



1 **In situ <sup>10</sup>Be modeling and terrain analysis constrain subglacial**  
2 **quarrying and abrasion at Jakobshavn Isbræ, Greenland**

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4 Brandon L. Graham<sup>1</sup>, Jason P. Briner<sup>1</sup>, Nicolás E. Young<sup>2</sup>, Allie Balter-Kennedy<sup>2</sup>, Michele  
5 Koppes<sup>3</sup>, Joerg M. Schaefer<sup>2</sup>, Kristin Poinar<sup>1</sup> and Elizabeth K. Thomas<sup>1</sup>

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7 <sup>1</sup>Department of Geology, University at Buffalo, Buffalo NY USA

8 <sup>2</sup>Lamont-Doherty Earth Observatory, Columbia University, USA

9 <sup>3</sup>University of British Columbia, Vancouver, BC, Canada

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11 *Correspondence to:* Jason P. Briner ([jbriner@buffalo.edu](mailto:jbriner@buffalo.edu))

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13  
14 **Abstract.** Glacial erosion creates diagnostic landscapes and vast amounts of sediment. Yet, knowledge about the  
15 rate by which glaciers erode and sculpt bedrock and the proportion of quarried (plucked) versus abraded material is  
16 limited. To address this, we quantify subglacial erosion rates and constrain the ratio of quarrying to abrasion during  
17 the 19th/20th century overriding of a bedrock surface fronting Jakobshavn Isbræ, Greenland, by combining  $^{10}\text{Be}$   
18 analyses, a digital terrain model, and field observations. Cosmogenic  $^{10}\text{Be}$  measurements along a 1.2-m-tall quarried  
19 bedrock step reveal a triangular wedge of quarried rock. Using individual  $^{10}\text{Be}$  measurements from abraded surfaces  
20 across the study area, we derive an average abrasion rate of  $0.13\pm 0.08\text{ mm yr}^{-1}$ . By applying this analysis across a  
21  $\sim 1.33\text{ km}^2$  study area, we estimate that the Greenland Ice Sheet quarried  $378\pm 45\text{ m}^3$  and abraded  $322\pm 204\text{ m}^3$  of  
22 material at this site. These values result in an average total erosion rate of  $0.26\pm 0.16\text{ mm yr}^{-1}$  with abrasion and  
23 quarrying contributing in roughly equal proportions within uncertainty. Additional cosmogenic  $^{10}\text{Be}$  analysis and  
24 surface texture mapping indicate that many lee steps are relict from the prior glaciation and were not re-quarried  
25 during the recent overriding event. These new observations of glacier erosion in a recently exposed landscape  
26 provide one of the first direct measurements of quarrying rates and indicate that quarrying accounts for roughly half  
27 of total glacial erosion in representative continental shield lithologies.

28

## 29 1. Introduction

30 Distinctive features of glacier erosion characterize most glaciated regions, ranging from polished bedrock  
31 surfaces to overdeepened fjords. Additionally, vast amounts of sediment are produced via glacial erosion. The  
32 Greenland Ice Sheet accounts for a disproportionate delivery of sediment to the oceans, which impacts marine  
33 ecosystems and carbon sequestration (e.g., Overeem et al., 2017). The two dominant mechanisms of glacier erosion  
34 are subglacial quarrying and abrasion (Alley et al., 2019). Quarrying occurs when bedrock blocks are episodically  
35 entrained and removed by overriding glaciers (e.g., Hallet, 1996; Iverson, 2012; Koppes, 2022). Abrasion occurs via  
36 the gradual wearing down of bedrock surfaces as rock fragments are entrained and pressed into the bed by sliding  
37 ice (Hallet, 1979; Iverson, 1990; Koppes, 2022). The rate at which each of these processes occur is dictated by rock  
38 properties (e.g., Matthes, 1930; Dühnforth et al., 2010; Krabbendam and Glasser, 2011), glacio-hydraulic factors  
39 (e.g., Egholm et al., 2012; Zoet et al., 2013; Anderson, 2014) and climate (e.g., Cook et al., 2020; Koppes 2022).  
40 Although the result of the work done by glaciers on landscapes is dramatic, observational datasets that constrain  
41 how quickly landscapes are modified by ice remain sparse (Alley et al., 2019).

42 Despite considerable challenges in observing erosional processes occurring under ice, our understanding of  
43 subglacial erosion rates continues to expand. Total glacial erosion rates (i.e., abrasion + quarrying) have been  
44 inferred using a variety of approaches (e.g., Hallet et al., 1996; Herman et al., 2021; Koppes, 2022) and are found to  
45 generally fall between  $0.01$  and  $\geq 1\text{ mm yr}^{-1}$ ; however, higher rates have been measured on short (annual to decadal)  
46 timescales (e.g., Koppes and Montgomery, 2009; Cowton et al., 2012). Attempts at separating the components of  
47 quarrying and abrasion have been made based on sediment flux measurements (e.g., Loso et al., 2004; Riihimaki et  
48 al., 2005), cosmogenic-nuclide inversions across subglacial bedforms (e.g., Briner and Swanson, 1998) and



49 theoretical considerations related to sparsely vs. intensely fractured bedrock (e.g., Anderson, 2014). To date,  
50 measurements that isolate the eroded rock volume that can be attributed to quarrying are rare.

51 Here, we quantify subglacial erosion at a site that experienced a well constrained advance-retreat cycle of  
52 Jakobshavn Isbræ, a major outlet glacier in West Greenland (Fig. 1). We partition total erosion into abrasion and  
53 quarrying by pairing cosmogenic  $^{10}\text{Be}$  measurements with analysis of a high-resolution terrain model and field  
54 mapping of bedrock surface textures. We model the accumulation of cosmogenic  $^{10}\text{Be}$  that we measured across a  
55 quarried bedrock step to reconstruct the surface profile of the removed material, and the abrasion depth in adjacent  
56 surfaces. Our data allow us to identify which bedrock steps experienced quarrying during the most recent advance of  
57 the ice versus those unaltered since the prior glaciation. We thus calculate the volume of rock removed during the  
58 recent overriding event by abrasion and by quarrying, and estimate the average erosion rate of each over the duration  
59 of glacier overriding.

60

## 61 2. Study area

62 The north and south branches of Jakobshavn Isbræ merged and extended westward ~35 km within  
63 Jakobshavn Isfjord to attain the “historical limit,” which was observed in the fjord in 1850 CE (Fig. 1; Weidick and  
64 Bennike, 2007). Adjacent to Jakobshavn Isfjord, the historical limit is represented by a prominent moraine  
65 demarcating the extent of the “historical advance,” which more or less coincides with the Little Ice Age. Prior  
66 authors calculated (1) the timing of deglaciation following the last glacial maximum to the historical limit at 7500 yr  
67 ago (Young et al., 2011; Balter-Kennedy et al., 201) and to the present ice position by 7400 yr ago, and (2) the  
68 advance (~1790 CE) and retreat (2010 AD; a duration of  $220\pm 5$  yr) of Jakobshavn Isbræ at the study site (Briner et  
69 al., 2011; Young et al. 2016; Balter-Kennedy et al., 2021; Fig. 1). It is thought that Jakobshavn Isbræ receded during  
70 the Holocene deglaciation to a position ~20 km inland of the present ice margin (Weidick et al., 1990; Kajanto et al.,  
71 2020). Our study builds on Young et al. (2016) and Balter-Kennedy et al. (2021), who utilized cosmogenic  $^{10}\text{Be}$   
72 measurements to quantify total subglacial erosion rates of the gneissic bedrock in this area (Fig. 1).

73

## 74 3. Methods

75 In August 2018, we investigated a bedrock forefield adjacent to the north branch of Jakobshavn Isbræ that  
76 emerged from beneath the ice between 2008 and 2010 based on available satellite imagery (Balter-Kennedy et al.,  
77 2021). The surface of glacially abraded and quarried bedrock exhibits pristine features of glacial erosion (Fig. 2).  
78 We measured ice-flow orientations, noted rock surface texture (variations in texture are accompanied by tonal  
79 differences in the color of rock surfaces), used drone imagery to generate a high-resolution digital terrain model, and  
80 collected samples for cosmogenic  $^{10}\text{Be}$  measurements.

81 Two stoss and lee landforms were chosen for detailed cosmogenic  $^{10}\text{Be}$  analysis, with the goal of  
82 characterizing quarrying volume and timing. We chose one landform (Location A; Fig. 3A) to (1) estimate the  
83 dimensions of the bedrock removed based on the geometry of a quarried divot, where there is a sharp transition from  
84 rough to abraded surface texture surrounding the quarried zone, and (2) use  $^{10}\text{Be}$  concentrations in samples collected  
85 from the quarried divot to reconstruct the profile of the pre-quarried surface. We created a 3D forward model of



86 cosmogenic  $^{10}\text{Be}$  production to estimate the shape of the quarried material (single or multiple blocks) at location A.  
87 The fundamental set-up of our conceptual model is shown in Figure 4. At another site (Location B; Fig. 3B), where  
88 two adjacent lee steps have different surface textures, we measured the  $^{10}\text{Be}$  concentration at the base of each step to  
89 test our hypothesis that the variations in surface texture relate to quarrying during the historical overriding versus the  
90 prior glaciation.

91

### 92 **3.1 Field sampling for $^{10}\text{Be}$ analysis**

93 At Location A, we nearly continuously sampled every ~5 cm from the top of the vertical face (0 cm, at the edge of  
94 the stoss surface) to 69 cm depth, then we skipped down to sample the base of the lee face at 115 cm. We measured  
95  $^{10}\text{Be}$  concentrations in five samples on the lee face: the top of the lee cliff (“surface”), from 12-15 cm, 30-33 cm, 65-  
96 69 cm and 110-115 cm at the base. Wide, thin samples were collected (30 cm W x 3-5 cm H x 2-4 cm D) to  
97 optimize the quartz mass within a narrow depth range and to minimize depth integration. We also collected three  
98 samples along the horizontal floor, two from within the quarried scar and one beyond the distal edge of the quarried  
99 scar from a polished surface (Fig. 3). At Location B, we collected one sample from the base of the lee cliff from  
100 each zone (Fig. 3). All samples were collected with a combination of Hilti brand angle grinder with 5-inch diameter  
101 diamond bit blades, and hammer and chisel. At all sampling locations, field observations of topographic shielding  
102 were collected using a Brunton compass. Location and elevation were collected with a GPS time averaging smart  
103 phone application with  $\pm 5$  m accuracy.

104

### 105 **3.2 Terrain analysis and surface textures**

106 Aerial imagery was collected with a DJI Mavic Pro unmanned aerial vehicle (UAV) with continuous and  
107 overlapping nadir imagery acquired using DJI smartphone app software. Maps Made Easy  
108 ([www.mapsmadeeasy.com](http://www.mapsmadeeasy.com); last access: April 26, 2023) was used to generate orthoimagery and a digital elevation  
109 model (DEM) of the field area using structure from motion principles (Graham, 2023). Mosaic imagery was used as  
110 a base layer for field mapping three surface roughness categories of the stoss and lee landforms based on the degree  
111 of freshness (1: freshly exposed surfaces with minor grain-to-grain relief and no apparent abrasion, 2: lightly  
112 abraded, 3: heavily abraded and polished). We also observed that the fresh-appearing surfaces exhibited darker  
113 surface colors, and that smoother surface textures exhibited lighter surface colors. The orientation of ice flow  
114 indicators consisting of striae, gouges, chatter marks, and crescentic gouges were measured using a compass.

115

### 116 **3.3 Beryllium-10 Laboratory Methods**

117 All physical rock processing and isolation of quartz for  $^{10}\text{Be}$  analysis was performed at the University at Buffalo  
118 Cosmogenic Isotope Laboratory (Corbett et al., 2016; Kohl & Nishiizumi, 1992). Pure quartz was processed at the  
119 Lamont-Doherty Earth Observatory cosmogenic dating laboratory following established beryllium extraction  
120 procedures. We processed eight samples from Location A, and two samples from Location B. AMS measurements  
121 of  $^{10}\text{Be}/^9\text{Be}$  were performed at the Center for Accelerator Mass Spectrometry at Lawrence Livermore National  
122 Laboratory (LLNL-CAMS), with references relative to the 07KNSTD standard of known  $^{10}\text{Be}/^9\text{Be}$  ratio of 2.85 x





123  $10^{-12}$  (Nishiizumi et al., 2007). Measured  $1\sigma$  analytical uncertainty ranged from 1.77% to 3.43% (Table S1).  
124 Apparent exposure ages were calculated using the online cosmogenic age calculator v3 (Balco et al., 2008) using the  
125 Baffin Bay  $^{10}\text{Be}$  production rate calibration data set (Balco et al., 2008; Young et al., 2013). Apparent exposure age  
126 refers to the calculated age if the samples were at the surface and experienced zero erosion. Although these apparent  
127 ages are not used in our erosion models, they are instructive in analyzing and visualizing the context of the data  
128 based on a priori assumptions.

129

### 130 **3.4 Cosmogenic Nuclide Modeling**

131 Following Balco et al. (2011), we created a 3D forward model (Graham, 2023) of cosmogenic  $^{10}\text{Be}$  production in the  
132 upper 1.2 meters of the glacially eroded bedrock at Location A using the known exposure and burial history. The  
133 history we adopt is shown in Fig. 4 and is as follows: Exposure from 7400 years ago to 1790 CE (~7200 years of  
134 exposure), burial from 1790 to 2010 CE (220 years of burial/erosion), and exposure from 2011 to 2018 CE (year of  
135 sample collection). We use the model to not only quantify the pre-quarrying surface, but also to determine the  
136 sensitivity of the specific sampling locations in the resulting divot. We thus prioritized certain sample locations from  
137 the vertical (lee) face to optimize the number of samples measured. To start, we simulated the  $^{10}\text{Be}$  concentrations  
138 using a variety of pre-quarrying surface shape geometries ranging from a rectangular cross section to a triangular  
139 cross section to a geometry that is the same as the present-day surface. End members of these pre-quarrying surface  
140 options are illustrated as the purple, green and red lines in Figure 5B. Three-dimensional representations were  
141 generated by extending the 2D surface profiles laterally. This simplified the hypothetical surface models and was  
142 justified by the presence of laterally similar surface profiles observed on the landscape. Simulated cosmic particle  
143 bombardment was prescribed based on Gosse and Phillips (2001) for azimuth and elevation angles through the  
144 simulated overlaying bedrock to each sample location.

145 We next created an inverse model to solve for the pre-quarrying surface profile at Location A. An adaptive  
146 Metropolis Hastings Markov Chain Monte Carlo (MCMC) Matlab solver package (Haario et al., 2006) was  
147 implemented to estimate the parameters necessary to minimize the chi-squared reduction of the estimated  $^{10}\text{Be}$   
148 concentrations to the measured  $^{10}\text{Be}$  concentrations. The unknown parameters were: 1) the surface profile  $x$   
149 (horizontal distance within the quarried block) inflection point, 2) the surface profile  $z$  (depth) inflection point, 3)  
150 the depth of surface abrasion applied equally across all samples, and 4) the absolute attenuation length ( $\Lambda_{\text{abs}}$ ) of the  
151 high energy neutron spallation through the rock. Acceptable a priori parameter ranges were initially prescribed  
152 (Table 1). We used the MCMC inversion to solve for the posterior parameters that correspond to the minimized  $^{10}\text{Be}$   
153 concentrations through the chi squared reduction. Due to the relatively shallow maximum sample depth (~1.2  
154 meters) and small amount of abrasion previously estimated by Balter-Kennedy et al. (2021), muon production is  
155 minimal and approximately linear across the narrow depth range. Therefore, we treated production via muons as a  
156 linear function of depth across all sample sites.

157 The surface profile was generated via a point with  $X,Z$  coordinates located within the pre-quarrying  
158 geometries prescribed above. To expand laterally, a 25-point smoothed surface interpolation (Matlab function `pcinterp`)  
159 was applied between the generated point and the edges of the quarried block (top of the scarp cliff, and the rough-to-



160 smooth transition around the perimeter of the quarried block). The initial estimate of abrasion depth for the model is  
161 based on an abrasion depth estimate from the surface sample 18JAK-Surface following the methods described in  
162 Briner and Swanson (1998) and Young et al. (2016) and is independent (but complementary) to results obtained by  
163 Balter-Kennedy et al. (2021). The absolute attenuation length ( $\Lambda_{\text{abs}}$ ) is based on the range of values estimated in  
164 Gosse and Phillips (2001). Most estimations of spallation attenuation with depth rely on the apparent attenuation  
165 length ( $\Lambda_{\text{app}}$ ) because it assumes a horizontally infinite half space, or a flat surface profile, which the sample lays  
166 beneath at some depth,  $z$  (cm). Due to the off-zenith incoming cosmic particles travelling through an increasing  
167 length of mass, an integrated value of attenuation results in the apparent attenuation (Dunai, 2010). Because our  
168 research incorporates a complex surface model, the absolute attenuation length is required to properly simulate the  
169 attenuation through varying thicknesses of rock from off-zenith angles. Our inversion results in an estimate for an  
170 absolute attenuation length of  $184 \pm 13 \text{ g cm}^{-2}$ . When converted to an apparent attenuation length, via  $\Lambda_{\text{app}} =$   
171  $(3.3/4.3) * \Lambda_{\text{abs}}$ , this becomes  $141 \pm 10 \text{ g cm}^{-2}$  and is within the range reported for the Arctic by Gosse and Phillips  
172 (2001).

173

### 174 **3.5 Terrain analysis and volume of quarried material**

175 We applied the resulting most probable profile of the quarried block at Location A (see Results) to other divots that  
176 were quarried during the historical advance. Incidentally, the shape of the quarried material is consistent with, and  
177 could largely be defined by, the non-quarried surfaces surrounding the quarried divots. Informed by results from the  
178 cosmogenic nuclide measurements at Location B and surface texture mapping, we identified which of the quarried  
179 divots were excavated during the historical advance versus glacier overriding associated with the last glaciation. The  
180 latter quarried zones were excluded from the analysis to prevent overestimating the quarried rock volume attributed  
181 to the historical overriding event. All geographical information system (GIS) analysis was performed in QGIS  
182 Desktop 3.16 Long Term Release, with all datasets transformed to NSIDC Sea Ice Polar Stereographic North. The  
183 UAV-generated DEM, nominally 0.03 m raster cell size after transformation, was re-gridded to 0.05 m cell size to  
184 which all further raster analysis was standardized to. We defined our field area based on the extent of an  
185 exceptionally bedrock-rich part of the glacier forefield, with a higher degree of surface sediment cover around its  
186 periphery. Some areas of sediment cover from within our outlined study zone are excluded because they occluded  
187 accurate identification of the underlying surface texture and are not included in area calculations of the study site.

188 We defined the quarried zones attributed to the historical advance with polygons and removed them from  
189 the DEM of the present-day surface. We then interpolated a synthetic surface across the missing holes in the DEM  
190 to recreate the pre-1790 CE surface, or “paleo-surface” using the geometry guided by results from Location A. Next,  
191 we generated a difference map between the paleo-surface DEM and the present-day surface DEM. We then summed  
192 these values from the difference map. Finally, when applying the resultant abrasion rate across the study area, we  
193 estimated a cavity area below each of the historically quarried zones (assuming a seasonally averaged cavity roof of  
194  $45^\circ$ ) and subtracted this area from the total study area.

195



196 **4. Results**

197 The  $^{10}\text{Be}$  concentrations from Location A (Table 2) decrease with depth and increase along the floor  
198 outwards from the lee cliff base (Fig. 5B). All samples result in lower apparent exposure ages than the estimated  
199 exposure duration of 7200 yr (7400 yr deglaciation minus 200 yr of subsequent burial), indicating that glacial  
200 erosion recently took place. The best fit of our forward model is a triangular wedge shape of removed material (Fig.  
201 5B & C, green). This shape is supported by the surface morphology and textures adjacent to the quarried divot.  
202 Furthermore, this triangular wedge shape is supported by the MCMC model, which reveals a slightly concave pre-  
203 quarried block surface (see “MCMC” in Fig. 5B). Additionally, our MCMC modelling using all samples at Location  
204 A yielded a surface abrasion depth of  $4.1\pm 1.9$  cm (Table 1). When using individual samples from the top (stoss) side  
205 of the lee ledge and from beyond the quarried divot, we derive abrasion depths of  $2.7\pm 1.1$  and  $5.8\pm 1.1$  cm,  
206 respectively.

207 To estimate an abraded volume of the study site, we consider several distinct abrasion rates calculated  
208 across the study area. Combining abrasion depths mentioned above with four nearby values reported by Balter-  
209 Kennedy et al. (2021) yields an average abrasion depth of  $2.78\pm 1.84$  cm and an abrasion rate of  $0.126\pm 0.084$  mm  
210  $\text{yr}^{-1}$ . Calculating the volume of material abraded requires the removal of areas where cavities existed in the  
211 immediate lee of bedrock steps. Although cavities change in size seasonally, we estimate that 12% of the field area  
212 consists of cavities assuming a  $45^\circ$  sloping cavity roof from the lip of bedrock steps. We thus calculate a volume of  
213  $322\pm 204$   $\text{m}^3$ .

214 Results from Location B show significant differences in the measured  $^{10}\text{Be}$  concentrations between the two  
215 lee steps. Sample ER2-A was collected at the base of an 85-cm-tall lee face that exhibits a fresh (non-polished)  
216 surface texture and a darker color (Fig. 3C). Its apparent exposure age of 2.3 ka (accounting for shielding using  
217 present topography) is significantly less than the expected age of  $\sim 7.2$  ka, indicating quarrying during the historical  
218 advance over the site. Sample ER2-B is from the base of a 120-cm-tall lee cliff and exhibits a lightly abraded texture  
219 and lighter color (Fig. 3B). Its apparent exposure age when accounting for shielding using present topography is 6.9  
220 ka. We attribute the difference in apparent age of sample ER2-B and its expected age of 7.2 ka to a few centimeters  
221 of abrasion, and more importantly, to a lack of quarrying during the historical advance. Thus, the results from  
222 Location B indicate that other bedrock steps that exhibit smoother, lightly abraded surfaces were quarried during the  
223 prior glaciation, and that only rougher, darker-colored surfaces in some lee faces were quarried during the historical  
224 advance.

225 Our field mapping of rock surface textures exhibits quarried zones with a mixture of rough and abraded lee  
226 surfaces. We identified 73 quarried zones classified with rough-textured, dark-colored surfaces (“historical”  
227 quarrying) and 84 quarried zones classified as having slight smoothing and lighter surface tone (quarrying during the  
228 last glaciation; Fig. 6). We calculate an area of quarried material during the historical advance of  $1,635\text{--}2,050$   $\text{m}^2$   
229 (the derivation of this range is discussed below) of the total  $13,256$   $\text{m}^2$  field area (12–15%) and a quarried volume of  
230  $378\pm 45$   $\text{m}^3$ . Using the duration of overriding during the historical advance, this equates to an equivalent quarrying  
231 rate of  $0.13\pm 0.03$   $\text{mm yr}^{-1}$  when averaged across the study site. We calculate a combined (total) eroded rock volume



232 of  $700 \pm 249 \text{ m}^3$  and total subglacial erosion rate of  $0.26 \pm 0.16 \text{ mm yr}^{-1}$ , of which 47% is attributed to abrasion and  
233 53% is attributed to quarrying.

234 Measurements of ice flow indicators, including striations, crescentic gouges and chatter marks, reveal a  
235 south ( $180^\circ$ ) to southwest ( $225^\circ$ ) ice-flow direction (Fig. 7). When sorted by type of ice flow indicator, a pattern  
236 emerges showing an evolution of flow direction during the most recent ice advance. Small striations, being the most  
237 likely to represent the final ice-flow direction before deglaciation, show the most recent ice flow direction toward  
238 the south. Crescentic gouges, chatter marks and lee face orientations, which are more likely to persist after some  
239 surface abrasion, reveal a southwesterly direction of ice flow. This shift likely represents the evolving flow direction  
240 and velocity change as ice flow over the field area increased in velocity, shifted to the southwest and thickened  
241 during the maximum phase of the historical advance. Based on the orientation of quarrying ledges and ice flow  
242 indicators, it thus appears that much of the quarrying occurred when the ice flowed southwest during what was  
243 presumably the highest ice flow velocity and thickness of the historical advance.

244

## 245 5. Discussion

246 We provide a new approach for quantifying the quarried volume of sediment across a glacial landscape and  
247 for partitioning the relative contributions of quarrying and abrasion. Due to the inherent difficulty in measuring  
248 quarrying directly, previous estimates rely on computational models or inferences made from measurements of  
249 proglacial sediment discharge (Hallet, 1996; Loso et al., 2004; Riihimaki et al., 2005; Ugelvig et al., 2018).  
250 Quarrying estimates from stream sediments (e.g., bedload) require assumptions about the portion of the suspended  
251 load that is also derived from quarrying (Riihimaki et al., 2005). Here, our measurements of quarrying volume and  
252 rate stem from the combination of in situ  $^{10}\text{Be}$  measurements and terrain analysis.

253 Our erosion rate measurements are similar to other estimates for glacial erosion in Greenland and beyond  
254 (Koppes and Montgomery, 2009; Cook et al., 2020). Our total erosion rate of  $0.32 \pm 0.09 \text{ mm yr}^{-1}$  is similar to what  
255 Balter-Kennedy et al. (2021) found at the same site using both surface  $^{10}\text{Be}$  measurements ( $0.4\text{--}0.8 \text{ mm yr}^{-1}$ ) and a  
256  $^{10}\text{Be}$  depth profile from a 4-m-deep rock core ( $0.3\text{--}0.6 \text{ mm yr}^{-1}$ ). Although these rates are lower than those found  
257 using a sediment-budget approach in southwestern Greenland ( $4.8 \pm 2.6 \text{ mm yr}^{-1}$ ; Cowton et al., 2012), they are  
258 similar to centennial-scale erosion rate estimates of  $0.29\text{--}0.34 \text{ mm yr}^{-1}$  in northwestern Greenland (Hogan et al.,  
259 2020).

260 Quarrying is inferred to be highly dependent on glaciological and lithological conditions, including bedrock  
261 hardness and fracture spacing (Dühnforth et al., 2010; Krabbendam and Glasser, 2011; Iverson, 2012). Our study  
262 site contains competent, hard crystalline rock with widely spaced fractures (on the order of several meters). Thus,  
263 based on these characteristics, we would expect abrasion to dominate at our field site (Anderson, 2014). However,  
264 despite only 12–15% of the field site by area exhibiting recent quarrying, we calculate that 53% of total glacial  
265 erosion occurred as quarrying.

266 Our MCMC results and field observations suggest that, prior to quarrying, the bedrock surface was  
267 relatively low relief, likely with wave cavities in lee locations (Zoet et al., 2013) as opposed to stepped geometries  
268 that are more often considered in theoretical studies of quarrying (e.g., Anderson et al., 1982; Hallet, 1996; Iverson,



269 2012; Anderson, 2014). Despite bedrock characteristics inhibiting quarrying, the Greenland Ice Sheet experiences  
270 significant seasonal and sub-seasonal changes in subglacial hydrology in this area (Das et al., 2008; Andrews et al.,  
271 2014), which is thought to aid quarrying processes (Anderson, 2014; Ugelvig et al., 2018). Propagating fractures that  
272 are presumed to eventually lead to failure and quarrying appear to not solely rely on pre-existing fractures in the  
273 bedrock at our study site, but could have been induced from processes related to the formation of crescentic gouges  
274 (Gilbert, 1905) that we observed in abundance in the field (Fig. 2A). That many crescentic gouge trains increase in  
275 size toward quarried ledges—with a crescentic gouge at the lip of many edges—may indicate that gouge formation is a  
276 fracture nucleation point that leads to quarrying events in this field area (Figs. 2 and 8).

277         There are uncertainties associated with calculating erosion depth, volume and rate. We do not expect  
278 uniform abrasion across the study area given the stepped nature of the terrain and localized variations in basal stress.  
279 At Site A, we find a lower abrasion depth at the lip of the divot ( $2.7\pm 1.1$  cm) than the floor beyond the quarried zone  
280 ( $5.8\pm 1.0$  cm). We do not have enough data to elucidate predictable spatial patterns of more or less abrasion across  
281 the study site; instead, we rely on an average of a number of data points that provide a useful representative abrasion  
282 depth to apply across our field area.

283         It is useful to further consider uncertainties, such as those perhaps associated with our erosion thickness,  
284 volume and rate results. Abrasion depth estimates reported here have high uncertainty due to the inherent  
285 measurement error in measuring cosmogenic nuclide concentration. An analysis of errors in Young et al. (2016) and  
286 Balter-Kennedy et al. (2021) for shallow abrasion depths shows a consistently appreciable uncertainty in relation to  
287 the low magnitudes of rock removal via abrasion. The measurement uncertainties for samples in the companion  
288 study of Balter-Kennedy et al. (2021) is  $\sim 2.5$ –3 cm, but when the estimated depth of abrasion is small and similar to  
289 mean uncertainty, the uncertainty can result in a significant range of the abraded depth. One advantage of our  
290 experiment at Location A is that multiple samples were used in the MCMC inversion, reducing the uncertainty in the  
291 estimated abrasion depth. Unfortunately, even with the added resolving power of multiple samples, the uncertainty  
292 in the abrasion depth is still 46%.

293         When converting the abrasion depth to an abrasion rate, another source of uncertainty is the duration of  
294 erosion. Whereas the timing of recent deglaciation and exposure is well constrained, the timing of burial is less well  
295 constrained. We use the overriding duration of 1790–2010 CE used in Balter-Kennedy et al. (2021), which is based  
296 on prior work in the area (Briner et al., 2011; Young et al., 2016). Although we use an absolute date range in our  
297 erosion rate calculations, the initiation glaciation at the onset of the historical advance at our study site is  
298 reconstructed, not observed, and the initiation timing of overriding would affect the calculated erosion rates. If the  
299 ice arrived decades earlier (we think this is more likely than ice arriving later than 1800 CE), our calculated erosion  
300 rates would decrease, but the ratio of abrasion to quarrying would be unaffected.

301         An additional source of uncertainty relates to the reconstructed profile of the paleo-surface slope of  
302 quarried blocks, and thus of the volume of each removed block. We use the three-dimensional nuclide production  
303 inversion of the quarried zone at Location A to guide the shape for other quarried zones. To estimate the uncertainty  
304 of each quarried block, and the cumulative uncertainty of the quarried volume across the study site, each zone was  
305 analyzed for the likelihood of having a pre-quarrying sloped, triangular profile versus a more rectangular, stair-step



306 profile. Of the 73 quarried zones, 63 were identified as triangular shape based on the localized topography around  
307 each quarried zone, as was the case at Location A that we confirmed with our cosmogenic nuclide measurements  
308 and modeling. The remaining 10 locations were identified as likely to have been rectangular blocks, and the rock  
309 volume quarried at these sites was calculated by doubling the volume generated by a triangular cross-section.

310 The uncertainty in our estimates of quarried rock volume is independent of the cosmogenic nuclide  
311 concentration. To estimate uncertainty in our manual outlining of each area of the quarried zones, a 0.5-meter buffer  
312 was extended at the edge of the floor of each quarried zone; this edge is based on changes in surface texture from  
313 rough to smooth as recorded in the high-resolution orthoimagery. The location of this transition is also dictated by  
314 the presence/absence of chatter marks/crescentic gouges, surface patina, and rock color. While many locations have  
315 a well-defined transition, 0.5 meters is an upper limit on our ability to define this boundary. The lee cliff is a well-  
316 defined feature on the landscape, and is accurately identified from the orthoimagery, with assistance using other  
317 products such as the DEM, and Hillshade/Roughness QGIS processing products. We consider our 0.5 m buffer on  
318 the extent along the quarried floor to be a conservative estimate. When used to define the volume of each block, we  
319 find that the 0.5 m buffer equates to a volume range of  $379\pm 45\text{ m}^3$ , and a quarried area of  $1842\pm 100\text{ m}^2$  (12–15% of  
320 the study area).

321 Our inverse modeling of cosmogenic nuclide production at Location A highlights the continued importance  
322 of cosmogenic nuclides in glacier erosion studies. Optimizing sampling locations to estimate the parameters of  
323 interest (surface geometry of a removed block, depth of abrasion, and attenuation length) was important for our  
324 inversion results. The sensitivity analysis to determine how samples were important in our forward model scenarios  
325 aided in sample selection for processing. The samples along the horizontal lee floor (FL1, FL2) are the most  
326 important for constraining the surface profile shape. Samples at the present-day surfaces (Surface, FL3) are the most  
327 important for constraining the depth of abrasion, while the samples collected along the vertical lee cliff are sensitive  
328 to the depth of abrasion and the attenuation length. In fact, not all samples collected along the vertical cliff were  
329 needed for the analysis, while additional samples along the floor near the quarrying-abrasion transition could have  
330 been beneficial.

331

## 332 **6. Conclusion**

333 Our pairing of cosmogenic nuclide analysis with inverse modeling of cosmogenic nuclide  
334 production through quarried material, along with topographic and morphologic analysis of a recently deglaciated  
335 bedrock landscape, provides one of the first direct observation-based estimates of glacial quarrying and partitioning  
336 of glacial erosion processes. We found that quarried volume generally matched that of abrasion despite a hard  
337 crystalline bedrock with wide fracture spacing and a low-relief surface morphology, all conspiring to limit  
338 quarrying. It seems that quarrying mostly took place via triangular wedge removal at this site. Field observations  
339 suggest clast-bed impacts evidenced by abundant crescentic gouges are a possible mechanism to nucleate quarrying  
340 events, assisted by seasonal and sub-seasonal fluctuations in subglacial water pressure. These results are a small  
341 addition to a field that needs further analysis. Yet, field data like these are important for grounding landscape  
342 evolution models with observational datasets and for providing fundamental information for understanding coupled



343 glacier-hydrology-sediment production processes. Ultimately, the results of our work invite further analysis at this  
344 field site, including testing of both theoretical and computational models of glacial erosion.

345

#### 346 **Code and data availability**

347 Code and data are available on GitHub at <https://github.com/w0gpr/Cosmo3D> (last access: April 26, 2023) and  
348 Zenodo (<https://doi.org/10.5281/ZENODO.7858913>; Graham, 2023).

349

#### 350 **Author contribution**

351 BG, JPB, NEY and AB-K designed the study and collected field data. BLG, JPB and JMS led rock sample  
352 preparation and  $^{10}\text{Be}$  analysis. BG modeled  $^{10}\text{Be}$  production, computed terrain analysis, and derived erosion results.  
353 MK, KP and EKT provided significant input throughout the course of this research. BG and JPB prepared the paper  
354 with contributions from all co-authors.

355

#### 356 **Competing Interests**

357 The contact author declares that none of the authors have any competing interests. Kristin Poinar is a member of the  
358 editorial board of The Cryosphere

359

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362 fieldwork, and Alan Hidy at Lawrence Livermore National Laboratory for beryllium isotope measurements.

363

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367

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496

#### 497 **Figure captions**

498

499 **Figure 1.** A. Greenland. B. Jakobshavn region Aug 2018; extent of Jakobshavn Isbræ (J.I.) in 1850 CE;  
500 J.If.=Jakobshavn Isfjord; nb/sb=north branch/south branch. C. Study area showing glacial erosion depths from  
501 Balter-Kennedy et al. (2021) and this study (star). D. Oblique drone photograph of the study area (point of view  
502 shown in C) showing study site A and B.

503

504 **Figure 2.** Photographs of surfaces in the study area. A) Heavily abraded and polished surface showing one of the  
505 many “gouge trains;” view to SW. B) Small lee step (approximately 20 cm high) within a heavily abraded and  
506 polished zone; note downflow from the lee cliff is a zone with more lightly abraded surfaces. C) Fresh surfaces with  
507 minor grain-to-grain relief and limited evidence for abrasion shown within quarrying ‘scars.’ D) Focus on a lee step  
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509 colored, fresh lee faces; some of the dark color in this image is from subglacial precipitate “staining.”

510

511 **Figure 3.** A) Study location A; blue area is extent of the quarried material. Stars are locations of <sup>10</sup>Be measurements.  
512 B) Study location B; pair of quarried zones with a fresh, rough lee surface (left; sample ER2-A), and smooth,  
513 abraded lee surface (right, sample ER2-B).

514

515 **Figure 4.** Concept model for <sup>10</sup>Be production and concentration for the field area. 1) Retreat of the ice sheet from  
516 the field area 7.4 ka. Erosion during the last glaciation is sufficient to remove <sup>10</sup>Be to background levels. 2) The  
517 paleo-surface is exposed to cosmic radiation during the Holocene until ice overrides at ~1790 CE, building up <sup>10</sup>Be  
518 in the upper ~2 m of bedrock. 3) Ice readvances and erodes via abrasion and quarrying during the historical  
519 advance. 4) The present-day surface is exposed in 2010 CE.

520

521

522 **Figure 5.** A) Photograph of Location A (see also Fig. 3A) showing fresh quarried face and floor. B) Cross section  
523 representation of the 3D model domain for Location A. Sample locations are marked as black boxes. The red line  
524 shows the present-day surface profile, while purple and green lines show rectangular and triangular pre-quarrying  
525 surface profiles, respectively, used in forward model. The thin gray lines are the minimized surface profiles from the



526 MCMC inversion. C) Measured (small circles) and simulated (lines in color)  $^{10}\text{Be}$  concentration of the three forward  
527 model scenarios; colors match top.

528

529 **Figure 6.** A. Orthoimage of the field area showing fractures (blue lines) and lee cliff faces (red lines). Zones  
530 quarried during the most recent glacial advance are outlined in purple. Rose diagram (inset) shows all measured ice  
531 flow indicators (in the direction of ice flow). B. Elevation difference in quarried divots assigned to block removal  
532 during the historical advance.

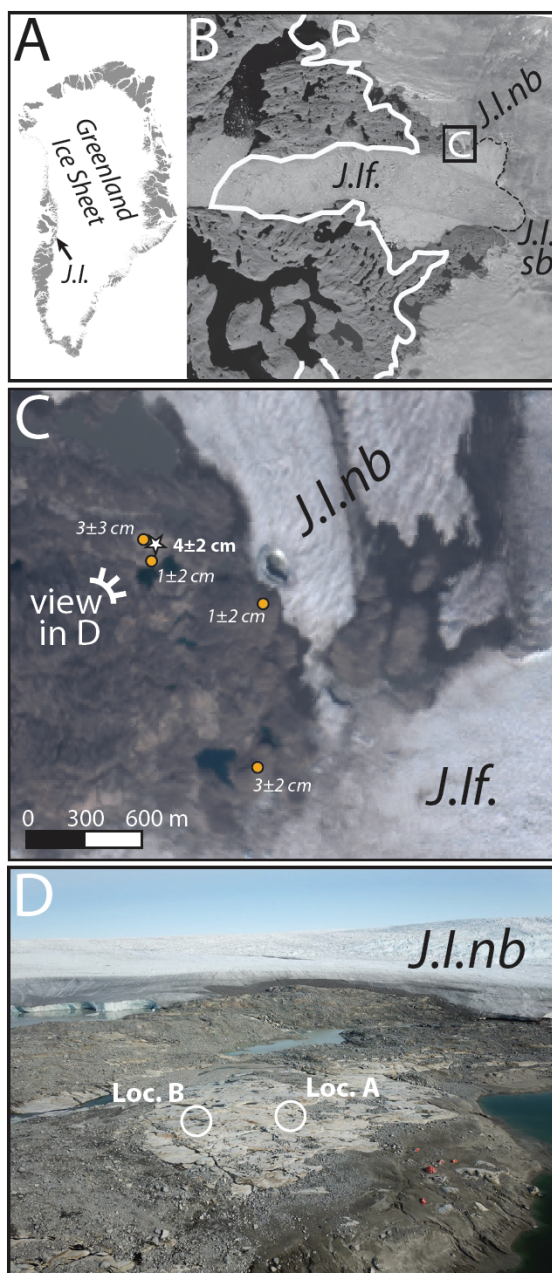
533

534 **Figure 7.** The orientation of ice-flow indicators subdivided into type. Blue lines encompass orientations from all  
535 ice-flow indicators combined (see Fig. 6).

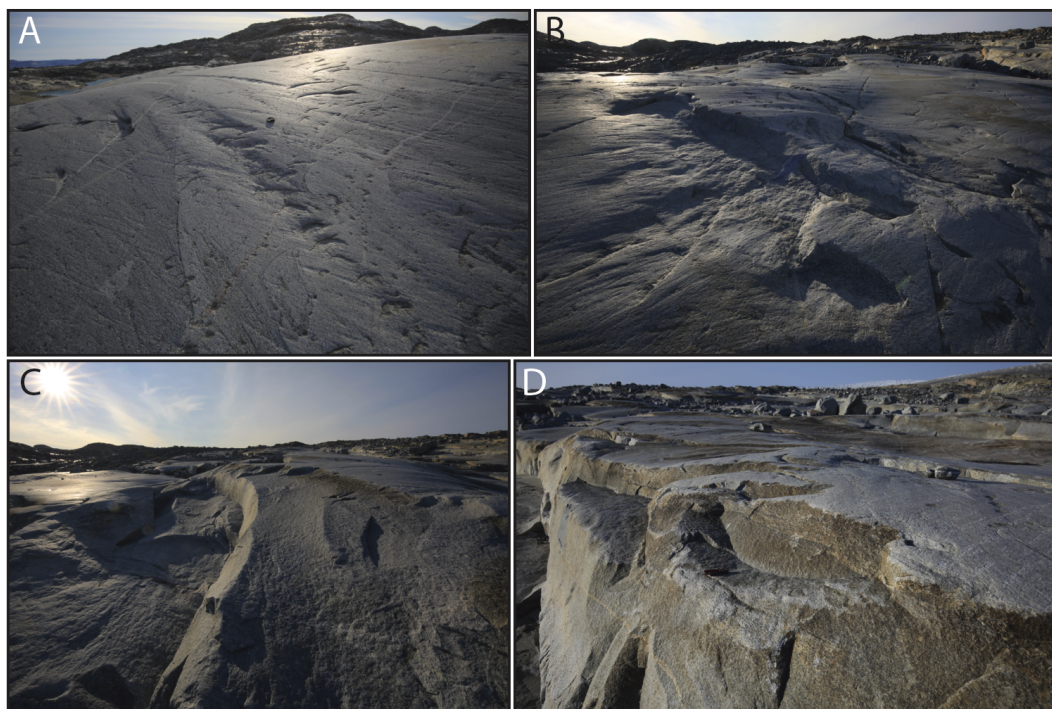
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537 **Figure 8.** Photographs showing the relationship between crescentic gouges and quarrying at the field site. A) Gouge  
538 trains leading to a lee face with evidence for quarried flakes initiated by a gouge process (ice flow from upper right  
539 to lower left). B) Example of angled (and polished) lee face from which a relatively thin flake has been quarried and  
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541

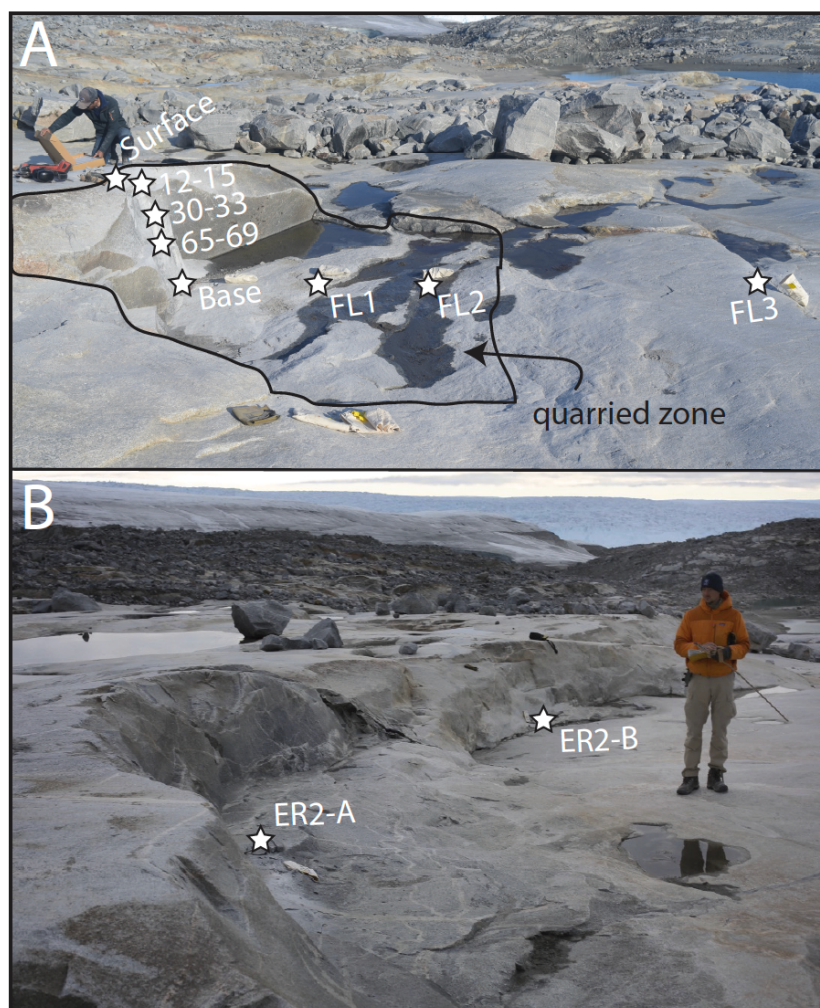


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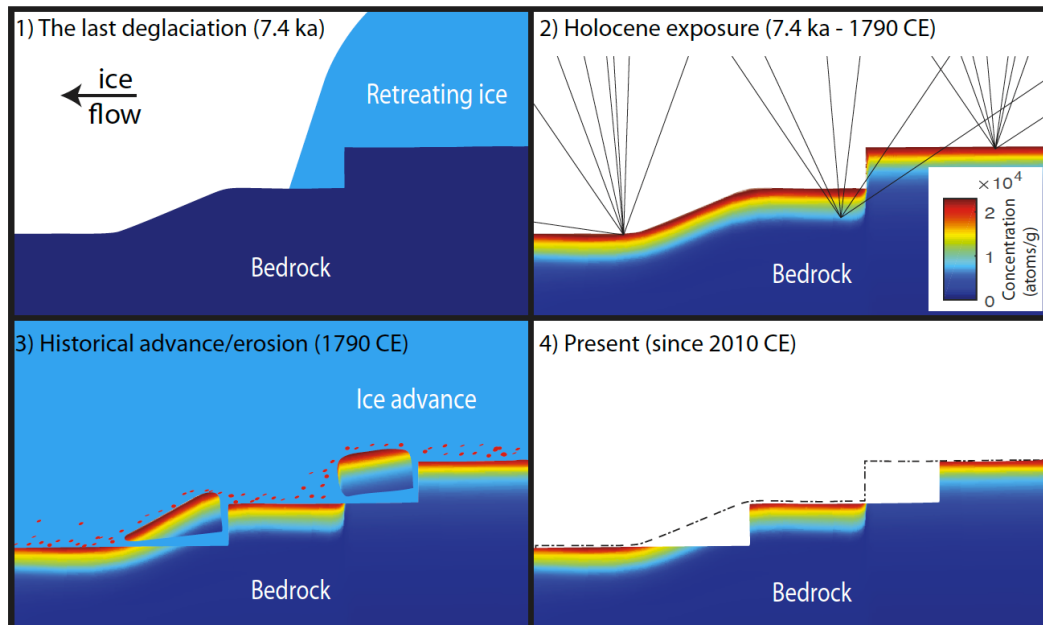


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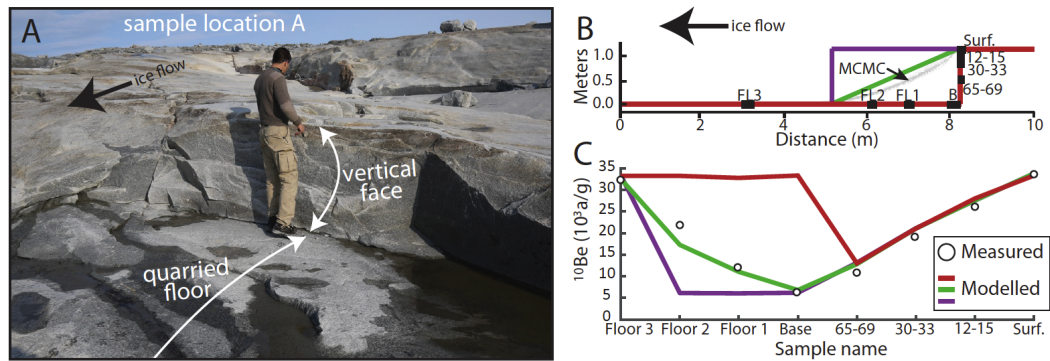


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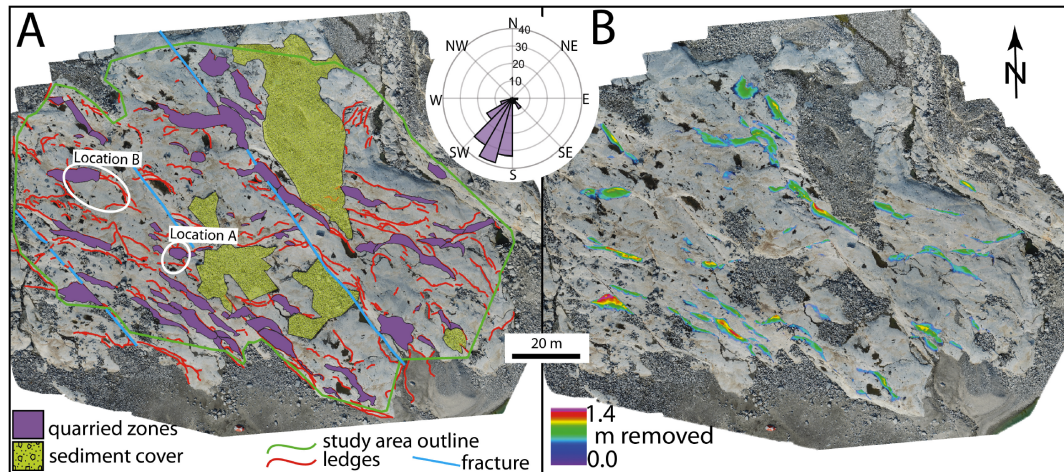


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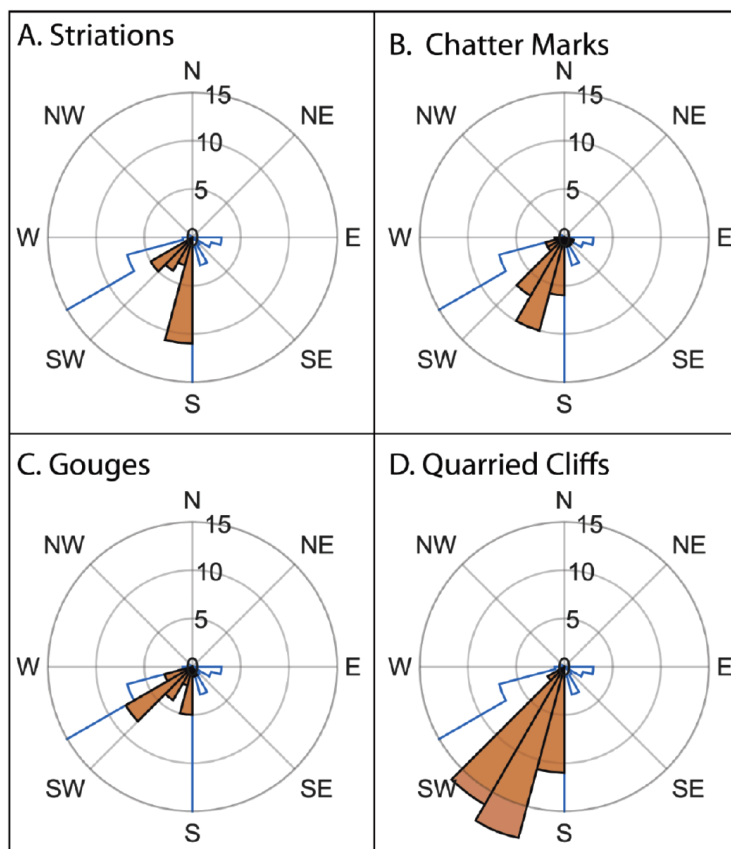




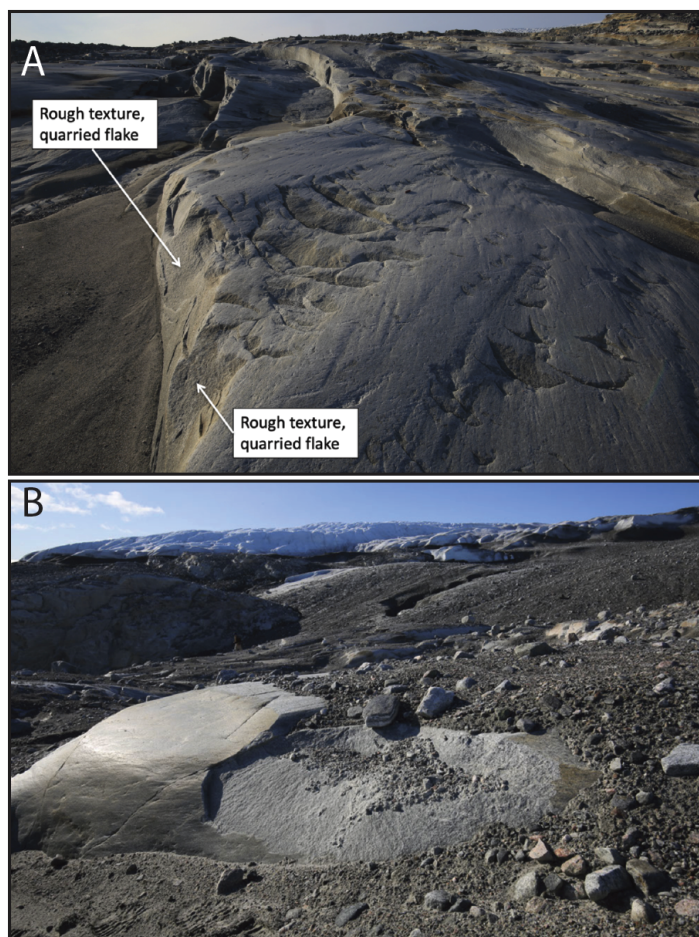
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**Table 1.** MCMC parameters *a priori* and posterior.

Parameter Name	Initial Guess	Input		Output	
		Minimum	Maximum	mean	std
xPoint	0.6	0	1	0.70353	0.18268
zPoint	0.6	0	1	0.50464	0.22515
Lambda (g cm <sup>-2</sup> )	208	150	240	184.26	12.518
Abrasion Depth (cm)	2.75	0	10	4.1375	1.9038

The *a priori* input into the MCMC inverse and the posterior output from the model runs that minimized the chi squared reduction.

**Table 2.** Beryllium-10 sample data.

Sample Name	Qtz weight (g)	Carrier added (g)	<sup>10</sup> Be/ <sup>9</sup> Be (x10 <sup>-14</sup> )	Blank corrected <sup>10</sup> Be (atoms g <sup>-1</sup> )	Apparent Age (yr)
Surface	56.821	0.1817	15.3±0.3	33,610±630	7,100±130
12-15	55.872	0.1822	11.7±0.2	26,090±490	5,510±100
30-33	60.139	0.1830	9.2±0.2	19,130±360	4,030±80
65-69	64.043	0.1818	5.5±0.1	10,730±240	2,260±50
Base	34.677	0.1820	1.8±0.1	6,210±210	1,310±40
FL1	34.663	0.1832	3.3±0.1	11,910±320	2,510±70
FL2	45.816	0.1835	8.0±0.2	21,870±500	4,630±110
FL3	33.552	0.1832	8.5±0.2	31,940±570	6,740±120
ER2-A	26.190	0.1832	2.0±0.1	9,150±310	1,930±70
ER2-B	73.360	0.1834	14.6±0.3	25,090±480	5,300±100

Location A samples were located at 69.2316°N and 49.8093°W, and Location B samples (ER2) at 69.2318°N and 49.8103°W. All samples were at an elevation of 107 meters above sea level. Sample density was 2.65 g cm<sup>-3</sup>, and the 07KNSTD Be standard was used. The Apparent Age is the St scaling apparent exposure duration, assuming no shielding.

**Table 3.** Eroded rock volume and glacial erosion rates

	Volume (m <sup>3</sup> )	Area (m <sup>2</sup> )	Rate (mm yr <sup>-1</sup> )
Abrasion	323±204	11,623*	0.13±0.08
Quarrying	378±45	1843±208	0.13±0.03
Total	700±249	13,256	0.26±0.16

\*value is 12% less than total area because of estimated area of subglacial cavities