

Supporting Information for

Estimating Marine Carbon Uptake in the Northeast Pacific Using a Neural Network Approach

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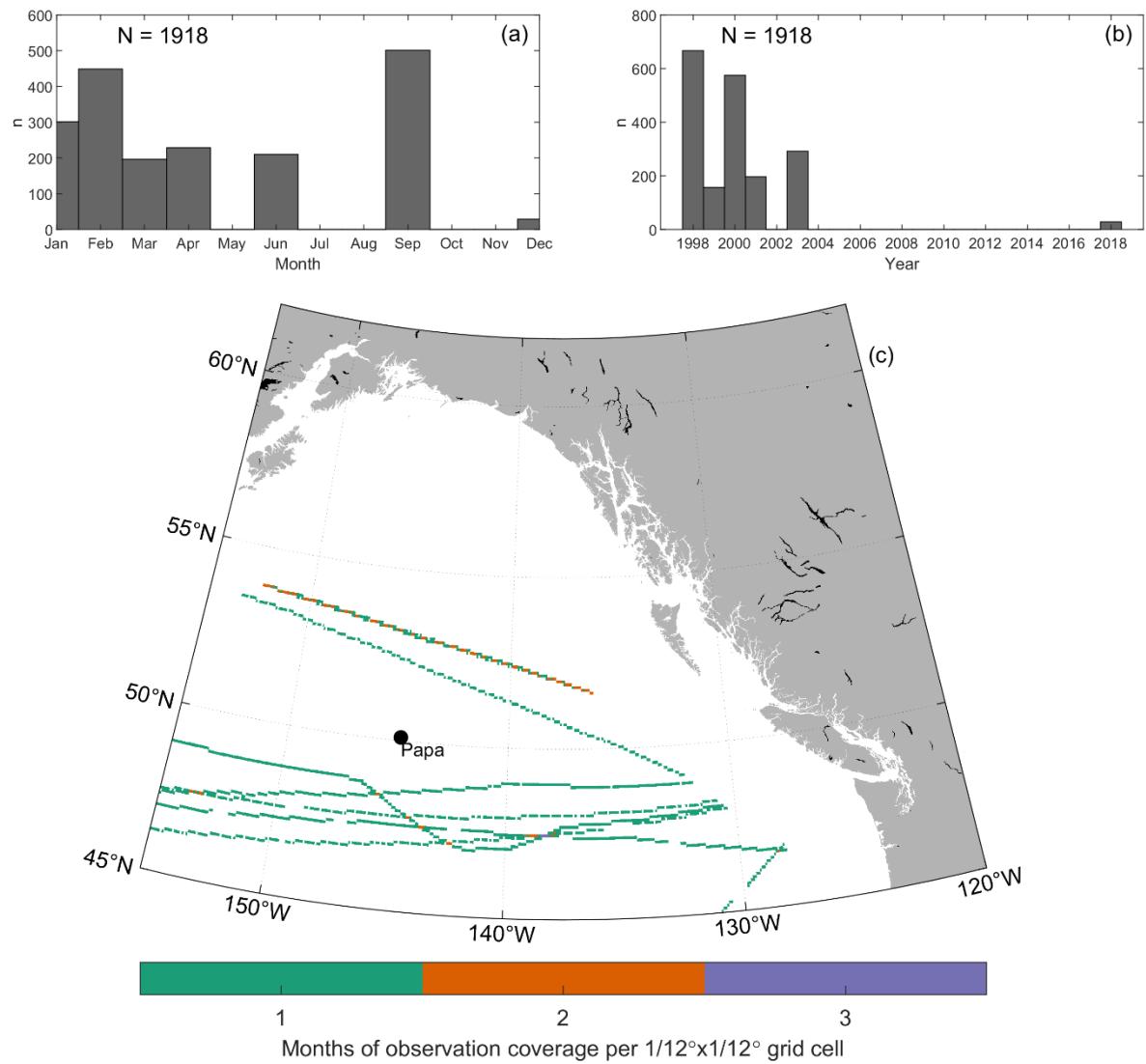


Figure S1 Withheld data distribution in (a) month, (b) years, (c) geographically as the number of months of observational coverage per $1/12^\circ \times 1/12^\circ$ grid cell. Ocean Station Papa is shown for reference.

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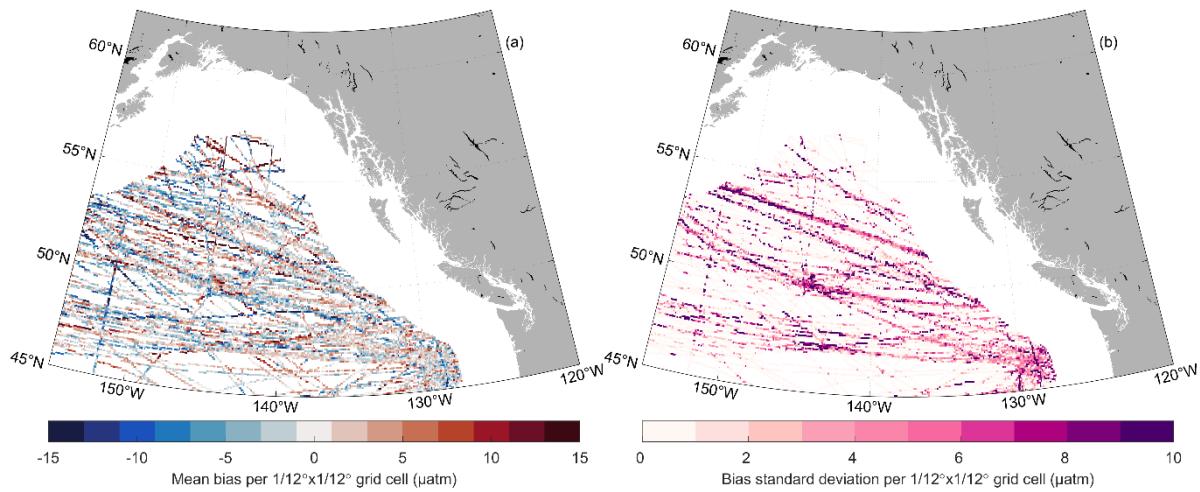
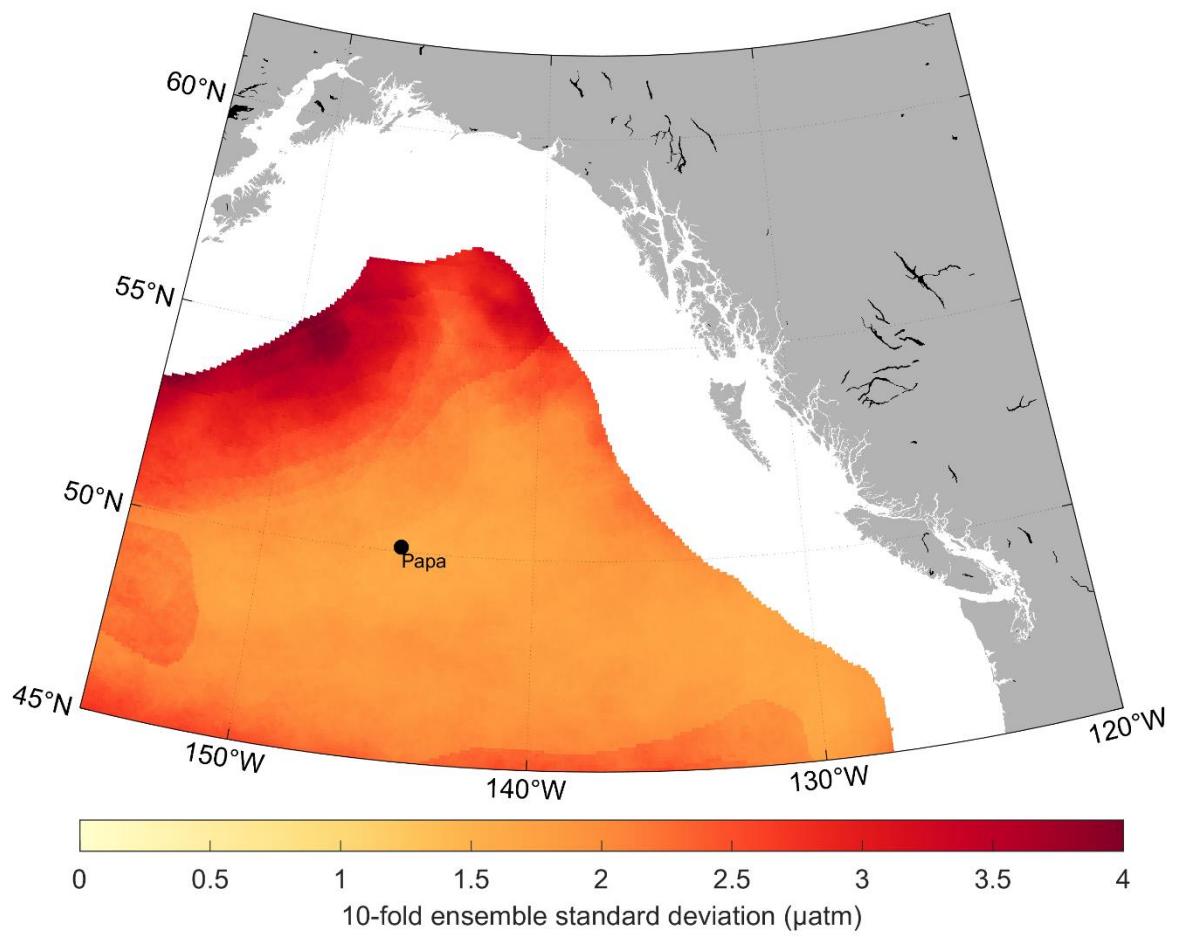


Figure S2 Mapped mean bias and standard deviation in residuals between ANN-NEP pCO₂ estimate and 1/12°x1/12° gridded SOCAT data.



30 **Figure S3 Mean pCO₂ standard deviation between ANN-NEP 10-fold ensemble members. Ocean Station Papa is shown for reference.**

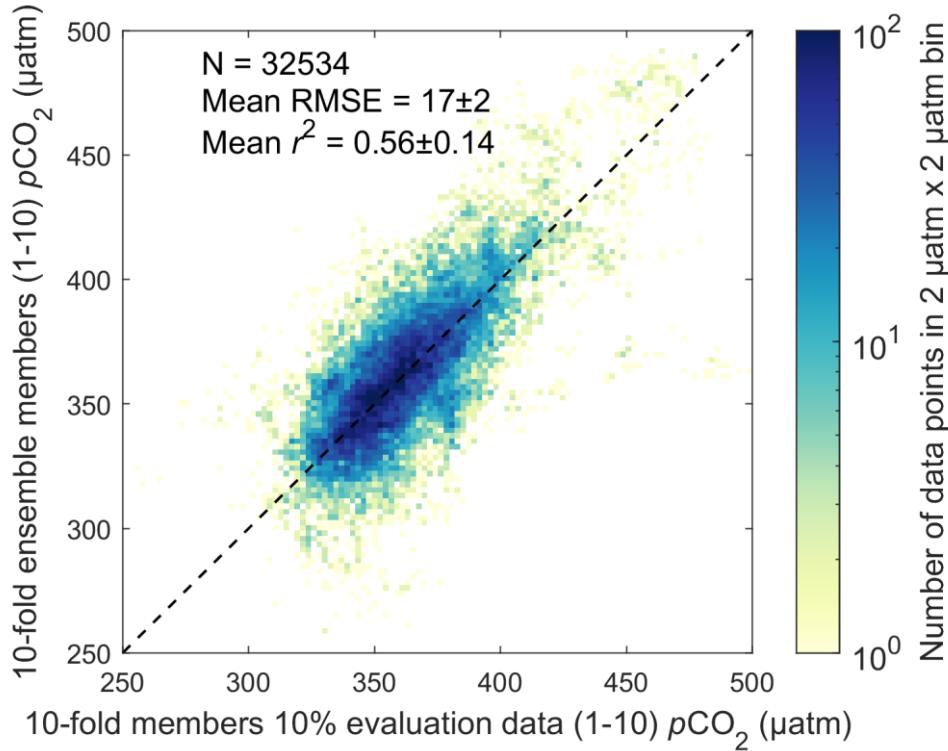


Figure S4 10-fold cross-evaluation (Section 2.4) individual ensemble member estimated $p\text{CO}_2$ against the 10% 10-fold evaluation data specific to that ensemble member. Mean root mean squared error (RMSE) and coefficient of determination (r^2) are across all individual ensemble members compared to the 10% evaluation data specific to that ensemble member. Data is binned into $2 \mu\text{atm}$ by $2 \mu\text{atm}$ bins. The dashed black line represents a perfect fit of slope ($c_1 = 1$) and intercept = 0.

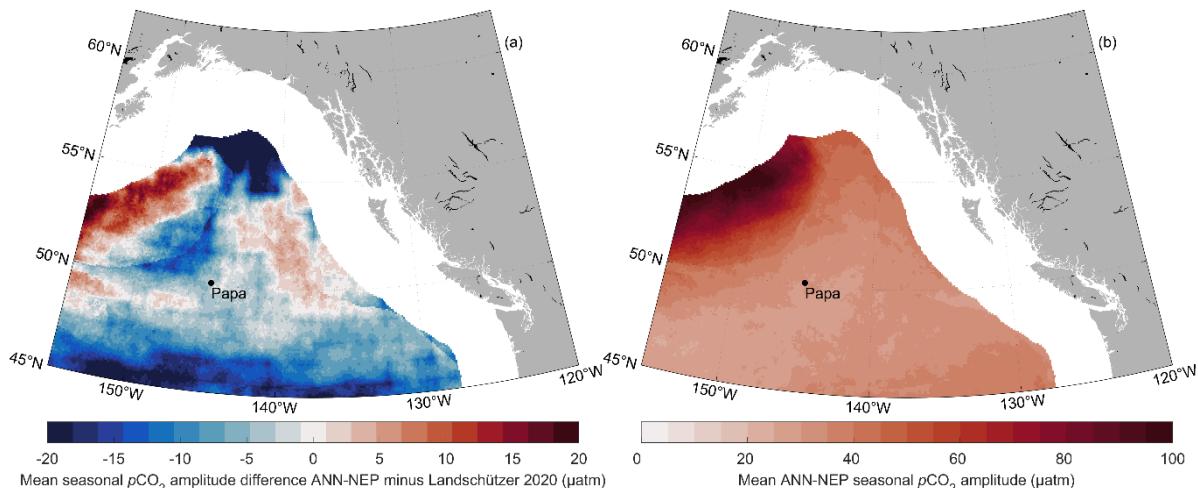


Figure S5 (a) Mean difference in the surface ocean $p\text{CO}_2$ seasonal amplitude in μatm between the ANN-NEP estimate (this study) and the Landschützer et al. (2020) global product. Positive (negative) differences indicate higher $p\text{CO}_2$ seasonal amplitude for the ANN-NEP (Landschützer et al. (2020)) estimate. The Landschützer et al. (2020) estimates have been interpolated to the

1/12°x1/12° grid of this study. (b) Mean ANN-NEP seasonal surface ocean $p\text{CO}_2$ seasonal amplitude in μatm . Ocean Station Papa is shown for reference.

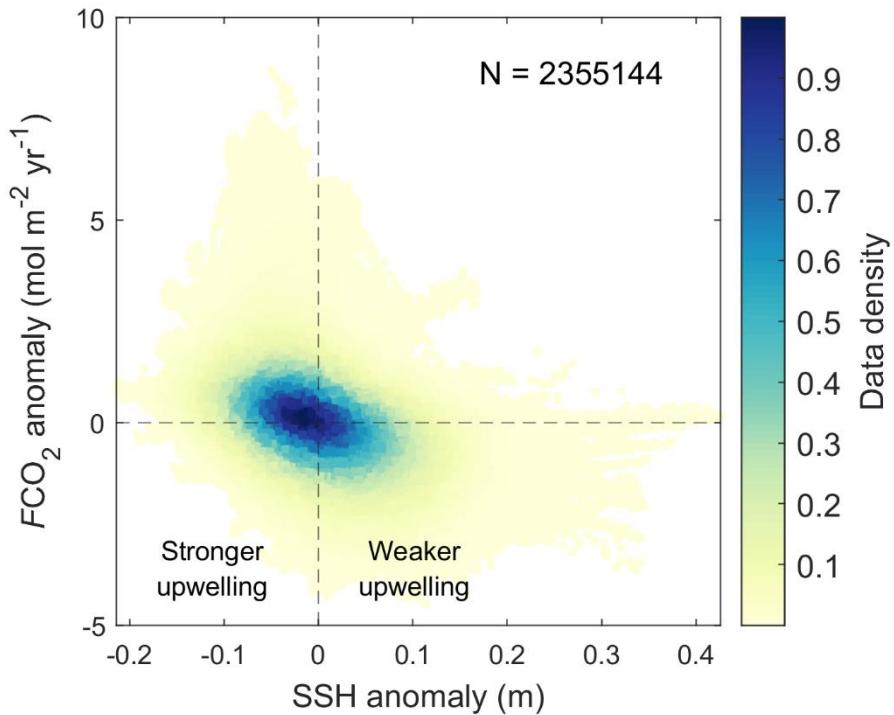


Figure S6 Property to property plot of air-sea CO_2 flux density anomalies and sea surface height (SSH) anomalies (grid cell by grid cell) in the subpolar Alaskan Gyre region of our study area (latitudes north of 52° N). Stronger (weaker) upwelling label relates to gyre upwelling strength driven by winds enhancing (damping) Ekman pumping and depressing (elevating) SSH.

Table S1 Regional high-resolution artificial neural network Northeast Pacific (ANN-NEP) pCO₂ product performance against all SOCAT pCO₂ observation data grouped by year and month. Number of observations (N), root mean squared error (RMSE), coefficient of determination (r²), and mean bias (calculated as the mean residual).

	N	RMSE	r ²	Mean bias
<i>Year</i>				
1998	3085	8.1	0.73	-1.4
1999	2184	7.5	0.91	1.4
2000	5195	8.1	0.93	0.0
2001	2404	5.7	0.96	1.2
2002	2110	7.1	0.91	1.0
2003	2526	5.2	0.84	-1.3
2004	652	4.5	0.94	1.2
2005	110	6.8	0.69	-3.6
2006	413	3.3	0.93	-2.6
2007	405	6.4	0.87	-2.8
2008	217	4.0	0.95	-1.3
2009	2751	5.0	0.94	-0.4
2010	1267	6.5	0.96	1.9
2011	980	9.1	0.87	-1.0
2012	1567	6.1	0.93	1.3
2013	1593	4.3	0.99	0.9
2014	1017	5.1	0.95	-1.5
2015	836	9.1	0.95	1.5
2016	919	6.3	0.91	-0.4
2017	511	4.7	0.89	1.0
2018	1303	5.7	0.94	1.2
2019	2051	8.1	0.93	-0.6
<i>Month</i>				
January	2731	5.2	0.97	0.7
February	2971	5.8	0.98	-0.7

March	1816	6.8	0.96	-1.0
April	2277	4.3	0.97	0.3
May	3041	5.6	0.94	0.1
June	4077	9.0	0.92	-1.1
July	3601	9.6	0.86	-0.1
August	3922	7.5	0.94	1.0
September	4121	6.6	0.93	0.2
October	2240	4.9	0.91	1.2
November	1511	3.9	0.97	-0.4
December	1788	4.4	0.97	0.8

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55 **Table S2 Regional artificial neural network Northeast Pacific pCO₂ product performance at varying resolutions against training and independent withheld SOCAT pCO₂ observations. Mean and standard deviation between lower 10th percentile (5 of 50 runs) of overfitting metric values for each resolution with varying internal data division ratios between the pCO₂ training data used by the ANN to train and internally evaluate. Number of observations (N), root mean squared error (RMSE), coefficient of determination (r²), mean absolute error (MAE), mean bias (calculated as the mean residual), and the slope of the linear regression (c₁). Courser resolution product uncertainties are also included where overall pCO₂ product uncertainty (θ_{pCO_2}) is calculated from the square root of the sum of the three squared errors: observational uncertainty (θ_{obs}), gridding uncertainty (θ_{grid}), and ANN interpolation uncertainty (θ_{map}). The 10-fold ensemble approach was not run for the courser resolution products, likely leading to a slight underestimate of overall uncertainty as ANN run randomness uncertainty (θ_{run}) was excluded.**

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<i>Training data</i>						
Resolution	N	RMSE	r²	Mean Bias	c₁	MAE
1°	2547	11.8±0.6	0.79±0.02	-0.1±0.1	0.73±0.02	8.8±0.5
1/2°	5569	10.9±0.7	0.83±0.02	0.1±0.2	0.77±0.02	7.9±0.6
1/4°	11253	11.3±0.9	0.82±0.03	0.0±0.1	0.77±0.03	8.2±0.7
1/8°	21869	12.2±1.0	0.79±0.03	0.0±0.2	0.74±0.03	8.8±0.8
1/12°	31392	10.5±1.0	0.84±0.03	0.0±0.2	0.79±0.03	7.4±0.8
<i>Independent withheld data</i>						
1°	155	11.7±0.3	0.76±0.01	-0.7±0.5	0.88±0.01	8.4±0.1
1/2°	350	11.5±0.6	0.78±0.02	0.1±0.7	0.93±0.03	8.3±0.5
1/4°	716	11.5±0.8	0.79±0.03	0.1±0.6	0.98±0.02	8.6±0.7
1/8°	1387	12.5±0.6	0.76±0.01	-0.1±1.2	0.93±0.04	9.2±0.5
1/12°	1857	11.4±0.5	0.79±0.01	2.1±0.6	0.92±0.03	8.4±0.5
<i>pCO₂ product uncertainty</i>						
	θ_{obs}	θ_{grid}	θ_{map}		θ_{pCO_2}	
1°	3.1	3.7	11.7		12.6	
1/2°	3.1	2.8	11.5		12.3	
1/4°	3.1	2.0	11.5		12.2	
1/8°	3.1	2.0	12.5		13.0	