Spatial biases reduce the ability of earth system models to simulate soil heterotrophic respiration fluxes

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Abstract. Heterotrophic respiration (Rh) is, at a global scale, one of the largest CO_2 fluxes between the earth's surface and atmosphere and may increase in the future. Yet, the capacity of Earth System Models (ESMs) used within the Coupled Model Intercomparison Project Phase 6 (CMIP6) to reproduce this flux has never been evaluated, causing uncertainty in resulting CO_2 flux estimates. In this study, we combine recently released observational data on Rh and ESM simulations to evaluate,

20   for the first time, the ability of 13 ESMs to reproduce Rh. Only four of the 13 tested were able to reproduce the total Rh flux but spatial analysis underlined important bias compensation. We observed that mean annual precipitation was the most important driver explaining the difference between ESM simulations and observation-derived product of Rh with higher bias between ESM simulations and Rh products where precipitation was high. Based on our results, next-generation ESMs should focus on improving the response of Rh to soil moisture.

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1 Introduction

Stocks of soil organic carbon are estimated to represent around three times the amount of carbon in the atmosphere (Scharlemann et al., 2014). This soil carbon is used as a substrate by soil microorganisms to obtain their energy and feed their metabolism, which account for the majority of heterotrophic soil organism biomass. Annual fluxes that result from the respiration of these heterotrophic organisms (hereafter referred to as heterotrophic respiration) are estimated (Warner et al., 2019; Hashimoto et al., 2015; Konings et al., 2019; Ciais et al., 2021) to be five times higher than annual anthropogenic emissions (Friedlingstein et al., 2022) and roughly similar to annual terrestrial net primary production (Zhao et al., 2005). Thus, due to the size of fluxes relating to heterotrophic respiration, even minor changes in soil organic carbon dynamics can lead to significant impacts on carbon feedbacks and, ultimately, on climatic changes. As a result, modification of soil organic carbon stocks due to human activities is considered to be an important driver of future climate trajectories (Chabbi et al., 2017).

Despite the importance of heterotrophic respiration fluxes, the scheme representing this flux in ESMs, which aim to simulate the most important drivers of the earth's climate system, are currently challenged because important drivers are missing (Huang et al., 2021; Wieder et al., 2015) but the proposed new schemes lacks of sufficient evaluation on long term time series (Le Noë et al., 2023). Thus, how accurate are the prediction of ESMs for heterotrophic respiration fluxes is a key question to well constraint the carbon climate feedbacks in ESMs. The ability of ESMs to reproduce this flux has been performed earlier in particular by Shao et al., (2013) but it is important to note that it was done on the previous ESM generation using the simulations done during the Coupled Model Intercomparison Project Phase 5 (CMIP5). Moreover, at that time no gridded products were avalaible. Since then, the model were largely improved and assessing how accurately current ESMs reproduce the fluxes associated with heterotrophic respiration is therefore of major importance. Until now, it was not possible to undertake a robust spatial assessment because of the lack of observation-derived gridded products of Rh. In recent years, new gridded products derived either from (i) upscaling of local observation or (ii) calculations using atmospheric inversions and satellite observations have filled this gap. These products provide the opportunity to evaluate the simulations of ESMs used within the Coupled Model Intercomparison Project Phase 6 (CMIP6) against observation-derived products for heterotrophic respiration. CMIP is a key initiative which aims to compare current ESMs and is a central element of national and international assessments of climate change(Masson-Delmotte et al., 2021).

In this study we have two major aims:

1. Compare predictions of the total flux of heterotrophic respiration from 13 earth system models with three recent gridded products of heterotrophic respiration derived from observations and identify the spatial biases of heterotrophic respiration in the models.

2. Identify the major drivers of the heterotrophic respiration bias in earth system models to propose way of improvement for the next generation of earth system models using a model residue approach to disentangle the main effect.

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a supprimé : Despite the importance of heterotrophic fluxes, they have not been well characterized and incorporated into earth system models (ESMs), which aim to simulate the most important drivers of the earth's climate system. Although the carbon fluxes of oceans and plants have been well characterized and incorporated into earth system models (Luyssaert et al., 2018; Séférian et al., 2020) this is not true of fluxes resulting from heterotrophic respiration – and as such, these represent a key source of uncertainty regarding carbon flux. Given the importance of carbon exchange between the earth's surface and atmosphere as a driver of atmospheric CO_2 it is vital that such exchanges are accurately represented in earth system models. ¶

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2 Materials and Methods

2.1 Earth System Models simulations.

In this study, we used the model outputs from the 6th Coupled-Model Intercomparison Project (CMIP6) (Eyring et al., 2016)
75 which coordinates global climate model simulations of the past, current, and future climate. CMIP6 proposes historical
simulation spanning from 1850 to 2014. Historical simulations are driven from an initial point chosen in control integration
(*piControl*). We chose to use the latest CMIP6 results for basic initial state (r1i1p1f1). We choose outputs from thirteen ESMs
that provide heterotrophic respiration fluxes (BCC-CSM2-MR, BCC-ESM1, CanESM5, CESM2, CNRM-ESM2-1, E3SM-1-
1-ECA, IPSL-CM6A-LR, MIROC-ES2L, MPI-ESM1-2-LR, NorCPM1, NorESM2-LM, SAM0-UNICON and UKESM1-0-
80 LL). The variable used is "rh" corresponding to the total heterotrophic respiration on land. We computed annual average over
the 1990-2010 period which corresponds to the period in which most of the observations in the global Soil Respiration Database
(Bond-Lamberty and Thomson, 2010) v3.0 were made. Two observation products we used were obtained using those data.

2.2 Observation-derived products.

85 In this study we used three observation derived products (Warner et al., 2019; Konings et al., 2019; Hashimoto et al., 2015).
In Warner et al. (2019), the authors predicted annual soil respiration and associated uncertainty across terrestrial areas at a
resolution of 1 km using a quantile regression forest algorithm trained with observations from the global Soil Respiration
Database (Bond-Lamberty and Thomson, 2010) v3.0 (commit number 651770 in GitHub, https://github.com/bpbond/srdb)
spanning from 1961 to 2011 but mostly after 1990. Then they deduced Rh from the soil respiration using two different methods
90 (Bond-Lamberty et al., 2004; Subke et al., 2006). They therefore proposed two Rh maps derived from a unique mean map of
Rs from quantile regression forest model. Here, we decided to use the mean of two approaches as a reference for Warner et al.
(2019) Rh results. The second product we used (Hashimoto et al., 2015) called here Hashimoto et al. (2015) is also based on
the Soil Respiration Database (Bond-Lamberty and Thomson, 2010) v3.0 but in this case they derived the Rh flux using
a climate-driven model of soil respiration derived from the Raich's model (Raich et al., 2002). They provided a 0.5∘ resolution
95 product at a monthly step time between 1965 and 2012. In our case, we used the yearly average over the period. The third
product used (Konings et al., 2019) called here Konings et al. (2019) estimated Rh as a residual remote-sensing data exploiting
recent advance in carbon-flux estimations. In contrast with the two other products which can be considered as bottom up, the
Konings et al., (2019) product propose a top-down approach combining net ecosystem productivity estimates from atmospheric
inversions with an optimally scaled gross primary productivity dataset derived from satellite observations. Rh is then derived
100 using the CARbon DAta MOdel fraMework, (CARDAMOM). Their result is a monthly evaluation of Rh, between 2010-01
and 2012-12, at a resolution 4°×5°.

2.3 Data treatment and regriding.

All the ESMs outputs and products were not at the same resolution. Thus, we needed to choose a reference for map-grid resolution. The coarser resolution was from Konings et al. (2019)'s product with a 4°×5° resolution grid. Degrading every Rh map at such resolution would be a substantial loss of information. Thus, we increased the resolution of those datasets and

110 decreased the very fine scale maps to an arbitrary reference corresponding to the CNRM-ESM2-1 model which runs at 0.7° resolution. We chose to set the reference at the maximum resolution available among CMIP6's ESMs predicting Rh. We used the common regridding routine Climate Data Operators (CDO) remapdis (nco module) that performs regridding by distance-weighted average remapping and conserve latitudinal and longitudinal means. The CDO software is a collection of multiple operators for standard processing of climate and forecast model data. The operators include simple functions (statistical and

115 arithmetic) to be used for data selection, subsampling, and spatial interpolation. To avoid coastal pixels encroaching into oceans, we weighted each pixel by its proportion of land. The sum of Rh over the lands was compared before and after regridding to ensure that it was conservative. When comparing the original and the regrided version of the Konings et al. (2019)'s product we observed very similar pattern (Fig. 1).

120 **2.4 Comparison between models' outputs and heterotrophic respiration products.**

To estimate the ability of the CMIP6's model to reproduce soil heterotrophic respiration, we first compared the global flux summed over all the grid cells and averaged over 1990-2010 period in Pg C yr^{-1}. We also compared the Rh maps after regridding averaged over the 1990-2010 period. We also performed latitudinal and longitudinal means calculus including oceanic zero-values. Secondly, we wanted to assess spatial bias distribution. Therefore, we i) compare CMIP6 model average

125 with observation products and ii) compare each CMIP6 models with observation products. Thus, we first represented the model average (over the period 1990-2010) and all the observation derived products on a same figure with their associated latitudinal and longitudinal means. We also calculated the 25th and 75th quantiles of latitudinal and longitudinal CMIP6 model means. Then, we computed the difference for each single CMIP6 models with the median of the three observation products. To compare the ESMs with the observation products, we calculated the root mean square error (RMSE) and the R^2 using the

130 median of the observation products. Finally, we also calculated the median absolute deviation (MAD) for each grid cells and we calculated the number of pixels for each models that fit within the median ± MAD.

2.5 ESM's model residual analysis.

We defined here the ESM's model residuals as median of the difference between each single CMIP6's model output and the

135 observation-based products median calculated for each grid cell. The ESM's model residuals were calculated in three steps:

    1. We calculated first the median for each cell using the three observation-derived products. We consider this median as our best-estimate.

    2. Then, we calculated the difference between each CMIP6's model output and our best-estimate for each grid cell.

    3. Finally, we calculated the ESM's model residuals as the median of this difference.

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Using the ESM's model residuals, we performed a statistical analysis to identify the main drivers. We proceed with a two-step methodology. First, we compared several linear generalized least square models with different spatial structures (gaussian, exponential, spherical, linear or rational (gls package. (Venables and Ripley, 2002))) and without spatial structures to estimate the effect of spatial correlation. Based on Akaike information criterion (AIC) values we selected the rational quadratic spatial correlation structure that had the smallest AIC values for the second step of the analysis. Then, we used generalized additive mixed model with ESM's model residuals as variable to explain and mean annual temperature (MAT), mean annual precipitation (MAP), observation derived SOC, ESM's model residuals on NPP and lithology as predictors variables. MAT and MAP are derived from the Global Soil Wetness Project Phase 3 (GSWP3) reanalysis (http://hydro.iis.u-tokyo.ac.jp/GSWP3/ last access: April 5 2022). SOC was taken from the Soilgrid250m product (Hengl et al., 2017). ESM's model residuals on NPP are calculated as the median of the difference between ESM's NPP and NPP from the global inventory monitoring and modelling studies group (GIMMS). Lithology maps from the global lithological map (GLiM) (Hartmann and Moosdorf, 2012) was used but since lithology was not significant (p>0.05) and the model has a lower AIC without it was not included in the final generalized additive mixed model presented here. All statistical analysis were made using R v3.5 (R Core Team, 2018).

3 Results

3.1 Global heterotrophic respiration flux and spatial biases

Global heterotrophic respiration flux simulated by the 13 ESMs ranges from 29 to 78 Pg C yr^{-1} (Fig. 2), whereas the equivalent estimates for observationally derived products estimate range from 43 to 51 Pg C yr^{-1}. The multi-model mean of the ESMs (49 Pg C yr^{-1}) falls within the range of the observation-derived products. However, only four out of 13 ESMs (BCC-CSM2-MR, CNRM-ESM2-1, IPSL-CM6A-LR, and SAM0-UNICOM) simulate an overall heterotrophic respiration flux that is within the range of the observation-derived products (Fig 2). When comparing the model observation products' with the median ± MAD from the observation products (46 ± 7 Pg C yr^{-1}) seven out of the 13 ESMs predicted an heterotrophic respiration within this range (Fig. 2). The R^2 between the model outputs and the median of the observation products range between 0.57 for E3SM-1-1-ECA and 0.82 for MIROC-ES2L (Table 1). When using RMSE to compare the model outputs and the median of the observation products 170.9 gC m^{-2} yr^{-1} for IPSL-CM6A-LR and 345.1 gC m^{-2} yr $^{-1}$ for CanESM5 (Table 1). Finally, we also estimate the number of pixels that falls within the median ± MAD and using this metrics BCC-ESM1performed better followed by BCC-CSM2-MR and CNRM-ESM2-1.

Despite similar global-scale values, regional-scale differences between the observation-derived products are much larger (Fig. 3). The Konings et al. (2019) product estimates large heterotrophic fluxes in the tropics and lower fluxes in other regions such as the west coast of Northern America or central Asia, as compared to the Warner et al. (2019) and the Hashimoto et al. (2015)

products that share similar spatial patterns (Fig. 4). The mean of the 13 ESMs simulations also gives a much larger heterotrophic respiration fluxes over the tropics in particular over South-East Asia compared to any of the three observation-derived products. In general, the heterotrophic respiration fluxes from the 13 ESMs mean is closer to Konings et al. (2019) product over the tropics but closer to the Warner et al. (2019) and the Hashimoto et al., (2015) products over temperate regions. For boreal regions, the three observations-derived products and the 13 ESMs means are very close.

To generate our best-estimate of heterotrophic respiration fluxes from the three observation-derived products we calculated the median for each cell. Thus, we obtained the spatially distributed best-estimate. At each grid cell, we then compared each ESM with the observation-derived products median (Fig. 5). This evaluation indicates that, compared to observation-based products, ESMs (apart from the ESM NorCPM1) tend to overestimate heterotrophic respiration flux in tropical regions (approx. 1,000 gC m^{-2} yr^{-1} for MPI-ESM1-2-LR over the Amazon or 1,500 gC m^{-2} yr^{-1} for UKESM1-0-LL over South-East Asia, for instance). Models perform relatively well in temperate regions with for instance bias close to 0 gC m-2 yr-1 for BCC-ESM-1 over North America and Europe. Important discrepancies were observed for boreal regions with some models largely underestimating the heterotrophic respiration fluxes (e.g. NorCPM1 or SAM0-UNICON) and other overestimating the fluxes (MPI-ESM1-2-LR). The BCC models (BCC-CSM2-MR and BCC-ESM1) were performing quite well over this region. Importantly, the four models that predict a global heterotrophic respiration flux within the range given by the observation-derived products (BCC-CSM2-MR, CNRM-ESM2-1, IPSL-CM6A-LR and SAM0-UNICOM), do not perform well at finer scales - with over estimation of the flux in some regions and under estimation in others. Therefore, this good global-scale performance masks spatial bias compensation.

3.2 Identification of the major drivers of the heterotrophic respiration bias in earth system models.

In order to improve predictions of heterotrophic respiration fluxes in future ESMs we need to understand the spatial biases we observed and determine their causes. To explore these biases, we performed a statistical analysis based on a generalized additive mixed model of the ESMs residuals defined as the median of the difference between each CMIP6's model output and the median of the observation-based products calculated in each grid cell. ESMs share a very common approach based on first order kinetics with soil organic decomposition driven by soil moisture and temperature (Varney et al., 2022; Todd-Brown et al., 2014). This approach is derived from the very first attempts to describe soil organic decomposition with mathematical equations (Henin and Dupuis, 1945) and is still the most used to describe this process (Manzoni and Porporato, 2009; Wutzler et al., 2008). Since SOM decomposition schemes in ESMs are very similar, comparing each model individually can be redundant and not very informative and less generalizable. To allow broader conclusions and suggestions to improve ESMs performances, we decided to perform the residual analysis on the ESMs median rather on each individual model.

The main drivers of heterotrophic respiration are soil carbon availability, soil moisture and temperature, carbon inputs and mineralogy (Doetterl et al., 2015). To explain our model residues we used soil organic carbon, net primary production residuals

calculated using similar methods to heterotrophic respiration flux residuals, mean annual precipitation, mean annual temperature and lithology. Our method identified the main drivers of ESMs residuals as soil organic carbon, net primary production residuals, mean annual precipitation, and mean annual temperature (Fig. 6). Lithology was not significant (p>0.05) and the model has a lower AIC without this variable and so we did not include lithology in the final model presented here. We observed that the residuals due to soil organic carbon stock are close to zero for soil with a low carbon stock but heterotrophic respiration is under estimated by ESMs for soils rich in organic carbon (> 3,000 g C m^{-2}) (Fig. 6a). The model residuals on the heterotrophic respiration flux are partially explained by the model residuals on net primary production with a slight increase from model underestimation to model overestimation when model residual on net primary production increase from -1,000 to 400 g C m^{-2} yr^{-1}. We noted that when net primary production fits well with satellite products (i.e model residuals close to 0 g C m^{-2} yr^{-1}), the ESM residuals on the heterotrophic respiration flux are also close to 0 g C m^{-2} yr^{-1}. For a few grid cells where ESMs largely overestimate net primary production (i.e. model residuals higher than 400 g C m^{-2} yr^{-1}), the ESMs residuals on heterotrophic respiration flux tend to be negative suggesting that ESM underestimate heterotrophic respiration flux. The clearest tendency we obtained was with mean annual precipitation, the more it increases the more the models overestimate the heterotrophic respiration flux (Fig. 6c). The median ESMs residual was also partially controlled by mean annual temperature (Fig. 6d) with a relatively low overestimation by the models for cold temperatures such as those recorded in polar climate zones and in some continental climate zones (e.g. subartic climate), a relatively good fit for temperature between 0 and 20°C corresponding to temperate and some continental climate zones (e.g. Hot summer continental climates) and then a sudden underestimation for warm temperatures above 20°C corresponding to tropical and dry climate zones. This sudden underestimation might be explained by an arbitrary maximum respiration level observed in this dataset and identified as the result of the temperature-dependence of soil respiration used by Hashimoto et al., (2015) (Varney et al., 2020). Such bias can therefore be a consequence of the observation-based products used here rather than a real ESMs bias. It is important to note that similar results were obtained when performing the same analysis with means instead of medians (Fig. 7).

4 Discussion

In this study we evaluated, for the first time, the ability of the ESMs to reproduce heterotrophic respiration flux. Indeed, previous dataset were not gridded and so far spatial pattern of heterotrophic respiration in ESMs could only by constraint indirectly by constraining other C fluxes including heterotrophic respiration such as net ecosystem exchange fluxes or through ecosystem respiration in which heterotrophic respiration is just one component the other being the autotrophic respiration (Stoy et al., 2013). We showed that only four of 13 of the CMIP models produce global-scale estimates that are consistent with observation-derived products. However, we also showed that this consistency was due to spatial bias compensations driven by different environmental variables. Heterotrophic respiration represents a carbon flux that is roughly five times that of anthropogenic emissions (Friedlingstein et al., 2022) and, as such, it is vital that work is done to improve the ability of ESMs to reproduce this flux. Nevertheless, we also observed large discrepancies between observation-based products

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showing that our ability to provide heterotrophic flux based on observations is not optimal. To better constrain ESMs projections, some efforts are needed to reduce uncertainties between observation-based products.

However, working only on heterotrophic respiration may not be sufficient to improve the entire soil organic carbon module of the ESMs (Table 2). ESM capacities to reproduce observed soil organic carbon stocks also need to be improved (Ito et al., 2020; Varney et al., 2022). To improve both soil organic carbon stocks and heterotrophic respiration fluxes soil organic carbon decomposition rates needs to be better constrained. The ESM residual analysis we performed here suggests some new research avenues and in particular for the response of the major drivers. First, it must be noted that most of the boundary conditions of the soil organic carbon modules of an ESM are calculated by the ESM itself. Thus, if soil moisture, soil temperature or litter production are incorrect, the soil organic carbon dynamic cannot be correct. We observed that when the residual of NPP was close to zero the residual on heterotrophic respiration is also close to zero. Thus, improving the plant functioning scheme may ultimately improve the capacities of the ESMs to reproduce the heterotrophic respiration flux. Our study also showed that mean annual temperature is an important driver of the ESM residuals in particular for hot regions with large underestimations of the flux. It probably corresponds to very arid regions since for most of the ESMs, heterotrophic respiration fluxes from regions like Australia, Middle East or Northern Africa tend to be underestimated. Nevertheless, the underestimation observed in these regions can be also due to reduced C inputs and low SOC stocks reducing mechanically the heterotrophic respiration fluxes.

The response of soil organic decomposition by microorganisms is likely to be temperature dependent, with lower rates of decomposition seen in cold regions and higher rates in hot regions (Wang et al., 2010; Zhou et al., 2009). In contrast, the response of soil organic decomposition to temperature in ESMs is generally controlled by Q10 equations (Davidson and Janssens, 2006) with fixed parameters not dynamic and not spatially distributed (Ito et al., 2020). Previous studies suggested that a spatially distributed Q10 constrained on observations would be an important step to improve ESMs (Koven et al., 2017; Varney et al., 2020). Our results are online with this statement and suggest that having more flexible Q10 parameters may help to improve ESMs capacities to reproduce observation-derived products of heterotrophic respiration fluxes. Moreover, land surface scheme of ESMs are known to be very sensitive to Q10 values (Jones et al., 2003; Todd-Brown et al., 2018).

Finally, we observed a relatively linear, positive relationship between mean annual precipitation and the ESMs' residuals (Fig. 6c). This response is probably driven by soil moisture because it is a key driver of microbial activity and therefore of heterotrophic respiration fluxes (Moyano et al., 2012). ESMs use three main groups of soil moisture response function (Falloon et al., 2011): i) some models do not represent soil moisture effect, ii) some models increase soil organic decomposition when soil moisture increases assuming less water limitation for microbial activity and iii) some models assume a humped relationship between soil moisture and soil organic decomposition, with high decomposition at intermediate soil moisture and low decomposition in very wet soils where microbial activity is reduced because of limitation by oxygen availability and in dry soils where microbial activity is reduced because of limitation by water. As with Q10, the land surface schemes are highly sensitive to the soil moisture response function chosen approach and most of the ESMs use option ii) (Varney et al., 2022).

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Soil incubations have repeatedly shown that the response of heterotrophic respiration fluxes to soil moisture is approximated by a bell-shaped function with parameters depending on soil organic carbon, soil clay content, and soil bulk density (Moyano et al., 2012). Thus, for wet soils, heterotrophic respiration fluxes are probably reduced because of oxygen limitation. Implementing this bell-shaped function approach is necessary to accurately represent the soil organic carbon stock of peatland in some land surface schemes used by ESMs (Qiu et al., 2019). The approach proposed by Moyano et al., (2012) seems well adapted to ESMs constraint since the author proposed several versions of the bell-shaped function and did the effort to define one function using drivers that are included in ESMs (the model 2 in Moyano et al., (2012)). The model including bulk density might perform better but bulk density is not calculated by ESMs and consequently such approach is hardly implementable in ESMs. Other approaches have been proposed in the literature (Davidson et al., 2014; Sierra et al., 2014) but the solutions proposed are mostly based on Michaelis-Menten function whereas most of the ESMs used first order kinetics approach to describe SOM decomposition. Moreover, alternative solutions are based on O_2 diffusion which is more mechanistic but more difficult to implement in an ESM compared to a more empirical solution as proposed by Moyano et al. (2012). Gas diffusion implementation at the spatial resolution of ESMs is quite challenging because it depends on drivers highly variables at small scales. Not considering the possible oxygen limitation effect on wet soils can explain why ESMs tends to overestimate the heterotrophic respiration flux when mean annual precipitation is high. Changing soil moisture function to better represent this effect should be relatively easy and may substantially improve the capacities of ESMs to reproduce the heterotrophic respiration flux.

Another important parameter controlling heterotrophic respiration flux is carbon use efficiency defined as the ratio between the carbon remaining in a system and the carbon entering that system (Manzoni et al., 2018). In our context this is the ratio between the carbon mineralized through microbial heterotrophic respiration and the carbon incorporated into the microbial biomass. The heterotrophic respiration flux therefore results from two processes in ESMs, the soil organic carbon decomposition and its allocation to other soil carbon pools or to heterotrophic respiration. Carbon use efficiency is highly variable and depends on several biotic and abiotic factors (Sinsabaugh et al., 2013; Manzoni, 2017; Manzoni et al., 2012). In ESMs, carbon use efficiency is not dynamic and not spatially distributed, thus having flexible carbon use efficiency control may help to reproduce observations (Zhang et al., 2018). A simple approach that may aid a better representation of heterotrophic respiration fluxes is optimizing the carbon use efficiency parameters of the ESMs using a Bayesian approach as is done for other land fluxes (Kuppel et al., 2012). This would result in a spatially distributed set of parameters for carbon use efficiency but this approach would not be dynamic. Another option might to benefit to the current large carbon use efficiency measures existing in the literature (Manzoni et al., 2012) to define statistical functions predicting carbon use efficiency based on explanatory variables that could themselves be dynamic (soil temperature, pH, soil C:N ratio, etc.). Thus, carbon use efficiency might be spatialized and dynamic.

A better representation of the heterotrophic respiration flux is also important for other biogeochemical variables in particular in ESMs with explicit nitrogen cycle representation in their land surface scheme. Indeed, heterotrophic respiration fluxes are

indicators of soil organic carbon decomposition but when nitrogen is explicitly represented it also becomes an indicator of soil N mineralization (Vuichard et al., 2018). In the field, the soil organic matter is composed by complex molecules made of carbon and nitrogen among others (Cleveland and Liptzin, 2007). Microorganisms decompose soil organic matter releasing CO_2 to the atmosphere and mineral nitrogen to the soil solution. Microbial activity is therefore a major driver of mineral nitrogen availability and partially control nitrogen limitation on primary production and therefore on land carbon sink (Bragazza et al., 2013). Since more and more ESM represent explicitly the nitrogen cycle in their land surface scheme (Varney et al., 2022; Davies-Barnard et al., 2020) constraining well the heterotrophic respiration flux may help to constrain the nitrogen mineralization flux as they both come from the soil organic matter decomposition by extracellular enzymes. A better representation of the mineral N release flux would probably, in turn, improve the simulation of NPP.

5 Conclusion

Our study showed that despite previous ESMs evaluation on heterotrophic respiration (Shao et al., 2013), a few current ESMs are fairly representing the total heterotrophic respiration flux but all failed at representing the spatial distribution. Since heterotrophic fluxes are large and are a major determinant of whether land surfaces represent a carbon sink or source it is of major importance to better constrain these fluxes and how they will be impacted by climate and land use changes. We showed that current ESMs failed to reproduce heterotrophic respiration fluxes where precipitation is important probably because heterotrophic respiration responses to soil moisture are poor representations of reality. Nevertheless, it is important to note that soil moisture is not only driven by precipitation. Other water fluxes like runoff, drainage and evapotranspiration affect the water balance in soils. In this study we did not directly consider soil moisture because it was not available for all the ESMs. Another limitation of our study is that we did not account for other important drivers of heterotrophic respiration in our model residual analysis like pH, microbial biomass, nitrogen availability, etc. We decided to focus on explanatory variables calculated by all the models because we aimed to identify biases due to feedbacks between ESMs variables rather than identifying missing mechanisms. We propose several options to improve the ESM without deep modifications of the current schemes. Our propositions might be easily implemented in the next ESMs generation resulting in possible substantial improvements.

a supprimé: Our study showed that despite the absence of constraint on the heterotrophic respiration flux before the CMIP6 exercise, a few current ESMs are fairly representing the total heterotrophic respiration flux but

Data availability

 All data are available in the main text.

Author contributions

BG, LC, PB and LB designed the study, BG, JO, OT and LS performed the analysis. All the authors participated to the results interpretation and to the writing.

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Competing interests

All other authors declare they have no competing interests.

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Figures
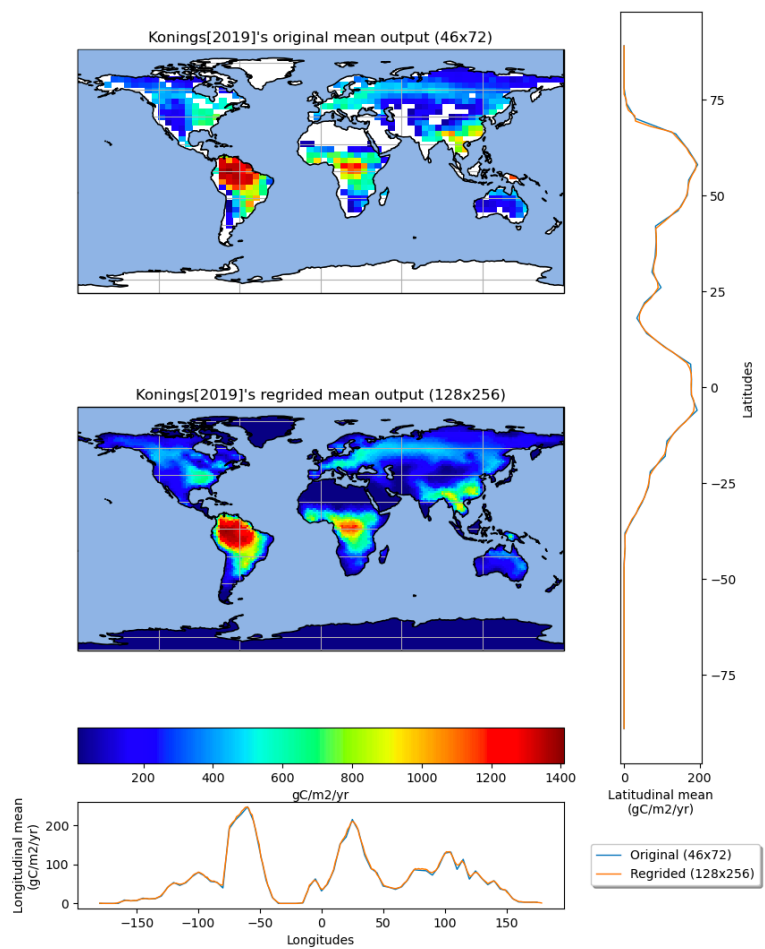
Fig. 1. Mean Rh spatial distribution over 2010-2012 from the Konings et al., (2019) product –original (46x72, top panel) vs regrided (128x256, bottom panel).

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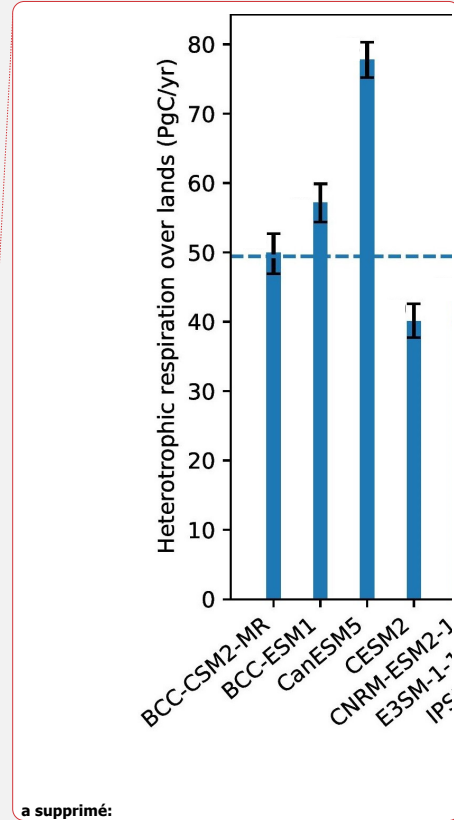
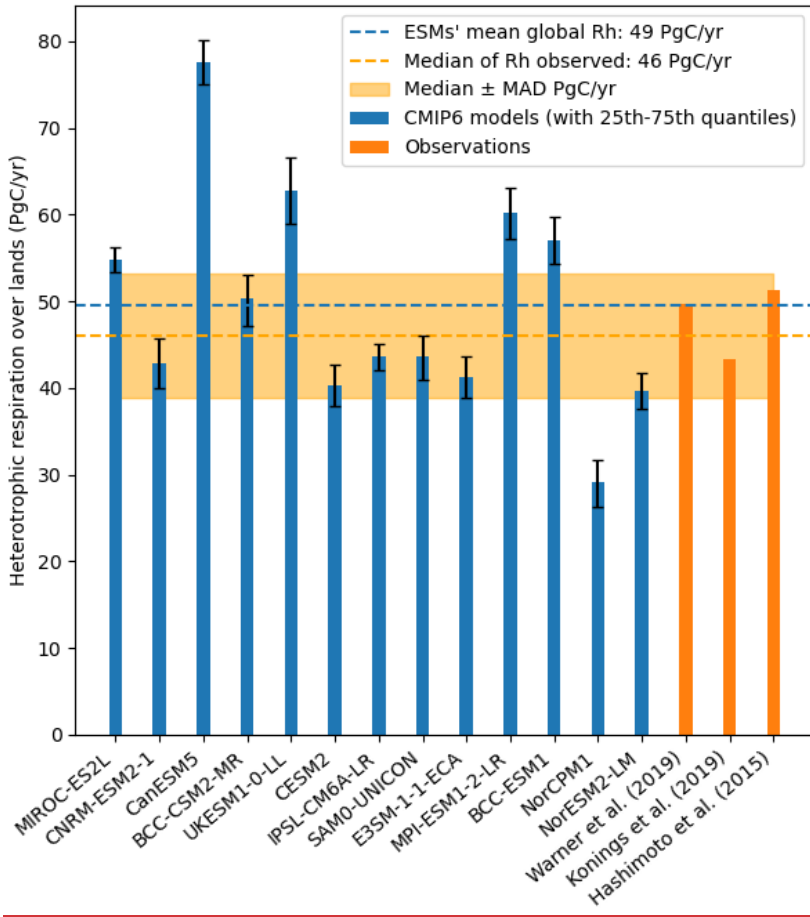


Fig. 2. Global estimations of soil heterotrophic respiration mean over 1990-2010 period.

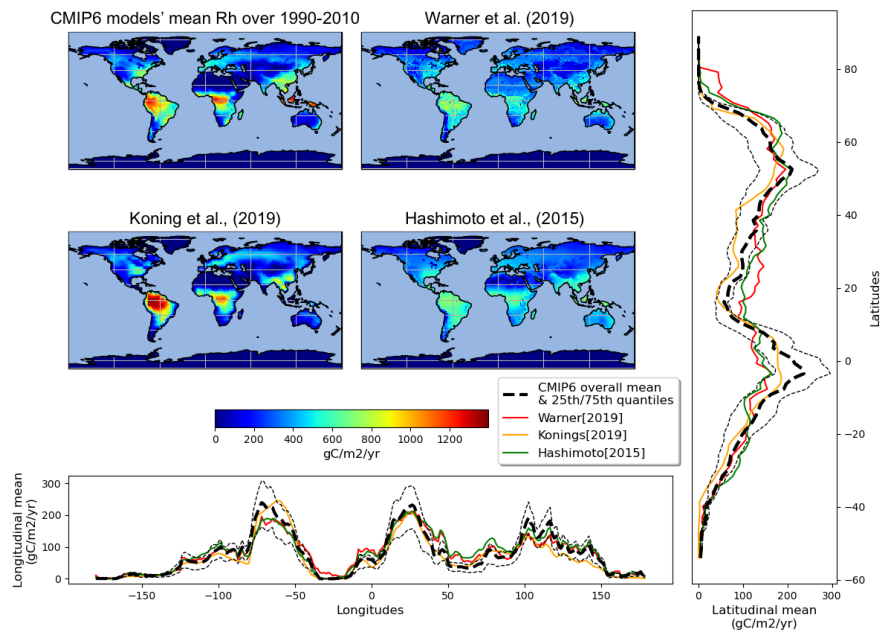



Fig. 3. Comparison of mean soil heterotrophic respiration spatial distribution among mean CMIP6 outputs and observation data.

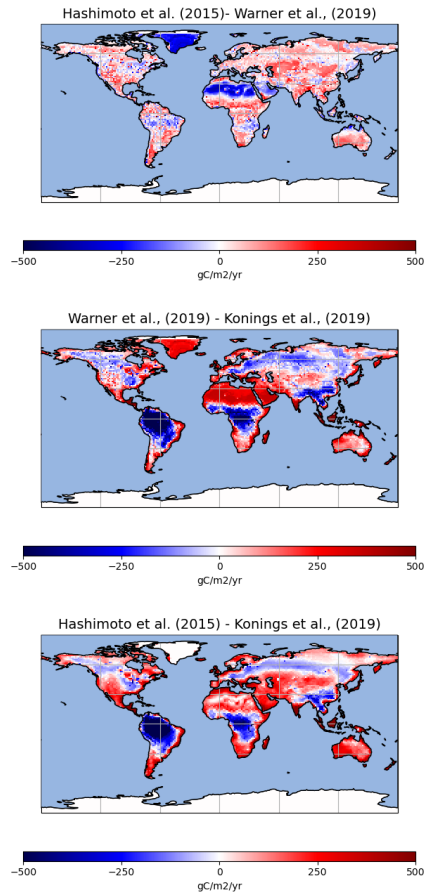



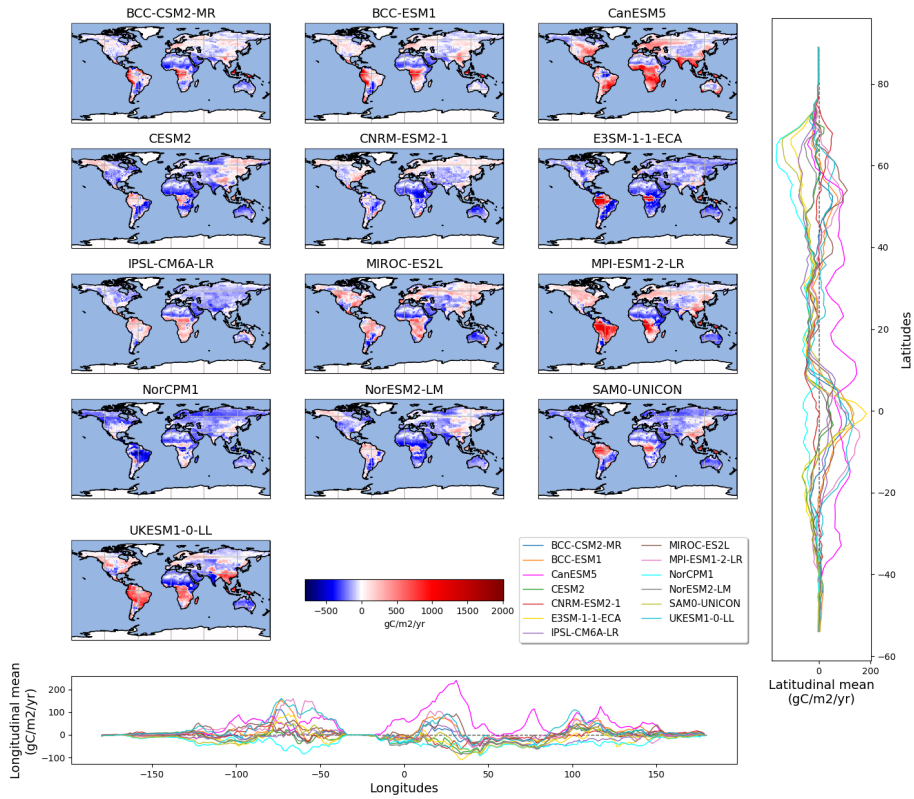
Fig. 4. Maps of difference between the observation based product used in this study (Hashimoto et al., (2015) – Warner et al., (2019) in the top panel, Warner et al., (2019) – Konings et al. (2019) in the middle panel and Hashimoto et al., (2015) – Konings et al. (2019) in the bottom panel).

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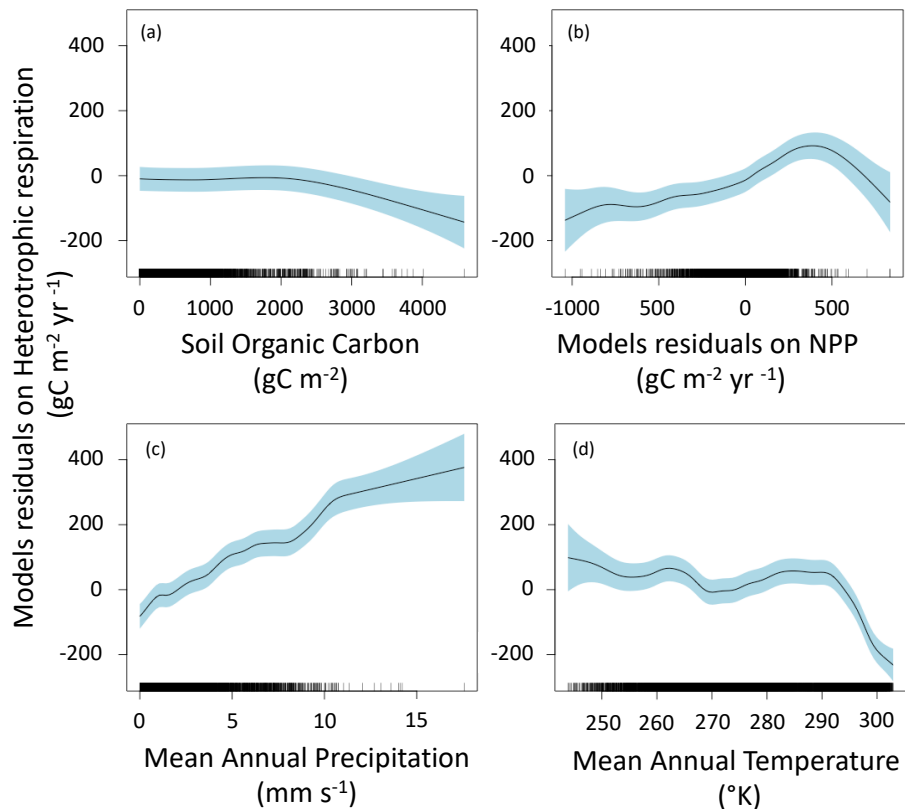
Fig. 5. Spatially distributed residuals of CMIP6 ESMs predictions over the period 1990-2010 with respect to median observation products.

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Fig. 6. Median of ESMs residuals on soil heterotrophic respiration. The residuals are explained by soil organic carbon (a), median of NPP residuals (b), mean annual precipitation (c) and mean annual temperature (d). Negative values mean model underestimation.

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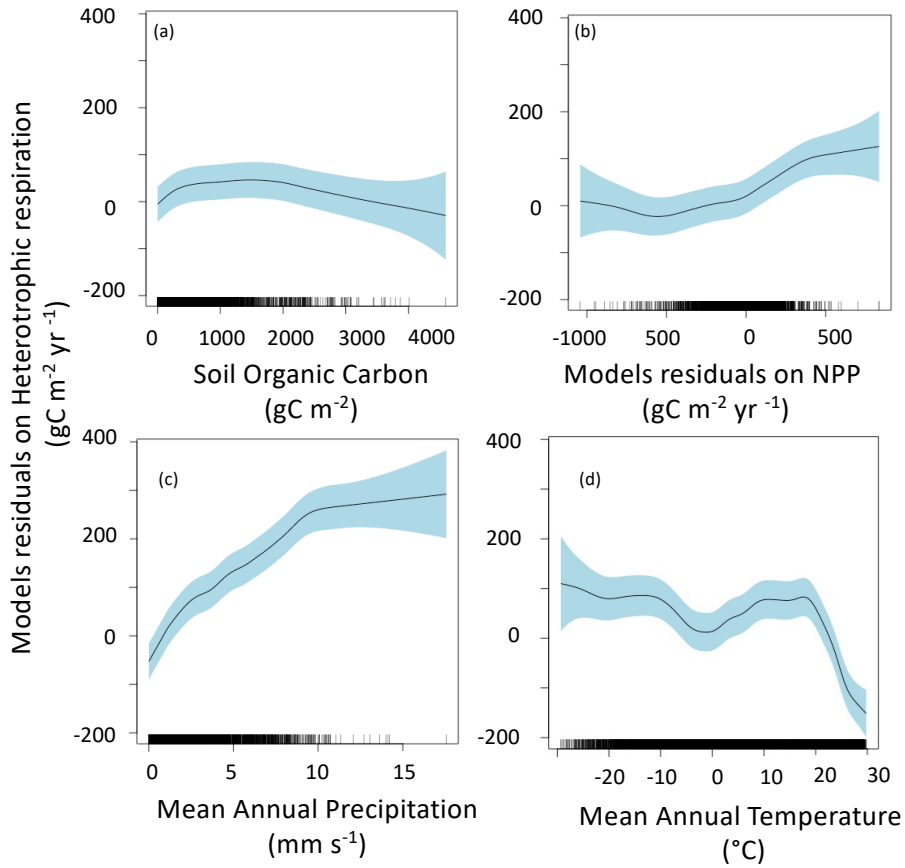
Fig. 7. Mean of ESMs residuals on soil heterotrophic respiration. The residuals are explained by soil organic carbon (a), mean of NPP residuals (b), mean annual precipitation (c) and mean annual temperature (d). Negative values mean model underestimation.

Table 1. Evaluation metrics for the different Earth system models.

Models	BCC-CSM2-MR	BCC-ESM1	CanESM5	CESM2	CNRM-ESM2-1	E3SM-1-1-ECA	IPSL-CM6A-LR	MIROC-ES2L	MPI-ESM1-2-LR	NorCPM1	NorESM2-LM	SAM0-UNICON	UKESM1-0-LL
#pixels within median ± mad	2225	2243	1543	1656	2129	1515	1838	1270	1531	1374	1826	1274	1406
RMSE	224.4	229.0	345.1	199.2	171.1	281.4	170.9	229.3	314.0	212.3	187.7	231.9	302.1
R2	0.75	0.78	0.80	0.72	0.79	0.57	0.79	0.82	0.73	0.68	0.74	0.69	0.75

Table 2. Summary of the main features proposed in this study to improve the heterotrophic respiration fluxes in Earth system models.

	Main features to improve in the next ESM generation
NPP residues	Improving plant inputs through NPP is key to improve heterotrophic respiration by implementing N cycle for instance.
MAT	Dynamic and/or spatialized temperature sensitivity parameters such as Q10.
MAP	Improving the soil moisture functions using bell shape functions for instance.
SOC	More constrained parameters such as CUE and/or residence times.