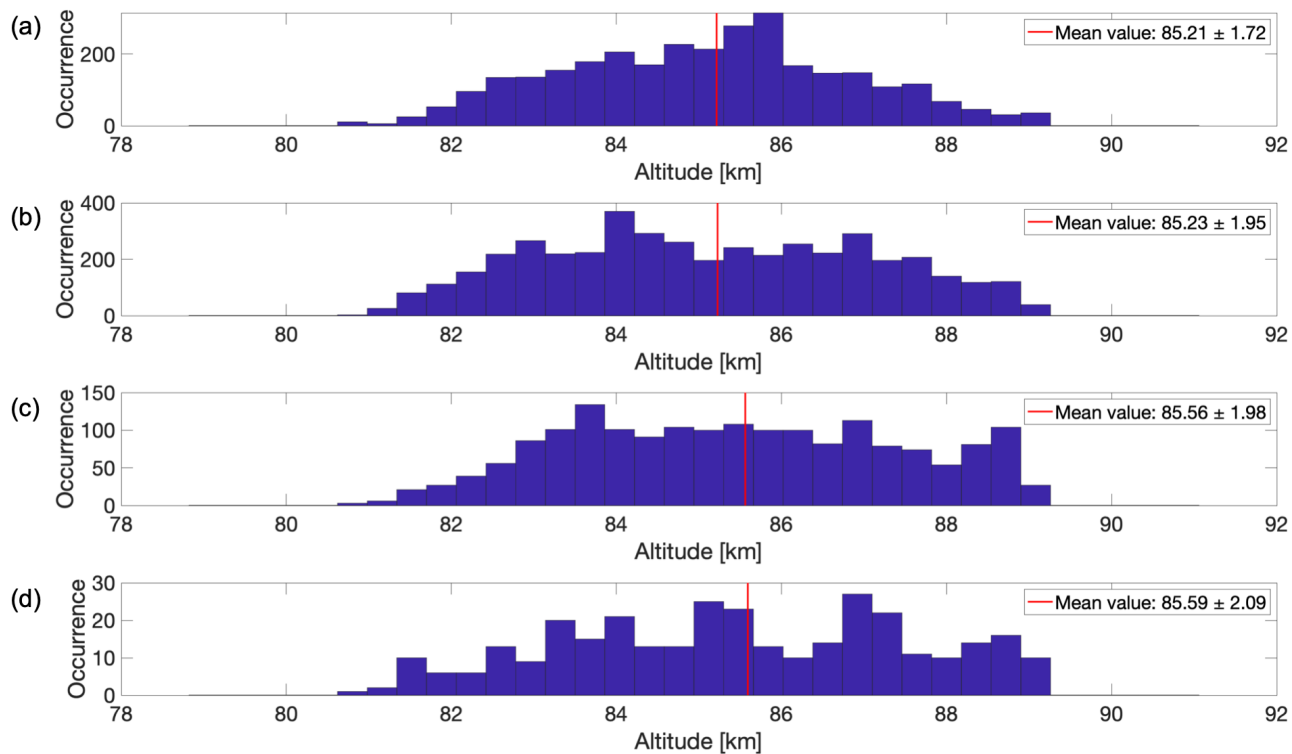
Figure A1. Altitude distribution of the data during solar maximum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. Each subplot was its respective averaged mean altitude of all the multilayers, represented with a red line on the graph, and specified in the legend together with one standard deviation.
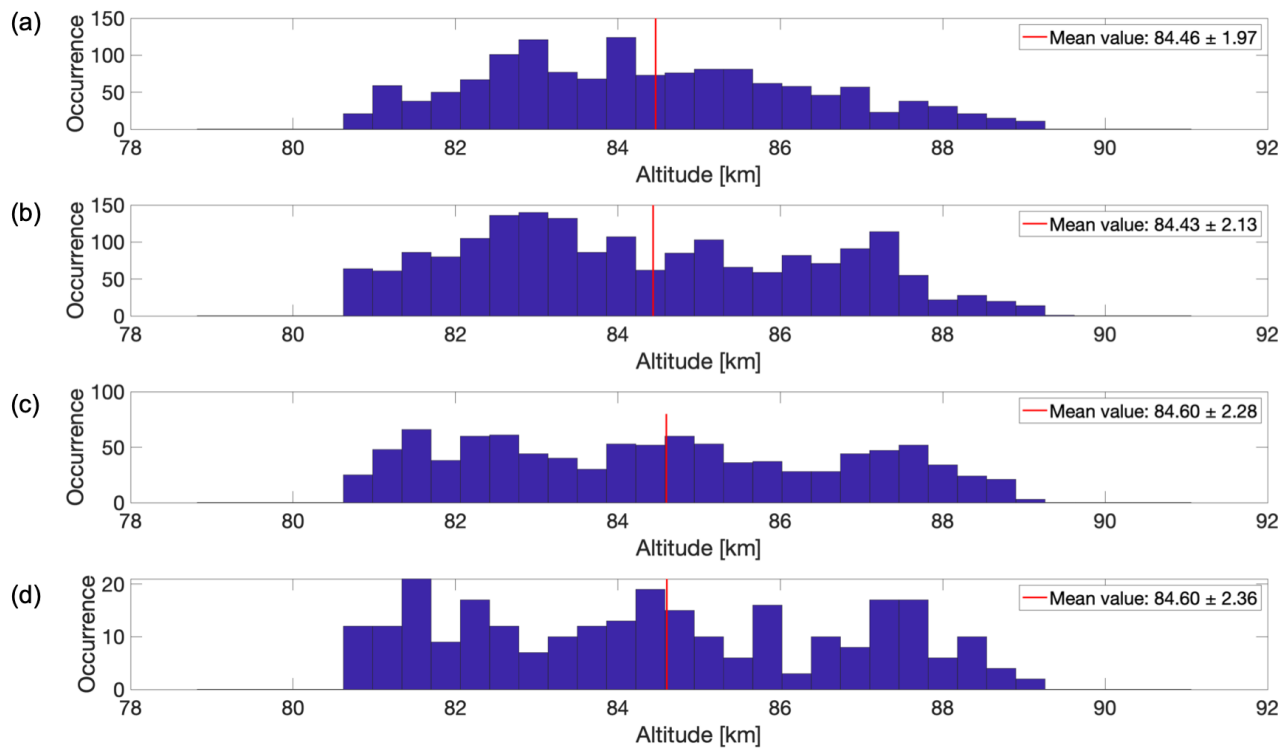
Figure A2. Altitude distribution of the data during solar minimum for **(a)** mono layers, **(b)** multi layers with 2 layers, **(c)** multi layers with 3 layers, and **(d)** multi layers with 4 layers. Each subplot was its respective averaged mean altitude of all the multilayers, represented with a red line on the graph, and specified in the legend together with one standard deviation.