

Response to EGUSPHERE-2023-637 Review

WeiHuang , Lei Liu , BinYang , Shuai Hu , Wanying Yang , Zhenfeng Li , Wantong Li and Xiaofan Yang

Dear editor,

We thank you very much for processing our manuscript entitled “Retrieval of temperature and humidity profiles from ground-based high-resolution infrared observations using an adaptive fast iterative algorithm” (ID: EGUSPHERE-2023-637). We also thank the referees for their comments, which are all valuable and very helpful for improving our work. We have studied comments carefully and have made extensive modifications which are marked in a smaller font size in our revised submission manuscript. We have addressed the issues pointed out by the referees, to which we respond in detail below. We hope that the referees will find our responses satisfactory, and we are willing to further revise the manuscript regarding any additional suggestions that the referees may have. Please find below the referees’ comments in light blue with our responses after each comment.

Referee #1

Dear Referee:

We would like to express our sincere appreciation for your careful reading and invaluable comments to improve this paper. We have studied carefully on these detailed comments. They are helpful to improve our manuscript. After deep consideration of your valuable comments, we substantially modify the manuscript. Corresponding changes are marked in a smaller font size in the modified manuscript. Point-by-point responses to your comments are seriously completed for your consideration. If there are still severe issues with our manuscript, please let us know, and we will try our best to modify our article. Thanks for your time!

Major comments:

C1. The value of K_Index determines the iterative process of Jacobians. However, the threshold of K_Index is chosen by the distributions of the K_Index values for each iteration, which is dependent on the datasets used in the experiment. This affects the suitability of the fast retrieval algorithm. The authors should point this out. More discussions on this inadequacy of the proposed algorithm should be provided in Section 3.3.3 or in the conclusions.

R1: Thanks for the suggestion. The value of K_Index is dependent on the height range of atmospheric profiles and the atmospheric constituents that intended to retrieve. They are presented ‘as is’ and are not intended to be directly applied to the retrieval of different atmospheric profiles or instruments. The discussion of this issue is provided in Section 3.2.3 of the revised manuscript.

For your convenience, the corresponding part in our revised submission is given as follows:

It should be noted that the threshold of K_Index used in the Fast AERIoe algorithm is dependent on the datasets used in the retrieval. They are presented ‘as is’ and are not intended to be directly applied by the reader. We encourage readers to develop their own indicator to reduce the recalculation of Jacobians based on the atmospheric constituents they intend to retrieve.

C2. Figure 3: I am confused by the X-axis in the two panels. The authors said that IC and DFS change with K_Index are denoted with black lines, while the X-axis represents K_index is red. The illustrations of Figure 3 seems elusive to me and thus further clarification is needed in the figure

caption or in the main text.

R2: We appreciate the suggestion. We admit that the logic here is indeed a bit confusing. Some modifications have been made to Fig 3 and the analysis of this picture. The indicator “IC” was changed to Shannon Information Content (SIC) to be consistent with the work described by Turner and Löhnert (2014). The change of K_Index with factor γ was removed since it may lead to some confusion and occasional misunderstanding. Fig 3 and the analysis of this figure were reworked. Thanks for the suggestion again. We added the detailed discussion in the revised manuscript.

For your convenience, the corresponding revised part in our revised submission is given as follows:

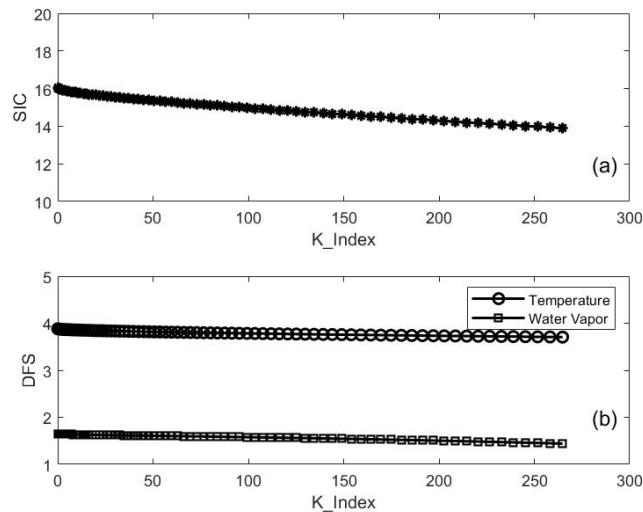


Figure 2. (a) The change of *SIC* with *K_Index*. (b) The change of *DFS* with *K_Index* for temperature (unfilled circles) and water vapor (open squares), respectively.

The values of *K_Index*, which covers most of the *K_Index* during AERIoe retrieval process (ranged from 0 to 260, see Fig. 3), were obtained by multiplying the a prior profile by different scale factors. The atmosphere dependent **K** were computed by LBLRTM with the prior profiles above, and *SIC* and *DFS* were calculated using equations (3) and (4) with different Jacobians, respectively. Fig. 2 shows the curve of *SIC* and *DFS* changed with *K_Index*. Both of them change slowly with *K_Index*, with the variation of *SIC* within 13.46% (from 13.89 to 16.05), and *DFS* within 4.38% (from 3.71 to 3.88) for temperature and within 12.73% (from 1.44 to 1.65) for water vapor, which demonstrates that *SIC* and *DFS* remain almost unchanged as *K_Index* increases on the condition that the value of *K_Index* is small. This provides an effective means to improve the retrieval speed of AERIoe by recalculating **K** selectively when **X** is not changing much or *K_Index* is small. This could be achieved by comparing the value of *K_Index* and its threshold at each iteration to determine whether **K** is recalculated or not.

C3. 4.2.3 Accuracy: The smoothing error cannot be ignored when retrieved profiles are compared directly to radiosondes. Thus, the radiosonde observations should be smoothed with the averaging kernel to minimize the vertical representativeness error.

R3: Thanks for pointing this problem out. We've made two modifications to Fig.9. One is that the radiosonde observations have been smoothed with the averaging kernel **A** to reduce the vertical representativeness errors.

$$\mathbf{X}_{\text{sonde}}^{\text{smoothed}} = \mathbf{A}(\mathbf{X}_{\text{sonde}} - \mathbf{X}_a) + \mathbf{X}_a$$

Another modification is the transformation of water vapor into the form of $\log(\text{ppmv})$. This is due to the fact that the unit of **K** output by LBLRTM is $\log(\text{ppmv})$ during the retrieval, which means that

the adjustment of the iterative profile is also in the form of \log (ppmv). Therefore, we believe that it is more reasonable to compare water vapor profiles of different retrieval algorithms in the form of \log (ppmv).

For your convenience, the corresponding revised part in our revised submission is given as follows:

... $\mathbf{X}_{sonde}^{smooth}$ is radiosonde observations which are smoothed with the averaging kernel A by the following multiplication to reduce the vertical representativeness errors

$$\mathbf{X}_{sonde}^{smooth} = \mathbf{A}(\mathbf{X}_{sonde} - \mathbf{X}_a) + \mathbf{X}_a, \quad (10)$$

The BIAS and RMSE of AERIoe and Fast AERIoe are calculated for 826 sets of samples using the above equations within the altitude range of 0-3 km, and the results are shown in Fig. 8.

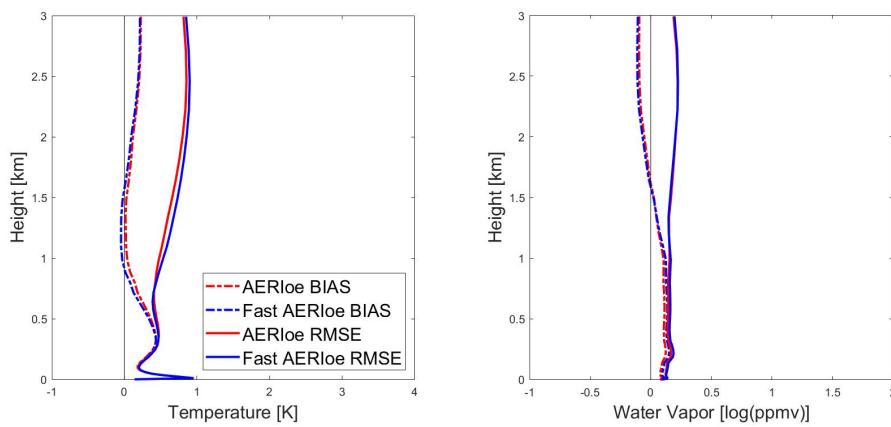


Figure 8. Bias (solid curves) and RMSE (dashed curves) profiles for the comparisons of AERIoe (red curves) and Fast AERIoe (blue curves) retrievals with radiosondes. (Left) Temperature profile, (right) Water Vapor profiles.

C4. One subject where the manuscript lacks is the discussion on the comparison between the retrieval time and the temporal resolution of AERI spectrum. If most of the AERIoe's retrieval time exceeds the temporal resolution, then the importance of the fast retrieval algorithm will be highlighted and vice versa. Please discuss this issue.

R4: Thank you for pointing out the problem. The comparison of the retrieval time with the temporal resolution of AERI spectrum has been discussed.

For your convenience, the corresponding revised part in our revised submission is given as follows:

The average retrieval time of Fast AERIoe for the 826 cases used in the study is 3.69 min, which is more than 50% shorter than that of AERIoe, with an average retrieval time of 8.96 min, which is beyond the temporal resolution (about 8 min) of AERI observations. All of the samples of AERIoe consumed more than 8 minutes, while only 10 cases exceeded the temporal resolution of AERI for Fast AERIoe algorithm. Note that the retrieval time is dependent on the computing platform and the method used to compute Jacobians and are not intended to be directly applied by the reader.

Minor comments:

C5. For the title, may be “Ground-based infrared hyperspectral retrievals of temperature and humidity profile based on Adaptive Fast Iterative Algorithm” is better.

R5: Thanks for the suggestion. The title has been modified as follows:

Retrieval of temperature and humidity profiles from ground-based high-resolution infrared observations using an

adaptive fast iterative algorithm

C6.Line10: “due to” is usually not placed at the beginning of a sentence

R6: Thank you for pointing out the problem. The sentence in line10has been rephrased.

For your convenience, the corresponding revised part in our revised submission is given as follows:

Various retrieval algorithms have been developed for retrieving temperature and water vapor profiles from the Atmospheric Emitted Radiance Interferometer (AERI) observations. The physical retrieval algorithm, named AERI Optimal Estimation (AERIoe), outperforms other retrieval algorithms in many aspects except the retrieval time, which is significantly increased due to the complex radiative transfer process

C7.Line12: “part” -> “step”; Line15: “is” -> “was”; Line17: suggest revising to “resulting in an average retrieval time reduction from 8.96 min to 3.69 min” instead of “with the average retrieval time reduced from 8.96 min to 3.69 min”; Line41: “FTIR” -> “The FTIR instrument”; Line45: “which is more advantageous” can be revised to “which makes it more advantageous”.

R7: Thanks for the constructive suggestions to improve our manuscript. We have modified the manuscript as suggested by the reviewers.

For your convenience, the corresponding revised part in our revised submission is given as follows:

The calculation of the Jacobian matrix is the most computationally intensive step of the physical retrieval algorithm.

The performance of the algorithm was evaluated using synthetic ground-based infrared spectra observations.

... resulting in an average retrieval time reduction by 58.82%.

The FTIR instrument observes near-infrared and mid-infrared high-resolution solar spectra, which are mainly used to retrieve water vapor ...

... which makes it more advantageous in detecting thermodynamic profiles.

C8.Line57: this sentence should be reworked

R8: Thanks for the suggestion. The sentence in line57 has been rephrased.

For your convenience, the corresponding revised part in our revised submission is given as follows:

However, the AERIprof algorithm has several significant drawbacks, such as its high dependence on the first-guess profile and inability to provide uncertainty estimates for retrieval results.

Referee #2

Dear Referee:

We would like to express our sincere appreciation for your professional review work and valuable comments that greatly helped to improve our manuscript. After deep consideration of your valuable comments, we substantially modify the manuscript. Corresponding changes are highlighted within the document by using smaller font size. Point-by-point responses to your comments are seriously completed for your consideration. If there are still severe issues with our manuscript, please let us know, and we will try our best to modify our article. Thanks for your time!

Overall:

C1. The authors state that the new method results in equivalent retrieval accuracy. However, for water vapor, the bias increase appears to be up to about 40% (0.7 to 0.9), and the RMS increase up to

~12%. This does not seem to me to be comparable retrieval accuracy.

R1: Thank you for pointing this problem out. We agree with the referee that retrieval accuracy of the new method is not comparable to that of AERIoe. However, we believe that the retrieved profiles rather than the retrieval accuracy of the two algorithms are comparable. This is because the increment of BIAS is much smaller than the value of the retrieved water vapor profile itself, and this increment had little impact on the retrieval results of AERIoe. We have modified the statement as “The retrieval results of the fast retrieval model are comparable to that of AERIoe.”. Details for this modification are discussed in the response to comments on lines 346 - 348.

C2. The authors need to clarify the scope of the work and fix the errors, typos and unclear parts of the paper. Is the novelty of this work just in implementing the k_index and updating the Jacobian less often, or did they also introduce different formulations, methodology, etc? Given that this work follows closely from Turner and Lohnert (2014), the authors should make it clear what is the same as in that prior work by referencing it as needed, avoiding repeating details from it except as necessary, avoiding typos/errors when they do paraphrase from that work, and discussing clearly what is novel in this work. For example, Eqn (1) differs from prior work (and from Rodgers (2000)) in that X_a is replaced with X_0 . Is this intentional, and if so, why? More examples of specific issues follow.

R2: Thanks for the constructive suggestions to improve our manuscript. Sections 3.1 and 3.2, which are similar to the work from Turner and Lohnert (2014), have been removed from the manuscript and the descriptions of Fast AERIoe configurations that differ from AERIoe have been added in the paragraph between line142 and line153.

The variable representing the prior profile in Equation (1) in the manuscript is incorrect, and we are really sorry for our careless mistakes. We have replaced X_0 with X_a in Eqn (1).

Other comments:

C3. Did the authors modify the AERIoe code itself or did they develop a new code base from scratch? Please state in the Data availability if/where/how the fast AERIoe code is available. (Proprietary or open source? How does one obtain it?).

R3: Thank you for the comments. The code for the Fast AERIoe algorithm was developed by ourselves written in MATLAB language. The code for recalculating Jacobians are not publicly available at this time but may be obtained from the authors upon reasonable request.

For your convenience, the corresponding part in our revised submission is given as follows:

Data availability. The data used in the manuscript (including AERI, radiosonde, etc) are available from the ARM Data Archive (<https://adc.arm.gov/discovery/#/>, accessed on 19 January 2022). The code for recalculating Jacobians are not publicly available at this time but may be obtained from the authors upon reasonable request.

C4. Given that the main goal is to reduce the computation time, specifics in that regard are needed. Has the code timing been analyzed and what are the bottlenecks? I assume calculation of the Jacobian is the main bottleneck; is that the case?

R4: We appreciate the suggestion. The code timing has been analyzed both for Fast AERIoe and AERIoe if we understand correctly. The code for the retrieval algorithm was divided into several sections, the time consumed by each section has been analyzed and given in the table bellow, of which the sections denoted with superscript “**” indicate that K is not recalculated during Fast AERIoe retrieval process.

Sections	AERIoe	Fast AERIoe
preparation	0.29	0.22

iteration 1	inversion	0.29	0.22
	recalculation of $F(\mathbf{X})$	17.11	16.69
iteration 2	recalculation of \mathbf{K}	68.76	70.27
	inversion	0.31	0.27
	recalculation of $F(\mathbf{X})$	17.18	17.04
iteration 3	recalculation of \mathbf{K}	70.55	0.00
	inversion	0.22	0.22
	recalculation of $F(\mathbf{X})$	17.71	16.36
iteration 4	recalculation of \mathbf{K}^*	70.07	0.00
	inversion	0.25	0.21
	recalculation of $F(\mathbf{X})$	16.97	17.38
iteration 5	recalculation of \mathbf{K}^*	68.93	0.00
	inversion	0.21	0.25
	recalculation of $F(\mathbf{X})$	16.08	15.08
iteration 6	recalculation of \mathbf{K}^*	68.23	0.00
	inversion	0.24	0.24
iteration final	recalculation of $F(\mathbf{X})$	15.91	18.45
	recalculation of \mathbf{K}^*	68.11	0.00
	inversion	0.28	0.23

From the table, we can find that the recalculation of $F(\mathbf{X})$ and \mathbf{K} consumed an immense amount of time in the retrieval process of AERIoe, and the latter is the most time consuming section. Therefore, by reducing the recalculation of \mathbf{K} , the retrieval time of Fast AERIoe is greatly reduced compared to AERIoe.

For your convenience, the corresponding part in our revised submission is given as follows:

The codes for the retrieval algorithm are written in MATLAB language and runs on a Lenovo Aircross 510P computer, of which the CPU is Intel Core i7-7700 and the operating system is Ubuntu 14.04. To analyze the code timing of the retrieval algorithm, the code was divided into the following sections: preparation, iteration 1, iteration 2, iteration 3,... and iteration final. The preparation section mainly consists of atmosphere construction, observation vector construction and pre-calculated variables importation. The iteration sections include the recalculation of \mathbf{K} and $F(\mathbf{X})$ and the inversion using equation (1). Note that iteration 1 does not need to calculate \mathbf{K} and $F(\mathbf{X})$ because the prior profile \mathbf{X}_a is fixed (mean value of the atmosphere), and the \mathbf{K} and $F(\mathbf{X})$ associated with it are pre-calculated. The time consumed by each section was analyzed both for AERIoe and Fast AERIoe, results for an arbitrarily selected case are provided in Table 2. The recalculation of $F(\mathbf{X})$ and \mathbf{K} consumed an immense amount of time in the retrieval process of AERIoe, and the latter is the most time consuming section. Therefore, by reducing the recalculation of \mathbf{K} , the retrieval time of Fast AERIoe is greatly reduced compared to AERIoe.

Table 2. List of time consumption (units: s) by the sections of AERIoe and Fast AERIoe. The sections denoted with superscript “*” indicate that \mathbf{K} is not recalculated during Fast AERIoe retrieval process.

Sections	AERIoe	Fast AERIoe
preparation	0.29	0.22
iteration 1	inversion	0.29
iteration 2	recalculation of $F(\mathbf{X})$	17.11
	recalculation of \mathbf{K}	68.76

	inversion	0.31	0.27
iteration 3	recalculation of $F(\mathbf{X})$	17.18	17.04
	recalculation of \mathbf{K}	70.55	0.00
	inversion	0.22	0.22
iteration 4	recalculation of $F(\mathbf{X})$	17.71	16.36
	recalculation of \mathbf{K}^*	70.07	0.00
	inversion	0.25	0.21
iteration 5	recalculation of $F(\mathbf{X})$	16.97	17.38
	recalculation of \mathbf{K}^*	68.93	0.00
	inversion	0.21	0.25
iteration 6	recalculation of $F(\mathbf{X})$	16.08	15.08
	recalculation of \mathbf{K}^*	68.23	0.00
	inversion	0.24	0.24
iteration final	recalculation of $F(\mathbf{X})$	15.91	18.45
	recalculation of \mathbf{K}^*	68.11	0.00
	inversion	0.28	0.23

Abstract:

C5. Please begin with a sentence that more clearly gives the background - something like: “Two methods for retrieving ... are physical and statistical retrieval algorithms ...”

R5: Thanks for the constructive suggestions to improve our manuscript. We have modified the problem in our revised submission.

For your convenience, the corresponding part in our revised submission is given as follows:

Various retrieval algorithms have been developed for retrieving temperature and water vapor profiles from the Atmospheric Emitted Radiance Interferometer (AERI) observations. The physical retrieval algorithm, named AERI Optimal Estimation (AERIoe), outperforms other retrieval algorithms in many aspects except the retrieval time, which is significantly increased due to the complex radiative transfer process.

C6. Line 12: Begins with “Further analysis showed...” but no analysis has yet been discussed. What changes were made to the Jacobians and why was that expected to speed up performance (but didn’t)?

R6: Thank you for pointing out this problem. Analysis of the change of Jacobians in the retrieval process and the dependence of AERIoe algorithm on Jacobians has been added in the abstract.

For your convenience, the corresponding part in our revised submission is given as follows:

Analysis of the change of AERI observations’ information content with Jacobians revealed that the performance of AERIoe algorithm had little dependence on Jacobians. Thus, the Jacobian matrix could remain unchanged when the variation of atmospheric state is small in the retrieval process. This significantly reduces the amount of computation and thus increases the retrieval speed of AERIoe.

C7. The time estimates are not useful without knowing what type of computing platform was used. Perhaps just give the percent improvement. Also, are 3 significant figures warranted here?

R7: Thank you for the suggestion. We have modified the problem in our revised submission.

For your convenience, the corresponding part in our revised submission is given as follows:

The retrieval speed was significantly improved compared with the original AERIoe algorithm under the condition that the parameters of the computing platform remain unchanged, resulting in an average retrieval time reduction by 58.82%.

C8. What is meant by “certain impact”? What is meant by “to some extent”? Why not state the

convergence rate of the traditional algorithm?

R8: Thank you for pointing out the problems. The sentence has been reworked and the convergence rate of the AERIoe algorithm has been added in the abstract.

For your convenience, the corresponding part in our revised submission is given as follows:

Results based on synthetic observations revealed that the fast retrieval algorithm reached an acceptable convergence rate of 98%, which is slightly lower than the 99.88% convergence rate of AERIoe for the 826 cases used in this study.

C9. The authors say that “The retrieval accuracy of the fast retrieval model is equivalent to that of the traditional algorithm.” However, on lines 346-348 differences indicate that the accuracies are not equivalent.

R9: Thank you for pointing this problem out. We have modified the sentence as “ The retrieval results of the fast retrieval model are comparable to that of AERIoe.” Reasons for this modification are discussed in detail in the response to comments on lines 346 - 348.

For your convenience, the corresponding part in our revised submission is given as follows:

The retrieval results of the fast retrieval model are comparable to that of AERIoe.

C10. How is the convergence criteria adjusted to give reliable retrieval results? It was previously stated that the results were equally accurate. Do you mean they are equally accurate when they both converge?

R10: Thank you for the comments. The sentence ‘However, reliable retrieval results can still be obtained by adjusting the convergence criteria.’ has been removed.

Lines 115-124:

C11. Line 115: If the authors are using $X_0 = X_a$, they should replace X_0 with X_a in Eqn (1) so it is consistent with Turner and Lohnert. If not, they should explain this change.

R11: Thanks for the suggestion. We have replaced X_0 with X_a in Eqn (1).

For your convenience, the corresponding part in our revised submission is given as follows:

$$X_{n+1} = X_a + (K_n^T S_e^{-1} K_n + \gamma S_a^{-1})^{-1} K_n^T S_e^{-1} \times (Y^m - F(X_n) + K_n (X_n - X_a)), \quad (1)$$

C12. Line 116 says “Y is the observed radiance vector, F(X) is the AERI observed spectrum...” Is it rather that Y is the observed radiance vector (from the observed AERI spectrum) and F(X) is the estimate of Y from the forward model calculation? It would also be helpful to define that the background refers to the a priori atmospheric state, if that is the case.

R12: Thanks for the suggestion. We have replaced ‘F(X) is the AERI observed spectrum’ with ‘F(X) is the computed radiance for X’. The sentence ‘ S_a is the background covariance matrix’ has been changed to ‘ S_a is the a priori covariance matrix’.

For your convenience, the corresponding part in our revised submission is given as follows:

Here, X is the profile of the atmospheric state to be retrieved, X_a is the prior profile of the atmosphere, S_a is the a priori covariance matrix, Y^m is the observed radiance vector, $F(X)$ is the computed radiance for X ,...

C13. Eqn. 1: I'm curious why this formulation is used instead of the Levenberg-Marquardt formulation (Rodgers 2000, Eqn 5.36). How is the behavior the same or different? Carissimo et al. 2005 state that their method is almost equivalent to Levenberg-Marquardt. In Levenberg-Marquardt, increasing gamma decreases the step size and makes the retrieval weighted more toward steepest descent. How is the formulation here the same or different?

R13: Thank you for the comments, we have put our thinking caps on this question and the discussion regarding it is presented as follows:

The iterative equation for AERIoe is as follows

$$\mathbf{X}_{n+1} = \mathbf{X}_a + (\mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n + \gamma \mathbf{S}_a^{-1})^{-1} \mathbf{K}_n^T \mathbf{S}_e^{-1} \times (\mathbf{Y}^m - F(\mathbf{X}_n) + \mathbf{K}_n(\mathbf{X}_n - \mathbf{X}_a)) \quad (1)$$

The equation for the Levenberg-Marquardt method is given as follows (Rodgers, 2000)

$$\mathbf{X}_{n+1} = \mathbf{X}_n + (\mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n + (1 + \gamma) \mathbf{S}_a^{-1})^{-1} \times (\mathbf{K}_n^T \mathbf{S}_e^{-1} (\mathbf{Y}^m - F(\mathbf{X}_n)) - \mathbf{S}_a^{-1} (\mathbf{X}_n - \mathbf{X}_a)) \quad (2)$$

We believe that the comparison of the two methods can be analyzed from two aspects: the retrieval process and the retrieval results.

(1) In terms of retrieval process, Carissimo et al. (2005) state that gama in Eqn (1) damps the width of the step between two consecutive iterates and leads its direction toward the steepest descent of the cost function. Gama in Eqn (2) is chosen at each step to reduce the cost function and also tends to the steepest decent of cost function. Therefore, the role of gama in Levenberg-Marquardt method is equivalent to that of AERIoe.

However, the values of gama in the two formulas are quite different, as the profiles in Eqn (1) are retrieved by adjusting the a prior profile \mathbf{X}_a , while the profiles in Eqn (2) are iterated by adjusting the iterative profile \mathbf{X}_n . For example, in the work of Foth and Pospichal (2017) the initial value of gama is 2, and increases by a factor of 10 if the cost function \mathbf{J} has increased and reduces by a factor of 2 if \mathbf{J} has decreased. Therefore, the value of gama in Levenberg-Marquardt method shows a significant difference from AERIoe ($\gamma = 1000, 300, 100, 30, 10, 3, 1, \dots$).

(2) In terms of retrieval results, gama in Equation (1) needs to be set to 1 in the final step to eliminate regularization errors in the solutions, which gives

$$\mathbf{X}_{n+1} = \mathbf{X}_a + (\mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n + \mathbf{S}_a^{-1})^{-1} \mathbf{K}_n^T \mathbf{S}_e^{-1} \times (\mathbf{Y}^m - F(\mathbf{X}_n) + \mathbf{K}_n(\mathbf{X}_n - \mathbf{X}_a)) \quad (3)$$

It can be seen that $(\mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n + \mathbf{S}_a^{-1})^{-1} \cdot \mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n$ is equivalent to $I - (\mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n + \mathbf{S}_a^{-1})^{-1} \cdot \mathbf{S}_a^{-1}$, thus Eqn (3) can be written as

$$\mathbf{X}_{n+1} = \mathbf{X}_a + (\mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n + \mathbf{S}_a^{-1})^{-1} \mathbf{K}_n^T \mathbf{S}_e^{-1} (\mathbf{Y}^m - F(\mathbf{X}_n)) + \left(I - (\mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n + \mathbf{S}_a^{-1})^{-1} \mathbf{S}_a^{-1} \right) (\mathbf{X}_n - \mathbf{X}_a) \quad (4)$$

So the solution becomes

$$\mathbf{X}_{n+1} = \mathbf{X}_n + (\mathbf{K}_n^T \mathbf{S}_e^{-1} \mathbf{K}_n + \mathbf{S}_a^{-1})^{-1} \times (\mathbf{K}_n^T \mathbf{S}_e^{-1} (\mathbf{Y}^m - F(\mathbf{X}_n)) - \mathbf{S}_a^{-1} (\mathbf{X}_n - \mathbf{X}_a)) \quad (5)$$

Eqn (5) is a special case of Eqn (2) when gama in Eqn (2) is chosen to be 0. Therefore, the Levenberg-Marquardt is a combination of a Gauss-Newton (without gama) and steepest descent minimization technique and equivalent to AERIoe.

References:

- Rodgers, C. D.: Inverse methods for atmospheric sounding: theory and practice, World scientific, 119-120 pp., ISBN9814498688, 2000.
- Carissimo, A., De Feis, I., and Serio, C.: The physical retrieval methodology for IASI: the δ -IASI code, Environmental Modelling & Software, 20, 1111-1126, <https://doi.org/https://doi.org/10.1016/j.envsoft.2004.07.003>, 2005.
- Foth, A. and Pospichal, B.: Optimal estimation of water vapour profiles using a combination of Raman lidar and microwave radiometer, Atmos. Meas. Tech., 10, 3325-3344, <https://doi.org/10.5194/amt-10-3325-2017>, 2017.

C14. Figure 1: This figure needs improvement and explanation. E.g. please define “iterative

observations" and "iterative profiles" in the caption. Use of the symbol "Sa" is inconsistent with use of "Jacobians" instead of "K". K_Index has not yet been defined.

R14: Thanks for the suggestion. We have changed "Sa" to "a prior covariance matrix". A symbol "compute monitoring index" was used instead of "K_Index". We have defined "iterative profiles" as temperature and water vapor profiles at iteration n and "iterative observations" as computed radiance for \mathbf{X}_n in the caption.

For your convenience, the corresponding part in our revised submission is given as follows:

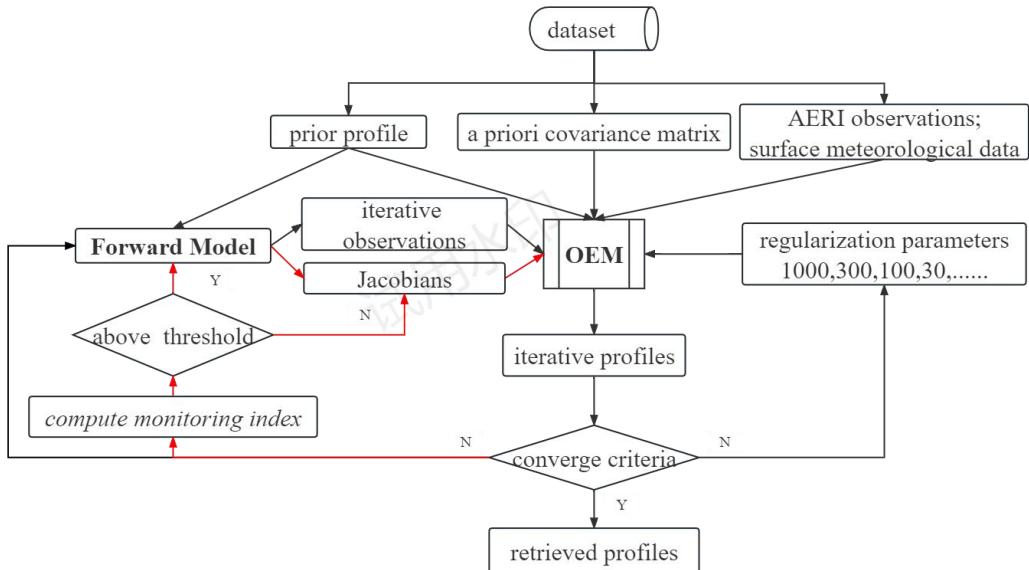


Figure 1. Flowchart of the Fast AERIoe retrieval process. Note that the red line indicates the Jacobian updating process. The iterative profiles and observations are defined as temperature and water vapor profiles at iteration n and computed radiance for \mathbf{X}_n . The monitoring index is used to derive the variations of \mathbf{X}_n .

C15. Line 118: I don't think n is the number of iterations, but rather the iteration number.

R15: Thanks for the suggestion. We have changed 'the number of iterations' to 'the iteration number'.

For your convenience, the corresponding part in our revised submission is given as follows:

... S_e is the observation error covariance matrix, and n denotes the iteration number ...

C16. Line 120: The description of how gamma is used is not clear.

R16: Thanks for the suggestion. The description of how gamma is used has been added in the revised manuscript.

For your convenience, the corresponding part in our revised submission is given as follows:

AERIoe begins with scalar γ of large values is to stabilize the retrieval and ends with a unity γ to add more information from AERI observations as n increases. This approach allows the AERIoe algorithm to overcome a poor first guess and achieve a results that have the most information from AERI observation, the detailed description of how γ is used can be found in Turner and Löhner (2014).

C17. Line 122: Remove "progress".

R17: Thanks for the suggestion. The word 'progress' in Line 122 has been removed.

For your convenience, the corresponding part in our revised submission is given as follows:

As γ decreases with iterations, more observation information is introduced to improve the retrieval accuracy.

C18. Line 122: Please change "is not allowed to converge until..." to "Iterations are continued until..." if that is what is meant here.

R18: Thanks for the suggestion. We have modified this problem in our revised manuscript.

For your convenience, the corresponding part in our revised submission is given as follows:

Iterations are continued until γ decreases to 1 and the following convergence criterion is satisfied.

[C19. Line 124: Use consistent symbols. You have superscript n sometimes and subscript n other times.](#)

R19: Thanks for the suggestion. We have changed all of superscript n into subscript n.

For your convenience, the corresponding part in our revised submission is given as follows:

$$\text{convergence_index} = \frac{(\mathbf{X}_n - \mathbf{X}_n) \mathbf{S}^{-1} (\mathbf{X}_n - \mathbf{X}_{n+1})}{N} \leq 1, \quad (2)$$

$$K_Index = \frac{(\mathbf{X}_n - \mathbf{X}_n)^T (\mathbf{X}_n - \mathbf{X}_n)}{N}, \quad (7)$$

[C20. Line 214-215: It is not true that “what affects IC and DFS lies only in gamma and Jacobian”. In fact, when gamma = 1, IC and DFS are determined by \$\mathbf{S}_e\$ and \$\mathbf{S}_a\$, with the purpose of the Jacobian being to transform \$\mathbf{S}_e\$ into the state space for \$\mathbf{S}_a\$, so that they have the same units and size \(rows and columns\). I think what you mean is that IC and DFS only change with iteration due to changes in gamma and the Jacobian. \(But see below\).](#)

R20: We appreciate the suggestion. The sentence in line 214-215 has been rephrased.

For your convenience, the corresponding part in our revised submission is given as follows:

It can be seen from equations (3) and (4) that SIC and DFS are determined by \mathbf{S}_e , \mathbf{S}_a , \mathbf{K} and γ . However, \mathbf{S}_a and \mathbf{S}_e remain unchanged during retrieval, which makes SIC and DFS change with iteration due to variations in γ and \mathbf{K} . As γ drops to 1 at the final iteration, the values of SIC and DFS are only dependent on \mathbf{K} .

[C21. Lines 214 - 232: I don't understand the logic here. On line 224, it is strange to say that gamma changes with the adjustment of the profile, since gamma is prescribed. Figure 3 is confusing. The x-axis goes in the reverse direction as the retrieval proceeds, the figure caption description seems to be wrong \(red is actually \$K_index\$ \), and it isn't stated where \$K_index\$ starts and ends \(starts at the high end, ends at the low end?\). It is not surprising that the \$DFS\$ and \$IC\$ increase as gamma drops to 1, since gamma weights the retrieval away from the observation and toward the first-guess, which presumably has no information content at all. It is also not surprising that there is not much change in \$DFS\$ and \$IC\$ with the Jacobian, since, as stated previously, the purpose of the Jacobian here is to transform \$\mathbf{S}_e\$ onto the dimensions of \$\mathbf{S}_a\$. I don't see how this shows that the change of the Jacobian has less influence on the retrieval ability than gamma. Gamma is not supposed to influence the retrieval ability, but only the retrieval stability. That is why iterations are continued until gamma is 1, whereupon the retrieval equation is equivalent to the Gauss-Newton formulation and the maximum information content is used. In fact, I don't see the point of this paragraph or figure at all. The authors could simply state that if \$\mathbf{X}\$ is not changing much, as evidenced by the \$K_Index\$, then the Jacobian is probably not changing much either, and therefore does not need to be recomputed. \(Note, however, that this is not necessarily true, and they need to show that it is an ok approximation\).](#)

R21: We appreciate the suggestion. We admit that the logic here is indeed a bit confusing. Some modifications have been made to Fig 3 and the analysis of this picture. The indicator “ IC ” was changed to Shannon Information Content (SIC) to be consistent with the work described by Turner and Löhnert (2014). The change of K_Index with factor γ was removed since it may lead to some confusion and occasional misunderstanding. Fig 3 and the analysis of this figure were reworked.

Thanks for the suggestion again. We added the detailed discussion in the revised manuscript.
For your convenience, the corresponding revised part in our revised submission is given as follows:

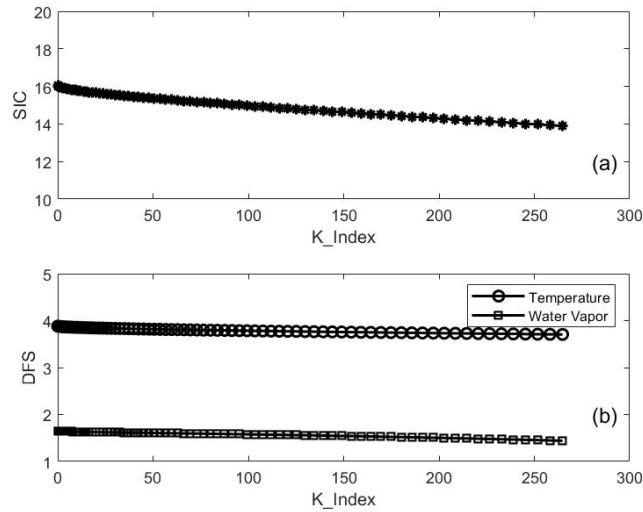


Figure 2. (a) The change of SIC with K_Index . (b) The change of DFS with K_Index for temperature (unfilled circles) and water vapor (open squares), respectively.

The values of K_Index , which covers most of the K_Index during AERIoe retrieval process (ranged from 0 to 260, see Fig. 3), were obtained by multiplying the a prior profile by different scale factors. The atmosphere dependent \mathbf{K} were computed by LBLRTM with the prior profiles above, and SIC and DFS were calculated using equations (3) and (4) with different Jacobians, respectively. Fig. 2 shows the curve of SIC and DFS changed with K_Index . Both of them change slowly with K_Index , with the variation of SIC within 13.46% (from 13.89 to 16.05), and DFS within 4.38% (from 3.71 to 3.88) for temperature and within 12.73% (from 1.44 to 1.65) for water vapor, which demonstrates that SIC and DFS remain almost unchanged as K_Index increases on the condition that the value of K_Index is small. This provides an effective means to improve the retrieval speed of AERIoe by recalculating \mathbf{K} selectively when \mathbf{X} is not changing much or K_Index is small. This could be achieved by comparing the value of K_Index and its threshold at each iteration to determine whether \mathbf{K} is recalculated or not.

C22. Turner and Lohnert state that “Future versions of AERIoe will use the Carissimo et al. (2005) approach in order to more efficiently converge and reduce computational time.” Did the authors explore that approach, and how might that change their analysis?

R22: Thank you for the comments. In fact, the first approach we studied to reduce the retrieval time happens to be the L-curve method recommended by Turner and Lohnert (2014). In our study the codes in Regularization Tools developed by Per Christian Hansen were used to calculate the L-curve and locate the corner, and the retrieval results using gama from the L-curve method did not show any superiority over the method used in AERIoe. The reason lies in that the gama obtained from L-curve method does not gradually decrease with iterations in the retrieval process. In order to figure out the impact of gama on the iterations of AERIoe, we find that the change of \mathbf{K} is negligible during most of the retrieval process, which inspired this study to reduce the retrieval time by recalculating \mathbf{K} selectively.

C23. Sections 3.1 and 3.2. are unclear. The description of the retrieval forms is confusing. Is the state vector comprised of the temperature and log of water vapor on the 37 atmospheric layers? Why isn't it parametrized, given that there are far fewer degrees of freedom? It continues to be difficult to tell what is new here and what is the same as previous work. Please avoid repeating details where you

could reference the previous work. For example, you could say, “The forward model is the same as that described by Turner and Lohnert, except as follows...” Was LBLRTM used here to apply the spectral response function, in contrast to the previous work? It is stated that LBLRTM can be used to calculate the Jacobian. Was it used for this purpose? Again, is this a departure from previous work?

R23: Thanks for the suggestion. We have removed Sections 3.1 and 3.2 from the manuscript and added descriptions of Fast AERIoe configurations that differ from AERIoe in the paragraph between line143 and line154.

For your convenience, the corresponding part in our revised submission is given as follows:

Note that \mathbf{K} depends on \mathbf{X} used for estimating the Jacobian, which means that \mathbf{K} must be recomputed for every iteration step. The updating of the Jacobians in the above retrieval process requires the calculation of the optical thickness or radiance (intensity)with respect to different atmospheric constituents at each height, which might be computationally expensive depending on the lengths of \mathbf{X} and \mathbf{Y}^m (Maahn et al., 2020). Owing to the constraints of γ , the decrease of the difference between simulated and observed radiation is not very much in the adjustment of individual iterations to the retrieval profile. At this time, the change in the Jacobian calculated as per the iteration profile is negligible. Backed by the above analysis, a fast iterative algorithm called Fast AERIoe is proposed on the basis of the AERIoe algorithm. The flowchart of Fast AERIoe is shown in Fig. 1, most of the configurations are consistent with AERIoe described by Turner and Löhner (2014), except some modifications highlighted as follows:

a. atmospheric configurations: The height grid of \mathbf{X} is consistent with AERIoe, but the maximum retrieval height is limited to 3 km. This is done because the variations of \mathbf{K} above 3 km is negligible due to the fact that most of the information in AERI spectrum lies in the lowest 2 km of the atmosphere for temperature and water vapor profiles (Turner and Löhner, 2014). The cloud properties were excluded from the state vector \mathbf{X} , which is beyond the scope of this study. The corresponding priori profile \mathbf{X}_a and the priori covariance matrices represented by \mathbf{S}_a are modified to be consistent with \mathbf{X} .

b. observational vector \mathbf{Y} : Spectral regions that sensitive to cloud properties were removed from the observational vector \mathbf{Y} to be consistent with the state vector \mathbf{X} . Furthermore, additional observations including surface temperature and water vapor were incorporated into the observation vector, details are described by Turner and Blumberg (2019) .

c. Jacobian matrix \mathbf{K} : \mathbf{K} is derived from LBLRTM, which is the same as AERIoe except the version (12.8 instead of 12.1). Another modification is that \mathbf{K} is not recomputed to improve the retrieval speed of the algorithm when the variations of the iterative profile \mathbf{X}_n is small.

C24. Line 176: Please remove the statement that LBLRTM is the most accurate forward model or provide a reference for it.

R24: Thanks for the suggestion. The statement that LBLRTM is the most accurate forward model has been removed.

C25. Line 196-197: Please rephrase this: “...determined whether updating or not by monitoring the indicators that can reflect the changes of Jacobian in the iterative process”.

R25: Thanks for the suggestion. The sentence in line 196-197 has been rephrased.

For your convenience, the corresponding part in our revised submission is given as follows:

Adaptive updating of \mathbf{K} is the key to reduce the calculation amount of the AERIoe algorithm. The Jacobians are dependent on the atmospheric constituents, which means that \mathbf{K} must be recalculated for every iteration step. The question arises as to under what circumstances \mathbf{K} does not need to be recalculated. Therefore, the dependence of the retrieval capability on Jacobians must be analyzed and indicators that reflect the changes of Jacobians should be figured out to determine whether \mathbf{K} recalculated or not.

C26. Line 344: Please change, “with only slight differences in BIAS metrics between 500 m and 1.5 km” to include a quantitative value, such as “with differences within x% to y%”

R26: Thanks for the suggestion. We have rephrased this sentence and the values of BIAS and RMSE were also changed when radiosonde observations were smoothed with A.

For your convenience, the corresponding part in our revised submission is given as follows:

The Fast AERIoe retrieved temperature profiles shows a negative deviation of 0.05K between 1.0km and 1.5 km and a maximum increase of RMSE within 0.08 K above 1.0 km when compared with AERIoe.

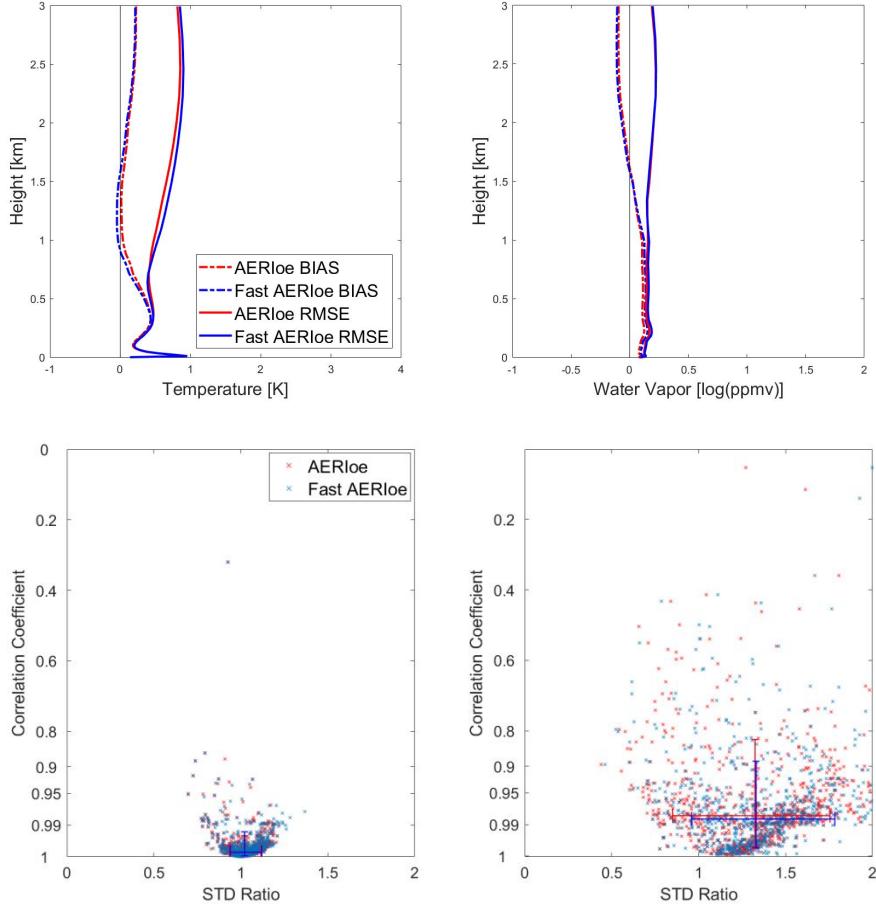
C27. Lines 346 - 348: It seems like “a maximum increase of 0.29 g/kg in BIAS and a maximum of 0.32 g/kg in RMSE” are significant. The bias increase appears to be up to about 40% (0.7 to 0.9), and the RMS increase up to ~12%. This does not seem to me to be comparable retrieval accuracy. Please clarify.

R27: Thanks for pointing this problem out. We've made two modifications to Fig.9. One is that the radiosonde observations have been smoothed with the averaging kernel A, as suggested by first reviewer, to reduce the vertical representativeness errors.

$$\mathbf{X}_{sonde}^{smoothed} = \mathbf{A}(\mathbf{X}_{sonde} - \mathbf{X}_a) + \mathbf{X}_a$$

Another modification is the transformation of water vapor into the form of $\log(\text{ppmv})$. This is due to the fact that the unit of \mathbf{K} output by LBLRTM is $\log(\text{ppmv})$ during the retrieval, which means that the adjustment of the iterative profile is also in the form of $\log(\text{ppmv})$. Therefore, we believe that it is more reasonable to compare water vapor profiles of different retrieval algorithms in the form of $\log(\text{ppmv})$.

In the figure of BIAS and RMSE, the Fast AERIoe retrieved temperature profiles shows a negative deviation of 0.05 K between 1.0 km and 1.5 km and a maximum increase of RMSE up to 13.3% (from 0.60 K to 0.68 K) above 1.0 km when compared with AERIoe. For the water vapor profile, the BIAS and RMSE profiles of Fast AERIoe are in good agreement with AERIoe, except for a maximum increase of BIAS up to 25% (from 0.12 $\log(\text{ppmv})$ to 0.15 (ppmv)) bellow 1.0 km. Therefore, we agree with the reviewers' comments that Fast AERIoe does not reach a comparable retrieval accuracy. However, we believe that the retrieved profiles rather than the retrieval accuracy of the two algorithms are comparable. This is because the increment of BIAS (within 0.03 $\log(\text{ppmv})$) is much smaller than the value (roughly on the order of 5-10 $\log(\text{ppmv})$) of the retrieved water vapor profile itself, and this increment had little impact on the retrieval results of AERIoe. The comparison of the profiles retrieved by the two algorithms can be demonstrated more clearly by the modified Taylor plots. Most of the blue and red symbols ‘ \times ’ in the figure , which indicate the scores for the individual profiles of the two algorithms, are closed to each other. Therefore, the retrieval results of the AERIoe and Fast AERIoe algorithms are comparable both for temperature and water vapor profiles.



To be more precisely, we have rephrased all the sentence like “the retrieval accuracy of Fast AERIoe is comparable to that of AERIoe” in the manuscript to “the retrieved profiles of Fast AERIoe is comparable to that of AERIoe.

For your convenience, the corresponding part in our revised submission is given as follows:

Traditional methods used to evaluate the accuracy of retrieved profiles against radiosondes compute the BIAS and Root Mean Square Error (RMSE), with the calculation formula as follows:

$$BIAS(i) = \frac{\sum_{j=1}^M (\mathbf{X}_{sonde}^{smooth}(i, j) - \mathbf{X}_{retrieval}(i, j))}{M}, \quad (8)$$

$$RMSE(i) = \sqrt{\frac{\sum_{j=1}^M (\mathbf{X}_{sonde}^{smooth}(i, j) - \mathbf{X}_{retrieval}(i, j))^2}{M}}, \quad (9)$$

Where i and j represent the serial numbers of vertical stratification and samples, respectively, with M being the number of samples. $\mathbf{X}_{retrieval}$ is defined as retrieved profiles, $\mathbf{X}_{sonde}^{smooth}$ is radiosonde observations which are smoothed with the averaging kernel \mathbf{A} by the following multiplication to reduce the vertical representativeness errors

$$\mathbf{X}_{sonde}^{smooth} = \mathbf{A}(\mathbf{X}_{sonde} - \mathbf{X}_a) + \mathbf{X}_a, \quad (10)$$

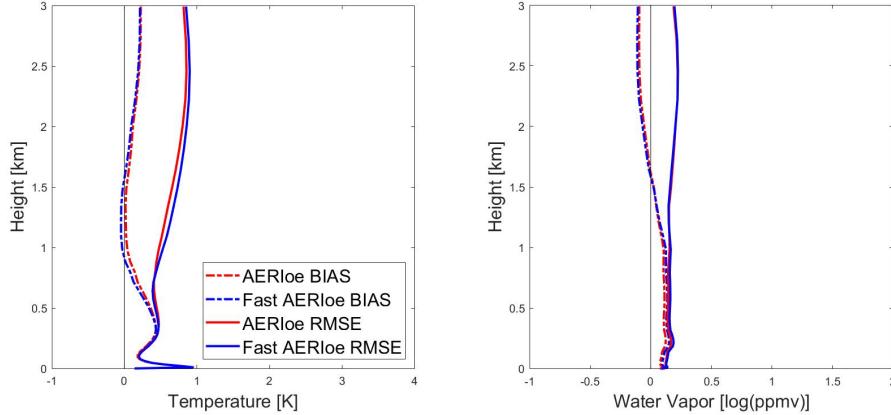


Figure 8. Bias (solid curves) and RMSE (dashed curves) profiles for clear-sky comparisons of the AERIoe(red curves) and Fast AERIoe (blue curves) retrievals with radiosondes. (Left) Temperature profile, (right) Water Vapor profiles.

The BIAS and RMSE of AERIoe and Fast AERIoe are calculated for 826 sets of samples using the above equations within the altitude range of 0-3 km, and the results are shown in Fig. 8. The temperature profile below 1.0km and the water vapor profile below 1.5 km have obvious positive deviations, with the maximum deviation reaching 1.0 K and 0.2log(ppmv), respectively. However, the BIAS and RMSE at the bottom are significantly reduced due to the constraint of the surface observations, indicating that the introduction of surface meteorological observation data in the observation vector has an obvious positive effect. The Fast AERIoe retrieved temperature profiles shows a negative deviation of 0.05K between 1.0km and 1.5 km and a maximum increase of RMSE within 0.08 K above 1.0 km when compared with AERIoe. For the water vapor profile, the BIAS and RMSE profiles of Fast AERIoe are in good agreement with AERIoe, except for a maximum increase of BIAS within 0.03 log(ppmv) bellow 1.0 km. When considering the magnitude of the temperature (roughly on the order of 300 K) and water vapor (roughly on the order of 5-10 log(ppmv)) profiles, the differences between the retrieved profiles are negligible, indicating that the retrieval results of Fast AERIoe are comparable to that of AERIoe.

The comparison of the profiles retrieved by the two algorithms can be demonstrated more clearly by the modified Taylor plots (Turner and Löhnert, 2014), which are used to evaluate how well each retrieved profile can capture the vertical shapes of its true profile, as BIAS and RMSE can only describe the average accuracy of the whole dataset at each height. These Taylor diagrams show Pearson's correlation coefficient between two datasets on the y-axis and the ratio of the standard deviation on the x-axis. Each retrieval/sonde pair is used to derive the correlation coefficient (r) from Eq. (11) and the ratio of the standard deviations from Eq.(12), both are used by Turner and Löhnert (2014).

$$r = \frac{\frac{1}{N} \sum_{z=0}^{z=h} [s(z) - \bar{s}][a(z) - \bar{a}]}{\sigma_s \sigma_a}, \quad (11)$$

$$SDR = \sigma_a / \sigma_s, \quad (12)$$

Within the equations, $s(z)$ and $a(z)$ are defined as the radiosonde observations and retrieved profiles between 0 and 3 km, (\bar{s}, \bar{a}) and (σ_s, σ_a) are the mean values and standard deviations at the same height range.

Retrievals that have a correlation coefficient of 1 and a standard deviation ratio (SDR) of 1 mean that the two datasets match perfectly. Fig. 9a and Fig. 9b show these plots for the clear-sky AERIoe and fast AERIoe retrievals. For the temperature retrievals, both the Fast AERIoe and the AERIoe perform well, with 90 percent of correlation coefficients above 0.9 and the intersection of the arms close to 1. Fig. 9b shows that retrieving the water vapor structure is much more difficult with both algorithms; the spread in the correlation coefficient and SDR are much larger for water vapor than for temperature. Most of the blue and red symbols '×' in Fig. 9 , which indicate the scores for the individual

profiles of the two algorithms, are closed to each other both for temperature and water vapor profile. Therefore, the modified Taylor plots also confirms the conclusion that the retrieval results of the AERIoe and Fast AERIoe algorithms are comparable.

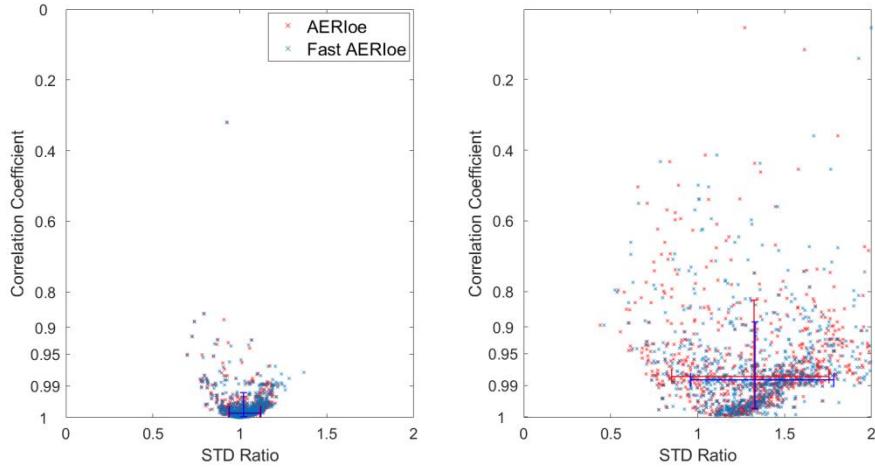


Figure 9. Modified Taylor plots showing the correlation coefficient and standard deviation ratio between the smoothed radiosondes and the retrieved clear-sky (a) temperature and (b) water vapor using AERIoe (red symbols) and Fast AERIoe (blue symbols). There are 826 cases from the SGP site within 2012. Each symbol indicates the score for an individual profile. The arms of the plotted crosses span the 10th–90th percentiles for the correlation coefficient (vertical arms) and the standard deviation ratio (horizontal arms).

C28. Line 350: More detail is needed about how you calculated “Pearson’s correlation coefficient between two datasets on the y-axis and the ratio of the standard deviation on the x-axis”, and the caption of Fig. 10 needs to be improved.

R28: Thanks for the suggestion. The details to calculate the variables in the modified Taylor plot have been added in the revised manuscript. The caption of Fig. 10 has been modified and the sentence 'The intersection of the arms represents the location of the median correlation coefficient and standard deviation ratio of the datasets.' in the caption of Fig.10 has been removed.

For your convenience, the corresponding part in our revised submission is given as follows:

Each retrieval/sonde pair is used to derive the correlation coefficient (r) from Eq. (11) and the ratio of the standard deviations from Eq.(12), both are used by Turner and Löhnert (2014).

$$r = \frac{\frac{1}{N} \sum_{z=0}^{z=h} [s(z) - \bar{s}][a(z) - \bar{a}]}{\sigma_s \sigma_a}, \quad (11)$$

$$SDR = \sigma_a / \sigma_s, \quad (12)$$

Within the equations, $s(z)$ and $a(z)$ are defined as the radiosonde observations and retrieved profiles between 0 and 3 km, (\bar{s}, \bar{a}) and (σ_s, σ_a) are the mean values and standard deviations at the same height range.

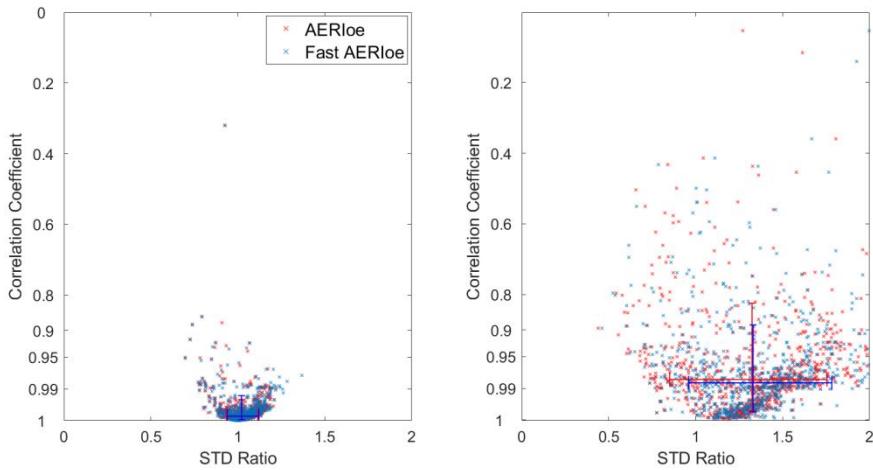


Figure 9. Modified Taylor plots showing the correlation coefficient and standard deviation ratio between the smoothed radiosondes and the retrieved clear-sky (a) temperature and (b) water vapor using AERIoe (red symbols) and Fast AERIoe (blue symbols). There are 826 cases from the SGP site within 2012. Each symbol indicates the score for an individual profile. The arms of the plotted crosses span the 10th–90th percentiles for the correlation coefficient (vertical arms) and the standard deviation ratio (horizontal arms).

References:

C29. For use of FTIR viewing solar spectra, you could also reference the work of Kimberly Strong's group; e.g.: <https://amt.copernicus.org/articles/7/1547/2014/>

For retrievals from AERI, please add a reference Rowe et al. 2006, which used constrained linear inversion to retrieve temperature profiles from an AERI instrument: Rowe, P.M., Walden, V.P. and Warren, S.G., 2006. Measurements of the foreign-broadened continuum of water vapor in the 6.3 μm band at -30°C . *Applied optics*, 45(18), pp.4366-4382.

R29: Thank you for the suggestion. We have read the references recommended by the reviewers carefully. The two references have been added into the revised manuscript.

For your convenience, the corresponding part in our revised submission is given as follows:

The FTIR instrument observes near-infrared and mid-infrared high-resolution solar spectra, which are mainly used to retrieve..., and various trace gas(... [Viatte et al., 2014](#)) profiles or total columns.

The spectral region of AERI covers the range of 520-3000 cm^{-1} , containing a 15 μm absorption band of CO_2 commonly used for the retrieval of temperature profiles, which makes it more advantageous in detecting thermodynamic profiles([Rowe et al., 2006](#)).

References

Viatte, C., Strong, K., Walker, K. A., and Drummond, J. R.: Five years of CO, HCN, C_2H_6 , C_2H_2 , CH_3OH , HCOOH and H_2CO total columns measured in the Canadian high Arctic, *Atmos. Meas. Tech.*, 7, 1547-1570, <https://doi.org/10.5194/amt-7-1547-2014>, 2014.

Rowe, P. M., Walden, V. P., and Warren, S. G.: Measurements of the foreign-broadened continuum of water vapor in the 6.3 μm band at -30°C , *Applied Optics*, 45, 4366-4382, <https://doi.org/10.1364/AO.45.004366>, 2006.

C30. English grammar and clarity: If possible, please have a native English speaker edit your paper throughout, including use of “the” in English, which is very challenging to get right. Examples:

Line 25 and throughout: When you are talking about something in general, omit the word “the” and change the noun to the plural. Examples: change “the observation network” to “observation networks”. Change “the convective scale numerical weather prediction system” to “convective scale numerical weather prediction systems”. Change “the radiosonde profiles” to “radiosonde

profiles". Only use "the" if you are talking about a specific thing, and if you have made it clear which one you are talking about. For example, on line 73, add "the" before "ARM program" since it is clear which program you are talking about (ARM).

R30: Thank you for the suggestion. We have modified the issues identified by the authors in the revised manuscript. Similar issues have been modified and marked in red in the revised manuscript. Moreover, we have carefully polished our paper to improve the English writing. If there are still writing problems with our manuscript, please let us know, and we will try our best to revise our article.

For your convenience, some modifications in our revised submission are given as follows:

The accuracy of the initial field provided by observation networks is becoming a key factor restricting the skill of ...
The existing observation networks are insufficient to meet the needs of convective scale numerical weather prediction systems, ...

As the spatiotemporal resolution is too coarse, radiosonde profiles cannot capture the atmospheric phenomena in detail.

The data used in the study are from the ARM program supported by the U. S. Department of Energy, ...

C31. Line 26: Please define all acronyms (e.g. NWP model)

R31: Thank you for the suggestion. We have checked our manuscript carefully and modified the similar problems in our revised submission.

For your convenience, the corresponding part in our revised submission is given as follows:

The accuracy of the initial field provided by observation networks is becoming a key factor restricting the skill of numerical weather prediction (NWP) models

C32. Line 32: Change "shows" to "has" or "demonstrates". Line 57: remove "to boot".

R32: Thank you for the suggestion. We have modified the problems in our revised submission.

For your convenience, the corresponding part in our revised submission is given as follows:

Space-based detection equipment observes atmospheric upwelling radiance, which demonstrates some drawbacks in the detection of the planetary boundary layer (PBL) owing to the influence of the cloud layer and underlying surface.

However, the AERIprof algorithm has several significant drawbacks, such as its high dependence on the first-guess profile and inability to provide uncertainty estimates for retrieval results.

We are very grateful for your and referees' professional work earnestly. In all, we found the referees' comments are quite helpful. They point the technical issues about our manuscript, also the aspects that we have not done enough. We have tried our best to improve the manuscript and made extensive modifications in the original manuscript according to the comments. Here did not list all the changes but marked in red in revised manuscript.

Thank you and the referees again for your help.