

1 **In situ ^{10}Be modeling and terrain analysis constrain subglacial**
2 **quarrying and abrasion rates at Sermeq Kujalleq (Jakobshavn**
3 **Isbræ), Greenland**

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14
15 **Abstract.** Glacial erosion creates diagnostic landscapes and vast amounts of sediment. Yet, knowledge about the
16 rate by which glaciers erode and sculpt bedrock and the proportion of quarried (plucked) versus abraded material is
17 limited. To address this, we quantify subglacial erosion rates and constrain the ratio of quarrying to abrasion during
18 a recent, ~200-year-duration overriding of a bedrock surface fronting Sermeq Kujalleq (Jakobshavn Isbræ),
19 Greenland, by combining ^{10}Be analyses, a digital terrain model, and field observations. Cosmogenic ^{10}Be
20 measurements along a 1.2-m-tall quarried bedrock step reveal a triangular wedge of quarried rock. Using individual
21 ^{10}Be measurements from abraded surfaces across the study area, we derive an average abrasion rate of 0.13 ± 0.08
22 mm yr^{-1} . By applying this analysis across a $\sim 1.33 \text{ km}^2$ study area, we estimate that the Greenland Ice Sheet quarried
23 $378 \pm 45 \text{ m}^3$ and abraded $322 \pm 204 \text{ m}^3$ of material at this site. These values result in an average total erosion rate of
24 $0.26 \pm 0.16 \text{ mm yr}^{-1}$ with abrasion and quarrying contributing in roughly equal proportions within uncertainty.
25 Additional cosmogenic ^{10}Be analysis and surface texture mapping indicate that many lee steps are relict from the
26 prior glaciation and were not re-quarried during the recent overriding event. These new observations of glacier
27 erosion in a recently exposed landscape provide one of the first direct measurements of quarrying rates and indicate
28 that quarrying accounts for roughly half of total glacial erosion in representative continental shield lithologies.

29

30 **1. Introduction**

31 Distinctive features of glacier erosion characterize most glaciated regions, ranging from polished bedrock
32 surfaces to overdeepened fjords. Additionally, vast amounts of sediment are produced via glacial erosion. The
33 Greenland Ice Sheet accounts for a disproportionate delivery of sediment to the oceans, which impacts marine
34 ecosystems and carbon sequestration (e.g., Overeem et al., 2017). The two dominant mechanisms of glacier erosion
35 are subglacial quarrying and abrasion (Alley et al., 2019). Quarrying occurs when bedrock blocks are episodically
36 entrained and removed by overriding glaciers (e.g., Hallet, 1996; Iverson, 2012, Koppes, 2022). Abrasion occurs via
37 the gradual wearing down of bedrock surfaces as rock fragments are entrained and pressed into the bed by sliding
38 ice (Hallet, 1979; Iverson, 1990, Koppes, 2022). The rate at which each of these processes occur is dictated by rock
39 properties (e.g., Matthes, 1930; Dühnforth et al., 2010; Krabbendam and Glasser, 2011), glacio-hydraulic factors
40 (e.g., Egholm et al., 2012; Zoet et al., 2013; Anderson, 2014) and climate (e.g., Cook et al., 2020; Koppes 2022).
41 Although the result of the work done by glaciers on landscapes is dramatic, observational datasets that constrain
42 how quickly landscapes are modified by ice remain sparse (Alley et al., 2019).

43 Despite considerable challenges in observing erosional processes occurring under ice, our understanding of
44 subglacial erosion rates continues to expand. Total glacial erosion rates (i.e., abrasion + quarrying) have been
45 inferred using a variety of both direct and indirect approaches (e.g., Hallet et al., 1996; Herman et al., 2021; Koppes,
46 2022) and are found to generally fall between 0.01 and $\geq 1 \text{ mm yr}^{-1}$; however, higher rates have been measured on
47 short (annual to decadal) timescales (e.g., Koppes and Montgomery, 2009; Cowton et al., 2012). Attempts at
48 separating the components of quarrying and abrasion have been made based on sediment flux measurements (e.g.,
49 Loso et al., 2004; Riihimaki et al., 2005), cosmogenic-nuclide inversions across subglacial bedforms (e.g., Briner
50 and Swanson, 1998) and theoretical considerations related to sparsely vs. intensely fractured bedrock (e.g.,

51 Anderson, 2014). To date, measurements that isolate the eroded rock volume that can be attributed to quarrying are
52 rare.

53 Here, we quantify subglacial erosion at a site that experienced a well constrained advance-retreat cycle of
54 Sermeq Kujalleq (Jakobshavn Isbræ), a major outlet glacier in West Greenland (Fig. 1). We partition total erosion
55 into abrasion and quarrying by pairing cosmogenic ^{10}Be measurements with analysis of a high-resolution terrain
56 model and field mapping of bedrock surface textures. We model the accumulation of cosmogenic ^{10}Be that we
57 measured across a quarried bedrock step to reconstruct the surface profile of the removed material, and the abrasion
58 depth in adjacent surfaces. Our data allow us to identify which bedrock steps experienced quarrying during the most
59 recent advance of the ice versus those unaltered since the prior glaciation. We thus calculate the volume of rock
60 removed during the recent overriding event by abrasion and by quarrying, and estimate the average erosion rate of
61 each over the duration of glacier overriding.

62

63 2. Study area

64 Greenland Ice Sheet margins are presently retreating, exposing terrain that was ice-covered during the latest
65 Holocene advance that generally coincides with the Little Ice Age (Kjær et al., 2022). The north and south branches
66 of Sermeq Kujalleq merged and extended westward ~35 km within the fjord to attain the “historical limit,” which
67 was observed in the fjord in 1850 CE (Fig. 1; Weidick and Bennike, 2007). Along the fjord, the historical limit is
68 represented by a recognizable trimlines, and north and south of the fjord, prominent end moraines can be mapped to
69 demarcate the extent of the “historical advance.” In addition to the 1850 CE observation, this latest Holocene
70 advance and retreat cycle has been dated in this region with lake sediment records (Briner et al., 2010, 2011) and a
71 variety of imagery datasets (Csatho et al., 2007). The retreat of ice at our study site took place between 2008 and
72 2010.

73 During the Last Glacial Maximum, the Greenland Ice Sheet margin in the Sermeq Kujalleq sector rested on
74 the continental shelf edge in Baffin Bay far west of Disk Bugt (e.g., Hogan et al., 2016). During the last
75 deglaciation, the ice-sheet margin retreated eastward and eventually onto land on the eastern shores of Disko Bugt
76 around 10,000 years ago. Later the ice margin retreated to within (east of) the extent of ice later attained during the
77 historical limit. Prior authors calculated the timing of deglaciation to the historical limit at 7500 yr ago (Young et al.,
78 2011; Balter-Kennedy et al., 2021) and to the present ice position by 7400 yr ago. It is thought that Sermeq Kujalleq
79 receded during the Holocene deglaciation to a position ~20 km inland of the present ice margin (Weidick et al.,
80 1990; Kajanto et al., 2020). We infer that ice flowed over our study site for a duration of 220 ± 5 yr. The advance
81 phase timing stems from prior research at an ice-dammed lake (which drained in 1990) that was first dammed (based
82 on varve counts) around 1800 CE (Briner et al., 2011). As in Young et al. (2016), we estimate that the ice had
83 advanced across our study area about a decade prior to it reaching the site of the ice-dammed lake, resulting in our
84 estimate of 1790 CE as the timing of ice arrival at our study area. The retreat of ice from our study site in 2010 CE is
85 based on historical imagery (Balter-Kennedy et al., 2021). Our study builds on Young et al. (2016) and Balter-
86 Kennedy et al. (2021), who utilized cosmogenic ^{10}Be measurements to quantify total subglacial erosion rates of the
87 gneissic bedrock in this area (Fig. 1).

88

89 **3. Methods**

90 In August 2018, we investigated a bedrock forefield adjacent to the north branch of Sermeq Kujalleq at
91 69.23°N and 49.81°W. The surface of glacially abraded and quarried bedrock exhibits pristine features of glacial
92 erosion (Fig. 2). The study site contains competent, hard crystalline rock with widely spaced fractures (on the order
93 of several meters). We measured ice-flow orientations, noted rock surface texture (variations in surface roughness
94 are accompanied by tonal differences in the color of rock surfaces), used drone imagery to generate a high-
95 resolution digital terrain model, and collected samples for cosmogenic ^{10}Be measurements.

96 Two stoss and lee landforms were chosen for detailed cosmogenic ^{10}Be analysis, with the goal of
97 characterizing quarrying volume and timing. The premise of this approach requires no ^{10}Be in these surfaces
98 inherited from prior to the previous glaciation, the LGM in this case. After extensive ^{10}Be dating in the region of
99 heavily scoured surfaces, inheritance seems absent (e.g., Young et al., 2013). We chose one landform (Location A;
100 Fig. 3A) to (1) estimate the dimensions of the bedrock removed based on the geometry of a quarried divot, where
101 there is a sharp transition from rough to abraded surface roughness surrounding the quarried zone, and (2) use ^{10}Be
102 concentrations in samples collected from the quarried divot to reconstruct the profile of the pre-quarried surface. We
103 created a 3D forward model of cosmogenic ^{10}Be production to estimate the shape of the quarried material (single or
104 multiple blocks) at location A. The fundamental set-up of our conceptual model is shown in Figure 4. At another site
105 (Location B; Fig. 3B), there are two adjacent lee steps, each exhibiting a different surface roughness (one rougher,
106 one smoother). Here, we measured the ^{10}Be concentration at the base of each step to test our hypothesis that
107 different surface roughness relates to quarrying during the historical (Little Ice Age) overriding versus the prior
108 LGM glaciation.

109

110 **3.1 Field sampling for ^{10}Be analysis**

111 At Location A, we measured ^{10}Be concentrations in five samples on the lee face: the top of the lee cliff (“surface”),
112 from 12-15 cm, 30-33 cm, 65-69 cm and 110-115 cm at the base. Wide, thin samples were collected (30 cm W x 3-5
113 cm H x 2-4 cm D) to optimize the quartz mass within a narrow depth range and to minimize depth integration. We
114 also collected three samples along the horizontal floor, two from within the quarried scar (1.2 and 2.1 m from cliff
115 base) and one beyond the distal edge of the quarried scar from a polished surface (5 m from cliff base; Fig. 3). At
116 Location B, we collected one sample from the base of the lee cliff from each zone (Fig. 3). All samples were
117 collected with a combination of Hilti brand angle grinder with 5-inch diameter diamond bit blades, and hammer and
118 chisel. At all sampling locations, field observations of topographic shielding were collected using a Brunton
119 compass. Location and elevation were collected with a GPS time averaging smart phone application with ± 5 m
120 accuracy.

121

122 **3.2 Terrain analysis and surface textures**

123 Aerial imagery was collected with a DJI Mavic Pro unmanned aerial vehicle (UAV) with continuous and
124 overlapping nadir imagery acquired using DJI smartphone app software. Maps Made Easy

125 (www.mapsmadeeasy.com; last access: April 26, 2023) was used to generate orthoimagery and a digital elevation
126 model (DEM) of the field area using structure from motion principles (Graham, 2023). Mosaic imagery was used as
127 a base layer for field mapping three surface roughness categories of the stoss and lee landforms based on the degree
128 of freshness (1: freshly fractured exposed surfaces with minor grain-to-grain relief and no apparent abrasion, 2:
129 lightly abraded, 3: heavily abraded and polished). We also observed that the fresh-appearing fracture surfaces
130 exhibited darker surface colors, and that smoother surface textures exhibited lighter surface colors. The orientation
131 of ice flow indicators consisting of striae, chatter marks and crescentic gouges were measured using a compass.

132

133 **3.3 Beryllium-10 Laboratory Methods**

134 All physical rock processing and isolation of quartz for ^{10}Be analysis was performed at the University at Buffalo
135 Cosmogenic Isotope Laboratory (Corbett et al., 2016; Kohl & Nishiizumi, 1992). Pure quartz was processed at the
136 Lamont-Doherty Earth Observatory cosmogenic dating laboratory following established beryllium extraction
137 procedures. We processed eight samples from Location A, and two samples from Location B. AMS measurements
138 of $^{10}\text{Be}/^9\text{Be}$ were performed at the Center for Accelerator Mass Spectrometry at Lawrence Livermore National
139 Laboratory (LLNL-CAMS), with references relative to the 07KNSTD standard of known $^{10}\text{Be}/^9\text{Be}$ ratio of $2.85 \times$
140 10^{-12} (Nishiizumi et al., 2007). Measured 1σ analytical uncertainty ranged from 1.77% to 3.43% (Table S1).
141 Apparent exposure ages were calculated using the online cosmogenic age calculator v3 (Balco et al., 2008) using the
142 Baffin Bay ^{10}Be production rate calibration data set (Balco et al., 2008; Young et al., 2013). Apparent exposure age
143 refers to the calculated age if the samples were at the surface and experienced zero erosion. Although these apparent
144 ages are not used in our erosion models, they are instructive in analyzing and visualizing the context of the data
145 based on a priori assumptions.

146

147 **3.4 Cosmogenic Nuclide Modeling**

148 Following Balco et al. (2011), we created a 3D forward model (Graham, 2023) of cosmogenic ^{10}Be production in the
149 upper 1.2 meters of the glacially eroded bedrock at Location A using the known exposure and burial history. The
150 history we adopt is shown in Fig. 4 and is as follows: Exposure from 7400 years ago to 1790 CE (~ 7200 years of
151 exposure), burial from 1790 to 2010 CE (220 years of burial/erosion), and exposure from 2011 to 2018 CE (year of
152 sample collection). We use the model to not only quantify the pre-quarrying surface, but also to determine the
153 sensitivity of the specific sampling locations in the resulting divot. We thus prioritized certain sample locations from
154 the vertical (lee) face to optimize the number of samples measured. To start, we simulated the ^{10}Be concentrations
155 using a variety of pre-quarrying surface shape geometries ranging from a rectangular cross section to a triangular
156 cross section to a geometry that is the same as the present-day surface. End members of these pre-quarrying surface
157 options are illustrated as the purple, green and red lines in Figure 5B. Three-dimensional representations were
158 generated by extending the 2D surface profiles laterally. This simplified the hypothetical surface models and was
159 justified by the presence of laterally similar surface profiles observed on the landscape. Simulated cosmic particle
160 bombardment was prescribed based on Gosse and Phillips (2001) for azimuth and elevation angles through the
161 simulated overlaying bedrock to each sample location.

162 We next created an inverse model to solve for the pre-quarrying surface profile at Location A. An adaptive
163 Metropolis Hastings Markov Chain Monte Carlo (MCMC) Matlab solver package (Haario et al., 2006) was
164 implemented to estimate the parameters necessary to minimize the chi-squared reduction of the estimated ^{10}Be
165 concentrations to the measured ^{10}Be concentrations. The unknown parameters were: 1) the surface profile x
166 (horizontal distance within the quarried block) inflection point, 2) the surface profile z (depth) inflection point, 3)
167 the depth of surface abrasion applied equally across all samples, and 4) the absolute attenuation length (Λ_{abs}) of the
168 high energy neutron spallation through the rock. Acceptable a priori parameter ranges were initially prescribed
169 (Table 1). We used the MCMC inversion to solve for the posterior parameters that correspond to the minimized ^{10}Be
170 concentrations through the chi squared reduction. Due to the relatively shallow maximum sample depth (~ 1.2
171 meters) and small amount of abrasion previously estimated by Balter-Kennedy et al. (2021), muon production is
172 minimal and approximately linear across the narrow depth range. Therefore, we treated production via muons as a
173 linear function of depth across all sample sites, using a computationally efficient approximation of muon production
174 rates near the earth surface (Balco, 2017).

175 The surface profile was generated via a point with X, Z coordinates located within the pre-quarrying
176 geometries prescribed above. To expand laterally, a 25-point smoothed surface interpolation (Matlab function pchip)
177 was applied between the generated point and the edges of the quarried block (top of the stoss cliff, and the rough-to-
178 smooth transition around the perimeter of the quarried block). The initial estimate of abrasion depth for the model is
179 based on an abrasion depth estimate from the surface sample 18JAK-Surface following the methods described in
180 Briner and Swanson (1998) and Young et al. (2016) and is independent (but complementary) to results obtained by
181 Balter-Kennedy et al. (2021). The absolute attenuation length (Λ_{abs}) is based on the range of values estimated in
182 Gosse and Phillips (2001). Most estimations of spallation attenuation with depth rely on the apparent attenuation
183 length (Λ_{app}) because it assumes a horizontally infinite half space, or a flat surface profile, which the sample lays
184 beneath at some depth, z (cm). Due to the off-zenith incoming cosmic particles travelling through an increasing
185 length of mass, an integrated value of attenuation results in the apparent attenuation (Dunai, 2010). Because our
186 research incorporates a complex surface model, the absolute attenuation length is required to properly simulate the
187 attenuation through varying thicknesses of rock from off-zenith angles. Our inversion results in an estimate for an
188 absolute attenuation length of $184 \pm 13 \text{ g cm}^{-2}$. When converted to an apparent attenuation length, via $\Lambda_{\text{app}} =$
189 $(3.3/4.3) * \Lambda_{\text{abs}}$, this becomes $141 \pm 10 \text{ g cm}^{-2}$ and is within the range reported for the Arctic by Gosse and Phillips
190 (2001).

191

192 **3.5 Terrain analysis and volume of quarried material**

193 We applied the resulting most probable profile of the quarried block at Location A (see Results) to other divots that
194 were quarried during the historical advance. Incidentally, the shape of the quarried material is consistent with, and
195 could largely be defined by, the non-quarried surfaces surrounding the quarried divots. Informed by results from the
196 cosmogenic nuclide measurements at Location B and surface texture mapping, we identified which of the quarried
197 divots were excavated during the historical advance versus glacier overriding associated with the last glaciation. The
198 latter quarried zones were excluded from the analysis to prevent overestimating the quarried rock volume attributed

199 to the historical overriding event. All geographical information system (GIS) analysis was performed in QGIS
200 Desktop 3.16 Long Term Release, with all datasets transformed to NSIDC Sea Ice Polar Stereographic North. The
201 UAV-generated DEM, nominally 0.03 m raster cell size after transformation, was re-gridded to 0.05 m cell size to
202 which all further raster analysis was standardized. We defined our field area based on the extent of an exceptionally
203 bedrock-rich part of the glacier forefield, with a higher degree of surface sediment cover around its periphery. Some
204 areas of sediment cover from within our outlined study zone are excluded because they occluded accurate
205 identification of the underlying surface texture and are not included in area calculations of the study site.

206 We defined the quarried zones attributed to the historical advance with polygons and removed them from
207 the DEM of the present-day surface. We then interpolated a synthetic surface across the missing holes in the DEM
208 to recreate the pre-1790 CE surface, or “paleo-surface” using the geometry guided by results from Location A. Next,
209 we generated a difference map between the paleo-surface DEM and the present-day surface DEM. We then summed
210 these values from the difference map. Finally, when applying the resultant abrasion rate across the study area, we
211 estimated a cavity area below each of the historically quarried zones (assuming a seasonally averaged cavity roof of
212 45°) and subtracted this area from the total study area.

213

214 4. Results

215 The ^{10}Be concentrations from Location A (Table 2) decrease with depth and increase along the floor
216 outwards from the lee cliff base (Fig. 5B). All samples result in lower apparent exposure ages than the estimated
217 exposure duration of 7200 yr (7400 yr deglaciation minus 200 yr of subsequent burial), indicating that glacial
218 erosion took place recently. The best fit of our forward model is a triangular wedge shape of removed material (Fig.
219 5B & C, green). This shape is supported by the surface morphology and textures adjacent to the quarried divot.
220 Furthermore, this triangular wedge shape is supported by the MCMC model, which reveals a slightly concave pre-
221 quarried block surface (see “MCMC” in Fig. 5B). Additionally, our MCMC modelling using all samples at Location
222 A yielded a surface abrasion depth of 4.1 ± 1.9 cm (Table 1). When using individual samples from the top (stoss) side
223 of the lee ledge and from beyond the quarried divot, we derive abrasion depths of 2.7 ± 1.1 and 5.8 ± 1.1 cm,
224 respectively.

225 To estimate an abraded volume of the study site, we consider several distinct abrasion rates calculated
226 across the study area. Combining abrasion depths mentioned above with four nearby values reported by Balter-
227 Kennedy et al. (2021) yields an average abrasion depth of 2.78 ± 1.84 cm and an abrasion rate of 0.126 ± 0.084 mm
228 yr^{-1} . Calculating the volume of material abraded requires the removal of areas where cavities existed in the
229 immediate lee of bedrock steps. Although cavities change in size seasonally, we estimate that 12% of the field area
230 consists of cavities assuming a 45° sloping cavity roof from the lip of bedrock steps. We thus calculate a volume of
231 322 ± 204 m³.

232 Results from Location B show significant differences in the measured ^{10}Be concentrations between the two
233 lee steps. Sample ER2-A was collected at the base of an 85-cm-tall lee face that exhibits a fresh (non-polished)
234 surface texture and a darker color (Fig. 3C). Its apparent exposure age of 2.3 ka (accounting for shielding using
235 present topography) is significantly less than the expected age of ~ 7.2 ka, indicating quarrying during the historical

236 advance over the site. Sample ER2-B is from the base of a 120-cm-tall lee cliff and exhibits a lightly abraded texture
237 and lighter color (Fig. 3B). Its apparent exposure age when accounting for shielding using present topography is 6.9
238 ka. We attribute the difference in apparent age of sample ER2-B and its expected age of 7.2 ka to a few centimeters
239 of abrasion, and more importantly, to a lack of quarrying during the historical advance. Thus, the results from
240 Location B indicate that other bedrock steps that exhibit smoother, lightly abraded surfaces were quarried during
241 LGM glaciation, and that only rougher, darker-colored surfaces in some lee faces were quarried during the historical
242 advance.

243 Our field mapping of rock surface textures exhibits quarried zones with a mixture of rough fractured and
244 smooth abraded lee surfaces. We identified 73 quarried zones classified with rough-textured, dark-colored surfaces
245 (“historical” quarrying) and 84 quarried zones classified as having slight smoothing and lighter surface tone
246 (quarrying during the last glaciation; Fig. 6). Of the 73 quarried zones, 63 were identified as triangular shape based
247 on the localized topography around each quarried zone, as was the case at Location A that we confirmed with
248 cosmogenic nuclide measurements and modeling. The remaining 10 locations were identified as likely to have been
249 rectangular blocks, and the rock volume quarried at these sites was calculated by doubling the volume generated by
250 a triangular cross-section.

251 We calculate an area of quarried material during the historical advance of 1,635–2,050 m² (the derivation of
252 this range is discussed below) of the total 13,256 m² field area (12–15%) and a quarried volume of 378±45 m³.
253 Using the duration of overriding during the historical advance, this equates to an equivalent quarrying rate of
254 0.13±0.03 mm yr⁻¹ when averaged across the study site. We calculate a combined (total) eroded rock volume of
255 700±249 m³ and total subglacial erosion rate of 0.26±0.16 mm yr⁻¹, of which 47% is attributed to abrasion and 53%
256 is attributed to quarrying.

257 Measurements of ice flow indicators, including striations, crescentic gouges and chatter marks, reveal a
258 south (180°) to southwest (225°) ice-flow direction (Fig. 7). When sorted by type of ice flow indicator, a pattern
259 emerges showing an evolution of flow direction during the most recent ice advance. Small striations, being the most
260 likely to represent the final ice-flow direction before deglaciation, show the most recent ice flow direction toward
261 the south. Crescentic gouges and chatter marks, which are more likely to persist after some surface abrasion, reveal a
262 southwesterly direction of ice flow. This shift likely represents the evolving flow direction and velocity change as
263 ice flow over the field area increased in velocity, shifted to the southwest and thickened during the maximum phase
264 of the historical advance. Although the velocity of ice over the study site during the maximum phase of the advance
265 is not known, in 1985 when the site was still covered, surface velocity is in the 150-300 m yr⁻¹ range (Howat, 2020).
266 Based on the orientation of quarrying ledges and ice flow indicators, it appears that much of the quarrying occurred
267 when the ice flowed southwest during what was presumably the highest ice flow velocity and thickness of the
268 historical advance.

269 270 **5. Discussion**

271 We provide a new approach for quantifying the quarried volume of sediment across a glacial landscape and
272 for establishing the relative contributions of quarrying and abrasion. Due to the inherent difficulty in measuring

273 quarrying directly, previous estimates rely on computational models or proxy inferences made from measurements
274 of proglacial sediment discharge (Hallet, 1996; Loso et al., 2004; Riihimaki et al., 2005; Ugelvig et al., 2018).
275 Quarrying estimates from stream sediments (e.g., bedload) require assumptions about the portion of the suspended
276 load that is also derived from quarrying (Riihimaki et al., 2005). Here, our measurements of quarrying volume and
277 rate stem from the combination of in situ ^{10}Be measurements and terrain analysis.

278 Our erosion rate measurements are similar to other estimates for glacial erosion in Greenland and beyond
279 (Koppes and Montgomery, 2009; Cook et al., 2020). Our total erosion rate of $0.32 \pm 0.09 \text{ mm yr}^{-1}$ is similar to what
280 Balter-Kennedy et al. (2021) found at the same site using both surface ^{10}Be measurements ($0.4\text{--}0.8 \text{ mm yr}^{-1}$) and a
281 ^{10}Be depth profile from a 4-m-deep rock core ($0.3\text{--}0.6 \text{ mm yr}^{-1}$). Although these rates are lower than those found
282 using a sediment-budget approach in southwestern Greenland ($4.8 \pm 2.6 \text{ mm yr}^{-1}$; Cowton et al., 2012), they are
283 similar to centennial-scale erosion rate estimates of $0.29\text{--}0.34 \text{ mm yr}^{-1}$ in northwestern Greenland (Hogan et al.,
284 2020).

285 Quarrying is inferred to be highly dependent on glaciological and lithological conditions, including bedrock
286 hardness and fracture spacing (Dühnforth et al., 2010; Krabbendam and Glasser, 2011; Iverson, 2012). Based on the
287 hard nature of the bedrock with widely spaced fractures, we would expect abrasion to dominate at our field site
288 (Dühnforth et al., 2010; Anderson, 2014). However, despite only 12–15% of the field site by area exhibiting recent
289 quarrying, we calculate that 53% of total glacial erosion occurred as quarrying.

290 Our MCMC results and field observations suggest that, prior to quarrying, the bedrock surface was
291 relatively low relief, likely with wave cavities in lee locations (Zoet et al., 2013) as opposed to stepped geometries
292 that are more often considered in theoretical studies of quarrying (e.g., Anderson et al., 1982; Hallet, 1996; Iverson,
293 2012; Anderson, 2014). Despite bedrock characteristics inhibiting quarrying, the Greenland Ice Sheet experiences
294 significant seasonal and sub-seasonal changes in subglacial hydrology in this area (Das et al., 2008; Andrews et al.,
295 2014), which is thought to aid quarrying processes (Anderson, 2014; Ugelvig et al., 2018). Propagating fractures that
296 are presumed to eventually lead to failure and quarrying appear to not solely rely on pre-existing fractures in the
297 bedrock at our study site. The fracturing process, namely high clast-bed contact forces exerted by clasts embedded in
298 basal ice pressing onto the bed, leads to the formation of crescentic gouges (Gilbert, 1906; Harris, 1943;
299 Krabbendam et al., 2017) that we observed in abundance in the field (Fig. 2A). That many crescentic gouge trains
300 increase in size toward quarried ledges—with a crescentic gouge at the lip of many edges—may indicate that gouge
301 formation is a fracture nucleation point that leads to quarrying events in this field area (Figs. 2 and 8).

302 There are uncertainties associated with calculating erosion depth, volume and rate. We do not expect
303 uniform abrasion across the study area given the stepped nature of the terrain and localized variations in basal stress.
304 At Site A, we find a lower abrasion depth at the lip of the divot ($2.7 \pm 1.1 \text{ cm}$) than the floor beyond the quarried zone
305 ($5.8 \pm 1.0 \text{ cm}$). We do not have enough data to elucidate predictable spatial patterns of more or less abrasion across
306 the study site; instead, we rely on an average of a number of data points that provide a useful representative abrasion
307 depth to apply across our field area.

308 It is useful to further consider uncertainties, such as those perhaps associated with our erosion thickness,
309 volume and rate results. Abrasion depth estimates reported here have high uncertainty due to the inherent

310 measurement error in measuring cosmogenic nuclide concentration. An analysis of errors in Young et al. (2016) and
311 Balter-Kennedy et al. (2021) for shallow abrasion depths shows a consistently appreciable uncertainty in relation to
312 the low magnitudes of rock removal via abrasion. The measurement uncertainties for samples in the companion
313 study of Balter-Kennedy et al. (2021) is $\sim 2.5\text{--}3$ cm, but when the estimated depth of abrasion is small and similar to
314 mean uncertainty, the uncertainty can result in a significant range of the abraded depth. One advantage of our
315 experiment at Location A is that multiple samples were used in the MCMC inversion, reducing the uncertainty in the
316 estimated abrasion depth. Unfortunately, even with the added resolving power of multiple samples, the uncertainty
317 in the abrasion depth is still 46%.

318 When converting the abrasion depth to an abrasion rate, another source of uncertainty is the duration of
319 erosion. Whereas the timing of recent deglaciation and exposure is well constrained, the timing of burial is less well
320 constrained. We use the overriding duration of 1790–2010 CE used in Balter-Kennedy et al. (2021), which is based
321 on prior work in the area (Briner et al., 2011; Young et al., 2016). Although we use an absolute date range in our
322 erosion rate calculations, the initiation of glaciation at the onset of the historical advance at our study site is
323 reconstructed, not observed, and the initiation timing of overriding would affect the calculated erosion rates. If the
324 ice arrived decades earlier (we think this is more likely than ice arriving later than 1800 CE), our calculated erosion
325 rates would decrease, but the ratio of abrasion to quarrying, and the total depth of glacial erosion during the
326 historical advance, would be unaffected.

327 An additional source of uncertainty relates to the reconstructed profile of the paleo-surface slope of
328 quarried blocks, and thus of the volume of each removed block. We use the three-dimensional nuclide production
329 inversion of the quarried zone at Location A to guide the shape for other quarried zones. To estimate the uncertainty
330 of each quarried block, and the cumulative uncertainty of the quarried volume across the study site, each zone was
331 analyzed for the likelihood of having a pre-quarrying sloped, triangular profile versus a more rectangular, stair-step
332 profile. It is possible, perhaps likely, that at least some pre-quarried surfaces were somewhere between sloped
333 (triangular block removed) and stepped (rectangular block removed), and not one or the other.

334 The uncertainty in our estimates of quarried rock volume is independent of the cosmogenic nuclide
335 concentration. To estimate uncertainty in our manual outlining of each area of the quarried zones, a 0.5-meter buffer
336 was extended at the edge of the floor of each quarried zone; this edge is based on changes in surface texture from
337 rough to smooth as recorded in the high-resolution orthoimagery. The location of this transition is also dictated by
338 the presence/absence of chatter marks/crescentic gouges, surface patina, and rock color. While many locations have
339 a well-defined transition, 0.5 meters is an upper limit on our ability to define this boundary. The lee cliff is a well-
340 defined feature on the landscape, and is accurately identified from the orthoimagery, with assistance using other
341 products such as the DEM, and Hillshade/Roughness QGIS processing products. We consider our 0.5 m buffer on
342 the extent along the quarried floor to be a conservative estimate. When used to define the volume of each block, we
343 find that the 0.5 m buffer equates to a volume range of 379 ± 45 m³, and a quarried area of 1842 ± 100 m² (12–15% of
344 the study area).

345 Our inverse modeling of cosmogenic nuclide production at Location A highlights the continued importance
346 of cosmogenic nuclides in glacier erosion studies. Optimizing sampling locations to estimate the parameters of

347 interest (surface geometry of a removed block, depth of abrasion, and attenuation length) was important for our
348 inversion results. The sensitivity analysis to determine how samples were important in our forward model scenarios
349 aided in sample selection for processing. The samples along the horizontal lee floor (FL1, FL2) are the most
350 important for constraining the surface profile shape. Samples at the present-day surfaces (Surface, FL3) are the most
351 important for constraining the depth of abrasion, while the samples collected along the vertical lee cliff are sensitive
352 to the depth of abrasion and the attenuation length. In fact, not all samples collected along the vertical cliff were
353 needed for the analysis, while additional samples along the floor near the quarrying-abrasion transition could have
354 been beneficial.

355

356 **6. Conclusion**

357 Our pairing of cosmogenic nuclide analysis with inverse modeling of cosmogenic nuclide
358 production through quarried material, along with topographic and morphologic analysis of a recently deglaciated
359 bedrock landscape, provides one of the first direct observation-based estimates of glacial quarrying and partitioning
360 of glacial erosion processes. We found that quarried volume generally matched that of abrasion despite a hard
361 crystalline bedrock with wide fracture spacing and a low-relief surface morphology, all conspiring to limit
362 quarrying. It seems that quarrying mostly took place via triangular wedge removal at this site. Field observations
363 suggest clast-bed impacts evidenced by abundant crescentic gouges are a possible mechanism to nucleate quarrying
364 events, assisted by seasonal and sub-seasonal fluctuations in subglacial water pressure. These results are a small
365 addition to a field that needs further analysis. Yet, field data like these are important for grounding landscape
366 evolution models with observational datasets and for providing fundamental information for understanding coupled
367 glacier-hydrology-sediment production processes. Ultimately, the results of our work invite further analysis at this
368 field site, including testing of both theoretical and computational models of glacial erosion.

369

370 **Code and data availability**

371 Code and data are available on GitHub at <https://github.com/w0gpr/Cosmo3D> (last access: April 26, 2023) and
372 Zenodo (<https://doi.org/10.5281/ZENODO.7858913>; Graham, 2023).

373

374 **Author contribution**

375 BG, JPB, NEY and AB-K designed the study and collected field data. BLG, JPB and JMS led rock sample
376 preparation and ^{10}Be analysis. BG modeled ^{10}Be production, computed terrain analysis, and derived erosion results.
377 MK, KP and EKT provided significant input throughout the course of this research. BG and JPB prepared the paper
378 with contributions from all co-authors.

379

380 **Competing Interests**

381 The contact author declares that none of the authors have any competing interests. Kristin Poinar is a member of the
382 editorial board of The Cryosphere

383

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387

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544

545 **Figure captions**

546

547 **Figure 1.** A. Greenland. B. Study region August 2018; extent of Sermeq Kujalleq in 1850 CE. C. Study area
548 showing glacial erosion depths from Balter-Kennedy et al. (2021) and this study (star). D. Oblique drone photograph
549 of the study area (point of view shown in C) showing study site A and B.

550

551 **Figure 2.** Photographs of surfaces in the study area. A) Heavily abraded and polished surface showing one of the
552 many “gouge trains;” view to SW. B) Small lee step (approximately 20 cm high) within a heavily abraded and
553 polished zone; note downflow from the lee cliff is a zone with more lightly abraded surfaces. C) Fresh surfaces with
554 minor grain-to-grain relief and limited evidence for abrasion shown within quarrying ‘scars.’ D) Focus on a lee step
555 (approximately 1 m high) showing the transition from a heavily abraded stoss surface (lightly colored) to darker-
556 colored, fresh lee faces; some of the dark color in this image is from subglacial precipitate “staining.”

557

558 **Figure 3.** A) Study location A; blue area is extent of the quarried material. Stars are locations of ^{10}Be measurements.
559 B) Study location B; pair of quarried zones with a fresh, rough lee surface (left; sample ER2-A), and smooth,
560 abraded lee surface (right, sample ER2-B).

561

562 **Figure 4.** Concept model for ^{10}Be production and concentration for the field area. 1) Retreat of the ice sheet from
563 the field area 7.4 ka. Erosion during the last glaciation is sufficient to remove ^{10}Be to background levels. 2) The
564 paleo-surface is exposed to cosmic radiation during the Holocene until ice overrides at ~1790 CE, building up ^{10}Be
565 in the upper ~2 m of bedrock. 3) Ice readvances and erodes via abrasion and quarrying during the historical
566 advance. 4) The present-day surface is exposed in 2010 CE.

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Figure 5. A) Photograph of Location A (see also Fig. 3A) showing fresh quarried face and floor. B) Cross section representation of the 3D model domain for Location A. Sample locations are marked as black boxes. The red line shows the present-day surface profile, while purple and green lines show rectangular and triangular pre-quarrying surface profiles, respectively, used in forward model. The thin gray lines are the minimized surface profiles from the MCMC inversion. C) Measured (small circles) and simulated (lines in color) ^{10}Be concentration of the three forward model scenarios; colors match top.

Figure 6. A. Orthoimage of the field area showing fractures (blue lines) and lee cliff faces (red lines). Zones quarried during the most recent glacial advance are outlined in purple. Rose diagram (inset) shows all measured ice flow indicators (in the direction of ice flow). B. Elevation difference in quarried divots assigned to block removal during the historical advance.

Figure 7. The orientation of ice-flow indicators subdivided into type. Blue lines encompass orientations from all ice-flow indicators combined (see Fig. 6).

Figure 8. Photographs showing the relationship between crescentic gouges and quarrying at the field site. A) Gouge trains leading to a lee face with evidence for quarried flakes initiated by a gouge process (ice flow from upper right to lower left). B) Example of angled (and polished) lee face from which a relatively thin flake has been quarried and removed.

Table 1. MCMC parameters a prior and posterior.

Parameter Name	Initial	Input		Output	
	Guess	Minimum	Maximum	Mean	Std
xPoint	0.6	0	1	0.70353	0.18268
zPoint	0.6	0	1	0.50464	0.22515
Lambda (g cm ⁻²)	208	150	240	184.26	12.518
Abrasion Depth (cm)	2.75	0	10	4.135	1.9038

The *a priori* input into the MCMC inverse and the posterior output from the model runs are those that minimized the chi squared reduction.

Table 2. Beryllium-10 sample data.

Sample Name	Sample thickness (cm)	Quartz Weight (g)	Carrier (g)	¹⁰ Be/ ⁹ Be (x10 ⁻¹⁴)	Blank Corrected ¹⁰ Be (atoms g ⁻¹)	Apparent Age (yr)
Surface	1.5	56.821	0.1817	15.3±0.3	33610±630	7100±130
12-15	3.0	55.872	0.1822	11.7±0.2	26090±490	5510±100
30-33	3.0	60.139	0.1830	9.2±0.2	19130±360	4030±80
65-69	4.0	64.043	0.1818	5.5±0.1	10730±240	2260±50
Base	5.0	34.677	0.1820	1.8±0.1	6210±210	1310±40
FL1	1.5	34.663	0.1832	3.3±0.1	11910±320	2510±70
FL2	1.5	45.816	0.1835	8.0±0.2	21870±500	4630±110
FL3	1.5	33.552	0.1832	8.5±0.2	31940±570	6740±120
ER2-A	5.0	26.190	0.1832	2.0±0.1	9150±310	1930±70
ER2-B	5.0	73.360	0.1834	14.6±0.3	25090±480	5300±100

Location A samples were located at 69.2316°N and 49.8093°W. Location B samples (ER2) at 69.2318°N and 49.8103°W. All samples were at an elevation of 107 meters above sea level.

Sample density is 2.65 g cm⁻³, and the 07KNSTD Be standard was used. The apparent age is the St scaling apparent exposure duration, assuming no shielding.

Table 3. Eroded rock volume and glacial erosion rates.

	Volume (m ³)	Area (m ²)	Rate (mm yr ⁻¹)
Abrasion	323±204	11,623*	0.13±0.08
Quarrying	378±45	1843±208	0.13±0.03
Total	700±249	13,256	0.26±0.16

*value is 12% less than total area because of estimated area of subglacial cavities















