The flexural isostatic response of climatically driven sea-level changes on continental-scale deltas

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Abstract. The interplay between climate-forced sea-level change, erosional and depositionional processes, and flexural isostasy in deep time on passive margin deltas remains poorly understood. We performed a series of conceptual simulations to investigate flexural isostatic responses to high-frequency fluctuations in water and sediment load associated with climatically driven sea-level changes. We model a large drainage basin that discharges to a continental margin and produces a large deltaic depocenter, then prescribe synthetic and climatic-driven sea-level curves of different frequencies to assess flexural response. Results show that flexural isostatic responses are bidirectional over 100-1000 kyr timescales and are in sync with the magnitude, frequency, and direction of sea-level fluctuations, and that isostatic adjustments play an important role in driving along-strike and cross-shelf river-mouth migration and sediment accumulation. Our findings demonstrate that climate-forced sea-level changes produce a feedback mechanism that results in self-sustaining creation of accommodation into which sediment is deposited and plays a major role in delta morphology and stratigraphic architecture.

1 Introduction

Flexural isostatic processes in large deltaic depocenters generally reflect the accumulation of sediment loads on the crust over 10s of millions of years, and, within the depositional basin itself, can be treated as unidirectional subsidence at the first order (Fig. 1; e.g., Driscoll and Karner et al., 1994; Reynolds et al., 1991; Watts et al., 2009). Over time scales of 10^3 to 10^6 yrs, however, the nature of flexural isostatic response to crustal loading and unloading by ice during Quaternary climate-forced glacial-interglacial cycles is well-documented: such glacial isostatic adjustments (GIA) include bidirectional (subsidence and uplift) and cyclical deflections of earth's surface (e.g., Clark et al., 1978; Mitrovica and Peltier 1991; Lambeck et al., 2014; Whitehouse, 2018). In addition to near-field flexural responses to the direct loading and unloading by ice, GIA includes far-field effects, and is associated with hydro-isostatic responses of shorelines to climate-forced global changes in sea level (e.g., Chappell, 1974; Thom and Chappell, 1978; Lambeck and Nakada, 1990; Lambeck et al., 2003; Potter and Lambeck, 2003;

Muhs et al., 2020 and many others). The cummulative deep-time (10^7 to 10^8 yrs or more) subsidence within the depositional basin represents the accommodation that results in preservation of the stratigraphic record, and is generally well understood, but the stratigraphic imprint of bidirectional and cyclical flexural responses to changes in sediment and water loads over shorter time scales ($<10^6$ to 10^7 yrs; Fig. 2), as driven by global climate and sea-level change, remain less well known.

A large body of data demonstrates close coupling over multiple time scales between climate and the globally coherent component of sea-level change that reflects global changes in ice volumes (Fig. 3; Miller et al., 2020 and references therein). Interglacial periods are characterized by lower ice volumes, higher sea level, and more landward shoreline positions, and generally result in sediment accumulation in more proximal parts of the shelf. By contrast, glacial periods are characterized by higher ice volumes, lower sea-level positions, and a corresponding basinward shift in shorelines, and generally result in the preferential transfer of sediment to the shelf margin and deep-water parts of sedimentary basins (Johannessen and Steel, 2005; Carvajal et al., 2009; Blum et al., 2008; Sømme et al., 2009; Sweet and Blum, 2016; Mason et al., 2019; Sweet et al., 2020; 2021). Bidirectional high-frequency glacio- and hydro-isostatic adjustments have been extensively studied and are known to significantly impact relative sea-level histories (e.g., Clark et al., 1978; Nakada and Lambeck, 1989; Lambeck, 1995; Mitrovica and Milne, 2003; Peltier, 2004; Lambeck et al., 2014; Whitehouse, 2018). Moreover, a few studies have begun to elucidate the presence and significance of high-frequency, cyclical sediment- and hydro-isostatic adjustments associated with the response of fluvial and deltaic systems to climate and sea-level change. Such studies have focused on the continental scale Mississippi River delta (e.g., Ivins et al., 2007; Blum et al., 2008; Wolstencroft et al., 2014; Kuchar et al., 2018), the Rhone delta in southern France (e.g., Jouet et al., 2008) and conceptual modeling (e.g., Blum et al., 2013).

In this paper, we use numerical models to examine the impact of climate-forced global sea-level change, erosional and depositional processes, and flexural isostatic response on the stratigraphic evolution of large deltaic depocenters over time scales of 10^6 to 10^7 yrs (Fig. 3). We use the basin and landscape dynamics code BADLANDS (Salles and Hardiman, 2016; Salles et al., 2018) to develop a continental-scale fluvial-deltaic to deep-water sediment-dispersal system and perform a series of tests where we impose synthetic and climate-driven sea-level curves of different frequencies to explore the relationships between patterns of sediment accumulation, flexural subsidence, and load partitioning. The coupling of surface processes with flexural isostasy allows us to investigate feedbacks between global sea-level change, erosional and depositional processes, and flexural uplift and subsidence within a dynamic framework. Hence, we use an iterative approach because the flexural response can also generate relative changes in sea level, which in turn can modify the spatio-temporal characteristics of isostatic compensation. Our approach is more comprehensive than previous studies that have investigated the role of high-frequency flexural isostatic adjustments in a static manner (e.g., Blum et al., 2008; Jouet et al., 2008), and our experiments produce the clear stratigraphic impacts of high frequency, bidirectional flexural adjustments that are driven by climate-forced global sea-level change on the morphology, architecture and long-term stratigraphic evolution of large deltaic depocenters.

2 Components of Vertical Motion in Passive Margin Deltaic Depocenters

Accommodation from subsidence in large passive margin deltaic depocenters is generated by multiple processes that operate over different time scales, at different depths, and at different rates. (Fig. 1). At the largest spatial and temporal scales, tectonic subsidence is initiated during the initial rifting phase by stretching and thinning of the lithosphere (e.g., Mackenzie, 1978; Galloway, 1989), followed by thermal cooling and contraction of upwelled asthenosphere, which causes the margin to subside during the post-rift phase. In some cases, the amount of post-rift subsidence may exceed the possible thermal contribution, in which case anomalous subsidence has been attributed to dynamic processes that reflect changes in mantle flow (e.g., Wang et al., 2017; Wang et al., 2020).

Vertical movements in passive margin deltaic depocenters over time scales of 10^6 yrs and longer are also known to include flexural isostatic response to sediment loading, which produces bending of the lithosphere (Watts et al., 2009). Flexural responses of this kind are typically characterized by subsidence in the depositional basin and development of low-amplitude peripheral bulges 100s of km onshore and/or alongshore from the depocenter. Published examples include the Amazon (Driscoll and Karner, 1994; Watts et al., 2008), Niger (Doust and Omatbola, 1990) and Mississippi (e.g., Jurkowski et al., 1984; Feng et al., 1994; Frederick et al., 2019) systems. Over shorter Milankovitch orbital time scales of 10^4 to 10^6 yrs, GIA results from climate-driven growth of land ice and loading of continental land masses, and the inverse, melting of land ice and unloading (glacial-isostatic adjustment or GIA) (e.g., Sella et al., 2007; Milne, 2015; Whitehouse, 2018). The growth and decay of land ice also results in global sea-level fall and rise, with unloading and loading of the continental shelves. The impacts of GIA and associated hydro-isostasy extend through the marine to terrestrial parts of the system to different degrees, but are bidirectional and cyclical over Milankovitch time scales. GIA has a large footprint that includes development of a foredeep proximal to the ice load, and a low-amplitude peripheral forebulge located 1000s of km away, with each migrating as a flexural wave in response to growth and decay of ice masses. By contrast, hydro-isostasic impacts are generally limited to the marine environment and the lower reaches of large fluvial-deltaic systems, but can result in cycles of uplift and subsidence that have been hypothesized to drive changes in the magnitude of fluvial incision and filling of coastal plain to cross-shelf valley systems as the river mouth migrates basinward and landward (Blum et al., 2013).

Growth faults (e.g., Gagliano, 2003; Armstrong et al., 2014; Shen et al., 2016; Pizzi et al., 2020), salt tectonics (Morley et al 2011; King et al., 2012; Jackson and Hudec, 2017) and compaction of the sediment column (Athy, 1930; Meckel et al., 2007) also contribute to long- and short-term subsidence in deltaic depocenters. Subsidence patterns associated with these drivers can affect coastal and fluvial depositional processes, for example, the steering of fluvial channels and their associated patterns of deposition due to creation of local topographic highs and lows (100s to 1000s of km^2 e.g., Gagliano, 2003; Armstrong et al., 2014; Morón et al., 2017). Moreover, for the modern Mississippi and other large deltas, delta-plain subsidence over

timescales of 10^4 yrs or less is dominated by dewatering and consolidation of recently deposited muddy and/or peat-rich Holocene sediments within the uppermost 10s of m of strata (Tornqvist et al., 2008; Keogh et al., 2021; Steckler et al., 2022).

100 Subsidence processes in deltaic depocenters operate at different rates, and there is generally an inverse relationship between measured or estimated rates and the time interval over which rate measurements are integrated (e.g., Sadler, 1981; 1999; Frederick et al., 2020; Steckler et al., 2022). On one end of the spectrum, annual cycles of uplift and subsidence with amplitudes up to 60-75 mm have been recorded in the Amazon basin and the Ganges-Brahmaputra delta due to loading by, then drainage of, seasonal rains (Bevis et al., 2005; Steckler et al., 2010). Moreover, over time scales of decades to centuries,

105 subsidence rates associated with consolidation and dewatering of Holocene deltaic sediments can be 5-15 mm/yr (e.g., Tornqvist et al., 2008; Jankowski et al., 2017; Keogh et al., 2021; Steckler et al., 2022). On the other end of the spectrum, time-averaged rates of vertical motion associated with deep-seated subsidence drivers (tectonic and/or dynamic subsidence, long-term loading and lithospheric flexure, and deep-seated long-term compaction) can be very low (Frederick et al., 2019): for example, over time scales of 10^6 yrs or more, flexural uplift of ~0.1 mm/yr characterizes the landward margin of the

110 Mississippi depocenter. Then, moving south from a hinge line on the delta plain, long-term subsidence rates increase from zero to ~3 mm/yr at the shelf margin,(e.g., Frederick et al., 2019; Fig. 11e).

3 Numerical methods

Measuring vertical motion from the longer-term stratigraphic record within a sedimentary basin tends to result in a sense of unidirectional subsidence with low rates that decrease as the interval over which they are measured increases. By contrast,

115 studies of the more recent stratigraphic record of deltaic depocenters make it clear that isostatic processes can be driven by climate change, and are both bidirectional and cyclical (e.g., Blum et al., 2008; Jouet et al., 2008; Bevis et al., 2005; Steckler et al., 2010). In this paper, we use the BADLANDS modelling software (Salles and Hardiman, 2016; Salles et al., 2018) to examine the effects of climate-forced sea-level change, erosional and depositional processes, and bidirectional flexural isostasy on the morphology, architecture and stratigraphic evolution of large deltaic depocenters in deep time. BADLANDS links

120 landscape and basin dynamics through simulation of erosion, landscape evolution, and sedimentation where the rate of river incision is described using the stream power equation (Howard, 1980). The hillslope processes are simulated based on a linear sediment transport law, which sets the transport flux equal to a linear function of topographic slope: the simple diffusion law. The isostatic response to changes in water and sediment load is calculated using a two-way coupling between BADLANDS and *gFlex* (Wickert, 2016), which computes the flexural deflection of the Earth's surface by using an elastic plate flexure

125 solution. For a more detailed description of BADLANDS' constitutive laws see Salles and Hardiman, (2016) and Salles et al., (2018).

Our experimental design consists of a series of simulations where the initial configuration of the modeling domain resembles the topography of a natural source-to-sink system with 3400 m elevation in the headwaters, a length of 4500 km, a downstream-decreasing fluvial channel slope, and successive inflections in gradient associated with transitions from the coastal-plain to continental shelf and from the shelf to slope (Fig. 4a, S1, S2). To ensure that our simulated drainage basin produces a point-source for sediment input to the marine domain we imposed a longitudinal topographic low in the middle of the model. The resultant drainage basin, river channels, deltas, shallow-marine shelves and shelf margins are then self-generated as a result of landscape dynamics that are in turn controlled by hillslope and channel processes, sediment diffusion, uniform precipitation, sea-level changes and flexural isostasy. The three-dimensional spatial mesh size and temporal resolution were chosen to adequately reproduce the geomorphology and architectural evolution of deltaic systems at the first order (Fig. 4c), and to ensure that the frequency of sea-level fluctuations is adequately captured. Details about boundary conditions and input parameters used in modeling simulations can be found in Table 1 and the data repository.

Our simulations produce catchment areas, river lengths, and volumes of deposited sediment that are consistent with the ranges observed in continental-scale source-to-sink systems such as the Mississippi and Amazon rivers (Fig.4). We do not aim to reproduce the geological history of a particular continental-scale source-to-sink system, our goal is to better understand first-order relationships between sea-level changes, flexural isostasy, and erosion and deposition. The general similarity between our simulated river length and catchment area, and large-scale natural source-to-sink systems (Fig. 4b), supports choices made for our initial settings and allows us to draw general comparisons between simulated results and natural systems.

After the initial drainage basin and river system is formed, we perform a series of simulations that first hold sea level constant, then impose synthetic and climate-forced sea-level curves. Synthetic curves were constructed to reflect frequencies of 500 kyr and 5 Myr, whereas climate-forced sea-level curves were selected from intervals in geologic time with contrasting climatic regimes and therefore contrasting sea-level amplitudes and directions: we extracted data from Miller et al. (2020) that correspond to the ice-free Paleocene, ca. 66-56 Ma (hereafter greenhouse) and the ice-dominated Oligocene ca. 33.9-23.9 Ma (icehouse) periods (Fig. 3 b, c). These simulations are then compared to a suite of non-flexurally-compensated models. The sea-level curves we use are resampled to time steps of 50 kyr with outputs generated every 100 kyrs. We let each simulation initialize and run for 2 Myr without any sea-level fluctuations so that the delta can reach dynamic equilibrium without any disturbances in base level, then impose both the synthetic and climate-forced sea-level changes.

For flexurally-compensated models, we use an effective elastic thickness (T_e) of 50 km. This value is within the range observed in passive margins (Tesauro et al., 2012) and similar values have been used in previous flexural studies of continental-scale deltaic depocenters (e.g., Driscoll and Karner 1994; Watts et al., 2009). Moreover, we test the sensitivity to T_e by running a series of simulations where T_e varies from 10 to 100 km: results show similar patterns of flexural response when using T_e values <60 km, whereas larger values result in a smaller flexural amplitude and larger flexural wavelength (Fig. S3), which is

consistent with observations made for rigid lithosphere in cratonic regions (Tesauro et al., 2012). We use a spatially uniform T_e value in all simulations and do not account for possible spatial variations that could generate small spatial differences in flexural deflections. However, we consider such differences to be negligible when compared to the flexural response caused by the large sediment loads typical of passive margins. To ensure the computed flexural response is in-phase with our imposed sea-level cycles, we use a temporal resolution of 100 kyr: here too, we have conducted sensitivity tests with higher temporal resolution (up to 10 kyr) as well, and the emergent behaviors are similar to those presented here.

Our models do not include the effect of waves, tides, and shelf currents, although BADLANDS is capable of simulating wave-induced longshore drift (see Salles et al., 2018, which implements the equations from Longuet-Higgins 1970). We recognize the importance of waves, tides, and shelf currents in sediment transport but those processes move sediment volumes generally in the vicinity of deltaic depocenters and therefore would not play a crucial role in sediment load redistribution. Our simulations hold precipitation constant over time, and do not include tectonic or dynamic uplift in upstream regions, or lithological changes in subsurface sedimentary layers. Such parameters clearly play a role in the sediment volumes and rates delivered to the marine environment, and therefore the accumulated sediment load, but are not considered here to avoid complicating the analysis of the effect of high-frequency, high-resolution isostatic adjustments to changes in crustal loading due to both the sediment and water load, the primary effect that we aim to unravel in this paper. Our simulations also do not account for sediment compaction or sediments of different grain sizes.

4 Results and discussion

4.1 Model description

All of our simulations develop a drainage basin where rivers merge on the coastal plain and form a delta, and act as a point-source for sediment input to the marine domain. The simulated sediment flux is controlled by river incision and hillslope diffusion, whereas river incision is governed by precipitation, drainage area, the topographic gradient, and erodibility. Hillslope diffusion is dependent on diffusivity and the topographic gradient. Once the sediment load is deposited in the marine domain, a continental shelf emerges and shelf-margin clinothems (Fig. 4c) are generated.

Our results feature the response of the fluvial-deltaic system to flexural isostasy driven by climate-forced sea-level change, and illustrate significant impacts on the morphology, architecture and stratigraphic evolution of continental scale deltaic depocenters in deep time. Below, we highlight three distinct results: (a) the effects of flexural isostasy on the morphology and

stratigraphy of large deltas, (b) the flexural isostatic response to sea-level change, and its effect on delta evolution, and (c) the effects of hydro-isostasy on delta evolution.

4.2 Effects of flexural isostasy on the evolution of deltaic depocenters

The comparison between flexurally-compensated simulations and their non-flexurally-compensated counterparts allows us to isolate the effects of flexural isostasy on delta evolution. In non-flexurally-compensated simulations, elevation is controlled by erosion whereas bathymetry is controlled by deposition and base-level changes caused by sea-level fluctuations. By contrast, in flexurally-compensated simulations vertical changes in erosion and deposition are amplified by sediment unloading and loading, which causes uplift and subsidence, respectively (Fig. 5d). In addition, the flexurally-compensated simulations display peripheral bulges landward and alongshore of the deltaic depocenters, which are the result of the uplift and subsidence generated by flexural isostasy (Figs. 4a, c; S5; S6). As expected, the spatial variation in flexural response is a consequence of the spatial and temporal variations of sediment and water loads, and the bulges and curvatures noted above are absent in simulations without flexural compensation (Figs 4c, S5, S6). Hence, our models capture features that have been used in natural systems to provide evidence of flexural isostasy.

In all simulations, mean river-mouth transit distances and lateral river-mouth migration distances are significantly greater in non-flexurally-compensated simulations when compared to their flexurally-compensated counterparts (Figs. 5, 6). We attribute these patterns to reduced accommodation when flexural compensation is absent, which limits sediment accumulation close to the river mouth, forces the delta to prograde farther into the coastal ocean, and forces the river channel to migrate or avulse laterally, creating laterally extensive delta plains (Fig. 5a). Conversely, in simulations with flexural compensation, accommodation increases near the delta front as the load accumulates, which reduces cross-shelf transit distances and lateral migration of the river channel (Fig. 5c). To the extent that mean maximum rates of sediment accumulation at the river mouth are an indicator of accommodation that has been generated, they are significantly smaller in non-flexurally-compensated simulations when compared to their flexurally-compensated counterparts (Table S1).

4.3 Flexural isostatic response to sea-level change and its effect on delta evolution and stratigraphy

Our simulations show a close correspondence between cross-shelf transit distances of river mouths and sea-level position (Figs. 6, 7), confirming the role that sea level plays as an important driver for sediment dispersal on passive margins (e.g. Carvajal et al., 2009; Sømme et al., 2009). Hence, we first describe the flexural response to sediment and water load at the river mouth.

Simulations where we impose synthetic sea-level changes show that flexural response are bidirectional at a rate of change and direction that amplifies the climate-forced sea-level changes themselves. These results therefore demonstrate that significant

bidirectional flexural compensation can be important at high frequencies, in this case with sea-level cycles of 500 kyr and 5 Myr (Fig. 6 f-h, 7b). In each case there is a background monotonic increase in the accumulated flexural subsidence as the sediment load increases through time, but flexure is uniformly unidirectional if, and only if, sea level is held constant (Fig. 6d, 7b). The synchronicity between sea-level change and flexural response is confirmed by spectral analyses that show peaks at frequencies similar to the imposed synthetic sea-level fluctuations and flexural response at the river mouth (Fig. 7). Simulations that use climate-driven empirical sea-level curves also show that flexural response is bidirectional, cyclical and in-phase with the frequencies and amplitudes of sea-level fluctuations as well (Fig. 6 i-j), and thus reflects climate-driven changes in sediment loading and unloading, and climate-driven changes in sea level that produce change in thickness of the water column.

The synthetic stratigraphy produced by our simulations records the coupling of climate-driven sea-level change, flexural compensation, and generation of accommodation, which in turn drives river mouth lateral migration and cross-shelf transit distances (Fig. 6 p-y). First, simulations without flexural compensation show a larger proportion of hiatuses in the stratigraphic record when compared to flexurally-compensated simulations (Figs. 6 u-y), which we attribute to the absence of flexural subsidence Second, flexurally-compensated simulations with no sea-level change record a simple normal regression (Fig. 6u), whereas simulations with imposed synthetic and empirical sea-level curves display significant hiatuses during sea-level fall and basinward transit of the river mouth and shoreline (*sensu* the forced regression of Posamentier & Allen, 1999), but fewer hiatuses during sea-level rise when the river mouth and shoreline migrate landwards. In a natural system, significant hiatuses would be produced by the valley incision and cross-shelf extension of river systems that accompanies sea-level fall, whereas few hiatuses would be produced during the period of valley aggradation and filling that accompanies shortening of the river system as the shoreline steps landward during sea-level rise (Fig. u-y). Third, simulations with higher amplitude icehouse sea-level curves show a higher number of erosional hiatuses when compared to simulations with lower amplitude greenhouse sea-level curves. We attribute this observation to more frequent and extensive subaerial exposure of the shelf, with longer and more frequent cross-shelf river mouth transits in the icehouse case, and less frequent and extensive exposure of the shelf, with shorter and fewer cross-shelf transits of the river mouth in the greenhouse case.

4.4 Hydro-isostatic effects on delta evolution

In our simulations, net vertical changes are the result of the interplay between flexural isostasy (of the sediment and water loads) and erosion and deposition. By running a series of simulations where we impose different sea-level scenarios we were able to show that hydro-isostatic effects play an important role in the spatial and temporal evolution of large deltaic depocenters (Fig. 5). To further demonstrate the importance of hydro-isostasy we isolated the component of vertical changes that are solely associated with the water load by computing changes in the water column in the marine part of the modeling domain for each time step and then calculated hydro-isostatic responses in gFlex (Wickert 2016): we chose this approach because BADLANDS and gFlex are fully coupled to calculate the flexural isostatic compensation of both the sediment and water load, and we therefore were able to extract the water load component in the post-processing stage. As expected, our results show that the

spatial variation of hydro-isostatic adjustments is a function of the magnitude and frequency of sea-level change, and related
to the loading of the prograding sediment wedge (Figs. 8-9). In simulations where sea level is held constant, changes in relative
sea level and hydro-isostasy are associated with the progradation of the sediment wedge, which changes the distribution of
water depths, and in turn causes variations in gradient of the shelf, shelf margin and slope. By contrast, simulations with sea-
level change experience bidirectional hydro-isostatic adjustments that vary in amplitude from the shoreline to the shelf margin
(Fig. 8). We calculated the mean hydrostatic variation both along a cross-section (Fig. 9b) and at the river mouth (Fig. 9c) for
each time step, and found that simulations driven by a green-house sea-level curve had a distribution skewed towards positive
hydro-isostasy, which corresponds to uplift. These results are in agreement with the shelf-to-slope profile in Figure 10 that
show that simulations with a green-house sea-level curve have the highest elevations and bathymetries. As expected,
simulations where the ice-house sea-level curve was imposed display the largest range in hydro-isostatic response (Fig. 9) and
the down-dip shelf-to-slope profile has elevations and bathymetries that are 20% lower than simulations with a green-house
sea-level curve.

Our simulations also incorporate the effects of erosion and deposition in a dynamic manner, and in doing so we are able to
interogate the cumulative effects of feedbacks between hydro-isostasy and erosional and depositional processes. First, our
simulations with no sea-level change produces large cross-shelf transits of the river mouth, as well as extensive progradation
of the shelf margin and slope: without flexural compensation, the final elevation of the coastal plain is simply a result of the
initial topography, erosion and deposition, and base-level changes (Fig. 9, 10). Second, in natural settings, shelf-margin width
and water depth correlate to the length scale and gradient of river systems, and the magnitude of climate-driven sea-level
change (e.g., Blum and Womack, 2009; Blum et al., 2013): if sea level falls, the shelf is subaerially exposed, and river mouths
transit the shelf to the shelf margin, which is located in shallow water depths, whereas if sea level rises, the shelf is submerged
with the shelf margin residing in significant water depths. In our simulated ice-house scenario, with high-amplitude sea-level
changes, the shelf is inherently wide and the shelf gradient is steeper because of the long-distance back-and-forth cross-shelf
river mouth transits: the depth of valley incision during sea-level fall is amplified by large magnitude hydro-isostatic uplift,
whereas corresponding large magnitude hydro-isostatic subsidence in response to sea-level rise enhances accommodation and
result in increased valley filling as the river mouth migrates landward. By contrast, in the greenhouse scenario, and holding
river system scale constant, the shelf is inherently narrow due to low-amplitude sea-level changes, river mouth transit distances
are inherently short, and the shoreline remains proximal to the shelf margin (see Blum and Womack, 2009; Blum et al., 2013):
the slope of the shelf is shallower than in the ice-house case because of relatively continuous and widespread delta topset
aggradation.

Last, our simulations demonstrate the potential role of high-frequency climate-forced sea-level changes in generating high-
frequency flexural responses because they drive changes in the location and volume of fluvial-deltaic sediment accumulation,
which then drives changes in the spatial distribution of water depths. Our results show that accommodation is not first created

and then filled later, but instead coevolves in-sync with the actual responses of fluvio-deltaic systems to climate-driven sea-level change. In this way, climate-forced sea-level changes set up a feedback mechanism that results in self-sustaining destruction of accommodation and generation of hiatuses during sea-level fall, and self-sustaining creation of accommodation and sediment accumulation during sea-level rise.

4.5 Implications for natural systems

The results of our simulations demonstrate that climate-forced sea-level changes result in self-sustaining creation and destruction of accommodation into which sediment is deposited and therefore plays a major role in delta morphology and stratigraphic architecture. This self-sustaining process might help explain the discrepancies between clinothem thicknesses, relative sea-level and global mean sea level estimates (Sømme et al., 2023).

We argue that the results of the non-flexurally compensated simulations can be extrapolated to ancient deltaic systems that formed over a rigid lithosphere. We interpret that such systems will have inherently long progradation distances, areally extensive delta plains, and relativly low accommodation because of the rigid lithosphere they overlye. For example, the Triassic sequences of the North West Shelf of Australia (Martin et al., 2018; Morón et al., 2019) and the Boreal Ocean (Klausen et al., 2019) represent deltaic successions that prograded >500 km into the basin, creating widespread delta plains. Based on the fact that the reconstructed paleo-bathymetric relief of the Triassic Boreal Ocean is one order of magnitude smaller than other modern shelves, Klausen et al., (2019) conclude that a shallow marine basin is the most important prerequisite to create such a widespread delta plain. We equate those conditions to those observed in our non-flexurally compensated simulations. Another possible example of this phenomenon might be the Early Cretaceous McMurray Formation in the Alberta foreland, which represents a continental-scale river system (see Blum and Pecha, 2014; Wahbi et al., 2022) whose stratigraphic record is very thin, and lacks an obvious thick deltaic depocenter within the area of preserved McMurray strata.

Our simulations show patterns and rates of bidirectional vertical motions that are similar to the chronostratigraphic data analyzed by Frederick et al. (2019; see also Fillon, 2016) from the Mississippi deltaic depocenter (Fig. 11), however vertical motions in our models are generated by flexural isostasy alone. We therefore argue that the correspondence between subsidence and uplift patterns in the Gulf of Mexico and in our models can be used to support the idea that the majority of the vertical motions in the Gulf of Mexico at time scales of 10^6 years or more are generated by flexural isostatic responses to sediment and water loads.

Rates of subsidence from our study can also be compared with rates of motion generated by other processes that include fault motion, compaction and annual water loading. As noted above, in large deltaic depocenters such as the Mississippi and Niger deltas, the locations of growth-fault systems tend to migrate basinward as the shelf margin progrades (e.g., Galloway et al.,

2008; Pizzi et al., 2020), and they illustrate this inverse relationship between rates and the time over which rates are integrated. Total throw on these faults can be measured in kilometers, but motion is inherently episodic, and, when faults are active, they likely produce rates of vertical motion of 10s of mm/day for short periods of time. However, long periods of quiescence in between episodes of active motion ensure that time-averaged rates of fault slip are very low over time scales of 10^4 yrs or more (e.g., Shen et al., 2017).

Our study focuses on the impact of the interplay between climate-forced sea-level change, changes in sediment and water loads, and associated flexural adjustments on the evolution of continental scale deltaic depocenters in deep time, but the results of our simulations also help explain the spatial variarion of relative sea-level changes in the Holocene as well (e.g., Lambeck et al. 2014; Khan et al., 2015; Whitehouse 2018). Previous empirical studies that have calculated sea-level fluctuations have noted that sea-level estimates around deltas do not correspond with other adjacent sites (Lambeck et al., 2014). For example, many observations from large deltaic systems in Asia, and comparisons of such data with observations from adjacent sites, often indicate lower sea levels of the former, corresponding to differential subsidence rates of the order of 1 mm/yr for the past ~8ka. Interestingly, Lambeck et al. (2014) did not include data from the deltas of Chao Phraya of Thailand, Mekong and Red rivers of Vietnam, and Pearl and Yangtze rivers of China, for the purpose of estimating the equivalent sea level function. We suggest the mismatch between subsidence rates in large deltaic depocenters and adjacent non-deltaic sites can be attributed to the interplay between spatially non-uniform progradation and aggradation of the deltaic sediment wedge, and spatially non-uniform flexural isostatic response to changes in sediment and water load sediment load as forced by climate-driven sea-level change.

5 Conclusions

We use conceptual simulations to unravel the flexural isostatic response to the interplay between climate-forced sea-level change, sediment erosion and deposition in deep time on passive margin deltaic depocenters. Our results illustrate how cumulative high-frequency, bidirectional isostatic adjustments play an important role in driving along-strike and cross-shelf river-mouth migration and sediment accumulation. Our results also show that accommodation coevolves in-sync with flexural isostatic adjustments to climate-driven sea-level change, and the associated responses of large fluvial-deltaic systems. We find that only simulations with no imposed sea-level change produce a true monotonic increase in flexural subsidence and unidirectional deltaic progradation, regardless of time scale. We therefore view cyclical and bidirectional flexural responses to be inherent in fluvio-deltaic systems because they are coupled to the increasingly well-understood nature of how surface dynamics in fluvial-deltaic systems respond to climate-forced sea-level changes to produce the stratigraphic record.

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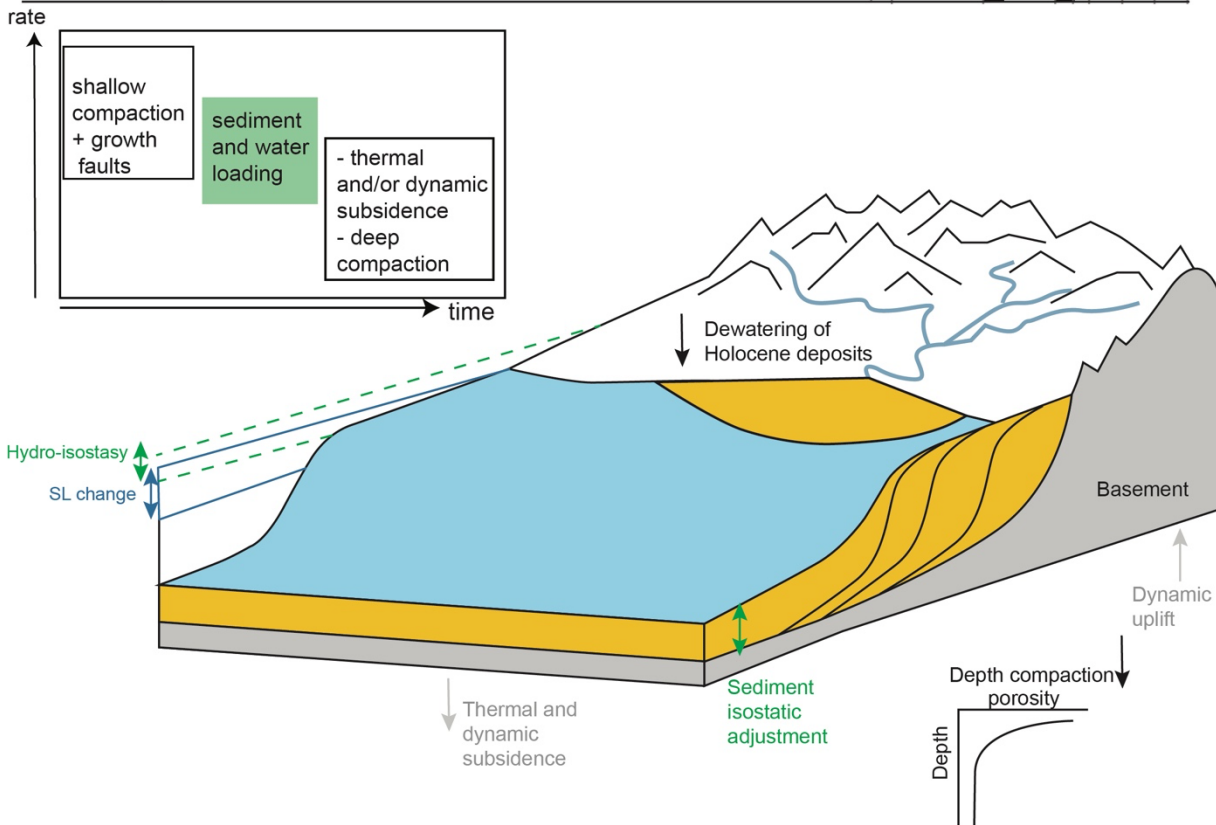
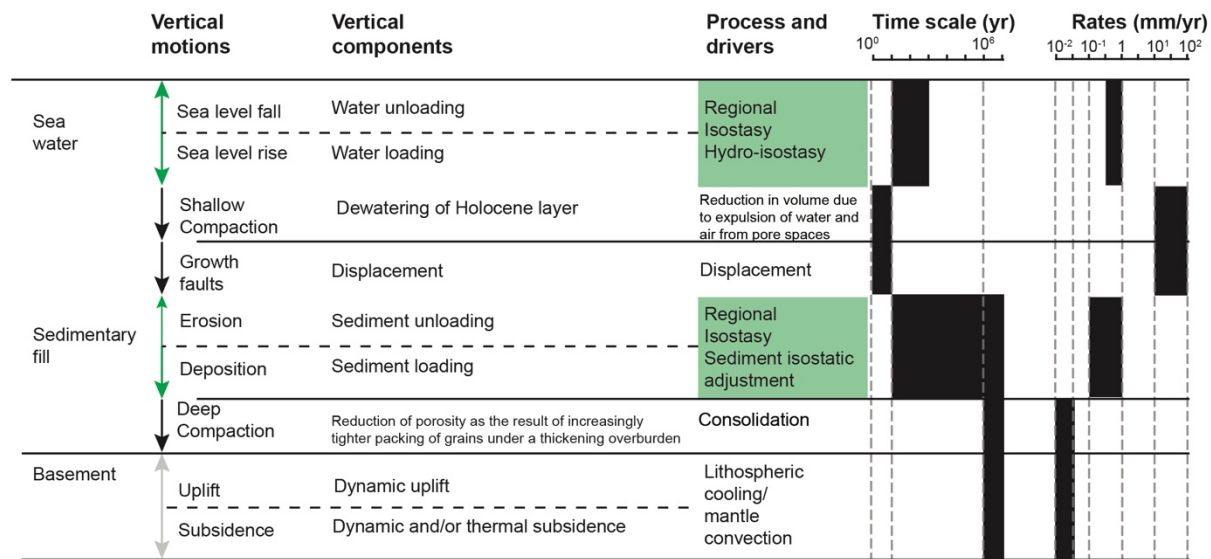
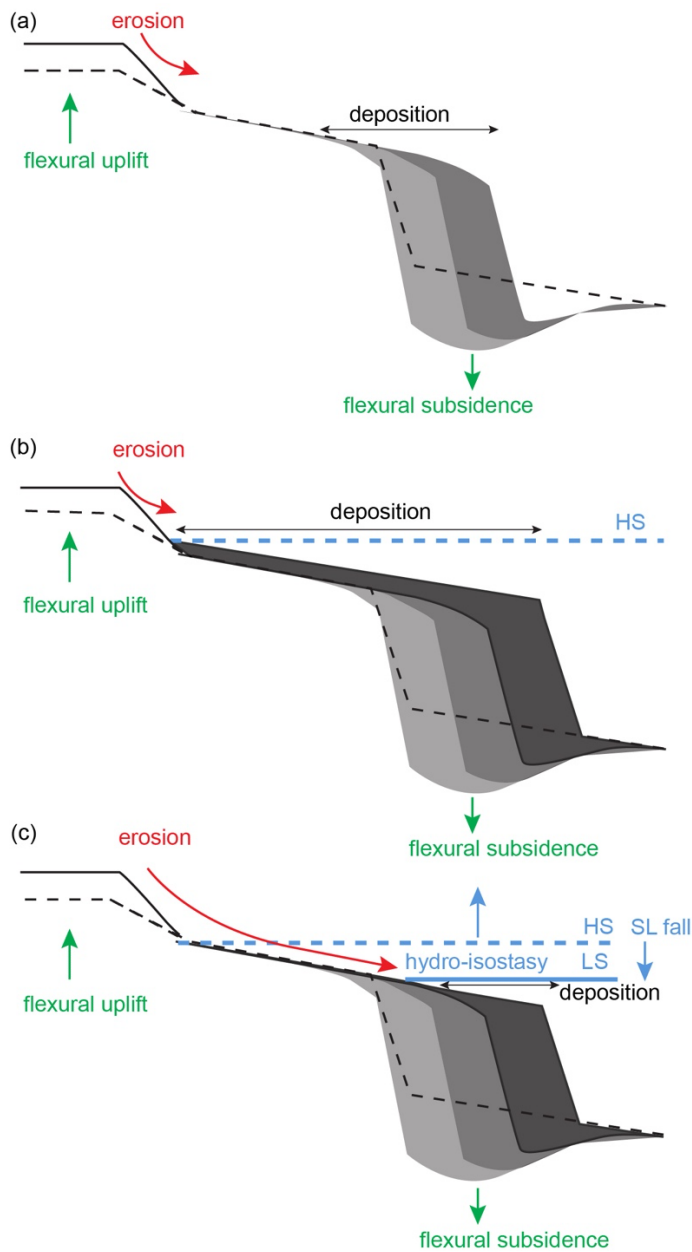


Figure 1. Conceptual diagram showing the components of vertical motions in passive margins with deltaic depocenters at different spatio-temporal scales. Rates of vertical motions are from Allen and Allen (2005); Jouet et al., (2008) and Frederick et al., (2019). Processes that can result in both uplift or subsidence, refered to as bidirectional, are shown in green. Sea-level change produces hydro-isostatic adjustments that affect both the landward portion of the continental margin and the ocean basin.

535 **Figure 2. Conceptual model illustrating the complex interaction between surface processes (erosion, red and deposition, black), sea level change and flexural isostasy. (a) Shows the uplift generated by the erosion of the sediment load and the subsidence created by the deposition of the prograding sediment load. (b-c) Shows how the position of the sediment load changes with the position of the sea level (SL) and how hydrostatic uplift takes place as a result of sea-level fall. These processes and interactions have been proposed to be key to explain the concept of continental levering (e.g. Lambeck and Nakada 1990; Clement et al., 2016; Whitehouse, 2018).**

540 **HS=High stand, LS= Low stand. The black dashed-line represents the elevation and or bathymetry of the initial surface. Modified from Watts (1989).**

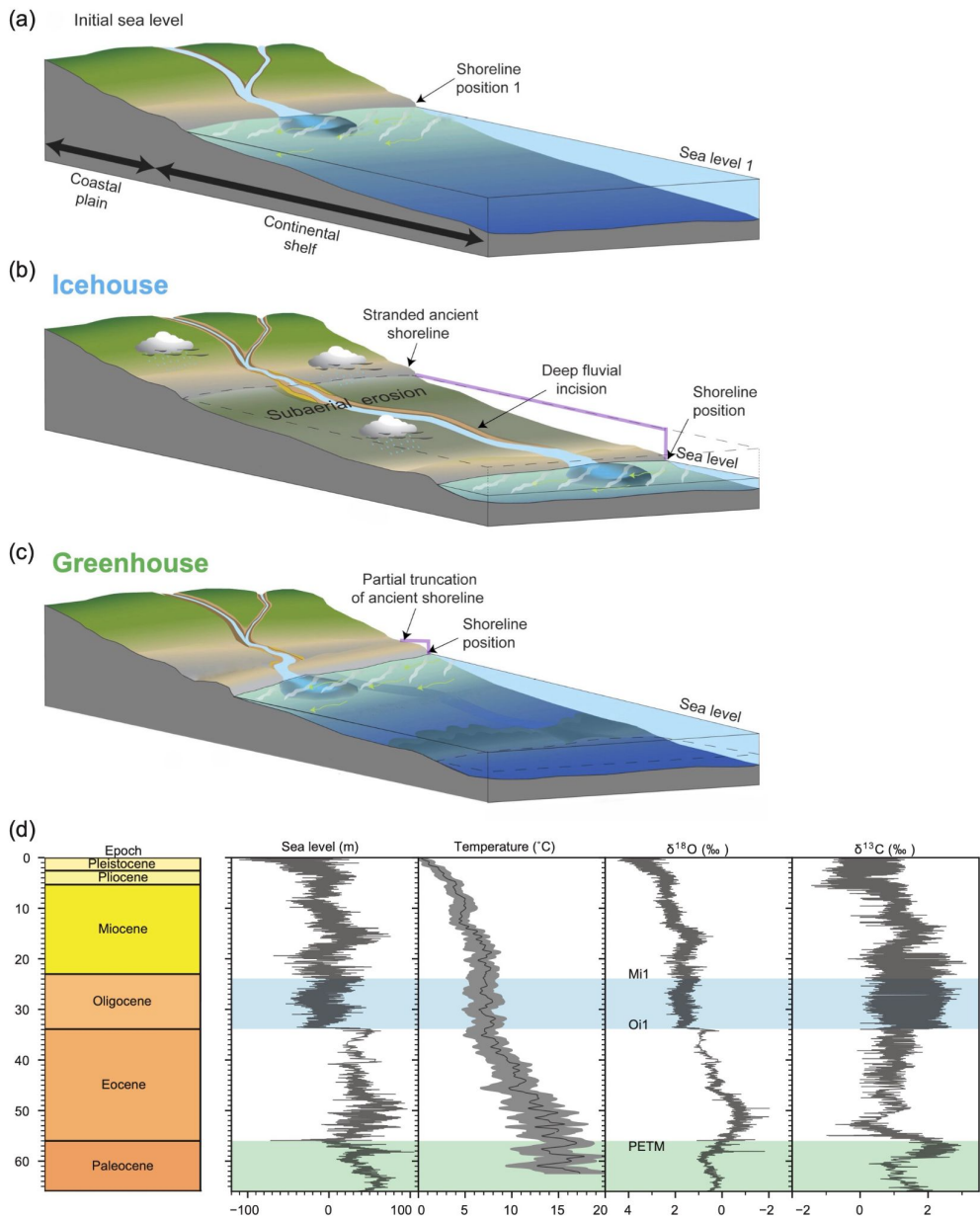



Figure 3. Conceptual model for the evolution of (a) deltaic depocenters in response to sea level changes during (b) icehouse and (c) greenhouse periods. The frequent and large amplitude variation of the sea-level (purple line) during icehouse periods results in the exposure of the continental shelf and deep fluvial incision and sediment loads being deposited deep into the basin. In contrast, during greenhouse periods the smaller amplitude of the sea-level variation (purple line) results in sediment being deposited closer to the continent. We test the flexural isostatic response of the aforementioned water and sediment partitioning. Figure modified from https://pubs.usgs.gov. (d) Evidence of the coupling between climate and global sea-level change that reflects global changes in ice volumes. The coupling is particularly strong in ice-free (ca. 66-56 Ma, greenhouse) and ice-dominated (ca. 33.9-23.9 Ma, icehouse) periods, which are the focus of this study. Data sources: sea level (Miller et al., 2020), temperature estimates based on Mg/Ca values (Cramer et al., 2011), benthic foraminiferal δ^{18}O (Miller et al., 2020) and carbon isotope record δ^{13}C (Zachos et al., 2001).

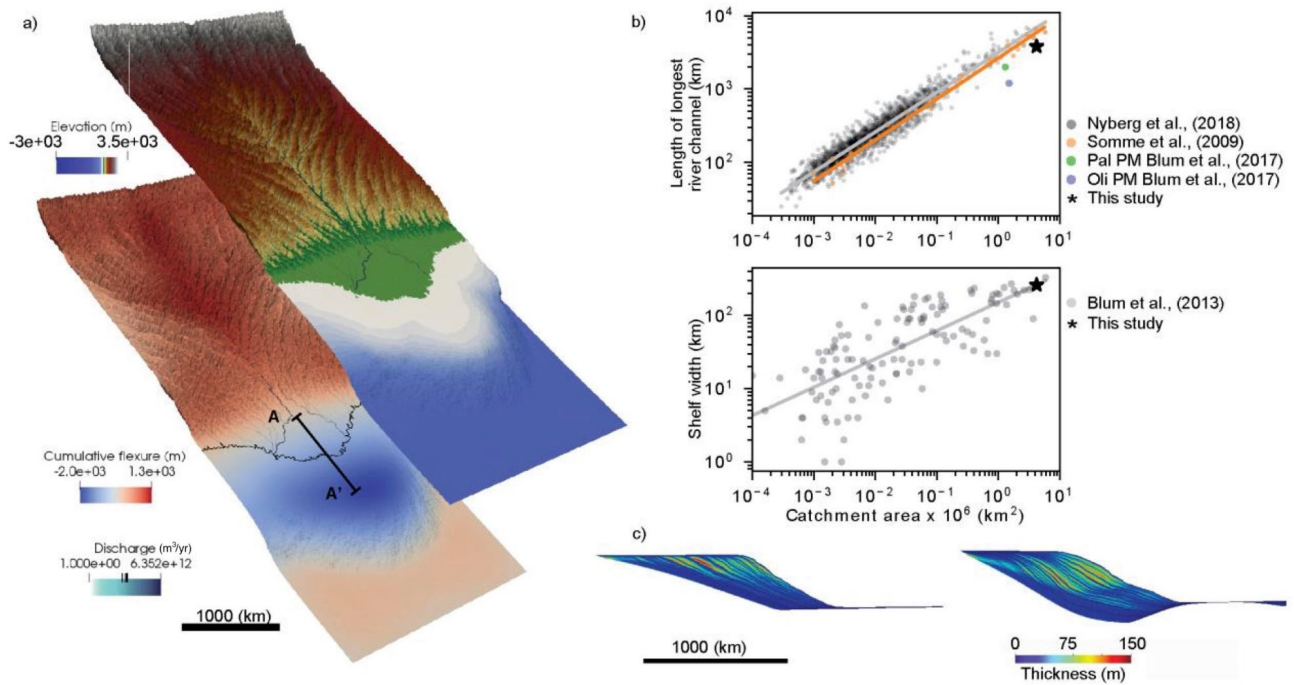



Figure 4. (a) Example of the outputs from numerical simulations that show elevation and bathymetry (top) and cumulative flexure (bottom). Discharge is shown in both maps to visualize the paths of the fluvial-deltaic system Model dimensions are 4500 km x 2000 km, with a vertical exaggeration of 100x. (b) Scatter plot of river length (top) and shelf width (bottom) versus catchment area from river systems. Data is from Somme et al. (2009), Nyberg et al. (2018), Blum et al. (2013, 2017) and simulations presented in this study. Pal= Paleocene, Oli=Oligocene, PM= Paleo-Mississippi. (c) Example of synthetic stratigraphy from a simulation without (left) and with flexural compensation (right). Vertical exaggeration is 150x. Cross-section A-A' shows where the Wheeler diagrams presented in Figure 5 were constructed.

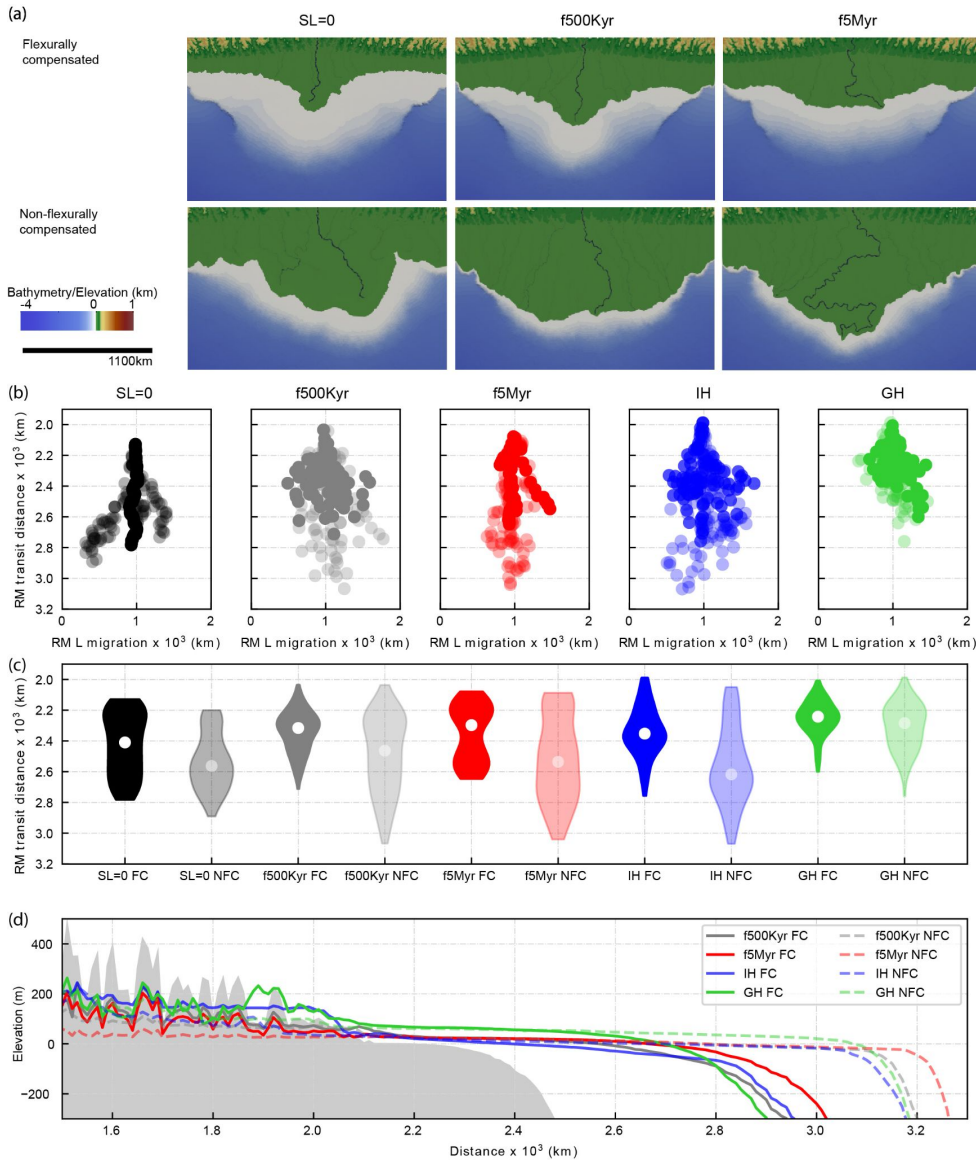



Figure 5. (a) Output of numerical simulations with imposed synthetic sea-level curves with different frequencies showing elevation, bathymetry and discharge of the river mouth at 8 Myr. (b) River mouth (RM) location for each time step for all simulations, which illustrates the river mouth transit distance and lateral (L) migration. (c) Violin plots (modified kernel density plots) show that in all simulations, mean river-mouth transit distances (white dots) are significantly greater in non-flexurally-compensated (NFC, lighter shades) simulations when compared to their flexurally-compensated (FC, darker shades) counterparts. (d) Comparison of the down-dip shelf-to-slope profile for all the simulations. These results show that flexurally compensated models have significantly smaller progradation distances in the river mouth and the shelf break, smaller areal extend and larger coastal elevations (due to flexural uplift) compared to their non-flexurally compensated counterparts. IH = icehouse, and GH = greenhouse.

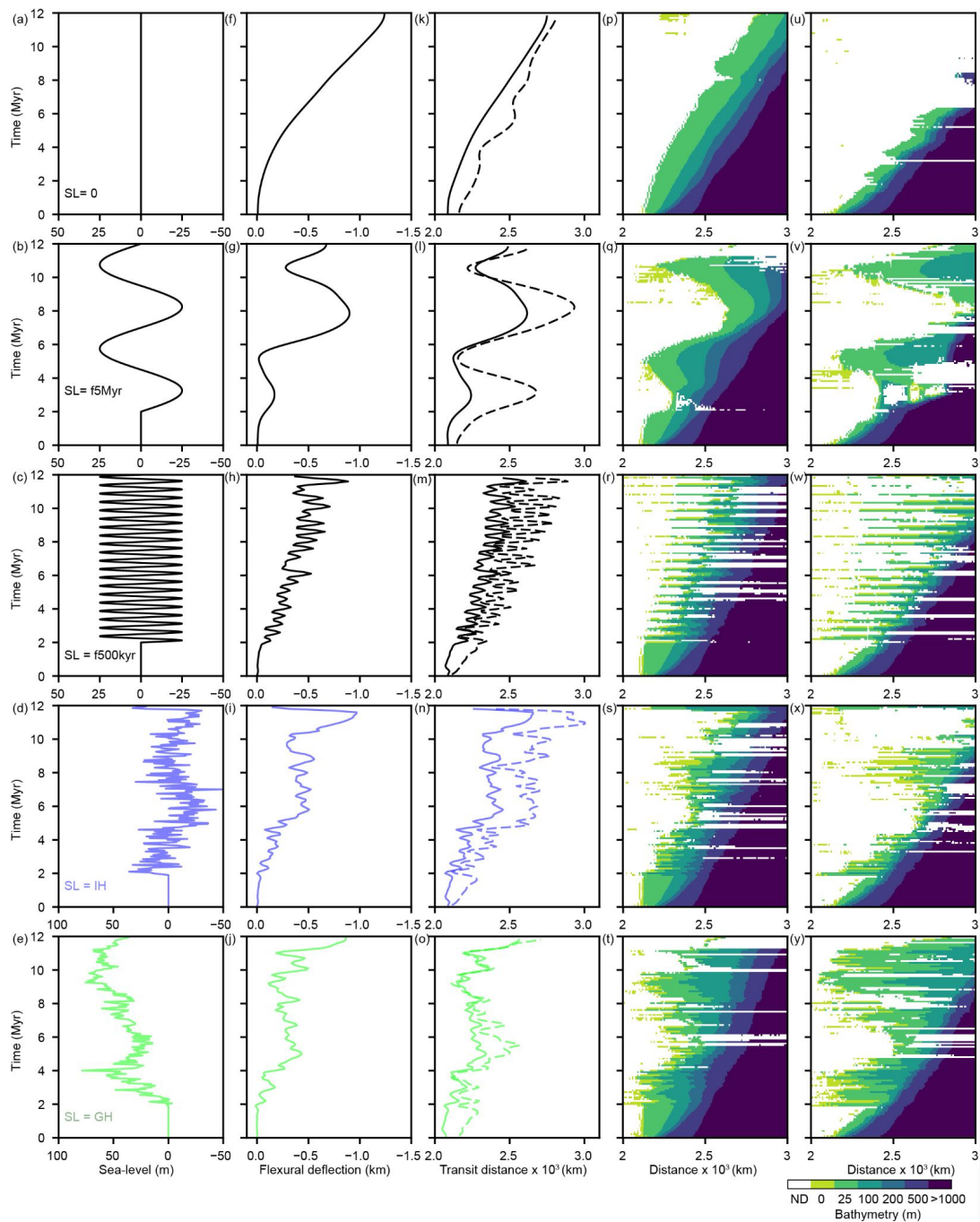



Figure 6. Outputs of numerical simulations for the different scenarios where we impose synthetic (a-c) and empirical (d-e) sea-level curves (SL). Outputs represent the temporal evolution of the flexural deflection (f-j) and travel distance of the river mouth (k-o). Wheeler diagrams show the changes in bathymetry through time for the flexurally compensated (p-t) and non-flexurally compensated (u-y) simulations. The location of the cross-section used to construct the Wheeler diagram is shown in Figure 4. Wheeler diagrams are constructed using the post-processing module of BADLANDS (Salles et al., 2018). ND= No deposition. Model abreviations are listed in Table 1.

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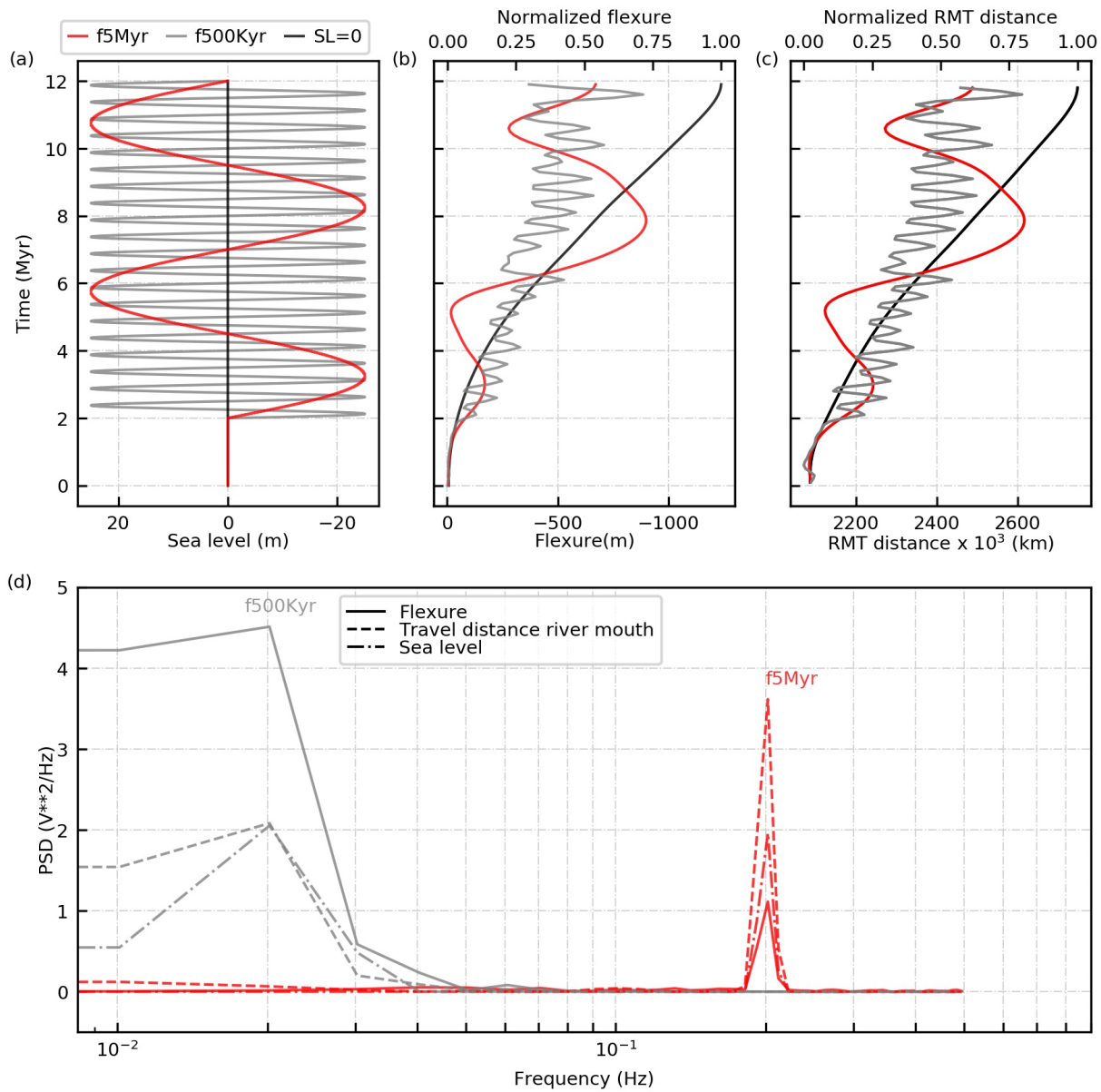
Figure 7. (a) Synthetic sea-level curves with a frequency of 5 Myr (red), 500 kyr (grey) and no sea-level change (SL=0, black). Comparison of **(b)** flexural deflection and **(c)** transit distance extracted at the river mouth (RMT). **(d)** Power-spectral density (PSD) for simulations with a frequency of 5 Myr (red) and 500 kyr (grey). The correspondence in peak frequencies between sea level, flexural deflection and river mouth migration provides further evidence of the synchronicity between flexural deflection and sea-level changes.

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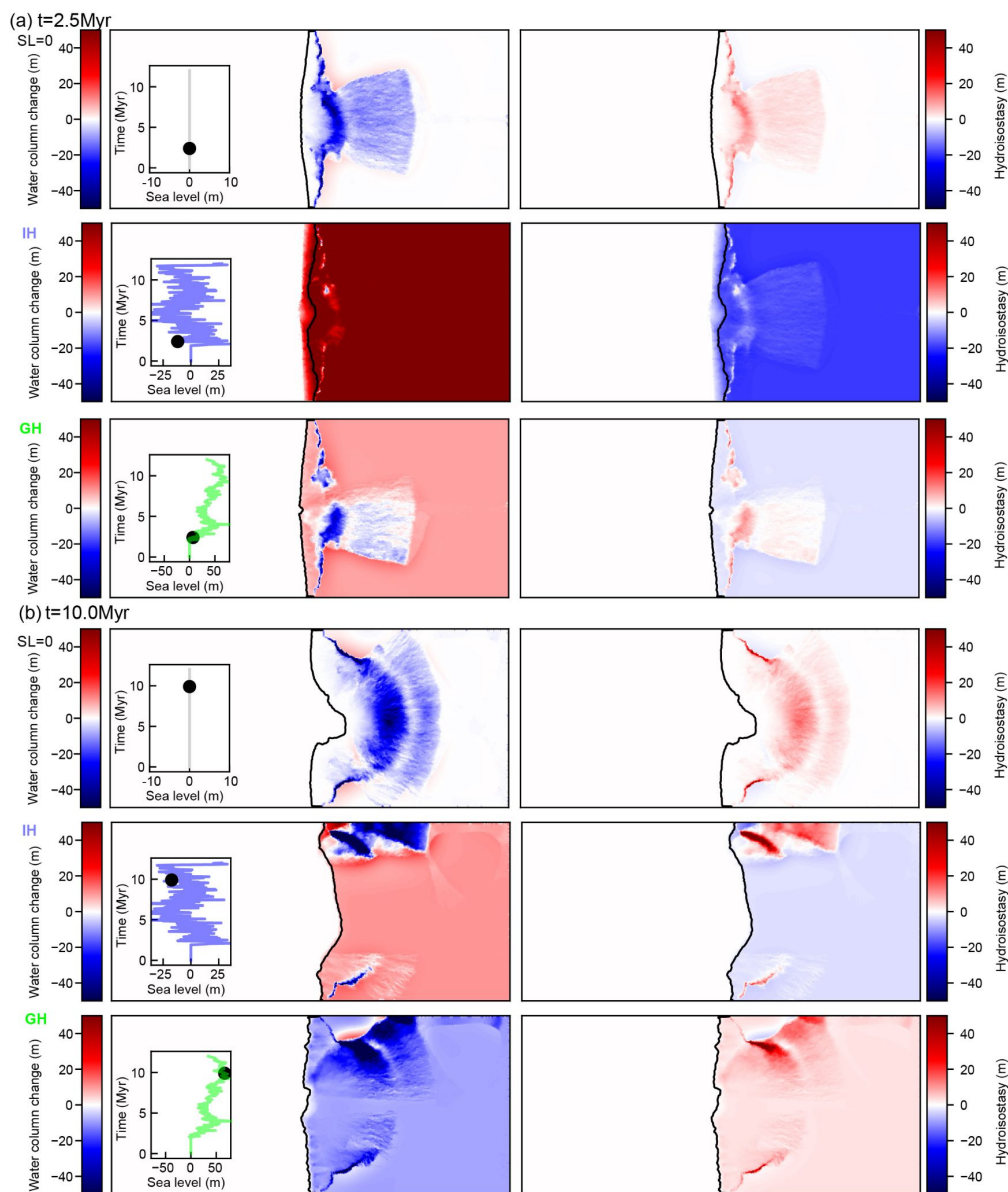


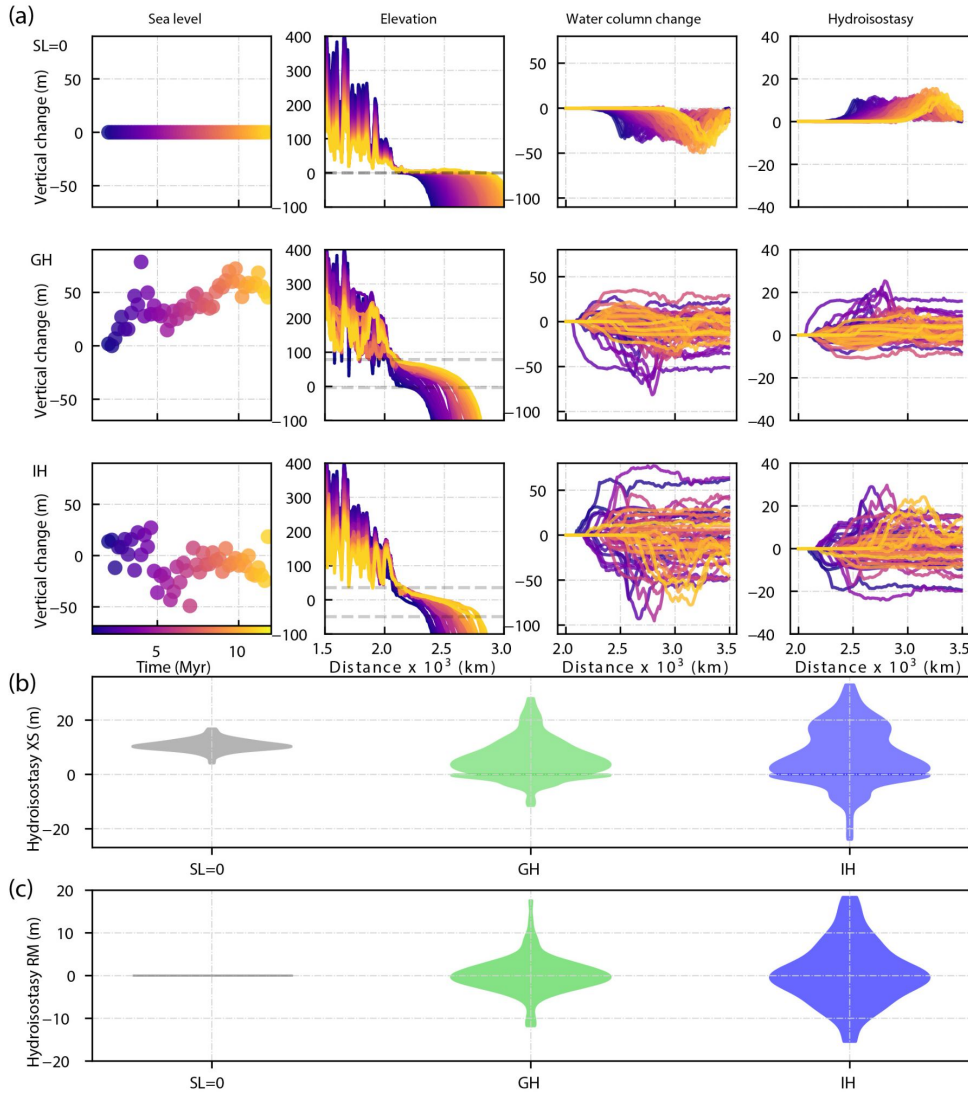
Figure 8. Map views showing the temporal evolution of the change in water column (left) and associated hydro-isostasy (right) at (a) 2.5 Myr and at (b) 10Myr in the numerical simulations with different sea level scenarios: SL0=0 constant, IH=icehouse and GH=greenhouse. These result show the vertical changes that are solely associated with the water load. Insets on the left panels show the imposed sea-level curve and the round symbol the point in time when the simulation output was taken. The variations in the direction of hydro-isostasy through time for GH and IH, which contrasts with the results from the simulations with no sea-level change. Note length of the modeling domain is 4500 km, therefore because of the scale, in some cases it might look like the hydro-isostasy is not affecting the areas proximal to the shoreline.

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Figure 9. (a) Temporal evolution of sea-level, elevation, water column change and hydro-isostasy along a down-dip section in the middle of the modeling domain for the simulations with different sea level scenarios: SL0=0 constant (first row), GH=greenhouse (second row), and IH=icehouse (third row). The spatial variation of hydro-isostatic adjustments is a function of the magnitude and frequency of sea-level change, and related to the loading of the prograding sediment wedge. The positive values in the hydro-isostasy fluctuate because of bathymetric changes caused by the progradation of the sediment wedge and flexural subsidence. Dashed horizontal lines on the second column show the minimum and maximum sea level for each of the scenarios. Violin plots (modified kernel density plots) show the range of)hydro-isostasic adjustments for the three sea level scenarios along a (b) cross-section (XS) and at (c) the river mouth (RM). Note how the largest range in the hydro-isostatic response occurs in the simulations where the ice-house sea level was imposed.
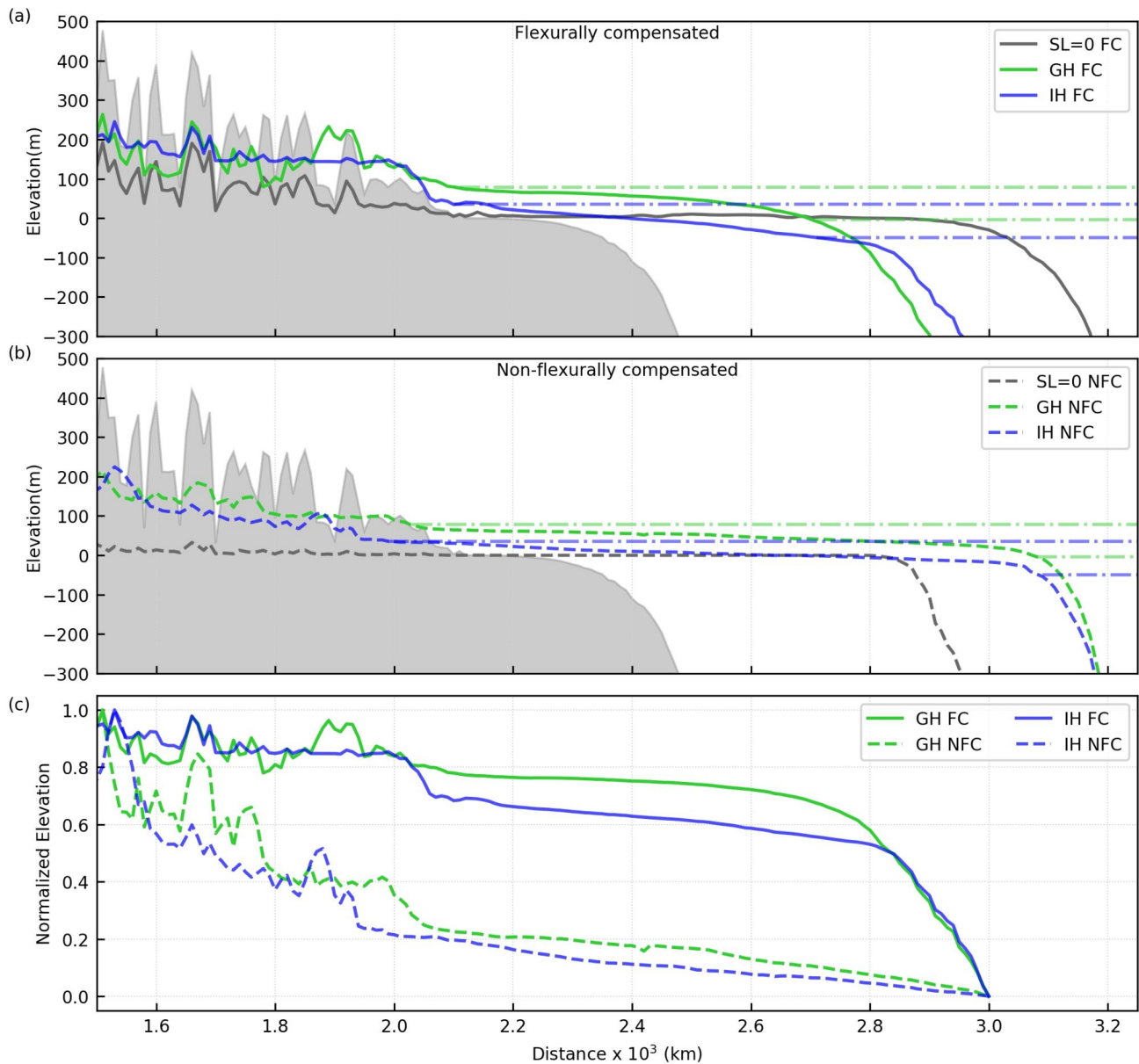
Figure 10. Comparison of the down-dip shelf-to-slope profile for scenarios with no sea level change (dark grey) green house (green) and ice house (blue) for (a) flexurally compensated and (b) non-flexurally compensated models. The net vertical change presented in this figure is the result of the interplay between flexural isostasy and erosion and deposition. Where the flexural isostatic compensation is derived from both the sediment and water loads, the latter referred to as hydro-isostasy. Note how the shelf rollover depth adjusts to changes in sea-level amplitude and frequency. In the models without flexural compensation the final elevation of the coastal plain is the result of the initial topography, in that case only erosion and base-level changes control the vertical adjustments, as illustrated by the lack of relief in the case with no sea level change. The grey shaded background represents the longitunidal profile before the sea-level condition is imposed (t=2 Myr). Horizontal dashed lines show the minimum and maximum sea level for each of the scenarios, which correspond with the upper and lower boundary of the shelf's slope.
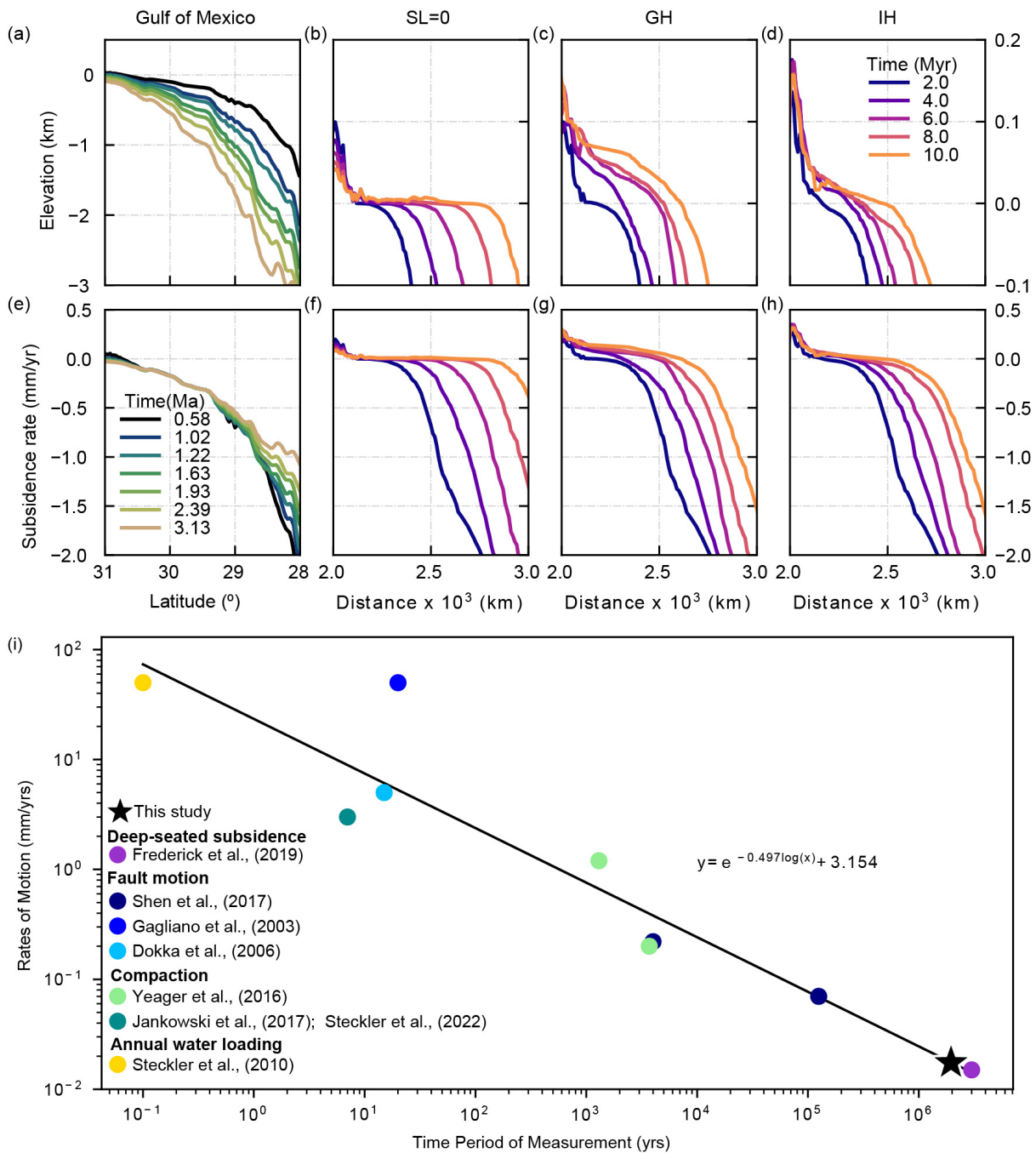
Figure 11. Elevation-bathymetry (top) and associated subsidence rates (botom) from the Gulf of Mexico (a-e) and from simulations with no sea level change (SL=0, b, f) green house (GH c, g) and ice house (IH d,h). (i) Vertical rates of motion measured over different time scales, illustrating a "Sadler" type rate decrease as a negative log-log relationship with time scales of measurement.

Table 1 Summary of the different input parameters used in the numerical simulations presented in this study. All the boundary conditions and parameters can be found in https://github.com/saraemp/egusphere-2023-53. SL=sea level, f=frequency, A=amplitude, FC=Flexurally compensated, NFC=Non- Flexurally compensated, T_e= Elastic thickness

Simulations with synthethic sea-level curves			
Simulation ID	**f (yr)**	**A (m)**	**T_e (km)**
SL0 FC	0	0	50
f500kry FC	500k	25	50
f5Myr FC	5M	25	50
SL0 NFC	0	0	-
f500kry NFC	500k	25	-
f5Myr NFC	5M	25	-
Simulations with empirical sea-level curves			
Simulation ID	**SL age interval (Ma)**		**T_e (km)**
IH FC	33.9 - 23.9		50
GH FC	66.0 - 56.0		50
IH NFC	33.9 - 23.9		-
GH NFC	66.0 - 56.0		-
Main input parameters and boundary conditions for all simulations			
Rain (m/yr)	1		
Erodibility coefficient	4.00E-07		
Surface diffusion coefficient (m^2/yr)	3.00E-02		
Marine diffusion coefficient (m^2/yr)	5.00E-02		
Temporal resolution (yr)	1.00E+05		
Mantle density (km/m^3)	3330		
Sediment density (km/m^3)	2170		
Young's Modulus (Pa)	1.00E+11		
Grid resolution (m)	1.00E+04		

Code availability

650   The model inputs and outputs as well the post-processing codes used in this study are available online at https://github.com/saraemp/egusphere-2023-53

Author contribution

SP Designed the simulations, carried them out and prepared the manuscript. MB contributed to the conceptual design of the simulations and the manuscript writing. TS significantly contributed to the performance of the simulations and code

655   development. TS, RF, XD, BM and CM helped with the post-processing codes. All authors contributed to the revision and editing of the manuscript.