

1 **Thrusts control the thermal maturity of accreted sediments.**

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Abstract.

Thermal maturity assessments of hydrocarbon-generation potential and thermal history rarely consider how upper-plate structures developing during subduction influence the trajectories of accreted sediments. Our thermomechanical models of subduction support that thrusts evolving under variable sedimentation rates and décollement strengths fundamentally influence the trajectory, temperature, and thermal maturity of accreting sediments. This is notably true for the frontal thrust, which pervasively partitions sediments along a low and a high maturity path. Our findings imply that interpretations of the distribution of thermal maturity cannot be detached from accounts of the length and frequency of thrusts and their controlling factors. Our approach takes these factors into consideration and provides a robust uncertainty estimate in maximum exposure temperatures as a function of vitrinite reflectance and burial depth. As a result, our models reduce former inconsistencies between predicted and factual thermal maturity distributions in accretionary wedges.

44 **1. Introduction**

45 Organic material transforms into coal, oil, and gas at rates primarily controlled by temperature. This transformation,
46 critical for the hydrocarbon industry, is also useful to study the tectonic and sedimentary evolution of basins and
47 orogens. The extent of this transformation in sediments, known as thermal maturity, can be measured as vitrinite
48 reflectance, i.e., the percentage of incident light reflected from the surface of vitrinite particles in those sediments.
49 Thermal maturity has been used to estimate the thermal evolution of igneous intrusions and seismic slip, the extent
50 of low-grade metamorphism, porosity, and compaction in basin sediments, and the geothermal history of accreting
51 material during subduction (e.g., Bostick and Pawlewicz, 1984; Rabinowitz et al., 2020; Fukuchi et al., 2017;
52 Kamiya et al. 2017).

53 Inferences on the geothermal history of subduction margins based on thermal maturity depend on the
54 trajectory followed by the accreting sediments (Miyakawa et al., 2019). Low-temperature, high-pressure
55 metamorphic rocks in the subduction wedge are often attributed to the pressure maxima that typically predate the
56 temperature maxima in accreted sediments undergoing diagenesis in the wedge (Ruh, 2020). However, the
57 existence of complicated patterns in sediment trajectories is supported by numerical models and field observations
58 (Giunchi & Ricard, 1999). As the orogenic wedge evolves, sediments accreting along different paths reach different
59 depths and velocities and are exposed to different regional peak temperatures. Miyakawa et al. (2019) proposed to
60 subdivide these trajectories based on their final characteristics, like thermal maturity. In this manner, the
61 spatiotemporal evolution of sediments and their thermal maturity is regulated to a first order by the partition of
62 incoming sediments along two endmember pathways; (I) a deeper path leading to elevated thermal maturities and
63 constituted by underthrust material, the *high thermal-maturity path*, and (II) a shallower path that typically lies
64 closer to the surface or gets frequently exhumed to near-surface levels, the *low thermal-maturity path*.

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66 Previous studies have used numerical and analogue approaches to study the trajectories of sedimentary
67 particles, and their spatial and pressure-temperature evolution, as a function of changes in erosion, sedimentation,
68 or décollement strength. The trajectory followed by underthrust sedimentary units is primarily determined by
69 orogenic wedge dynamics and its controlling forces (Plat, 1986). Although these sediments may only be exhumed
70 near the backstop of the wedge, the trajectories of other accreted sediments generally deflect toward the surface
71 under the influence of erosion (Konstantinovskaia and Malavieille, 2005). In fact, sedimentary particle trajectories
72 gradually shift from deflection toward the surface near the front of accretion to final exhumation near the wedge
73 backstop (Wenk and Huhn, 2013). Still, even under-thrust sediments, which would co-relate to high-maturity
74 paths in our study, have variable pressure-temperature paths (Ruh, 2020a). It is important to highlight that the
75 majority of past studies have explored a snapshot of sediment trajectories, assuming that the general nature of
76 trajectories remains relatively fixed with time or is stationary in nature. However, the intrinsic connection between
77 thermal maturity and the comprehensive thermal exposure along the entire trajectory necessitates an in-depth
78 investigation into the dynamic and transitory nature of sediment trajectories.

79 Although there is general consensus on the rate and extent of sediment trajectory transition from horizontal
80 to vertical during accretion, the dynamic perturbations in sediment dynamics have yet to be adequately examined.
81 For instance, while most studies show a great degree of correlation between the initial depth of incoming sediments
82 and their final position in the wedge (e.g., Mulugeta and Koyi, 1992; Willett, 1992), a dynamic fluctuation in this
83 correlation due to thrusting can result in non-stationary exhumation paths for accreting sediments in a wedge (e.g.,
84 Konstantinovskaia and Malavieille, 2005; Miyakawa et al., 2019). Much remains to be explored regarding the
85 partition of high and low thermal maturity paths and how sediments travel inside natural wedges, given the
86 conventional assumption that accreting sediments remain at the same relative depth and translate along the adjacent
87 “layers” without vertical mixing throughout the tectonic evolution of the wedge (Hori and Sakaguchi, 2011).

88 Our assessment identifies a primary gap in existing research: the prediction and mapping of the initial
89 sediment influx to their final location in the orogenic wedge. More specifically, the challenge lies in determining
90 which portions of incoming sediment will predominantly constitute the core of the wedge and which will reside at
91 comparatively shallower depths. Given that the maximum exposure temperature estimation from the thermal
92 maturity is inherently reliant on the path of sediments inside the wedge, information on path diversity would
93 inherently constrain the uncertainty in maximum exposure temperature used for the identification of paleothermal
94 structures of subduction zones. Moreover, to better understand the time-depth paths of wedge sediments, their
95 dependence on the initial state of undeformed sediments, and thus their thermal maturity, the factors that control
96 the evolution of subduction-accretion systems, like sedimentation, erosion, and décollement strength, ought to be
97 considered (Mannu et al., 2016; Simpson, 2010).

98 Here, we explore in detail the impact of accretion in a subduction wedge has on the thermal maturity of its
99 sediments. We simulate subduction-accretion using 2D finite-difference thermomechanical models incorporating
100 empirical thermal conductivity values from the Nankai accretionary margin. We track the evolution of thermal
101 maturity by computing vitrinite reflectance (%R_o) on each marker and throughout the model, using three well-
102 established methods of %R_o computation, as accretion develops the wedge under different sedimentation rates and
103 décollement strengths. These factors notably alter the trajectories and thermal maturities of incoming sediments.
104 Particularly, thrusts define sharp thermal maturity boundaries leading to stark differences in the thermal maturity
105 of sediments that accrete in different thrust blocks, even when they follow similar trajectories and lay nearby.

106 **2. Geological settings and model generalization**

107 We use a generalized model for the subduction of an oceanic plate under a continental plate, with explicit
108 integration of key parameters from the Nankai subduction margin off the Kii island in southwest Japan. The Nankai
109 subduction margin is a product of the ongoing, northwest-directed subduction of the Philippine Sea Plate beneath

110 the Amurian Plate at a convergence rate of 4.1-6.5 cm/yr (Seno et al., 1993; Miyazaki and Heki, 2001; DeMets et
111 al., 2010). Past studies posit the initiation of this subduction within the Nankai region at circa 6 Ma (Kimura et al.,
112 2014). The accretionary wedge adjacent to the Nankai margin is marked by the accretion of extensive sediment
113 layers (>1 km), predominantly formed by overlying younger trench sediments atop Shikoku Basin sediments. Mean
114 sedimentation rates of ~0.4 mm/yr for this area are calculated from sediment data onland and may largely reach the
115 trench through submarine channels (Korup et al., 2014).

116 Another reason to select the Nankai subduction margin is that it is a particularly well-studied accretionary margin
117 regarding its paleo-thermal history and thermal maturity distribution. For example, Underwood et al. (1993) and
118 Sakaguchi (1999) used thermal maturity estimates from Shimanto accretionary wedge in the Nankai subduction
119 margin to suggest that ridge subduction can explain the resulting paleo-heat flow. Following this, Ohmori (1997),
120 published a distribution of thermal maturity and maximum exposure temperature for the Shimanto accretionary
121 wedge identifying out-of-sequence activity in the region. The accretionary wedge adjacent to the Kumano forearc
122 basin in the Nankai subduction margin has also been the subject of the NanTroSEIZE (Nankai Trough Seismogenic
123 Zone) project, which drilled C0002 borehole during the 2012 Integrated Ocean Discovery Program Expedition 338.
124 C0002 borehole is located approximately km southwest of Japan's Kii Peninsula in the Kumano Basin, within the
125 Nankai accretionary margin, and extends 3,348 meters below the seafloor. Having data on both thermal maturity
126 and thermal conductivity from the same borehole in subduction wedges is quite uncommon. To our knowledge, the
127 C0002 borehole, located next to the Kumano forearc basin, is the only place where such data can be found in an
128 accretionary wedge. Because of this unique characteristic, the C0002 borehole serves as an excellent dataset for
129 validation purposes. We modify the thermal conductivity computation for sediments and décollement (see Table
130 1) to match the empirical relationship between depth and thermal conductivity, as measured on core samples in the
131 borehole C0002 (Sugihara et al., 2014).

132 While these adjustments render our models somewhat specific to the Nankai accretionary wedge, we propose that
133 the thermal conductivity values and trend are representative of patterns typically observed in forearc basins and
134 accretionary wedges across the globe, making it broadly applicable to general subduction margins. For instance, in
135 our simulations, the sediment thermal conductivity within our wedge steadily increases with depth from 0.96-4.0,
136 which is within the range of thermal conductivity estimates for comparable depth in other subduction zones, such
137 as the Hikurangi subduction margin, Japan Trench, and Taiwan subduction zone (Fig. S1, Henrys et al. 2003, Lin
138 et al. 2014, Chi and Reed, 2008). As a result, we compare our simulation results not only to thermal maturity values
139 in the Nankai accretionary margin but also to those of the Miura-Boso plate subduction margin in central Japan
140 and the fold and thrust belts of the Western Foothills complex in western Taiwan.

141 **3. Methods**

142 We employ I2VIS, a conservative finite-difference 2-D thermomechanical subduction-accretion model with visco-
143 plastic/brittle rheology (Gerya and Yuen, 2003a, 2003b). The code solves the governing equations for the
144 conservation of mass, momentum, and heat as well as the advection equation with a non-diffusive marker-in-cell
145 scheme constrained by thermal conductivity values inferred from Nankai accretionary wedge. Our numerical
146 approach has several advantages over earlier attempts to simulate thermal maturity in an accretionary wedge, such
147 as a more realistic geothermal profile, variable particle paths, and thermal evolution. In the following sections, we
148 provide information regarding the governing equations, the modified thermal conductivity formulations based on
149 the C0002 borehole, boundary conditions, the rheological model, model setup, surface processes, and the
150 computation of thermal maturity.

151 ***3.1 Governing equations***

152 The mass conservation is described by the continuity equation with the Boussinesq approximation of
153 incompressibility.

154
$$\frac{\partial v_x}{\partial x} + \frac{\partial v_y}{\partial y} = 0 \quad (eq. 1)$$

155 and the equation for conservation of momentum with an incompressibility assumption is expressed in the 2D-
 156 stokes equation, for the x -axis and y -axis, respectively,

157
$$\frac{\partial \sigma_{xx}}{\partial x} + \frac{\partial \sigma_{xy}}{\partial y} = \frac{\partial P}{\partial x} \quad (eq. 2)$$

158
$$\frac{\partial \sigma_{yy}}{\partial y} + \frac{\partial \sigma_{xy}}{\partial x} = \frac{\partial P}{\partial x} - g\rho(T, P, C, M) \quad (eq. 3)$$

159 Where density $\rho(T, P, C, M)$ depends on temperature (T), pressure (P), composition (C), and mineralogy (M).

160 The thermal equation used in the model is as follows:

161
$$\rho C_P \frac{DT}{Dt} = \frac{\partial q_x}{\partial x} + \frac{\partial q_y}{\partial y} + H_r + H_a + H_s + H_l \quad (eq. 4)$$

162 where,

163
$$q_x = -k(T, C, Z) \frac{\partial T}{\partial x}, \quad q_y = -k(T, C, Z) \frac{\partial T}{\partial y} \quad (eq. 5)$$

164
$$H_a = T\alpha \frac{DP}{Dt}, \quad H_s = \sigma_{xx}\dot{\epsilon}_{xx} + \sigma_{yy}\dot{\epsilon}_{yy} + \sigma_{xy}\dot{\epsilon}_{xy} \quad (eq. 6)$$

165 Where $\frac{D}{Dt}$ is the Lagrangian time derivative, and x and y denote the horizontal and vertical coordinates, respectively;

166 σ_{xx} , σ_{xy} , σ_{yy} are components of the deviatoric stress tensor; $\dot{\epsilon}_{xx}$, $\dot{\epsilon}_{xy}$, $\dot{\epsilon}_{yy}$ are components of the strain rate tensor;

167 P is pressure; T is temperature; q_x , q_y are the components of heat flux in the horizontal and vertical direction; ρ is

168 density; g is the vertical gravitational acceleration; C_p is the isobaric heat capacity; H_r, H_a, H_s, H_l , denote the
169 radioactive, adiabatic, shear and latent heat production, respectively. $k(T, C, Z)$ is the thermal conductivity, a
170 function of composition, depth, and temperature (Table 1).

171 In order to accurately assess thermal maturity, it is crucial to consider the temperature distribution, which
172 necessitates a realistic thermal conductivity profile when modeling thermal maturity. Many geodynamic models
173 assume that thermal conductivity decreases as temperature increases, following a defined relationship (e.g., Clauser
174 and Huenges, 1995). These models typically predict a decrease in thermal conductivity with depth within
175 accretionary wedges, as geothermal profiles tend to increase in temperature with depth. However, empirical data
176 reveal a different trend: thermal conductivity increases with depth, primarily due to sediment porosity influencing
177 shallow thermal conductivity (Henry et al. 2003, Lin et al. 2014). Additionally, the thermal conductivity values
178 calculated using the Clauser and Huenges model (1995) are significantly higher than those observed at shallow
179 depths (< 3 km). To address these disparities, we incorporate the observed empirical relationship between depth
180 and thermal conductivity from the IODP Site C0002 borehole in the Nankai accretionary wedge into our
181 simulations. By adjusting the thermal conductivity formulation for sediments based on temperature and depth, we
182 aim to replicate the empirical relationship observed in the core samples taken from the borehole at IODP Site C0002
183 (Sugihara et al., 2014) and account for the decrease in thermal conductivity near the surface caused by increased
184 porosity. We modify the thermal conductivity formulation for sediments as a function of temperature and depth as
185 follows.

$$186 \quad k_{sed} = k_0 + \frac{807}{T + 77} \left(1 - \exp\left(\frac{-Z^2}{1.3e^7}\right) \right) \quad (eq. 6)$$

187 $k_0 = 0.96$ and 1.5 for the wedge sediment and décollement respectively. The larger thermal conductivity of the
 188 décollement emulates higher heat transfer in shear zones due to fluid advection (Fig. S1).

189 **3.2 Rheological model**

190 The expression for effective creep viscosities (η_{eff}) is computed as follows

$$191 \quad \eta_{disl} = 0.5(\dot{\epsilon}_{II})^{\frac{1}{n}-1} A_D^{\frac{1}{n}} h^m \exp\left(-\frac{E_a + V_a P}{nRT}\right) \quad (eq. 7)$$

$$192 \quad \eta_{diff} = 0.5 \frac{A_D}{S^{n-1}} \exp\left(-\frac{E_a + V_a P}{RT}\right) \quad (eq. 8)$$

$$193 \quad \eta_{eff} = \left(\frac{1}{\eta_{disl}} + \frac{1}{\eta_{diff}}\right)^{-1} \quad (eq. 9)$$

194 where P is pressure (Pa), T is the temperature (K), R is the gas constant (8.314 J/K/mol), h is grain size (m) and,
 195 A_D, n, m, E_a and V_a are experimentally determined rheological parameters: A_D is the material constant
 196 ($\text{Pa}^{-n} \text{s}^{-1} \text{m}^{-m}$), n is the stress exponent, m is the grain size exponent, E_a is activation energy (J/mol), V_a is activation
 197 volume (J/Pa), and S is a stress factor for diffusion creep. As dislocation creep does not depend on grain size,
 198 therefore, we assume $h^m = 1 \cdot \dot{\epsilon}_{II}$ is the second invariant of strain tensor computed as

$$199 \quad \dot{\epsilon}_{II} = \sqrt{\frac{\dot{\epsilon}_{ij} \cdot \dot{\epsilon}_{ij}}{2}} \quad (eq. 10)$$

200 The model uses visco-plastic rheology to account for both brittle rheology of the shallower and colder rigid
 201 lithosphere and deeper, hotter ductile lithosphere and asthenosphere. Using the plastic yield threshold as per the
 202 Drucker-Prager criterion we limit effective viscosity as

203
$$\eta_{eff} \leq \frac{P \cdot \sin\varphi \cdot (1 - \lambda) + C \cdot \cos\varphi}{2\varepsilon_{II}} \quad (eq. 11)$$

204 Where c is cohesion and φ is an effective internal angle of friction or $\mu = \tan \varphi$ where is the coefficient of internal
 205 friction and λ the fluid pressure ratio.

206 **3.3 Boundary conditions**

207 A free-slip boundary condition is implemented on all boundaries, except on the lower boundary, which is passable
 208 in the vertical direction. Where we implement, an external free slip condition similar to where a free slip condition
 209 is satisfied at an external boundary such that

210
$$\frac{\partial V_x}{\partial x} = 0, \text{ and } \frac{\partial V_y}{\partial y} = \frac{V_y}{\Delta Y_{external}} \quad (eq. 10)$$

211 Where, V_x and V_y , are the velocities in the horizontal and vertical directions at the boundary, $\Delta Y_{external}$ is the depth
 212 that lies outside the modeling domain, and where free slip condition is maintained. Similarly, we set thermally
 213 insulating boundary conditions on all sides except the lower one where the external thermal boundary condition is
 214 implemented.

215 **3.4. Surface processes**

216 The rock-water/air boundary is simulated by an adaptive irregular grid that is advected horizontally and vertically
 217 and is coupled to the thermomechanical grid which controls the tectonic change of the surface. Apart from the
 218 tectonic changes, surface processes prescribed in the model can also change the topography. The surface process
 219 in the model is controlled by the conversion of rock markers to air/water and vice versa. All sedimentation in the

220 model happens as a focused deposition of sediments from sea to land in morphological depressions (e.g., trench)
221 is modelled as follows (Fig. S2)

$$222 \quad Y_{new} = Y_{old} + K * Y_{fill} \quad (eq. 11)$$

223 Where, $K = \min \left(\frac{V_{budget}}{V_{basin}}, 1 \right)$

224 The shape of the basin and the resolution of the surface grid can lead to overfilling or underfilling when using the
225 equation mentioned above to fill the basin. To address this issue, we calculate the volume of deposited sediments
226 and adjust for any deficit or overfill in the subsequent step. This ensures that, over time, the total amount of
227 sedimentation remains consistent with the prescribed value. However, it is challenging to ensure that all sediments
228 added in a particular step are accommodated within the basins, especially in models with high sedimentation rates
229 where significant runoff occurs. Therefore, the sedimentation rates mentioned in this study are computed as
230 effective sedimentation rates after the model runs, rather than being predetermined. We perform multiple models
231 runs (approximately 100) with sedimentation rates uniformly distributed in the range of 0.1-0.9 mm/yr. From these
232 runs, we select models that exhibit appropriate sedimentation rates. This selection process ensures that the average
233 sedimentation rates across all our models (ranging from 0.1-0.9 mm/yr) fall within the observed sedimentation rates
234 in our chosen natural equivalent, the Nankai accretionary wedge in the southwestern subduction margin of Japan
235 (Korup et al., 2014). For more specific information about the model run and prescribed sedimentary conditions,
236 please refer to Table 2

237 ***3.5 Thermal maturity calculation***

238 The model computes the %R_o of each marker to estimate the thermal maturity of sediments during the model run
239 using three widely used methods of thermal maturity modelling Easy%R_o (Burnham and Sweeney, 1989, Sweeney

240 and Burnham 1990), Simple% R_o (Suzuki et al., 1993) and Basin% R_o (Nielsen et al., 2017). All the models
241 presented here employ a simplified parallel Arrhenius reaction model, which accommodates an array of activation
242 energies for every component of the kerogen, allowing it to estimate thermal maturity under varying temporal and
243 thermal scales. The Easy% R_o model by Sweeney and Burnham (1990) can be described using the following
244 equations:

$$245 \quad x_i(t) = x_{oi} \exp\left(-\int A \exp\left(-\frac{E_{ai}}{RT(t)}\right) dt\right) \quad (eq. 12)$$

$$246 \quad X(t) = \sum_{i=1}^N x_i(t) \quad eq. 13$$

$$247 \quad F(t) = X(t = 0) - X(t) \quad (eq. 14)$$

$$248 \quad \%R_o = \%R_{o0} \exp(3.7F) \quad (eq. 15)$$

249 Where, x_{oi} are weights of reactions for i^{th} component of the kerogen also described as the stoichiometric coefficient,
250 A is the pre-exponential factor, E_{ai} is the activation energy of the i^{th} component of the kerogen, R is the gas constant,
251 $T(t)$ is the temperature history, F is the amount of fixed carbon as a percentage and $\%R_{o0}$ is the vitrinite reflectance
252 of the immature unaltered sediment. Sweeney and Burnham (1990) provided a set of 20 activation energies (E_{ai})
253 and the stoichiometric coefficient (x_{oi}) listed in Table 3. All thermal models used in this study use the same method
254 of vitrinite reflectance computation albeit with different sets of activation energies, stoichiometric coefficient, pre-
255 exponential factor and $\%R_{o0}$. Table 3 provides a comprehensive list of all these parameters.

256 All these approaches for computing % R_o yield similar trends albeit with different absolute values. In the interest of
257 clarity, we have mostly illustrated Easy% R_o , which is the most extensively used method for Vitrinite Reflectance

258 computation and hereafter we refer Easy% R_o as % R_o , unless explicitly stated. % R_o is set to % R_{o0} in sediment
259 markers at the start of the model till 2.5 Myr, while % R_o in markers for other rocks, air, and water is undefined at
260 all times. After 2.5 Myr, the model computes % R_o on each marker as a function of temperature (T), time (t), and
261 amount of fixed carbon as a percentage (F). The initial % R_o of newly deposited sediments is computed using an
262 assumed water-sediment interaction temperature assumed to be the same as the thermocline. The thermocline used
263 in the model has been estimated using the data obtained and made freely available by International Argo Program
264 and the national programs that contribute to it for the region near Nankai (Fig. S3; <https://argo.ucsd.edu>,
265 <https://www.ocean-ops.org>).

266 **3.5 Model Set-up**

267 The modelling domain is 3500 km wide and 350 km deep and is discretized into 3484×401 nodes populated with
268 ~ 125 million markers (Fig. 1). The high resolution of 220 m (horizontal) \times 130 m (vertical) that we assign at the
269 site of accretionary wedge evolution, decreases steadily toward the edges of the modelling domain to a minimum
270 resolution of 3000 m \times 3200 m. The simulation consists of an oceanic plate converging with a velocity of ~ 5 cm/yr
271 and subducting beneath a continental plate (Fig. 1). The oceanic plate consists of a 1-km-thick upper oceanic crust
272 and a 7-km-thick lower crust. The thickness of the oceanic lithosphere depends on its age which is set to 20 Myr at
273 the start of the simulation (Turcotte and Schubert, 2002). The initial age of the oceanic lithosphere corresponds to
274 the age of the subducting lithosphere in the Nankai subduction margin (Zhao et al. 2021). Displacement along the
275 megathrust, at the contact between subducting oceanic plate and the overriding continental plate, occurs in a
276 relatively weak basal layer in accretionary wedges across the globe (Byrne and Fisher, 1990). We simulate this
277 with a predefined configuration at the interplate, with a 350-meter-thick weak décollement below a sediment layer
278 that is a km thick. The wedge forms above this interphase by the accretion of sediments against the continental
279 plate. The continental plate consists of an upper and lower continental crust with thicknesses of ~ 20 km and ~ 15

280 km, respectively, and is underlain by a mantle lithosphere of ~25 km. We use a thin (10 km) "sticky air" layer to
281 overlay the top face of the rock strata inside the model which is a fluid with a low viscosity of 5×10^{17} Pa·s, and a
282 low density, similar to air (white in Fig. 1) or water (light blue in Fig. 1) (Cramer et al., 2012). The transition
283 between the lithosphere and asthenosphere is prescribed to occur at 1300°C. A weak layer is emplaced at the
284 junction of both plates, which fails mechanically and leads to subduction initiation. All sediments (light and dark
285 brown in Fig. 1) are rheologically identical, but colours are alternated in time to allow tracking the development of
286 different geological structures. Readers are referred to Table 1 for the rheological and thermal properties of all the
287 materials used. Note that in our models, we refer to the measure all distances from the point where the continental
288 and oceanic plates initially and is situated 1850 km from the right boundary of the modelling area. The terms
289 "landward" and "seaward" indicate the relative direction towards the continental plate or the oceanic plate,
290 respectively. The "Backstop" refers to the edge of the continental plate that buttresses the wedge and acts akin to
291 an indenter for the accretionary wedge. The "forearc high" represents the highest point in the forearc zone, which
292 includes both the accretionary wedge and the forearc basin.

293

294 **3.6 Experimental Strategy**

295 Here, we present a total of 10 models that vary in their effective basal friction or their effective sedimentation rate
296 to discern patterns of thermal maturity evolution in wedge sediments. Models $M_0^{4.5} - M_0^{14.5}$ have no sedimentation
297 and effective internal angle values for the décollement of $\varphi_b = 4.5^\circ, 7^\circ, 9.5^\circ, 12^\circ$ and 14.5° respectively. The chosen
298 range of effective decollement strength is well within the range of values postulated by several studies for the
299 Nankai accretionary wedge (Tesei et al., 2015). The rest of the models ($M_{0.1}^{9.5} - M_{0.9}^{9.5}$) and have a medium-strength
300 décollement and variable effective sedimentation rate ranging from 0.1 to 0.9 mm/yr. In all the models presented
301 in this study, sedimentation is limited to the trench, extending from the sea to the land. Restricting sedimentation
302 to the trench allows us to observe and analyse the length and frequency of thrust sheets, enabling comprehensive

303 investigation of their role in determining sediment trajectories. With these models, we evaluate the particle
304 trajectory and %R_o of accreting sediments as a function of décollement strength and sedimentation rate. To restrict
305 the number of parameters influencing our observations, models have no erosion. Moreover, all models lack surface
306 processes during the first ~2.5 Myr and have sedimentation thereafter. Sediments used in the model have an angle
307 of friction (φ) of 30° and a strain-softened value of 20° after a threshold of 0.5-1.5 strain. The coefficient of friction
308 ($\tan \varphi$) increases linearly between the strain thresholds.

309 **4. Results**

310 In our models, subduction begins at 0.1 Myr by failure of the weak material between continental and oceanic plate
311 (Fig. 2, Fig. S4-S13 , also [see supporting information movies](#)). Continued and sustained accretion of sediments
312 against the deforming continental crust forms the accretionary wedge from the interplate contact landwards. After
313 ~5 Myr, all models develop a distinct wedge in agreement with the critical wedge theory (Davis et al., 1983).
314 Surface slopes, measured by fitting a line in the surface of the wedge for every timestep between 2.5-7.5 Myr and
315 reported as mean \pm standard deviation, increase systematically, as effective basal friction increases from ~4.5° to
316 ~14.5° (Fig. 1, Fig S4-S13, Table 2, $M_0^{4.5} - M_0^{14.5}$). Whereas models with a relatively weaker décollement, as
317 ($M_0^{4.5}, \varphi_b = 4.5^\circ$), have surface slopes of $0.95^\circ \pm 0.3^\circ$, models with very strong décollement, as ($M_0^{14.5}, \varphi_b = 14.5^\circ$),
318 have slopes as steep as $5.9 \pm 1^\circ$ (Table 2). Our estimations of surface slopes consistently exhibit an excess of
319 approximately 1.5° compared to the surface slopes predicted by the critical wedge theory (Table 2). This is probably
320 due to the penetration of weaker decollement material into high shear zones, resulting in faults that are weaker than
321 the strain-softened wedge material.

322

323 Models without trench sedimentation grow solely by accretion of incoming seafloor sediments, with frequent
324 nucleation of frontal thrusts. Models with weaker décollements develop thrust sheets that are lengthier but remain

325 active for shorter periods. This is clear when comparing, for models with increasingly strong décollement
326 ($M_0^{4.5}, M_0^7, M_0^{9.5}, M_0^5, M_0^{14.5}$), the average distance between first and second frontal thrusts are 15.5 ± 7.0 km, 12.1
327 ± 3.6 km, 8.8 ± 3.3 km, 8.7 ± 2.1 km and 8.0 ± 1.8 km, respectively. Increasing sedimentation rate also leads to an
328 increase in thrust sheet length from 7.3 ± 1.1 km for model $M_{0.1}^{9.5}$ to 13.8 ± 7.8 km in model $M_{0.9}^{9.5}$.

329

330 In models with similar basal friction, models with higher sedimentation rates have lengthier thrust sheets that
331 remain active for longer periods (Table 2). Steeper surface slopes with increased décollement strengths and change
332 in thrust sheet length with sedimentation and décollement strength are well-known effects that have been
333 confirmed by previous numerical and analytical (Malavieille and Trullenque, 2009; Storti and McClay, 1995)
334 models. All the reported values are mean \pm Standard Deviation values recorded between 2.5-7.5 Myr in individual
335 models. All models exhibit a temperature gradient that corresponds well with the temperature profile observed in
336 the boreholes at IODP Site C0002 in the Kumano forearc basin, on top of the Nankai accretionary wedge (Fig.
337 S14).

338

339 *4.1 Thermal maturity of the wedge*

340 Sediments are more thermally mature in wedges that have a higher sedimentation rate or décollement strength. For
341 example, the mean %R₀ of simulations for wedges with the highest sedimentation is 12% higher (0.75) than in
342 those without sedimentation ($M_0^{4.5}$, Table 2, Fig. 3). Similarly, simulations of wedges with the strongest
343 décollement have the highest mean %R₀ (0.94) of all the simulations presented in this study.

344 Thermal maturity values increase with depth and landward distance from the trench to the forearc high
345 irrespective of the décollement strength, sedimentation rates and method of thermal maturity computation (Fig. 3-
346 4). The absolute value of %R₀ and the rate at which thermal maturity values increase landward from the trench are

347 larger for wedges with high décollement strength (Fig. 4A). For wedges characterized by the same décollement
348 strength but higher trench sedimentation, we observe that the rate of thermal maturity increases in a landward
349 direction from the trench and remains consistent across these wedges (Fig. 4B). Comparing the values of %R_o
350 along a horizontal marker at the depth of trench in several models emphasizes this result; the model with the highest
351 décollement strength reaches a maximum %R_o of 1.25 and has the highest rate of landward increase in thermal
352 maturity (Fig. 4A). However, all models with similar décollement strength but different sedimentation do not
353 visibly vary in their rate or magnitude of landward increase in thermal maturity. All models show a decrease in
354 thermal maturity landward of the forearc high, commonly of 0.2 %R_o. Other interesting observations that we
355 explore below are the increased thermal maturity occurring in the vicinity of thrusts and the reversal in sediment
356 maturity around out-of-sequence thrust active over longer times visible across several models (e.g. Fig. 3).

357 The magnitude of %R_o varies consistently among Easy%R_o, Simple%R_o and Basin%R_o. On average
358 Easy%R_o have the smallest values, followed very closely by Basin%R_o (with an average difference of only 0.02).
359 However, Simple%R_o had the highest average value of thermal maturity, being 0.16 and 0.13 higher than Easy%R_o
360 and Basin%R_o (Fig. 3).

361 *4.2 Sediment trajectory inside the wedge*

362 In wedges with a higher décollement strength or sedimentation rate, sediments tend to follow high-maturity paths
363 in larger proportions. We demonstrate this effect by creating a map of the thermal maturity of sediments at 7.5 Myr
364 of the model run, mapped to their spatial position at 2.5 My of the model run to analyse the spatial correlation
365 between sediment position (depth and distance) from the trench and thermal maturity (Fig. 5). We also show the
366 mean thermal maturity attained by sediments at a given horizontal distance from the trench during this period by a
367 dashed black line in Fig. 5. The scatter plot shows sharp changes in eventual thermal maturity with horizontal

368 distance from the trench that relate to changes in sediment trajectory. The mean thermal maturity is also variable
369 along the horizontal length of the wedge and has a periodicity (Λ) increasing in distance with higher sedimentation
370 rate but relatively constant with changing basal friction (Fig. 5). The periodicity of mean %R_o was computed by
371 finding the average wavelength of the auto-correlated mean %R_o. Whereas the mean thermal maturity has a short
372 periodicity of ~7.2 km for the model $M_0^{9.5}$ with no sedimentation rates, the model $M_0^{9.5}$ shows the longest periodicity
373 of 21 km. However, for all models with no sedimentation ($M_0^{4.5} - M_0^{14.5}$), the periodicity remains relatively
374 consistent between the range of 7-8 km.

375 Fig. 3 also represents the distribution of trajectories that exist in an accretionary wedge and how these
376 trajectories get impacted under trench sedimentation (a subset of these trajectories can be viewed in the
377 supplementary Fig. S15). Whereas in wedges with weak décollements ($M_0^{4.5}$), none of the shallowest half of
378 incoming sediments reach %R_o > 1 in 5 Myr, 2% of sediments reach this value in wedges with strong décollement
379 ($M_0^{14.5}$). The effects of décollement strength in the thermal maturity of sediments can be quantified as well at deeper
380 levels, with one-eighth vs more than half of the sediments surpassing values of %R_o = 1 for the deepest half of
381 incoming sediments (12% and 54% respectively) in weak vs strong-decollement wedges ($M_0^{4.5}$ vs $M_0^{14.5}$),
382 respectively. In wedges for the model without sedimentation ($M_0^{9.5}$), the top half of the incoming sediments
383 fail to achieve %R_o > 1, as opposed to ~ 15% of them reaching %R_o > 1 in the models with a sedimentation rate
384 of 0.9 mm/yr ($M_0^{9.5}$). In sum, the proportion of sediments in the top half and bottom half of the wedge that reach
385 high maturity steadily increases with both sedimentation rate and décollement strength (Table 2).

386 ***4.3 Patterns of trajectory and thermal maturity in incoming sediments***

387 The diversity in the trajectory of sediments in the wedge leads to a plethora of pathways in which the sediments
388 can become thermally mature and thus introduces epistemic uncertainty in the estimation of maximum exposure

389 temperature. Fig. 6, captures this uncertainty where we plot the maximum exposure temperature as a function of
390 %R_o for all the models simulated in this study. The colours in for individual markers represent the depth of the
391 markers normalized by the thickness of the wedge represented as Y_n (See Fig S16 for mode details). We find that
392 almost all the models show a remarkable similarity in their relationship between maximum exposure temperature
393 and %R_o (for individual models please see Fig. S16) and differ mostly in their proportion of sediments with extreme
394 values of %R_o. We observe that the typical uncertainty in maximum exposure temperature increases with an
395 increase in values of %R_o with ~ 15°C interval at around %R_o=0.2 compared to ~33°C interval at %R_o= 3 (both for
396 95% confidence interval, Fig. 6b). Moreover, we observe that incorporating information about the normalized depth
397 of sediments (Y_n) significantly aids in constraining the maximum exposure temperature. For instance, although the
398 overall uncertainty at %R_o=1, is ~23°C, for sediments with a Y_n of 0.2-0.4, the uncertainty greatly reduces to only
399 ~10.5°C. Thus, the range of thermal maturity values for sediments clearly has a large correlation with their
400 trajectories.

401 ***4.4 Comparison of Easy%R_o, Simple%R_o and Basin%R_o***

402 The usage of Easy%R_o, Simple%R_o, and Basin%R_o in our models provides us with a distinct perspective on the
403 comparative (dis)advantages of each method in estimating thermal maturity values. The non-uniqueness of
404 maximum exposure temperatures for the same values of %R_o arises from the variation in sediment trajectory and
405 thermal exposure. This diversity among sediment markers results in multiple markers attaining the same level of
406 thermal maturity. We refer to the range of maximum exposure temperatures corresponding to similar %R_o values
407 as the uncertainty in maximum exposure temperatures. Uncertainty for all three models increases with increasing
408 %R_o from ~20–25°C at ~0.3 to ~35°C at %R_o=3.5 (Fig. 6b). Easy%R_o, probably the best-recognised method of
409 thermal maturity computation, yields the best constraint on uncertainty for very small changes nearing <1 values.
410 For the values of %R_o between 1 and 3, all models yield very similar uncertainty, with Simple%R_o yielding the

411 most constrained exposure temperatures (Fig. 6b). However, beyond $\%R_o = 3$, Simple $\%R_o$ becomes unreliable, with
412 uncertainty in exposure temperatures as high as 55°C at $\%R_o = 4$. Easy $\%R_o$ yields an uncertainty range of ~37°C
413 till $\%R_o = 4.4$, and starts to be unreliable above this value. Basin $\%R_o$ remains consistent until a very high value of
414 $\%R_o \sim 6$, and thus provides the best constraint on the widest range of values of thermal maturity (Fig. 6b).

415 **5. Discussion**

416 The thermomechanical models presented in this study provide (a) an explanation for the trend in thermal maturity
417 observed in accretionary wedges, (b) a new venue to explore the uncertainty in the estimation of maximum exposure
418 temperature using vitrinite reflectance, and (c) an estimate of the minimum lateral distance between the trench and
419 the location of a paleo-thermal anomaly on the subduction plate for it to be identified after accretion.

420

421 ***5.1 Thermal maturity distribution and importance of thrusting in wedges***

422 Collectively, our results support a general increase of thermal maturity with depth and landward in accretionary
423 wedges. The thermal maturity increase with depth is primarily the result of progressively larger exposures to higher
424 temperatures as depth of burial increases. On the contrary, the landward increase in thermal maturity is caused by
425 the long-term deformation of sediments accumulated at older times and the exhumation of sediments that were
426 underthrust as they meet the backstop. Our models demonstrate that the rate of landward thermal maturity
427 increase is faster for thicker wedges, both for the case of sediment near the surface and deep inside the wedge (Fig.
428 4). This can be attributed to a larger proportion of sediments being exposed to higher temperatures over an extended
429 duration within thicker wedges, but validating this result with natural observations remains challenging, given to
430 the very limited availability of thermal maturity data across natural wedges. Accretionary wedges in our models
431 can be simplified as a system where the subducting oceanic plate acts as the primary heat source, while the seafloor
432 acts as a heat sink. The heat generated through other sources such as shear heating, radioactivity, and advection is

433 relatively insignificant compared to the heat originating from the younger oceanic plate. In our simulations, we
434 consider a relatively younger and hotter oceanic plate of approximately 20 Myr, which is consistent with the
435 accretionary wedge in the Nankai region adjacent to the Kumano forearc basin (Zhao et al., 2021). Given that the
436 convergence rate remains constant across all models, the heat received from the oceanic plate should remain
437 relatively similar. However, as the wedge thickness increases, the temperature gradient between the boundaries of
438 the wedge must become gentler, resulting in a larger portion of the wedge experiencing elevated temperatures.
439 Moreover, frequent advection from the subduction channel also results in elevated temperatures in the core of the
440 wedge. Finally, models with thicker wedges typically exhibit higher décollement strength, leading to increased
441 shear heating at the base of the wedge. Observational studies conducted by Yamano et al. (1992) on the thermal
442 structure of the Nankai accretionary prism have further highlighted that the landward increase in prism thickness
443 is the most significant factor contributing to temperature variations within the wedge. Consequently, the sustained
444 higher temperatures within thicker wedges over time would lead to a higher rate of landward thermal maturity.

445 Our models show two cases where the above-mentioned trend in thermal maturity is relevantly altered, which we
446 nominate "on-fault increase" and "fault-block inversion". For instance, Fig. 3 shows a steep rise in the thermal
447 maturity of sediments at fault sites. Thermal maturity inversions by thrusting, which are commonplace in
448 accretionary contexts, are the primary cause of thermal maturity differentiation among wedges with similar paleo-
449 thermal structures. During fault-block inversions, the positive gradient of thermal maturity with depth is inverted
450 as relatively mature sediments are thrust over less mature sediments (Underwood et al., 1992). The strong
451 differentiation in the trajectory of sediments led by thrusting has a larger influence over thermal maturity than their
452 burial depth or their in-wedge location. This novel inference has probably remained concealed thus far due to the
453 large number of parameters that condition thrust development, frequency, length, and thermal state and the lack of
454 high-resolution thermal maturity data.

455 The thermal maturity that incoming sediments reach also varies periodically as a function of thrust frequency. By
456 examining the lateral and vertical position of incoming sediments and their eventual thermal maturity, we can
457 deduce that the overall movement of sediments in the wedge is predominantly layered but not stationary over time.
458 Changes in the depth of the thermal maturity boundary are less frequent and have larger amplitudes with increased
459 décollement strength, and especially, increased sedimentation rates (Fig. 5). The periodicity in the thermal maturity
460 boundary marks the periodic oscillation of the predominant trajectory followed by incoming sediments, i.e. between
461 accretion (low thermal maturity path) and under-thrusting (high-thermal maturity path). As a result, it should also
462 strongly correlate with the periodicity observed in the evolution of forearc topography (Menant et al., 2020) and
463 the frequency of thrust formation in our models. This is expected, given that thrusts are active over longer mean
464 times, and they channel material toward the décollement more efficiently, in wedges with stronger décollement or
465 increased sedimentation. While sediments at internal and higher structural positions of the wedge are translated
466 toward the surface and have a lower thermal maturity, sediments at external and lower structural positions are
467 translated toward the décollement and have a relatively higher maturity. The entire cycle is repeated with the
468 formation of new in-sequence thrust.

469 This is a relevant observation for it typifies the causality of particular sediment grains following a high or low
470 maturity path, a long-standing unanswered question (Miyakawa et al., 2019). We corroborate this observation by
471 analyzing the terminal thermal maturity of sediments across a frontal thrust active at a younger age. An example in
472 Fig. 7 shows the thermal maturity of sediments at ~ 7.5 Myr across a thrust active at ~ 4 Myr. Whereas this occurs
473 for all thrusts in the wedge, the frontal thrust is particularly pronounced in partitioning sediments into the high and
474 low maturity paths. Thermal maturity correlates with sediment depth weakly near faults and more strongly away
475 from them. The distance of sediment from the frontal thrust dictates the trajectory of sediment grains, and as a
476 result, the pressure-temperature conditions to which they are exposed.

477 Our results show the need to consider all factors influencing fault frequency when inferring the geothermal history
478 of contractional terrains by means of thermal maturity. In this study, we have considered solely how décollement
479 strength and the rate of trench sedimentation vary the frequency, architecture, and overall behavior of thrusts, and
480 the frontal thrust, as the wedge evolves. Fortunately, this predictive exercise should be relatively straightforward,
481 for the impact of these external factors on the fault structure of wedges has been established (Fillon et al., 2012;
482 Mannu et al., 2016, 2017; Mugnier et al., 1997; Simpson, 2010; Storti and McClay, 1995), and the effect of each of
483 these factors can be accounted for when assessing the trajectory of sediments and the distribution of thermal
484 maturity in accretionary wedges. It is nevertheless important to note that the frequency of faults in a wedge can be
485 impacted by many other factors, including hinterland sedimentation (Storti and McClay, 1995; Simpson, 2010;
486 Fernández-Blanco et al. 2020), erosion (Konstantinovskaia, 2005; Willett, 1992), and seafloor topography
487 (Dominguez et al., 2000).

488 ***5.2. Implications***

489 The main implications of this contribution emerge from its predictive power. Our approach can predict to a precise
490 degree the thermal maturity of sediments and the uncertainty associated with the maximum exposure temperature
491 in accretionary contexts with known structuration. A more accurate quantification of the thermal evolution and
492 thermal state of accreted sediments reduces the uncertainties attached to the location of temperature-led
493 transformations of organic material into hydrocarbons in subduction margins and other accretionary contexts. Such
494 increased accuracy in the distribution of thermally mature sediments may also be applied for improved assessments
495 of the evolution in time of any other geothermal process, including seismic slip, magmatic and metamorphic extent,
496 porosity, compaction, and diagenesis of sediments, and the reconstruction of convergent margins in general
497 (Bostick and Pawlewicz, 1984; Mählmann and Le Bayon, 2016; Rabinowitz et al., 2020; Sakaguchi et al., 2011;
498 Totten and Blatt, 1993; Underwood et al., 1992).

499 Our simulations also imply that the paleo-thermal information stored in the incoming sediments can only be
500 retrieved if sediments are at appropriate locations with respect to emergent thrusts. We illustrate this using two runs
501 of the same model and tracking an artificial thermal anomaly imposed on incoming sediments at two different
502 locations (Fig. 8). This hypothetical thermal anomaly can be conceptualized as any alteration of the thermal
503 maturity profile of incoming sediments, for example, elevated heat flows by an antecedent magmatic intrusion.
504 While the change in %Ro associated with the short-lived thermal anomaly results in abnormally high values of
505 thermal maturity in both sediment packages, it can only be retrieved for the end-model run of sediments located
506 further from the trench (those in the right panel, Fig. 8B). Contrarily, the end-model run of sediments closer to the
507 trench (those in the left panel, Fig. 8A) shows no signs of discontinuity in the thermal maturity distribution of the
508 wedge. This is because we deliberately placed the thermal anomaly at sites that evolve at two structural locations
509 during the model run, i.e., above and below a yet-undeveloped frontal thrust (Fig. 8). The sediment sector affected
510 by the thermal anomaly closer to the trench is overthrust by the frontal thrust and remains in a footwall location
511 thereafter (Fig. 8a). In contrast, the homologous sedimentary package further away from the trench is accreted by
512 the frontal thrust and remains in a hanging-wall location (Fig. 8b). Thus, the preservation of the record of an
513 antecedent thermal anomaly is only possible in the former case. We further note that, in our simulations, the entire
514 vertical column of sediments records the thermal anomaly, while in nature, the anomaly may affect only sediments
515 at the deeper locations of the sedimentary pile, which are in turn the sediments that most likely to follow a high-
516 maturity path. We thus regard the possibility of retrieving such antecedent geothermal information as minimal.

517 Finally, among the three methods of %Ro computation, Easy%Ro and Basin%Ro are more consistent and well-
518 constrained on a wide range of thermal maturities in comparison to Simple%Ro, which seems to be particularly
519 useful for a smaller range of thermal maturity values. This simply illustrates the fact that while Easy%Ro and
520 Basin%Ro computation deals with several parallel reactions related to the maturity of kerogen (and hence multiple

521 activation energies), Simple% R_o is based on best-fitted single activation energy, and hence yields large confidence
522 intervals at the extreme % R_o values. Additionally, the inclusion of the higher activation energy reactions in
523 Basin% R_o makes it the best-suited formulation for sediments at the deeper and shear zone sediments which usually
524 get saturated using Easy% R_o .

525 *5.3 Comparisons to previous numerical studies*

526 The thermomechanical models presented in this study offer a dynamic representation of trajectories within the
527 wedge. Although the averaged trends in thermal structure and sediment trajectories remain consistent, there are
528 short-term dynamic fluctuations near the frontal thrust. These fluctuations contribute to a diverse range of sediment
529 paths along the depth of the incoming sediments. Miyakawa et al. (2019) conducted a similar study, modeling
530 vitrinite reflectance using Simple% R_o and a stationary thermal field, which also resulted in an increase in thermal
531 maturity towards the continent and thermal maturity inversions due to thrusting. However, the use of Simple% R_o
532 led to premature saturation and the disappearance of thermal maturity variations at a shallower depth in their model.

533 We can compare our findings with other geodynamic models that examine the thermal structure of the wedge,
534 although there are only a limited number of numerical models of thermal maturity in wedges. Pajang et al. (2022)
535 recently investigated the distribution of the brittle-ductile transition in wedges and proposed a region dominated by
536 viscous shear near the backstop, with the wedge core reaching temperatures of 450°C and typically containing
537 forearc basins. Although trench sedimentation in our model does not result in the formation of forearc basins, the
538 overall flattening of the wedge slope and the high vitrinite reflectance in the core align with consistent structures.
539 Moreover, the presence of highly mature sediments in the wedge core suggests compacted sediments with greater
540 strength and higher P-wave velocity. Although empirical studies have shown a strong correlation between V_p and
541 thermal maturity estimates for depths of up to 4 km (Baig et al, 2016, Mallick et al. 1995), the exact nature of this

542 correlation may vary depending on the specific location. Nevertheless, the patterns of thermal maturity values in
543 the wedge core in our models also correspond to the patterns of P-wave velocity observed in the Nankai and
544 Hikurangi margins (Górszczyk et al., 2019; Nakanishi et al., 2018; Dewing and Sanei, 2009; Arai et al., 2020).

545 Two modes of sediment trajectory evolution, from incoming sediment to their position inside the wedge, are
546 generally considered; depth dependence sediment trajectories, as observed in studies by Mulugeta and Koyi, (1992)
547 and Hori and Sakaguchi (2011), and crossover exhumation pathways, as illustrated by Konstantinovskaia et al.
548 (2005) and Miyakawa (2019). We consider the latter as non-stationary sediment trajectories that vary with time
549 and cut across sediment trajectories of sediments previously located at the same spatial position. Our models show
550 that both modes of sediment trajectories are valid, and that changes in trajectory patterns leading to path crossovers
551 are controlled by the horizontal distance of sediments from the frontal thrust. Starting at a threshold distance from
552 the trench, sediments at different depths follow laminar paths along different trajectories within the wedge.
553 Laminar-type trajectories can be reproduced in a broad range of simulations and are particularly common in models
554 with low sedimentation and décollement strengths. However, the depth dependence of sedimentary paths varies
555 periodically as a function of distance from the trench of specific sedimentary packages (Fig. 5). This effect, which
556 is particularly marked in the neighbourhood of the frontal thrust, explains the crossover paths for incoming
557 sedimentary packages at similar depths but different horizontal locations (Konstantinovskaia et al. 2005).
558 Therefore, thrust faults in the wedge act as the primary agent controlling whether sediments sustain depth-
559 controlled laminar flow or sediment mixing.

560 ***5.4 Comparisons to natural wedges***

561 Our models achieve thermal maturity distributions that are in good agreement with their natural analogues, despite
562 several relevant assumptions. Our models are very simplified with regard to their natural analogues, with
563 assumptions such as no elasticity, predefined décollement, no erosion, and simple and uniform rheology. Also, our

564 models have an insufficient resolution for small-scale fault activity and lack empirical relations to simulate the
565 compaction of sediments and multiscale fluid flow. Although these assumptions hinder a wholesale comparison
566 between our simulations and natural examples of accretionary wedges, we still find an acceptable agreement
567 between our model and natural observations, primarily due to simulations that have a temperature evolution
568 assimilating empirical data and a fine spatiotemporal resolution. Our estimated %R_o values for the model are in
569 very good agreement with those measured for the borehole C0002 Nankai accretionary wedge by Fukuchi et al.
570 2009 (Fig. 9). The maximum exposure temperature estimated from the observed thermal maturity for the C0002
571 borehole also strongly correlates with maximum temperatures recorded on markers in the model with similar
572 thermal maturity with 95% confidence (Fig. S17). However, our result is reliant on the empirical thermal
573 conductivity profiles estimated for the C0002 borehole, which does not show any large thermal discontinuity
574 between the forearc basin and inner wedge that has been observed in fossil accretionary wedges (e.g., Underwood
575 et al. 1989).

576 Landward increase in thermal maturity is well documented in studies of the Japan trench, at the Miura–Boso plate
577 subduction margin, the fold and thrust belts Western Foothills complex in western Taiwan, the Mesozoic
578 accretionary prism in the Franciscan subduction complex in northern California, as well as Cretaceous Shimanto
579 accretionary complex in Nankai subduction margin (Yamamoto et al. 2017; Sakaguchi et al. 2007; Underwood et
580 al, 1989; Sakaguchi, 1999). The natural wedges mentioned above display vitrinite reflectance values with
581 maximum %R_o values ranging from 0.2 to 4.0 near the surface, which is generally much higher than the near-
582 surface %R_o values observed in our models. Underwood et al. (1989) suggested that this discrepancy is likely due
583 to the ongoing process of progressive exhumation and erosion, leading to the exposure of deeper sections of the
584 accretionary prism over time. As a result, younger wedges, such as those found in the Miura–Boso plate subduction
585 margin, exhibit a much closer resemblance to the %R_o values near the surface of our our models.

586 On-fault increases in vitrinite reflectance are well also documented in nature, as for boreholes C0004 and C0007,
587 which sample the megasplay fault in Nankai accretionary margin (Sakaguchi et al., 2011). The vitrinite reflectance
588 data from the megasplay and frontal thrusts in Nankai indicate the faults reach a temperature well in excess of
589 300°C during an earthquake, much larger than the background thermal field. Therefore, on-fault increases in
590 thermal maturity are comparatively smaller in our simulations and lack the marked increase in %Ro observed at
591 fault sites in nature. We consider this is due to a discrepancy in the rate of change of thermal diffusion occurring
592 in simulated thrusts, given that our models develop much wider fault zones than their natural equivalents. For
593 instance, the location of megasplay fault in C0007 borehole exhibits an unevenness within the high-reflectance
594 zone with a maximum %R_o ~1.9 (Sakaguchi et al., 2011). This is in line with the prediction by Fulton and Harris
595 (2012) about the impact of fault thickness on change in vitrinite reflectance. Natural observations also exhibit a
596 much higher incidence of on-fault increase in thermal maturity compared to our simulations, given that our models
597 do not have sufficient spatial resolution to capture the large number of thin faults that develop inside the wedge.
598 Natural examples of fault-block inversion have been well-documented in natural settings, providing evidence of
599 past thrust activity preserved in the shallower sections of the Nankai accretionary wedge. Sakaguchi (1999) reported
600 the presence of step increments of thermal maturity, similar to increments in vitrinite reflectance in Fig. 3 and 4
601 across the faults. Other examples are the fault block inversion along the Fukase Fault in the Shimanto accretionary
602 wedge (Ohmori et al., 1997) and the inversion beneath the forearc basin in the Nankai accretionary wedge (Fukuchi
603 et al., 2017).

604 Our study highlights that paleo-thermal anomalies that extend laterally beyond the average thrust spacing have a
605 significantly higher likelihood of being retained in the final thermal maturity record of the wedge. This allows
606 several inferences. For example, the subduction of the Cretaceous ridge, as identified by Underwood et al. (1993)
607 and Sakaguchi (1999), must have caused a substantial alteration in thermal maturity during the Kula-Pacific
608 subduction in order to be discernible in vitrinite reflectance records. Likewise, we can anticipate the preservation

609 of the paleo-thermal anomaly near Ashizuri in the southern Nankai wedge, which has high thrust frequency, in
610 contrast to that at the Muroto transect, where thrust sheets are widely spaced. In the case of the accretionary wedge
611 adjacent to the Boso peninsula, Kamiya et al. (2017) proposed the emplacement of an ophiolite complex beneath
612 the Miura group. Our findings indicate that the preservation of the thermal-advection heating event coincided with
613 a decrease in trench sedimentation. This likely led to an increase in the thrust frequency, which facilitated the
614 preservation of the thermal-advection heating event in the thermal maturity data.

615 **6. Conclusion**

616 This study demonstrates how contractional faults alter the paths of sediments as they accrete and how this
617 fundamentally controls the distribution of the thermal maturity of sediments in accretionary wedges and emphasizes
618 the role that sedimentation rate and interplate contact strength have in such distribution. The increased resolution
619 of our approach leads to findings that have relevant implications. For example, the geothermal history that can be
620 retrieved from the thermal maturity of sediments in drills, i.e., at the shallow wedge, provides, at best, an incomplete
621 record that is skewed towards the thermal evolution of sediments near the trench. Coevally, relevant sectors of
622 sediments located further seaward, when not subducted, follow high-maturity paths that overprint their antecedent
623 thermal history. Finally, this study also provides a first-order uncertainty measure for the thermal maturity of
624 sediments based on the diversity in their trajectory.

625

626 **Competing interests**

627 The authors declare that they have no conflict of interest.

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773 **List of Tables**774 **Table 1: Properties for the different materials used for the model runs**

Rock Type	Density (kg/m ³)	Cohesion (MPa)	Angle of friction (°)	Thermal Conductivity (W/ (m K))	Flow law	E (kJ/mol)	n
Water	1000	0	0	20		0	0
Air (Sticky-air)	0	0	0	20		0	0
Décollement	2600	0.001	4.5-14.5	$(1.5+807/(T+77))^*$ $(1-\exp(-Z^2/1.3e7))$	Wet quartzite	154	2.3
Sediments1	2600	1/0.05	30/20*	$(0.96+807/(T+77))^*$ $(1-\exp(-Z^2/1.3e7))$	Wet quartzite	154	2.3
Sediments2	2600	1/0.05*	30/20*	$(0.96+807/(T+77))^*$ $(1-\exp(-Z^2/1.3e7))$	Wet quartzite	154	2.3
Upper Continental Crust	2700	1	31	$0.64+807/(T+77)$	Wet quartzite	300	2.3
Lower Continental Crust	2800	1	31	$0.64+807/(T+77)$	Wet quartzite	300	3.2
Upper Oceanic Crust	3000	1	31	$1.18+474/(T+77)$	Plagioclase An75	300	2.3
Lower Oceanic Crust	3000	1	31	$1.18+474/(T+77)$	Plagioclase An75	300	3.2
Mantle Lithosphere	3300	1	31	$0.73+1293/(T+77)$	Dry olivine	532	3.5
Asthenosphere	3300	1	0.6	$0.73+1293/(T+77)$	Dry olivine	532	3.5
*Strain-softened Cohesion/Coefficient of friction T is Temperature, Z is the depth from the seafloor.							

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778 **Table 2: Model runs and their specific characteristic observations**

Models	φ_b	φ / φ_{ss}	λ	<i>SR</i>	<i>L</i>	$\beta(^{\circ})$	$\alpha(^{\circ})$	α predicted (φ_{ss}/φ) ($^{\circ}$)	<i>D</i>	$\langle R_o\% \rangle$	% <i>top-half</i>	% <i>Bottom-half</i>
$M_0^{4.5}$	4.5°	30°/20°	0	None	123.2±15.7	4.2±0.6	0.95±0.3	0.03±0.2/-1.3±0.3	15.5±7.0	0.54	0.0	12.7
M_0^7	7°	30°/20°	0	None	97.7±9.9	4.9±0.8	2.6±0.8	0.97±0.2/-0.95±0.3	12.1±3.6	0.60	0.0	22.5
$M_0^{9.5}$	9.5°	30°/20°	0	None	77.8±4.8	5.3±0.8	3.7±0.9	2.1±0.4/-0.32±0.3	8.7±2.1	0.67	0.0	31.3
$M_{0.1}^{9.5}$	9.5°	30°/20°	0	0.1	76.1±5.9	5.0±0.9	2.3±0.7	2.3±0.4/-0.12±0.3	7.3±1.1	0.71	0.1	35.3
$M_{0.3}^{9.5}$	9.5°	30°/20°	0	0.3	79.3±8.2	4.9±0.9	2.0±0.5	2.3±0.4/-0.1±0.3	7.8±2.5	0.69	0.1	32.0
$M_{0.5}^{9.5}$	9.5°	30°/20°	0	0.5	79.9±7.4	4.9±0.8	2.1±0.5	2.3±0.4/-0.1±0.2	9.5±4.0	0.71	2.7	34.4
$M_{0.7}^{9.5}$	9.5°	30°/20°	0	0.7	81.3±10.5	5.0±0.9	2.1±0.5	2.3±0.7/-0.11±0.3	9.9±5.0	0.73	4.2	41.5
$M_{0.9}^{9.5}$	9.5°	30°/20°	0	0.9	82.5±11.0	5.0±0.9	2.3±0.7	2.2±0.4/-0.16±0.3	13.8±7.8	0.75	14.6	51.8
M_0^{12}	12°	30°/20°	0	None	71.6±5.0	5.6±1.0	5.1±1.0	3.5±0.6/0.4±0.4	8.8±3.3	0.83	1.2	40.6
$M_0^{14.5}$	14.5°	30°/20°	0	None	62.7±6.0	5.9±1.0	6.7±1.4	5.1±0.8/1.2±0.4	8.0±1.8	0.94	2.0	54.0

φ_b is décollement Strength (internal angle of friction).

φ Sediment Strength.

φ_{ss} Sediment Strength (Strain weakened)/ (internal angle of friction).

SR Average Sediment rate (mm/yr).

λ is pore-fluid pressure ratio.

L Average Length of the wedge (in km) between ~2.5-7.5Myr. Length of the wedge is computed as the distance between trench and backstop(set at 1850 km from the right edge of the modelling domain).

β Average basal dip angle β (in degrees) between ~2.5-7.5Myr measure by fitting a line in the basal surface.

α Average surface slope angle α (in degrees) between ~2.5-7.5Myr measure computing the slope of fitting the best fitted line in the surface.

D Average Distance between the first and second frontal thrust between ~2.5-7.5Myr (in km). The frontal thrust is always identified from the trench. The send thrust is identified by the high strain rate and deviation of the weak décollement material from the trend of oceanic plate.

α predicted (φ_{ss}/φ) is the surface slope predicted using critical wedge theory using the β observed in the model and sediment strength (Initial /Strain weakened).

T Average time a frontal thrust remains active between ~3.5-7.5Myr.

$\langle R_o\% \rangle$ Average vitrinite reflectance of the wedge between ~3.5-7.5 Myr.

%*top* Proportion of >1 eventual $R_o\%$ (*vitrinite reflectance at 7.5 Myr*) at shallow half of the incoming sediment at 2.5 Myr.

%*bottom* Proportion of >1 eventual $R_o\%$ (*vitrinite reflectance at 7.5 Myr*) at deep half of the incoming sediments.

*Please see Fig. S18 for details on the various measurement done on the wedge.

780 **Table 3: Parameters for Easy% R_o , Simple% R_o and Basin% R_o vitrinite reflectance model.**

S. No.	Stoichiometric Coefficient for Easy% R_o (x_{0i_Easy})	Activation Energy for Easy% R_o (kJ/mol) (E_{ai_Easy})	Stoichiometric Coefficient for Simple% R_o (x_{0i_Simple})	Activation Energy(E) for Simple% R_o (E_{ai_Simple})	Stoichiometric Coefficient for Simple% R_o (x_{0i_Basin})	Activation Energy(E) for Basin% R_o (kJ/mol) (E_{ai_Simple})
1	0.0300	142256	1	1.38e5	0.0185	142256
2	0.0300	150624			0.0143	150624
3	0.0400	158992			0.0569	158992
4	0.0400	167360			0.0478	167360
5	0.0500	175728			0.0497	175728
6	0.0500	184096			0.0344	184096
7	0.0600	192464			0.0344	192464
8	0.0400	200832			0.0322	200832
9	0.0400	209200			0.0282	209200
10	0.0700	217568			0.0062	217568
11	0.0600	225936			0.1155	225936
12	0.0600	234304			0.1041	234304
13	0.0600	242672			0.1023	242672
14	0.0500	251040			0.076	251040
15	0.0500	259408			0.0593	259408
16	0.0400	267776			0.0512	267776
17	0.0300	276144			0.0477	276144
18	0.0200	284512			0.0086	284512
19	0.0200	292880			0.0246	292880
20	0.0100	301248			0.0096	301248
$A_{Easy} = 1e13$ and $\%R_{o0} = 0.2$, $A_{Simple} = 1e13$ and $\%R_{o0} = 0.2$, $A_{Basin} = 9.7029e12$ and $\%R_{o0} = 0.2104$						

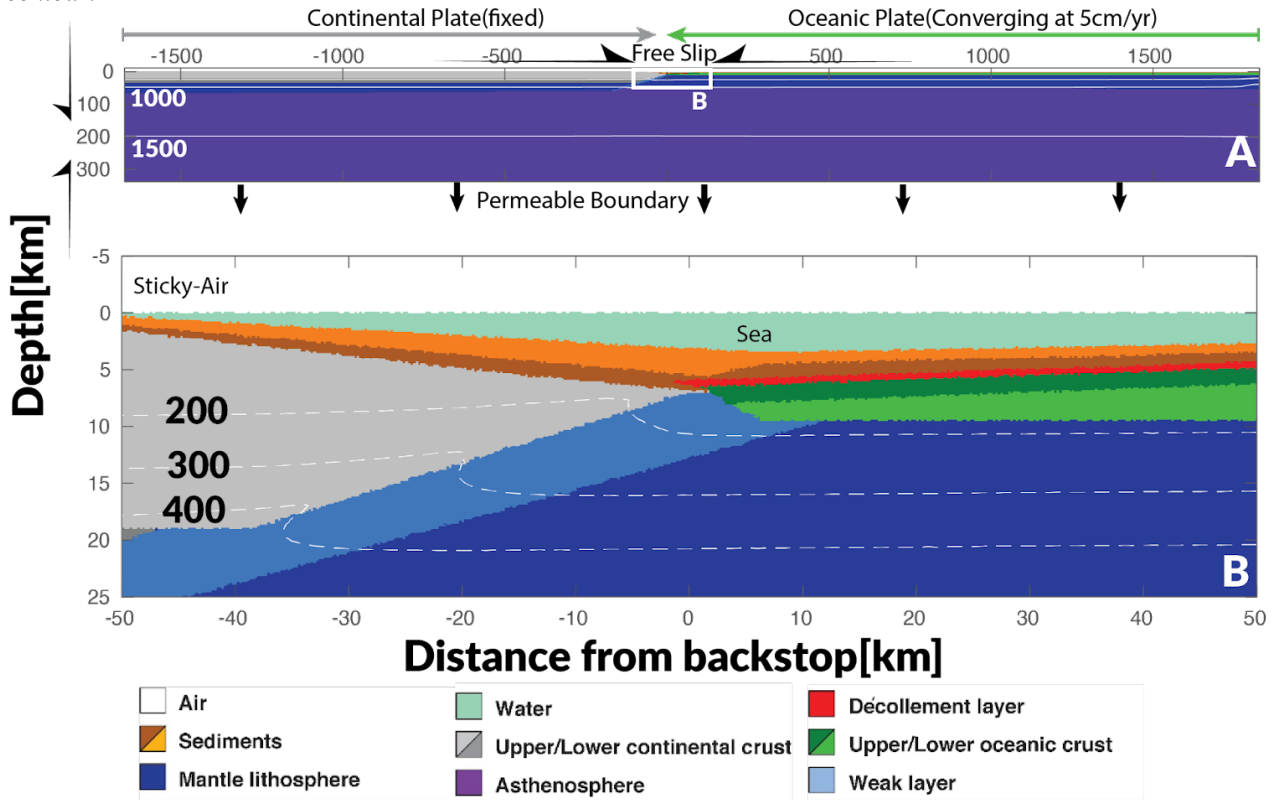
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783 **List of Figures**

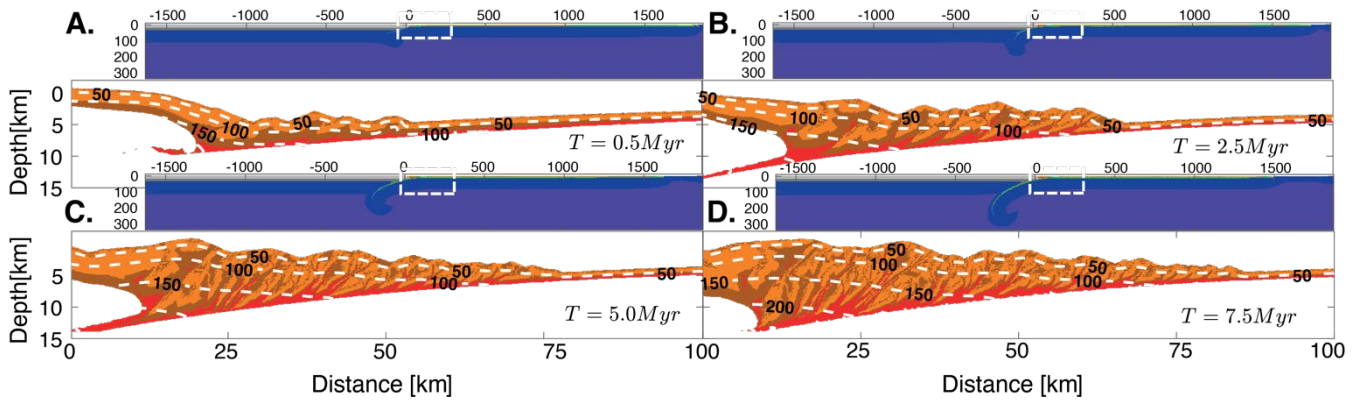
784 **Fig. 1:**

785 *Initial model setup. A. The lithological and geothermal map of the whole computational domain with boundary conditions. B.*
 786 *The zoomed lithological and geothermal map of the inset illustrates the junction of continental and oceanic plates. The colors*
 787 *represent different lithology of the materials used in the models, with upper and lower crust represented by light and dark*
 788 *grey, upper and lower oceanic crust represented by dark and light green. The arrows around the computational domain*
 789 *represent the imposed boundary conditions, while the white contour lines (dashed in the zoomed panel) show the geothermal*
 790 *gradients used for the initial model. The numbers on the white contour lines represent the temperature values in °C for the*
 791 *contour.*



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800 **Fig. 2:**
 801 Typical thermomechanical evolution of the accretionary wedge for model. The illustrated Figure is for the model M_0^7 at (a)0.5
 802 Myr (b)2.5 Myr (c)5.0 Myr (d) 7.5 Myr. Similar Figures for other models have been illustrated in supplementary images. The
 803 colormap for the panels is same as Figure 1.
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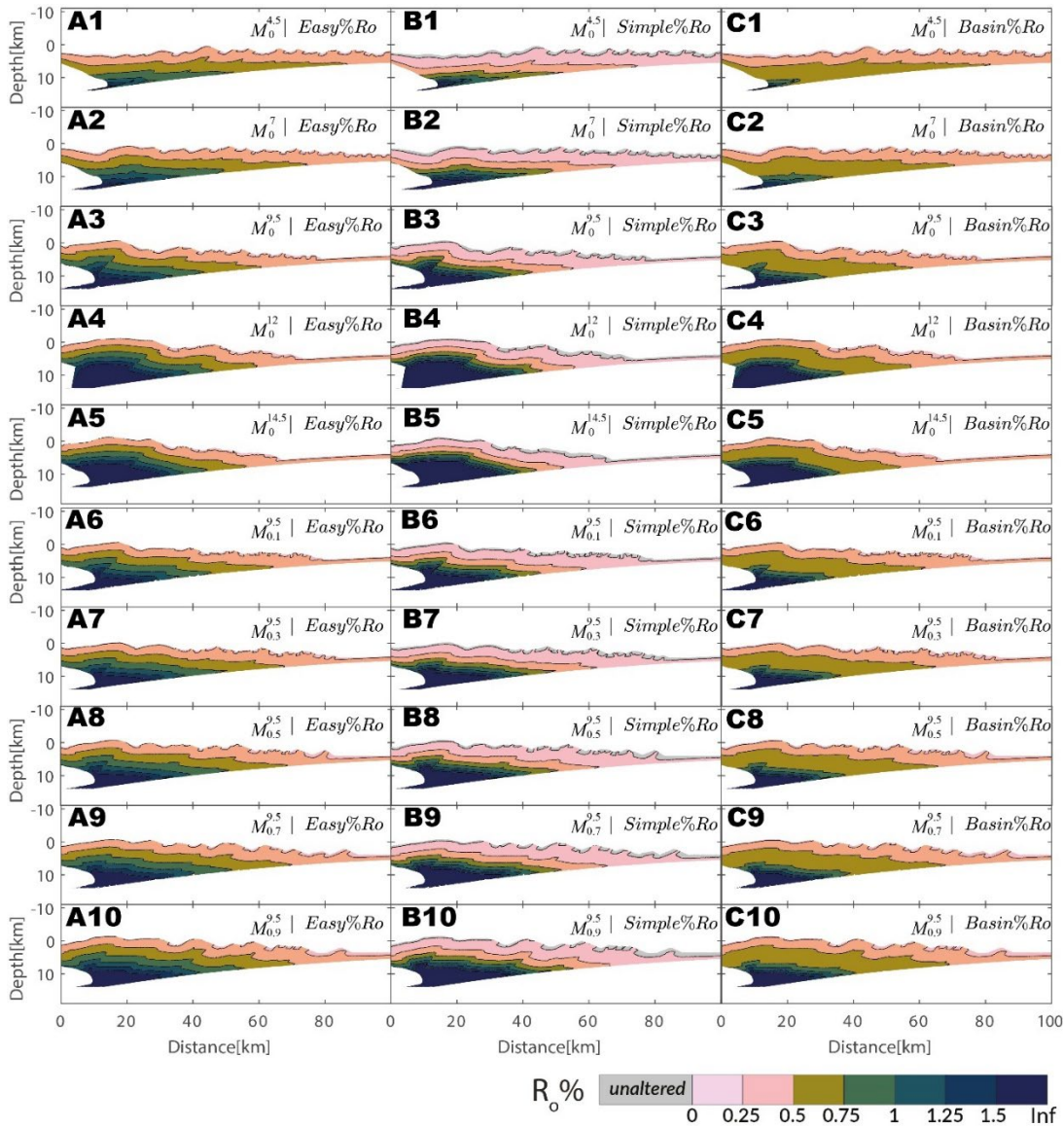
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Fig. 3:

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827 *Distribution of thermal maturity for different models at ~6.0 Myr (3.5 Myr of thermal maturation). Panels A1-A5 show the*
 828 *thermal maturity distribution (computed using Easy%Ro) in subduction wedges of models as a function of décollement strength*
 829 *, respectively. A6-A10 show the thermal maturity distribution in subduction wedges of models function of sedimentation rate ,*
 830 *respectively. The grey color of the markers indicate that no thermal maturity change in these sediments have not occurred.*
 831 *B1-B10 and C1-C10 similarly show the thermal maturity distribution in subduction wedges computed using Simple%Ro and*
Basin%Ro, respectively.

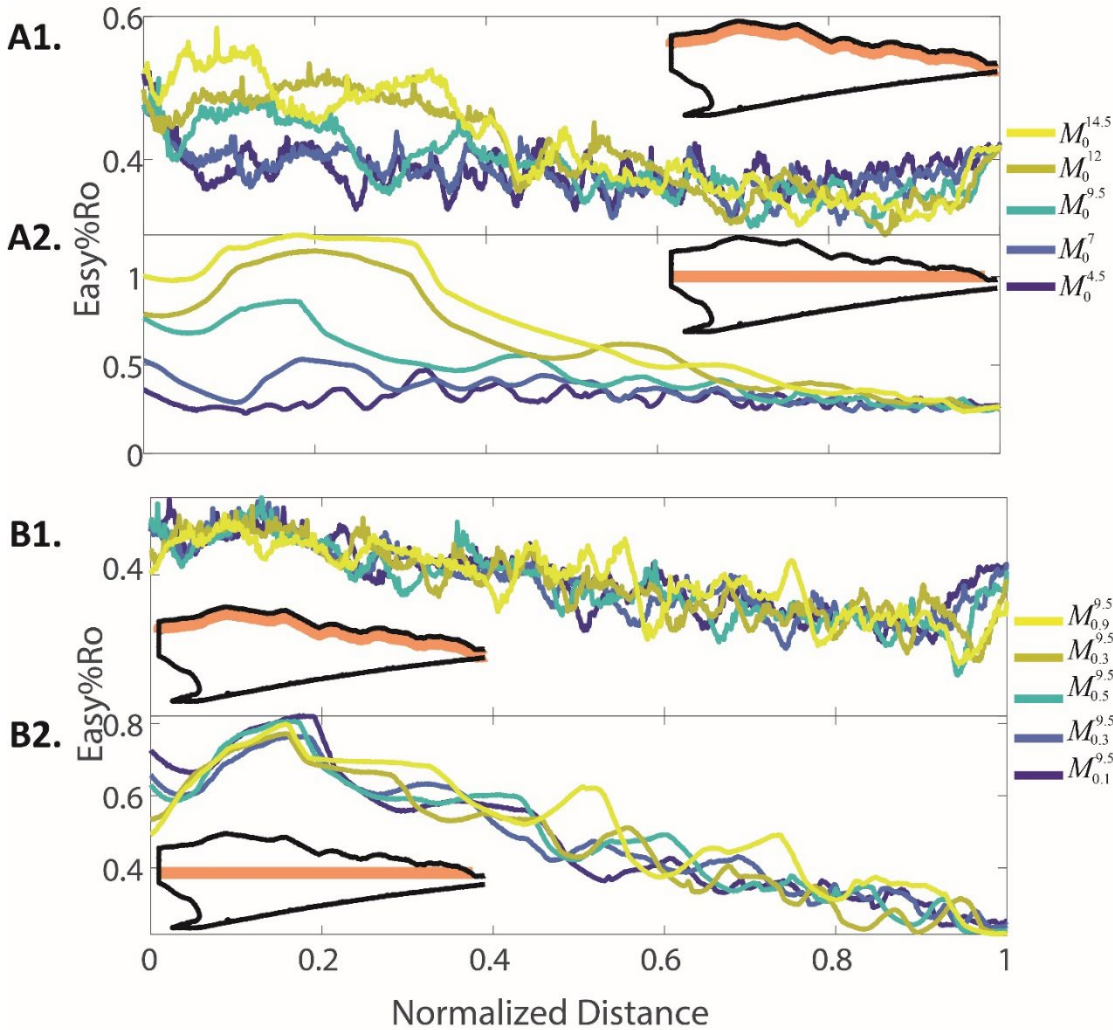
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Fig. 4:

The variation of % R_o for a horizon as indicated by the orange band in the inset at 7.5 Myr. Panel A1 and A2 shows all the models with different decollement strength. Panel B1 and B2 shows all the models with different sedimentation rates. Horizons in panel A1 and B1 are located at 1 km depth from the surface, whole in panel A2 and B2 the horizons are horizontal zones located at the trench depth. The horizontal distance from the backstop is normalized by the wedge length. Horizontal distance 0 represents the fixed backstop and 1 represents the trench.

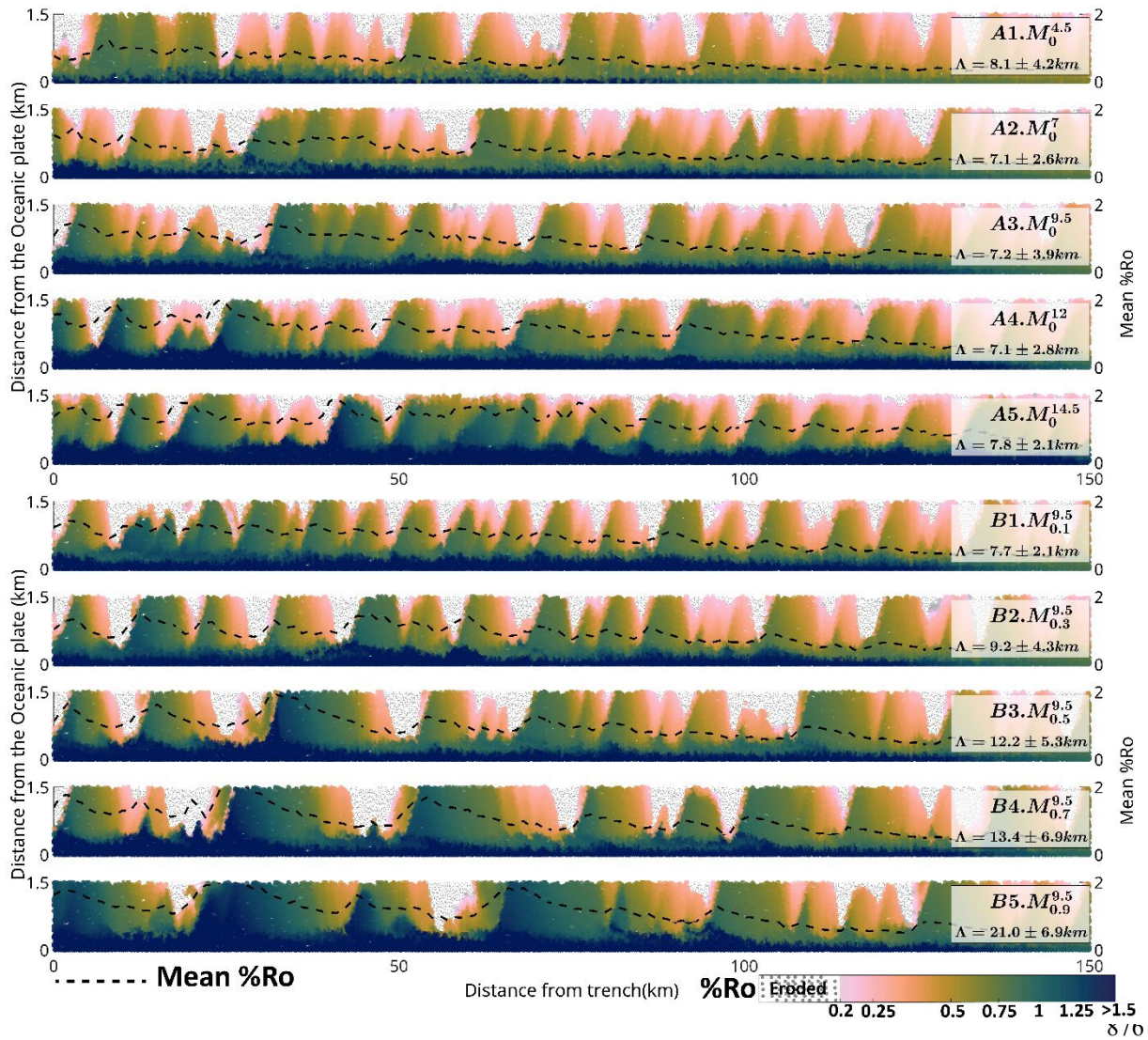


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Fig. 5:

Map of thermal maturity at 7.5 Myr mapped to sediments at 2.5 Myr. Panel A1-A5, B1-B5 show the mapping for models - and - respectively. The vertical axis (distance from the oceanic plate) has been corrected for the bending of the plate. The horizontal axis represents the distance of sediments from the trench. The grey colour of the markers indicates that these sediments have been eroded/reworked due to slope failure. The broken black line represents the mean %Ro attained sediment at a given distance from the trench. Λ represents the horizontal periodicity in mean %Ro for the given model.



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Fig. 6:

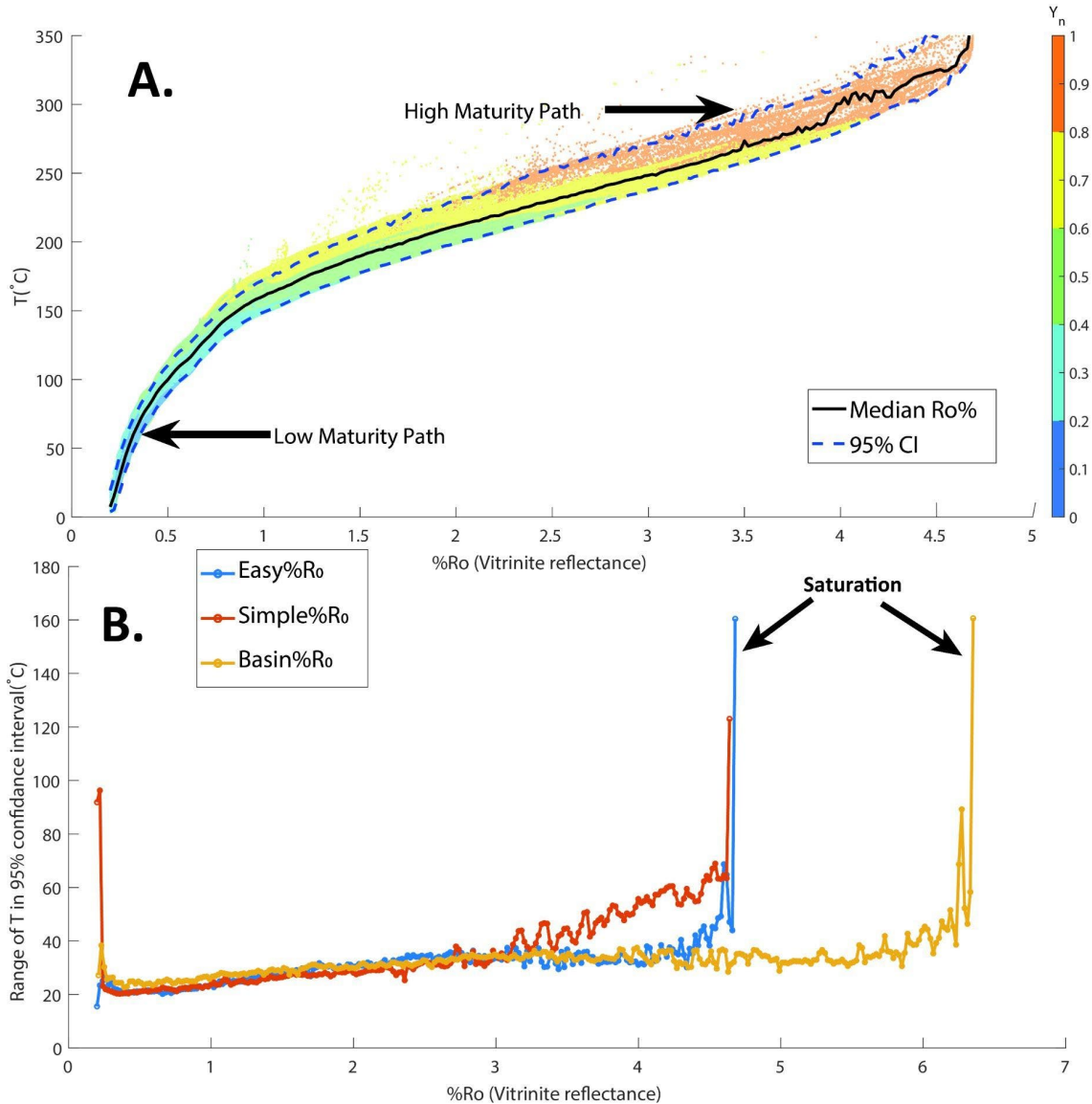
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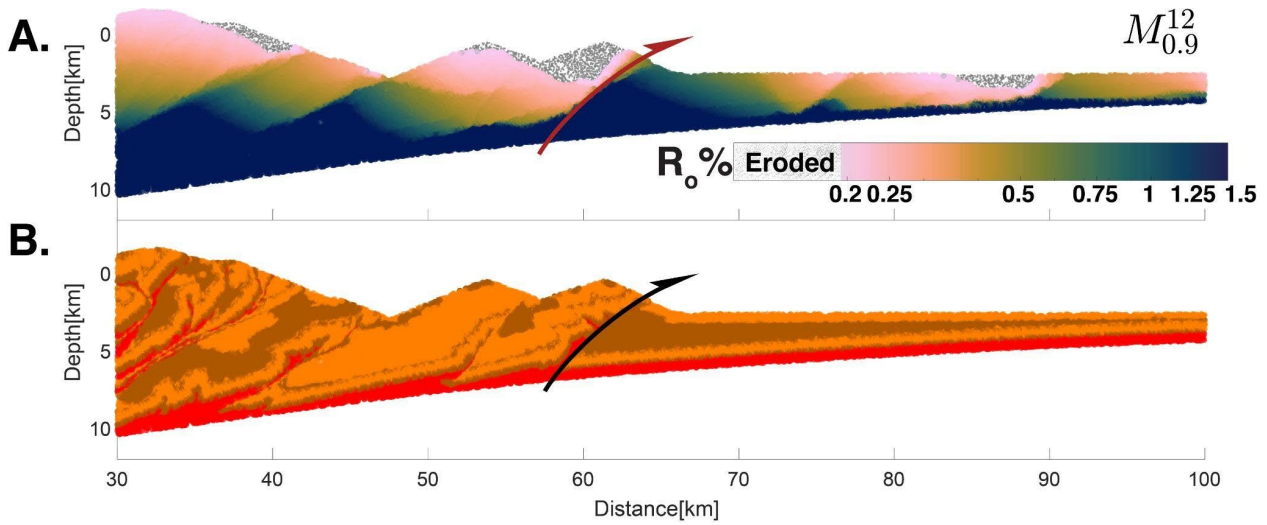
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886 **Fig. 7:**

887 Mapping of eventual thermal maturity (vitrinite reflectance at 7.5Myr) to the location of same markers at ~4Myr in model .
888 Panel A shows the values of thermal maturity for the markers while the lithology of the wedge is shown in panel B. The half
889 arrow represents the active frontal thrust. The sediments which were eroded by 7.5Myr but exist at 4Myr have been markers
890 eroded using dotted grey points.



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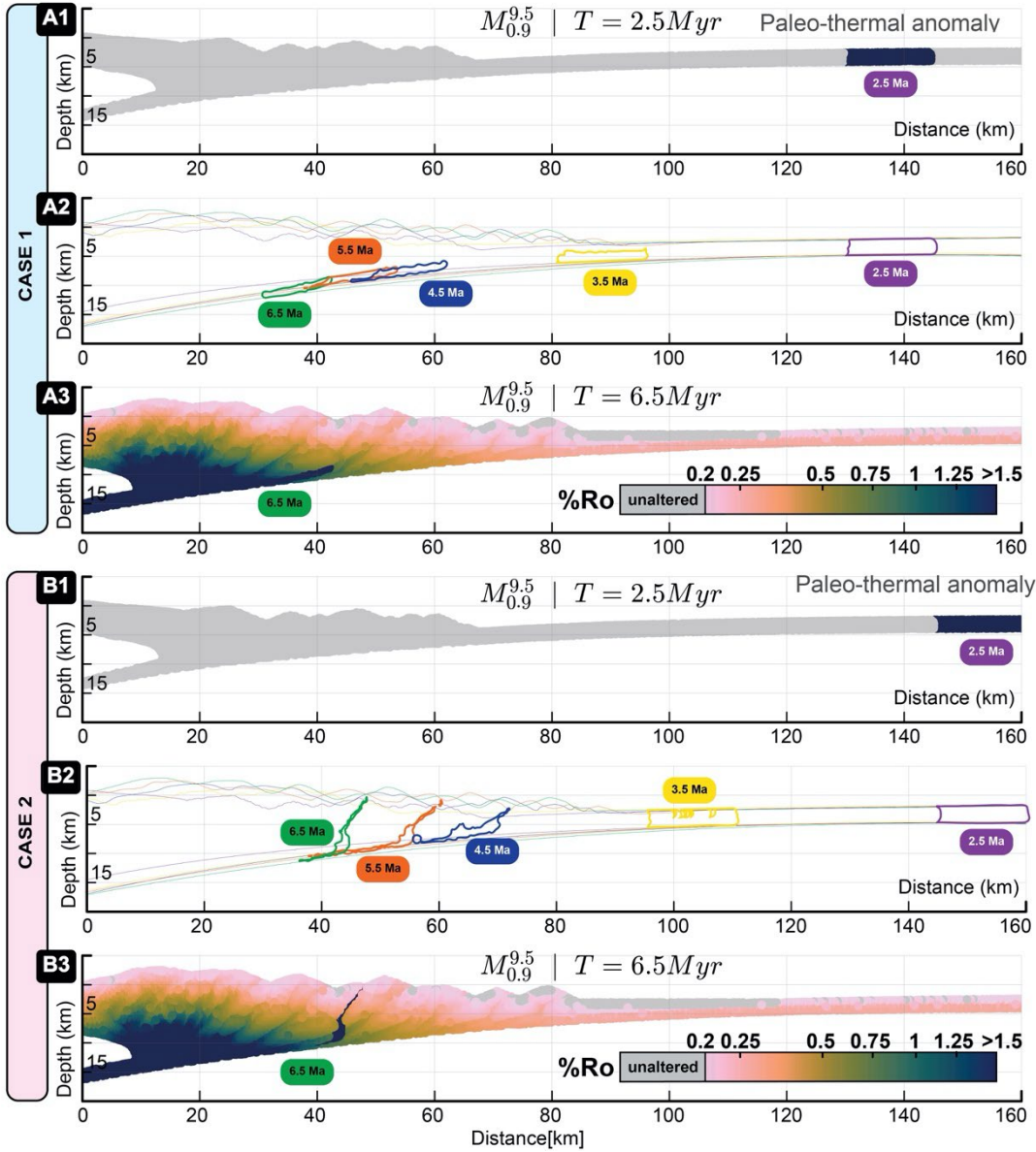
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Fig. 8:

Position dependency of thermal maturity preservation. A1. Distribution of %R₀ at 2.5 Myr with a paleo-thermal anomaly emplaced at 130-145 km from the backstop. A2. The evolution of the emplaced paleo-thermal anomaly from 2.5 Myr to 6.5 Myr in case 1. A3. Distribution of %R₀ at 2.5 Myr. B1. Distribution of %R₀ at 2.5 Myr with a paleo-thermal anomaly emplaced at 145-160 km from the backstop. B2. The evolution of the emplaced paleo-thermal anomaly from 2.5 Myr to 6.5 Myr in case 2. B3. Distribution of %R₀ at 2.5 Myr with a paleo-thermal anomaly emplaced at 145-160 km from the backstop.



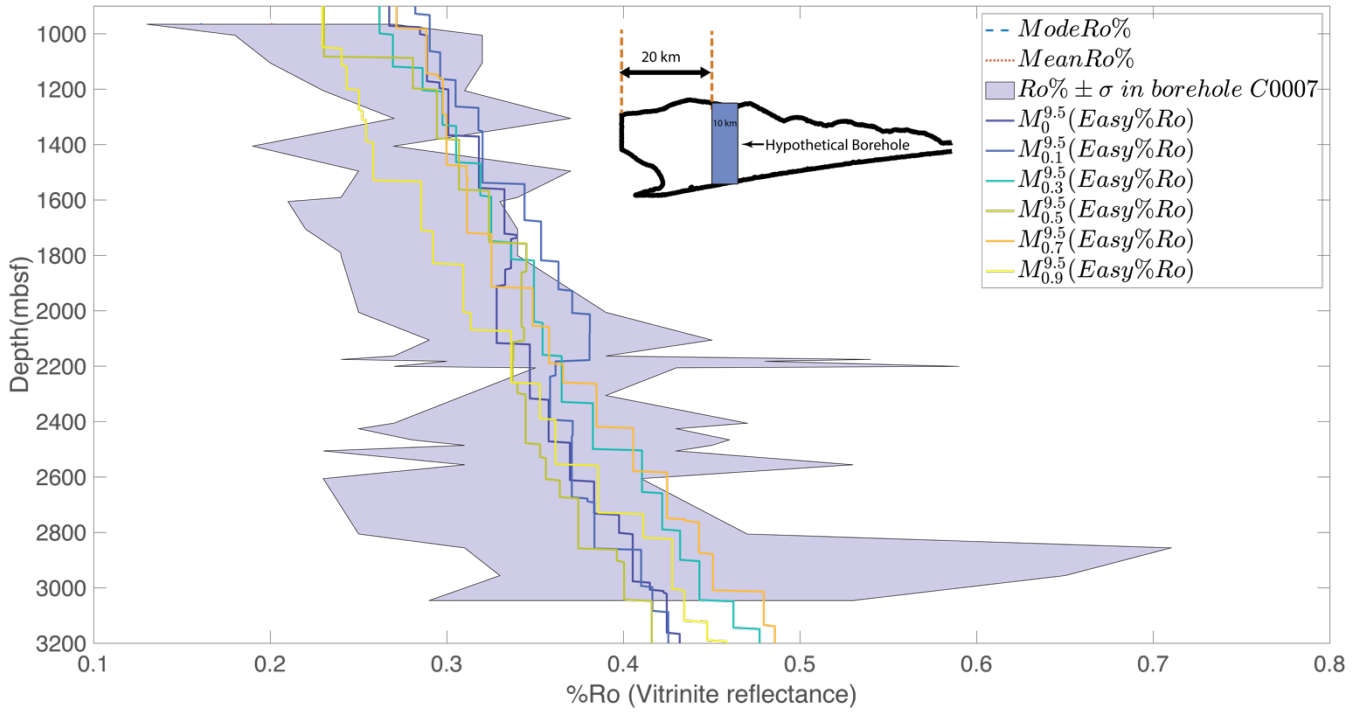
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919 **Fig. 9:**

920 *Depth vs Thermal maturity (%R_o). The shaded (in violet) region shows the range of observed R_o% (mean±1SD) from the C0002*
921 *borehole ,colored lines represent the values in models sampled from a 10 km wide hypothetical borehole 20km seaward of the*
922 *backstop as shown in the inset .*
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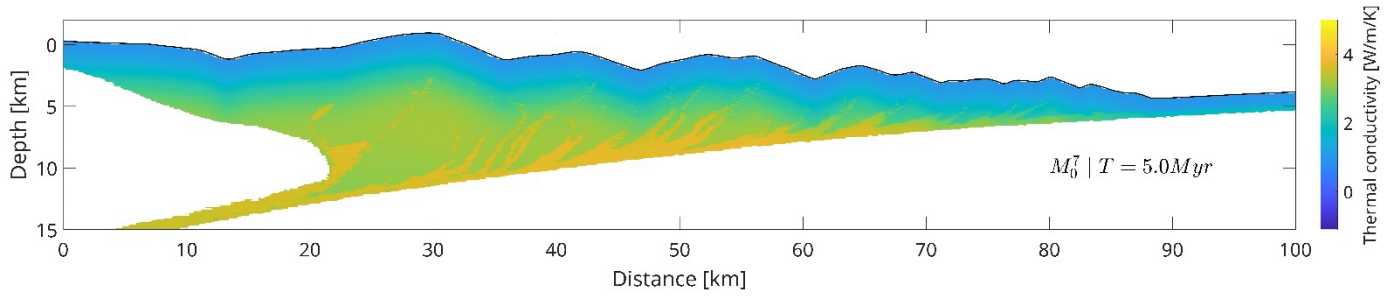
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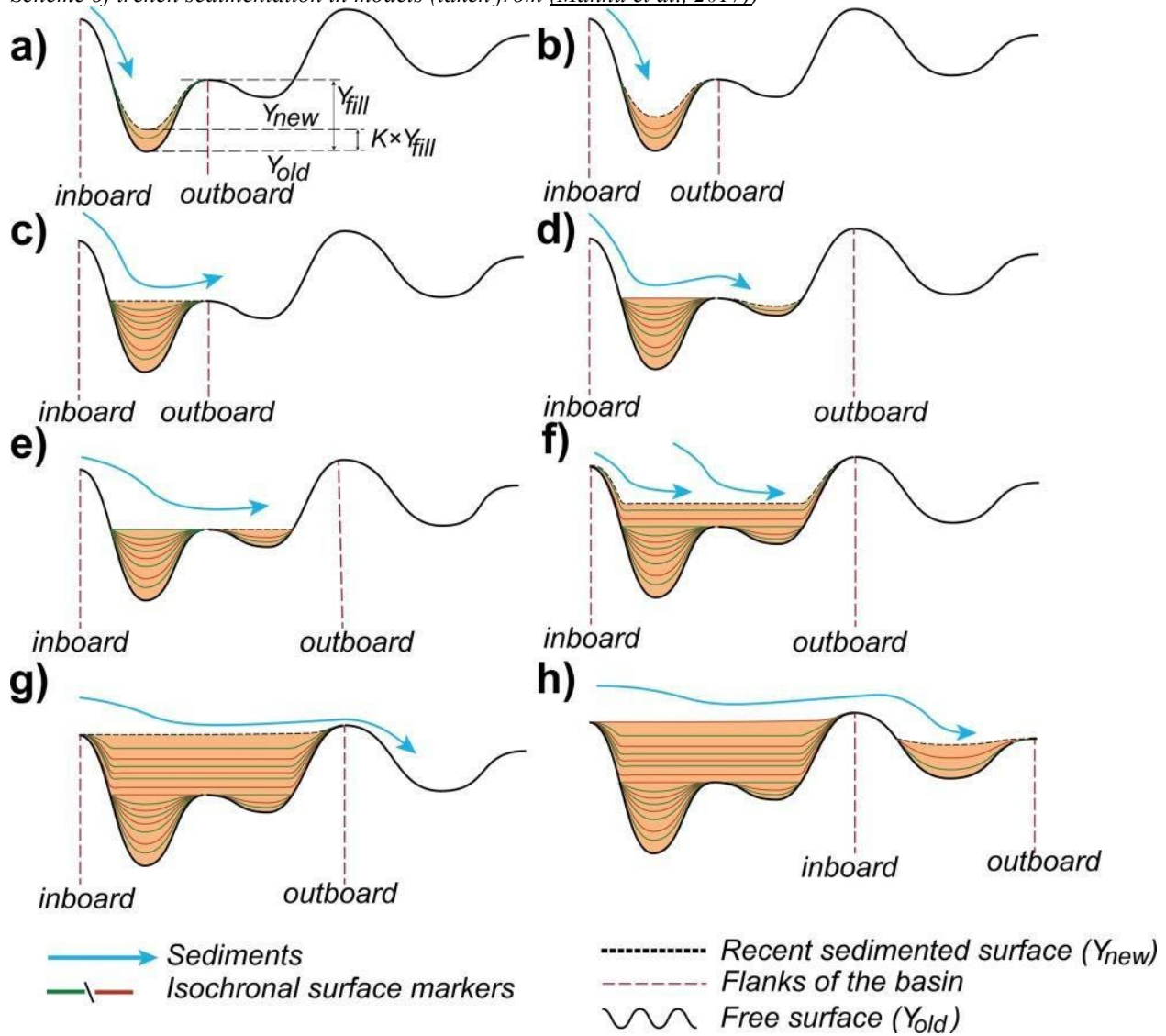
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928 **Supplementary Figures**

929 **Fig. S1:**

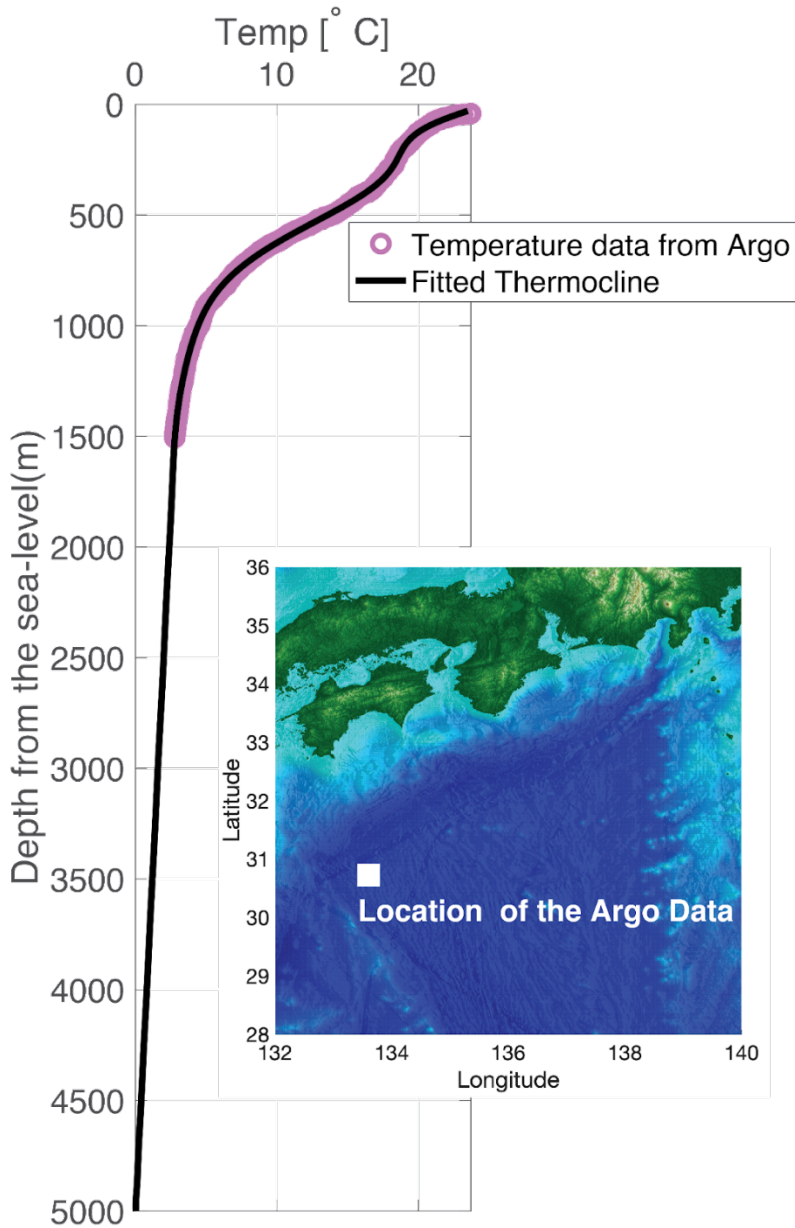
930 *Typical Distribution of thermal conductivity in wedge*





954 **Fig. S3:**

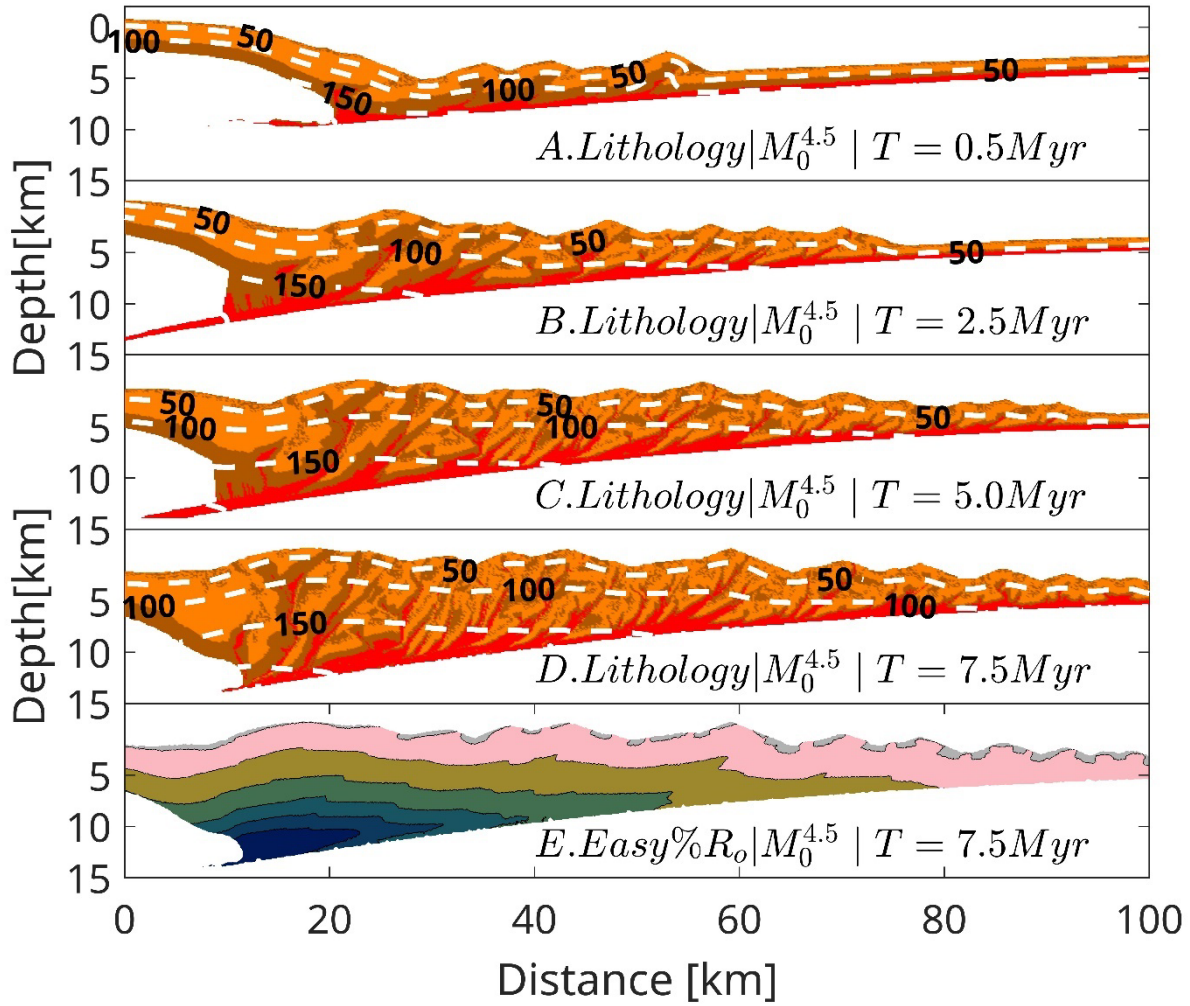
955 *Plot of Temperature vs Depth profile in for water-sediment interaction using the data from the International Argo Program*
956 *and the national programs that contribute for the location(represented by the white square) given in the inset The magenta*
957 *circle represents the Temperature vs Depth profile from the data while the black line is the fitted thermocline used in our*
958 *models for water-sediment thermal interaction.*
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961 **Fig. S4:**
 962 Typical thermomechanical evolution of the accretionary wedge for model $M_0^{4.5}$ at 0.5 Myr, 2.5 Myr, 5.0 Myr and 7.5 Myr of
 963 lithological evolution (Panel A-D). The dashed white lines represent the contours of the temperature field. The colormap for
 964 the first 4 panels is same as Figure 1. The last panel represents thermal maturity values at ~ 7.5 Myr computed using Easy%Ro.
 965 The colormap for Panel E is same as that of Figure 3.
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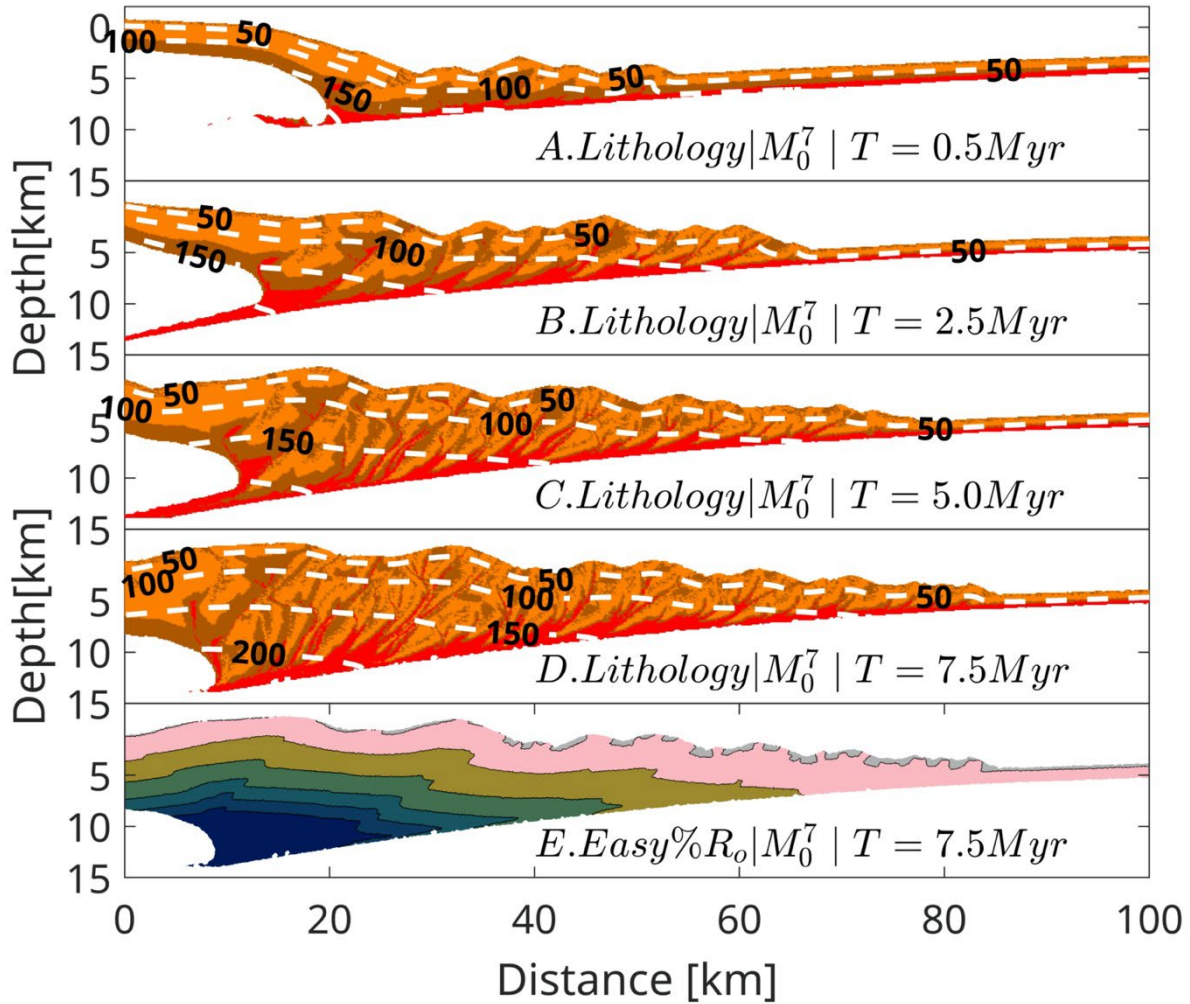
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972 **Fig. S5:**
 973 Typical thermomechanical evolution of the accretionary wedge for model M_0^7 at 0.5 Myr, 2.5 Myr, 5.0 Myr and 7.5 Myr of
 974 lithological evolution (Panel A-D). The dashed white lines represent the contours of the temperature field. The colormap for
 975 the first 4 panels is same as Figure 1. The last panel represents thermal maturity values at ~ 7.5 Myr computed using Easy% R_o .
 976 The colormap for Panel E is same as that of Figure 3.
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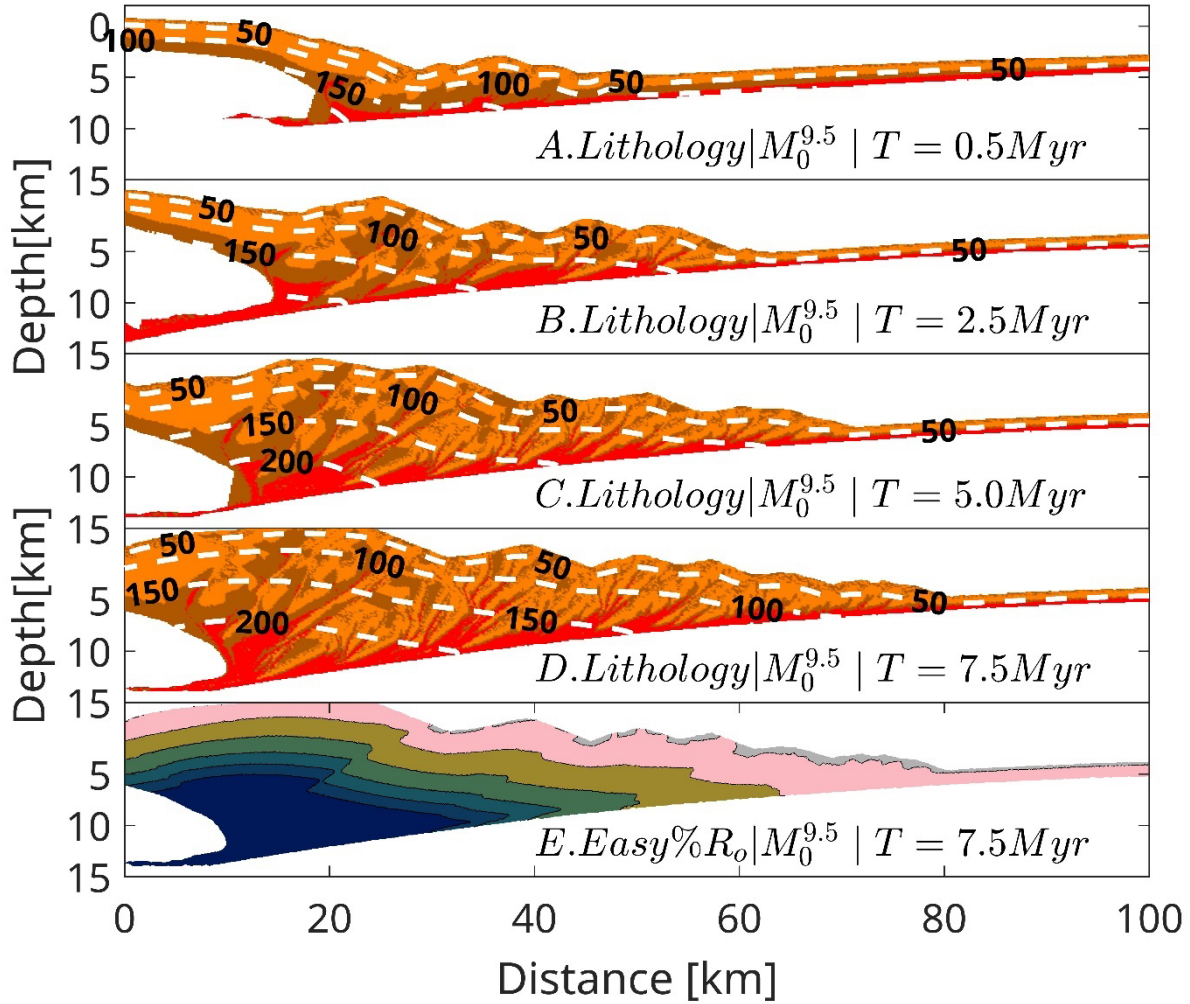
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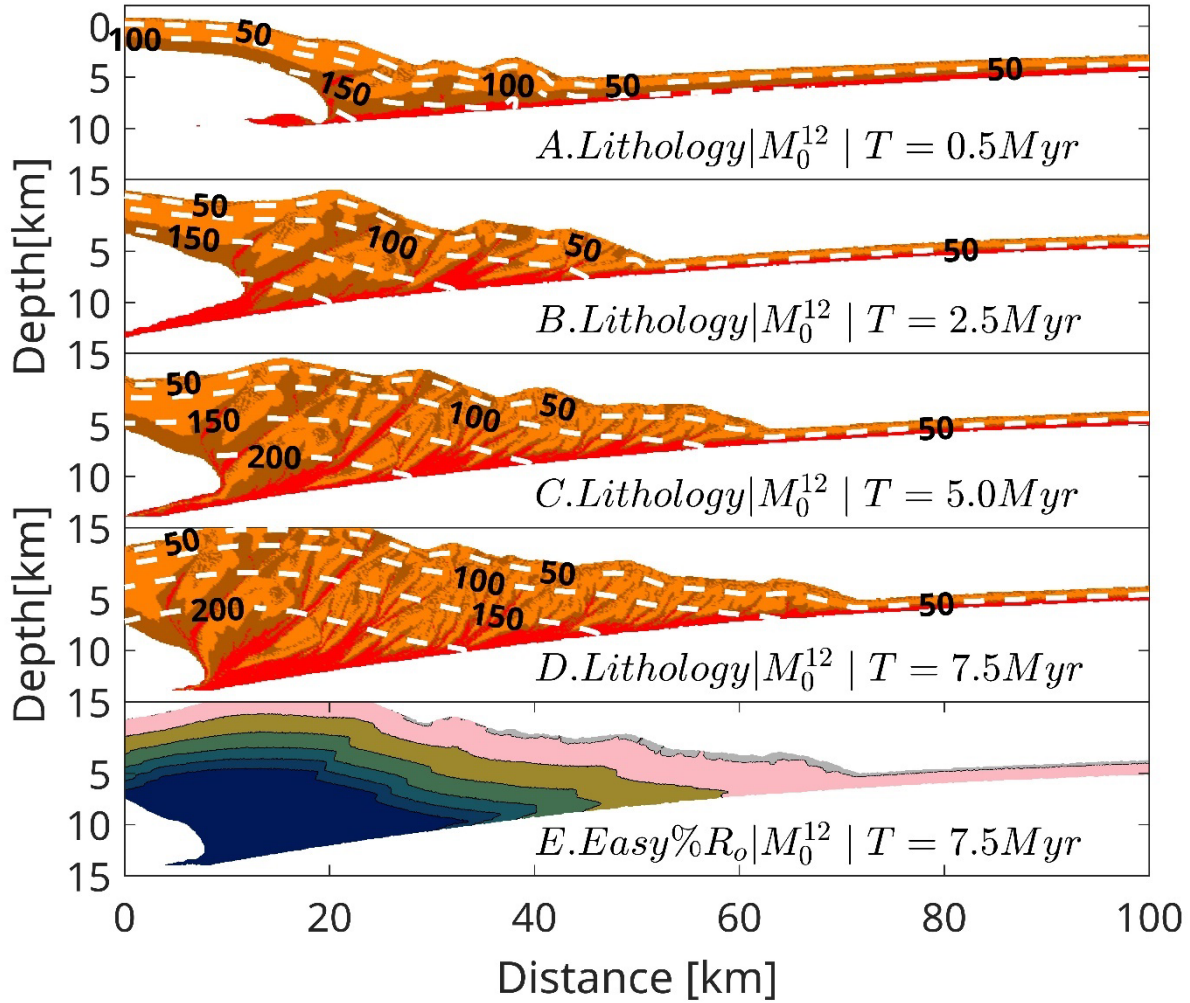
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984 **Fig. S6:**
 985 Typical thermomechanical evolution of the accretionary wedge for model $M_0^{9.5}$ at 0.5 Myr, 2.5 Myr, 5.0 Myr and 7.5 Myr of
 986 lithological evolution (Panel A-D). The dashed white lines represent the contours of the temperature field. The colormap for
 987 the first 4 panels is same as Figure 1. The last panel represents thermal maturity values at ~ 7.5 Myr computed using Easy%Ro.
 988 The colormap for Panel E is same as that of Figure 3.
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997 **Fig. S7:**
 998 Typical thermomechanical evolution of the accretionary wedge for model M_0^{12} at 0.5 Myr, 2.5 Myr, 5.0 Myr and 7.5 Myr of
 999 lithological evolution (Panel A-D). The dashed white lines represent the contours of the temperature field. The colormap for
 1000 the first 4 panels is same as Figure 1. The last panel represents thermal maturity values at ~ 7.5 Myr computed using Easy% R_o .
 1001 The colormap for Panel E is same as that of Figure 3.
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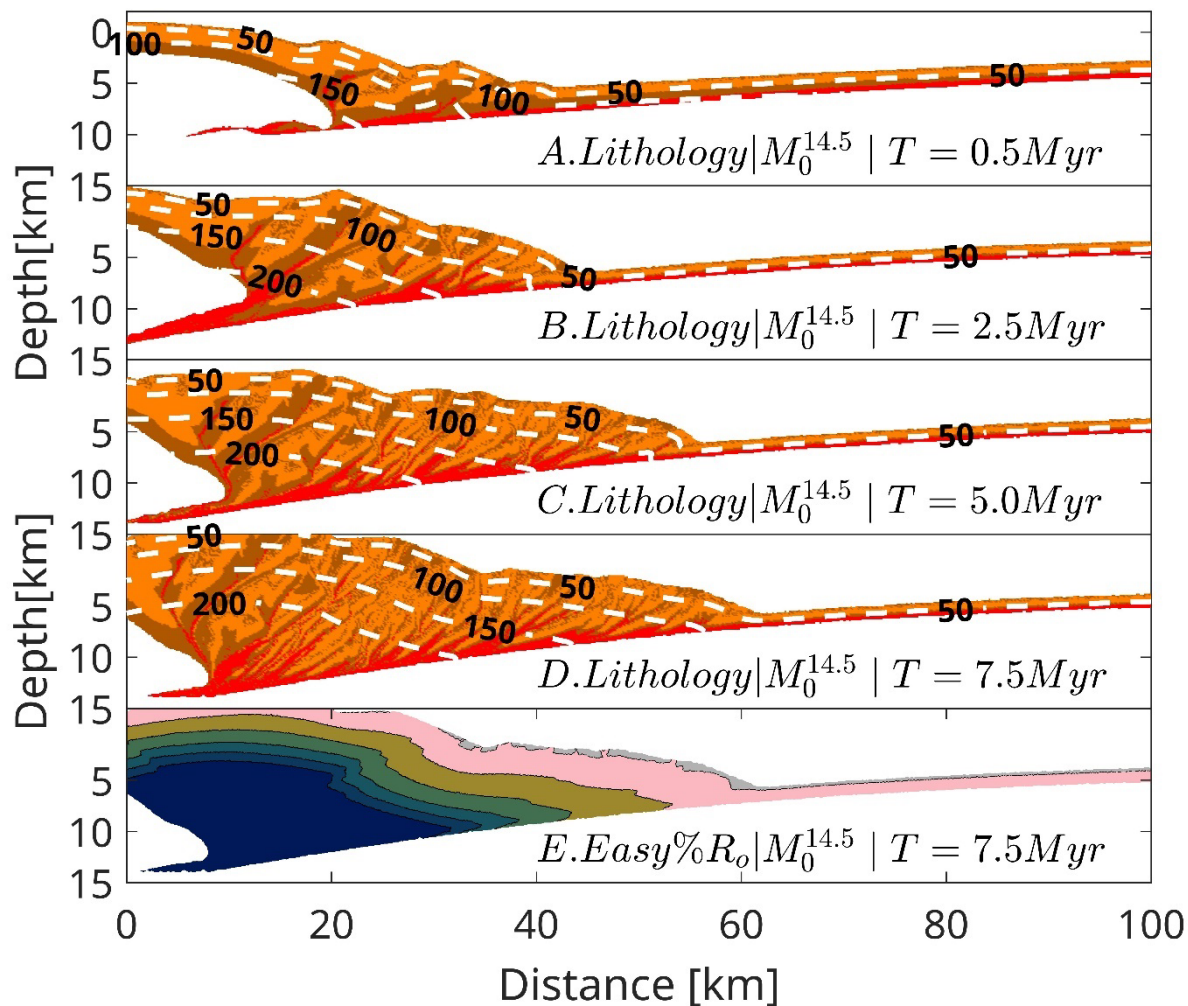


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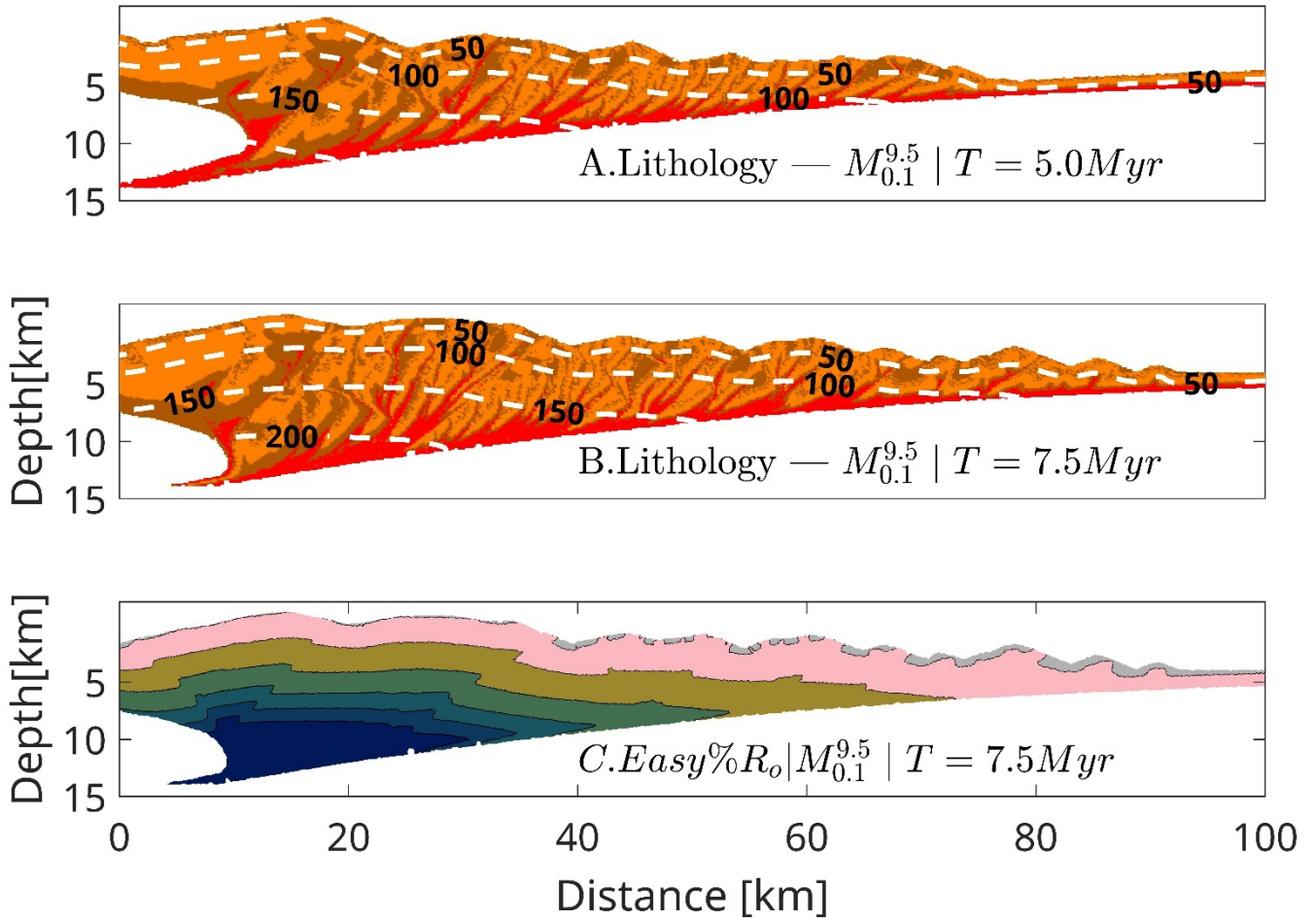
Fig. S8:

Typical thermomechanical evolution of the accretionary wedge for model $M_0^{14.5}$ at 0.5 Myr, 2.5 Myr, 5.0 Myr and 7.5 Myr of lithological evolution (Panel A-D). The dashed white lines represent the contours of the temperature field. The colormap for the first 4 panels is same as Figure 1. The last panel represents thermal maturity values at ~ 7.5 Myr computed using Easy%Ro. The colormap for Panel E is same as that of Figure 3.



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1020 **Fig. S9:**
 1021 Typical thermomechanical evolution of the accretionary wedge for model $M_{0.1}^{9.5}$ at 5.0 Myr and 7.5 Myr of lithological evolution
 1022 (Panel A-B). The dashed white lines represent the contours of the temperature field. The colormap for the first 2 panels is
 1023 same as Figure 1. The Panel C represents thermal maturity values at ~ 7.5 Myr computed using Easy%Ro. The colormap for
 1024 Panel E is same as that of Figure 3.
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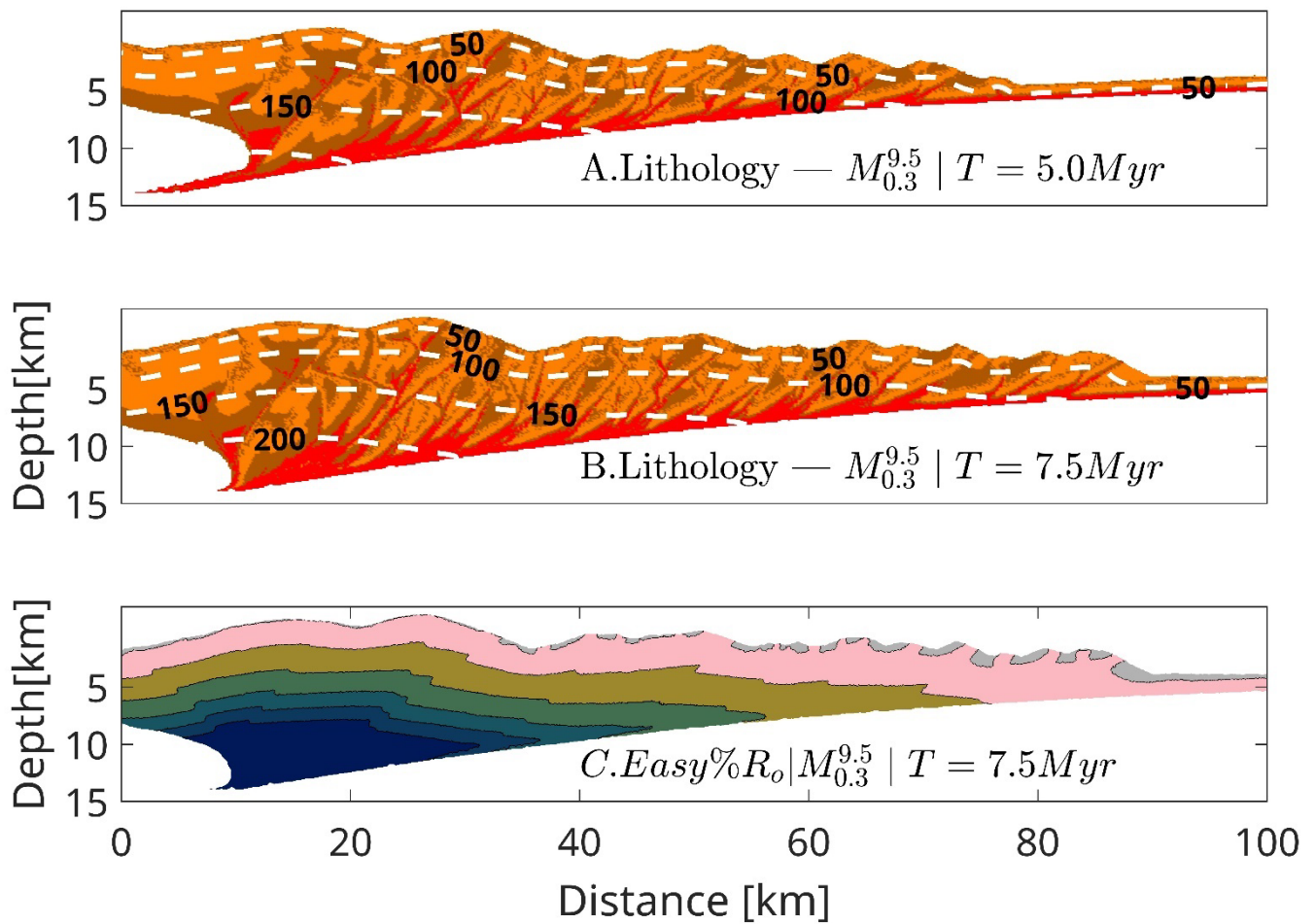
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1034 **Fig. S10:**

1035 Typical thermomechanical evolution of the accretionary wedge for model $M_{0.3}^{9.5}$ at 5.0 Myr and 7.5 Myr of lithological
1036 evolution (Panel A-B). The dashed white lines represent the contours of the temperature field. The colormap for the first 2
1037 panels is same as Figure 1. The Panel C represents thermal maturity values at ~ 7.5 Myr computed using Easy%Ro. The
1038 colormap for Panel E is same as that of Figure 3.

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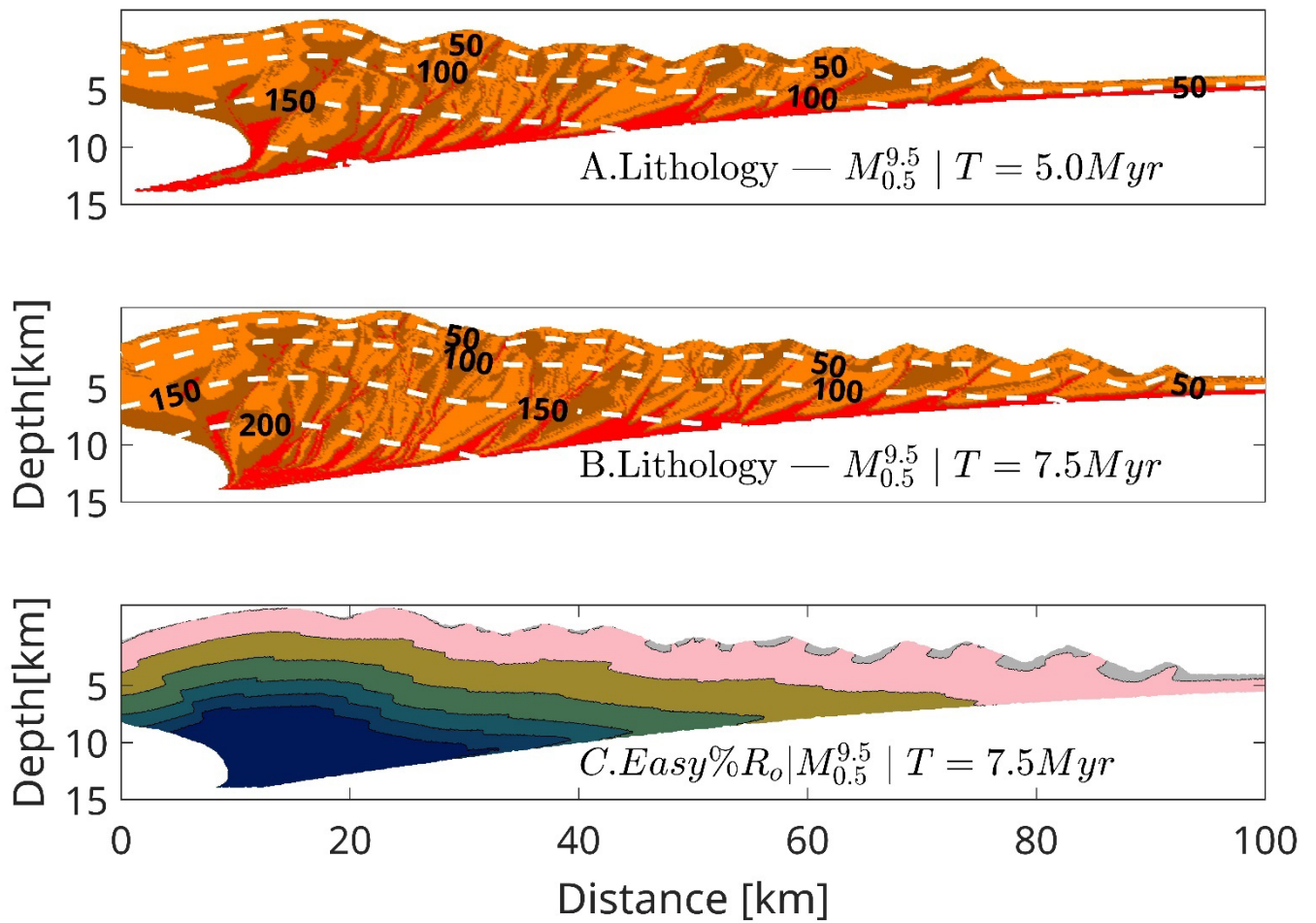
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1047 **Fig. S11:**

1048 Typical thermomechanical evolution of the accretionary wedge for model $M_{0.5}^{4.5}$ at 5.0 Myr and 7.5 Myr of lithological evolution
1049 (Panel A-B). The dashed white lines represent the contours of the temperature field. The colormap for the first 2 panels is
1050 same as Figure 1. The Panel C represents thermal maturity values at ~ 7.5 Myr computed using Easy% R_o . The colormap for
1051 Panel E is same as that of Figure 3.

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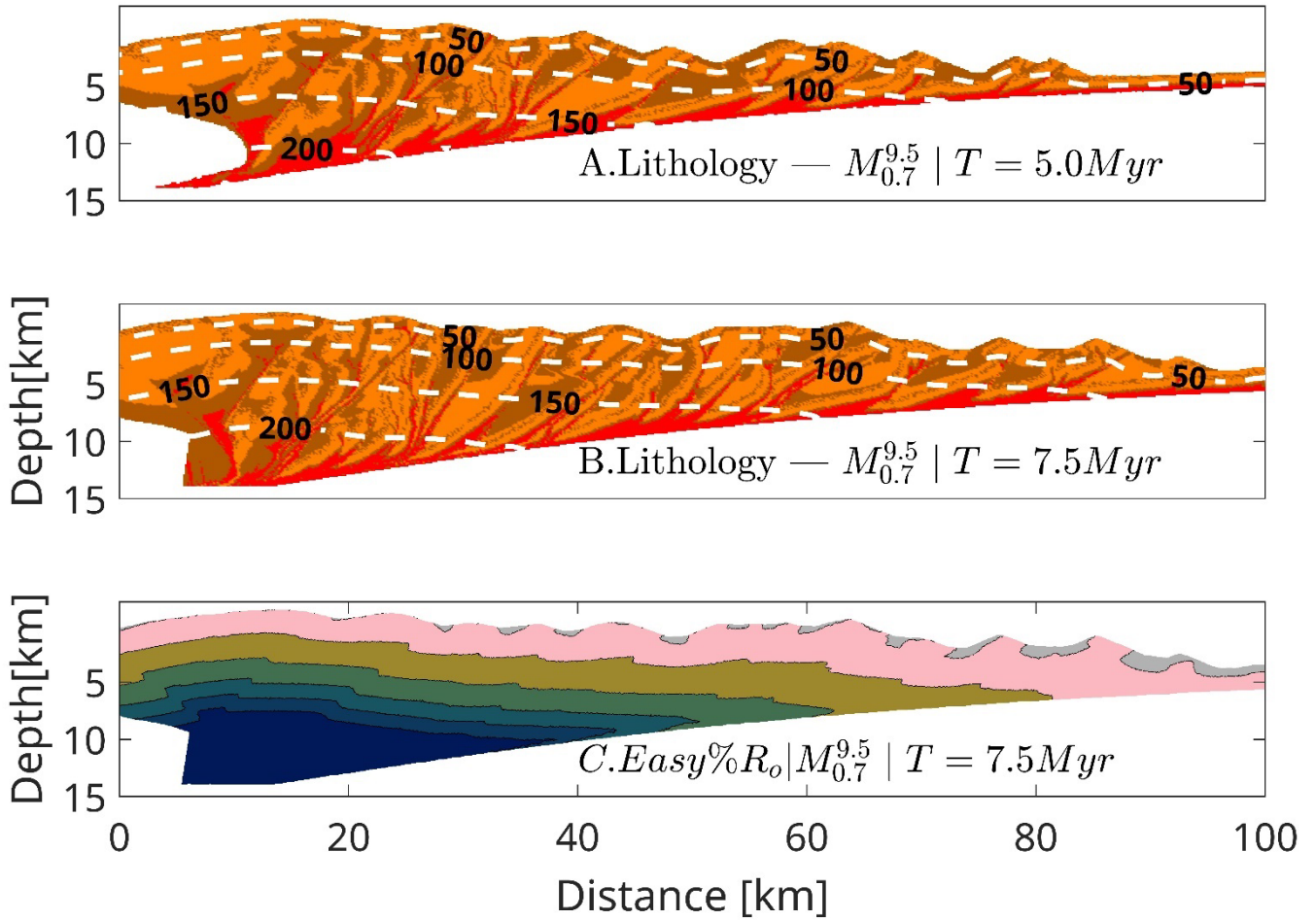
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1059 **Fig. S12:**
 1060 Typical thermomechanical evolution of the accretionary wedge for model $M_{0.7}^{9.5}$ at 5.0 Myr and 7.5 Myr of lithological evolution
 1061 (Panel A-B). The dashed white lines represent the contours of the temperature field. The colormap for the first 2 panels is
 1062 same as Figure 1. The Panel C represents thermal maturity values at ~ 7.5 Myr computed using Easy%Ro. The colormap for
 1063 Panel E is same as that of Figure 3.
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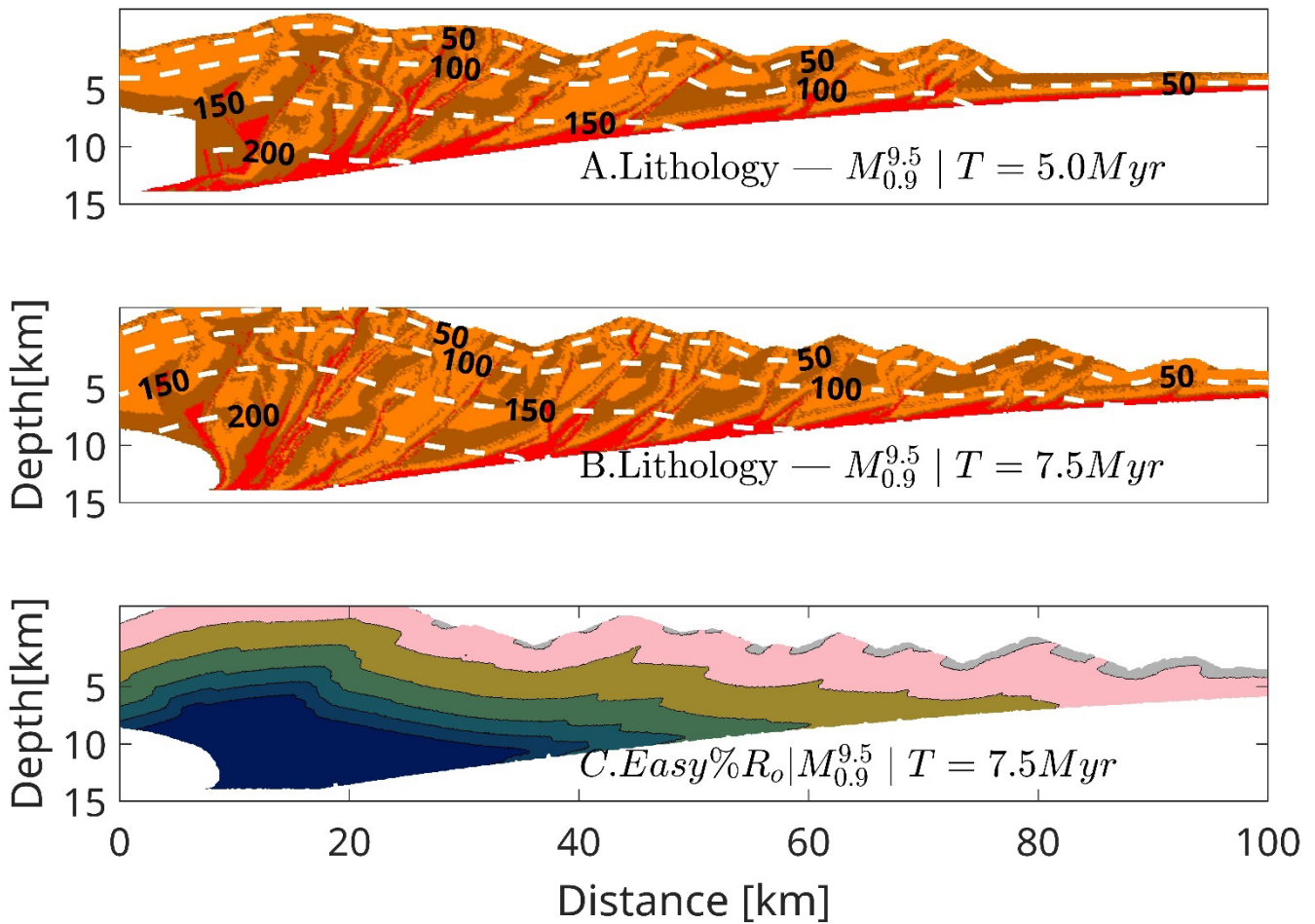
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1073 **Fig. S13:**

1074 Typical thermomechanical evolution of the accretionary wedge for model $M_{0.9}^{9.5}$ at 5.0 Myr and 7.5 Myr of lithological evolution
1075 (Panel A-B). The dashed white lines represent the contours of the temperature field. The colormap for the first 2 panels is
1076 same as Figure 1. The Panel C represents thermal maturity values at ~ 7.5 Myr computed using Easy% R_o . The colormap for
1077 Panel E is same as that of Figure 3.

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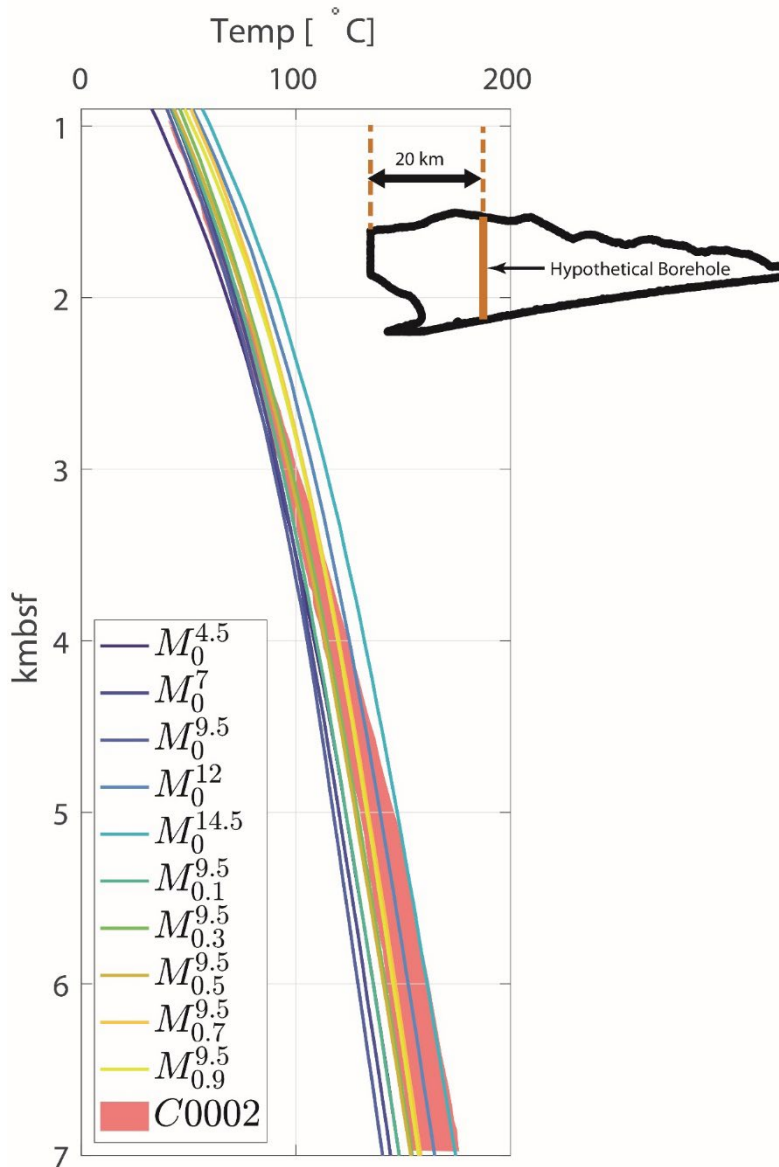
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1105 **Fig. S14:**

1106 *Plot of Temperature vs Depth profile in all models compared to Temperature-depth profile based on in-situ temperature from*
1107 *the long-term borehole monitoring system (indicated red patch is the range of temperature estimated by (Sugihara et al.,*
1108 *2014)). The temperature vs depth profiles for the models are computed for 20 kms from the backstop as shown in the inset.*
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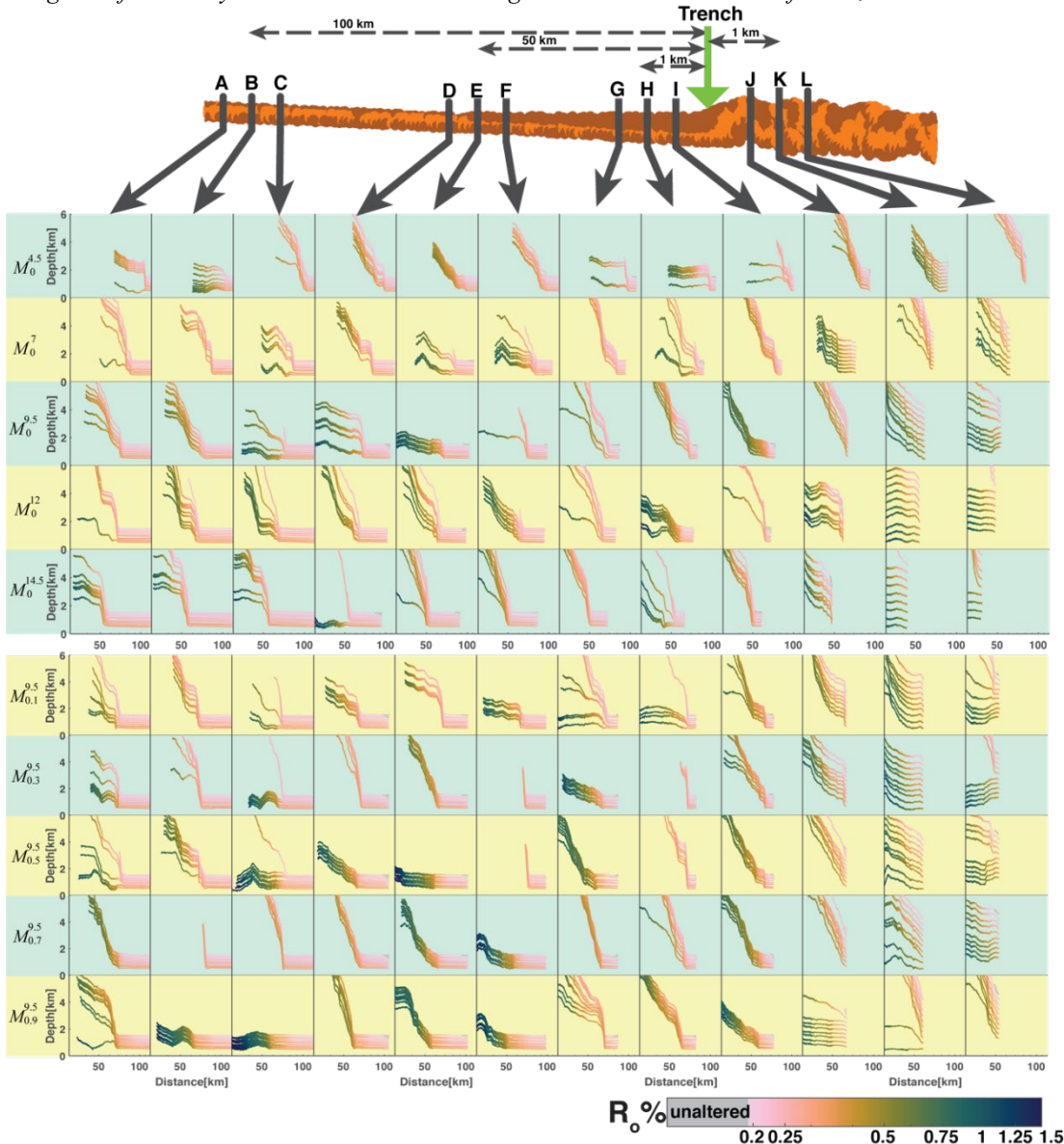
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1112 **Fig. S15**

1113 *Trajectory of sediments in model. The wedge on top shows the location of individual boreholes relative to the position of the*
1114 *trench at 2.5 Myr. In each borehole, A-L 10 points are plotted for their trajectories between 2.5 Myr and 7.5 Myr. The color*
1115 *of markers in the trajectories represent the evolution of thermal maturity on individual sediment markers while undergoing*
1116 *evolution. The image of the wedge on top is a representative image showing the relative location of boreholes with respect to*
1117 *the trench and each other. We present 4 set of boreholes (each having 3 boreholes separated by a km), one of which lies in the*
1118 *wedge itself at 2.5 Myr and 3 lies in the incoming sediments at a distance of 1 km, 50km and 100 kms from trench.*



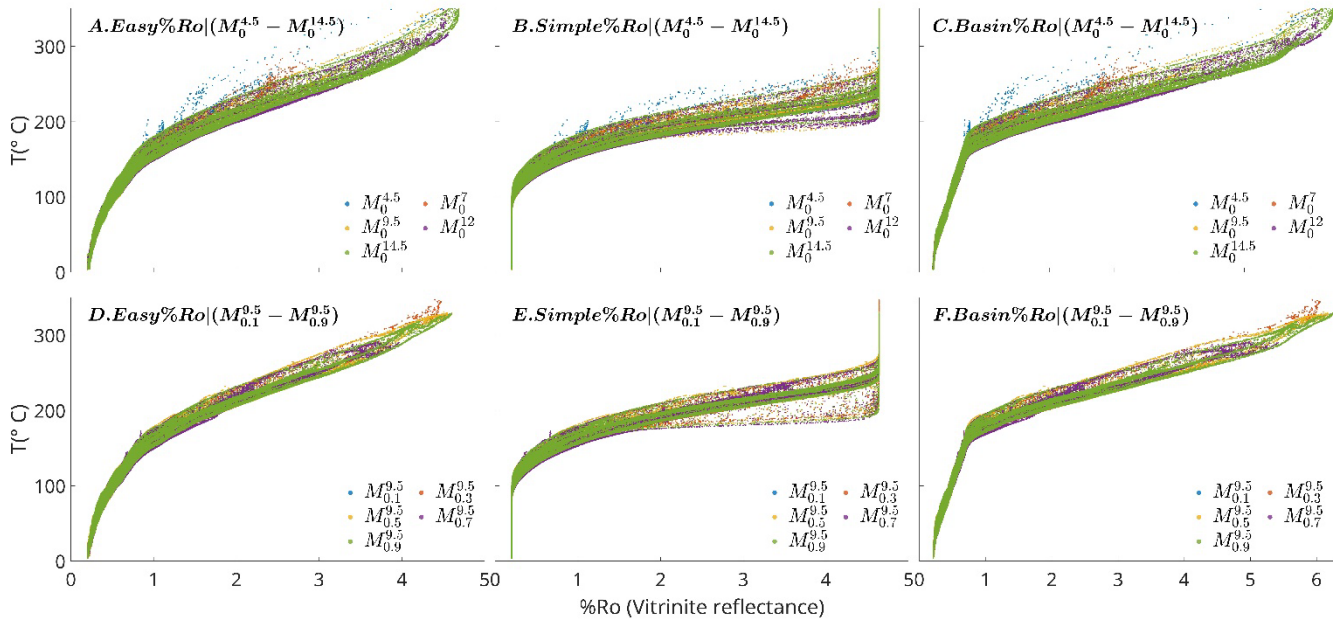
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1121 **Fig. S16**

1122 *Vitrinite Reflectance(%R_v) vs Maximum Exposure temperature in models. Panel A, B and C show the Temperatures as a*
 1123 *function of %R_v computed from Easy%R_v, Simple%R_v, Basin%R_v for models $M_0^{4.5} - M_0^{14.5}$. Similarly panels D, E and F show*
 1124 *the Temperatures as a function of %R_v computed from Easy%R_v, Simple%R_v, Basin%R_v for models $M_{0.1}^{9.5} - M_{0.9}^{9.5}$.*

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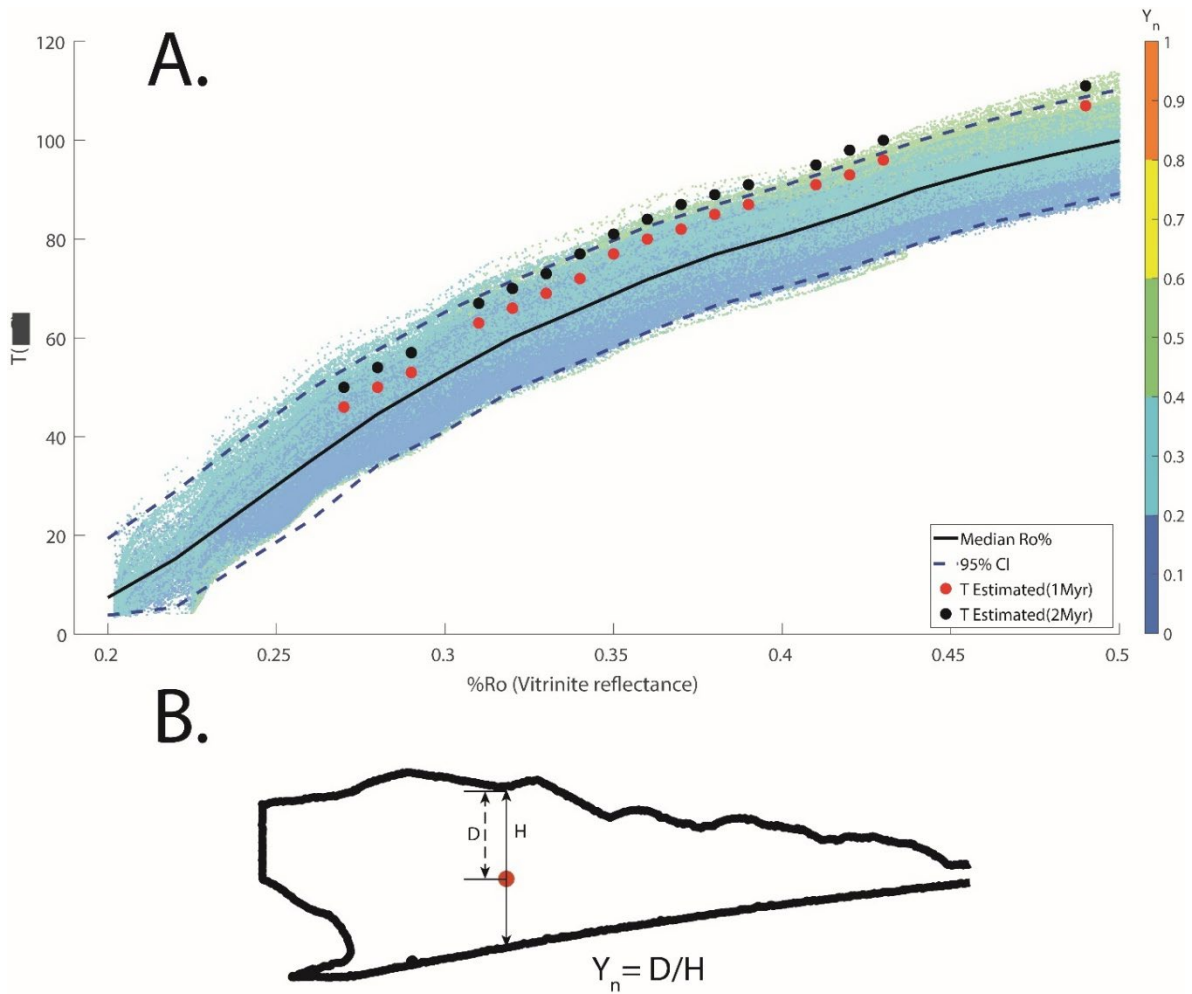
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1139 **Fig. S17:**

1140 Panel A shows %Ro vs T for model (shown by smaller markers) and C0002 borehole (shown by large circular markers)
1141 (Fukuchi et al., 2017). Y_n is the depth of the marker from the surface normalized by the thickness (vertical extent) of the wedge
1142 at the location of the marker as illustrated in Panel B.
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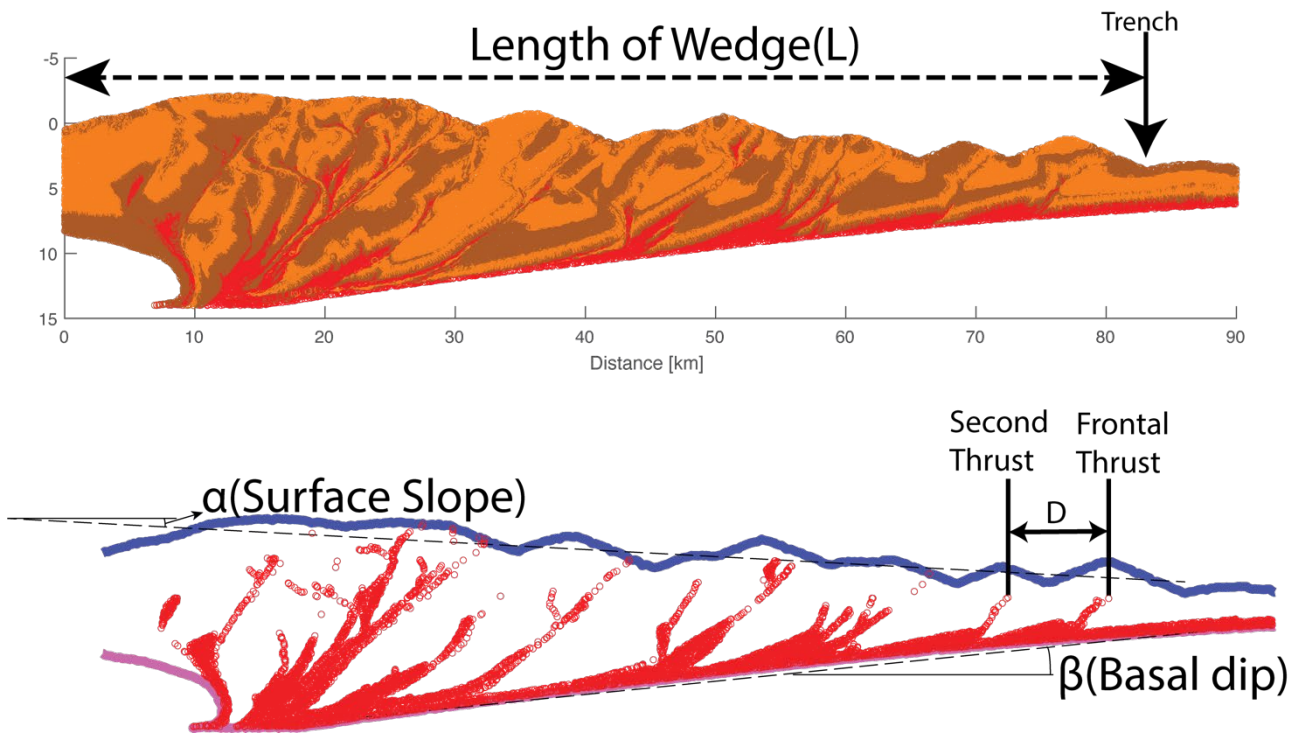
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1149 **Fig. S18:**

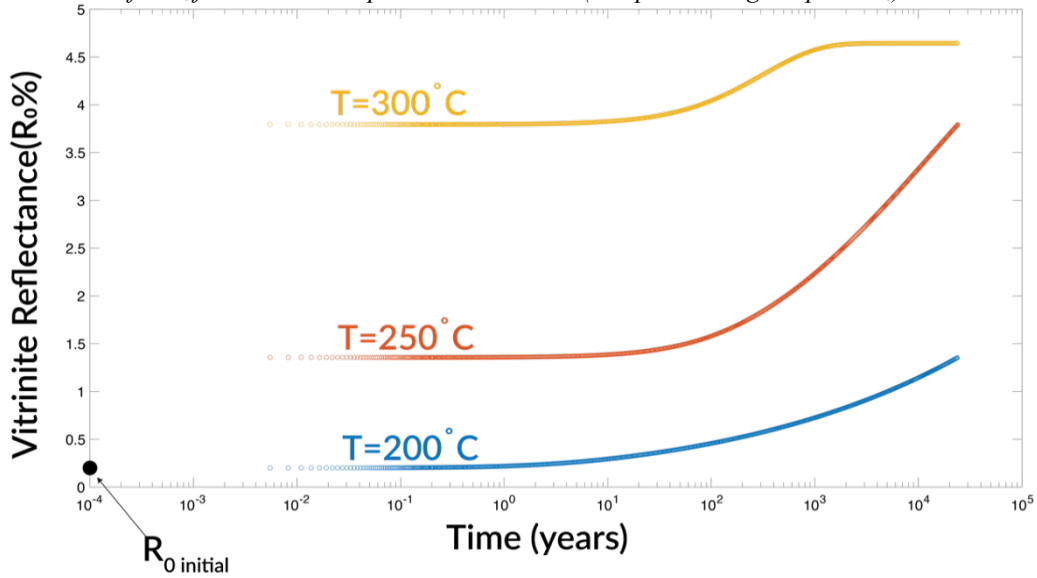
1150 Illustration to show the measurement of L (length of wedge), α (surface slope), β (basal dip and, D (Distance between the first
1151 and second frontal thrust).



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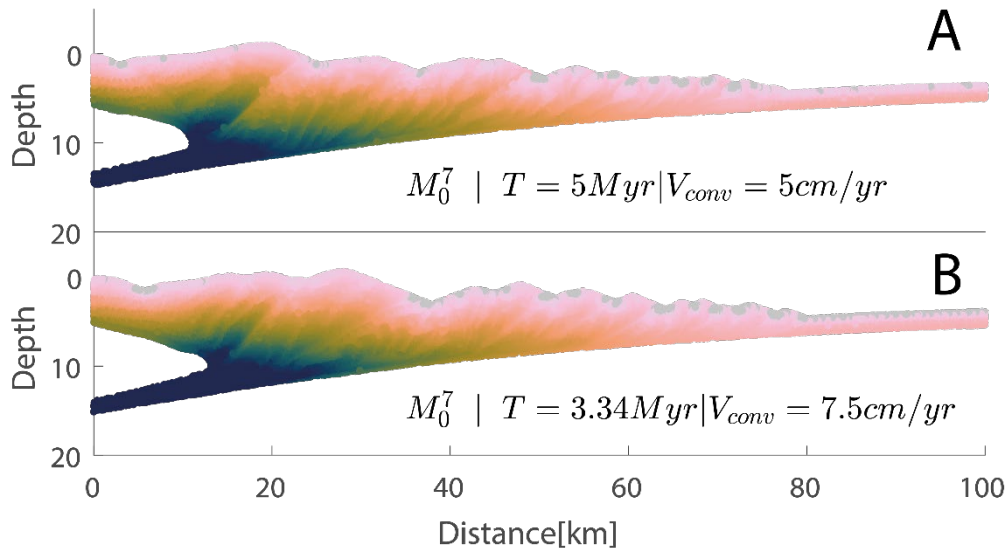
1165 **Fig S19:**

1166 Evolution of % R_o for constant temperatures with time (computed using Simple % R_o)



1167 **Fig S20:**
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1169 Thermal maturity distribution in two models with different convergent velocity. Panel A and B shows a models with convergent
1170 velocity of 5 cm/yr and 7.5 cm/yr respectively. The colormap for the images is same as for Figure 3. The comparison between
1171 the models has been shown for different time to keep the volume of incoming sediments ($T \cdot V_{conv}$) similar.



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