



Development of Inter-Grid Cell Lateral Unsaturated and Saturated Flow Model in the E3SM Land Model (v2.0)

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Abstract. The lateral transport of water in the subsurface is important in modulating the terrestrial water-energy distribution. Although few land surface models have recently included lateral saturated flow within and across grid cells, it is not a default configuration in the Climate Model Intercomparison Project version 6 experiments. In this work, we developed the lateral subsurface flow model with both unsaturated and saturated zones in the Energy Exascale Earth System Model (E3SM) Land Model version 2 (ELMv2.0). The new model, called ELM_{lat} , was benchmarked against PFLOTRAN, a 3D subsurface flow and transport model, for three idealized hillslopes that included a convergent hillslope, divergent hillslope, and titled V-shape hillslope with variably saturated initial conditions. ELM_{lat} showed comparable performance with PFLOTRAN in terms of capturing the dynamics of soil moisture and groundwater table for the three benchmark hillslope problems. Specifically, the mean absolute errors (MAE) of the soil moisture in the top five layers between ELM_{lat} and PFLOTRAN were within $1\% \pm 4\%$ and the MAE of water table depth were within ± 0.3 m. Next ELM_{lat} was applied to the Little Washita experimental watershed to assess its prediction of groundwater table, soil moisture, and soil temperature. The spatial pattern of simulated groundwater table depth agreed well with the global groundwater table benchmark dataset generated from a global model calibrated with long term observations. The effects of lateral groundwater flow on the energy flux partitioning were more prominent in low land areas with shallower groundwater tables, which the difference of simulated annual surface soil temperature could reach $0.4 - 0.5$ °C at low land areas between ELMv2.0 and ELM_{lat} . Incorporating lateral subsurface flow in ELM improves the representation of the subsurface hydrology which will provide a good basis for future large-scale applications.

1 Introduction

Groundwater, which stores $\sim 30\%$ of the world's freshwater, plays an important role in the global hydrologic cycle and is a critical water resource for the environment and human systems. As the bottom boundary, groundwater moderates soil moisture that is extracted by vegetation roots while is recharged by water percolation and acts as an important buffer in the water cycle (Maxwell et al., 2007; Fan et al., 2007; Miguez-Macho et al., 2007; Fan, 2015). Groundwater also interacts with rivers by supporting the base flow or receiving the percolated water from rivers and feeds the groundwater dependent wetlands (De Graaf et al., 2014; de Graaf et al., 2017; Condon and Maxwell, 2019; Qiu et al., 2019). Groundwater is a major freshwater resource for drinking and irrigation, and has been used for various industrial purposes (Döll et al., 2012; Wada et al., 2011). With the surging growth of population and water demand, overexploitation of groundwater resources have been witnessed world



wide (Wada et al., 2010, 2012; Gleeson et al., 2012; Pokhrel et al., 2015) , which unsustainably impacted the long term water supplies and impaired the health of many ecosystems (Wada et al., 2012; Gleeson et al., 2012).

Improving the representations of groundwater flow in Land Surface Models (LSMs), which serve as the land component of Earth System Models (ESMs) could promote the address of important scientific questions (Clark et al., 2015). Groundwater movement in the critical zone, usually defined as the shallow groundwater (between 1-5 m), is important in modulating the terrestrial water-energy distribution and land-atmosphere interactions (Kollet and Maxwell, 2008; Condon and Maxwell, 2019; Fan, 2015). Long term groundwater movement and storage variations are found highly influential in predicting the long-term water and energy partitions across different scales (Wang, 2012; Fang et al., 2016; Zhang et al., 2022). All these factors determine the important role that groundwater is playing in regulating the eco-hydrological processes, especially in the groundwater supplied ecosystems (Chui et al., 2011; Miguez-Macho and Fan, 2012; Subin et al., 2014; Vrettas and Fung, 2017; Fang et al., 2022). Moreover, the role of groundwater in regulating the water and energy balances at the land/atmosphere interface and how its feedback to climate change would affect ecosystem functioning at various spacial and temporal scales remain partly understood (Kløve et al., 2014; Clark et al., 2015). Lateral groundwater flow represents a critical process in representing groundwater dynamics. The magnitude of lateral groundwater flow is suggested to be scaling with grid resolution (Krakauer et al., 2014). With grid resolution less than 0.1° (10 km), lateral flow is comparable to the recharge rate and thus is non-negligible (Krakauer et al., 2014). Therefore, incorporating detailed representations of the lateral groundwater flow is important in LSMs regarding the surging interests in Hyper-resolution modeling at regional or global scales (Wood et al., 2011; Bierkens et al., 2015; Fan et al., 2019).

Despite the importance of groundwater systems in the terrestrial processes, incorporation of lateral groundwater flow models in LSMs is just nascent. Nearly all LSMs that participated in the Climate Model Intercomparison Project version 6 (Eyring et al., 2016) ignored lateral groundwater flow. Most of these LSMs simulate vertical only soil water movement without lateral connections and parameterize the saturated groundwater dynamics with a lumped unconfined aquifer, e.g. CLM4.5 (Oleson et al., 2013), HiGW-MAT (Pokhrel et al., 2015). A few recent works have incorporated lateral groundwater flow within/across grids in LSMs. For example, Swenson et al. (2019) incorporated intra-grid saturated lateral groundwater flow into Community Land Model (CLM) v5.0 at the hillslope scale. Recently, a number of inter-grid cell lateral groundwater flow models have been developed, which can be categorized into two major groups. The first group solves quasi three dimensional (3-D) groundwater flow that accounts for vertical soil water movement in the unsaturated zone and only lateral groundwater flow in the saturated zone. For example, Zeng et al. (2018) coupled a lateral groundwater flow model in the saturated zone with CLMv4.5 (Oleson et al., 2013); Felfelani et al. (2021) extended the work of Swenson et al. (2019) to include inter-grid cell saturated lateral groundwater flow in CLM5.0 and applied the model at continental scale; Chaney et al. (2016, 2021) developed the HydroBlocks model by coupling the dynamic TOPMODEL, which used a kinematic wave approach and recently updated to Darcy flux, to represent the saturated lateral flow, with Noah-MP; H3D model (Troch et al., 2003; Paniconi et al., 2003; Hazenberg et al., 2015) couples a vertical 1-D soil column model with a pseudo-2D saturated groundwater model and was validated with a 3-D Richards equation model (Richards, 1931); similarly, PAWS (Shen and Phanikumar, 2010; Shen et al., 2013) solves the saturation based (θ -based) 1-D Richards equation in the unsaturated zone and 2-D diffusive groundwater



equation in the saturated zone, and was coupled with CLMv4.0 for solving land surface processes. The second group solves fully 3-D groundwater flow in both the saturated and unsaturated zones. For example, ParFlow solves the variably saturated 3-D Richards equation for both unsaturated and saturated groundwater and has a comprehensive representation of the surface and subsurface processes (Kollet and Maxwell, 2006, 2008; Maxwell, 2013). CLM-PFLOTRAN couples PFLOTRAN (Hammond and Lichtner, 2010) with CLM4.5 (?), which simulates the 3-D subsurface flow by solving the 3-D variably saturated Richards equation and represents the land surface processes with CLM4.5 (Bisht et al., 2017); Similarly, Miura and Yoshimura (2020) developed the 3-D Variably saturated groundwater model considering the storativity of groundwater, and validated the model for different idealized situations. However, the second group of models is not applied to global-scales but are limited to watershed-, regional-, and continental-scales studies due to high computational costs (Archfield et al., 2015).

The surging interests of applying hyper-resolution LSMs at continental or global scales motivated the development of more comprehensive and efficient representations of subsurface hydrology in LSMs (Archfield et al., 2015). Stemming from the Community Earth System Model (CESM) version 1_3_beta10 (Oleson et al., 2013), the Energy, Exascale, Earth System Model (E3SM) is a state-of-the-art ESM sponsored by the U.S. Department of Energy (Leung et al., 2020). The latest E3SM Land Model version 2.0 (ELMv2.0) solves the 1-D Richard equation in the unsaturated zone based on (Zeng and Decker, 2009) and parameterize the saturated groundwater process with a lumped unconfined aquifer. The goal of this study is to develop and validate a computationally efficient inter-grid cell lateral unsaturated and saturated groundwater flow model within ELMv2.0. Instead of solving the fully 3-D Richards equation, the model solves a modified 1-D θ -based Richards equation including unsaturated and saturated zones, and considers the lateral groundwater flux as a source term. The developed model was first benchmarked against PFLOTRAN (Hammond and Lichtner, 2010) for three idealized hillslope planforms that included a convergent hillslope, divergent hillslope, and titled V-shape hillslope with variable saturated initial conditions. The model was next applied to the Little Washita Watershed (LWW) in the USA to assess its performance with field observations of soil moisture and soil temperature. The impacts of lateral flow on the surface energy fluxes were also evaluated.

2 Methods

2.1 Numerical formulation

2.1.1 Lateral flow in unsaturated zone

In ELMv2.0, the water movement in the unsaturated zone is governed by the 1D θ -based Richards equation given as

$$\frac{\partial \theta}{\partial t} = -\frac{\partial q}{\partial z} - Q \quad (1)$$

where θ [$\text{mm}^3 \text{mm}^{-3}$] is the volumetric soil water content, t [s] is time, z [mm] is the height above some datum in the soil column, q [mm s^{-1}] is the water flux, and Q [$\text{mm}^3 \text{mm}^{-3} \text{s}^{-1}$] is the sink of soil moisture. The flux of water is given by

Darcy's law as

$$q = -\kappa \frac{\partial(\psi + z)}{\partial z} \quad (2)$$



where k [mm s^{-1}] is the hydraulic conductivity and ψ [mm] is the soil matric potential. The hydraulic conductivity and soil matric potential are modeled as the non-linear function of volumetric soil moisture (Clapp and Hornberger, 1978) as

$$\kappa = \Theta_{ice} \kappa_{sat} \left(\frac{\theta}{\theta_{sat}} \right)^{2B+3} \quad (3a)$$

$$95 \quad \psi = \psi_{sat} \left(\frac{\theta}{\theta_{sat}} \right)^{-B} \quad (3b)$$

where κ_{sat} [mm s^{-1}] is saturated hydraulic conductivity, ψ_{sat} [mm] is saturated soil matric potential, B is a linear function of percentage clay and organic content (Oleson et al., 2013), and Θ_{ice} is the ice impedance factor (Swenson et al., 2012). ELMv2.0 uses the modified form of Richards equation of Zeng and Decker (2009) that computes Darcy flux as

$$q = -\kappa \frac{\partial(\psi + z - C)}{\partial z} \quad (4)$$

100 where C is a constant hydraulic potential above the water table, z_{∇} , given as

$$C = \psi_E + z = \psi_{sat} \left[\frac{\theta_E(z)}{\theta_{sat}} \right]^{-B} + z \quad (5)$$

where ψ_E [m] is the equilibrium soil matric potential and θ_E [$\text{mm}^3 \text{mm}^{-3}$] is the equilibrium volumetric soil water content. At the water table depth, $z = z_{\nabla}$, the soil water content is $\theta_E(z_{\nabla}) = \theta_{sat}$, thus $C = \psi_{sat} + z_{\nabla}$. Substituting equation (5) in equation (4) leads to

$$105 \quad q = -\kappa \frac{\partial(\psi - \psi_E)}{\partial z} \quad (6)$$

ELMv2.0 uses finite volume spatial discretization to rewrite the equation 1 as (Oleson et al., 2013):

$$\begin{aligned} \frac{\partial}{\partial t} \int_{\Omega_n} \theta \, dV &= - \int_{\Gamma_n} (\mathbf{q} \cdot d\mathbf{A}) - \int_{\Omega_n} Q \, dV \\ \left(\frac{\partial \theta_n}{\partial t} \right) V_n &= - \sum_{n'} (\mathbf{q}_{nn'} \cdot \mathbf{A}_{nn'}) - Q_n V_n \end{aligned} \quad (7)$$

110 where Ω_n represents the n -th non-overlapping control volume with volume V_n , such that $\cup_i^n \Omega_i = \Omega$, Γ_n represents the boundary surface of the n -th control volume. Applying semi-implicit time discretization and based on Taylor series expansion leads to:

$$\begin{aligned} \left(\frac{\Delta \theta_n^{t+1}}{\Delta t} \right) V_n &= - \sum_{n'} (\mathbf{q}_{nn'}^{t+1} \cdot \mathbf{A}_{nn'}) - Q_n^{t+1} V_n \\ \left(\frac{\Delta \theta_n^{t+1}}{\Delta t} \right) V_n &= - \sum_{n'} \left(\mathbf{q}_{nn'}^t + \frac{\partial \mathbf{q}_{nn'}^t}{\partial \theta_n} \Delta \theta_n^{t+1} + \frac{\partial \mathbf{q}_{nn'}^t}{\partial \theta_{n'}} \Delta \theta_{n'}^{t+1} \right) \cdot \mathbf{A}_{nn'} - Q_n^{t+1} V_n \end{aligned} \quad (8)$$

115 where $\Delta \theta_n^{t+1}$ is the change in the volumetric liquid soil moisture over the time interval Δt . Since ELMv2.0 only resolves vertical soil water movement, the control volume n at layer k is connected to the soil layer above and below and has no column



connections. The discretized equation 8 leads to a tridiagonal system of equations for each ELM soil column such that at k -th soil layer:

$$a\Delta\theta_{k-1}^{t+1} + b\Delta\theta_k^{t+1} + c\Delta\theta_{k+1}^{t+1} = r \quad (9)$$

where:

$$120 \quad a = -\left(\frac{\partial q_{k-1/2}^t}{\partial \theta_{k-1}^t}\right) \quad (10)$$

$$b = \left(\frac{\partial q_{k-1/2}^t}{\partial \theta_k^t} - \frac{\partial q_{k+1/2}^t}{\partial \theta_k^t}\right) - \frac{\Delta z_k}{\Delta t} \quad (11)$$

$$c = \left(\frac{\partial q_{k+1/2}^t}{\partial \theta_{k+1}^t}\right) \quad (12)$$

$$r = -\left(q_{k-1/2}^t - q_{k+1/2}^t + e_k\right) \quad (13)$$

125 where $q_{k-1/2}$ mm s⁻¹ is the Darcy flux between $k-1$ -th and k -th soil layer, Δz_k mm is the soil thickness of the k -th soil layer, and e_k mm s⁻¹ is the sink of water.

In this work, we modified the ELMv2.0 tridiagonal system given by equation 9 to include unsaturated lateral flux, q_k^{ulat} , between g -th and g' -th grid cell for the k -th soil layer (Figure 2). The ELM with the newly developed lateral flow model is hereafter abbreviated as ELM_{lat}. Specifically, the equation 13 is modified to account for lateral flux, which is explicit time integration and yields

$$130 \quad r = -\left(q_{k-1/2}^t - q_{k+1/2}^t + e_k\right) + \sum_{g'} \left(q_k^{ulat,gg'}\right)^t \left(\frac{A_k^{gg'}}{V_k^g}\right) \quad (14)$$

135 where $q_k^{ulat,gg'}$ is lateral flux between grid cell g and its neighbor cells g' for the k -th soil layer. The calculation of q^{ulat} is routed based on the connections for each two neighbouring columns. As shown in Figure 1, for a 4-column (marked as x1, x2, x3 and x4) x-z 2-D transect, there are overall 3 connections which are marked as c12, c23, and c34 on the figure. Following Maxwell (2013), we adapt the grid alignment in ELMv2.0 with parallelogram grid cells to better represent the real world terrain. The adaption is illustrated in Figure 1 for a x-z transect with a uniform Δz . In this setup, the lateral Darcy flux in unsaturated zone is modified to follow the grid alignment in Figure 1 (Celia et al., 1990; Maxwell, 2013):

$$q_k^{ulat,gg'} = -\kappa_x \left(\frac{\partial(\psi + z)}{\partial x} \cos\theta_x + \sin\theta_x\right) \quad (15)$$

140 where θ_x is the local (cell center) angle of slope at the horizontal (x) direction and θ_z is the angle between the normal vector of the cell surface and the vertical direction (z) The vertical fluxes including q_z and evapotranspiration (ET)/infiltration are adapted accordingly to align with the terrain following shape as well, which can be expressed as:

$$q_z' = q_z \cos\theta_z \quad (16)$$



where θ_z is the angle between the normal vector of the cell surface and the vertical direction (z). The lateral Darcy flux at y -direction adopts the same computation method as equation 15. Otherwise, the computation of hydraulic properties and derivatives of the Darcy fluxes relevant to the soil liquid water content follows the same method with Oleson et al. (2013).

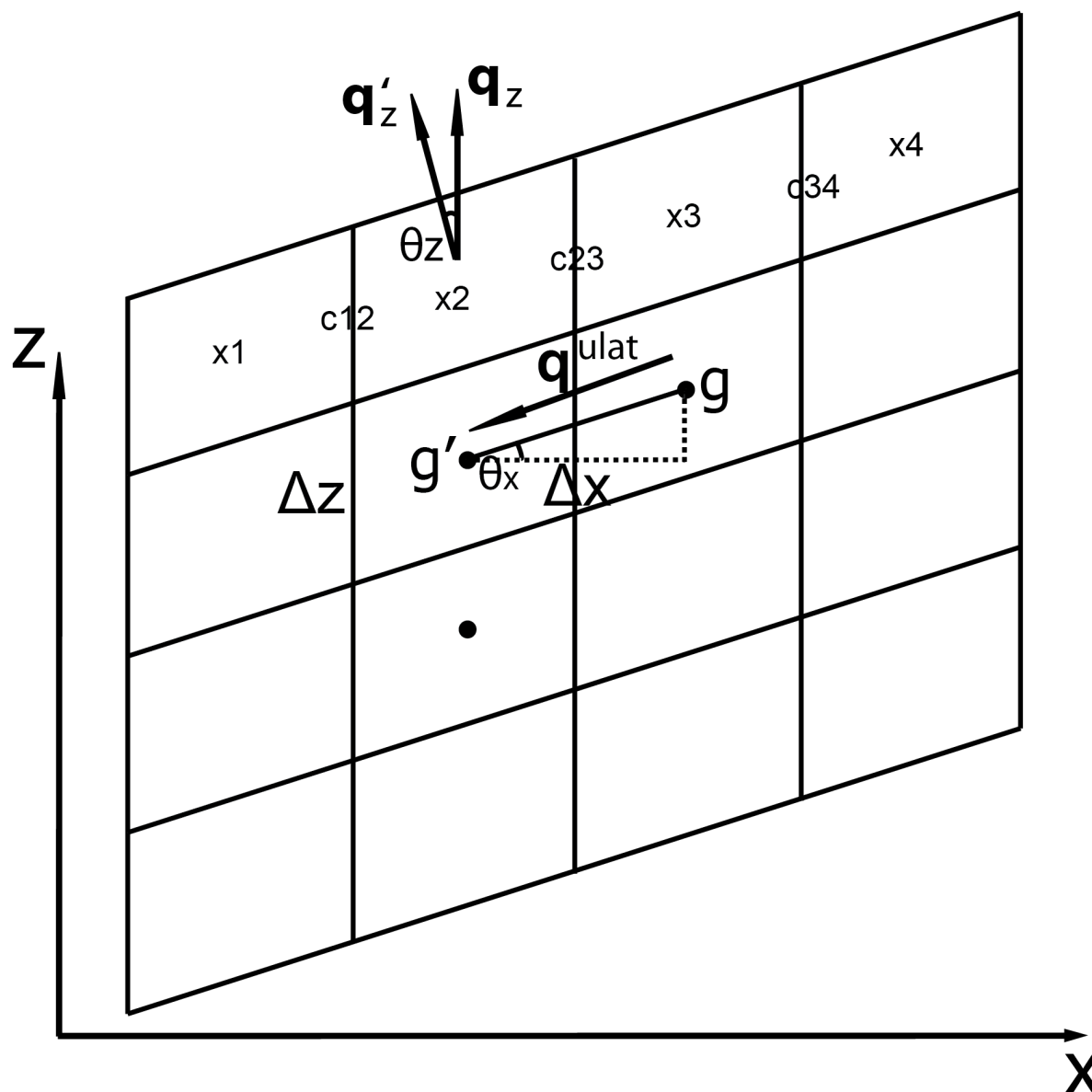


Figure 1. Sketches of the terrain following grid formulations. θ_x is the local angle of slope at the horizontal (x) direction, and θ_z is the angle between the normal vector of the cell surface and the vertical direction (z)



145 **2.2 Lateral flow in saturated zone**

The lateral flow in the saturated zone, q^{slat} [m^3/s], is also modeled using Darcy's law while taking the soil matric potential gradient as the groundwater hydraulic head gradient. In such a manner, the volumetric lateral groundwater flow can be given as:

$$q^{slat} = -wT \frac{\partial z_{\nabla}}{\partial x} \quad (17)$$

150 where w [m] is the width of the grid cell, and T [m^2/s] is the transmissivity. The transmissivity is calculated following the method used in Fan et al. (2007). The q^{slat} is computed across inter-grid cell using the same grid cell connections as used for the q^{ulat} . The water table depth for each soil column within a grid cell is thereafter adjusted based on q^{slat} . Specifically, the q^{slat} increases/decreases the soil water content of the soil layer where the groundwater table is currently located. The soil moisture is updated while ensuring the soil moisture remains below/above the maximum/minimum allowable value. If the
155 change in the soil moisture is less than the q^{slat} , the soil moisture of layers above/below is recursively increased/decreased till the total change in soil moisture in all updated soil layers matches q^{slat} . In ELMv2.0, the groundwater table is adjusted by a conceptual recharge flux which depends on whether the water table is within or below the soil column. The approach by explicitly subtracting the hydrostatic equilibrium soil moisture distribution from the Richards equation resolved the numerical deficiencies when the water table is within the soil columns while using θ -based Richards equation (Zeng and Decker, 2009).
160 In ELM_{lat}, the water table is assumed within the soil columns, such that the conceptual recharge flux is no longer employed. The groundwater table depth is computed based on the soil water content following the θ -based water table method in CLM5.0 (Figure 2). A no flux boundary condition is applied to the last hydrologically active soil layer. Following ELMv2.0, the saturated zone is depleted by a drainage flux, i.e. the subsurface runoff, that is computed based on the SIMTOP scheme of Niu et al. (2007), with modifications to account for frozen soils (Oleson et al., 2013).

165 **2.3 Model benchmarking against PFLOTRAN for idealized hillslopes**

Three idealized hillslopes that included a convergent hillslope (CH), divergent hillslope (DH), and titled V-shape hillslope (VH) with variable saturated initial conditions are used to validate ELM_{lat} by benchmarking against a 3D subsurface flow and transport model, PFLOTRAN (Hammond and Lichtner, 2010).

2.3.1 Idealized hillslope geometries

170 The CH/DH problems have been widely used to test the newly developed lateral groundwater flow model, e.g. (Troch et al., 2003; An et al., 2010; Hazenberg et al., 2015). Different from ELMv2.0 which uses uniform grid cells, the surface area of CH/DH grid cells change along the slope. The surfaces of CH/DH are curved by the sinusoidal function (Figure 3):

$$z(x, y) = 10 \sin\left(\frac{x\pi}{100} - \frac{\pi}{2}\right) + \frac{y}{50} \quad (18)$$

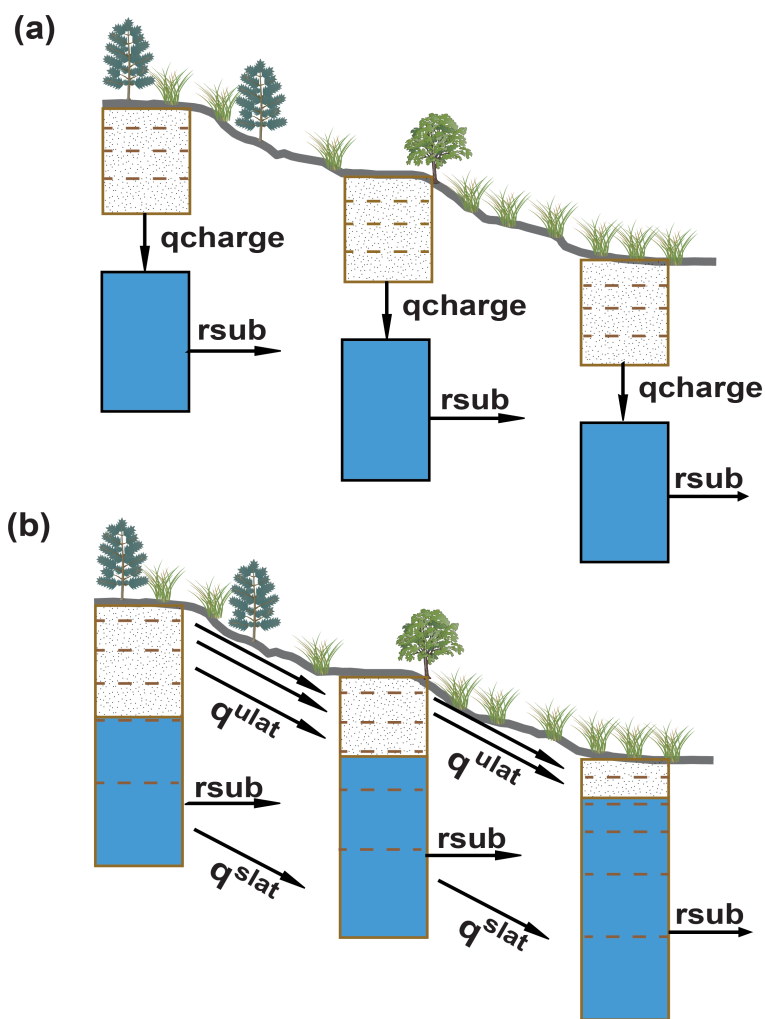


Figure 2. Schematic illustration of the subsurface flow implementation in unsaturated and saturated zone from (a) ELMv2.0 to (b) ELM_{lat}; q_{charge} is the conceptual recharge flux used to update the groundwater table, q^{ulat} is the lateral flux in unsaturated zone, q^{slat} is the lateral flux in saturated zone, r_{sub} is the subsurface runoff



where x , y , and z are the coordinates of the cell vertices. For the CH, the total width along the y -direction linearly shrinks from 100 m at hill top to 80 m at hill bottom; whereas for the DH, it linearly expands from 80 m at hill top to 100 m at hill bottom (Figure 3). The total width along the x -direction is 100 m for both CH and DH.

The tilted V-catchment hillslope is another popular benchmark problem for validating groundwater flow in land surface models (Park et al., 2009; Sulis et al., 2011; Maxwell et al., 2014). As shown in Figure 3 (c), the V-shape catchment is formed by the union of two symmetrically inclined planar surfaces ($80\text{ m} \times 100\text{ m}$) on the sides connected by a channel in the middle ($20\text{ m} \times 100\text{ m}$). The two planar surfaces are inclined with slopes of ± 0.05 and 0.02 at x and y directions, respectively. The channel is inclined following the slope of 0.02 at the y direction.

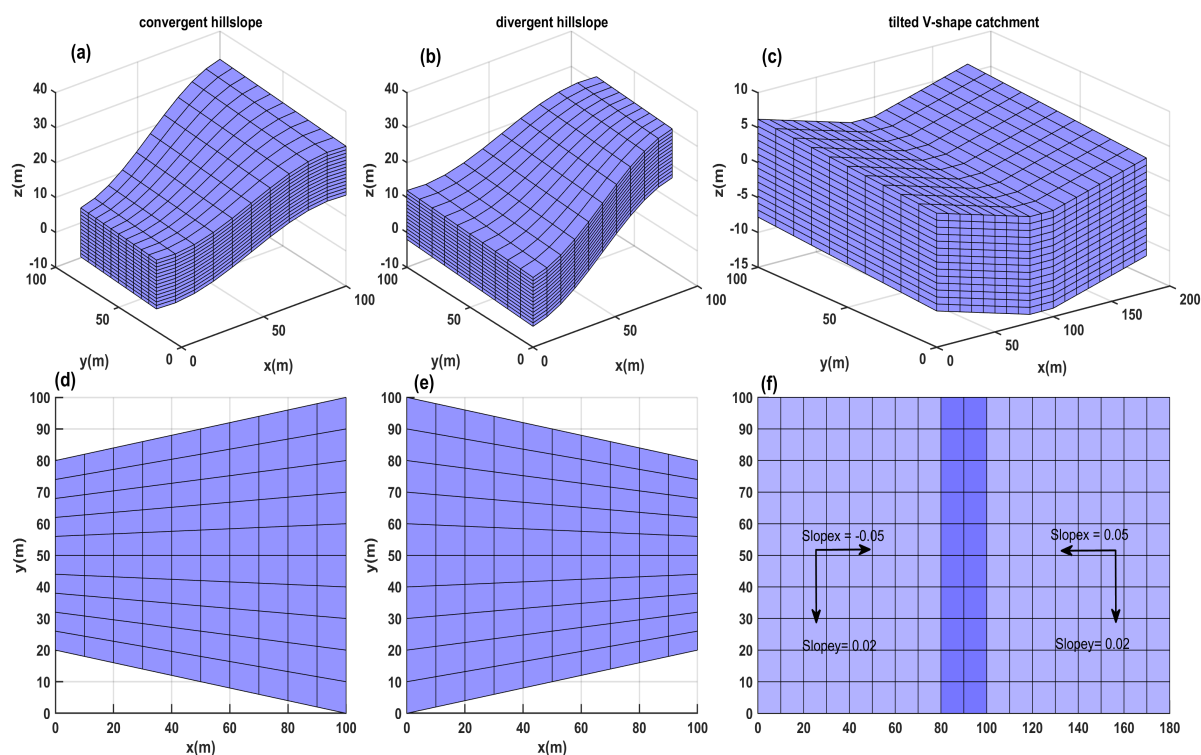


Figure 3. Geometries of the three benchmark test problems. (a), (b), (c) are 3-D views, and (d), (e), (f) are x - y views of the three benchmark test problems, respectively. S_x and S_y are slopes along the x and y directions, respectively.

2.3.2 Model setup

By default, the soil columns of ELMv2.0 are vertically discretized into 15 soil layers of exponentially varying soil thicknesses reaching a depth of 42.1 m. Only the first 10 soil layers are hydrologically active and occupy the top 3.8 m of a soil column.



185 For the model benchmarking, we modified the default model setup by allowing all 15 soil layers to be hydrological active and have a uniform soil thickness of 1 m to be consistent with the setup for PFLOTRAN simulations. The soil columns were horizontally discretized to a 10×10 mesh with a grid resolution of 10 m at x direction and changing resolution at y direction for CH and DH. For VH, the soil columns were discretized horizontally with a uniform grid resolution of 10 m at both x and y directions, which produced a mesh of 18×10 . A homogeneous soil texture was used with a porosity of 0.43. The soil
190 water retention properties in ELMv2.0 were described using the Clapp-Hornberger formula (Clapp and Hornberger, 1978) while in PFLOTRAN they were described using the Brooks Corey's formula (Brooks, 1965). We matched the soil water retention property parameters in PFLOTRAN with ELM. The anisotropic ratio for the hydraulic conductivity was set as 1.0 for the CH and DH cases ($K_x = K_y = K_z$), and was set as 10.0 for the VH case ($K_x = K_y = 10K_z$). The same boundary and initial conditions were applied for the three benchmark problems. A no-flow boundary condition was applied on all sides of
195 the domain. Hydrostatic pressure was used as the initial condition with the groundwater table depth (WTD) set at 7 m deep from the top surface. ELM_{lat} and PFLOTRAN simulations were performed for 80 days for all three benchmark problems and results were compared at the end of the simulation. The performance of soil moisture dynamics was evaluated using the mean absolute error (MAE) between ELM_{lat} and PFLOTRAN, while the performance of groundwater was directly evaluated by the difference between ELM_{lat} and PFLOTRAN simulations.

200 2.4 Model application

2.4.1 Study region

ELM_{lat} is applied to study the role of lateral subsurface flow on terrestrial processes in the Little Washita Watershed (LWW), which is located in the southwestern Oklahoma, USA (Figure 4). The LWW has a drainage area of $\approx 611 \text{ km}^2$ and is one of the seven selected experimental watersheds jointly administrated by the U.S. Department of Agriculture (USDA) and U.S.
205 Environmental Protection Agency for a variety of hydrologic research projects. The LWW has a subhumid climate with annual precipitation of approximately 760 mm and annual temperature of approximately 16°C . The elevation of LWW ranges from approximately 320 m to 460 m., and the slope ranges from 0° to 3° (Figure 4). Grassland is the dominant land cover of LWW, with small portions of land occupied with crops, shrubs, and deciduous trees. The mean annual Leaf Area Index (LAI) is within the range of $0.5\text{-}3 \text{ m}^2/\text{m}^2$. Soil textures of LWW are composed of sand, loam, and silty loam (Allen and Naney, 1991). LWW
210 has a relatively higher soil content of sand and organic matter in the northwestern part and southeastern part; several spots in the southern region have higher clay content(Figure 4a-c).

2.4.2 Model configuration and data

The model domain covered a $35 \text{ km} \times 50 \text{ km}$ area encompassing the LWW and was laterally discretized at $1 \text{ km} \times 1 \text{ km}$. All 15 soil layers were set as hydrologically active. Results from Fan et al. (2013) show the maximum WTD could reach upto
215 60 m deep in this region. By default, the 15th soil layer in ELMv2.0 reaches a depth of 48m. Therefore, we modified the soil thickness of the last two soil layers by adding 20 meters each to their default values in ELMv2.0 while keeping the discretization

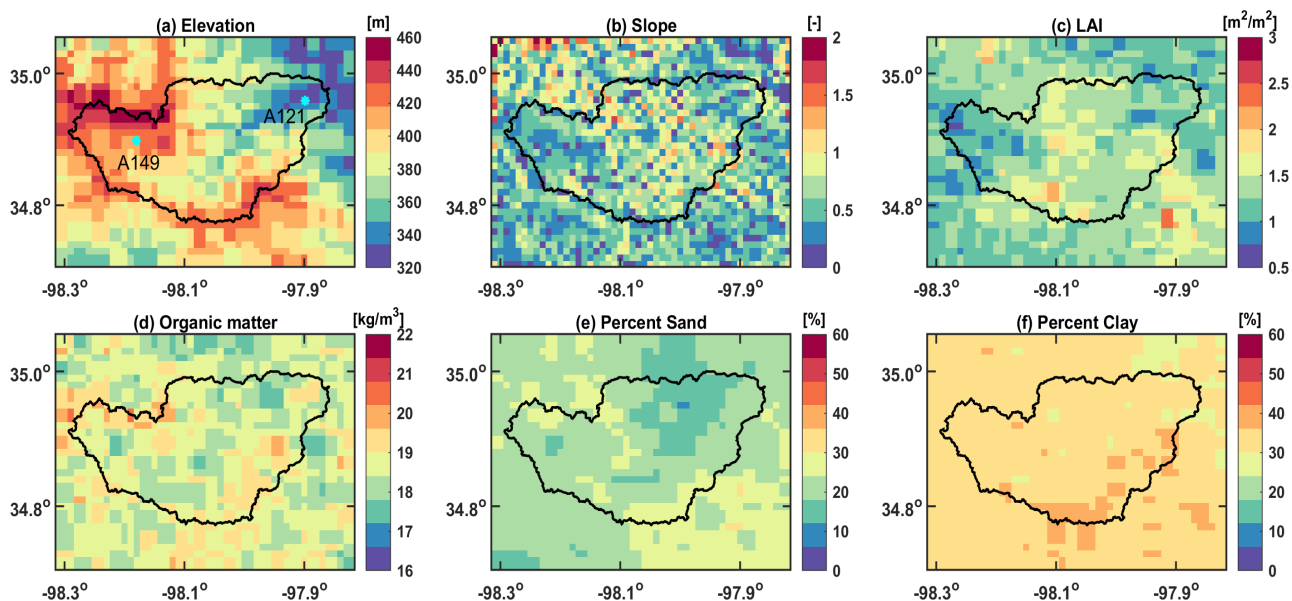


Figure 4. Spatial distributions of (a) elevation, (b) slope, (c) mean monthly leaf area index, (d) organic matter density, and (e–f) percentages of sand and clay, respectively, over the study area at a resolution of 1 km.

of the other 13 soil layers unchanged. The total soil thickness could reach 82 m. The initial WTD was spatially uniformly set at 8 meters deep below the top surface of the domain. The hourly NLDAS data (<https://ldas.gsfc.nasa.gov/nldas/v2/forcing>) was used as the climate forcing which has a spatial resolution of 1/8th-degree grid. We performed 100-year simulations with ELM_{lat} and $ELMv2.0$ while cycling the atmospheric forcing data of 2008 to allow sufficient time for the model spin-up. The model results from the last year of the spin-up were used for analysis.

The 1 km surface data used in this study was generated using multiple high-resolution, sub-kilometer data sets including vegetation, soil, and topography related variables (Table 1). The soil, elevation and LAI datasets were first aggregated to 1 km using the area-weighted average method, and the land cover data was aggregated to 1 km using the majority resampling method. Specifically, MODIS 500 m land cover was at year 2005 obtained from the Google Earth Engine (Gorelick et al., 2017). Following Ke et al. (2012), the LC_Type 5 class of MCD12Q1 v6 land cover product (Friedl and Sulla-Menashe, 2019) was used to determine the lake, urban, glacier, and vegetation plant functional types (PFTs). These PFTs were further classified into tropical, temperate, and boreal sub-types based on the rules presented in Bonan et al. (2002) and using meteorological data from WorldClim V1 (Hijmans et al., 2005). The monthly climatology LAI was derived from the 4-day MCD15A3H V6.1 (Myneni et al., 2021) over 2003–2020 using GEE. Then based on the method in Zeng et al. (2002), we calculated the monthly climatology stem area index (SAI) from the LAI data. For the soil data, we used the Soilgrid v2 data with an original resolution of 250 m (Poggio et al., 2021). Soilgrid is generated based on machine learning using multiple data sources of soil profiles and remote sensing data (Hengl et al., 2017). The percent clay, percent sand, and soil organic matter at multiple depths were



Table 1. Specifications of high-resolution data sets used in this study.

Type	Parameter	Spatial resolution	Temporal resolution	Data source	Reference
Land cover	Vegetation type	500 m	yearly	MODIS MCD 12Q1 V6	Friedl and Sulla-Menashe (2019)
	leaf area index	500 m	2003–2020, 4-day	MODIS MCD15A3H V6.1	Myneni et al. (2021)
	Stem area index	500 m	2003–2020, 4-day	Calculated	
Soil	Percent sand	250 m	Static	Soilgrid v2	Poggio et al. (2021)
	Percent clay	250 m	Static	Soilgrid v2	Poggio et al. (2021)
	Organic matter	250 m	Static	Soilgrid v2	Poggio et al. (2021)
Topography	Elevation	90 m	Static	SRTM v4	(Jarvis et al., 2008)

processed for ELM. The 90 m digital elevation from the Shuttle Radar Topography Mission (Jarvis et al., 2008) was used to
 235 derive topography-related parameters in ELM, including the standard deviation of elevation and slope. These 0.01 deg datasets
 were processed using GEE based on the original 90 m elevation. We used a continuous global WTD map with a resolution
 of 30 arc-second (≈ 1 km) (Fan et al., 2013) to validate the simulated WTD, which is hereafter referred as Fan2013. The
 impacts of lateral flow on the model performance were assessed by comparing the soil moisture and energy fluxes including
 soil temperature, Latent and sensible heat flux, with ELMv2.0 simulation. Site-level observations of soil moisture and soil
 240 temperature were collected from the ARS Micronetwork (<https://ars.mesonet.org/>) which is operated and maintained by the
 USDA.

3 Results and discussion

3.1 Evaluation of simulations for the benchmark problems

ELM_{lat} can accurately reproduce the evolution of vertical soil moisture profile simulated by PFLOTRAN for all three bench-
 245 mark problems (Figure 5). The model correctly simulates the drying out of uphill soil columns (Figure 5a-b) and the wetting

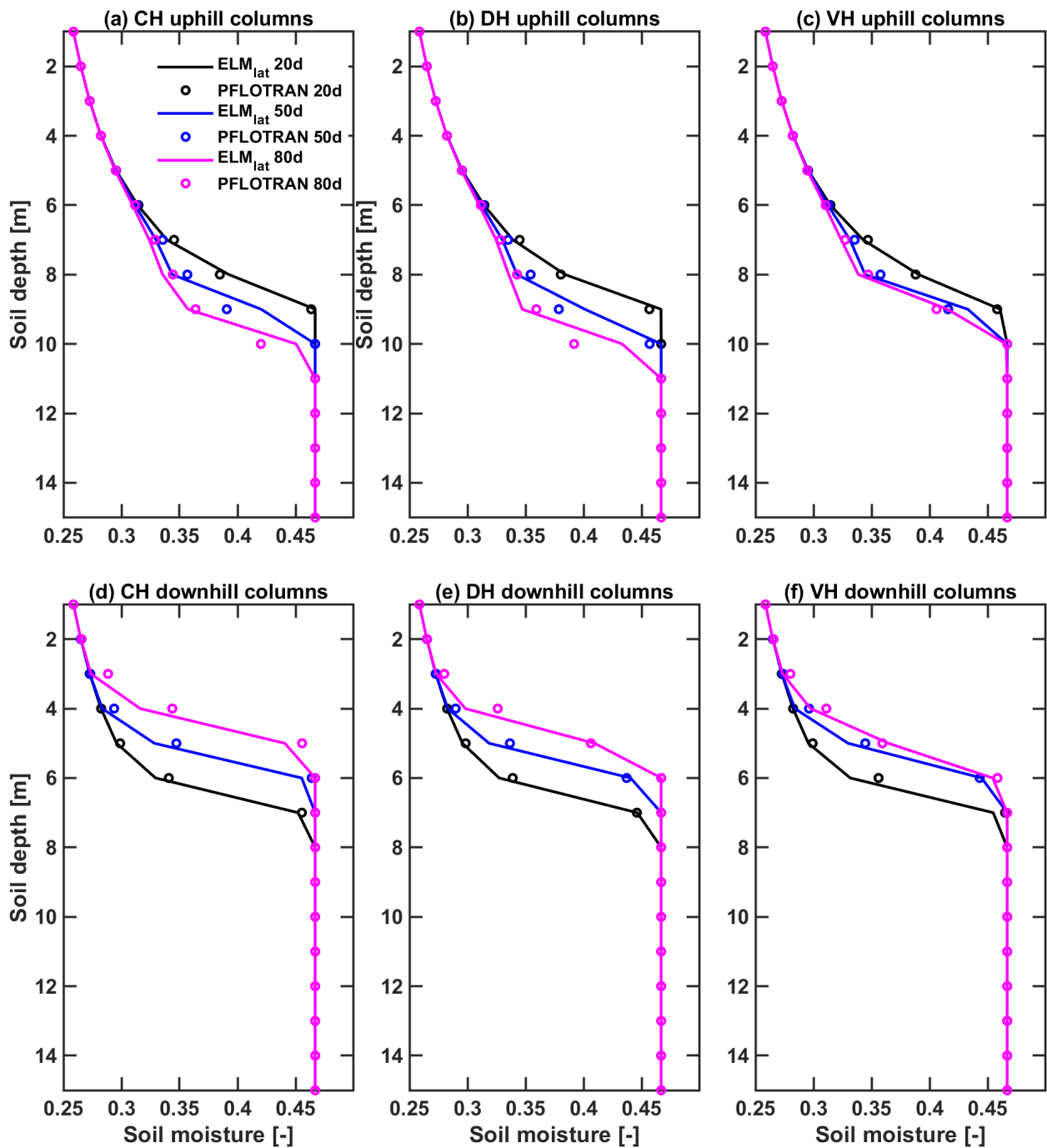


Figure 5. ELM_{lat} simulated mean soil moisture profile for the ten uphill columns of (a) convergent hillslope, (b) divergent hillslope, (c) V-shape hillslope, and ten downhill columns of (d) convergent hillslope, (e) divergent hillslope, (f) V-shape hillslope, at 20th, 50th and 80th simulation day, respectively.

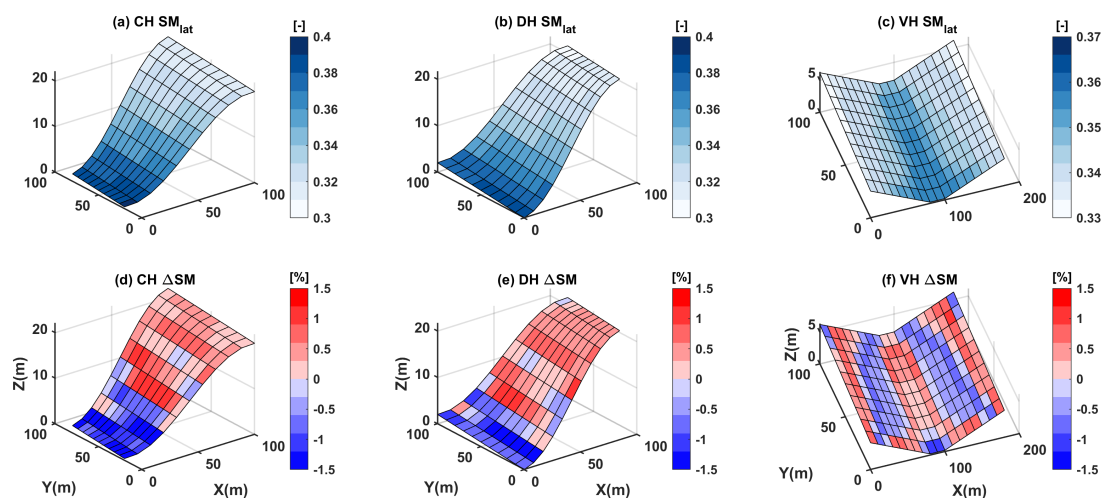


Figure 6. ELM_{lat} simulated average soil moisture for the top 5 layers at 80th day for (a) convergent hillslope, (b) divergent hillslope, (c) V-shape hillslope, and the differences with PFLOTRAN for (d) convergent hillslope, (e) divergent hillslope, (f) V-shape hillslope, respectively.

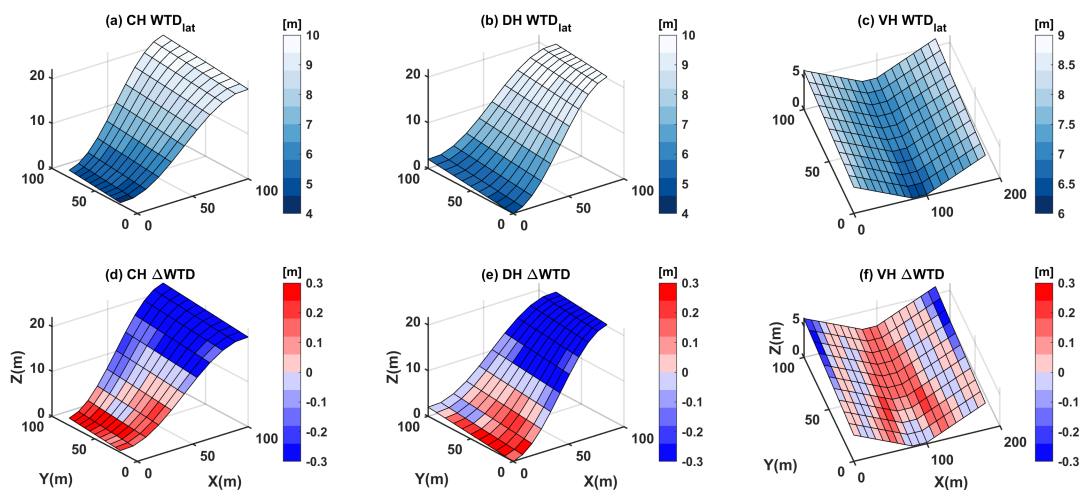


Figure 7. ELM_{lat} simulated water table depth at 80th day for (a) convergent hillslope, (b) divergent hillslope, (c) V-shape hillslope, and the differences with PFLOTRAN for (d) convergent hillslope, (e) divergent hillslope, (f) V-shape hillslope, respectively.



up of downhill soil columns (Figure 5d-e) for all the three hillslopes. In the VH case, the soil moisture shifted quickly during 20 d – 50 d but slowed down during 50 d – 80 d, whereas the soil moisture changing pace are nearly steady for the CH and DH cases during the two periods. The soil properties used in the three test cases are exactly the same except that the VH case has a higher anisotropic ratio and therefore higher lateral hydraulic conductivity. It is probable that during the period of 50 d - 80 d, the VH case is more approaching hydrostatic condition than the other two cases. These differences were well captured by ELM_{lat} as compared with PFLOTRAN. The largest discrepancies in the simulated soil moisture are in soil layers that are closer to the water table, and these discrepancies could be explained by the differences in the model structure (Figure A1). PFLOTRAN solves the variably saturated subsurface flow equation, which is applicable for both the unsaturated and saturated zones, while ELM_{lat} has two separate flow models for the unsaturated and saturated zone. Thus, the difference between the two models is expected to be the largest near unsaturated-saturated zone transition.

After 80 days evolution, the soil moisture redistributed and transported following the surface topography via the lateral flow (Figure 6a-c). The most downhill columns of CH and DH are approaching saturated. As compared to PFLOTRAN, ELM_{lat} underestimated the soil moisture transport from the upland to the lowland such that the upland cells were wetter and the lowland cells were drier for all three benchmark problems, as shown in Figure 6. However, the difference between the two models was small ($< \pm 2\%$) for the top five layers on the 80-th simulation day, which provides confidence in the ability of ELM_{lat} to simulate lateral unsaturated soil moisture dynamics. During the 80 days simulation period, the MAE in ELM_{lat} simulated soil moisture for all cells in the top 5 soil layers remains within $1\% \pm 4\%$ for all three test problems, as shown in Figure A2.

At the end of the simulation, the simulated groundwater table evolves from the spatially uniform initial depth (i.e., 7 m) to a spatially varying depth that is inversely related to the surface elevation (Figure 7a-c). Similar to the flow in the unsaturated zone, ELM_{lat} underestimates the lateral flow in the saturated zone as compared to PFLOTRAN with a shallower (deeper) simulated groundwater table in upland (lowland) cells (Figure 7d-f). The use of different soil water retention curves (i.e., Clapp and Hornberger (1978) in ELM_{lat} and Brooks (1965) in PFLOTRAN) could account for the differences in simulated WTD. Additionally, it should be noted that the prognostic variable in PFLOTRAN is the soil water pressure and the simulated WTD is diagnosed by linearly interpolating the vertical pressure profile for each soil column. Despite those structural differences, ELM_{lat} simulated WTD is comparable to that of PFLOTRAN with differences within ± 0.3 m throughout the simulation period (Figure A3). Overall, the above evaluation results demonstrate ELM_{lat} could accurately represent vertical and lateral transport of soil moisture and groundwater.

3.2 Evaluation of simulations over LWW

Applying ELM_{lat} in LWW significantly improves the simulation of WTD when compared to the ELMv2.0 results. Simulated WTD by ELM_{lat} showed strong correlations ($r = -0.71$) with surface topography which is consistent with Fan2013 results, while ELMv2.0-simulated WTD has no spatial variations (Figure 8). The simulated WTD in the higher northwest part of the watershed was not as deep as that reported in Fan2013. One major reason for this could be due to the climate forcing data used in this study may not represent the long term steady state as suggested by Fan2013. Moreover, it has been previously shown that the subsurface drainage parameter (f_d) exerts a strong control on the long-term simulated WTD in 1D ELM

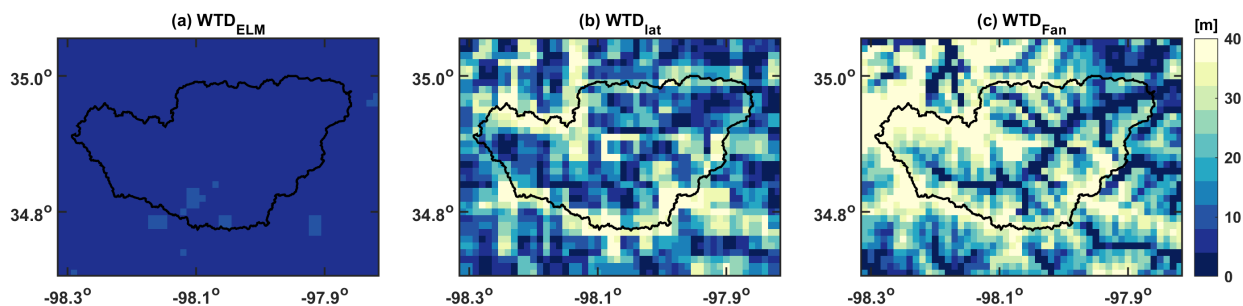


Figure 8. Annual average groundwater table depth (WTD) simulated by (a) ELMv2.0 and (b) ELM_{lat}, along with (c) the Fan2013 dataset

280 simulations (Bisht et al., 2018). However, since the primary goal of this study is to develop the model structure and evaluate the model performance, calibration of f_d to match the Fan2013 results is out of the scope of this work, especially considering the differences of the climate forcings mentioned above. Therefore, no calibration of f_d was done to better match the WTD and the default value of f_d ($= 2.5 \text{ m}^{-1}$) was used in this study.

ELM_{lat} simulated generally lower soil temperature (TS) and sensible heat flux (SH) but higher latent heat flux (LH) than ELMv2.0 for most of the grid cells (Figure 9). The spatial annual TS showed a gradually increasing trend from north to south. The LH and SH showed the opposite spatial pattern, where LH is higher the SH is lower. The effects of WTD changes on the energy fluxes were more pronounced at low elevation cells, especially at the stream and its surrounding cells. The delivery of the groundwater through the lateral flow to the valleys supported higher LH while reducing the SH compared with ELMv2.0 which has little spatial WTD variations.

290 Despite the observations being based on point measurements while simulated results representing 1km resolution, both ELM_{lat} and ELMv2.0 were able to capture the major fluctuations and wetting/drying cycles of soil moisture (SM) comparing with observations at the two stations (Figure 10). Station A121 is located at the lowland area of this catchment with an elevation of 343 m while station A149 is located in the high land area with an elevation of 420 m (Figure 4(a)). At station A121, ELM_{lat} simulated higher soil moisture, with the annual mean 0.013 higher at 5cm and 0.021 higher at 25cm than ELMv2.0 results. 295 At station A149, ELM_{lat} simulated slightly lower soil moisture, with annual mean 0.007 lower at 5cm and 0.009 lower than ELMv2.0 results.

For the soil temperature simulations, we focused on the summer temperature (Figure 11). Relative to ELMv2.0, ELM_{lat} simulated cooler summer temperature at both 5 cm (mean $\Delta \text{ST} = -0.063 \text{ }^\circ\text{C}$) and 30 cm depths (mean $\Delta \text{ST} = -0.061 \text{ }^\circ\text{C}$) at station A121. In contrast, at station A149, ELM_{lat} simulated slightly higher summer temperatures at soil depths of 5 cm (mean $\Delta \text{ST} = 0.018 \text{ }^\circ\text{C}$) and 30 cm (mean $\Delta \text{ST} = 0.019 \text{ }^\circ\text{C}$). The differences in summer temperature between ELM_{lat} and ELMv2.0 were consistent with the SH differences as discussed previously. More water cooled down the summer soil temperature at station A121, whereas less water increased the summer soil temperature at station A149. However, both ELM_{lat} and ELMv2.0 overestimated the temperature during July compared with observations, which may be due to the overestimation of incoming solar radiation or the discrepancies of the soil thermal properties between the model and reality at the sampled locations.

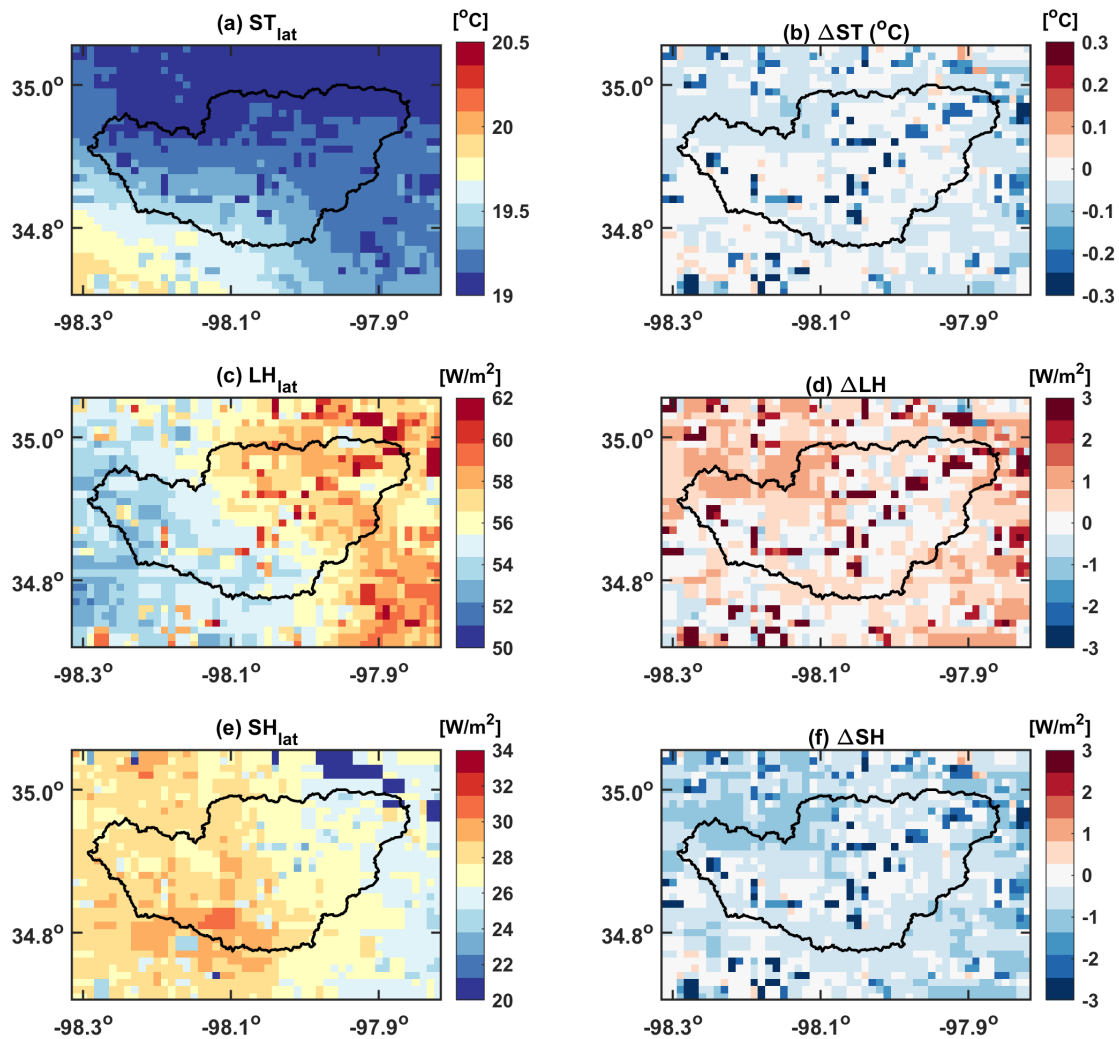


Figure 9. ELM_{lat} simulated annual (a) top layer soil temperature ($^{\circ}C$), (c) latent heat flux (W/m^2) and (e) sensible heat flux (W/m^2); (b), (d), (f) are the differences between ELM_{lat} and ELMv2.0 simulations for the three energy items, respectively

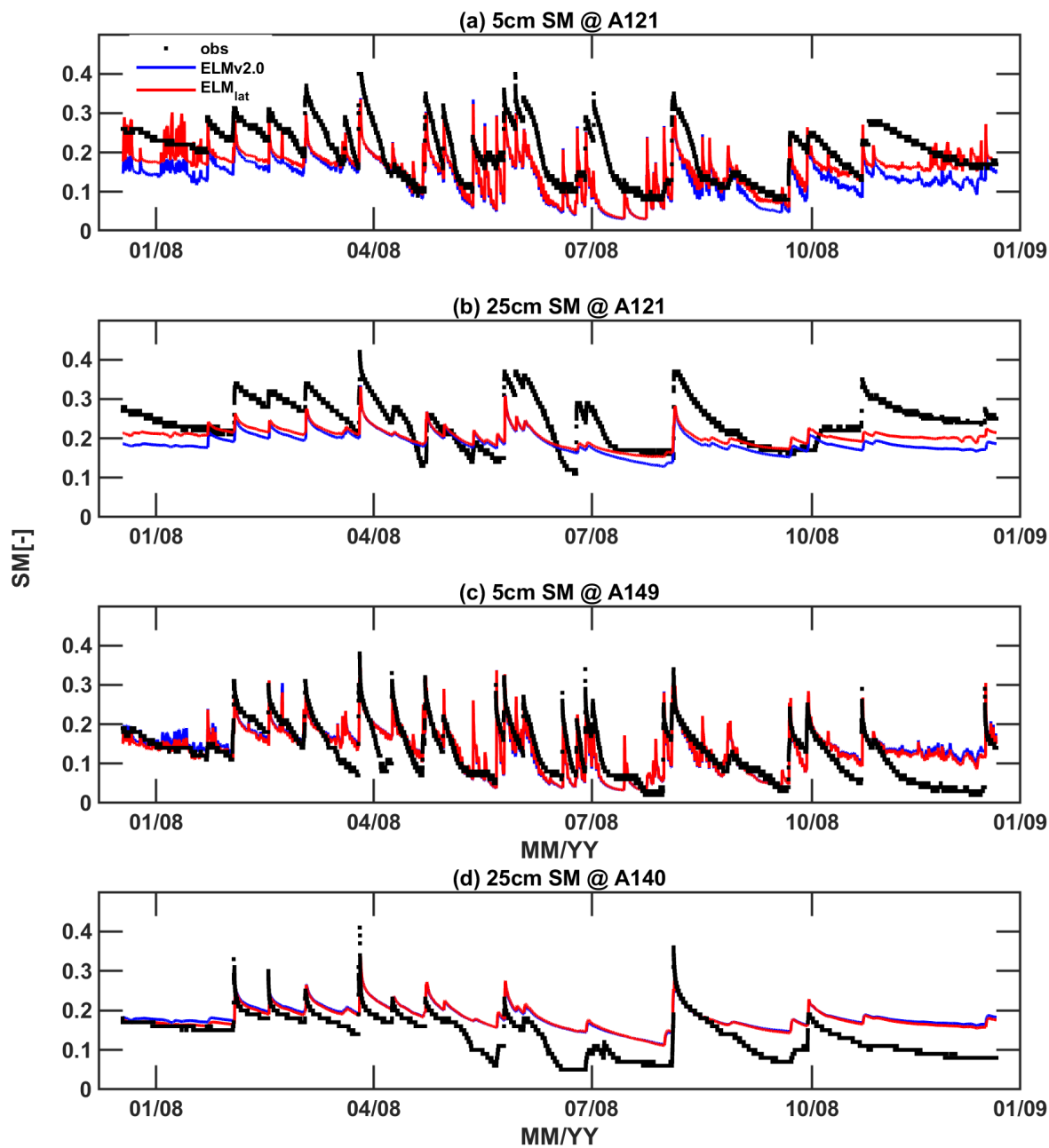


Figure 10. comparisons of simulated hourly soil moisture at depths of (a) 5 cm and (b) 25 cm of a low land station (A121) and at depths of (c) 5 cm and (d) 25 cm of a high land station (A149) between ELM_{lat} and ELMv2.0

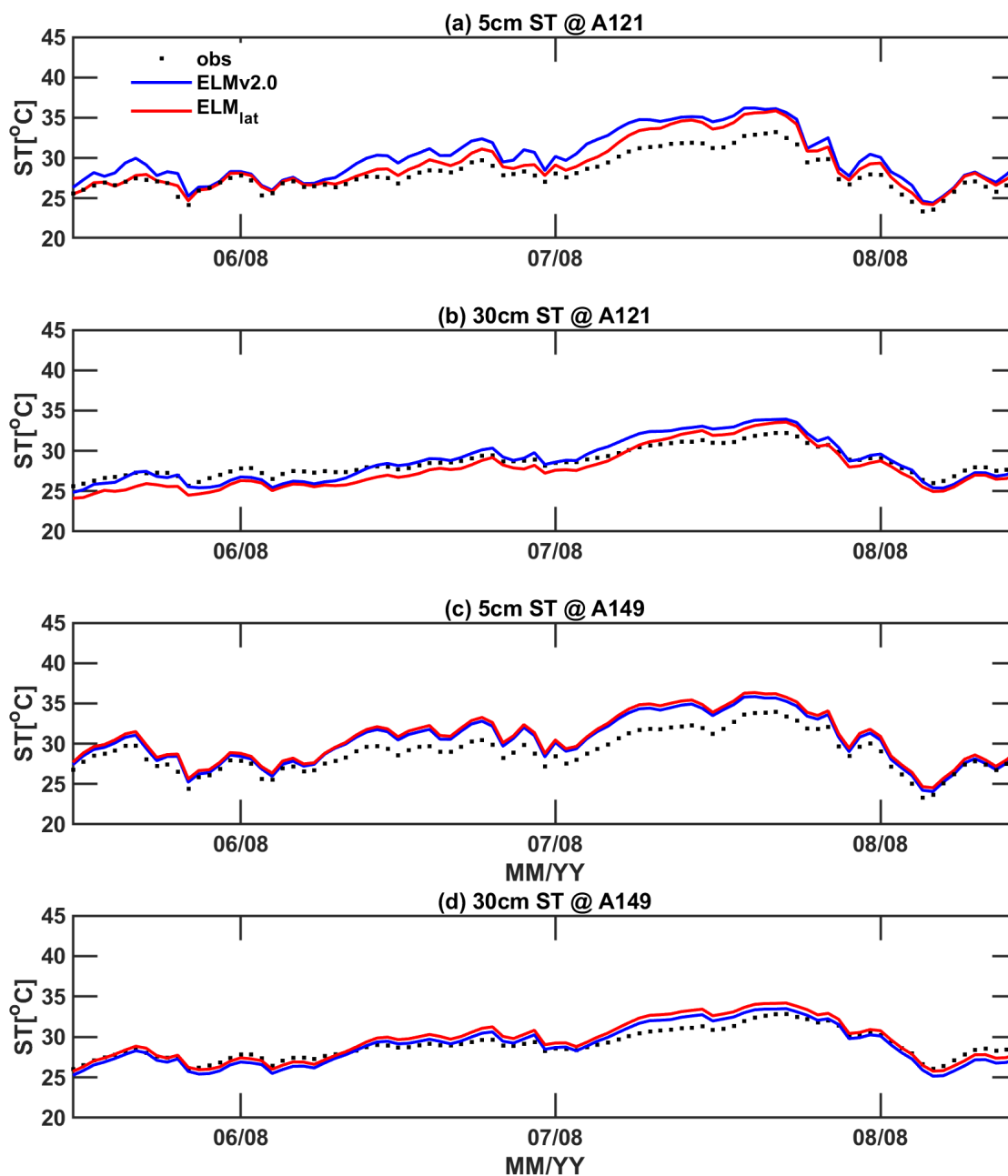


Figure 11. comparisons of simulated hourly summer soil temperature at depths of (a) 5 cm and (b) 25 cm of a low land station (A121) and at depths of (c) 5 cm and (d) 25 cm of a high land station (A149) between ELM_{lat} and $ELMv2.0$

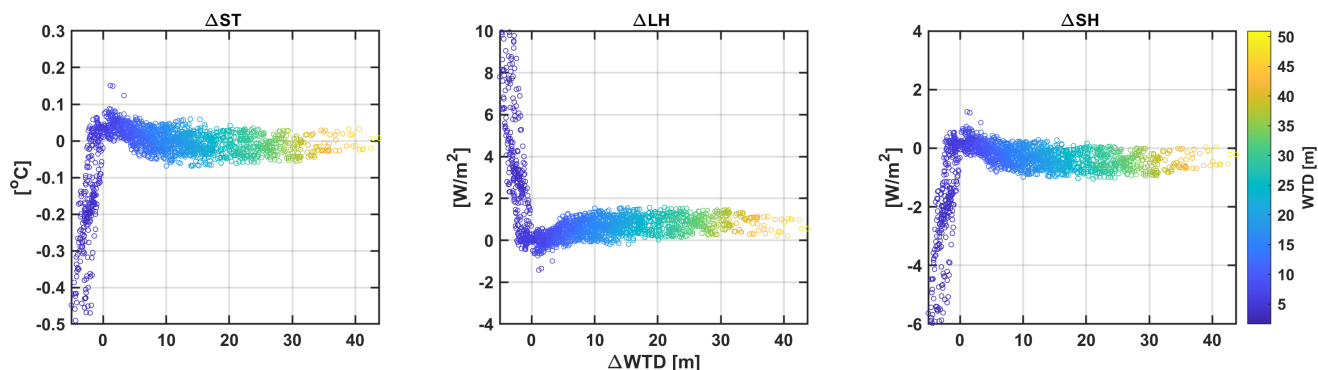


Figure 12. (a), (b), (c) are the difference of annual average surface soil temperature, latent heat flux, and sensible heat flux between ELM-lat and ELMv2.0 vs. simulated groundwater depth differences between ELM_{lat} and ELMv2.0; color bar indicates the groundwater table depths simulated by ELM_{lat}

305 Lateral groundwater flow reshapes the groundwater table map and impacts the surface heat fluxes (Figure 12). The most significant changes between ELM_{lat} and ELMv2.0 in heat fluxes occur when ELM_{lat}-simulated WTDs are less than 10 meters, where ELM_{lat} simulated generally shallower WTDs than ELMv2.0. As a result, ELM_{lat} simulated lower surface soil temperature and lower SHs, but higher LHs at shallower WTDs, which are consistent with previous discussions. And the difference of surface soil temperature, LHs and SHs are nearly linearly correlated with the WTD differences when the WTDs are less than 10 meters. At deeper layers, the heat fluxes are not sensitive to changes in WTDs. The maximum differences of simulated surface soil temperature values could reach -0.4 – -0.5 $^{\circ}C$, the LHs differences could reach 8 – 10 W/m^2 and the SHs differences could reach -4 – -6 W/m^2 , at grids where ELM_{lat} simulated WTDs are less than 5 meters. The depth at which groundwater can influence the vegetation functions are dependent on the roots' penetration depths (Fan, 2015). However, since the land use type is quite simple in this watershed (e.g., mainly grass), it is difficult to differentiate the effects of WTD changes on the vegetation functions for different PFTs.

315

3.3 Caveats and future work

ELM2.0 parameterizes the subsurface runoff with an exponential relationship of the water table depth (Bisht et al., 2018). Although a spatial uniform value of this parameter was used in this study, the simulated WTD is significantly improved in ELM_{lat} than the default scheme. Calibrating relevant parameters (e.g., f_d) can further improve the representation of WTD in ELM_{lat}. Moreover, a homogeneous anisotropic ratio was assumed in the LWW study given the relatively uniform soil properties. Homogeneous aquifer depth or depth to bedrock (DTB) was also assumed in the LWW study. Brunke et al. (2016) evaluated the effects of using spatially heterogeneous soil thickness and sedimentary deposits (Pelletier et al., 2016) on the simulated hydrological and thermal fluxes in CLM4.5. Incorporating heterogeneous DTB in CLM4.5 has more impacts

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observed in locations with shallow bedrock than in deep bedrock on the water and energy fluxes, reported by Brunke et al.
325 (2016). Incorporation of variable DTB and evaluation of the heterogeneity of parameters will be performed in the future study.

This study is primarily oriented to validate the new features of the unsaturated and saturated lateral flow in ELM across
grids and evaluate the connections between lateral groundwater flow and surface energy fluxes rather than rigidly close the
water balance by calibrating all the water balance components against observations. Therefore, water balance and streamflow
were not evaluated in this study. A holistic evaluation of the impacts of the lateral groundwater flow on the water and energy
330 balances, as well as the parameter sensitivities, will be tested and evaluated in a much larger domain in the future work. In the
present work, we have developed ELM_{lat} that runs serially and the model will be extended in the future to use high performance
computing to manage the high computational cost of global simulation.

Additionally, some anthropogenic activities, e.g., groundwater pumping, irrigation, as well as two way river/groundwater in-
teractions are not incorporated into the current model structure. Extensive groundwater pumping reduced discharge to streams,
335 with 10–23% of watersheds reaching critical environmental flow thresholds, revealed from large scale groundwater modeling
results (de Graaf et al., 2019). We envision a future road map with more holistic representations of hydrological functions
building upon the lateral connections of the grid network, not exclusively the lateral groundwater flow, but more realized
groundwater and surface water interactions in ELM.

4 Conclusions

340 Regarding the emerging highlights of lateral groundwater flow in the hyper-resolution large scale Earth system modeling, we
developed and validated an inter-grid cell lateral groundwater flow model for both saturated and unsaturated zone in the E3SM
Land Model framework.

By incorporating lateral groundwater flow in the ELMv2.0 and modifying the flux terms based on the non-horizontal terrain,
the ELM_{lat} could accurately simulate the soil moisture and WTD dynamics in three idealized hillslope problems validated
345 against PFLOTRAN. The ELM_{lat} underestimates the lateral groundwater flow relative to PFLOTRAN results, which may
be attributed to the different formulas used to parameterize the soil water retention properties in the two models. During the
simulation period, the MAE between the two models is within $1\% \pm 4\%$, and the simulated WTD differences are within ± 0.3
m.

The developed model was further tested in a realistic watershed, Little Washita Watershed. The simulated WTD by ELM_{lat}
350 showed a strong correlation ($r = -0.71$) with surface topography where higher land has a deeper groundwater table, which
agreed well with the WTD pattern in Fan2013. The effects of lateral groundwater flow on the energy flux partitions were more
pronounced at low elevation areas with shallower groundwater tables (i.e., $WTD < 10$ m). Lateral groundwater movement
from highland area to the valleys cooled down the summer surface soil temperature at low land areas; at high land area, less
water slightly increased the summer surface soil temperature. More water in the low land area supported higher LH while
355 reducing the SH compared with the ELMv2.0 simulation. In mountain area with very deep WTDs (> 10 m), the movement of
lateral fluxes have relatively small effects on the surface energy fluxes relative to the effects at the low land area. These results



underscore the importance of including lateral groundwater flow in the LSMs, especially in the critical zone to holistically understand the role of groundwater system on the terrestrial water-energy distribution and its feedback to climate change.

Code and data availability.

360 Data files and running scripts for model simulations are available at: <https://doi.org/10.5281/zenodo.7659300> (Qiu et al., 2023a). ELM_{lat} model are available at: <https://doi.org/10.5281/zenodo.7686303> (Qiu et al., 2023b) for the idealized hillslope problems and at: <https://doi.org/10.5281/zenodo.7686381> for the LWW application (Qiu et al., 2023c). E3SMv2.0 (including ELMv2.0) is supported by the Linux system.

The details for running E3SMv2.0 (including ELMv2.0) can be found at: <https://e3sm.org/model/running-e3sm/e3sm-quick-start/>.
365 ELM_{lat} adopts the same compilation and running approaches. PFLOTRAN can be installed and compiled on Linux, Mac, and Windows systems. The detailed instructions for PFLOTRAN installation and running are provided by the user's guidance at: https://www.pflotran.org/documentation/user_guide/user_guide.html

Appendix A

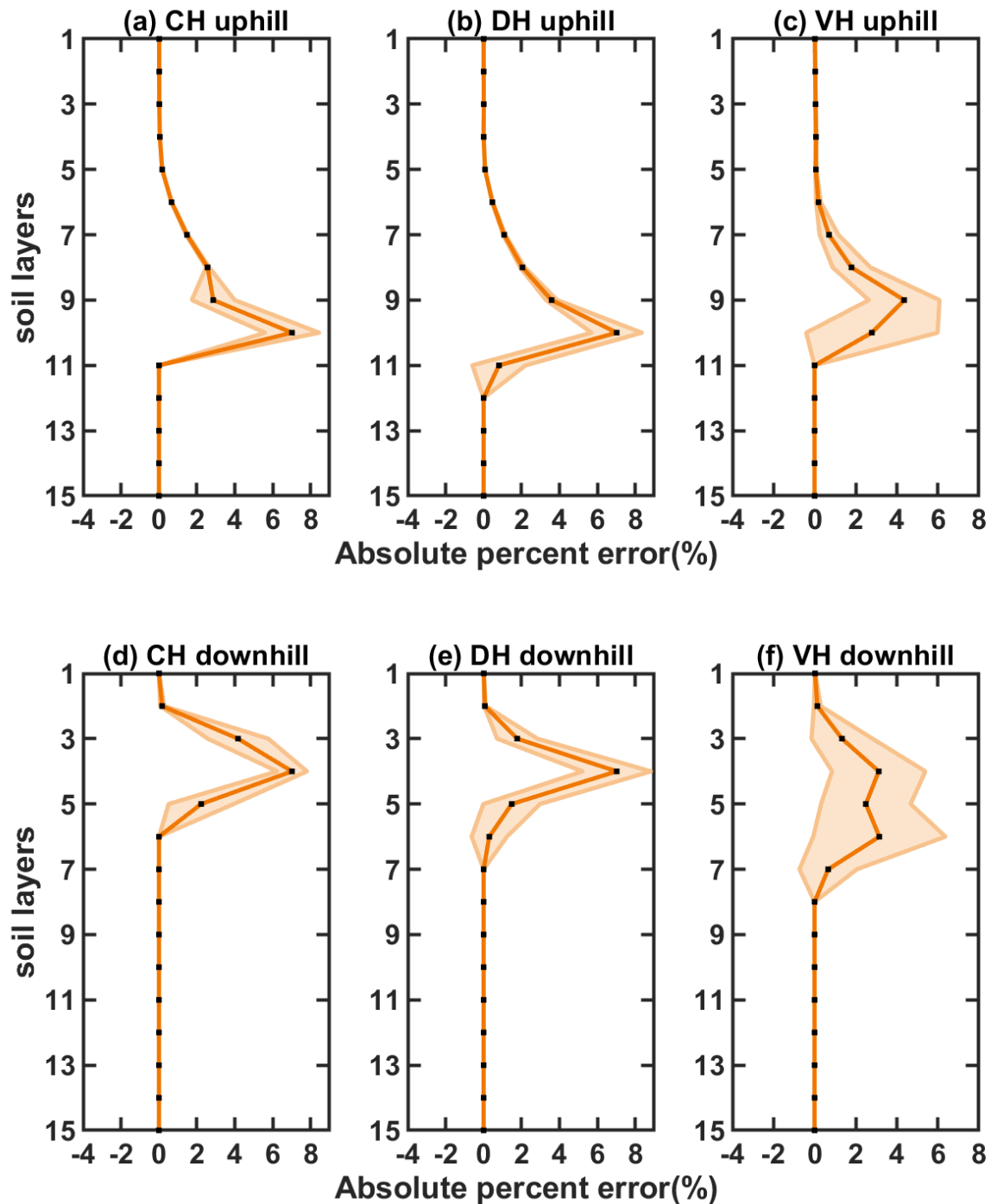


Figure A1. The mean absolute error of simulated soil moisture between ELM_{lat} and PFLOTRAN for the top five soil layers during the simulation period

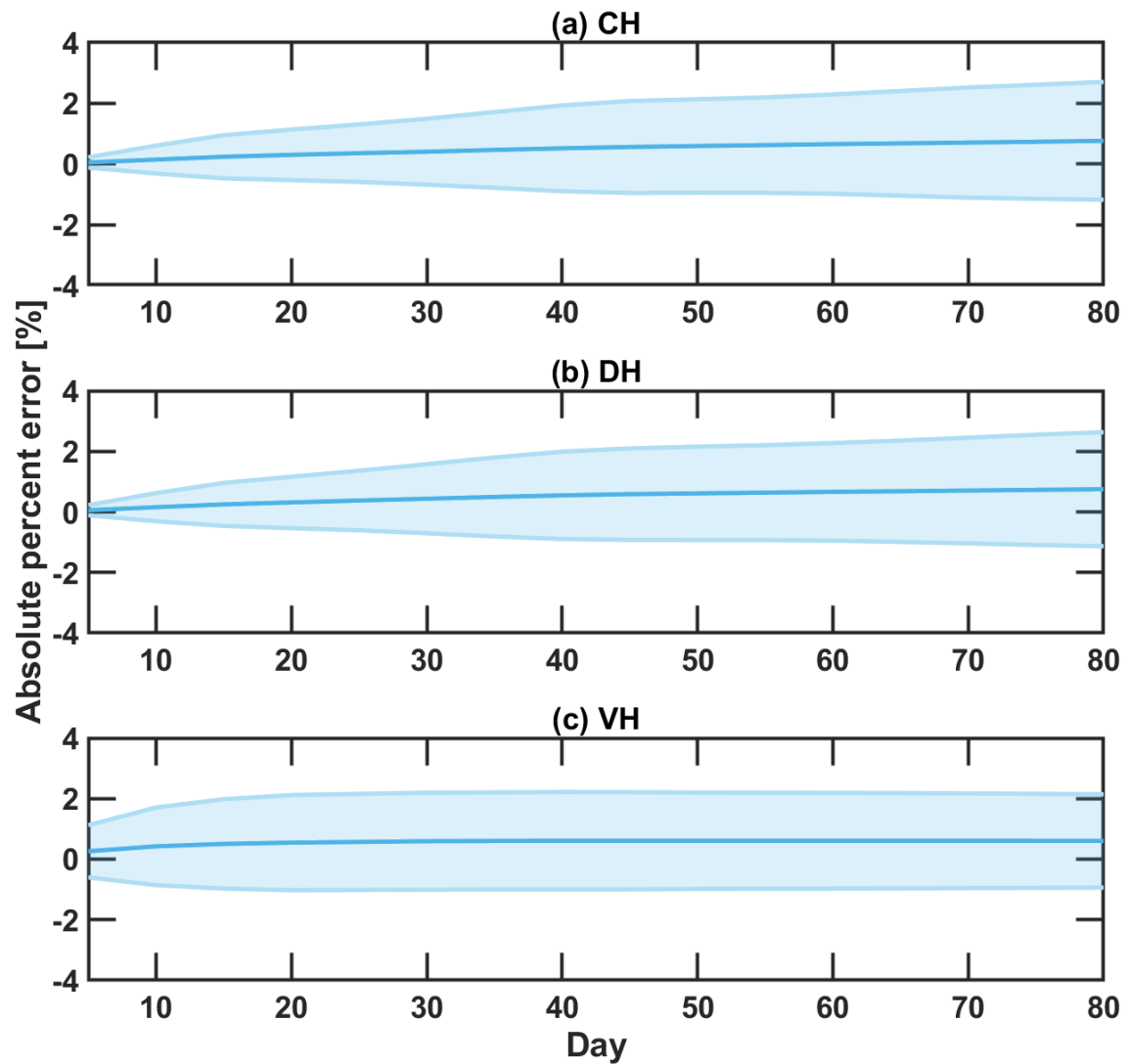


Figure A2. vertical absolute percent errors between ELM_{lat} and PFLOTRAN at the most uphill column for (a) CH, (b) DH, (c) VH and the most downhill column for (d) CH, (e) DH, (f) VH, for each layer at the 80th simulation day

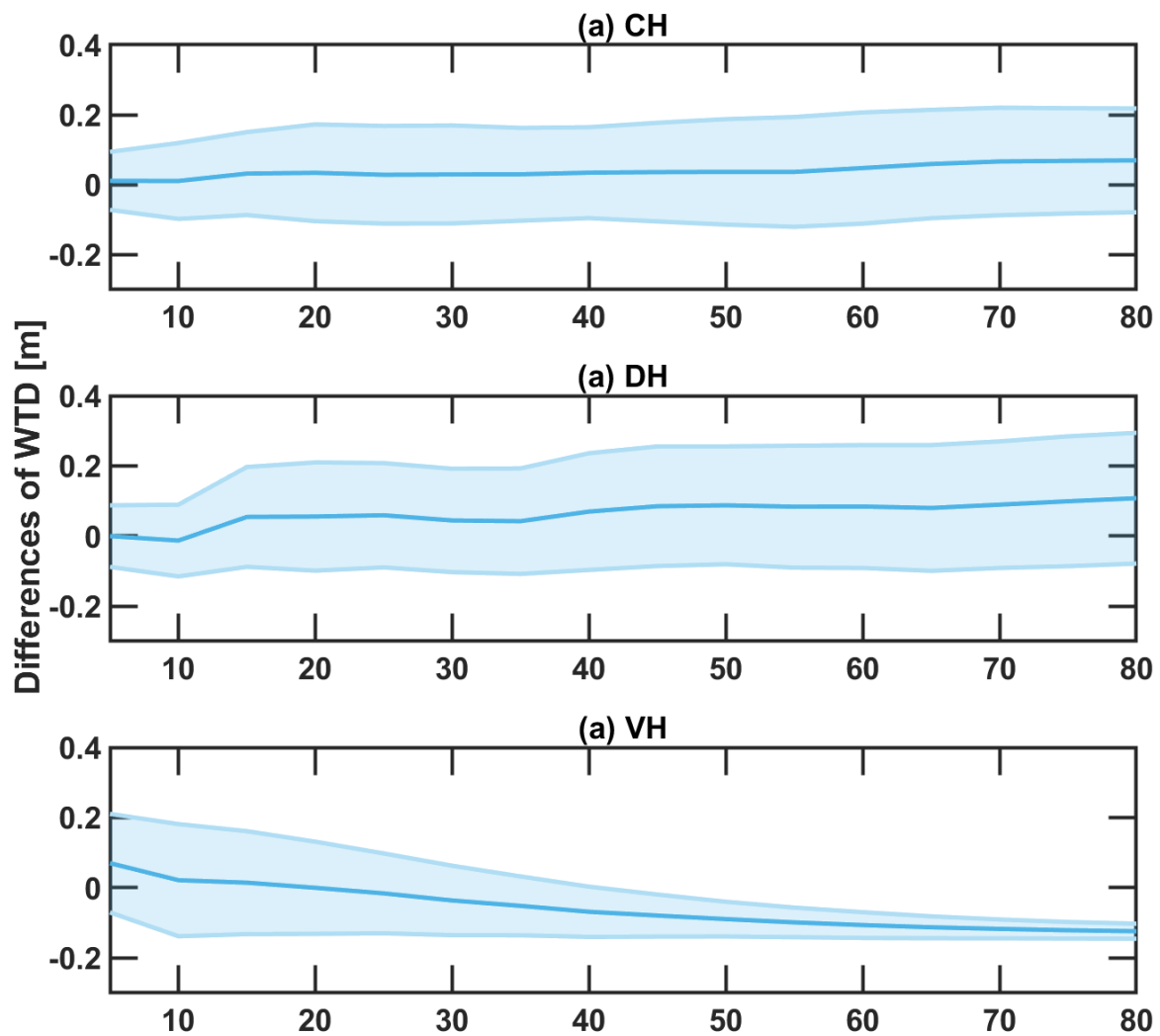


Figure A3. The differences of simulated groundwater table depths between ELM_{lat} and PFLOTRAN during the simulation period



Author contributions. HQ designed the study, developed the model, processed the data, and prepared the original manuscript. GB designed
370 the study, discussed the results, and edited the paper LL, DH, and DX processed the data, contributed to subsequent analysis, and helped
write and edit the manuscript.

Competing interests. The contact author has declared that none of the authors has any competing interests.

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375 the CompyMcNodeFace, a Department of Energy Office of Biological and Environmental Research's computer system



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