



Cloud and Precipitation Microphysical Retrievals from the EarthCARE Cloud Profiling Radar: the C-CLD product

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Abstract. The Earth Clouds, Aerosols and Radiation Explorer (EarthCARE) satellite mission developed by the European Space Agency (ESA) in cooperation with the Japan Aerospace Exploration Agency (JAXA) features a 94-GHz Doppler Cloud Profiling Radar (CPR). Here, the theoretical basis of the Cloud and Precipitation Microphysics (C-CLD) L2 algorithm is presented. The C-CLD provides best estimates of the vertical profiles of water mass content and hydrometeor characteristic size from CPR reflectivity and hydrometeor sedimentation Doppler velocity estimates using optimal estimation (OE) theory. An ensemble-based method is used to obtain the forward model relations and the associated uncertainty. The ensemble consists of a collection of in-situ measured drop size distributions that span natural microphysical variability. The ensemble mean and standard deviation represent the forward model relations and their microphysics-based uncertainty. The output variables are provided on the Joint-Standard-Grid (JSG) horizontal and L1b vertical grid (1 km along track and 100 m vertically). The OE framework is not applied to liquid-only clouds in drizzle-free and lightly drizzling conditions, where a more statistical approach is preferred.

1 Introduction

Clouds and precipitation systems play a critical role in Earth's energy and hydrological cycle (Stephens et al., 2010, 2012). The accurate representation of cloud and precipitation systems in numerical models is essential for improving the predictability of weather and climate models. While surface-based observatories (Illingworth et al., 2007; Mather and Voyles, 2013; Kollias et al., 2020) can provide high-resolution observations suitable for process studies, satellite-based active remote sensors have the potential to obtain global estimates of cloud and precipitation microphysics and dynamics (Battaglia et al., 2020b). The National Aeronautics and Space Administration (NASA) A-Train satellite constellation (Stephens et al., 2002, 2018) first demonstrated the potential of active remote sensing from space. The EarthCARE mission (Wehr et al., 2022) scheduled for launch in 2024 features the first space-borne cloud profiling radar (CPR) with Doppler capability (Illingworth et al., 2015;

Kollias et al., 2022a, b). The EarthCARE CPR observations will offer a unique opportunity for the collection of a global dataset of vertical motions and microphysics in clouds and precipitation.

Compared to CloudSat, the EarthCARE CPR has higher sensitivity (5-6 dB more sensitive), better vertical sampling (100 versus 240 m), higher along track resolution (500 versus 1100 m), smaller Instantaneous Field of View (IFOV, 800 versus 1400 m), includes Doppler velocity measurements and improved detection in the lower km of the atmosphere (Illingworth et al., 2015; Battaglia et al., 2020b; Burns et al., 2016; Lamer et al., 2019; Kollias et al., 2014). Based on these characteristics, the EarthCARE CPR is expected to provide an improved set of CPR observables, i.e., radar reflectivity, Path Integrated Attenuation (PIA), and Doppler velocity that after their post-processing and quality control by the C-PRO algorithms (Kollias et al., 2022b) will be used for the development of the CPR-only Cloud and Precipitation Microphysics Retrieval (C-CLD) product.

The long record of CloudSat observations and the parallel development and validation of the CloudSat data products provides a strong heritage for the C-CLD algorithm development. In particular, the use of the CloudSat CPR Path Integrated Attenuation (PIA in dB) for estimating the total liquid water path (LWP) in the atmospheric column and for constraining surface and profile estimates of rainfall rate (Haynes et al., 2009; Lebsock and L'Ecuyer, 2011) is applied in a similar manner in C-CLD. Another factor that influenced the C-CLD algorithm development is the development of sophisticated ground-based networks such as the U.S. Department of Energy Atmospheric Radiation Measurements (ARM) observatories and the Aerosol, Clouds and Trace Gases Research Infrastructure (ACTRIS) pan-European research infrastructure (Illingworth et al., 2007; Mather and Voyles, 2013; Kollias et al., 2020). The measurements from these surface-based networks have stimulated the development of several algorithms that utilize the combination of radar reflectivity and mean Doppler velocity (Delanoë et al., 2007; Heymsfield et al., 2008; Mason et al., 2018; Oue et al., 2019). These efforts highlighted the information content of the Doppler velocity that is a new EarthCARE CPR observable from space compared to CloudSat. In addition, the C-CLD algorithm utilizes our latest understanding of solid hydrometeors scattering at 94-GHz (Hogan and Westbrook, 2014; Kneifel et al., 2020) and the availability of extensive ground-based observations of particle size distributions (Williams, 2012; von Lerber et al., 2017).

2 Algorithm description

The C-CLD cloud and precipitation retrieval algorithm is based on a profile-by-profile approach. At each profile, it uses information available from the radar-only measurements provided in a form of the following products: CPR feature mask and radar reflectivity (C-FMR), CPR Cloud Doppler parameters (C-CD) and CPR target classification (C-TC), as described by Kollias et al. (2022b). The C-CLD algorithm derives the best estimates of cloud and precipitation microphysics that feed into the composite cloud and aerosol profiles product (ACM-COM, Cole et al., 2022) as explained in Eisinger et al. (2022). The main retrieved quantities consist of the water mass content and particle characteristic size. First, the output of the C-TC hydrometeor classification is used to determine the occurrence of the specific hydrometeor type (ice cloud, snow, rimed snow, melting snow, cold rain, warm rain, non-drizzling liquid cloud, drizzling liquid cloud). This information is used to determine which branch of the C-CLD retrieval will be employed.

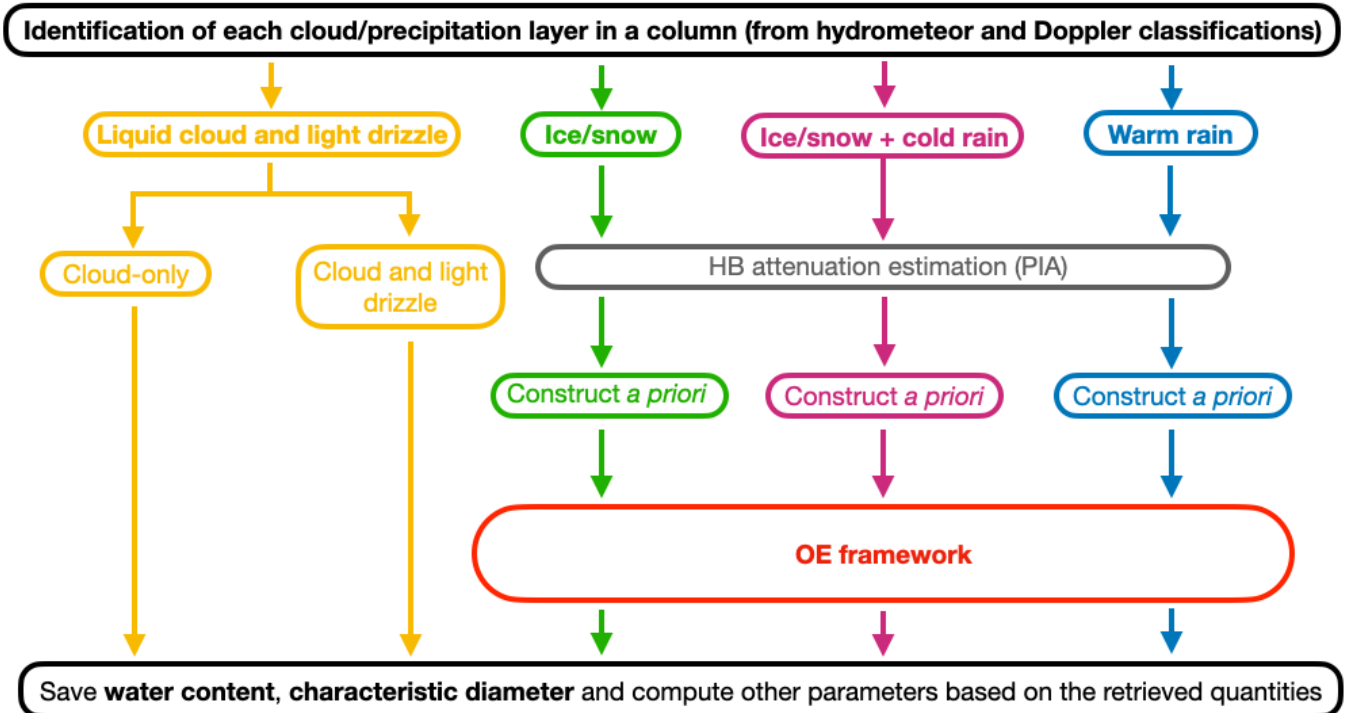


Figure 1. Cloud and Precipitation Retrieval scheme flow chart. OE theory is applied in the retrieval of solid and liquid precipitating clouds. The retrievals in the liquid clouds and lightly drizzling clouds (yellow box) are not performed using the OE method.

As illustrated in the flowchart shown in Fig. 1, the C-CLD processor contains specific algorithms designed to retrieve distinct cloud system types:

- 55
- a. liquid cloud retrieval with the separation between non-drizzling and drizzling liquid cloud;
 - b. ice cloud retrieval and precipitation retrieval with specific algorithms designed to retrieve ice cloud, snow, riming snow, cold rain, warm rain.

The optimal estimation (OE) variational approach, is applied as described in Rodgers (2000). It is based on a Gauss-Newton minimization algorithm that allows a quantitative evaluation of the uncertainty of the retrieved quantities. The forward model within the OE approach maps two moments of the Particle Size Distribution (PSD), the particle characteristic size D_m (i.e., mean mass-weighted melted-equivalent diameter), and mass water content MC to the CPR reflectivity and Doppler velocity (previously corrected in C-CD for vertical air motion).

The OE method is not applied for retrieval of drizzle-free clouds (i.e., not precipitating liquid clouds) and for lightly drizzling clouds (Group a). This is justified by the following facts.



- 65 – In the case of drizzle-free clouds, observed Doppler velocity does not provide any relevant information (fall velocity of cloud droplet is negligible) so the reflectivity is the only measurement available.
- In the case of lightly drizzling clouds, the observed Doppler velocity could be heavily dominated by vertical air motion, leading to a large uncertainty in the reflectivity-weighted velocity. Moreover, the observed reflectivity is, in general, dominated by drizzle.
- 70 Therefore, a retrieval approach involving the optimal estimation method and much simpler methods based on the use of power-law relationships will result in similar uncertainties of microphysical parameters. The main retrieved variables for liquid cloud and drizzle are liquid water content and particle effective diameter, i.e. the ratio of the third and the second PSD moments. Note that the case of heavy drizzle is included in the rain retrieval, as a subcategory of warm rain.

The individual algorithms will now be described in detail in the next sections.

75 2.1 Liquid cloud and light drizzle retrieval

Two distinct situations are analysed.

2.1.1 Drizzle-free clouds

The cloud Liquid Water Content (LWC) vertical structure is determined from the reflectivity values using the relationship $LWC - Z_e$, derived in a power-law form:

$$80 \quad LWC(z) = \langle A \rangle Z_e(z)^{1/2}, \quad (1)$$

where $\langle A \rangle$ is an average value assumed constant across the whole height (Frisch et al., 1998). This relationship assumes that both the cloud droplets' number concentration and the PSD spectral width are constant with height. While this is reasonable in marine clouds (Miles et al., 2000, e.g.), Löhnert and Crewell (2003) concluded that this assumption is the dominant error factor in continental clouds. In a measurable PIA signal is available, we can estimate the Liquid Water Path (LWP) and subsequently estimate the parameter $\langle A \rangle$. Otherwise, two constant values of 4.7 and 2.4 $\text{g mm}^{-3} \text{m}^{-3/2}$ are assumed over land and ocean, for $\langle A \rangle$ respectively.

The corresponding cloud-LWP obtained from such approximation is evaluated against the estimated cloud mass content adiabatic profile that represents an average in-cloud profile, independent of the reflectivity vertical variability with LWC increasing with the distance from the cloud base as:

$$90 \quad LWC_{ad}(z) = f_{wN} \Gamma_w \left[\frac{z_{0w}}{z_{0w} + (z - h_{cb})} \right] (z - h_{cb}) \quad (2)$$

where the term in the square brackets accounts for a decrease of adiabaticity in the thicker clouds as proposed in Wood et al. (2009), z_{0w} is a scaling parameter set to 500 m, Γ_w is the average vertical gradient of the change of adiabatic LWC (parameterized in eq. B1), h_{cb} is the height of the cloud base, f_{wN} is a normalization factor that is set to 1 and In the case of unreliable LWP estimates (i.e., when there is more than one cloud layer and the PIA corresponding to the cloud is smaller than



95 2 dB), then, a minimum and a maximum limit of the adiabatic profile ($0.3LWC_{ad}$ and $0.9LWC_{ad}$, respectively) is enforced on the estimate from the power-law formula.

The cloud effective radius is computed as a mean between the relationship proposed by Fox and Illingworth (1997):

$$r_{eff} = 23.3Z^{0.177} \quad (3)$$

100 and a relation derived for a log normal PSD with a spectra width of $0.38 \mu\text{m}$ reported by Miles et al. (2000) as an average value:

$$r_{eff} = 46.5 \sqrt[6]{Z/N_{cl}}. \quad (4)$$

In eq. 3 and 4, r_{eff} is in μm , Z in $\text{mm}^6 \text{m}^{-3}$, the number concentration, N_{cl} , is in cm^{-3} , and it is assumed to be equal to 288 and 74 over land and ocean, respectively (Miles et al., 2000).

2.1.2 Light drizzling clouds

105 The retrieval of LWC for light drizzling clouds combines two estimates:

1. The LWC derived from reflectivity based on power laws derived by Sauvageot and Omar (1987) and Baedi et al. (2000):

$$LWC_{SO87} = 12.25 Z^{0.763} \quad \text{for } Z < -22 \text{ dBZ} \quad (5)$$

$$LWC_{B00} = 0.457 Z^{0.193} \quad \text{for } Z > -15 \text{ dBZ} \quad (6)$$

and a linear interpolation between these two for the intermediary reflectivity regime (-22 to -15 dBZ).

- 110 2. The LWC profile derived from the adiabatic model (eq. 2) with f_{wN} set to fit LWP estimates, if present, otherwise set to 1.

The final LWC s are computed by combining the LWC_{ad} derived from the adiabatic model and LWC_z from the reflectivity profile. The used $LWC - Z$ relation for drizzling conditions represents an average relation, and can introduce a large bias, mainly close to the cloud base and cloud top; in such regions, large differences between LWC_{ad} and LWC_z are expected.

115 Therefore, in the calculation of the LWC the weight attached to LWC_z is progressively reduced where the absolute relative difference between LWC_{ad} and LWC_z becomes large.

3 Optimal estimation retrievals

For solid/liquid precipitation and ice clouds, the C-CLD algorithm applies a variational approach (Rodgers, 2000). It assimilates radar measurements and aims at balancing these data with the prior information to provide an optimal estimate of the state vector. Gauss-Newton iterations are used to find the best solution, which allows for a quantitative evaluation of the uncertainty of the retrieved quantities. This approach has been applied to similar radar-based microphysical retrievals in the past years



(Lebsock and L'Ecuyer, 2011; Szyrmer et al., 2012; Battaglia et al., 2016, 2020c; Tridon et al., 2019a; Mason et al., 2017) and in the EarthCARE synergistic microphysical retrieval product (ACM-CAP; Mason et al., 2022b).

Radar measurements depend on a number of microphysical properties of hydrometeors in the sampled volume, including the particle size distribution (PSD) and, for solid phase particles, the shape, and mass distribution. Assumptions on any of the parameters listed above lead to a variety of microphysical relations reported in the literature between radar observables and microphysical properties (Protat et al., 2007; Matrosov and Turner, 2018, e.g.). To assess the effect of the uncertainty associated with the microphysical description, the ensemble-based method is used to obtain the forward model relations and the associated simulation uncertainty. The ensemble consists of a number of particle size distributions collected at the ground for the Global Precipitation Measurement (GPM) mission ground validation program (Dolan et al., 2018). Scattering models are applied to these data to map the microphysical quantities to the radar observables. The ensemble mean relations and its spread defined by 1 standard deviation represent the forward model relations and their microphysics associated uncertainty, respectively.

3.1 Unknown variables

The PSD is parameterized using the concept of double moment normalization. Following Delanoë et al. (2005), the normalizing moments are defined as:

$$M_p = \int D^p N(D) dD \quad (7)$$

where p is the moment and D is the liquid sphere equivalent diameter. The ratio of the fourth and the third moment represents the mean mass-weighted melted diameter $D_m = M_4/M_3$ and it is used as the size scaling parameter, while M_3 is proportional to the water-equivalent mass content $MC = (\pi/6)\rho_w M_3$ that controls the magnitude of the PSD. By selecting these moments, the PSD can be expressed as

$$N(D; D_m, MC) = MC \times f(D; D_m) \quad (8)$$

where f represents functional forms that are reported in the literature, derived from large datasets for each given hydrometeor category.

The goal of the C-CLD algorithm is to retrieve two moments of the PSD, i.e., the mass content, MC , and D_m , from radar reflectivity and Doppler velocity measurements. Therefore, the vector of the retrieval unknowns has the following form:

$$\mathbf{x} = [\log_{10} D_m^1, \log_{10} D_m^2, \dots, \log_{10} D_m^N, \log_{10} MC^1, \log_{10} MC^2, \dots, \log_{10} MC^N]^T \quad (9)$$

where N is the total number of the CPR range gates, regardless of whether they include ice/snow or rain. In case of warm and cold rain retrieval, the vector \mathbf{x} includes also the cloud liquid water path with liquid water content distributed according to (2). In cold rain, the attenuation of the melting layer is an additional unknown. Note that the errors in the variables in the logarithmic units can be converted to fractional errors of the variable in the linear scale by the error propagation formula:

$$\frac{\Delta z}{z} \approx \frac{z' \Delta x}{z} = \frac{\ln 10 z \Delta x}{z} = \ln 10 \Delta x, \quad (10)$$



where $z = 10^x$ and x is either $\log_{10}D_m$ or $\log_{10}MC$, e.g., the root-mean-square-error in $\log_{10}z$ of 0.3 corresponds to the fractional error of 69% in z .

155 3.2 Vector of measurements

The forward model maps the retrieved microphysical parameters to the space of radar measurements (attenuated radar reflectivity Z_m , Doppler velocity corrected for air motion, U_D and in some cases path integrated attenuation).

The equivalent reflectivity factor for a radar operating at the wavelength λ is given by:

$$Z_e = \frac{\lambda^4}{\pi^5 |K_w|^2} \int_0^\infty \sigma_b(D, \lambda) N(D) dD \quad (11)$$

160 where σ_b is the backscattering cross-section of a particle and K_w is the dielectric factor of liquid water at a reference temperature and frequency. For this study, K_w is assumed to be equal to $3.195 + 1.667i$, which represents its value at 10°C according to the model of Turner et al. (2016). The reflectivity is usually expressed in $\text{mm}^6 \text{m}^{-3}$ or, due to its high variability, in logarithmic units of $\text{dBZ} = 10 \log_{10}(\text{mm}^6 \text{m}^{-3})$.

165 When analysing millimetre wavelength radar data, the attenuation due to gasses (mainly water vapour and oxygen) and the one caused by hydrometeors cannot be neglected (Battaglia et al., 2020b; Tridon et al., 2020; Lamer et al., 2019). The measured reflectivity at distance r from the radar is given by $Z_m(r) = Z_e(r) \exp[-0.2 \ln 10 \int_0^r k(s) ds]$ or in more commonly used logarithmic units $Z_m(r)[\text{dBZ}] = Z_e(r)[\text{dBZ}] - 2 \int_0^r k(s) ds$ where k is so-called specific attenuation given in dB per unit length; its component associated with the hydrometeors can be computed as the extinction cross-section (σ_e) weighted integral of the PSD:

$$170 \quad k = \frac{10}{\ln 10} \int_0^\infty \sigma_e(D) N(D) dD. \quad (12)$$

Over water bodies, the total path integrated attenuation ($\text{PIA} \equiv 2 \int k(s) ds$) can be estimated from the surface return, and then it is used as an additional observational constraint.

The mean Doppler velocity, is the backscattering-weighted line-of-sight velocity (v_{LOS}) of targets relative to the radar:

$$U_D = \int_0^\infty N(D) \sigma_b(D, \lambda) v_{LOS}(D) dD \times \left(\int_0^\infty N(D) \sigma_b(D, \lambda) dD \right)^{-1}. \quad (13)$$

175 Here, positive velocities correspond to downward motions (away from the CPR).

The CPR processor (C-PRO; Kollias et al., 2022b) derives an optimal estimate, along with uncertainties, of the CPR measurements. This includes the attenuated radar reflectivity, the PIA provided by the C-FMR product and the sedimentation Doppler velocity, where the contribution of the vertical air motion has been removed (C-CD product). All these estimates feed into the C-CLD algorithm, i.e., the measurement vector is composed of:

$$180 \quad \mathbf{y} = [Z_m^1, Z_m^2, \dots, Z_m^N, U_D^1, U_D^2, \dots, U_D^N, \text{PIA}]^T, \quad (14)$$



where N is the number of retrieval layers. The vertical resolution of the retrieval matches the resolution of the radar and it is equal to 100 m.

3.3 OE procedure

The aim of the OE is to provide the most probable value of the microphysical state vector \mathbf{x} given the information provided by the measurements and prior knowledge about the state of the atmosphere. This is done by an iterative search that minimizes the cost function Φ :

$$\Phi = [\mathbf{y} - F(\mathbf{x})]^T R_y^{-1} [\mathbf{y} - F(\mathbf{x})] + [\mathbf{x} - \mathbf{x}_a]^T R_a^{-1} [\mathbf{x} - \mathbf{x}_a] + \mathbf{x}^T R_{TT} \mathbf{x}. \quad (15)$$

Here, $R_y = R_m + R_F$ represents the sum of the measurement error covariance matrix R_m and the forward model error covariance matrix R_F , while R_a represents the prior covariance matrix. A smoothness constraint is introduced in the form of "Twomey-Tikhov" matrix R_{TT} , including a scaling coefficient, as described in Hogan (2006). The state vector at i -th iteration can be found using Gauss-Newton minimization steps, i.e.:

$$\mathbf{x}_i = \mathbf{x}_{i-1} + H^{-1} [J^T R_y^{-1} (\mathbf{y} - F(\mathbf{x}_{i-1})) - R_a^{-1} (\mathbf{x} - \mathbf{x}_{i-1}) - R_{TT} \mathbf{x}_{i-1}]^T; \quad (16)$$

$$H \equiv J^T R_y^{-1} J + R_a^{-1} + R_{TT}. \quad (17)$$

Usually, after a few iterations, the algorithm converges to the minimum that provides the final solution. If convergence criteria are not met within a set number of iterations, the state variables are set to the missing value.

The advantage of using the OE approach is that it provides a method for propagating errors in the measurements and uncertainties of the algorithm assumptions. The error covariance matrix R_x associated with the retrieval variables is given as:

$$R_x^{-1} = J^T R_y^{-1} J + R_a^{-1} \quad (18)$$

The diagonal elements of R_x provide the estimates of the variance of \mathbf{x} , i.e. decimal logarithm of the retrieved quantities (MC, and D_m). The off-diagonal elements give the cross-correlations between errors. The errors for any related quantity, like precipitation rate, can be computed by propagating these errors.

3.4 Warm rain

3.4.1 Forward model of rain reflectivity, attenuation and Doppler velocities

For rain, a gamma model is used to analytically approximate the PSD shape, i.e. the function f in (8) is:

$$f(D; D_m, \mu) = \frac{6(\mu + 4)^{\mu+4}}{\pi \rho_w D_m^4 \Gamma(4 + \mu)} \left(\frac{D}{D_m} \right)^\mu \exp\left(-\frac{D(\mu + 4)}{D_m}\right), \quad (19)$$

where Γ denotes the gamma function and μ is a shape controlling parameter. Schulte et al. (2022) have demonstrated that, in warm rain retrievals, single-moment PSD models can lead to large biases, of the order of 100%, when retrieving rain rates. The selection of the shape parameter μ is based on the methodology presented by Williams et al. (2014) where the expected



value of μ is found for a given D_m , based on the statistical analysis of in-situ microphysical measurements. In this study, 210 in-situ PSDs data collected during field campaigns and from the permanent sites of the Ground Validation program of the Global Precipitation Measuring Mission (GPM; Hou et al., 2014) are exploited (for more detail see Mróz et al., 2019). The analysis is restricted to the measurements from the two-dimensional video disdrometer (2DVD; Kruger and Krajewski, 2002) with a series of quality checks performed beforehand. These checks include discarding frozen precipitation or insufficient PSD sampling that happens for small rainfall rates (≤ 0.1 mm/h) and large sizes ($D_m \geq 4$ mm) that disdrometers are not well 215 suited to capture (Guyot et al., 2019). These filtering criteria are set to have statistically and physically meaningful PSDs. The final dataset includes almost 150,000 samples of rainy measurements over different latitudes, thus thoroughly covering natural variability.

Our analysis, confirmed previous findings of Williams et al. (2014) about the microphysical properties of PSDs, i.e. the mass-weighted standard deviation of D, so-called PSD width (σ_m) is highly correlated with D_m and its expected value is given 220 by

$$\sigma_m^{\text{expected}} = \frac{D_m^{1.4}}{\sqrt{10}}. \quad (20)$$

Although these statistics are based on binned PSD measurements with no underlying assumptions about the PSD shape, they can be translated into a gamma specific relation via $\sigma_m^\Gamma = D_m/\sqrt{4+\mu}$ gives:

$$\mu^{\text{expected}} = 10D_m^{-0.8} - 4. \quad (21)$$

225 For the forward model simulation, back-scattering and extinction cross-sections are computed with the T-matrix approximation assuming the axial-ratio formula of Brandes et al. (2005). The Doppler velocity is computed using the raindrop terminal fall speed as determined by Gunn and Kintzer (1949). It is assumed that the PSD shape can be parameterized by (19) with μ given by (21) to reduce the number of free parameters in the retrieval. The uncertainty of such approximation was estimated via analysis of the radar simulations for the binned PSDs collected at the ground. The forward model errors for the reflectivity, 230 specific attenuation and mean Doppler velocity are 0.42 dB, 10% and 0.12 m s^{-1} , respectively. Note, the specific attenuation uncertainty is given in terms of a fractional error, as it strongly varies with the absolute value. The simulated radar observables corresponding to the in-situ PSD measurements and the forward model parameterization used in this study can be found in Appendix A1.

3.4.2 Cloud liquid water correction

235 A crucial component in the warm rain algorithm for W-band radars is the cloud liquid water correction (Haynes et al., 2009; Battaglia et al., 2020a). The following strategy has been followed: first, the cloud boundaries are identified based on the lifting condensation level (cloud bottom) and by the highest altitude of the detectable reflectivity (cloud top); then the shape of the profile of cloud MC given by Eq. (2) is attributed to the measurement column. Once the shape is fixed, the magnitude of the liquid water content is controlled by the cloud liquid water path (CLWP) that, in the logarithmic units, is one of the



240 retrieved unknowns. Because the radar reflectivity of cloud droplets is much smaller than the one of raindrops, the retrieval of $\log_{10}(CLWP)$ is mainly driven by the PIA estimate.

3.4.3 A-priori

One of the essential elements of the OE procedure is the initial estimation of the microphysical parameter values along with their uncertainties. This can be done by providing climatological statistics based on long-term observations. This approach usually involves very large uncertainties that correspond to the natural variability of the rain microphysics. Alternatively, a much more constrained a-priori estimate can be obtained by statistical analysis of in-situ PSD measurements in relation to their radar simulations, as it was done by Tridon et al. (2019b). For example, an estimate of the mean value and standard deviation of $\log_{10} D_m$ and $\log_{10} MC$ in correspondence to a given reflectivity range ($Z \pm \text{std}Z$) can be provided. This approach is adopted in this study.

250 The a-priori information on $\log_{10} D_m$ and $\log_{10} MC$ is obtained from the rain microphysics statistics and their corresponding reflectivity simulations collected in the PSD dataset described in Sect. 3.4.1. Regression analysis reveals a moderate correlation ($CC=0.53$) between the state vector parameters via the following linear formula:

$$\log_{10} MC[\text{g m}^{-3}] = 1.863 \log_{10} D_m[\text{cm}] + 0.757. \quad (22)$$

The root-mean-square-error (RMSE) of this fit is estimated to be 0.33 B for $0.8 < D_m < 2$ mm. Since the PSD dataset does not include small raindrop sizes, we use regressions (21) and (22) together with the related uncertainties to supplement the in-situ data with low precipitation rate/low reflectivity points. This leads to the following a-priori relations in rain:

$$\log_{10} D_m[\text{cm}] = \begin{cases} 0.020 Z_e[\text{dBZ}] - 1.446 & \text{if } Z_e < 6.75 \text{ dBZ,} \\ 0.036 Z_e[\text{dBZ}] - 1.554 & \text{if } 6.75 \leq Z_e < 17 \text{ dBZ,} \\ 0.012 Z_e[\text{dBZ}] - 1.147 & \text{if } Z_e \geq 17 \text{ dBZ;} \end{cases} \quad (23)$$

$$\log_{10} MC[\text{g m}^{-3}] = \begin{cases} 0.038 Z_e[\text{dBZ}] - 2.043 & \text{if } Z_e \leq 12.5 \text{ dBZ,} \\ 0.109 Z_e[\text{dBZ}] - 2.932 & \text{if } Z_e > 12.5 \text{ dBZ.} \end{cases} \quad (24)$$

Uncertainties of these relations over the whole range of reflectivity values are estimated to be 0.15 B and 0.2 B, respectively (i.e. a factor 1.41 and 1.58), which represents the maximum RMSE value for PSD simulations partitioned into 1 dB reflectivity bins from -15 to 32 dBZ. Note that, for large reflectivity, the slope of the $Z - D_m$ relation is very small compared to the uncertainty estimate, which indicates a weak correlation between these parameters. In practice, it reduces the $Z - D_m$ relationship to the climatological value of $\log_{10} D_m$ provided by the in-situ dataset.

The derived regressions require effective reflectivity estimates; therefore, the radar measurements are approximately corrected for attenuation by using the Hitschfeld and Bordan methodology, before a-priori estimates are derived.

The expected value of the cloud liquid water path is estimated to be weakly related to the rain water path (RWP), i.e.:

$$\log_{10} \frac{CLWP}{RWP} = 0.344 \pm 0.26. \quad (25)$$



This formula is based on the statistical analysis of warm rain simulations over the Cape Verde islands.

3.4.4 Example of retrieved profiles and retrieval performances

270 The C-CLD algorithm has been validated with warm rain simulations over the Cape Verde islands produced by the Global
Environmental Multiscale (GEM) model (Côté et al., 1998; Girard et al., 2014). The cloud microphysical processes were
represented by the Predicted Particle Properties (P3) two-moment bulk microphysics scheme (Morrison and Milbrandt, 2015;
Milbrandt et al., 2016). In the P3 scheme, the ice-phase hydrometeors are represented by three ice categories whose physical
properties evolve continuously and were proved sufficient to represent the co-existence of cloud ice particles of different
275 sizes (Qu et al., 2022). In addition to the three distinct ice species, rain and cloud droplets are also simulated. The horizontal
resolution of the simulation is 250 m, which allows resolving fine scale convective cells that are characteristic of warm rain.
The readers are referred to Qu et al. for more details.

To simulate the radar measurements, the effective reflectivity and the specific attenuation of rain are estimated using formulas
A1 and A3 in each model bin. The cloud contribution is simulated with an exponential PSD and summed up with the rain
280 components. Then, the attenuated reflectivity, at the native model resolution, is computed by integrating the attenuation along
the vertical path. The resulting 3D reflectivity field is averaged horizontally over 3×3 pixels to provide a resolution of $0.75 \times$
 0.75 km^2 that is comparable with the one of the EarthCARE CPR. Similarly, mean Doppler velocity is first simulated at the
native resolution. Next, it is averaged over 3×3 pixels using the attenuated reflectivity (in the linear units) as the weights. This
provides the Doppler measurements at the radar scale. An estimate of the PIA aims to reflect as closely as possible the values
285 that would be observed with the surface reference technique. The normalized radar cross-section, σ_0 [dB], is assumed to be
uniform in the field of view. Then, the apparent PIA is given by:

$$PIA_{SRT} = \sigma_0 - 10 \log_{10} \left(\frac{1}{n} \sum_{i=1}^n 10^{0.1(\sigma_0 - PIA_i)} \right) = -10 \log_{10} \left(\frac{1}{n} \sum_{i=1}^n 10^{-0.1 PIA_i} \right) \quad (26)$$

where PIA_i denotes the path integrated attenuation in the i -th column, while $n = 9$ is the number of the spatially averaged
profiles of the simulations. The water mass content, similarly to the reflectivity field, is averaged over 9 neighbouring pixels.
290 The characteristic size at the radar resolution is the mean of the fine-scale D_m values weighted by the corresponding mass con-
tent. Both rain and cloud components are taken into account in the state and measurement vector computations. The ice/snow
species are neglected in these simulations because only warm rain columns are considered.

Contour Frequency Altitude Diagrams (CFADs) of the radar observables simulated for the warm rain profiles are shown in
Fig. 2. The freezing level is located at about 5 km. Two distinct hydrometeor populations can be seen in the reflectivity and in
295 the Doppler velocity data. In the dominant mode, the cloud top height is about 1 km above the freezing level, where the MDV
data do not exceed 1.5 m s^{-1} . This corresponds to raindrop diameters less than 0.3 mm (Fig. A1c) that are characteristic for
drizzle and cloud droplets. The velocity tends to increase towards the ground, indicating an increase in the size of the raindrops
caused either by collision-coalescence processes or growth by condensation. The reflectivity profiles reach their maximum at
approximately 4 km, then they tend to decrease toward the ground, which may be due to the signal attenuation, a decrease
300 in the water mass content, non-Rayleigh scattering effects (Kollias et al., 2002), or a combination of some of these factors.

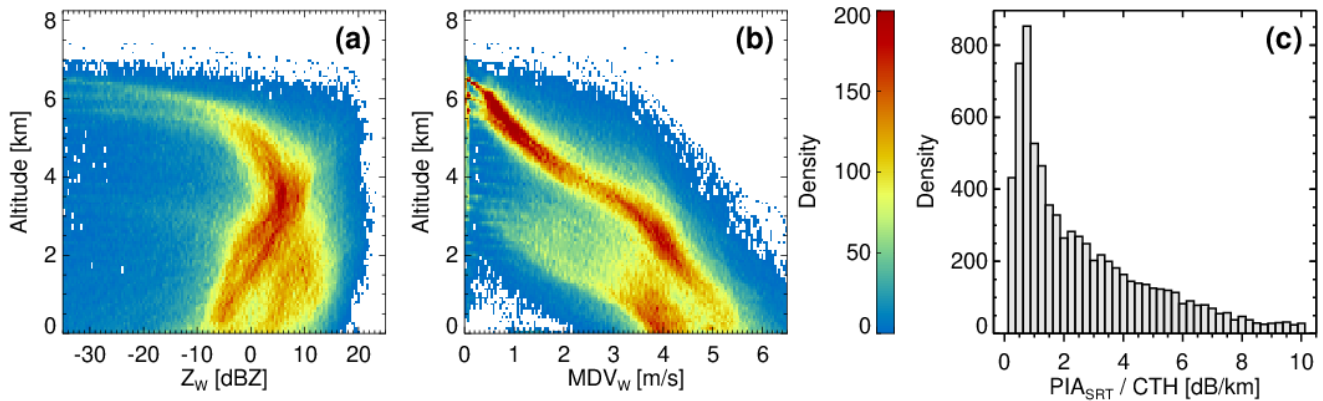


Figure 2. Contour Frequency Altitude Diagrams of the radar reflectivity (a) and mean Doppler velocity (b) of the warm rain profiles used for the C-CLD validation. Panel (c) shows a histogram of the SRT PIA estimates (one-way) normalized by the cloud top height.

The secondary mode of the radar observables corresponds to more shallow precipitation columns, with the cloud top height between 2 and 4 km above the ground. This suggests the presence of a liquid cloud at this altitude too. Although, similar peak reflectivity values are observed the Doppler velocity is reduced compared to the deeper profiles that indicates smaller rain drops with a higher concentration thus completely different microphysics. The presented simulations cover precipitation rates up to 15 mm h⁻¹, with a mean value of 0.4 mm h⁻¹. This is reflected in the PIA values, normalized by the cloud top height, shown in Fig. 2c.

Validation of the retrieval was performed using approximately 8000 warm rain columns and its performance is illustrated in Fig. 3. The algorithm accuracy and precision are quantified by the mean error (ME) and root-mean-square-error (RMSE) in the retrieved variables. The correlation coefficient (r) and normalized RMSE ($NRMSE(x) = RMSE(x)/std(x)$) are computed as additional quality metrics. Since the considered variables are given in the logarithmic units, i.e., $\log_{10} CLWP$, $\log_{10} MC$, $\log_{10} D_m$, the ME and RMSE are given in the units of bel (B). On average, the algorithm is overestimating the liquid cloud water path by about 32% ($ME = -0.12$ B and $10^{0.12} \approx 1.32$). For profiles with higher cloud water content, the overestimation is reduced but scattered more around the 1-1 line. An opposite behaviour is observed for rain, the algorithm underestimates the rain MC by approximately 36% ($ME = 0.13$ B and $10^{-0.13} \approx 0.74$) to compensate for the PIA overestimation due to the cloud droplets. The retrieval of D_m shows very good accuracy, for $0.1 \leq D_m < 3$ mm, the algorithm tends to underestimate the characteristic size by 5% ($ME = -0.02$ B), only. Because the same forward model was used for the retrieval and the scene simulations, the systematic underestimation for large sizes is believed to be caused by non-uniform beam filling (NUBF) effects, i.e. the antenna pattern averaged mean Doppler velocity is smaller than the Doppler velocity corresponding to the footprint averaged D_m because of the shadowing effect due to attenuation in correspondence to the fraction of the footprint with larger reflectivities (see Fig.9 in Mroz et al., 2018). The precision of the algorithm is greatly reduced when PIA estimates are not assimilated in the retrieval, which is reflected in a reduction of the correlation coefficient and an increase in the RMSE values, as can be seen in panels (d) and (e) of Fig. 3. The RMSE value increases from 0.24 B and 0.27 B to 0.48 B and

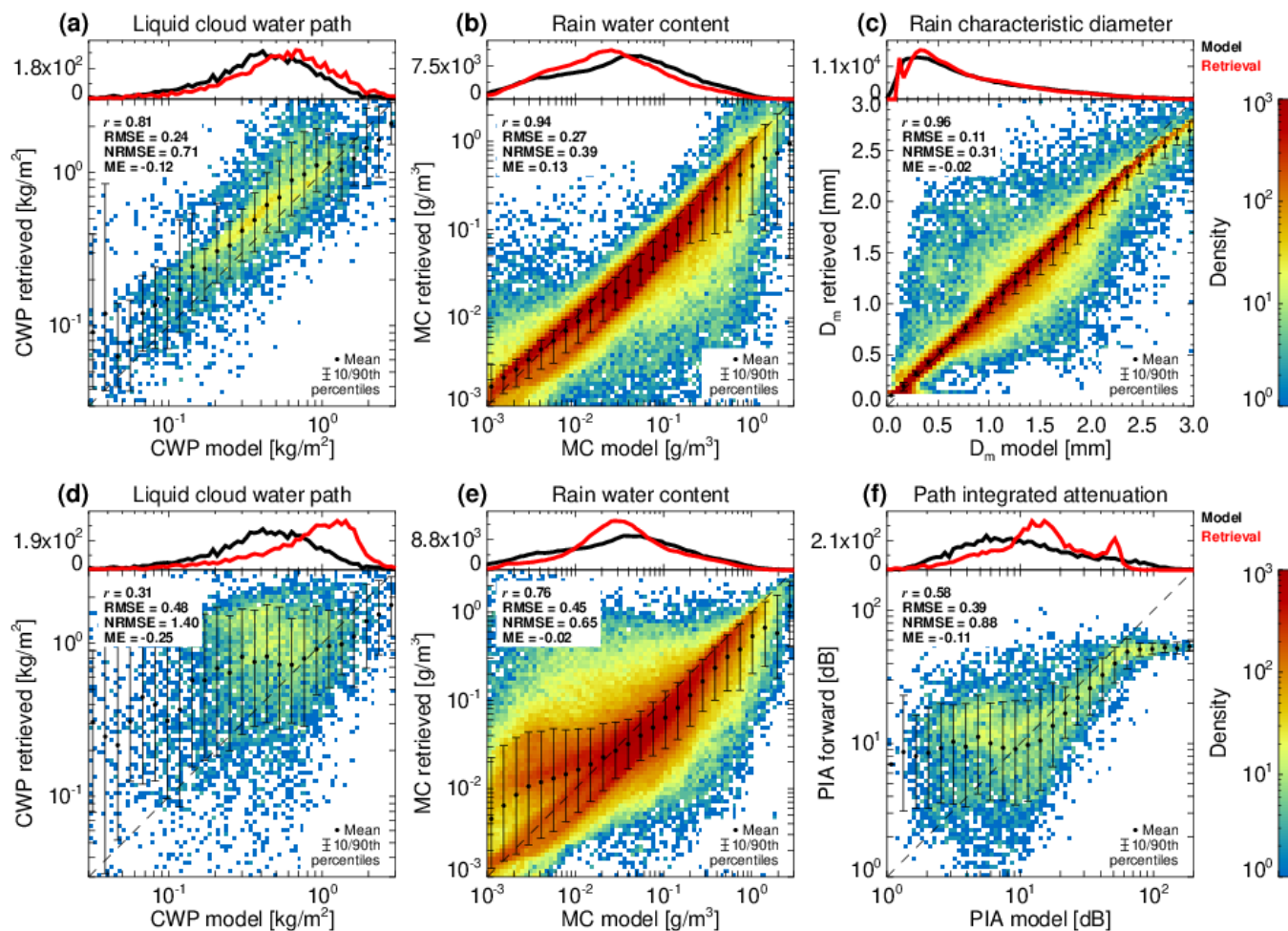


Figure 3. The warm rain algorithm performance histograms. The x-axis represents the model values, while the y-axis corresponds to the retrieval. Panels (a), (b) and (c) show the cloud liquid water path, rain water content, and rain characteristic diameter, respectively. Panels (d), (e) and (f) show the cloud liquid water path, rain water content, forward path integrated attenuation when assuming that the PIA is not available. The reported values of ME, RMSE, normalized RMSE (NRMSE), and correlation coefficient (r) are calculated for unknowns in the logarithmic units, i.e. $\log_{10} CLWP$, $\log_{10} MC$, $\log_{10} D_m$.

0.45 B while the correlation drops from 0.81 and 0.94 to 0.31 and 0.76 for CWP and rain MC, respectively. The estimate of the characteristic size is not affected by the lack of PIA measurements because is mainly retrieved from the Doppler velocity measurements.

When PIA measurements are available, the forward PIA is practically the same as the one being assimilated, with small differences due to the assumed error in the PIA measurements (i.e. 1 dB), giving a correlation of 0.99 and RMSE of 0.07 dB. When the PIA measurements are not available, the algorithm estimates the PIA using the maximum value of the reflectivity profile and the value close to the surface. While this approximation is useful, the lack of an integral constraint makes the correlation between measured and retrieved PIA drop to 0.58 and the RMSE increase to 0.39 dB as shown in Fig.3f. When raindrops are present in the CPR radar sampling volume, they dominate the CPR observables. In this case, the information provided by the radar reflectivity and mean Doppler velocity is not sufficient to predict well the PIA values reported by the model. This will result in a tendency to overestimate the amount of liquid cloud water content and thus to overestimate the observed attenuation.

The quality of the mass content retrieval can be further improved when the PIA estimate based on the surface reference technique (eq. 26) is corrected for NUBF. We quantify this, by replacing the PIA_{SRT} estimate with the fine-scale antenna pattern averaged attenuation values. In that case, the bias and RMSE in the rain MC estimate is reduced by 14 percentage points for both metrics. This indicates the need for more research on the NUBF and the related forward model adjustments, even in the case of satellite systems with such small footprints as the EarthCARE CPR (Battaglia et al., 2020a).

3.5 Ice and snow

Large natural variability of ice microphysics results in a variety of solid phase hydrometeor structure models. In this study, the mass of the snowflakes is modelled using the parameterization of Morrison et al. (2009), where riming is simulated by filling the gaps between the ice crystal branches with supercooled liquid droplets (Heymsfield, 1982). The mass of snowflakes is parameterized by the power law formula, $m[kg] = \alpha(D[m])^\beta$, with α and β varying for different size regimes. For unrimed aggregate, it is assumed that $\alpha = 0.01$ and $\beta = 2$ which agrees with the simulations (Leinonen and Szyrmer, 2015; Westbrook et al., 2004, e.g.) and in-situ measurements of aggregates (Brown and Francis, 1995; Erfani and Mitchell, 2017; Moisseev et al., 2017). For sizes where the power-law formula would exceed the mass of solid ice spheres, the latter is used. In riming conditions, the smallest aggregates are fully filled with rime, they grow by accretion, so their mass-size relation follows the one for graupel ($\alpha = 86.6$, $\beta = 3$). During riming, large aggregates do not increase their size due to the collection of supercooled droplets, but they only increase their mass proportionally to their projected surface area and the amount of supercooled liquid water the snowflake passes through. This implies that the exponent in the mass-size formula for partially rimed snow remains the same as for unrimed aggregates ($\beta = 2$) and it is only α that increases with the degree of riming. It is implicitly assumed that the mass of rimed aggregates is always larger or equal to the mass of unrimed snow, therefore the maximum between the power-law formulas for rimed and unrimed aggregates is taken. For more detail on this conceptual model, see Mroz et al. (2021) and their Fig. 1, which shows the transition points between different mass-size relationship regimes. With this parameterization, a degree of riming is fully represented by the value of α that is equal to 0.01 for unrimed aggregates and reaches 0.5 for heavily



rimed large graupel particles. The OE retrieval for snow profiles is performed for 5 different values of α , and the one that provides the lowest cost function (see eq. 15) is used as a final state estimate.

3.5.1 Forward model of ice reflectivity, attenuation and Doppler velocities

360 The scattering properties of snow particles are obtained by using discrete dipole approximation corresponding to realistic snowflake shapes (see Leinonen et al., 2016). The original dataset of Leinonen et al. is complemented by large aggregates generated by the authors using the same aggregation model (<https://github.com/jleinonen/aggregation>). The terminal velocity of particles is simulated for standard atmospheric conditions (relative humidity of 50%, $T = 20^\circ\text{C}$, $P = 1013\text{ hPa}$) using the parameterization of Böhm (1992). The physical and scattering properties of individual snowflakes are freely available at
 365 <https://doi.org/10.5281/zenodo.7510186>. The velocity, $U_D(p, T)$, at any temperature T and pressure p is computed via an air density correction as suggested by Foote and du Toit (1969):

$$U_D(p, T) = U_D(\tilde{p}, \tilde{T}) \left[\frac{\tilde{p} \tilde{T}}{p T} \right]^{0.4}. \quad (27)$$

Consistency between the microphysical parameterization and radar simulations is achieved by assuming that the scattering properties of snowflakes are functions of their mass and size only. For this purpose, for a selected mass-size formula (i.e. a selected degree of riming, α), the scattering database is searched for aggregates in the proximity of that relation. More specifically, for a given size D only snowflakes that satisfy $\Delta_m = 10 \log_{10} |m_{\text{snowflake}}(D)/m_{\text{expected}}(D)| < 3$ are considered, i.e., the mass is within a factor of 2 of the formula. Next, depending on the distance from the expected mass-size relation, the particle is assigned its weight, $w(m) = \exp(-\Delta_m^2)$. The scattering properties for a given mass (and α) are computed by locally fitting a degree 5 polynomial to the decimal logarithm of the cross-sections as a function of $\log_{10} m$. The fitting of logarithmic values is adopted because of the large variability of the cross-sections with respect to the mass. Moreover, it reduces the variability of the averaged variables. The terminal velocities are fitted without the logarithmic transformation.
 375

Once the snowflake density model is chosen and the corresponding scattering and falling velocity simulators are obtained, it remains to characterize the particle size distribution so that the description of the forward model of snow is complete. Due to the complexity of snow crystal shapes, the wide range of their densities, the ambiguities in the size definition (von Lerber et al., 2017) and the related difficulties in the PSD measurements, we decided not to use in-situ snow PSD measurements to derive their statistical properties. Instead, it is assumed that the rain that was captured by the disdrometers of the GPM ground validation program has formed from snow melting and thus, by taking into account the differences in raindrop and snowflake terminal velocities, can be used to fully describe the natural variability of PSDs in snow. Implicitly, we assume that melting is the only process that occurs while snowflakes melt, no collision-coalescence, breakup, condensation or evaporation takes
 385 place. By doing so, the particle size distributions in rain (N_r) and snow (N_s) are linked via the following relation:

$$N_s(D_{eq}, \alpha) V_s(D_{eq}, \alpha) dD_{eq} = N_r(D_{eq}) V_r(D_{eq}) dD_{eq} \Rightarrow N_s(D_{eq}, \alpha) = N_r(D_{eq}) \frac{V_r(D_{eq})}{V_s(D_{eq}, \alpha)} \quad (28)$$

where V_r , V_s denotes the terminal velocity in rain and snow, respectively, and D_{eq} is the equivalent-melted diameter. The statistics about the microphysical properties of rain derived in Sect. 3.4.1 translate naturally, through melting-only assumption



formula (28), into characteristics of snow. In particular, the PSD of snow, after melting, converts into the gamma PSD (19)
 390 with $\mu = 10D_m^{-0.8} - 4$. The radar forward model is obtained by combining the electromagnetic and microphysical properties
 of snow. The scattering properties for selected values of α are shown in the Appendix in Figure A2.

3.5.2 A-priori

The a-priori profiles of MC and D_m are generated using the empirical relations that take into account Z_{obs} and temperature.
 Estimates of the mass content and a-priori D_m are based on the relationships provided by Matrosov and Heymsfield (2008)
 395 and Matrosov and Heymsfield (2017).

$$MC[\text{g m}^{-3}] = 0.086 (Z_e[\text{mm}^6 \text{m}^{-3}])^{0.92} \quad (29)$$

$$D_m[\text{cm}] = \begin{cases} 0.052 (Z_e[\text{dBZ}])^{0.28} & \text{for snow,} \\ 0.047 (Z_e[\text{dBZ}])^{0.294} & \text{for cirrus.} \end{cases} \quad (30)$$

The reflectivity profiles are corrected for attenuation before the above relationships are applied. First, the cloud liquid water
 correction is performed. In presence of riming, a constant amount of supercooled LWC (SLWC) is present across the ice layer
 400 for all pixels flagged as riming snow in the C-TC product. Attenuation is computed according to the parameterization provided
 in Sect. A2 and the reflectivity profile is corrected for the SLWC attenuation. Then the ice profile is further corrected for ice
 attenuation using the Hitschfeld and Bordan (1954) approach with the two-way attenuation coefficient proposed by Protat et al.
 (2019):

$$k_{ice}[\text{dB km}^{-1}] = 0.0325Z[\text{mm}^6/\text{m}^3]. \quad (31)$$

405 In presence of a PIA measurement, if the attenuation is overestimated, the LWC is reduced to match the PIA. On the other
 hand, if the correction underestimates the PIA, the coefficient in Z-k relation is scaled to match the PIA.

3.6 Cold rain

The cold rain retrieval capitalizes on the modelling for the liquid phase described in Sect. 3.4 and on the solid phase described in
 Sect. 3.5. In cold rain, in the layer where temperatures become warmer than 0°C , hydrometeors transition between the solid and
 410 liquid phases. This region is very well identified by the target classification (C-TC). The modelling for Doppler velocities and
 reflectivities for the solid and the liquid phase follows what is described in Subsect. 3.4.1 and in Subsect. 3.5.1. The melting
 layer is not modelled and observables within the melting layer are not fitted like it was done in Tridon et al. (2019b). The
 melting layer attenuation coefficient is estimated to be proportional to the mean rain rate of the rain layer underneath:

$$k_{ML}[\text{dB km}^{-1}] = \gamma_{ML} \langle PR_{rain}[\text{mm}/\text{h}] \rangle^{\delta_{ML}} \quad (32)$$

415 with $\gamma_{ML} = 2.6$, $\delta_{ML} = 0.87$ as proposed by Matrosov (2008). This estimate is used as a soft constraint only, i.e., the bright
 band extinction is added to the vector of the unknown variables. During the OE iterations, the difference between its expected



and state vector value is minimized, assuming the uncertainty in the Matrosov formula to be a factor of 2. The liquid cloud content (in logarithmic units) is also retrieved in cold rain. It is assumed that the liquid cloud is distributed between the freezing level and the height of the LCL according to (2). Due to the high uncertainty as to the occurrence of the cloud and its possible water content, it is assumed that the a-priori estimate of the cloud water path is very small, i.e. 0.1 g m^{-2} , which has no effect on the radar measurements. The relative uncertainty of this estimate is set to be 100 dB which reflects no prior knowledge of this parameter.

Unlike the retrieval of snow profiles, the cold rain retrieval is performed for one value of α , only. Selection of the best α is based on the continuity of the mass flux between the solid and the liquid phase, and it follows these steps: first, utilizing equations (A1, A2) the mass content and the characteristic size of rain below the melting layer is estimated from the mean Doppler velocity and radar reflectivity measurements corrected for attenuation using the PIA constrained Hitschfeld and Bordan technique. Once the water content and the size of rain are known, the radar simulations in the ice part are performed for logarithmically sampled values of α ranging from 0.01 to 0.5 assuming that the melted equivalent D_m and the precipitation rate in rain and ice are the same, i.e. melting is the only process within the melting zone (Mróz et al., 2021). Then, the distance between the radar simulations and the measurements in the radar bin above the melting zone is computed for all considered values of α , taking into account corresponding measurement uncertainties. Finally, α that minimizes this distance is selected for the retrieval.

3.6.1 Example of retrieved profiles and retrieval performances

The cold rain and snow retrieval was applied to all the simulated scenes; in Fig. 4 the "Halifax" scene over eastern Canada is presented (for more detail on the simulated scenes see Donovan et al., 2022). The left-hand side panels show the model output, while the right-hand side panels depict the retrieval and the simulated radar observables. The first part of the scene is occupied by light and moderate snow, with the cloud tops below 5 km. The second part presents ice clouds reaching 8 km and the associated stratiform precipitation with the melting layer between 2 and 3 km ASL, clearly highlighted by a sharp change in the Doppler signal. The cold rain part features a heavy precipitation band associated with convection where the rain rates exceed 10 mm h^{-1} .

Overall, the C-CLD algorithm reliably reproduces the radar measurements corresponding to the precipitation structure and despite being designed for stratiform rain, it performs relatively well even for convective profiles characterized by moderate precipitation conditions. The largest differences between the simulations and the retrieval within the stratiform rain systems are observed around the along-track distance of 3450 km close to the ground.

The problem that affects these profiles is a misclassification in the C-TC product of pixels with a mixture of ice and rain as pure snow columns. This leads to erroneously large D_m estimates and failure of the algorithm. The worst performance of the algorithm is observed for the retrieval of D_m in snow. Due to limited information content about the density of ice in the instrument illuminated volume, different degrees of riming tested by the algorithm can provide comparable cost function values. Therefore, the choice of the final solution may not be entirely accurate. Future work on the algorithm should focus on including such ambiguities in the final uncertainty estimates of the state vector.

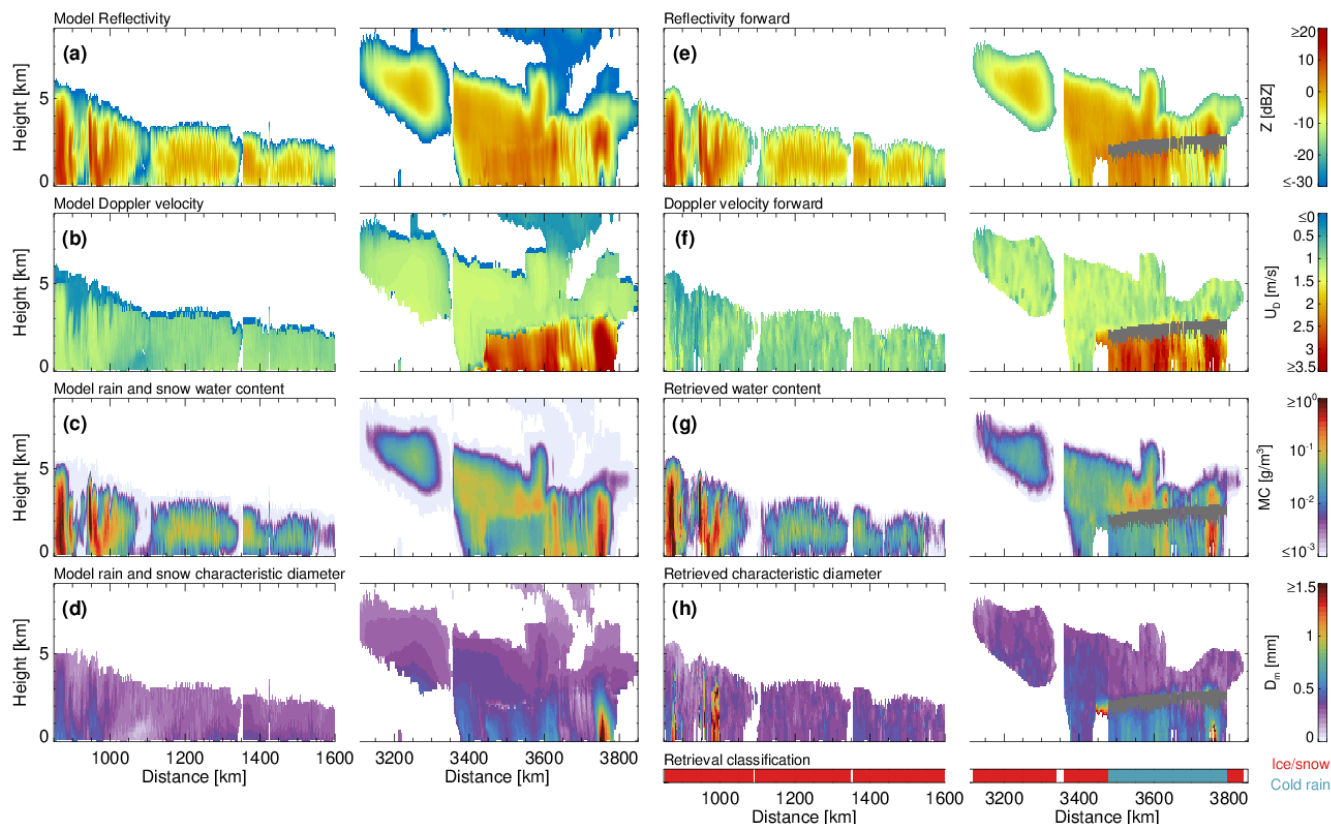


Figure 4. Panels (a), (b), (c) and (d) show the model radar reflectivity, Doppler velocity, mass content and mean mass weighted characteristic diameter for the ice and cold rain regions of the Halifax scene. Panels (e), (f), (g) and (h) show the forward radar reflectivity and Doppler velocity and the retrieved mass content and mean mass-weighted characteristic diameter applied to all regions where $Z > -21$ dBZ. The grey band represents the melting layer where the retrieval is not applied

Statistics on the retrieval accuracy based on all the scenes are presented in Fig. 5. The results for snow microphysical parameters combine the solid phase part of cold rain profiles and pure snow profiles. These statistics correspond to radar reflectivity values in excess of -21 dBZ where Doppler velocity is considered reliable and the retrieval shows a full potential of Z and U_D measurements. The snow MC retrieval is strongly correlated with the model output, with a slight tendency to underestimate. The reported RMSE of 0.23 B corresponds to a fractional uncertainty of 53%. The retrieval of D_m is more ambiguous (which is reflected in higher values of NRMSE) due to the limited variability of Doppler measurements with snow size, especially in the case of low-density ice (Fig. A2). Moreover, due to non-Rayleigh effects the reflectivity is not a monotonic function of the size, which additionally hampers the retrieval. This results in a moderate correlation coefficient of 0.68. As expected, the sizing retrieval in rain has a higher correlation and lower RMSE values than in ice due to the tighter relationship between the size and mean Doppler velocity. Like in the case of warm rain, the algorithm underestimates sizes above 0.6 mm and underestimates the MC values. However, in cold rain these differences are more pronounced because, in

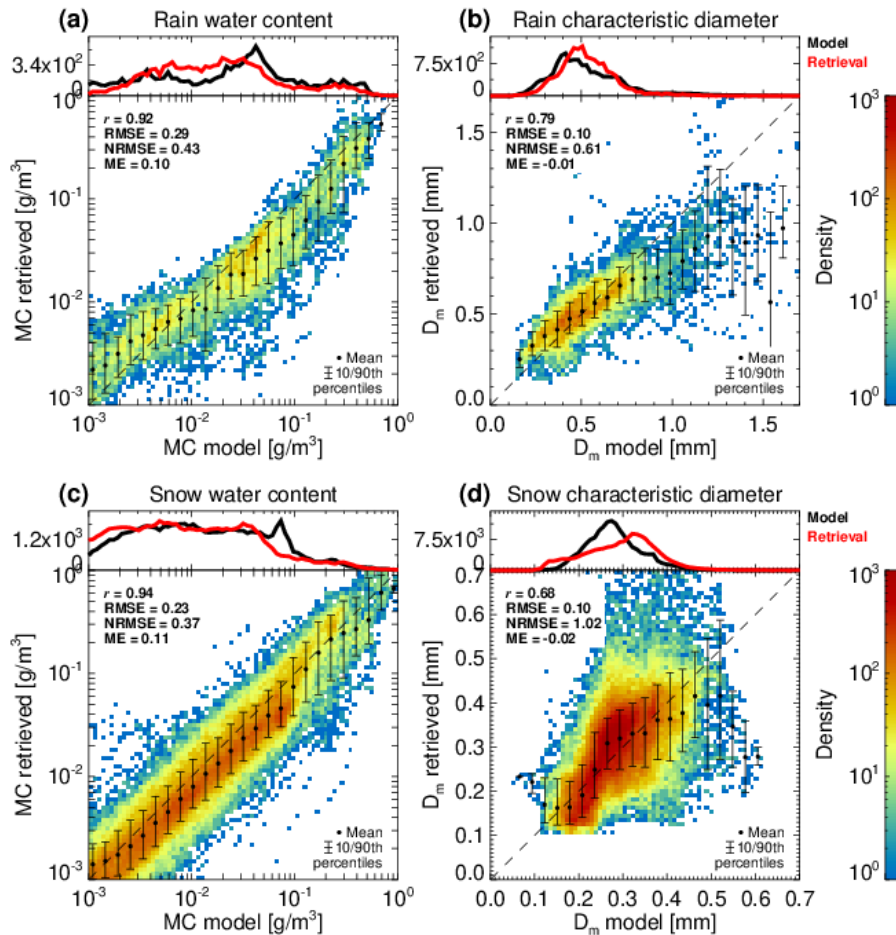


Figure 5. The algorithm performance histograms based on the 3 GEM scenes. The x-axis represents the model values while the y-axis corresponds to the retrieval. Panels (a) and (b) show the rain water content and rain characteristic diameter. Panels (c) and (d) show the snow water content and snow characteristic diameter. The profiles with significant contributions of graupel and hail and the regions at cloud tops where the measurements are not very well constrained (large U_D error) are excluded from the analysis.

465 addition to NUBF effects, they are amplified by differences between the forward model used in retrieval and the one used in GEM simulations (not shown). Our forward model provides higher Doppler velocity for sizes exceeding 0.7 mm and smaller velocities below this size, which explains differences in the retrieved size. These differences propagate further into the MC retrieval. For $D_m < 0.7$ mm the radar reflectivity increases with size, so an overestimate in D_m causes negative bias in the MC retrieval. When $D_m > 0.7$ mm, reflectivity decreases, and thus the MC is underestimated also for large raindrops.



3.7 Stability and sensitivity of the Optimal Estimation biases in the measurements, the forward model and the a-priori

The calibration of radar systems and correct assumptions on microphysics are paramount for the accuracy of remote sensing retrievals. This is presented in Fig. 6 where the precision of the C-CLD algorithm in rain with various error sources is tested. The quality of the retrieval is quantified in terms of the NRMSE. First, the sensitivity of the retrieval to biases in the measurements is tested by adding a constant offset in the forward model to the radar reflectivity and the Doppler velocity. Note that this is equivalent to adding a bias with an opposite sign to the measurements, thus the calibration errors and model biases are tested simultaneously. As expected, the retrieval of the MC is mainly affected by the biases in the reflectivity, which is manifested in the valley-like shape of a local minimum with the RMSE changing mainly along $\log_{10} MC$ direction. Having said that, some compensation effect is also observed, i.e., the RMSE shows little variability if Z and U_D are simultaneously increased or decreased according to the slope shown in Panel a. This is due to the characteristics of the forward model, namely the fact that the reflectivity depends on both the mass and the content of rain. Thus, for a fixed mass, deviations in the reflectivity are compensated for by changes in D_m corresponding to changes in the Doppler velocity. The accuracy of the retrieval of $\log_{10} D_m$ is also driven mainly by one variable, the mean Doppler velocity. As for the other unknowns, biases in the Doppler velocity measurements can be, at least to a certain degree, compensated by an offset in the reflectivity. However, due to a very constrained relation between D_m and U_D , the compensation is not as effective as for the MC retrieval and is mainly driven by the Z - D_m relationship used for the a-priori estimate.

The position of a local minimum of the average of the NRMSE in $\log_{10} D_m$ and $\log_{10} MC$ indicates the "reference" point that provides the best possible retrieval. As it can be seen, the minimum is shifted away from the origin, which indicates differences between the forward model used in the retrieval and the one used for simulations. An offset of 0.4 ms^{-1} and -1 dB in U_D and Z , respectively, would improve the reported retrieval uncertainties, but we decided not to alter our radar simulator as there is no evidence of the GEM model assumptions being superior to those used in the retrieval.

A similar analysis was performed to quantify the effect of the a-priori assumption on the quality of the retrieval. As expected, the retrieval of D_m is mainly affected by its a-priori, and the same applies to the retrieval of MC . The error in the MC estimation resulting from differences between forward models (or calibration errors) can be reduced by changing the a-priori assumptions and the optimal retrieval is obtained if $\log_{10} MC$ is increased by approximately 0.5 (i.e. a factor of 3.2). This indicates that for a given reflectivity value in rain, the mean mass content in the GEM model is larger than our a-priori estimate. It raises the question of whether the Z - MC relationship based on the DSD measurements at the ground (which typically fail in detecting small raindrops and low rain rates) that provides the basis of our forward model, is applicable in the low precipitation rate regime ($Z < 10 \text{ dBZ}$), that constitutes the majority of the profiles tested here.

4 Conclusions

The C-CLD is the L2 data product designed to take as input the EarthCARE 94-GHz Doppler Cloud Profiling Radar measurements and output microphysical information about cloud and precipitation systems. For the most part, C-CLD uses an

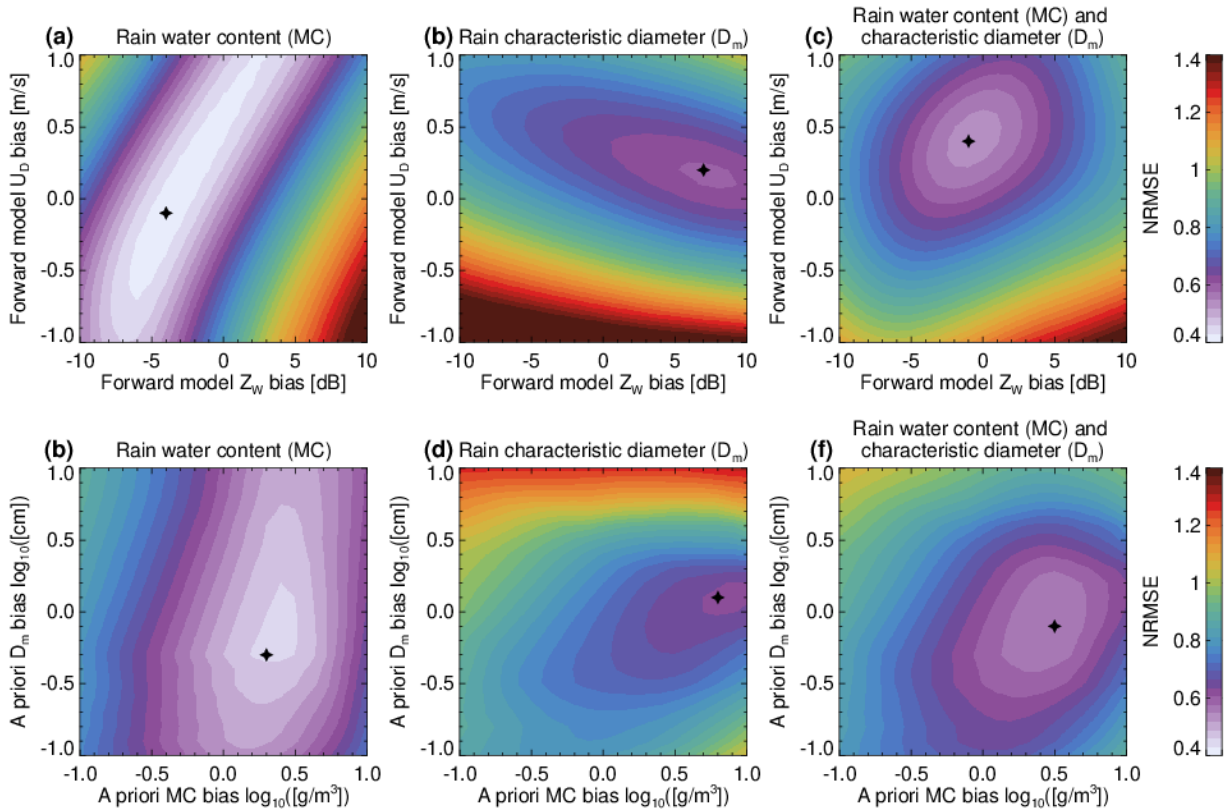


Figure 6. Performance of the C-CLD algorithm applied to the Halifax scene in terms of rain MC and D_m NRMSE as a function of forward model Z and U_D bias (panels (a), (b) and (c)) and a-priori MC and D_m bias (panels (d), (e) and (f)). Panels (c) and (f) represent the average MC and D_m NRMSE. The cross corresponds to the minimum of the NRMSE.

500 OE algorithm that balances information provided by the CPR and the a-priori knowledge on the climatology of cloud and precipitation systems. Due to the information content provided by the CPR, the algorithm is designed to retrieve profiles of two moments of the PSD drop size (mass content and mean mass weighted diameter).

A large dataset of in-situ, surface-based observations is used to reduce the number of free parameters and to obtain the forward model relations with the corresponding uncertainties. In addition, mass flux conservation through the melting layer is assumed and only small perturbations from this condition are allowed. A one-dimensional parameterization for the representation of a wide range of ice particle densities from unrimed snowflakes to dense graupel particles is proposed. In the case of drizzle-free and lightly drizzling warm clouds, the optimal OE framework is replaced by climatological relationships between the measured reflectivities and the microphysical parameters of interest.

The C-CLD retrieval framework has been applied to EarthCARE CPR simulated observations from high-resolution weather systems simulations occurring in three different climatological regimes (Donovan et al., 2022): tropical climate, humid conti-



mental climate bordering on an oceanic climate (Halifax), and mid-latitude conditions over the North America (Baja). The CPR reflectivity and Doppler radar measurements provide sufficient information to retrieve, with high confidence, two moments of the PSD, especially in rain due to the added value of the Doppler measurements, which, in stratiform rain, are closely related to the raindrop fall speed, and thus to its mean size. On average, the mean mass-weighted diameter (D_m) of rain can be estimated within a precision of 23% with negative bias reported for large sizes. As a result, the estimate of rain mass content (MC) is also well captured by matching the radar reflectivity to the observations. The uncertainty of the MC estimate is estimated to be 67% for all the GEM simulation scenes combined. Despite more complex and ambiguous scattering properties of ice particles, errors in the ice mass content are smaller than in rain, and they are equal to 53% for profiles including either snow-only or cold rain. This unexpected result may indicate differences in the forward model used in GEM simulations and in the retrieval of rain, or difficulties in separating path integrated attenuation (PIA) into the liquid cloud, melting layer, and rain components. The most challenging retrieval is the one of D_m that is characterized by the lowest correlation coefficient and the highest value of the normalized root-mean-square-error among all the considered unknowns. The variety of snowflake morphology and the corresponding diversity in the relation between particle size and terminal velocity results in uncertainties of 23 %.

Due to the high susceptibility of W-band measurements to signal attenuation, the quality of the retrieval is strongly reduced when the path integrated attenuation estimates are not assimilated. This is reflected in the degradation of the quality of the mass content retrieval in warm rain conditions, i.e., the RMSE in $\log_{10} MC$ increases from 0.27 B to 0.45 B while the correlation coefficient is reduced from 0.97 to 0.75.

Thanks to its large antenna, CPR's unprecedented fine horizontal resolution minimizes the impact of two of the challenges of space borne radar-based precipitation remote sensing: multiple scattering (Battaglia et al., 2010; Matrosov et al., 2008; Matrosov and Battaglia, 2009) and non-uniform beam filling (NUBF; Tanelli et al., 2012). Since the horizontal resolution of the model simulations is finer than the one of the radar, errors related to NUBF are quantified and included in the reported total algorithm errors, with small biases observed. Furthermore, negligible multiple scattering effects were simulated and reported to the flag produced in C-PRO (Kollias et al., 2022b).

Further development of the algorithm requires testing under conditions that are not included in the simulations used in this study. In particular, simulations of weather systems with raindrops/snowflakes significantly larger than 1 mm are missing here. These conditions are particularly challenging for W-band retrievals due to significant signal attenuation and saturation of the radar reflectivity and Doppler measurements (Mróz et al., 2019). On the other hand, more in-situ measurements of drizzle size particles are necessary for more credible a-priori estimates in this regime. This aspect should be addressed during the calibration-validation activities. Similarly, additional research is needed to characterize the shape of the liquid cloud mass content profiles, as it is one of the main sources of uncertainty in the path-integrated attenuation simulations and thus in the retrieved rain/snow mass content below the liquid cloud top. As suggested by Battaglia and Panegrossi (2020) this issue can be mitigated by the inclusion of the W-band brightness temperatures in the observables adopted in the derivation of the C-FMR product. In addition, in order to produce realistic transitions in the retrieved state vector between consecutive profiles, future algorithms could make use of the two-dimensional information provided by the radar. This should help not only in preserving the continuity of the state vector but also in the quantification of NUBF (and its correction) and in the detection of non-



precipitating liquid clouds whose boundaries tend to have long correlation lengths and therefore can be detected outside from precipitating systems where they may be visible and extrapolated inside precipitating systems where their signal is masked by the larger hydrometeors.

The reported uncertainties are heavily dependent on the forward model accuracy and on the measurement calibration biases. 550 The performed analysis revealed that, due to some differences in the fall velocities used in the GEM model and in the C-CLD retrieval framework, a systematic overestimation (underestimation) of small (large) raindrop sizes is present. These errors, combined with discrepancies in the reflectivity forward model, result in a negative bias of the rain mass content. The differences between the simulators are attributed to the different particle size distribution shape assumptions. Although the difference between the radar simulators was not systematic (i.e. it has a different sign depending on the rain characteristic size), the bias 555 in the mass content retrieval was. This shows how susceptible to model/measurement biases the optimal estimation framework is and how important the calibration of the EarthCARE reflectivity and Doppler velocity (Battaglia and Kollias, 2014) will be.

Despite the detection of differences between the GEM simulations and our radar model, the algorithm was not fine-tuned to match model assumptions due to the lack of evidence that the model could reflect reality better than the long-term particle size distribution statistics. This manuscript aims at providing a physical basis for the retrieval, and so the modifications of the 560 forward model or of a-priori assumptions are left for the calibration/validation activities period after the launch of the satellite.

Finally, future work should include cross-validation with the other precipitation products (Mason et al., 2022a), e.g. ACM-CAP that provides a synergistic retrieval of the hydrometeor properties based on the full suite of sensors onboard the Earth-CARE satellite. This latter product should provide more accurate estimates due to the increased information content provided by the other instruments.

565 **Appendix A: Parameterization of scattering properties at W-band**

Here, we report the parameterizations of the scattering properties at 94-GHz that are used in C-CLD. These relations link the CPR observables (reflectivity Z_e and Doppler velocity U_D) with two state vector parameters (D_m and MC) in terms of power laws. This simplifies the analytical computation of the Jacobian.



f	Z	k	U_D	PR
c_0	1.753507473e+02	1.061446625e+02	-7.878213785e+00	1.462599005e+01
c_1	1.516600758e+03	9.773037642e+02	-1.154722711e+02	-2.509159043e+00
c_2	6.283964040e+03	4.009203831e+03	-3.316155732e+02	-6.430492096e+00
c_3	1.421269360e+04	8.912225708e+03	-4.482927812e+02	-7.573354723e-01
c_4	1.916701560e+04	1.182437649e+04	-3.176017676e+02	
c_5	1.570071551e+04	9.570123072e+03	-1.130125193e+02	
c_6	7.622732776e+03	4.610284065e+03	-1.589687728e+01	
c_7	2.012452449e+03	1.211200335e+03		
c_8	2.223312876e+02	1.333794232e+02		

Table A1. Coefficients of the polynomial representation of the forward model for rain given by formulas A1, A2, A3, A4.

A1 Rain

570 The radar observables and PSD moments are approximated by polynomials in $x = \log_{10} MC[\text{g m}^{-3}]$ and $y = \log_{10} D_m[\text{cm}]$, i.e.:

$$Z[\text{dBZ}](x, y) = 10x + P_Z(y) = 10x + \sum_{i=0}^n c_i^Z y^i; \quad (\text{A1})$$

$$U_D[\text{m/s}](x, y) = P_{U_D}(y) = \sum_{i=0}^n c_i^{U_D} y^i; \quad (\text{A2})$$

$$10\log_{10}(k[\text{dB km}^{-1}])(x, y) = 10x + P_k(y) = 10x + \sum_{i=0}^n c_i^k y^i; \quad (\text{A3})$$

$$575 \quad 10\log_{10}(PR[\text{mm h}^{-1}])(x, y) = 10x + P_{PR}(y) = 10x + \sum_{i=0}^n c_i^{PR} y^i; \quad (\text{A4})$$

$$(\text{A5})$$

where the coefficients c_i^f for $f = Z, k, U_D, PR$ are given in Table A1. The degree of the fitting polynomial results from its high accuracy in replicating the simulations for the gamma PSD model over a broad range of characteristic rain sizes, i.e., from 0.1 to 3.5 mm.

580 A2 Cloud attenuation coefficients

The two-way attenuation coefficient in $\text{dB km}^{-1} \text{g}^{-1} \text{m}^3$ is parameterized as a quadratic function of the temperature expressed in Celsius with the 0^{th} , the 1^{st} and the 2^{nd} order coefficients equal to [8.4979, -0.0062, -0.0022]. This replicates very well the empirically verified model at 94 GHz (Tridon et al., 2020, Fig. 1) with a maximum of about $8.5 \text{ dB km}^{-1} \text{g}^{-1} \text{m}^3$ at 271.8 K decreasing to $7 \text{ dB km}^{-1} \text{g}^{-1} \text{m}^3$ at 245.7 K and at 297.8 K.

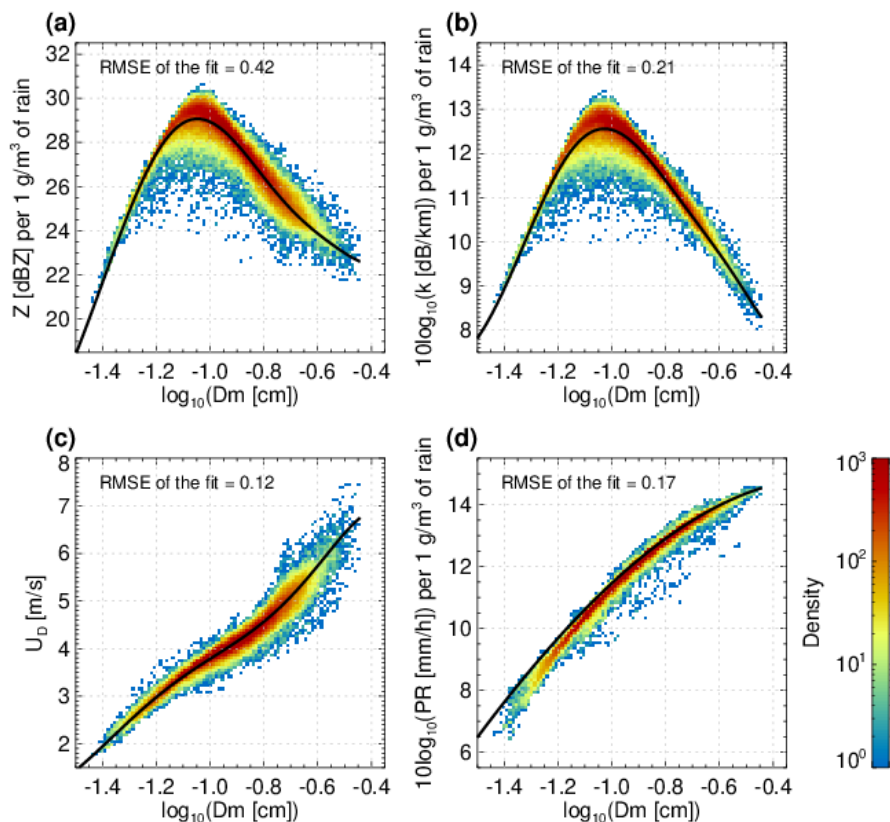


Figure A1. Two-dimensional histograms of the radar observable simulations corresponding to the in-situ PSD measurements at the ground. Panel (a): radar reflectivity factor in dBZ per 1 g m^{-3} of rain. Panel (b): $10\log_{10}$ of the (one way) specific attenuation [dB km^{-1}] per 1 g m^{-3} of rain. Panel (c): mean Doppler velocity in standard atmosphere Panel (d): precipitation rate in standard atmospheric conditions ($15^\circ\text{C}, 1013.25 \text{ mb}$) per 1 g m^{-3} of rain. The black line shows the simulations for the gamma PSD model with $\mu = 10D_m^{-0.8} - 4$ that is used as a forward model.

585 **A3 Ice**

As in the case of rain, the radar observables and PSD moments are approximated by polynomials in $x = \log_{10} MC[\text{g m}^{-3}]$ and $y = \log_{10} D_m[\text{cm}]$. These polynomials are of different degrees and their coefficients depend on the degree of riming. Therefore, it is impractical to list all the coefficients here. Instead, these tables are freely available at <https://doi.org/10.5281/zenodo.7529739>. Fig. A2 shows the scattering properties as parameterized in the forward model for 5 selected degrees of riming. Note that while attenuation and Doppler velocities tend to increase with melted diameter, reflectivities reach maximum values in correspondence to sizes between 0.4 and 0.8 mm.

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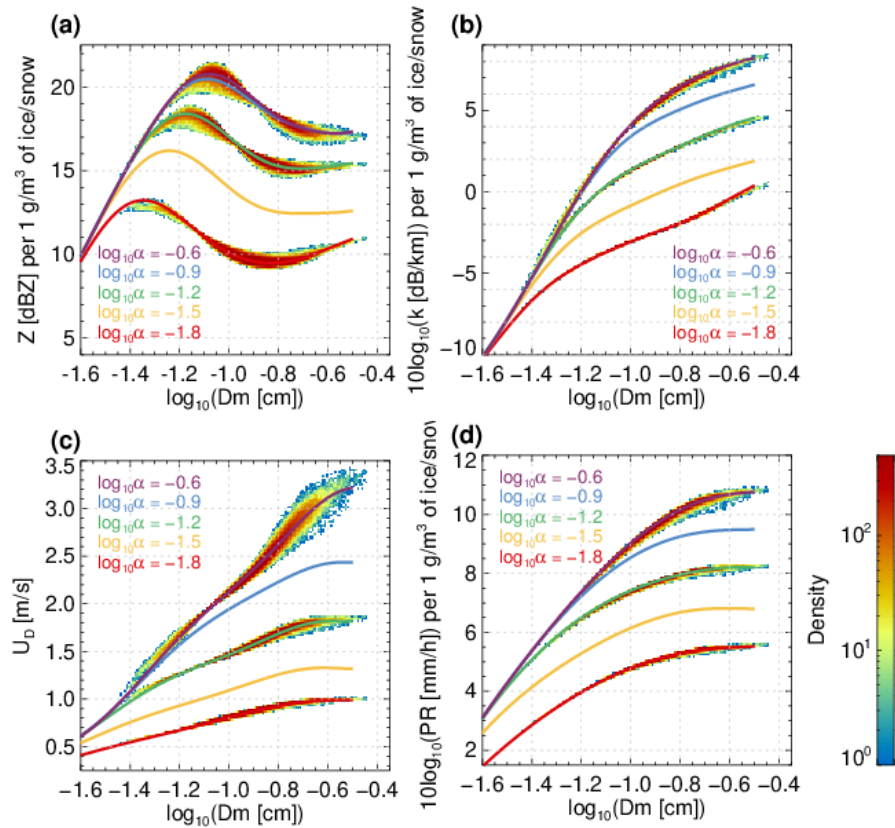


Figure A2. Ice scattering properties as parameterized in the forward model as a function of the melted equivalent size; different colors correspond to different degrees of riming (α). For selected values of α , the histograms in the background show the gamma PSD modeling corresponding to the rain PSD measurements collected at the ground based on the "melting only" assumption (see Sect. 3.5.1). The line represents $\mu = 10D_m^{-0.8} - 4$. All the simulations are performed for 1 g m^{-3} of snow. Panel (a): radar reflectivity factor in dBZ. Panel (b): $10 \log_{10}$ of the (one way) specific attenuation [dB km^{-1}]. Panel (c): mean Doppler velocity in standard atmosphere. Panel (d): precipitation rate in standard atmosphere.



Appendix B: Other parameterizations

The vertical gradient of the change of adiabatic LWC is calculated as in Rogers and Yau (1989) and is parameterized as:

$$\frac{\partial LWC}{\partial z} = \rho_{air} \frac{c_p}{L_{ev}} (\Gamma_d - \Gamma_s) \approx (d_0 + d_1 T_c + d_2 T_c^2) \left(\frac{p}{p_{90 kPa}} \right)^{c_0 + c_1 T_c} \quad (B1)$$

595 with $[d_0, d_1, d_2, c_0, c_1] = [1.615, 0.0554, -6.287 \cdot 10^{-4}, 0.42, 0.015]$.

Data availability. The EarthCARE Level-2 demonstration products from simulated scenes, including the C-CLD product discussed in this paper, are available from: <https://doi.org/10.5281/zenodo.7311704>. The dataset of single scattering properties of large snow aggregates used in this study is available at: <https://doi.org/10.5281/zenodo.7510186>. Parametrization of scattering properties at W-band for a population of ice particles is available at <https://doi.org/10.5281/zenodo.7529739>.

600 *Author contributions.* KM led the preparation of the paper and developed the retrieval scheme. KM and BPT performed the analysis presented here. AB and PK advised on the methodology of the algorithm. BPT and AT led the FORTRAN implementation of the algorithm. BPT generated all the figures. FT contributed to the development of the W-band radar simulator. The manuscript was written by KM, BPT, AB, PK.

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