

# Characteristics of atmospheric boundary layer height over the Arctic Ocean during MOSAiC

Shijie Peng<sup>1</sup>, Qinghua Yang<sup>1</sup>, Matthew D. Shupe<sup>2,3</sup>,

Xingya Xi<sup>1</sup>, Bo Han<sup>1</sup>, Dake Chen<sup>1</sup>, Sandro Dahlke<sup>4</sup>, Changwei Liu<sup>1\*</sup>

<sup>1</sup> School of Atmospheric Sciences, Sun Yat-sen University, and Southern Marine Science and Engineering Guangdong Laboratory (Zhuhai), Zhuhai 519082, China

<sup>2</sup> Cooperative Institute for Research in Environmental Sciences, University of Colorado Boulder, Boulder, CO, USA

<sup>3</sup> NOAA Physical Science Laboratory, Boulder, CO, USA

<sup>4</sup> Helmholtz Centre for Polar and Marine Research, Alfred Wegener Institute (AWI), Potsdam, Germany

Correspondence to: Changwei Liu (liuchw8@mail.sysu.edu.cn)

## Abstract

The important roles of the atmospheric boundary layer (ABL) in the central Arctic climate system have been recognized, but the atmospheric boundary-layer height (ABLH), defined as the layer of continuous turbulence adjacent to the surface, has rarely been investigated. Using a year-round radiosonde dataset during the Multidisciplinary drifting Observatory for the Study of Arctic Climate (MOSAiC), we improve a Richardson-number-based algorithm that takes cloud effects into consideration, and analyze the characteristics and variability of ABLH over the Arctic Ocean. The results reveal that the annual cycle is clearly characterized by a distinct peak in May and two minima in January and July. This annual variation in ABLH is primarily controlled by the evolution of ABL thermal structure. Temperature inversions in the winter and summer are intensified by seasonal radiative cooling and surface melting, respectively, leading to the low ABLH at these times. Near-surface conditions (e.g., friction velocity) also play a significant role in ABLH variation, and the ABLH can be roughly estimated based on these basic variables. In addition, the MOSAiC ABLH is more suppressed than the ABLH during the Surface Heat Budget of the Arctic Ocean (SHEBA) experiment in the summer, which indicates that there is large variability in the Arctic ABL structure during summer melting season.

## 1 Introduction

In recent years, the rapidly changing climate and declining sea ice in the Arctic have been reported by numerous studies (e.g., Matveeva and Semenov, 2022; Meier and Stroeve, 2022; Esau et al., 2023). The Arctic near-surface temperature is increasing at a rate 2–3 times larger than the global average, which is referred to as Arctic amplification (Overland et al., 2019; Blunden and Arndt, 2019), and the Arctic has entered the ‘new Arctic’ period (Landrum and Holland, 2020). As a key component of the Arctic climate system, the atmospheric boundary layer (ABL) over the Arctic Ocean is closely associated with Arctic warming and has a big impact on sea ice loss (Francis and Hunter, 2006; Graversen et al., 2008; Wetzel and Bruemmer, 2011). Thus, it is critical to improve our understanding of Arctic ABL processes under ‘new Arctic’ conditions.

The ABL structure over the Arctic Ocean has unique characteristics due to the presence of semipermanent

39 sea ice, and is shaped by various mechanisms including interactions with the surface, free atmosphere, and  
40 wave activity. Most studies of the Arctic ABL structure have been based on coastal observatories and limited  
41 drifting ice stations (Knudsen et al., 2018; Vullers et al., 2021). It has been found that a predominant  
42 temperature inversion in the lower troposphere exists in all seasons and is referred to as the “Arctic inversion”  
43 (Andreas et al., 2000; Tjernström et al., 2009). The Arctic inversion is sometimes elevated, with regions of  
44 near-neutral stability below the inversion (Persson et al., 2002; Tjernström et al., 2012). The Arctic vertical  
45 structure is influenced by many factors, such as warm-air advection, surface melt, cloud-top cooling, and  
46 turbulent mixing (Busch et al., 1982; Vihma et al., 2011; Vihma, 2014). Investigations of the ABL structure  
47 evolution and its controlling factors are the keys to knowing the ABL's role in the Arctic atmosphere (Sterk  
48 et al., 2014).

49 The atmospheric boundary-layer height (ABLH), here defined as the height of continuous turbulent  
50 mixing extending up from the surface, is the key indicator of the ABL structure (Seibert et al., 2000; Seidel  
51 et al., 2012). It determines the vertical extent of many atmospheric processes, such as convective transport  
52 and aerosol distributions, and is an important parameter for weather and climate models (Holtslag et al.,  
53 2013; Mahrt, 2014; Davy and Esau, 2016). In some previous studies, the ABLH over the Arctic Ocean is  
54 defined as the height of the surfaced-based inversion top or the capping inversion base (e.g., Tjernström et  
55 al., 2009; Sotiropoulou et al., 2014). However, as the most fundamental characteristic of the ABL, turbulence  
56 is not fully considered in this definition. There are two primary layers of turbulent mixing in the Arctic  
57 atmosphere. First, the surface layer, formed by turbulent mixing processes near the surface, is frequently  
58 shallower than the Arctic inversion layer (Mahrt, 1981; Andreas et al., 2000). Second, the turbulence  
59 associated with low-level clouds, which is driven by radiative cooling near the cloud top, forms a cloud-  
60 induced mixed layer (Solomon et al., 2011; Shupe et al., 2013). This cloud-driven mixed layer is sometimes  
61 decoupled from the surface mixed layer while at other times it extends down to form a coupled, well-mixed  
62 layer all the way to the surface (Shupe et al., 2013; Brooks et al., 2017). Wind-shear induced turbulence can  
63 also play a role in both of these layers and their interactions. Based on different turbulence characteristics,  
64 the ABLH is commonly determined using profiles of potential temperature, wind speed, and humidity, and  
65 various methods have been proposed for calculating ABLH (Seibert et al., 2000; Seidel et al., 2010).  
66 However, the applicability of these methods in the Arctic needs to be further assessed.

67 Due to the lack of observations, there are few analyses of ABLH over the Arctic Ocean based on  
68 observational data. Distributions of Arctic ABLH have been investigated by Tjernström and Graversen  
69 (2009), Liang and Liu (2010), and Dai et al. (2011), but their studies are all based on the Surface Heat Budget  
70 of the Arctic Ocean (SHEBA) campaign conducted 25 years ago (Uttal et al., 2002). To improve our  
71 understanding of the ABL structure and ABLH characteristics under “new Arctic” conditions, we need new,  
72 comprehensive observations in this environment. The Multidisciplinary drifting Observatory for the Study  
73 of Arctic Climate (MOSAiC) expedition was, in part, designed to achieve this goal (Shupe et al., 2022).  
74 Based on and around a drifting research vessel in the central Arctic for a whole year, the MOSAiC expedition  
75 provided a wealth of data and related data products with unprecedented high temporal resolution and year-  
76 round temporal coverage. These data make possible a more detailed analysis of the ABL structure evolution

77 and ABLH variability.

78 In this study, based on observational data from the MOSAiC expedition, we propose an improved ABLH  
79 algorithm and then examine the characteristics of the ABL evolution over the ‘new Arctic’ sea-ice surface.  
80 This paper is organized as follows: Section 2 briefly describes the MOSAiC expedition and the observations;  
81 section 3 provides an ABLH determination method to evaluate several automated algorithms, and develops  
82 an improved ABLH algorithm; section 4 presents the results of ABLH variation over the annual cycle, the  
83 controlling factors of ABLH variation, and mechanisms of ABL development and suppression; section 5  
84 compares the difference in ABLHs between SHEBA and MOSAiC; and conclusions are given in section 6.

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## 86 **2 Measurements**

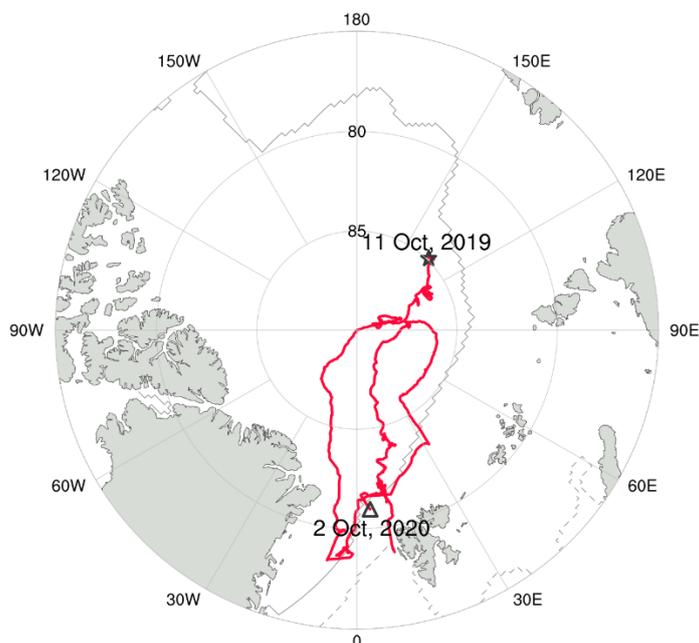
87 In this study, the SHEBA-based sounding data (Moritz, 2017) and multiple MOSAiC data are used. Here  
88 we mainly introduce the MOSAiC expedition. The MOSAiC track is shown in Fig. 1, which is based on the  
89 research vessel *Polarstern* (Knust, 2017), with the main period of atmospheric state observations starting in  
90 October 2019 and ending in September 2020. *Polarstern* drifted across the central Arctic Ocean and  
91 navigated through the sea ice north of 78° N during most of the MOSAiC year. The whole drifting period is  
92 divided into five parts, and the vessel sailed in the gap period between some of those parts. More details are  
93 provided in Shupe et al. (2022). The following are the descriptions of the instruments and data products used  
94 in this paper.

95

### 96 **2.1 Radiosonde observations and relevant data products**

97 The radiosonde data were obtained through a partnership between the leading Alfred Wegener Institute  
98 (AWI), the atmospheric radiation measurement (ARM) user facility, a US Department of Energy facility  
99 managed by the Biological and Environmental Research Program, and the German Weather Service (DWD)  
100 (Maturilli et al., 2022). Vaisala RS41-SGP Radiosondes were regularly launched on board throughout the  
101 whole MOSAiC year (from October 2019 to September 2020), including periods when the vessel was in  
102 transit. The sounding frequency is normally four times per day (launched at about 5:00, 11:00, 17:00, and  
103 23:00 UTC) and is increased to 7 times per day during periods of exceptional weather or coordination with  
104 other observing activities. The radiosoundings provide data on the atmospheric state, including vertical  
105 profiles of pressure, temperature, relative humidity (*RH*), and winds, from 12 m up to 30 km with a vertical  
106 resolution of 5 m. However, the sounding data below ~100 m altitude may be contaminated by the vessel  
107 itself. To avoid contamination affecting our analysis, we use a merged data product that combines the  
108 soundings with measurements from a meteorological tower on the sea ice away from the vessel, and was  
109 specifically designed to minimize ship effects and provide more reliable profiles in the lowest 100 m, which  
110 has been recently submitted (Dahlke et al., 2023). In this paper, data quality control and a six-point moving  
111 average in height are applied to the merged profile data to eliminate invalid data and measurement noise,  
112 and all data are interpolated onto a regular vertical grid with 10 m intervals. In total, there are 1484 sounding  
113 profiles available. In addition, DOE-ARM provides a Planetary Boundary Layer Height Value-Added  
114 Product (PBLHT VAP, Riihimaki et al., 2019), which uses several different automated algorithms to compute

115 ABLH estimates based on radiosonde profiles. This VAP provides 964 ABLH estimates, and we select 914  
116 samples from these to ensure that the estimates obtained by all algorithms are available.



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118 Figure 1 The MOSAiC expedition track from (star) 11 October 2019 through to (triangle) 2 October 2020 is  
119 plotted by the red line. Gray solid and dashed lines denote the approximate sea ice edge at the minimum (15  
120 September 2020) and the maximum (5 March 2020), respectively.

## 122 2.2 Meteorological and turbulence measurements near the surface

123 Meteorological and turbulence measurements were made from a tower on the sea ice at “Met City”,  
124 which was located 300–600 m away from the vessel (Cox et al., 2023). The u-Sonic-3 Cage MP anemometers  
125 by METEK GmbH and HMT300 air temperature sensors by Vaisala were fixed at nominal heights of 2 m, 6  
126 m, and 10 m on the meteorological tower. The tower was set up during the periods when the vessel passively  
127 drifted with an ice floe (i.e., from mid-October 2019 to mid-May 2020, from mid-June through July 2020,  
128 and from late August to mid-September 2020). The sampling frequency of fast response instruments (i.e., u-  
129 Sonic-3 Cage MP anemometer) was at 20 Hz, resampled to 10 Hz. To derive turbulence parameters, the  
130 following processes were carried out: despiking, block averaging over a 10-min interval, coordinate rotating  
131 via double rotation, frequency correcting, and virtual temperature correcting. In this study, sensible heat flux  
132 ( $SH$ , defined as positive upwards), near-surface air temperature at 2 m, friction velocity, and turbulent kinetic  
133 energy (TKE) dissipation rate are used. Based on a footprint analysis using the Kljun et al. (2015) model,  
134 90% of the sensible heat flux measurements have a source area fetch of no more than 275 m, a region that  
135 was typically strongly dominated by consistent sea ice throughout the year. Although the sounding site may  
136 typically be outside the source region of these flux measurements, we assume the conditions at the two sites  
137 are predominantly equivalent, which is also assumed in the merged sounding-tower product.

## 139 2.3 Cloud properties derived from combined sensors

140 Cloud-related measurements come from ShupeTurner cloud microphysics product (Shupe, 2022). This  
 141 product uses multiple measurement sources (e.g., cloud radar, ceilometer, depolarization lidar, and  
 142 microwave radiometer) to derive time-height data, including cloud phase type and condensed water content  
 143 for both liquid and ice. Details of the retrieval algorithm, its application, and uncertainties are provided in  
 144 Shupe et al. (2015). In our study, the condensed water content data are linearly interpolated onto the vertical  
 145 grid with resolution of 10 m for consistency. The cloud phase type data are used to determine clear and  
 146 cloudy environments. A grid point is labeled as “cloudy” if clouds are identified in the upper and lower cloud  
 147 phase type data points adjacent to the grid, otherwise it is labeled as “clear”.

### 148 **3 ABLH determination method and algorithm evaluation**

150 The most objective method of ABLH determination is based on profiles of turbulence measurements  
 151 deployed on aircraft or other platforms, but such measurements were not routinely carried out during the  
 152 MOSAiC expedition. Thus, the ABLH determination in our study is based on the thermal and dynamic  
 153 structure of radiosoundings. In previous literature, the ABLH is determined through multiple profiles of  
 154 atmospheric variables and manual visual inspection, which can be considered as the “observed” ABLH  
 155 (Liang and Liu, 2010; Zhang et al., 2014; Jozef et al., 2022). In this section, we will describe the manually-  
 156 labeled ABLH determination method and derive an ABLH for each sounding. Next, we will use these ABLHs  
 157 as a reference to evaluate the automated ABLH algorithms provided by the PBLHT VAP. Finally, we will  
 158 develop and evaluate an improved ABLH automated algorithm that is suitable for the Arctic atmosphere,  
 159 and further discuss an important parameter for the algorithms and its stability dependence.

#### 160 **3.1 ABL regime classification and ABLH determination**

162 The ABLH determination method starts with the classification of ABL regimes. Based on previous  
 163 studies (e.g., Vogelesang and Holtslag, 1996; Liang and Liu, 2010), we divide the ABLs into three types:  
 164 stable boundary layer (SBL), near-neutral boundary layer (NBL), and convective boundary layer (CBL),  
 165 corresponding with three different stability states near the surface. We first use  $SH$  to diagnose the ABL  
 166 regime types. The specific classification formula is presented below:

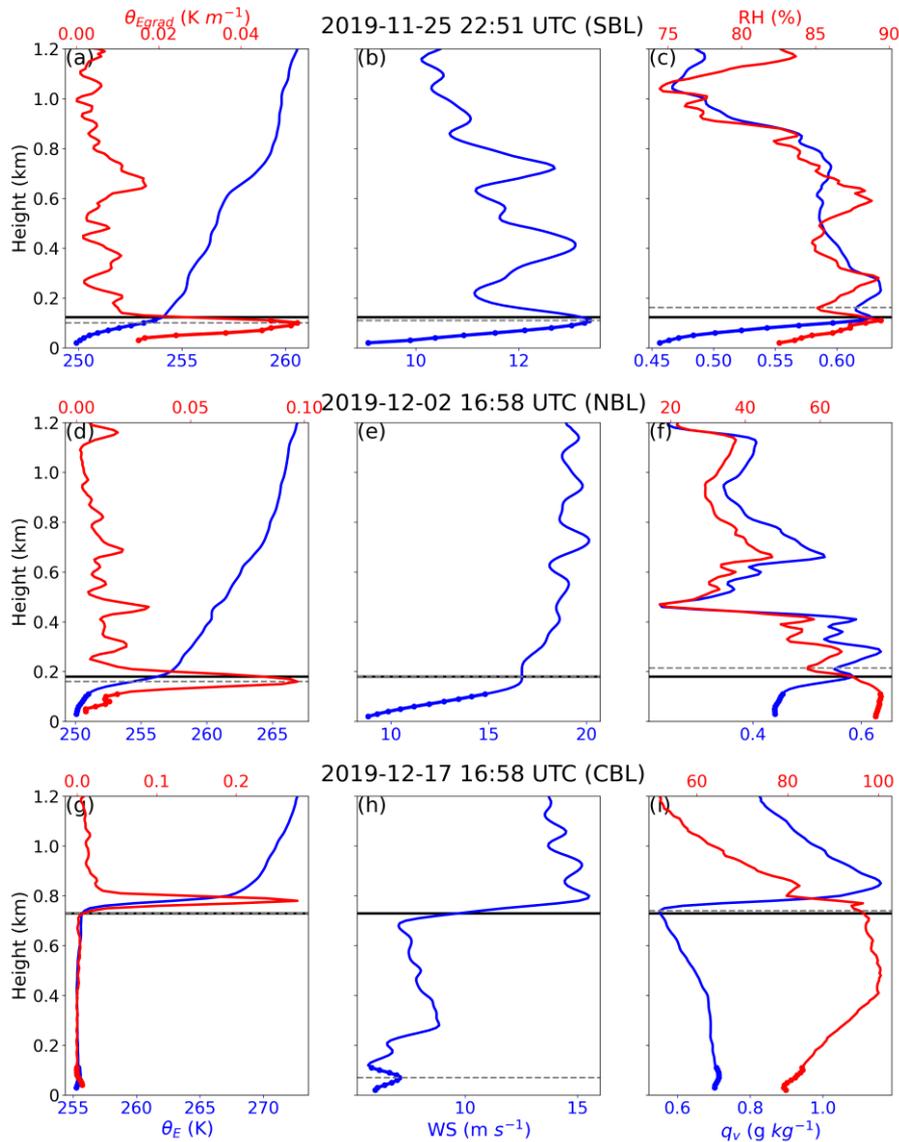
$$167 \begin{cases} SH > +\delta & \text{for CBL} \\ SH < -\delta & \text{for SBL, (1)} \\ \text{else} & \text{for NBL} \end{cases}$$

168 where  $\delta$  is the critical value that is specified as  $2 \text{ W m}^{-2}$ , following Steeneveld et al. (2007b). If corresponding  
 169  $SH$  data are unavailable, the difference of equivalent potential temperature ( $\theta_E$ ) between the 100 and 50 m  
 170 heights ( $\theta_E$  difference) derived from the sounding profile is used to determine the ABL type. Specifically, if  
 171  $\theta_E$  difference is larger than 0.2 K, the ABL is identified as SBL; if  $\theta_E$  difference is less than -0.2 K, the ABL  
 172 is identified as CBL; and other profiles are labeled as NBLs, roughly following Liu and Liang (2010).

173 The manually-labeled ABLH determination in our study is based on characteristics of sounding profiles  
 174 and regime types. For each atmospheric sounding profile, equivalent potential temperature ( $\theta_E$ ), equivalent  
 175 potential temperature gradient ( $\theta_{Egrad}$ ), wind speed ( $WS$ ), specific humidity ( $q_v$ ), and  $RH$  are used to obtain  
 176 multiple estimates of the ABLH, which are used to determine the final estimate. Three cases to describe the

177 method are presented in Fig. 2. Figures 2 (a–c) are the case of a SBL, which features surface-based  
178 temperature and humidity inversions. Figures 2 (d–f) are the case of a NBL, with approximately constant  $\theta_E$   
179 from the surface up to the inversion base and strong horizontal wind. Figures 2 (g–i) are the case of a CBL,  
180 with a deeper well-mixed layer and low-level cloud coupled to the surface (e.g., Shupe et al., 2013). In terms  
181 of  $\theta_E$  profiles, the estimated ABLH is the level at which the  $\theta_{Egrad}$  reaches its maximum for SBL and NBL  
182 cases, and the base of the  $\theta_E$  inversion for CBL cases (Martucci et al., 2007). In terms of  $WS$  profiles, the  
183 ABLH is estimated to be the height of the  $WS$  maximum for all three regime types (Mahrt et al., 1979). In  
184 terms of humidity profiles, the estimated ABLH is the level at which the  $RH$  rapidly decreases for SBL and  
185 NBL cases, and the base of the  $q_v$  inversion for CBL cases (Lenschow et al., 2000). The manually-observed  
186 ABLHs (solid black lines in Fig. 2) are then determined through consideration of these three distinct  
187 estimates using the following rules: (1) If the estimates differ slightly from each other, take the average of  
188 these estimates as ABLH; (2) If a strong characteristic (sharp gradients or peaks) of the profile is evident,  
189 select the estimate obtained based on this characteristic; (3) If the ABL structure is similar to that at the  
190 previous time, select the estimate with the smallest change to ensure that ABLHs are consistent in time. It is  
191 evident that the lowest layers of profiles have a great impact on the ABLH determination, particularly for  
192 shallow SBLs and NBLs. Thus, the merged radiosonde-tower profiles help make the ABLH determination  
193 more reliable than when using radiosondes alone.

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### 3.2 Automated algorithm evaluation

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Figure 2 Vertical profiles of (left) equivalent potential temperature ( $\theta_E$ ),  $\theta_E$  gradients ( $\theta_{Egrad}$ ), (middle) wind speed ( $WS$ ), and (right) relative humidity ( $RH$ ) and specific humidity ( $q_v$ ) at (a–c) 25 November 2019, 22:51 UTC, (d–f) 2 December 2019, 16:58 UTC, and (g–i) 17 December 2019 16:58 UTC. Boundary layers at the three times represent stable boundary layer (SBL), near-neutral boundary layer (NBL), and convective boundary layer (CBL), respectively. The gray dashed horizontal lines denote the atmospheric boundary-layer height (ABLH) estimates based on multiple profiles, and the black solid horizontal lines denote the manually observed ABLHs. The dots in the lowest 100 m denote the section of the profiles impacted by the radiosonde-tower merging.

The automated ABLH algorithms consist of various empirical formulas. Based on these empirical formulas, estimated ABLHs are determined automatically and without manual intervention. Therefore, these algorithms can perform real-time and fast calculations on large amounts of data and are widely used in model simulations (Seibert et al., 2000; Konor et al., 2009). However, automated algorithms might lead to large

210 errors in estimating ABLHs, and the parameter selection in these algorithms will have a great impact on the  
 211 results. In our study, estimated ABLHs obtained using three automated algorithms are compared with  
 212 manually-labeled ABLHs to evaluate their performance over the Arctic Ocean. These algorithms, including  
 213 the Liu-Liang algorithm, the Heffter algorithm, and the bulk Richardson number algorithm, are all available  
 214 in the PBLH VAP as described in Sivaraman et al. (2013). Here we give a brief description of the three  
 215 algorithms.

216 The Liu-Liang algorithm determines ABLH based on potential temperature and wind speed according to  
 217 Liang and Liu (2010). For CBL regimes, the definition of ABLH is the height at “which an air parcel rising  
 218 adiabatically from the surface becomes neutrally buoyant”, and the temperature excess value is 0.1 K. For  
 219 SBL regimes, two different estimates of the ABLH are obtained, if possible, based on stability criteria and  
 220 wind shear criteria, respectively. For stability, the ABLH is defined as the lowest level,  $k$ , at which the  $\theta_{Egrad}$   
 221 reaches a minimum and meets either of the following two conditions:

$$222 \quad \begin{cases} \theta_{Egrad\ k} - \theta_{Egrad\ k-1} < -40 \text{ K/km} \\ \theta_{Egrad\ k+1} < 0.5 \text{ K/km}, \theta_{Egrad\ k+2} < 0.5 \text{ K/km} \end{cases}, (2)$$

223 where the subscripts ( $k$ ,  $k-1$ ,  $k+1$ , and  $k+2$ ) represent the  $\theta_{Egrad}$  at corresponding levels. For wind shear, the  
 224 ABLH is defined as the height where the wind speed reaches a maximum that is at least 2 m/s stronger than  
 225 the layers immediately above and below while decreasing monotonically toward the surface (i.e., a low-level  
 226 jet). The final ABLH is defined as the lower of the two heights.

227 The Heffter algorithm, which was suggested by Heffter (1980), is a widely used algorithm (e.g., Marsik  
 228 et al., 1995; Snyder and Strawbridge, 2004). The algorithm determines ABLH through the strength of the  
 229 inversion and potential temperature difference across the inversion. The ABLH is defined as the lowest layer  
 230 in which the potential temperature difference between the top and bottom of the inversion is greater than 2  
 231 K. If no layer meets the criteria, the ABLH is defined as the layer at which the potential temperature gradient  
 232 reaches the largest maximum.

233 The bulk Richardson number algorithm is based on the profile of the bulk Richardson number ( $Ri_b$ ), and  
 234 has been shown to be a reliable algorithm for determining ABLHs (Seidel et al., 2012).  $Ri_b$  is a dimensionless  
 235 number that represents the ratio of thermally produced turbulence to that induced by mechanical shear. The  
 236  $Ri_b$  formula used in the PBLH VAP (Sørensen et al., 1998; Sivaraman et al., 2013) is expressed as:

$$237 \quad Ri_b = \left( \frac{gh}{\theta_{v0}} \right) \left( \frac{\theta_{vh} - \theta_{v0}}{u_h^2 + v_h^2} \right), (3)$$

238 where  $g$  is the acceleration of gravity;  $\theta_{vh}$  and  $\theta_{v0}$  are the virtual potential temperature at height  $h$  and the  
 239 surface, respectively;  $u_h$  and  $v_h$  are the horizontal wind speed component at height  $h$ . The ABLH is defined  
 240 as the height of  $Ri_b$  exceeding a critical threshold (the critical bulk Richardson number,  $Ri_{bc}$ ; Seibert et al.,  
 241 2000). The PBLH VAP includes ABLH estimates based on two widely used  $Ri_{bc}$  values: 0.25 and 0.5.

242 To quantitatively evaluate the performance of each automatic algorithm, we introduce the correlation  
 243 coefficient  $R$  and two other statistical measures: the *Bias* and the median absolute error (*MEAE*; Steeneveld  
 244 et al., 2007a). The formulas are as follows:

$$245 \quad Bias = \frac{2}{n} \sum_{i=1}^n \frac{H_{auto} - H_{obs}}{H_{auto} + H_{obs}}, (4)$$

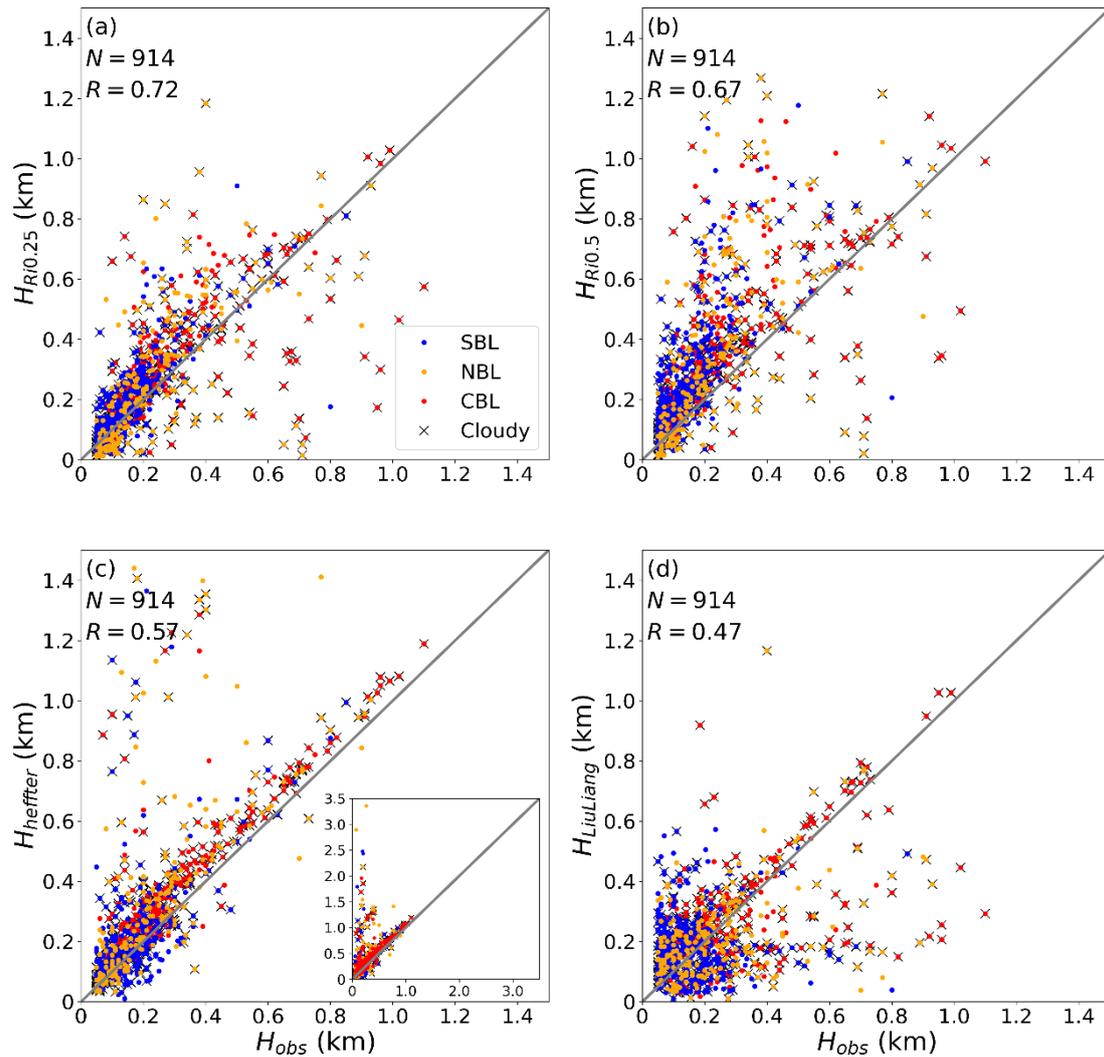
246 
$$MEAE = \text{median}(|H_{auto} - H_{obs}|), (5)$$

247 where  $H_{auto}$  is the ABLH obtained by the automated algorithm;  $H_{obs}$  is the ABLH manually determined;  $n$  is  
248 the number of valid sounding profile samples. According to the definitions of these statistical measures,  
249 larger  $R$  and smaller  $Bias$  and MEAE mean a better performance of the automated algorithm.

250 We also analyze the algorithm performances for cloudy and clear conditions, considering that low-level  
251 clouds containing liquid water play an important role in the Arctic ABL (Shupe and Intrieri, 2004; Brooks et  
252 al., 2017). In our study, the  $RH$  threshold of 96% (Silber and Shupe, 2022) and the cloud source flag data are  
253 used for cloud detection. If a cloud is detected in the cloud source flag data and the  $RH$  is larger than 96%,  
254 then the profile is labeled as cloudy. The sounding profiles that contain at least one identified cloud layer  
255 below 1500 m are classified as “cloudy”, and as “clear” otherwise.

256 Figure 3 presents the comparisons of estimated ABLHs with the manually-labeled ABLHs, and the  
257 associated statistical measures are given in Table 1. The results show that the  $Ri_b$  algorithm with  $Ri_{bc}$  of 0.25  
258 performs best overall, and particularly for SBL cases. The performance of the  $Ri_b$  algorithm with  $Ri_{bc}$  of 0.5  
259 is poorer than that of the  $Ri_b$  algorithm with  $Ri_{bc}$  of 0.25, with overestimations of ABLHs in general, and  
260 larger errors with lower correlation coefficients for all types of ABLs. The Heffter algorithm performs well  
261 in cases of high ABLH and particularly for cloudy and CBL cases, but does significantly overestimate ABLH  
262 in a large number of cases as shown in the Fig. 3c subgraph. This is attributed to the determination criterion  
263 of the Heffter algorithm, i.e., ABLHs are determined by inversion layers, which means that large errors occur  
264 when the inversion layer is higher than the mixed layer. Additionally, while the Heffter performance in many  
265 of the ABL conditions is only marginally worse statistically than the  $Ri_b$  algorithm with  $Ri_{bc}$  of 0.25, its  
266 correlations are notably worse for SBL and NBL cases. The performance of the Liu-Liang algorithm is  
267 generally poorer than the other algorithms, particularly for correlation coefficient, which is probably due to  
268 the impact of noise in the lower ABLH profiles and unsuitable parameters in the algorithm. In summary, the  
269  $Ri_b$  algorithm is reliable over the Arctic Ocean and performs better than other algorithms, and this result  
270 agrees with Jozef et al. (2022). Furthermore, we will explore ways to improve the  $Ri_b$  algorithm to make it  
271 more suitable for cloudy and convective conditions.

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 274 Figure 3 Comparisons of the ABLHs determined from radiosonde profiles using the bulk Richardson number  
 275 ( $Ri_b$ ) algorithm with the critical values ( $Ri_{bc}$ ) of (a) 0.25 and (b) 0.5, (c) the Heffter algorithm, and (d) the  
 276 Liu-Liang algorithm with the manually-identified "observed" ABLHs. The blue, yellow, and red colors  
 277 indicate regime types of SBL, NBL, and CBL, respectively. The "x" signs indicate the Cloudy ABLs. The  
 278 case numbers ( $N$ ) and correlation coefficients ( $R$ ) are given in each panel. The subgraph in (c) denotes all  
 279 data points ranging from 0 to 3.5 km.

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289 Table 1 The statistical measures ( $R$ ,  $Bias$ ,  $MEAE$ ) for the four algorithms applied to the radiosonde dataset.  
 290 All correlation coefficients are statistically significant ( $p < 0.05$ ), except for SBL types in the Liu-Liang  
 291 algorithm.

Algorithm	Regime type	$R$	Bias	MEAE (m)
<b>The <math>Ri_b</math> algorithm with <math>Ri_{bc} = 0.25</math></b>	ALL	0.72	0.10	50
	SBL	0.81	0.16	34
	NBL	0.68	-0.04	62
	CBL	0.65	0.15	71
	Cloudy	0.69	0.08	51
<b>The <math>Ri_b</math> algorithm with <math>Ri_{bc} = 0.5</math></b>	ALL	0.67	0.40	97
	SBL	0.73	0.50	88
	NBL	0.61	0.23	91
	CBL	0.60	0.39	120
	Cloudy	0.66	0.36	94
<b>The Heffter algorithm</b>	ALL	0.57	0.23	53
	SBL	0.46	0.17	33
	NBL	0.45	0.30	59
	CBL	0.66	0.28	74
	Cloudy	0.68	0.25	59
<b>The Liu-Liang algorithm</b>	ALL	0.47	0.04	82
	SBL	0.05	0.15	90
	NBL	0.44	-0.07	81
	CBL	0.56	-0.05	69
	Cloudy	0.52	-0.01	82
<b>The improved <math>Ri</math> algorithm with <math>Ri_{bc} = 0.35</math></b>	ALL	0.85	-0.06	29
	SBL	0.79	-0.08	21
	NBL	0.79	-0.18	35
	CBL	0.87	0.05	36
	Cloudy	0.86	-0.03	30

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### 3.3 An improved $Ri$ algorithm considering the cloud effect

295 As a traditional  $Ri_b$  formula, Eq. (3) may break down in cases of ABLs with relatively high wind speed  
 296 and upper-level stratification due to the overestimation of shear production (Kim and Mahrt, 1992).  
 297 Vogelezang and Holtslag (1996) proposed a finite-difference  $Ri$  formula, which is expressed as:

$$298 Ri_F = \frac{(g/\theta_{vs})(\theta_{vh}-\theta_{vs})(h-z_s)}{(u_h-u_s)^2+(v_h-v_s)^2+bu_*^2}, \quad (6)$$

299 where  $z_s$  is the lower boundary for the ABL,  $\theta_{vs}$ ,  $u_s$ , and  $v_s$  are the  $\theta_v$  and wind components at the height  $z_s$ ,  
 300 respectively,  $b$  is an empirical coefficient, and  $u_*$  is the surface friction velocity.  $Ri_F$  is considered for a parcel  
 301 located somewhat above the surface to avoid the above problem, and  $u_*$  is also taken into account to avoid  
 302 underestimation in the situation of a uniform wind profile in the upper layer. Here, we use  $Ri_F$  for clear-sky  
 303 profiles and take  $z_s$  and  $b$  values as 40 m and 100, respectively, according to Zhang et al. (2020).

304 As shown in Fig. 3, the estimations of cloudy ABLHs are sometimes quite poor, which motivates us to further  
 305 improve the algorithm. Under cloudy conditions, the moist Richardson number ( $Ri_m$ ) can be used to include  
 306 cloud effects on the buoyancy term. Brooks et al. (2017) adopted the  $Ri_m$  formula expressed as:

$$307 Ri_m = \frac{\left(\frac{g}{T}\right) \left(\frac{dT}{dz} + \Gamma_m\right) \left(1 + \frac{Lq_s}{RT}\right) - \frac{g}{1+q_w} \frac{dq_w}{dz}}{\frac{du^2}{dz} + \frac{dv^2}{dz}}, \quad (7)$$

308 where  $T$  is air temperature,  $\Gamma_m$  is the moist adiabatic lapse rate,  $L$  is the latent heat of vaporization,  $q_s$  is the

309 saturation mixing ratio, and  $q_w$  is the total water mixing ratio, i.e.,  $q_w = q_s + q_L$ , where  $q_L$  is the liquid water  
 310 mixing ratio and is obtained based on the condensed water content. However, Eq. (6) is a gradient  $Ri$  and is  
 311 calculated based on local gradients of wind speed, temperature, and humidity. To be consistent with the  $Ri$   
 312 formula proposed by Vogelezang and Holtslag (1996), we rewrite the formula in a finite-difference form  
 313 expressed as:

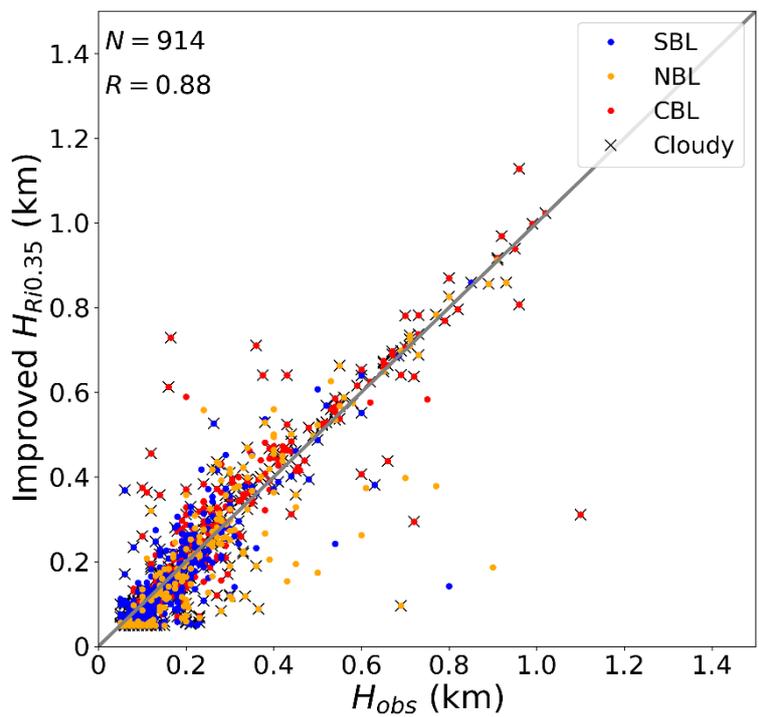
$$314 \quad Ri_m = \frac{\left[ (g/T_s) \left( \frac{T_h - T_s}{h - z_s} + \Gamma_m \right) \left( 1 + \frac{Lq_{sh}}{RT_h} \right) - \frac{g}{1 + q_{wh}} \frac{q_{wh} - q_{ws}}{h - z_s} \right] (h - z_s)^2}{(u_h - u_s)^2 + (v_h - v_s)^2 + bu_*^2}, \quad (8)$$

315 where subscripts ( $h$  and  $s$ ) of the variables denote the calculated height, similar to Eq. (6), but note that the  
 316  $s$  and  $z_s$  are adjusted to 130 m, given the cloud radar blind zone. Considering that  $Ri_m$  is only appropriate for  
 317 the liquid-bearing cloud cases, we use the  $Ri_F$  for “clear” grid points and use  $Ri_m$  for “cloudy” grid cells.  
 318 Using this improved approach, we evaluated the best value of  $Ri_c$  to minimize the errors compared to the  
 319 reference data set, arriving at an optimal value of  $Ri_c = 0.35$ . The comparison of ABLH estimates obtained  
 320 through the improved  $Ri$  algorithm with the manually-labeled ABLHs demonstrates significant improvement  
 321 relative to other algorithms, particularly for cloudy conditions (Fig. 4, Table 1).

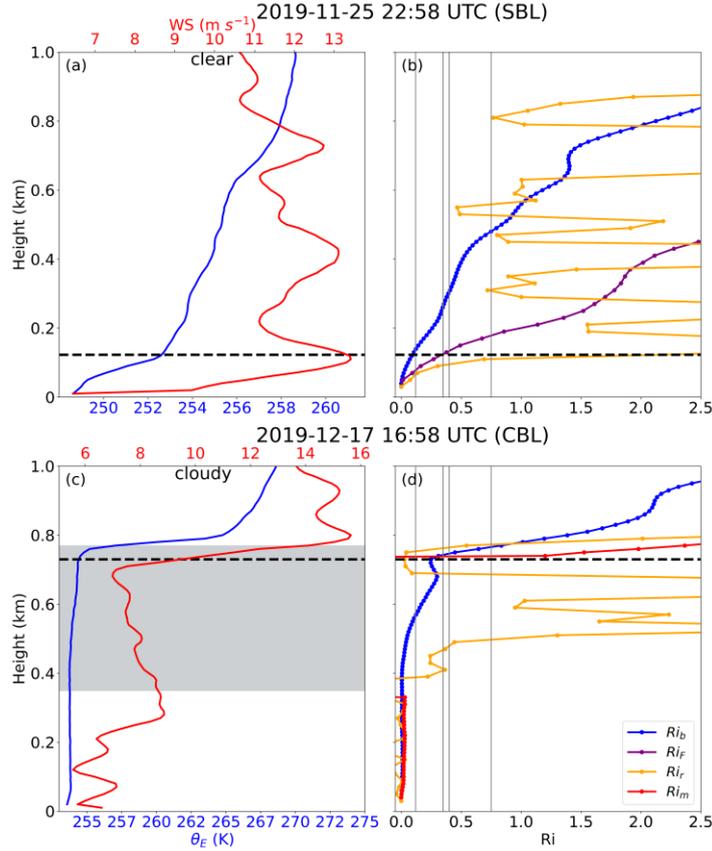
322 Since some other studies have proposed different  $Ri_c$  values for MOSAiC (e.g., Jozef et al., 2022; Barten  
 323 et al., 2023; Akansu et al., 2023), we will discuss the difference in  $Ri_c$  values here. The first thing to make  
 324 clear is that these studies use different formulas to obtain  $Ri$  profiles. Barten et al. (2023) and Akansu et al.  
 325 (2023) both use the traditional  $Ri_b$  algorithm based on Eq. (3), while they used  $Ri_c$  values of 0.4 and 0.12,  
 326 respectively. This difference was likely caused by the different methods to manually derive their reference  
 327 ABLH data sets. Jozef et al. (2022) calculates the  $Ri$  over a rolling 30 m altitude range, labeled as  $Ri_r$ , and  
 328 the criterion is modified to require four consecutive data points to be above the  $Ri_c$  of 0.75. In our study, we  
 329 use  $Ri_F$  proposed by Vogelezang and Holtslag (1996) for clear-sky conditions, and  $Ri_m$  for cloudy conditions.  
 330 Based on the results presented here, it is apparent that this more complex approach improves the error  
 331 statistics relative to approaches based on Eq. (3), regardless of  $Ri_c$ . In addition, some of the differences may  
 332 also related to authors using different data sets or time periods. For instance, Akansu et al. (2023) primarily  
 333 used sounding data based on tether balloon for a specific sub-period of MOSAiC, and Jozef et al. (2022)  
 334 used radiosondes from when they had concurrent UAV observations. The data used in our study are based  
 335 on merged sounding-tower product, as mentioned above.

336 To further explore the differences among the four different approaches, we examine one SBL and CBL  
 337 case. For a clear-sky SBL case (Fig. 5 a, b), the approaches from Akansu et al., Jozef et al. (2022), and this  
 338 study all agree closely with the manual ABLH, while the Barten et al. approach results in a significant  
 339 overestimation. For a cloudy-sky CBL case (Fig. 5 c, d), the approach from this study agrees with the manual  
 340 ABLH, while the approach from Barten et al. overestimates the ABLH by about 30 m, and the approaches  
 341 from Akansu et al. and Jozef et al. (2022) underestimate the ABLH by 130 m and 230 m, respectively. These  
 342 results further demonstrate how  $Ri_c$  depends on the choice of  $Ri$  formula. Moreover,  $Ri_c$  is not analytically  
 343 derived from basic physical principles (Zilitinkevich et al. 2007), and the concept of  $Ri_c$  is challenged by  
 344 non-steady regimes (Zilitinkevich and Baklanov, 2002) and the hysteresis phenomenon (Banta et al., 2003;

345 Tjernström et al., 2009). Therefore, an objective  $Ri_c$  does not exist. Rather, it is empirically used as an  
346 algorithmic parameter to simply derive the ABLH.  
347



348  
349 Figure 4 Similar to Fig. 3, but for the comparison of the ABLHs determined by the improved  $Ri$  algorithm  
350 with the observed ABLHs. The case number ( $N$ ) and correlation coefficient ( $R$ ) are given.  
351



352

353 Figure 5 Vertical profiles of (left)  $\theta_E$  and wind speed, and (right)  $Ri$  based on different formulas at (a–b) 25  
 354 November 2019, 22:58 UTC and (c–d) 17 December 2019, 16:58 UTC. Boundary layers at the two times  
 355 represent a clear-sky SBL and a cloudy-sky CBL respectively. The black dashed horizontal lines denote the  
 356 manually-identified ABLH, and the gray solid vertical lines denote the different  $Ri_c$  values, including 0.12,  
 357 0.35, 0.4, and 0.75. The gray shading in (c) denotes the cloud layer.

358

### 359 3.4 The stability dependence of critical Richardson number

360 Richardson et al. (2013) and Basu et al. (2014) suggested that there is a stability dependence of  $Ri_c$  in  
 361 stable conditions, which is different from the constant  $Ri_c = 0.35$  used in our improved algorithm. In this  
 362 section, we will discuss the impact of this dependence on ABLH estimation. We use the improved  $Ri$   
 363 algorithm to calculate the  $Ri$  at the manually-labeled ABLH ( $h$ ). This new parameter is named  $Ri_h$  to  
 364 distinguish it from the constant  $Ri_c$ . To be consistent with Basu et al. (2014), the bulk stability parameter  $h/L$   
 365 is used for our analysis, where  $L$  is the Obukhov length. Based on these two variables, the stability  
 366 dependence can be expressed as:

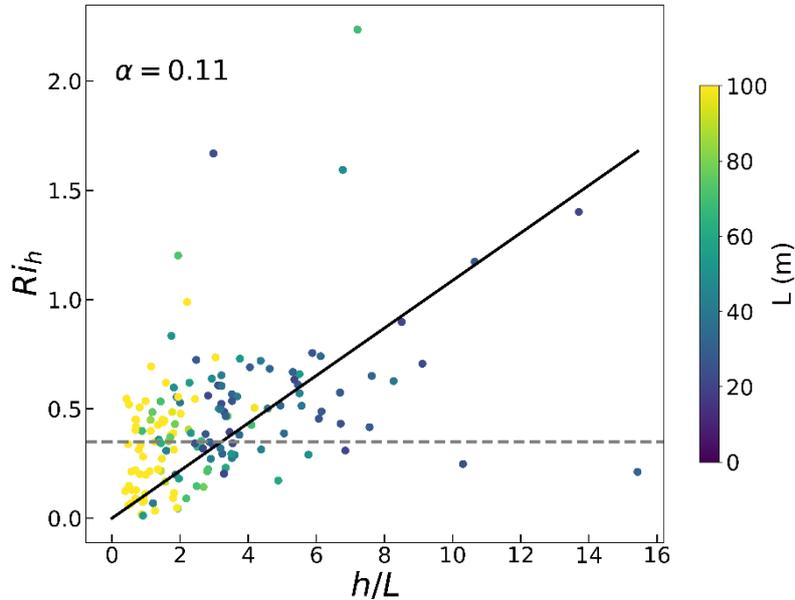
$$367 Ri_h = \alpha \frac{h}{L}, \quad (9)$$

368 where  $\alpha$  is a proportionality constant. As suggested in Basu et al. (2014), the data for convective, near-neutral,  
 369 and very stable conditions are excluded to obtain a credible  $\alpha$ . Specifically, data points that meet the  
 370 thresholds ( $L > 500$  m and  $L < L_{min}$ ) are excluded in our analysis, where the  $L_{min}$  corresponds to the heat flux  
 371 minimum (Basu et al. 2008) and is assumed as 20 m here. Finally, we select 168 samples. The  $Ri_h$  plotted as

372 a function of  $h/L$  for these selected data is presented in Fig. 6, and the value of  $L$  is colored to probe if the  
 373 dependence is simply due to self-correlation. The results show  $Ri_h$  values that mostly range from 0 to 0.75,  
 374 and the best-fit line indicates an overall positive correlation trend, with  $\alpha = 0.11$ . The  $\alpha$  value is somewhat  
 375 larger than the results in Richardson et al. (2013) and Basu et al. (2014), which is attributed to the different  
 376  $Ri$  algorithm used in our study. In addition, if a few of the extreme points are removed, the bulk of the data  
 377 does not show a strong  $h/L$  dependence and is instead fairly well represented by a constant  $Ri_h = 0.35$ , which  
 378 is also suitable for convective conditions (e.g., Fig. 5c, d).

379 In summary, we assess the stability dependence of  $Ri_c$  based on our improved  $Ri$  algorithm, and the  
 380 results present an overall positive correlation trend. However, this type of stability dependence of  $Ri_c$  is  
 381 challenged to be used in practical applications because the sensitivity of  $\alpha$  to surface characteristics and  
 382 atmospheric conditions can additionally degrade the accuracy of ABLH estimates. In addition, Eq. (9)  
 383 requires a priori determination of the ABLH, which also causes difficulties for practical applications of such  
 384 an approach. Therefore, we still use the  $Ri$  algorithm with fixed  $Ri_c = 0.35$  for simplicity.

385



386

387 Figure 6  $Ri_h$  versus  $h/L$  for selected cases. The data points are colored based on the value of  $L$ . The black  
 388 solid line is the best fit for the selected data points, and the best-fit  $\alpha$  value is also given. The gray dashed  
 389 line is the constant  $Ri_c = 0.35$  used in the improved  $Ri$  algorithm.

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## 392 4 MOSAiC ABLH variation and controlling factors

393

### 4.1 Overall distribution of ABLH

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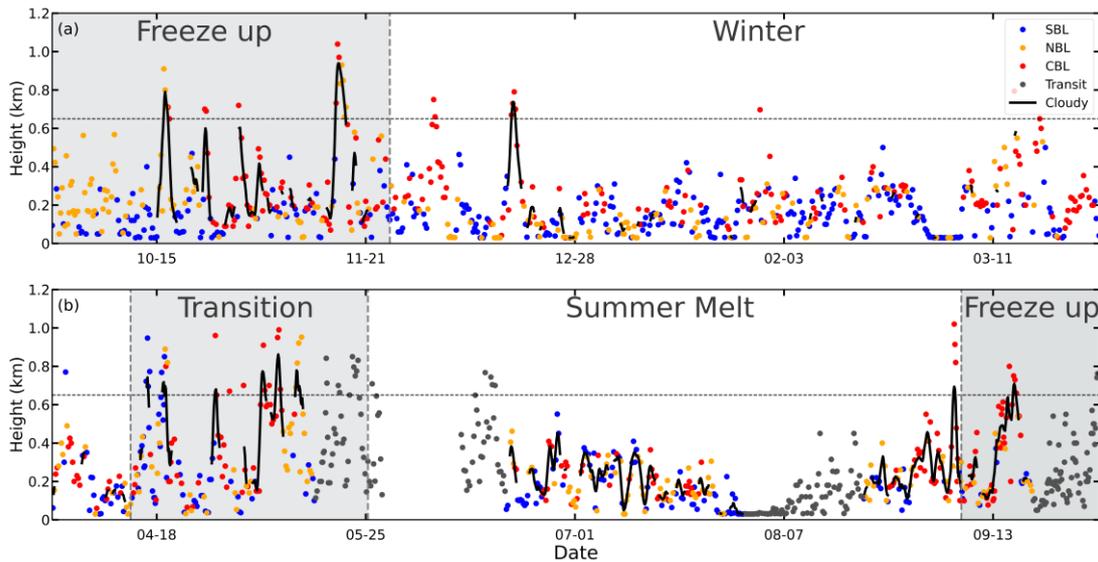
In this section, we analyze the ABLH variation during the MOSAiC and relevant controlling factors,  
 395 based on the manually-labeled ABLH dataset and the ABL types that are determined through Eq. (1), or only  
 396 the  $\theta_E$  difference if SH is unavailable. The full-time series of ABLH during the MOSAiC expedition is  
 397 presented in Fig. 7 and forms the basis for the remaining analyses. According to near surface conditions and

398 the sea ice state, the whole MOSAiC observation period is divided into “freeze up”, “winter”, “transition”,  
399 and “summer melt” periods (Shupe et al., 2022), roughly corresponding to the seasons of autumn, winter,  
400 spring, and summer, respectively. In Figure 7, the black solid lines indicate persistent low-level clouds that  
401 exist for more than 12 h; these occur most frequently in the late summer and autumn (the “freeze up” period),  
402 which agrees with Shupe et al. (2011). Note that the grey dots indicate that the ABL data were observed  
403 while the vessel was in transit, and the representativity of the ABLH data should be considered in this context.  
404 For the first such period, the vessel left the MOSAiC ice floe in mid-May and slowly progressed south  
405 through tightly consolidated sea ice, such that the data are generally representative of the sea ice pack in the  
406 region. Measurements from early June when the vessel was near or in open water close to Svalbard have  
407 been excluded entirely from the analysis. In the middle of June, as the vessel returned to the original  
408 MOSAiC ice floe, the sea ice was not as tightly consolidated and the vessel preferentially went through leads;  
409 the preferentially lower ice fraction along this transit could have impacted the thermal structure of the ABL.  
410 For the three weeks in early August, the vessel moved around in the Fram Strait area and then made its way  
411 north to another passive sea ice drifting position near the North Pole, again transiting through regions with  
412 lower sea ice fraction. Finally, at the very end of the expedition, the vessel took some time to exit the sea ice,  
413 stopping a few times to allow for work on the ice.

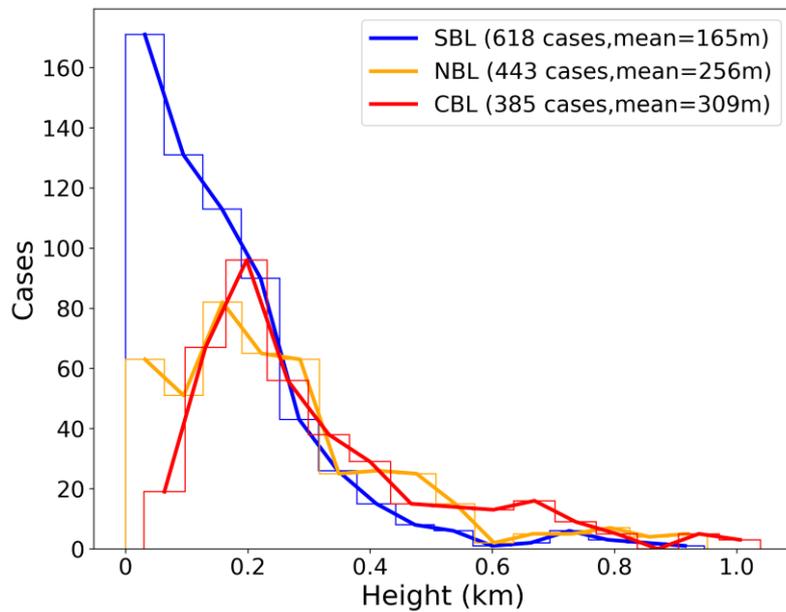
414 Overall, as shown in Fig. 7, the mean ABLH during the whole observation period is 231 m. This is  
415 lower than the typical ABLH over the Arctic land surface (Liang and Liu, 2010), which is primarily attributed  
416 to the stronger suppression of the temperature inversion over the sea-ice surface. The Arctic ABL is  
417 suppressed for most of the MOSAiC year, while for a few periods it intensively develops for several days at  
418 a time, most commonly when clouds and a CBL are present. For instance, frequent, intensive ABL  
419 development occurs in the “transition” period from 13 April through to 24 May 2020. In this period, the  
420 convective thermal structure and cloud effects contribute to ABLH reaching over the 95th percentile of the  
421 ABLH data (horizontal dotted line) for about 7 days, with the maximum ABLH of 1100 m. In contrast, the  
422 ABL is strongly suppressed in the period from 15 July through to 30 August 2020, with a mean ABLH of  
423 only 136 m. The specific mechanisms of ABL development and suppression in these two cases will be  
424 analyzed in Sections 4.3 and 4.4, respectively.

425 Figure 8 presents the frequency distribution of ABLH under SBL, NBL, and CBL regime types. Overall,  
426 the sample number of SBL cases is more than that of NBL and CBL cases during the MOSAiC period (43 %  
427 for SBL, 31% for NBL, and 26 % for CBL). These occurrence frequencies roughly agree with Jozef et al.  
428 (2023), while their results show more NBL and CBL and less SBL. It is likely to be attributed to differences  
429 in classification criteria. The distributions of SBL and NBL ABLH are skewed towards small values, with  
430 94 % and 79% of the ABLH values lower than 400 m, and mean values of 165 m and 256 m, respectively.  
431 For CBL, the distribution is shifted somewhat towards larger values, with 23 % of the ABLH values higher  
432 than 600 m and a mean value of 309 m.

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 435 Figure 7 Time series of ABLHs throughout the MOSAiC year is divided into (a) and (b). The blue, yellow,  
 436 and red dots indicate the heights of SBL, NBL, and CBL, respectively. The gray dots indicate ABL data  
 437 observed while the vessel was in transit. The black solid lines indicate the heights of cloudy ABLs and persist  
 438 for at least 12 hours. The gray dashed horizontal line denotes the 95th percentile of ABLH (650 m). The gray  
 439 and white background shadings indicate the periods under different surface-melting states, i.e., “freeze up”,  
 440 “winter”, “transition”, and “summer melt” periods.  
 441



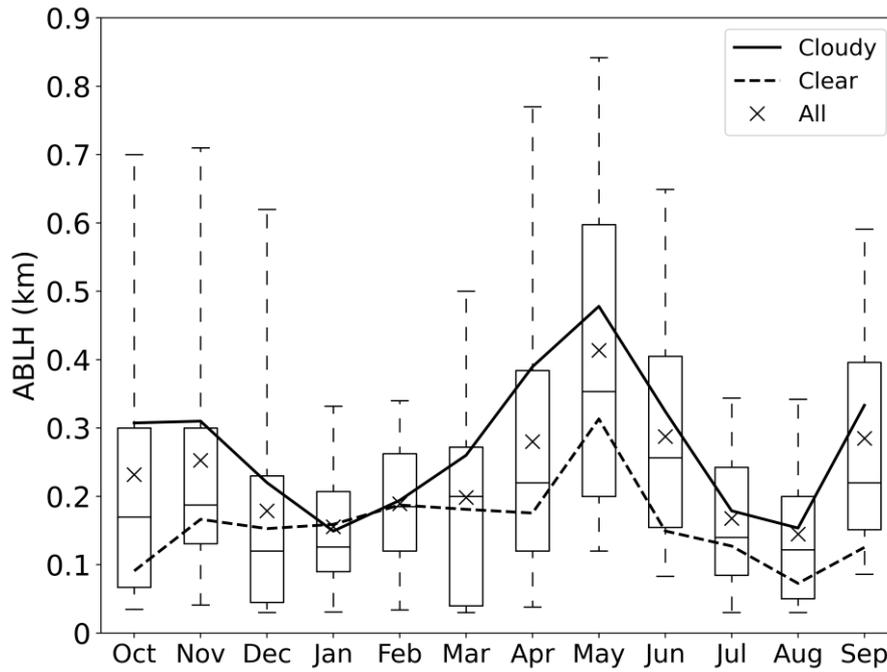
442  
 443 Figure 8 Frequency distribution of SBL height (blue), NBL height (yellow), and CBL height (red). The case  
 444 numbers and the mean values of ABLH for SBL, NBL, and CBL conditions are also given.  
 445

#### 446 4.2 Annual cycle of ABLH and related factors

447 Figure 9 presents the annual cycle of monthly ABLH statistics during the MOSAiC expedition in terms  
 448 of 5th, 25th, 50th, 75th, and 95th percentiles of ABLH (boxplots) and the mean value (“x” signs and solid

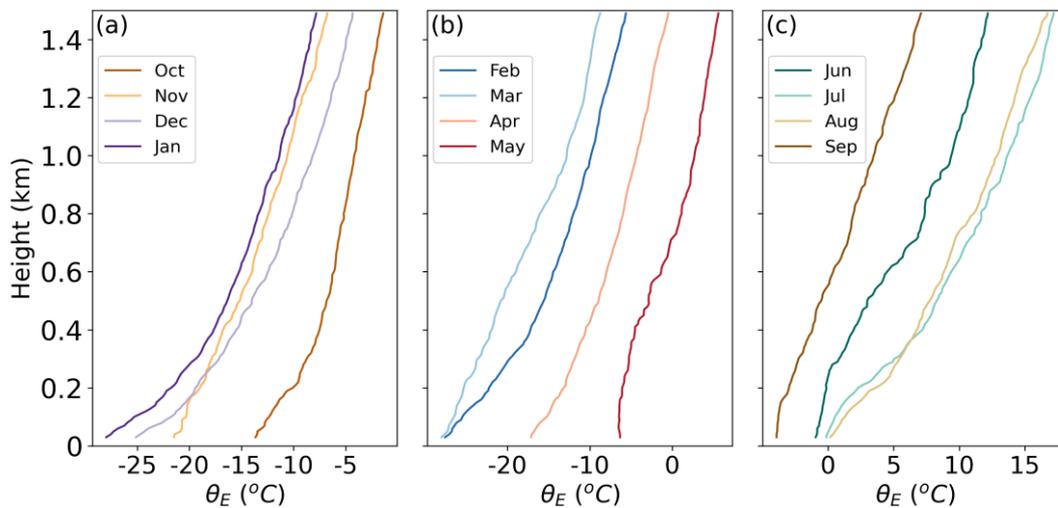
449 and dashed lines). The box-and-whisker plots show a distinct peak in May, with a median value of 363 m  
450 and the 95th percentile reaching over 800 m. An abrupt decrease occurs in the following July and August,  
451 and another minimum occurs in January, all with median values below 150 m. It should be noted that the  
452 ABLH data in transit (gray dots in Fig. 7) are also included in the statistics, which could have potential  
453 impact from somewhat more open-water surface conditions. Specifically, the ABLH data during transit  
454 periods cause higher mean ABLH for June and lower mean ABLH for August (see Fig. 7). The comparison  
455 between cloudy and clear-sky ABLHs indicates that the low-level clouds significantly contribute to the  
456 Arctic ABL development during the MOSAiC year, except in winter, when low-level clouds are rare.

457 The annual cycle of ABLH is determined by the seasonal evolution of the ABL structure (Tjernström  
458 et al., 2009; Palo et al., 2017), as revealed through median profiles of  $\theta_E$  in each month (Fig. 10). The results  
459 show that from the start of the MOSAiC expedition (October 2019), the near-surface  $\theta_E$  gradually decreases  
460 due to seasonal surface radiative cooling in the absence of sunlight, more rapidly than the atmosphere cools,  
461 which causes a strong surface temperature inversion. The increasing inversion strength through January leads  
462 to decreasing ABLH into “winter.” In February and March, the surface remains steady while the atmosphere  
463 cools more, leading to diminished temperature inversion strength and a small increase in ABLH. After March  
464 2020, with the return of sunlight, the  $\theta_E$  starts to rise over the whole lower atmosphere, and the near-surface  
465 air temperature warms somewhat more than the atmosphere above. This differential warming leads to more  
466 frequent near-neutral or convective thermal structures and contributes to high ABLH during the “transition”  
467 period. In July and August, the upper-layer temperature continues to rise while the near-surface temperature  
468 is constrained to  $\sim 0$  °C due to the melting sea ice surface, which leads again to a surface inversion and a  
469 diminished ABLH during the “summer melt” period. In September, as the sun descends to much lower angles,  
470 the  $\theta_E$  across the whole lower atmosphere starts to drop, with more rapid cooling in the atmosphere relative  
471 to the near-surface resulting again in near-neutral or convective thermal structures and an increase in the  
472 CBL height during the “freeze up” period. The whole process forms these general shifts over the annual  
473 cycle. In addition, we examined the potential implications of the diurnal cycle on the ABL thermal structure.  
474 Monthly profiles based on different moments of a day were found to show little variability (not shown), such  
475 that the impact of the diurnal cycle is minimal.



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Figure 9 Box-and-whisker plots of the ABLH distribution in each month throughout the MOSAiC year. The whiskers, the boxes, and the black horizontal lines show the 5th, 25th, 50th, 75th, and 95th percentile values of ABLH. The solid and dashed lines and the “x” signs indicate the mean ABLH of cloudy, clear, and all ABL types, respectively.



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Figure 10 Monthly median profiles of equivalent potential temperature throughout the MOSAiC year are divided into (a), (b), and (c).

486 To further explore the relations between surface conditions and the ABLH, we evaluate the correlations  
487 between the ABLH and three near-surface meteorological and turbulence parameters during the MOSAiC  
488 period, including the near-surface equivalent potential temperature gradient ( $\theta_{Egrad} = \theta_{E 10m} - \theta_{E 2m}$ ), friction  
489 velocity ( $u_*$ ), and TKE dissipation rate ( $\epsilon$ ). The results are shown in Fig. 11. Generally, the near-surface  
490 buoyancy and shear effects both modulate these variables. In Fig. 11a, the ABLH distribution for negative

491  $\theta_{Egrad}$  has a wide range from the lowest level to above 1 km. As  $\theta_{Egrad}$  becomes positive and increases, the  
 492 ABLH distribution rapidly narrows to below 200 m. In general, positive  $\theta_{Egrad}$  means a stably stratified ABL  
 493 and surface-based temperature inversion, both of which lead to low ABLH, and negative  $\theta_{Egrad}$  means that  
 494 atmospheric stability near the surface is near-neutral or convective, which is necessary for ABL development.  
 495 The  $u_*$  presents a significant correlation with the ABLH, with correlation coefficient of 0.58 (Fig. 11b). High  
 496  $u_*$  values, which are related to strong mechanical mixing, contribute to the ABL development. However, it  
 497 is worth noting that intensive ABL development (ABLH over 600 m) only occurs as  $u_*$  ranges between 0.2  
 498 and 0.5 m s<sup>-1</sup>, which suggests that other factors exist to facilitate further development of the ABL, such as  
 499 cloud effects (see Fig. 9). The  $\varepsilon$  is usually a qualitative proxy for turbulence kinetic energy, since higher TKE  
 500 means larger spectral values at low frequencies, hence higher dissipation rate due to the energy cascade in  
 501 the inertial subrange. In Fig. 11c, when  $\varepsilon$  is less than  $5 \times 10^{-5}$  m<sup>2</sup> s<sup>-3</sup>, turbulence in the ABL is limited with  
 502 almost all ABLH values below 200 m. As  $\varepsilon$  increases and becomes larger than  $5 \times 10^{-5}$  m<sup>2</sup> s<sup>-3</sup>, the average  
 503 ABLH increases with active turbulent mixing in the ABL. The threshold of  $5 \times 10^{-5}$  m<sup>2</sup> s<sup>-3</sup> is proposed by  
 504 Brooks et al. (2017) as the distinction between turbulent and non-turbulent flows.

505 The free-flow stability (characterized by the free-flow Brunt-Väisälä frequency,  $N$ ) can affect the ABLH  
 506 (Zilitinkevich et al., 2002; Zilitinkevich and Baklanov, 2002; Zilitinkevich and Esau, 2002, 2003), and  
 507 therefore is also examined here. Based on the buoyancy flux at the surface ( $B_s$ ) and  $N$ , the NBLs and SBLs  
 508 can be further divided into four types: the truly neutral (TN,  $B_s = 0$  and  $N = 0$ ), the conventionally neutral  
 509 (CN,  $B_s = 0$  and  $N > 0$ ), the nocturnal stable (NS,  $B_s < 0$  and  $N = 0$ ), and the long-lived stable boundary layer  
 510 (LS,  $B_s < 0$  and  $N > 0$ ). According to Zilitinkevich and Baklanov (2002), we calculate the  $N$  and  $B_s$  and  
 511 reclassify the SBLs and NBLs. We find that the percentages of  $N > 0.015$  in SBLs and NBLs are 89 % and  
 512 80 %, which indicates that LS and CN types dominate the stable and neutral conditions for MOSAiC,  
 513 respectively. Since only 80 TN cases were identified, these are deemed to be too few for additional analysis  
 514 of this type. Zilitinkevich and Esau (2003) gave ABLH equations relevant to each ABL type as:

$$515 \quad h_E = \begin{cases} C_N u_* |fN|^{-1/2} & \text{(Pollard et al., 1973) for CN ABL, (10)} \\ C_S u_*^2 |fB_s|^{-1/2} & \text{(Zilitinkevich, 1972) for NS and LS ABL, (11)} \end{cases}$$

516 where  $h_E$  is the equilibrium ABLH,  $f$  is the Coriolis parameter, and  $C_N$  and  $C_S$  are empirical coefficients. In  
 517 addition, Vogelesang and Holtslag (1996) and Steeneveld et al. (2007a) also explore a  $h_E$  equation without  
 518 taking into account  $f$  explicitly, expressed as:

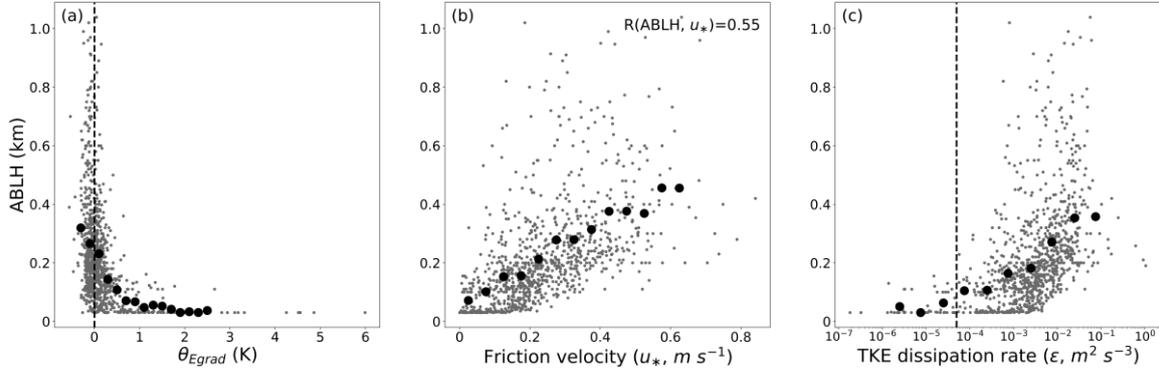
$$519 \quad h_E = C_i \frac{u_*}{N} \quad \text{for all SBL and NBL, (12)}$$

520 where  $C_i$  is an empirical coefficient. Here we select the CN, NS, and LS ABLH dataset, and fit the data with  
 521 the corresponding expressions in Eq. (10–12) to obtain the empirical coefficients, and the results are  
 522 presented in Fig. 12. All three expressions tend to well represent the ABLHs, with significant correlation  
 523 coefficients. The empirical coefficients  $C_N$  and  $C_S$  are 1.7 and 0.4, respectively, which are close to the typical  
 524 values determined through large-eddy simulations (Zilitinkevich, 2012). The coefficient  $C_i = 20$  in Fig. 12c  
 525 is double the typical value of 10 (Vogelesang and Holtslag, 1996), but agrees with the results reported by  
 526 Overland and Davidson (1992) for the ABL over sea ice. The difference in  $C_i$  may be attributed to the unique

527 free-flow stability or other potential mechanisms of ABL development in the Arctic atmosphere.

528 In summary, near-surface conditions and free-flow stability play a key role in ABL development and  
 529 are also an indicator, in that one can roughly determine the development state of the whole ABL from these  
 530 basic variables.

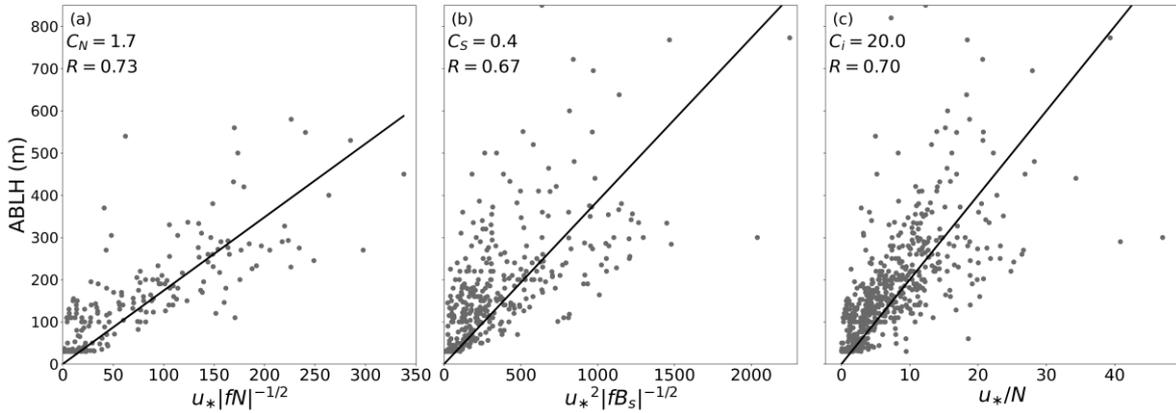
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533 Figure 11 The ABLHs and bin-averaged values for (a) equivalent potential temperature gradient,  $\theta_{Egrad}$  (K),  
 534 (b) friction velocity,  $u_*$  ( $m s^{-1}$ ), and (c) turbulent kinetic energy dissipation rate,  $\varepsilon$  ( $m^2 s^{-3}$ ). The average bins  
 535 for  $\theta_{Egrad}$ ,  $u_*$ , and  $\varepsilon$  logarithm are 0.2 K, 0.05  $m s^{-1}$ , and 0.5  $m^2 s^{-3}$ , respectively. The correlation coefficient  
 536  $R$  is given in (b), which is statistically significant ( $p < 0.05$ ). The dashed vertical lines indicate the thresholds  
 537 of (a)  $\theta_{Egrad} = 0$  K and (c)  $\varepsilon = 5 \times 10^{-5}$   $m^2 s^{-3}$ .

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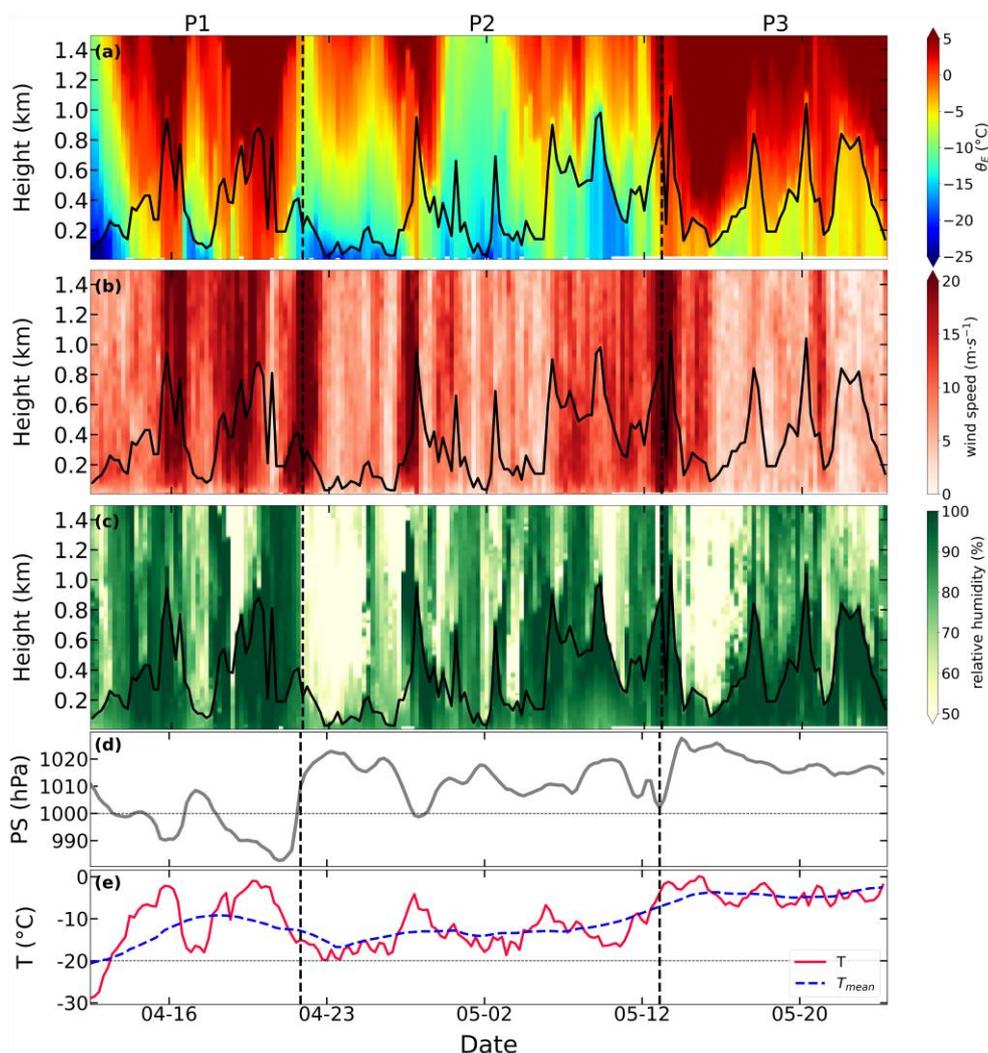
540 Figure 12 The ABLHs versus three expressions in Eq. (10–12). The empirical coefficients  $C_N$ ,  $C_S$ , and  $C_i$   
 541 are given in (a), (b), and (c), respectively, and represent the slope of the best fit line (black line). The  
 542 correlation coefficient  $R$  is given in each panel, which is statistically significant ( $p < 0.05$ ).

543

#### 544 4.3 Case study #1: Intensively developed ABL 13 April - 24 May 2020

545 To investigate the unique characteristics of the ABL development and its controlling factors in detail,  
 546 we analyze the association of the ABLH with vertical thermal structure and near-surface conditions during  
 547 the transition period (see Fig. 7) when the ABLH was generally the highest. Figure 13 presents time-height  
 548 cross sections of  $\theta_E$ , wind speed, and  $RH$ , and the time series of near-surface temperature and surface  
 549 pressure during this period. We divide the whole period into three parts based on the ABLH and the vertical

550 structure of the lower troposphere. Overall, the near-surface temperature is generally warmer than  $-20\text{ }^{\circ}\text{C}$   
 551 and shows gradual warming towards the melting point. In Period 1, a warm and moist air advection event  
 552 affects the measurement area, resulting in increased air temperature, near-saturated  $RH$ , strong winds  
 553 throughout the lower troposphere, and low surface pressure. The approximately constant  $\theta_E$  profile near the  
 554 surface facilitates exchange between the upper and lower layers, and the high-speed wind profile enhances  
 555 mechanical mixing, leading to highly developed ABL and ABLH exceeding 600 m. In Period 2, the near-  
 556 surface air temperature drops again to between  $-20$  and  $-10\text{ }^{\circ}\text{C}$ , which causes a temperature inversion and  
 557 partially suppresses the ABL development. However, periodic layers of near-saturated  $RH$  extending up to  
 558 600m or more indicate the presence of clouds. The ABLH at these times is related to the depth of the near-  
 559 saturated layer, consistent with a structure where the cloud-induced mixed layer aloft couples with the near-  
 560 surface mixed layer, forming a deeper ABL and higher ABLH (Wang et al., 2001; Shupe et al., 2013). In  
 561 Period 3, a high-pressure synoptic system occurs and suppresses the development of the ABL, but the cloud-  
 562 driven turbulent mixing still exists and counteracts the influence of the high-pressure system. In summary,  
 563 the development of the ABL mainly depends on large-scale synoptic processes, especially warm-air  
 564 advection events. Additionally, the interaction between the surface-mixed layer and cloud-mixed layer also  
 565 plays a significant role in the ABL development.



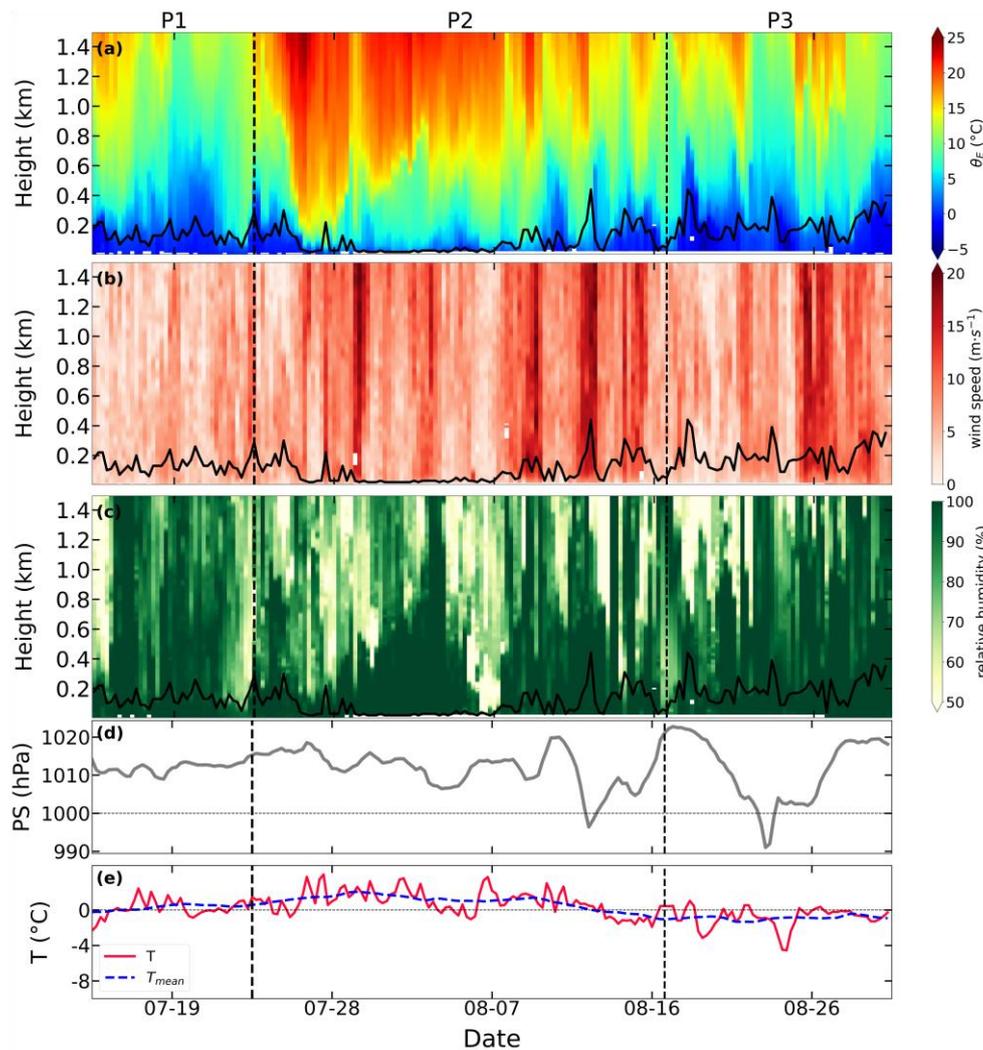
566

567 Figure 13 Time-height sections of (a) equivalent potential temperature, (b) horizontal wind speed, and (c)  
568 relative humidity and time series of (d) surface pressure and (e) near-surface air temperature (red line) and  
569 7 d running mean of near-surface temperature (blue line). The whole period is from 13 April 2020 to 24 May  
570 2020. Vertical dashed lines mark the identified periods P1 to P3. The black solid lines in panels (a–c) denote  
571 the ABLH during this period.

572

#### 573 **4.4 Case study #2: the severely suppressed ABL 15 July – 30 August 2020**

574 The Arctic ABL is suppressed most of the time, especially in the late summer for more than a month.  
575 We choose the severely suppressed ABL in this period as a case to analyze the influences of vertical thermal  
576 structure and near-surface conditions on the ABLH. The results are shown in Fig. 14, and the whole period  
577 is divided into three parts, similar to Fig. 13. In Period 1, the near-surface air temperature is constrained to  
578  $\sim 0$  °C due to the melting surface, and the temperature inversion and weak wind are dominant throughout the  
579 lower troposphere, which suppresses the ABL development. In Period 2, warm-air advection occurs in the  
580 lower troposphere, strengthening the temperature inversion and contributing to further ABL suppression and  
581 an ABLH often lower than 100 m. Because of the constrained near-surface temperature, this structure is  
582 distinct from that of the spring “transition” period when warm-air advection facilitates ABL development.  
583 In Period 3, the near-surface and upper-layer temperatures start to decrease, and the temperature inversion  
584 weakens, which makes the ABLH periodically grow up to  $\sim 400$  m. Despite that, the ABL is still stably  
585 stratified, and the ample moisture and clouds cannot contribute significantly to the ABL development, which  
586 is consistent with Shupe et al. (2013). It is important to note that during the second half of Period 2, the  
587 *Polarstern* transited from near the sea ice edge to near the North Pole, such that this transition towards  
588 weaker temperature inversions is related to both spatial and seasonal shifts. In summary, the suppression of  
589 the ABL during the “summer melt” period results from strong temperature inversions and weak winds, and  
590 cloud-driven turbulent mixing that is inhibited from interacting with the surface layer due to the near-surface  
591 stability. In this period, warm-air advection events enhance the ABL suppression, opposite to the “transition”  
592 period.



593

594 Figure 14 Similar to Fig. 13, but the period is from 15 July 2020 to 30 August 2020.

595

596

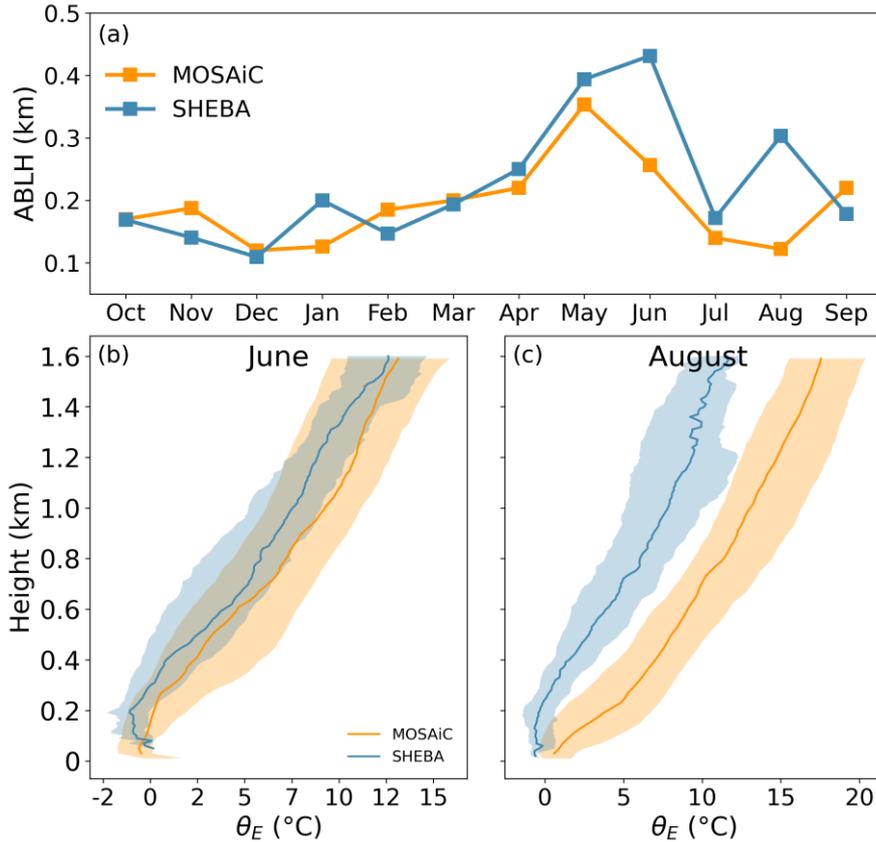
### 597 **5 MOSAiC – SHEBA comparison**

598 The MOSAiC and SHEBA observations were both made over the Arctic sea ice during yearlong periods.  
 599 In terms of the location of observation sites, the SHEBA campaign took place in the Beaufort and Chukchi  
 600 Seas (Perovich et al., 2003), while the MOSAiC observations took place along the transpolar drift for much  
 601 of the year, in the higher latitudes of the Fram Strait in June, July, and early August, and again near the North  
 602 Pole in late August and September. The comparison between the two campaigns could provide insight into  
 603 the spatial and temporal variability in the Arctic ABL structure. The monthly ABLHs of the two campaigns  
 604 are presented in Fig. 15a. The overall distributions of ABLH are similar during the annual cycle, however,  
 605 the SHEBA ABLH is significantly higher than the MOSAiC ABLH in June and August. We will discuss  
 606 these differences based on the ABL thermal structure.

607 Comparisons of monthly  $\theta_E$  profiles between the two campaigns during June and August are presented  
 608 in Fig. 15 (b, c). It is clear that  $\theta_E$  within the lower troposphere during MOSAiC is much higher than that  
 609 during SHEBA, especially in August. In June, the near-surface  $\theta_E$  values in both campaigns are close,

610 because both were over melting sea ice. However, on average, the upper-layer  $\theta_E$  during SHEBA is lower  
611 than that during MOSAiC, especially at a height of around 200 m, which results in decreased low-level  
612 stability that supports ABL development. This difference explains why the monthly SHEBA ABLH rises  
613 from May to June, but the monthly MOSAiC ABLH decreases at this time. In July at SHEBA, the increased  
614 air temperature in the lower troposphere combined with constrained near-surface  $\theta_E$  results in a significant  
615 temperature inversion that suppresses the ABL development (not shown). Thus, the ABLH values at SHEBA  
616 and MOSAiC are comparable in July. In August, the  $\theta_E$  profiles from the two campaigns are significantly  
617 different. The surface at both locations is still mostly constrained to be near the melting point, while the  
618 lower troposphere at SHEBA starts to cool more than that at MOSAiC. The SHEBA  $\theta_E$  profile exhibits a  
619 near-neutral or convective state, while the MOSAiC  $\theta_E$  profile shows a further enhanced surface temperature  
620 inversion due to warm air advection aloft, which maintains the ABL suppression. To sum up, the increase in  
621 air temperature in the lower troposphere in early summer during MOSAiC precedes that during SHEBA,  
622 while the cooling of the lower troposphere in late summer during MOSAiC lags that during SHEBA. These  
623 are the main factors contributing to the ABLH differences between the two campaigns.

624 The atmospheric warming during the MOSAiC summer may be attributed to ongoing Arctic warming  
625 that contributes a different atmospheric structure, but the impacts of transit periods and different synoptic  
626 backgrounds should also be considered. First, there is the complexity of the transit periods during MOSAiC.  
627 During the first half of June, *Polarstern* travelled northward into a somewhat loosened sea ice pack and  
628 followed open water areas as much as possible. If anything, the higher fraction of open water along this  
629 transit path would promote more heat exchange between the surface and ABL and higher ABLH than the  
630 regional ice pack (e.g., Fig. 7), which suggests that the observed difference between MOSAiC and SHEBA  
631 cannot be explained by this transit period. However, in the first part of August, when *Polarstern* transited  
632 preferentially through open water areas during its movement further north, the transit environment was in a  
633 persistent melting state with warm air advection aloft. It is not clear how this transit ultimately impacted the  
634 monthly ABLH results, although the values during the transit period were lower than those during the final  
635 10 days of August when *Polarstern* was again passively drifting with the sea ice (Figs. 7, 14). Thus, some  
636 of the difference from SHEBA at this time could have been attributed to the specific conditions encountered  
637 during movement of the vessel. Additionally, these two campaigns were in different storm tracks with  
638 markedly different types of regional advection patterns. For example, in summer, MOSAiC was approaching  
639 the Fram Strait where northward warm air advection is common. Thus, synoptic variability likely plays a  
640 big role in the ABL thermal structure. In summary, there is large variability in the Arctic ABL structure  
641 during summer caused by the surface melting state, and more detailed assessments are needed to study the  
642 specific causes for the atmospheric warming and possible influences of changing Arctic conditions on the  
643 ABL structure.



644

645 Figure 15 Comparison of ABL during SHEBA (blue squares, lines, and shadings) and MOSAiC (yellow  
 646 squares, lines, and shadings), including (a) annual cycle of monthly median ABLH and monthly  $\theta_E$  profiles  
 647 in (b) June and (c) August. The solid lines in (b–c) indicate the median profiles, and the shadings indicate  
 648 the range of 25th- and 75th- percentile profiles. The median ABLHs of SHEBA are from Dai et al. (2011).

649

## 650 6 Conclusions

651 This study is carried out using merged radiosounding data and corresponding surface meteorological  
 652 observations and cloud properties collected during the MOSAiC expedition over a year-long period. A  
 653 number of ABLH algorithms are first evaluated, prompting us to implement an improved  $Ri$  algorithm that  
 654 takes cloud effects into consideration. We propose a critical  $Ri = 0.35$  and further analyze its value choice  
 655 and stability dependence. Subsequently, we use the manually-labeled ABLH dataset to study how  
 656 atmospheric thermal structure and near-surface conditions impact the characteristics and evolution of the  
 657 ABL during the MOSAiC year. Lastly, we use two cases to explore the mechanisms of ABL development  
 658 and suppression over the Arctic sea-ice surface. The main conclusions are as follows.

659 During the MOSAiC year, the mean ABLH is 231 m, with SBLs, NBLs and CBLs accounting for 43 %,   
 660 31 %, and 26 % of the profiles, respectively. The annual cycle of the Arctic ABLH is clearly characterized  
 661 by a distinct peak in May and two minima in January and July-August. Low-level clouds significantly  
 662 contribute to the Arctic ABL development during the MOSAiC year, except in winter, when low-level clouds  
 663 are less frequent. Compared to the SHEBA ABLH, the MOSAiC ABLH is suppressed in June and August,  
 664 which is caused by increased atmospheric warming in the MOSAiC ABL during the “summer melt” period

665 compared to SHEBA.

666 The annual cycle of ABLH over the Arctic Ocean is primarily controlled by the seasonal evolution of  
667 the ABL thermal structure and near-surface meteorological conditions. In the “winter” period, temperature  
668 inversions form due to negative net radiation at the surface and are associated with low ABLHs. In the spring  
669 “transition” period, the rapid increase of near-surface temperature weakens the temperature inversion,  
670 facilitating the development of the ABL. In the “summer melt” period, temperature inversions result from a  
671 fixed surface temperature at the melting point and warm-air advection aloft, which suppresses ABL  
672 development. For near-surface conditions and free-flow stability, a negative  $\theta_{Egrad}$  and large TKE dissipation  
673 rate are characteristic of significant ABL development. In addition, empirical formulas relating ABLH to  
674 friction velocity, near-surface and free-flow stabilities are also tested, and the results suggest that the  
675 MOSAiC ABLH can be roughly estimated based on these basic variables.

676 During MOSAiC, the development of the ABL is irregular, and only occurs during intermittent periods.  
677 The year is characterized by occasions of abrupt growth of the ABLH and intensive ABLH variation for  
678 several days thereafter. These unique features are caused by large-scale synoptic processes (e.g., advection  
679 events) that bring heat, moisture, and clouds. It is worth noting that some large-scale events can have the  
680 opposite effect on the ABL. For example, warm-air advection can facilitate ABL development in the spring  
681 “transition” period but can cause ABL suppression in the “summer melt” period, when the constrained near-  
682 surface temperature cannot respond to the warmth aloft.

683 The findings reported here provide new insight into the annual variability and properties of the ABL  
684 and ABLH over sea ice in the ‘new Arctic.’ The ABLH contains information directly related to the thermal  
685 structure of the ABL and includes the impacts of weather events and large-scale circulations on the ABL  
686 structure. The ABL development supported by cloud processes was captured by the improved *Ri* algorithm,  
687 which is similar to Brooks et al. (2017). However, the representativity of these results must still be  
688 established by comparing them with additional observations, and the influences of other variables (e.g.,  
689 energy budget terms) on the ABLH should also be considered in future research.

690

## 691 **Data Availability**

692 The radiosonde data are available at the PANGAEA Data Publisher at  
693 <https://doi.org/10.1594/PANGAEA.943870> (Maturilli et al., 2022). All value-added products and surface  
694 meteorological data are available at the archive of the US Department of Energy Atmospheric Radiation  
695 Measurement Program. The Planetary Boundary Layer Height Value-Added Product is available at  
696 <http://dx.doi.org/10.5439/1150253> (Riihimaki et al., 2019). The cloud property data is available at  
697 <https://doi.org/10.5439/1871015> (Shupe, 2022). The MOSAiC surface flux and other meteorological data  
698 are available at the Arctic Data Center at <http://dx.doi.org/10.18739/A2PV6B83F> (Cox et al., 2023). The  
699 merged sounding-tower data are available at PANGAEA. The SHEBA-based sounding data are available at  
700 <https://doi.org/10.5065/D6FQ9V0Z> (Moritz, 2017).

701

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711

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