



Feedback mechanisms controlling Antarctic glacial cycle dynamics simulated with a coupled ice sheet—solid Earth model

Torsten Albrecht ¹, Meike Bagge ², and Volker Klemann ²

Correspondence: T. Albrecht (albrecht@pik-potsdam.de)

Abstract. The dynamics of the ice sheets on glacial-interglacial time scales are highly controlled by interactions with the solid Earth, i.e., glacial isostatic adjustment (GIA). Particularly at marine ice sheets, competing feedback mechanisms govern the migration of the ice sheet's grounding line and hence the ice sheet stability. In this study, we run coupled ice sheet-solid Earth simulations over the last two glacial cycles. For the ice sheet dynamics we apply the Parallel Ice Sheet Model PISM and for the load response of the solid Earth we use the three-dimensional viscoelastic Earth model VILMA, which, in addition, considers the gravitationally consistent redistribution of water (the sea level equation). We decided on an offline coupling between the two model components. By convergence of trajectories of the Antarctic Ice Sheet deglaciation we determine optimal coupling time step and spatial resolution and compare patterns of inferred relative sea level change since the Last Glacial Maximum with the results from previous studies. With our coupling setup we evaluate the relevance of feedback mechanisms for the glaciation and deglaciation phases in Antarctica considering different 3D Earth structures resulting in a range of load-response time scales. For rather long time scales, in a glacial climate associated with far-field sea level low stand, we find grounding line advance up to the edge of the continental shelf mainly in West Antarctica, dominated by a self-amplifying GIA feedback, which we call the 'forebulge feedback'. For the much shorter time scale of deglaciation, dominated by the Marine Ice Sheet Instability, our simulations suggest that the stabilizing GIA feedback can significantly slow-down grounding line retreat in the Ross sector, which is dominated by a very weak Earth structure (i.e. low mantle viscosity and thin lithosphere). This delaying effect prevents a Holocene grounding line retreat beyond its present-day location, which is discussed in the scientific community, supported by observational evidence at the Siple Coast and by previous model simulations. The described coupled framework, PISM-VILMA, allows for defining restart states to run multiple sensitivity simulations from. It can be easily implemented in Earth System Models (ESMs) and provides the tools to gain a better understanding of ice sheet stability on glacial time scales as well as in a warmer future climate.

1 Introduction

The observed accelerating retreat of large sectors of the Antarctic Ice Sheet (AIS) raises concerns about future sea level rise (Seroussi et al., 2020; IPCC, 2021). Self-amplifying, positive feedbacks may trigger the tipping and hence the destabilization and collapse of the marine-based parts of the ice sheet (Pattyn and Morlighem, 2020; Armstrong McKay et al., 2022; Lenton

¹Potsdam Institute for Climate Impact Research (PIK), Member of the Leibniz Association, Potsdam, Germany

²GFZ German Research Centre for Geosciences, Telegrafenberg, 14473 Potsdam, Germany





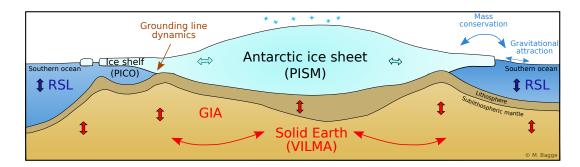


Figure 1. Schematics of coupled PISM Ice Sheet – PICO Ice Shelf – VILMA Solid Earth model components. Bedrock topography, relative sea level (RSL) and ice thickness are exchanged between VILMA and PISM in predefined coupling time steps.

et al., 2023). The Marine Ice Sheet Instability (MISI) is mainly controlled by the bedrock geometry (Fretwell et al., 2013; Morlighem et al., 2020), with retrograde slopes supporting a run-away dynamic feedback mechanism (Weertman, 1974; Mercer, 1978; Thomas and Bentley, 1978; Schoof, 2007), while buttressing forces can have a stabilizing effect for certain ice shelf geometries (Gudmundsson, 2013; Pegler, 2018; Haseloff and Sergienko, 2018; Reese et al., 2018b). The dynamic retreat of ice sheet grounding lines in response to the thinning of ice shelves and the subsequent speed-up of ice streams mainly in West Antarctica have been the dominant drivers of most of the recent mass loss in Antarctica (Rignot et al., 2019; Otosaka et al., 2023), and some studies suggests that MISI may already be underway (Joughin et al., 2014; Rignot et al., 2014; Reed et al., 2023). Depending on the water depth at marine-terminating glacier fronts, the ice sheet retreat may also be amplified by the Marine Ice Cliff Instability (MICI) (Pollard et al., 2015; DeConto and Pollard, 2016; Crawford et al., 2021; Li, 2022).

The solid Earth responds to ice sheet thinning or retreat with viscoelastic deformation, generally known as glacial isostatic adjustment (GIA), see Fig. 1. The strength as well as typical length and time scales of the GIA response depend on the Earth's mantle viscosity and lithosphere thickness (e.g. Peltier, 1974). The redistribution of land ice, ocean water and mantle material induces changes in the Earth's gravity field (with the 'geoid' as equipotential surface), and therefore alters the sea level globally, which follows the geoid (Farrell and Clark, 1976); a correction, which usually is considered as being part of GIA. Geodetic investigations of crustal uplift in the Amundsen Sea sector in West Antarctica (Barletta et al., 2018; Blank et al., 2021) postulate a laterally strongly varying viscoelastic Earth structure with mantle viscosities orders of magnitude lower than the global average. Hence, a low mantle viscosity implies much faster and, due to a thinner lithosphere, a more localised (short-wavelength) response of the solid Earth to ice sheet retreat (van der Wal et al., 2015; Larour et al., 2019; Wan et al., 2022). Furthermore, there is a clear dichotomy in the Earth structure between East and West Antarctica (Behrendt, 1999; Morelli and Danesi, 2004; Accardo et al., 2014; Nield et al., 2018; Whitehouse et al., 2019; Lloyd et al., 2020; Powell et al., 2020), but also within West Antarctica a large degree of heterogeneity exists on length scales of 100 km (An et al., 2015; Ramirez et al., 2016; Heeszel et al., 2016), with hot spots of enhanced geothermal heat flux (Lough et al., 2013; Dziadek et al., 2021; Bredow et al., 2023).



60



The relative sea level (RSL), which is the water depth, or more precisely the vertical distance between the geoid and the bottom of the ocean, directly determines the grounding line position of marine ice sheets via the flotation criterion (Gregory et al., 2019; Goelzer et al., 2020; Adhikari et al., 2020). When ice sheets decay and grounding lines retreat, the GIA-induced viscoelastic bed deformation reduces the water depth and hence induces indirectly a stabilizing negative feedback, which is additionally supported by near-field sea level lowering in response to reduced gravitational attraction (Gomez et al., 2010, 2012, 2015). As a side effect, the vertical bed displacement induces a bending of the elastic lithosphere and lateral flow of mantle material, which is associated with the migration of a bulge with opposite RSL sign in the vicinity (Adhikari et al., 2014). In grounded ice sheet regions, where bedrock uplift directly affects the ice sheet's height, the surface climate becomes generally colder and dryer (lapse effect), which in turn affects the overall ice dynamics (Van den Berg et al., 2008; Konrad et al., 2014; Zeitz et al., 2022). Potentially, solid-Earth feedbacks can slow down or even halt deglacial retreat, depending on the time scales of the viscoelastic deformation, which depend on the structure of the solid Earth (Konrad et al., 2015; Larour et al., 2019).

This complex interplay of solid Earth, sea level and ice dynamics has therefore played a major role during glacial cycles (Whitehouse et al., 2019). Since the Last Glacial Maximum (LGM) about 21,000 years ago (21 kyr BP) (Peltier, 2005), deglaciation of the AIS may have been initiated or amplified in periods of rapid sea level rise, as iceberg-rafted debris records in deep-sea sediments suggest (Weber et al., 2014; Jones et al., 2022). Such inter-hemispheric sea level effects may have contributed to the synchronicity of the large ice sheets during ice-age cycles (Gomez et al., 2020). There is growing evidence that during the Holocene period (the past 11,700 years) the solid-Earth uplift in combination with ice rise formation may have caused the re-advance of the Ross Sea grounding line to present-day location after an initial phase of rapid deglaciation (Lingle and Clark, 1985; Kingslake et al., 2018; Johnson et al., 2022), while in the Amundsen Sea grounding lines remained stable for the last 5,500 years until recently (Braddock et al., 2022). This is a highly relevant information in defining the present-day state of the AIS, including its contemporary rates of change (Coulson et al., 2021). It characterizes stability and the potential for sea level rise in an increasingly warming climate (Joughin and Alley, 2011).

Ice sheet models have been coupled to GIA models with different levels of complexity (de Boer et al., 2017; Whitehouse, 2018). The computationally efficient two-layer approach with an 'Elastic Lithosphere and a Relaxing Asthenosphere' (ELRA) accounts for the vertical bedrock adjustment for one given relaxation time (Brotchie and Silvester, 1969; Le Meur and Huybrechts, 1996) and is widely used in ice sheet modeling or coupled Earth system modeling (Pollard and DeConto, 2012; DeConto and Pollard, 2016; Pattyn, 2017; Quiquet et al., 2018). ELRA can be improved when the time-lagged mantle flow in the asthenosphere below an elastic thin plate is approximated by solving the corresponding biharmonic differential equation using Fast Fourier Transformation (Lingle and Clark, 1985; Bueler et al., 2007; Albrecht et al., 2020a; Book et al., 2022). In this 'Lingle-Clark' (LC) bed deformation model, a wavelength-depending response time spectrum replaces the single exponential decay parameter of the ELRA approximation. Hence, only the uniform mantle viscosity and flexural rigidity (or elastic lithosphere thickness) are used as input parameters valid for the considered half-space. In addition to the bedrock changes, commonly global mean sea level anomalies are used as external forcing for ice sheet models to account for water depth changes at





the grounding line (Goelzer et al., 2020). The LC model is limited to a certain region (e.g. Antarctica) and is unable to prescribe gravitational, globally self-consistent water-load changes or to account for feedbacks associated with polar motion due to GIA.

In order to account for both global and near-field spatial variablity of relative sea level change consistent with dynamic changes in ice sheet extent, coupled ice sheet–solid Earth models need to simultaneously solve the 'sea level equation' (Farrell and Clark, 1976), as realized in 'Self-Gravitating viscoelastic solid-Earth Models' (SGVEM: e.g., de Boer et al., 2014; Gomez et al., 2015, 2020; Konrad et al., 2015; Coulon et al., 2021). GIA models generally account for both solid-Earth deformation and gravitational effects in combination with rotational effects in response to changes in the redistribution of ice and ocean masses (Milne and Mitrovica, 1996). Most GIA models so far compute changes in Earth deformation and geoid for a radially varying (depth dependent) 1D Earth structure using spherical harmonics (Whitehouse et al., 2012; Konrad et al., 2015; Pollard et al., 2017). In regions of weak Earth structure, as for instance presumably in West Antarctica, the observed uplift rates are not compatible with the response of a viscosity structure usually applied for northern-hemisphere GIA in the range of 10^{20} – 10^{21} Pa's and a lithosphere thickness of $\approx 100 \, \mathrm{km}$ (Whitehouse, 2018; Ivins et al., 2023).

Recently, a new generation of GIA models accounts for the 3D Earth structure (A et al., 2012; van der Wal et al., 2015; Nield et al., 2018; Powell et al., 2021; Blank et al., 2021) for a prescribed ice thickness (load) history. Interactively coupled to ice sheet models, such 3D GIA models find significant differences in West Antarctic Ice Sheet (WAIS) evolution on glacial time scales compared to 1D GIA or standalone ice sheet models (Gomez et al., 2018; Han et al., 2022; Van Calcar et al., 2023). The underlying coupling methods all imply a similar iterative process to account for the unknown initial bed topography, but differ with respect to the coupling time steps in the respective approaches ranging from hundreds to thousands of years.

Here, we present a set of new simulations of Antarctic Ice Sheet evolution over the last 246,000 years (i.e. two full glacial cycles) with the Parallel Ice Sheet Model (PISM) coupled to the VIscoelastic Lithosphere and MAntle model (VILMA) solving for GIA.

2 Methods

100

110

2.1 PISM

The Parallel Ice Sheet Model (PISM¹, here based on v1.2.2) is an open-source² three-dimensional ice sheet model (Winkelmann et al., 2011; The PISM authors, 2023), written in C++ programming language. PISM has been previously applied in glacial-cycle simulations (e.g. Golledge et al., 2014; Sutter et al., 2019; Albrecht et al., 2020a, b), and can be easily coupled to other climate or Earth system model components (e.g. Kreuzer et al., 2021; Ziemen et al., 2019; Yang et al., 2022).

We here use a hybrid combination of two stress-balance approximations for the deformation of the ice, the Shallow Ice – Shallow Shelf Approximation (SIA-SSA Hindmarsh, 2004), that guarantees a smooth transition from vertical-shear dominated flow in the interior via sliding-dominated ice stream flow to fast plug flow in the floating ice shelves (Bueler and Brown, 2009), while neglecting higher-order modes of the flow. Driving stress at the grounding line is discretized using one-sided differences

 $^{^1\}mbox{https://www.pism.io},$ see also Section 'code and data availability'

²https://research-software-directory.org/software/pism



120

135

140

145



(Feldmann et al., 2014). Using a sub-grid interpolation scheme (Gladstone et al., 2010), the grounding line location simply results from flotation condition, without additional flux conditions imposed (Reese et al., 2018c). Basal friction and basal melt is interpolated accordingly (Seroussi and Morlighem, 2018; Hewitt and Bradley, 2023). Thus, grounding-line migration is reasonably well represented in PISM (compared to Stokes flow), even for coarse resolution (Pattyn et al., 2013; Feldmann et al., 2014). Ice deforms according to the Glen-Paterson-Budd-Lliboutry-Duval flow law with exponent n=3.

PISM simulates the three-dimensional polythermal enthalpy conservation for a given surface temperature and basal heat flux and thus captures melting and refreezing processes in temperate ice (Aschwanden and Blatter, 2009; Aschwanden et al., 2012). It is solved on a 3-dimensional grid with 81 vertical layers, with 20 m resolution at the base. The energy conservation scheme also accounts for the production of sub-glacial (and transportable) water (Bueler and van Pelt, 2015), which affects basal friction via the concept of a saturated and pressurized sub-glacial till. The till friction angle, which accounts for characteristics of the underlying substrate, has been optimized for present-day ice flow (Albrecht et al., 2020a). Depending on the resultant yield stress this allows for grow-and-surge instability (Feldmann and Levermann, 2017; Bakker et al., 2017; Schannwell et al., 2023). Here we use the non-conserving hydrology model, where the till water content in each grid cell is balanced by basal melting and a constant drainage rate.

ice shelf margins can evolve up to the edge of the continental shelf (here defined at 1800 m depth) constrained by a terminal thickness criterion (>75 m). Iceberg formation from ice shelves is parameterized based on spreading-rates (Levermann et al., 2012). Ice shelf melting is calculated using the Potsdam ice shelf Cavity mOdel (PICO) that considers basin-mean ocean properties on the continental shelf in front of the ice shelves and mimics the vertical overturning circulation in the ice shelf cavity (Reese et al., 2018a).

PISM comes with a generalized version of the Lingle-Clark bedrock deformation model (Bueler et al., 2007), assuming an elastic lithosphere, a resistant asthenosphere and a viscous half-space below (Whitehouse, 2018). The LC model is computationally efficient, the default coupling time step is 10 yr, but it does not account for regional sea level (geoid) variations.

A continental-scale representation of modern Antarctic bed and ice sheet topography is obtained from the Bedmap2 dataset (Fretwell et al., 2013). We simulate the entire Antarctic continent with 16 km grid resolution (381×381 regular grid size) compatible with the definition of the initMIP and ISMIP6 model intercomparison project (Nowicki et al., 2016, 2020). With an adaptive explicit time stepping of around 0.34 ± 0.03 yr, one glacial cycle (123 kyr) can be simulated within 1–2 days wall clock time with 64 CPU cores on a standard memory computing node³ ('AMD 7763' with 128 CPU cores in total, 256 GB main memory and 2.45 GHz base clock).

2.2 VILMA

The VIscoelastic LIthosphere and MAntle model (VILMA) solves the field equations for an incompressible self-gravitating viscoelastic sphere in the Lagrange domain, laterally in spherical harmonics, radially with finite elements, and in time using an explicit time-differencing scheme assuming a Maxwell rheology as material law. Lateral variations in viscosity are considered as shear energy perturbations, which are calculated on a Gauss-Legendre grid in the spatial domain and which are transformed

³https://docs.dkrz.de/doc/levante/configuration.html



150



back into the spectral domain at each time step (for details see Martinec, 2000). The code has been benchmarked for a spherical symmetric Earth structure (Spada et al., 2011), i.e. for a 1D Earth structure, and was applied in studies accounting for lateral variations, i.e. for a 3D Earth structure (Klemann et al., 2008; Bagge et al., 2021). In addition to viscoelastic deformations, the effect of rotational deformations is accounted for (Martinec and Hagedoorn, 2014).

The sea level equation, describing the gravitational consistent and mass-conserving redistribution of ice masses and ocean water (Farrell and Clark, 1976; Mitrovica and Milne, 2003; Kendall et al., 2006), is solved in the spatial domain (Hagedoorn et al., 2007) and was benchmarked in Martinec et al. (2018). Coast lines can freely migrate according to the local RSL, also accounting for floating ice shelves. There, the grounding line location is determined by the floation conditions and hence by densities of ice and ocean water (consistent with PISM). The migration of the grounding line is associated with a redistribution of water mass between ice sheets and ocean, which can result in large non-uniform near-field RSL patterns (Mitrovica et al., 2001; Spada et al., 2013).

For the radial discretization, we chose $\Delta z = 5 \, \mathrm{km}$ down to 420 km depth, followed below by $\Delta z = 10 \, \mathrm{km}$ down to 670 km and $\Delta z = 40$ to $60 \, \mathrm{km}$ down to the core–mantle boundary, where the parameterisation of the elastic shear modulus and density structure follows the Preliminary Reference Earth Model (PREM, Dziewonski and Anderson, 1981). The core is considered as a boundary condition, confining the solution domain to the Earth's crust and mantle. The spectral resolution we set to degree and order 170, meaning that layers with lateral variations are discretized on a $256 \times 512 \, (\mathrm{n}128)$ grid corresponding to a wavelength of $\sim 120 \, \mathrm{km}$. We consider this as sufficient due to the general low-pass response of the Earth to surface loading and the spectral resolution of the considered tomographic model of only degree 63 (Steinberger, 2016). Higher resolutions were tested in this project, but did not show significant changes (see Sect. 3.1). The sea level equation, defining the gravity-consistent mass redistribution of water between oceans and ice sheets in response to the deforming solid Earth, is solved in the spatial domain, also on a Gauss-Legendre grid, but with a significantly higher resolution of $1024 \times 2048 \, (\mathrm{n}512)$ corresponding to a wavelength of $\approx 30 \, \mathrm{km}$.

In order to allow for flexible restarts, the original Fortran77 code was modernized to Fortran90 during the PalMod project (see acknowledgements). For this, open MP^4 functionality was explicitly set up for calculation of the left-hand side elastic problem and the right-hand side viscous solution. In our coupled simulations, VILMA uses explicit time steps of $2.5 \,\mathrm{yr}$, in order to be able to solve also for very low mantle viscosities at the order of $10^{19} \,\mathrm{Pa}\,\mathrm{s}$. Considering this set up, one glacial cycle (123 kyr) can be simulated within 19 h wall clock time with 64 CPU cores on a standard memory computing node (same as indicated for PISM).

2.3 PISM-VILMA Coupling

PISM and VILMA are offline-coupled using a coupling time step that can be rather short ($\Delta t = 100 \,\mathrm{yr}$ as default). This is an advantage of the explicit time stepping and the weak formulation (in time-domain) of the solid-Earth dynamics (Martinec, 2000) in contrast to the normal-mode approach (in Laplace domain) used by most of the 1D Earth models (e.g. Peltier, 1974).

⁴https://www.openmp.org/resources/refguides/



190



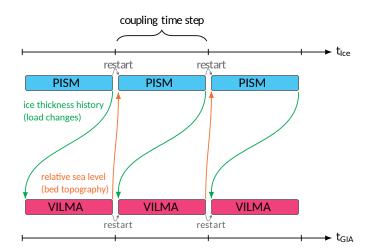


Figure 2. PISM-VILMA coupling scheme, adopted from Kreuzer et al. (2021).

In a first step, PISM runs for the coupling interval (from t_0 to t_1), based on the initial bed elevation, which remains constant over this time step Δt (see Fig. 2). Subsequently, VILMA integrates over the same interval (from t_0 to t_1) according to a global ice sheet load history, which combines ICE-6G_C (Peltier et al., 2015) north of 60°S and the PISM-simulated AIS changes south of 60°S, remapped to the VILMA grid. VILMA interpolates the ice sheet history between snapshots at beginning and end of the coupling interval and provides the global change in RSL at predefined snapshots. The RSL at t_1 is (bilinearly) remapped back to the PISM grid.

Then, this process restarts for the next coupling interval $(t_1 \text{ to } t_2)$. PISM interprets the RSL change as negative vertical displacement of the bed elevation with respect to a reference surface elevation (geoid), or as change in water depth, if the bed elevation has negative values. That means, the surface elevation of the ocean in the PISM simulations remains at z = 0. With the adjusted bed topography (water depth), the ice sheet's grounding line can move directly due to the flotation criterion or indirectly due to induced ice dynamical changes. These changes in the ice and water load are then passed to VILMA again, which simulates the same coupling interval (from t_1 to t_2), before PISM simulates for the next coupling interval.

In our coupling scheme, the PISM response always lacks behind the VILMA step by one coupling step. The implied numerical error remains small if short coupling time steps are used (see sensitivity to coupling time step in Sect. 3.1). We do not make use of (internal) iterations within a (longer) coupling time step as suggested, e.g., by Van Calcar et al. (2023), even though this could be easily implemented in PISM-VILMA. Furthermore, we avoid extrapolation of sea level and bed elevation changes to the next coupling interval as in Konrad et al. (2015), which principally can cause numerical instabilities. We also do not pass the sub-grid information of grounding line interpolation, used in PISM for the basal friction, to VILMA. In case of grounding line migration, this could avoid ad-hoc load changes from single grid cells. Our python coupler⁵ uses CDO and NCO tools⁶ for remapping two-dimensional RSL changes from the global Gauss-Legendre grid used in VILMA to the Antarctic Polar

⁵https://github.com/talbrecht/pismvilma, https://www.esm-tools.net

⁶http://nco.sourceforge.net, http://mpimet.mpg.de/cdo



205



step	$100 \times 10 \mathrm{yr}$	$10 \times 100 \mathrm{yr}$	$1 \times 1000 \mathrm{yr}$
PISM	2876 (49.7%)	1078 (52.2%)	999 (60.3%)
PISM2VILMA	871 (15.1%)	141 (6.8%)	19 (1.1%)
VILMA	1581 (27.3%)	802 (38.9%)	632 (38.2%)
VILMA2PISM	459 (7.9%)	43 (2.1%)	7 (0.4%)
TOTAL	5788 (1.60 h)	2063 (0.57 h)	1657 (0.47 h)

Table 1. Mean wall clock time for PISM-VILMA steps in seconds (and %) for 1 kyr simulation for the reference 3D Earth structure with 64 CPU cores and different coupling time steps, run on Levante (DKRZ). All three coupled simulations used the reference spatial resolution of n512 for the sea level equation in VILMA, n128 for the viscoelastic deformation in VILMA and 16 km for PISM in the Antarctic domain.

Stereographic⁷ equidistant Cartesian grid used by PISM, and vice versa, Antarctic ice thickness from the PISM grid back to the global VILMA grid.

On a High Performance Computing (HPC) system with a 'slurm' batch queue system, we make use of the heterogeneous job support⁸, which can simultaneously optimize for the openMP⁹ parallelization on a single compute node (in case of VILMA and the python coupler) and the MPI parallelization across multiple compute nodes (in case of PISM). The remapping takes about 23% of computational time for 10-yr coupling time step, 9% for 100 yr and only 1.5% for 1000-yr, when using 3D Earth structures (see PISM2VILMA and VILMA2PISM in Table 1). Total computation time for simulating 1 kyr on a standard memory computing node (128 cores in total, see details in Sect. 2.1) is about 25 min for the 1000 yr coupling time step (25 CPUh), 30 min for 100 yr (35 CPUh) and 100 min for 10 yr (100 CPUh), when using 64 CPU cores for VILMA, PISM and the remapping. Considering only 1D (radial) Earth structures in VILMA brings a speed-up by a factor of 5 for the VILMA step and hence of almost 50% speed-up in the coupled model performance, for coupling time steps of 100 yr.

For comparison, Van Calcar et al. (2023) used a 3D GIA finite-element model with 16 CPU cores to simulate the last glacial cycle, with coupling time steps between 5000 and 500 yr, 40 km resolution in the ice sheet model and between 30 and 200 km in the GIA model, showed a performance of 16 CPUh per 1 kyr. However, when internal iterations were considered, the coupled model system required about 120 CPUh per 1 kyr.

In order to account for (long) memory effects of the AIS to the climate history, we run the coupled simulation for two full glacial cycles (246 kyr, see Fig. 3 a), with the northern hemisphere described by the ICE-6G_C reconstruction (available for the last 123 kyr, repeated for the penultimate glacial cycle while smoothed at the Last Interglacial). For consistency, the climatic and ocean forcings are applied as described in previous PISM standalone simulations (Albrecht et al., 2020a), which have been coupled to the LC bed deformation model (Bueler et al., 2007). In order to support earlier deglaciation around 15 kyr BP (see Fig. 3 b), which provides a better match with paleo proxies (Briggs and Tarasov, 2013; Albrecht et al., 2020b), PISM

⁷https://epsg.io/3031

⁸https://slurm.schedmd.com/heterogeneous_jobs.html

⁹https://www.openmp.org





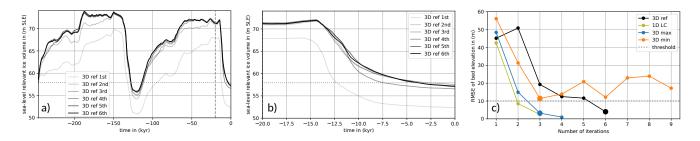


Figure 3. PISM sea level relevant Antarctic ice volume over 246 kyr a) and over the last 20 kyr b) showing convergence for six subsequent iterations of coupled simulations with reference 3D Earth structure at n128 resolution and n512 resolution for the sea level equation. In each iteration the initial bed topography is adjusted, such that the misfit of present-day bed topography according to VILMA is minimized. c) Ice volumes above flotation have been calculated considering cell-area weighting and density correction (Goelzer et al., 2020) with a temporal resolution of 100 yr.

parameters are in this study slightly adjusted (e.g. till water drainage rate or precipitation scaling). Simulations are run until the year 1950 (corresponding to 0 kyr BP), such that the recent anthropogenic warming is ignored in the climate forcing with ice core reconstructions (here a combination of EPICA Dome C and WAIS Divide ice core, cf. Albrecht et al., 2020a).

For the initial global bed topography we apply the present-day ETOPO1¹⁰ bathymetry (Amante and Eakins, 2009), updated with Bedmap2 (Fretwell et al., 2013) in the Antarctic sector. As the initial bed topography of the simulation (at 246 kyr BP) is not known a priori, we iterate several times over the period of two glacial cycles (Kendall et al., 2005), and successively correct for the initial bed topography according to the mismatch of the present-day bed topography to observations from Bedmap2 of the previous iteration (compare Fig. 3 and Fig. 4). Ideally, the present-day RSL subtracted from the initial bed topography should converge to the present-day topography. In the first iteration the present-day RSL is underestimated by up to 100 m in East Antarctica (bedrock too high) and overestimated by up to 100 m in West Antarctica (Fig. 4a). As measure of the mismatch we use the Root Mean Squared Error (RMSE) over the Antarctic computational domain. Generally, the RMSE reduces with each iteration by a factor of 0.2–0.4 (see Fig. 3 c). We stop iterating when the RMSE falls below the acceptance level of 10 m (dotted line). This iterative procedure aims at minimizing deviations from the present-day bed topography, but we also find convergence of the present-day sea level equivalent Antarctic ice volume against observations (Fig. 3 b); although in some regions the misfit in ice thickness remains comparably high (Fig. 4g–1).

2.4 Solid-Earth structures

225

230

In previous PISM simulations, the LC model (Lingle and Clark, 1985; Bueler et al., 2007) has been coupled every 10 yr to account for the viscoelastic displacement of the bedrock topography, assuming an elastic plate (with a flexural rigidity of 5×10^{24} Nm, corresponding to a lithosphere thickness of 88 km) overlying a viscous half-space (with the upper mantle

 $^{^{10}} https://www.ngdc.noaa.gov/mgg/global/relief/ETOPO1/data/bedrock/grid_registered/netcdf$





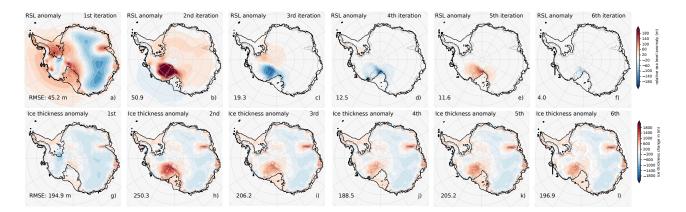


Figure 4. Anomalies of RSL (VILMA) and ice thickness (PISM) at present-day compared to Bedmap2 bedrock and ice thickness observations (Fretwell et al., 2013), for six iterations of coupled glacial cycle simulations with reference 3D Earth structure (n128) and sea level equation (n512), converging from 46 m RMSE to about 4 m RMSE for RSL anomaly (negative bed topography anomaly). This procedure does not optimize for the present-day ice thickness. The iterations show a convergence with alternating sign in mean RSL anomaly, particularly in the Siple Coast region in the Ross Sea sector.

viscosity of $5 \times 10^{20} \,\mathrm{Pa\,s}$). However, this approach is limited to a certain region (e.g. Antarctica) and is unable to solve self-consistently for sea level changes while considering a globally conserved water budget.

In VILMA not only vertically varying Earth structures (1D) can be considered, but also lateral changes in viscosity. Between West and East Antarctic plates, differences in the viscosity of the upper mantle at about 280 km depth can exceed two orders of magnitude (see Fig. 5b). Based on seismic tomography models and geodynamical constraints, a dataset for the 3D Earth structure (including the lithosphere thickness) has been optimized such that the VILMA response minimizes the misfit to a global compilation of relative sea level records (Bagge et al., 2021). In the following we refer to the Class-I-type ('v_0.4_s16') as our reference 3D Earth structure ('3D ref').

In order to test for the effects of low and high viscosity on the ice sheet dynamics and to investigate possible feedbacks we define end member Earth structures of the laterally varying reference 3D Earth structure, '3D ref'. The '3D min' and the '3D max' take the minimum and maximum of '3D ref' over the Antarctic regions south of 60° S at each depth interval (see Fig. 5a), respectively. The inferred minimum or maximum define a laterally uniform 1D Earth structure within the Antarctic region, while north of 60° S we consider the original '3D ref' structure. This implies a very thin lithosphere thickness of only a few kilometers and upper-mantle viscosities down to 10^{19} Pa s in the '3D min' case for Antarctica, while in the '3D max' case, the lithosphere thickness is around 130 km and upper-mantle viscosities remain larger than 4×10^{20} Pa s for all depth intervals (Fig. 5c).





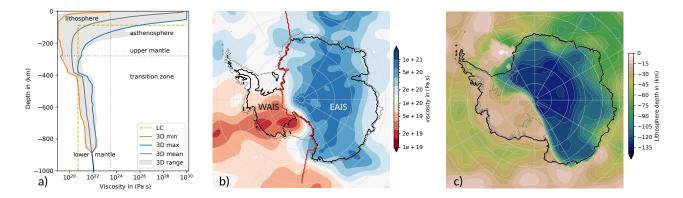


Figure 5. VILMA Earth structure. a) Vertical profiles down to 1000 km depth for 3D Earth structures, with global log-mean and range (grey), the Antarctic wide range (between orange and blue defining '3D min' and '3D max', respectively) and the two-layer profile as used in the Lingle-Clark model (olive). b) '3D ref' at 280 km depth (horizontally dotted line in a), showing a lateral variability of two orders of magnitude in viscosity (10^{19} – 10^{21} Pa s). Present-day grounding line and calving front (Bedmap2 contours from Fretwell et al. (2013), grey and black respectively), and Zwally et al. (2012) drainage basin divide (red) between WAIS (basins 2–17) and East Antarctica (basins 18–27 and 1). c) Lithosphere depth defined by $10^{23.5}$ Pa s threshold (vertical dashed line in a), showing a thin lithosphere (< 50 km) in West Antarctica and a thick lithosphere exceeding 130 km in East Antarctica.

3 Results

255

260

265

270

3.1 Sensitivity of Antarctic Ice Sheet deglaciation to spatial resolution and coupling time step

The coupling time step is an important parameter in a coupled model system. As in our coupling scheme, PISM responds to changes in relative sea level from VILMA of the previous time step, the coupling time step should be short enough to avoid delay effects of this asynchronicity. However, computational costs for the remapping of the data and the initialization of each of the model steps occur at each coupling time step (cf. Table 1). A reasonable coupling time step therefore balances costs and accuracy.

We evaluate the sensitivity of the coupled simulations to coupling time steps Δt of 1000, 100 and 10 yr by comparing the deglacial response of the Antarctic Ice Sheet over the last 20 kyr in terms of sea level equivalent ice volume (in units of m SLE). In all three cases we find a similar sea level relevant ice volume at LGM (in our simulations around 15 kyr BP) of around 72 m SLE, which is about 14 m SLE above the present level (see Fig. 6a). At the onset of deglaciation, around 14 kyr BP, we find small discontinuities in the response for the largest coupling time step (blue), at which PISM responds to changes in bed topography with 1000 yr delay. This is mostly a consequence of the diagnostic calculation of the sea level equivalent ice volume (above flotation) that also accounts for changes in bed elevation. Interestingly, during Holocene until present we find slightly smaller ice volumes (by about 1 m SLE) for $\Delta t = 1000$ yr. The extrapolation of the RSL change rate in the PISM step for this Δt (blue dashed) shows a similar effect during deglaciation. Comparing the ice sheet response for 100-yr (default) and 10-yr coupling time steps, we find only little differences, which we interpret as 'convergence'. As total



285



computational costs per modeled kyr decrease by about 20% between 1000 and 100-yr coupling time step, but by about 65% between 100 and 10 yr coupling time step, we choose a 100-yr coupling time step as the default choice for further experiments.

A recent study on time stepping and RSL precision (Han et al., 2022) with the coupled ice sheet–sea level model system of Gomez et al. (2013, 2020) suggests coupling time steps of at least 200 yr, while a previous coupled model study with coarser spatial resolution claimed that 1000 yr would be sufficient (de Boer et al., 2014). Coupling time steps of 500 yr are shown to yield accurate coupled results, when using internal iterations and linear interpolation over the coupling time step (Van Calcar et al., 2023). Idealized experiments performed with a coupled model framework with VILMA chose 50 yr (Konrad et al., 2015). In fact, an optimal temporal resolution is highly linked to the spatial resolution and the involved Earth structure.

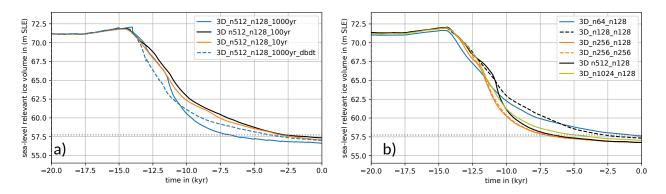


Figure 6. Sea level relevant Antarctic ice volume over last 20 kyr for different coupling time steps and different spatial resolutions.

a) Default coupling time step is 100 yr (black). Higher temporal resolution with 10 yr is shown in orange. Lower temporal resolution with a 1000 yr is shown in blue, and with extrapolation of RSL change rate in blue dashed. Here, all simulations were restarted from the default state at 20 kyr BP (6th iteration) with default spatial resolution. Shown time series have a resolution of 10 yr. b) Reference spatial resolution is n512 for the sea level equation in VILMA, n128 for the viscoelastic deformations and 16 km in PISM (black). Higher spatial resolution for the sea level equation is shown in olive (n1024), coarse resolution in blue (n64), black dashed (n128) and orange (n256). In orange dashed the resolution for the viscoelastic deformations in VILMA has been increased to n256. All simulations have been initiated from the default state at 246 kyr BP (4th iteration). The coupling time step and temporal resolution of the plotted time series is 100 yr. PISM resolution has not been varied here.

There are interactive processes between ice sheets, ocean and the solid Earth that need sufficient spatial resolution to be adequately resolved, in particular in the grounding zones of marine ice sheets. The default resolution in our coupled simulations is 16 km in the Antarctic Ice Sheet and 0.2° for the global sea level equation (n512), which corresponds to 20 km in latitude and to about 6 km in longitude at 71°S. The viscoelastic deformation is resolved with 0.7° (n128), which corresponds to about 78 km in latitude and 25 km in longitude at 71°S. A doubling in the viscoelastic resolution (n256) has only minor effects on the Antarctic Ice Sheet deglaciation (see orange lines in Fig. 6b). A coarser spatial resolution in the sea level equation, however, delays deglaciation during the Holocene (blue and black dashed lines for n64 and n128, respectively), with up to 2 m SLE difference to the reference resolution. Only small differences in ice volume are found at around 11 kyr BP for even higher spatial resolutions (cf. olive and black lines for n1024 and n512, respectively).



290

295



3.2 Antarctic Ice Sheet build-up and deglaciation within bounds of reference 3D Earth structure

The reference 3D Earth structure discussed in Bagge et al. (2021) ('3D ref') implies a large range of lithosphere thickness and mantle viscosity in key regions of the AIS. In order to evaluate the ice-dynamical effects for variation of the underlying Earth structure, we discuss changes in the AIS area (grounding line extent) and its sea level equivalent ice volume over the last 123 kyr.

First, we consider the lower bound of '3D ref', i.e. '3D min' (Fig. 5a). In our coupled simulations with '3D min' (3rd iteration), the AIS holds about $14 \,\mathrm{m}$ SLE more ice volume at the LGM (here at $15 \,\mathrm{kyr}$ BP) than observed at present ($57.9 \pm 0.9 \,\mathrm{m}$ SLE, Morlighem et al., 2020). This corresponds to a maximum LGM grounded ice extent of $15.9 \,\mathrm{mio}$. km^2 (Fig. 7b) and a total ice mass of $31.2 \,\mathrm{mio}$. Gt, respectively. For the highly viscous '3D max', the sea level relevant ice volume at LGM reaches only $10 \,\mathrm{m}$ SLE above present, corresponding to $28.9 \,\mathrm{mio}$. Gt and $15.1 \,\mathrm{mio}$. km^2 grounded ice sheet extent. In both cases, the WAIS contributes $2-3 \,\mathrm{times}$ more ice to the rising sea level since LGM than the East Antarctic Ice Sheet (EAIS) (Fig. S 2a). The largest differences in ice sheet response between '3D min' and '3D max' can be detected in the Ross and Ronne Ice Shelf basins and in the Bellinghausen and Amundsen Sea, where for '3D min' the relative sea level is up to $500 \,\mathrm{m}$ higher (and hence the underlying bedrock deeper), leading to more extended and more than $1000 \,\mathrm{m}$ thicker grounded ice (Fig. 8a, d). In Sec. 4, we will discuss this additional feedback mechanism that can explain enhanced LGM grounding line advance for weak Earth structures.

In the first iteration, without corrected initial bed topography, we find already similar differences of Antarctic ice volume evolution over time for the different Earth structures, but generally 3–4 m SLE lower ice volumes and lower ice sheet extents (transparent lines in Fig. 7a, b) than for the last iteration. During the iterations, bed topography and ice volume converge at present day towards their observed values (Fig. 3c). However, modeled grounding lines at present tend to be slightly more extended than in observations (solid lines in Fig. 7b).

The onset of deglaciation in our simulations occurs after meltwater pulse 1A (MWP1a) around 14.5 kyr BP (Peltier, 2005), with a global mean sea level rise of about 20 m in the following 350 yr (which corresponds to a mean rate of 50 mm yr⁻¹, see Fig. S 2b, c). This far-field effect, mainly in response to the northern hemisphere ice sheet losses (ICE-6G_C), reduces to about 10 mm yr⁻¹ between 14 and 7 kyr BP (in total around 55 m of global mean sea level change) and partly compensates for near-field sea level drop in Antarctica, e.g. by viscoelastic bedrock uplift (see Figs. 8g, i at 10 kyr BP, cf. Gomez et al. (2020)). During the period of deglaciation until present-day we find a slightly slower decline, both in ice volume and grounded ice area for '3D min' compared to '3D max' (Fig. 7b and Fig. S 1b). As their LGM ice volumes differ by around 3 m SLE, they provide different initial conditions at the onset of deglaciation. Grounding line retreat and ice sheet thinning (leading to ice shelf formation) can be slowed down if the isostatic rebound responds to these changes on rather short timescales. For '3D min', RSL change rates are in fact much higher than for '3D max', in West Antarctica reaching up to -500 mm yr⁻¹ instead of -20 mm yr⁻¹, while in the far-field, the RSL rises by about 10 mm yr⁻¹ (light orange shading, cf. Figs. 8g, i and Fig. S 2c, d). This quick and rather localized response defines a negative and hence stabilizing feedback on grounding line retreat (cf. Wan et al., 2022). For '3D min', rates of ice volume change and grounding line retreat remain comparably high until present. As



330

335



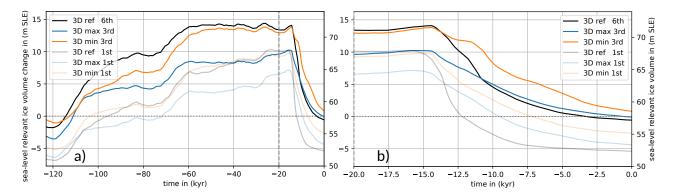


Figure 7. Sea level relevant Antarctic ice volume and grounded ice area over last 123 kyr and over last 20 kyr for different Earth structures. Blue and orange lines show the response of the Antarctic Ice Sheet in case of the '3D min' and '3D max' (cf. Fig. 5 a), which means respective 1D Earth structures south of 60°S and 3D further north. Black lines indicate the ice sheet response to '3D ref', i.e. 3D also at Antarctica. Transparent lines show the first iteration results with same initial topography; dotted horizontal line is present-day observation from Bedmap2 (Fretwell et al., 2013).

the viscoelastic rebound can take several millennia for '3D max', the stabilizing effect can be significantly delayed and active on a larger lateral extent. Over the last 3 kyr the AIS even shows a slight tendency of grounding line re-advance (Fig. S 1b), as suggested in earlier studies (with PISM-LC) for rather high mantle viscosities of 5×10^{20} Pa s (Kingslake et al., 2018).

The reference 3D Earth structure '3D ref' accounts for both, the weak Earth structure in West Antarctica and the higher mantle viscosities and thicker lithosphere in East Antarctica (Fig. 5b, c). The corresponding response of the AIS for '3D ref' shows a similar sea level equivalent ice volume ($72 \,\mathrm{m}$ SLE) and ice sheet area ($15.8 \,\mathrm{mio.\,km^2}$) at LGM as '3D min' (Fig. 7b and Fig. S 1b, black and orange contour, respectively). The largest differences in the ice loads, compared to '3D max', are located in the West Antarctic region, where a rather low mantle viscosity and a thin lithosphere are dominant (Fig. 8a, d). The additional ice load causes further subsidence of the bedrock underneath, by up to 200 m more than for '3D max' (Fig. S 3), while in the adjacent coastal region the sea floor becomes about $50 \,\mathrm{m}$ shallower than for '3D max' (Fig. 8a, light blue shading). This feature is called 'forebulge' and results from lateral transport of displaced mantle material and the flexure of the lithosphere. For '3D ref', ice loss rates can reach $1500 \,\mathrm{Gt} \,\mathrm{yr}^{-1}$ in the first millennia after the onset of deglaciation (Fig. S 2f). This is slightly higher and also earlier than for '3D min' and generally higher than for '3D max' ($<500 \,\mathrm{Gt} \,\mathrm{yr}^{-1}$). Maximum bedrock uplift rates with up to $200 \,\mathrm{mm} \,\mathrm{yr}^{-1}$ are possible for the low-viscosity response in West Antarctica (Fig. 8h), while maximum uplift rates below $50 \,\mathrm{mm} \,\mathrm{yr}^{-1}$ are associated with higher viscosities and a thicker lithosphere in East Antarctica (Fig. S 2d and Video S 1).

At present, the ice volume and grounded ice area for '3D ref' (6th iteration) converges against 57 m SLE, 13 mio. km², 24.6 mio. Gt, respectively, which is close to observations (in our diagnostic: 57.8 m SLE, 12.6 mio. km², 24.3 mio. Gt, dotted lines in Fig. 7a, b).

We have considered the upper and lower bounds of the reference 3D Earth structure in our coupled simulations ('3D max' and '3D min'). As expected, the ice sheet response for '3D ref' shows a trajectory in between those two end members.





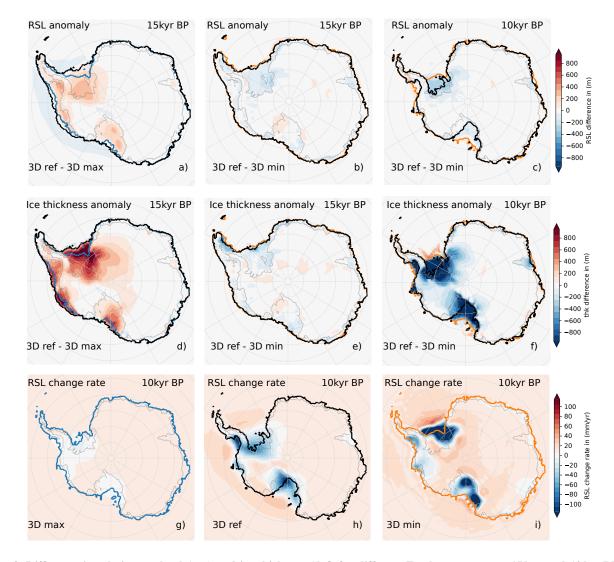


Figure 8. Difference in relative sea level (a-c) and ice thickness (d-f) for different Earth structures at 15 kyr and 10 kyr BP, and RSL change rates at 10 kyr BP for the different Earth structures (g-i). The modelled grounding line position due to the different Earth structures are shown for '3D min' (orange), '3D max' (blue) and '3D ref' (black).

Furthermore, the coupled simulations reveal that in glacial periods of grounding line advance the characteristics due to the weak Earth structure ('3D min') seem to dominate the overall ice sheet response, while in deglacial periods of grounding line retreat the AIS response is dominated rather by the characteristics of the stiffer Earth structure ('3D max'). The similarity of '3D max' and '3D ref' responses during deglaciation is even more pronounced for similar LGM ice sheet conditions (ice sheet history until 20 kyr BP prescribed as in '3D ref', see blue dashed line in Fig. S 1a).



350

355

360

365

370

375



3.3 Comparison to glacial-cycle simulations with the PISM-LC model

In order to discuss the impact of the more complete GIA model considered in the PISM-VILMA simulations, we run coupled PISM-LC simulations with the global mean sea level (GMSL) change derived from a coupled simulation with a 1D Earth structure (described in the next paragraph). The resultant GMSL timeseries is similar to the one obtained with '3D ref', as well as to the global mean ICE-6G_C, obtained with 'VM5a' Earth structure (90 km lithosphere and 500 km thick upper mantle with $5 \times 10^{20} \, \mathrm{Pa~s}$), as in all cases the same ice thickness history for the northern hemisphere is used (cf. Fig. 9a and Fig. S 2b). Note that in the PISM-LC coupling the change in global mean sea level is interpreted as a change in sea surface. For the same PISM parameters and climatic forcing as in the PISM-VILMA simulations, we find after three iterations with PISM-LC a much lower sea level relevant ice volume in Antarctica, with 59 m SLE at LGM (13 m SLE lower than for '3D ref') and 56 m SLE at present (1 m SLE lower than for '3D ref') (olive vs. black in Fig. 9b). Differences in LGM ice volume mainly result from smaller LGM grounding line extent, especially in the Weddell Sea sector (Fig. S 3). The PISM-LC results provide an estimate of the influence of GIA, although the inferred LGM ice volume in Antarctica does not seem realistic. Previous model simulations, some of them scored against different paleo records, suggest that the LGM ice volume in Antarctica was around $10 \, \mathrm{m}$ SLE larger than at present (see Fig. 11b in Albrecht et al., 2020b). For a slightly adjusted PISM parameter combination, a larger glacial ice sheet extent can be reproduced (Kingslake et al., 2018; Albrecht et al., 2020a).

If PISM-VILMA is run, analogous to PISM-LC, with a globally constant viscosity for the whole mantle of 5×10^{20} Pa s and a lithosphere thickness of 88 km (see Fig. 5a), we obtain lower Antarctic ice volumes than for '3D ref' (purple vs. black in Fig. 9b). In particular during glacial build-up the Antarctic Ice Sheet volume is about $10 \, \mathrm{m}$ SLE smaller, at LGM around $7 \, \mathrm{m}$ SLE (Fig. 9b). This is likely a consequence of the thicker lithosphere and the higher mantle viscosity in large parts of West Antarctica, which also alters the global mean sea level (Fig. 9a). Compared to the response from the PISM-LC simulations, the Antarctic Ice Sheet volume at LGM is about $6 \, \mathrm{m}$ SLE larger, likely a consequence of potentially stabilizing gravitational and rotational effects accounted for in VILMA. Regardless of the significant differences during glaciated periods, the present-day (and Last Interglacial) ice sheet volumes differ by less than $1 \, \mathrm{m}$ SLE in these simulations (Fig. 9b), as the iterative procedure minimizes the present-day misfit in bed topography.

3.4 Far-field and near-field RSL effects on Antarctic deglaciation

In our coupled simulations we focus on the dynamics of the AIS in response to the northern hemisphere ice sheet's decay. In this section we will provide an estimate of the far-field and near-field components of RSL change since LGM and compare our coupled simulation results with previous experiments in literature. Gomez et al. (2020) use a coupled ice sheet—GIA model that incorporates a global 1D (radially varying) viscoelastic mantle structure with four layers: a 50 km thick lithosphere, a 150 km thick low-viscosity zone of 10^{19} Pa s (representative for the weak structure beneath the West Antarctic Ice Sheet), an upper-mantle viscosity of 2×10^{20} Pa s and a lower-mantle viscosity of 3×10^{21} Pa s below 670 km depth (see Fig. 10c). Like in our coupled simulations, Gomez et al. (2020) prescribe the northern hemisphere ice sheet history (ICE-5G, see anomaly since LGM in Fig. 10a), while the AIS evolution is simulated with a dynamic ice sheet model (PSU-ISM with 20 km reso-





395

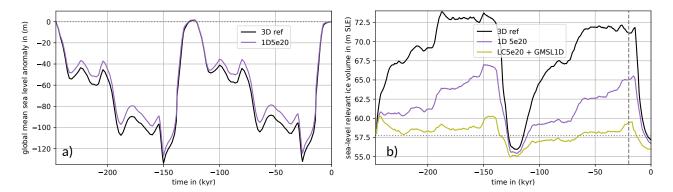


Figure 9. Comparison of global mean relative sea level a) and sea level relevant Antarctic ice volume b) over last 246 kyr for Earth models of different complexity. Olive colored for the Lingle-Clark bed deformation model with 100-yr coupling time step, upper mantle viscosity of $5 \times 10^{20} \,\mathrm{Pa\,s}$ ('LC 5e20') and 88 km lithosphere thickness ($5 \times 10^{24} \,\mathrm{Nm}$ flexural rigidity), suggesting about 3 m SLE sea level contribution since LGM. Purple for the coupled PISM-VILMA model with 100-yr coupling time step, a 1D-Earth structure with 88 km thick elastic lithosphere and $5 \times 10^{20} \,\mathrm{Pa\,s}$ viscosity in the mantle below ('1D 5e20'). This simulation also solves for the sea level equation, yielding a 6 m SLE larger contribution since LGM. The global mean of the sea level is used as forcing for the simulation with the LC model ('GMSL1D'). In black, the Antarctic Ice Sheet response to the reference 3D Earth structure '3D ref' is shown with more than 14 m SLE since LGM is shown.

lution). sea level calculations are performed up to spherical harmonic degree 512, coupled every 200 yr. Key differences are that PISM-VILMA uses a global 3D Earth structure and a synchronous coupling. Furthermore, we run iterations over the last two glacial cycles (246 kyr instead of 40 kyr). The sea level contribution from the AIS since LGM (here at 21 kyr BP) is considerably larger in our simulations (13 m SLE instead of 5 m SLE). In their coupled model setup, the simulated Antarctic ice volume changes since LGM suggest a rather low sensitivity to different radial 1D and 3D Earth structures (Pollard et al., 2017; Gomez et al., 2018).

In our coupled PISM-VILMA simulations, maximum LGM sea level fall of more than 400 m in West Antarctic Ross and Weddell embayments is much larger than the 150 m found in Gomez et al. (2020), although the pattern of RSL change is similar. As barystatic mean sea level change since LGM we find 120 m (about 107 m from the northern hemisphere in ICE-6G_C). If we prescribe the present-day AIS configuration, we can estimate the far-field RSL pattern in response to northern hemisphere ice sheet loss since LGM. It has a clear imprint of Earth rotational effects, with 75 m in East Antarctica and up to 125 m in West Antarctica (Fig. 10c), and is in agreement with Gomez et al. (2020). Substracting the far-field RSL pattern provides a first-order estimate of the near-field GIA effects, mainly the viscoelastic and gravitational GIA components. Accordingly, bedrock elevation in the interior of West Antarctica has been uplifted since LGM by up to 540 m, and in East Antarctica by less than 100 m, see Fig. 10d. At the edge of the continental shelf, the forebulge effect is of opposite sign with up to 85 m vertical bedrock displacement since LGM. This effect is presumably smaller and hence not visible in the corresponding plots by Gomez et al. (2020).





To test the impact of sea level forcing, we have also performed coupled PISM-VILMA simulations with the northern hemisphere ice history fixed at its stage 40 kyr BP, and hence a continuing far-field RSL of around 100 m below present. We found that the AIS remains almost at its LGM state until present (Fig. S 4) confirming the importance of sea level in triggering deglacial changes in our simulations, as already stated in Albrecht et al. (2020a). In a similar experiment, Gomez et al. (2020) find a delayed and less pronounced deglacial grounding line retreat in Antarctica.

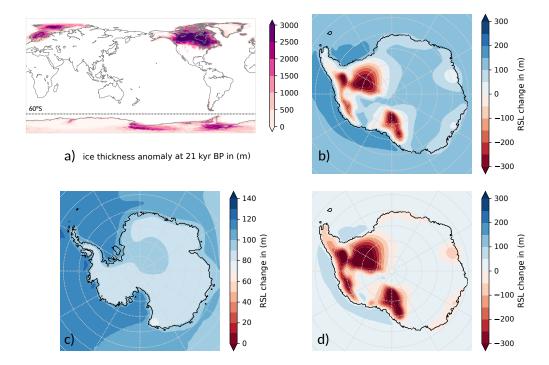


Figure 10. Contributions to deglacial sea level changes in Antarctica, analogous to Gomez et al. (2020)

a) Changes in grounded ice thickness at 21 kyr BP in the coupled PISM-VILMA simulation with reference 3D Earth structure '3D ref', based on the combination of ICE-6G_C ice history in the northern hemisphere (up to the dashed line at 60°S) and the dynamic ice sheet model for Antarctica. b) Associated total relative sea level change since 21 kyr BP in Antarctica. c) Component of relative sea level change associated with ice cover changes in the northern hemisphere, computed from a simulation with constant present-day Antarctic ice sheet thickness. Note the different color scale. d) Difference between b) and c), showing changes in relative sea level associated with Antarctic ice cover changes. These are basically caused by viscoelastic deformation and gravitational effects.

4 Discussions

A key finding of our coupled ice sheet–solid Earth study is that glacial build-up and deglacial retreat are controlled by different 405 feedbacks, which become dominant for different viscosity regimes that are associated with different response time and length scales (see Sect. 3.2). If the grounding line advances, the upstream grounded ice adds additional load. Subsidence and vis-



410

415

420

425

430

435

440



coelastically displaced mantle material produces a forebulge in the still ungrounded vicinity, which lowers the water depth and enhances grounding line advance (see schematic loop Fig. 11a). A weaker Earth structure yields faster and hence deeper subsidence in the interior during ice sheet expansion, as well as a more pronounced forebulge uplift. A thinner elastic lithosphere allows for more localized response. Grounding line advance supported by forebulge uplift can reach larger glacial extents and hence larger ice volumes, which increases loads and induces further subsidence. This is a positive *forebulge feedback* which stops, when grounding lines reach the edge of the continental shelf (Fig. 8e).

When temperatures rise and the grounding line starts to retreat into overdeepened embayments, the Marine Ice Sheet Instability (MISI) supports self-amplified grounding line retreat. With a thicker cross section, the grounding line flux increases in a non-linear manner (Schoof, 2007), which reduces the ice thickness at the grounding line leading to further retreat (Fig. 11a). As our coupled simulations suggest that a weaker Earth structure causes larger glacial ice sheet extent and more subsidence of the bedrock, this also implies an even more retrograde slope (Fig. 11b) and hence an increased potential for MISI-style grounding line retreat. However, gravitational and viscoelastic GIA effects dampen the MISI feedback and slow down grounding line retreat. This stabilizing *GIA feedback* is already known in literature (e.g. Whitehouse et al., 2019). It describes how loss in ice mass leads to lowering in RSL and hence to less grounding line retreat (see Fig. 11a).

Advancing and retreating grounding lines during Antarctic glacial cycles pass through roughly the same regions, while we assume that the solid Earth behaviour does not change over time. Largest changes in grounded ice sheet area (and in RSL) are found in the Weddell Sea and Ross embayments, as well as in the Amundsen and Bellinghausen Sea in West Antarctica, while changes in East Antarctica are comparably small. The weakest Earth structure underneath Antarctica spans between Ross embayment and Amundsen Sea (see Fig. 5), while the Earth structure becomes stronger towards the Weddell Sea, but still below the Antarctic-wide log-mean. In the Ross Sea sector the present-day grounding line seems loosely constrained by the geometry of the Siple Coast. As this is also the region with the weakest Earth structure in our setup, with a gradual and delayed modeled grounding line retreat until present-day (cf. Neuhaus et al., 2021), we find here the lowest convergence rates in the iterative procedure (Fig. 4). For grounding line advance during glacial build-up, the Earth structure in all those West Antarctic regions seems to be weak enough to be supported by the forebulge feedback. The maximum LGM extent is very similar to the LGM extent inferred in a coupled simulation with the Antarctic-wide minimum of the 3D Earth structure, '3D min'. Grounding line retreat during deglaciation tends to occur on much shorter time scales then during glacial build-up. However, due to the GIA feedback, the retreat can be strongly slowed down in regions with weak Earth structure, such as in the Ross Sea (Fig. 8). Yet, in the Weddell Sea and Bellinghausen Sea region, the MISI feedback seems to dominate the accelerated grounding line retreat. The resultant loss in total (sea level relevant) ice volume seems to follow a trajectory, which resembles a coupled simulation with the Antarctic-wide maximum or log-mean of '3D ref', i.e. '3D max' or '3D mean', respectively (see Fig. 7 and Fig. S 1). This implies, that in most Antarctic regions '3D ref' is not weak enough to obtain a significant delay of fast deglacial grounding line retreat due to the GIA feedback. This seems to be a robust feature, as we find a similar response of the Antarctic Ice Sheet for an even larger variability of 3D Earth structures (Fig. S 5–7).

The strength of the solid-Earth structure can be associated with a characteristic response time scale. In our coupled simulations we find a paradoxical behaviour: A weak Earth structure with comparably short response times tends to support the slow





glacial build-up, while it can slow down fast deglacial retreat. As we have a strongly heterogeneous 3D Earth structure, with large differences between East and West Antarctica, but also with moderate differences within West Antarctica, we find a clear asymmetry in the aggregated response to '3D ref': The mantle material is weak enough to support maximum LGM extent, while it is not weak enough to considerably slow down grounding line retreat.

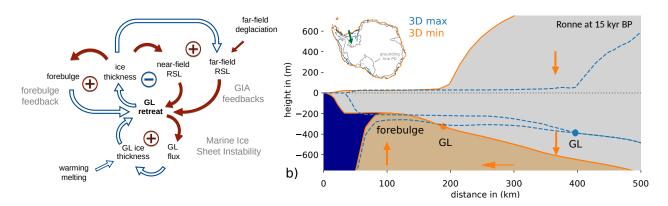


Figure 11. MISI and GIA feedbacks on grounding line migration. a) Feedback loops show the stabilizing near-field feedback of GIA on grounding line retreat (-) and the self-sustaining forebulge feedback (+) as well as the far-field (barystatic) RSL feedback (+). The Marine Ice Sheet Instability (MISI) represents a self-amplifying ice-internal feedback on grounding line (GL) retreat on retrograde slopes (+), which can be triggered by ocean-induced melting. Amplifying effects are indicated by red filled arrows (e.g. GL retreat leads to more GL flux), dampening effect by non-filled blue arrows (e.g more GL flux results in less ice thickness at the GL). b) Transect shows bedrock elevation and outlines of ice sheet and ice shelf along transect through Ronne embayment at LGM, for the two Antarctic end members of the reference 3D Earth structure, '3D max' and '3D min'. Respective grounding lines locations are about 200 km apart. Orange arrows indicate additional ice mass, subsidence of the underlying bedrock, lateral displacement of mantle material and subsequent forebulge uplift.

5 Conclusions

450

455

This study presents a new coupling framework between the ice sheet model PISM and the solid Earth model VILMA. We have run coupled simulations over two glacial cycles with PISM for Antarctica and VILMA with a global 3D viscosity structure. We find coupling time steps of $100 \, \mathrm{yr}$ between PISM and VILMA, grid resolutions of $16 \, \mathrm{km}$ for PISM in Antarctica, $0.2^{\circ} \, (\leq 20 \, \mathrm{km})$ for solving the sea level equation and $0.7^{\circ} \, (\leq 78 \, \mathrm{km})$ for solving the viscoelastic deformations in VILMA, as sufficient for capturing the relevant dynamics and feedbacks in glacial cycle simulations. We performed an outer iteration scheme over $246 \, \mathrm{kyr}$ (two glacial cycles) to adjust for the weakly constrained initial bed topography. Also, much higher resolutions are possible for the here applied offline coupling (e.g. $10 \, \mathrm{yr}$ coupling time step and 0.1° resolution for the exchange of loading and sea level response); this is possible as the field equations in VILMA are solved in the time-domain, which provides a great flexibility with regard to restart states from which further simulations can be set up.



460

465

480



The tectonic setting of the Antarctic continent reflects strong lateral contrasts in the viscoelastic Earth structure. Our model study highlights the complexity of the interactions between ice sheets, sea level and the solid Earth in Antarctica and worldwide, given the spatial variability and uncertainty of the Earth structure and associated characteristic response-time and length scales. We show that competing feedbacks and time scales are at play during Antarctic glacial build-up and deglaciation.

During phases of glacial build-up, when grounding lines advance over several ten thousands of years, a forebulge can emerge in response to viscoelastic deformations. As the forebulge supports further grounding line advance, eventually up to the edge of the continental shelf, it defines a self-amplifying feedback on ice sheet growth - which we phrase as forebulge feedback.

In contrast, during deglaciation, grounding line retreat can be slowed down as a consequence of the GIA feedback. In case of a weak Earth structure, it implies, that a fast and localized response of the solid Earth can lead to a slow response of the retreating ice sheet. On a retrograde sloping bed topography this stabilizing feedback can counteract the self-amplifying Marine Ice Sheet Instabilty, which favors fast deglaciation. In case of a stronger Earth structure, and hence longer response time scales, we find rather slow and delayed uplift, which can even cause grounding line re-advance.

Understanding the interplay of feedback mechanisms and involved time scales is highly relevant for the stability analysis of the Antarctic Ice Sheet in a warming climate. In particular, as the grounding lines of the Amundsen Sea ice shelves (e.g. Pine Island and Thwaites) are likely entry points for the initialization of the West Antarctic Ice Sheet collapse, possibly also for the Ross Sea and Weddell Sea. Hence, better constraints on the local Earth structure are required in those particularly sensitive key regions.

Our coupled model system yields self-consistent reconstructions of ice sheet and relative sea level evolutions for 3D solid-Earth structures. The modeled Antarctic ice volume at Last Glacial Maximum relative to present-day shows a high sensitivity between 10 and 15 m SLE for the different 3D Earth structures we have discussed. This is slightly more than in recent coupled ice sheet—solid Earth reconstructions (Gomez et al., 2020; Van Calcar et al., 2023), but within the range of previous model studies (Albrecht et al., 2020b, Fig. 11b). This provides confidence in the application of the PISM-VILMA coupling framework to future ice sheet and sea level projections and the investigation of tipping point characteristics.

Code and data availability. PISM code is freely available and is listed in the Research Software Directory: https://research-software-directory. org/software/pism. VILMA code can be obtained from the authors upon request. The coupling tool is freely available at: https://github.com/talbrecht/pismvilma. The data and processing code will be made publicly available on a public data repository i.e. PANGAEA or Zenodo. DOI links to the repositories will be provided upon publication.

Video supplement. Movie of change rate of relative sea level (RSL) and grounding line in Antarctica over the last 25 kyr from a coupled ice sheet–solid Earth model system, Copernicus Publications: https://doi.org/10.5446/65479, (Albrecht, 2023), Supplement Video S 1





485 Supplement.

Author contributions. TA designed the study and developed the coupling framework, with great support by MB and VK. MB provided the 3D viscoelastic Earth structures. TA wrote the manuscript and prepared the figures, with contributions from MB. All authors contributed to the interpretation of model results and revised the manuscript.

Competing interests. The authors declare that they have no competing interests.

Acknowledgements. TA and MB are funded by the German climate modeling project PalMod (FKZ: 01LP1918A, 01LP1925D, 01LP2305A and 01LP2305B) supported by the German Federal Ministry of Education and Research (BMBF) as a Research for Sustainability initiative (FONA). This work also used resources of the German High-Performance Computing Centre for Climate and Earth System Research (DKRZ) granted by its Scientific Steering Committee (WLA) under project ID bk0993. The authors gratefully acknowledge the European Regional Development Fund (ERDF), the German Federal Ministry of Education and Research and the Land Brandenburg for supporting this project by providing resources on the high performance computer system at the Potsdam Institute for Climate Impact Research (PIK). Development of PISM is supported by NASA grants 20-CRYO2020-0052 and 80NSSC22K0274 and NSF grant OAC-2118285. We thank Reyko Schachtschneider for helping revising the manuscript in an early stage.





References

- A, G., Wahr, J., and Zhong, S.: Computations of the viscoelastic response of a 3-D compressible Earth to surface loading: 500 an application to Glacial Isostatic Adjustment in Antarctica and Canada, Geophysical Journal International, 192, 557–572, https://doi.org/10.1093/gji/ggs030, 2012.
 - Accardo, N. J., Wiens, D. A., Hernandez, S., Aster, R. C., Nyblade, A., Huerta, A., Anandakrishnan, S., Wilson, T., Heeszel, D. S., and Dalziel, I. W.: Upper mantle seismic anisotropy beneath the West Antarctic Rift System and surrounding region from shear wave splitting analysis, Geophysical Journal International, 198, 414–429, https://doi.org/10.1093/gji/ggu117, 2014.
- Adhikari, S., Ivins, E. R., Larour, E., Seroussi, H., Morlighem, M., and Nowicki, S.: Future Antarctic bed topography and its implications for ice sheet dynamics, Solid Earth, 5, 569–584, https://doi.org/10.5194/se-5-569-2014, 2014.
 - Adhikari, S., Ivins, E. R., Larour, E., Caron, L., and Seroussi, H.: A kinematic formalism for tracking ice–ocean mass exchange on the earth's surface and estimating sea-level change, The Cryosphere, 14, 2819–2833, https://doi.org/10.5194/tc-14-2819-2020, 2020.
- Albrecht, T.: Movie: Simulation of the relative sea level change rate around Antarctica with PISM-VILMA over the last 25 kyr, Copernicus Publications, https://doi.org/10.5446/65479, 2023.
 - Albrecht, T., Winkelmann, R., and Levermann, A.: Glacial-cycle simulations of the Antarctic Ice Sheet with the Parallel Ice Sheet Model (PISM)—Part 1: Boundary conditions and climatic forcing, The Cryosphere, 14, 599–632, https://doi.org/10.5194/tc-14-599-2020, 2020a.
 - Albrecht, T., Winkelmann, R., and Levermann, A.: Glacial-cycle simulations of the Antarctic Ice Sheet with the Parallel Ice Sheet Model (PISM)—Part 2: Parameter ensemble analysis, The Cryosphere, 14, 633–656, https://doi.org/10.5194/tc-14-633-2020, 2020b.
- Amante, C. and Eakins, B. W.: ETOPO1 Arc-Minute Global Relief Model: Procedures, Data Sources and Analysis, NOAA Technical Memorandum NESDIS NGDC-24, National Geophysical Data Center, NOAA, Boulder, https://doi.org/10.7289/V5C8276M, 2009.
 - An, M., Wiens, D. A., Zhao, Y., Feng, M., Nyblade, A. A., Kanao, M., Li, Y., Maggi, A., and Lévêque, J.-J.: S-velocity model and inferred Moho topography beneath the Antarctic Plate from Rayleigh waves, Journal of Geophysical Research: Solid Earth, 120, 359–383, https://doi.org/10.1002/2014jb011332, 2015.
- Armstrong McKay, D. I., Staal, A., Abrams, J. F., Winkelmann, R., Sakschewski, B., Loriani, S., Fetzer, I., Cornell, S. E., Rockström, J., and Lenton, T. M.: Exceeding 1.5 C global warming could trigger multiple climate tipping points, Science, 377, eabn7950, https://doi.org/10.1126/science.abn7950, 2022.
 - Aschwanden, A. and Blatter, H.: Mathematical modeling and numerical simulation of polythermal glaciers, Journal of Geophysical Research: Earth Surface, 114, https://doi.org/10.1029/2008jf001028, 2009.
- Aschwanden, A., Bueler, E., Khroulev, C., and Blatter, H.: An enthalpy formulation for glaciers and ice sheets, Journal of Glaciology, 58, 441–457, https://doi.org/10.3189/2012JoG11J088, 2012.
 - Bagge, M., Klemann, V., Steinberger, B., Latinović, M., and Thomas, M.: Glacial-Isostatic Adjustment Models Using Geodynamically Constrained 3D Earth Structures, Geochemistry, Geophysics, Geosystems, 22, e2021GC009853, https://doi.org/10.1029/2021GC009853, 2021.
- Bakker, P., Clark, P. U., Golledge, N. R., Schmittner, A., and Weber, M. E.: Centennial-scale Holocene climate variations amplified by Antarctic Ice Sheet discharge, Nature, 541, 72, https://doi.org/10.1038/nature20582, 2017.
 - Barletta, V. R., Bevis, M., Smith, B. E., Wilson, T., Brown, A., Bordoni, A., Willis, M., Khan, S. A., Rovira-Navarro, M., Dalziel, I., et al.: Observed rapid bedrock uplift in Amundsen Sea Embayment promotes ice-sheet stability, Science, 360, 1335–1339, https://doi.org/10.1126/science.aao1447, 2018.





- Behrendt, J. C.: Crustal and lithospheric structure of the West Antarctic Rift System from geophysical investigations—a review, Global and Planetary Change, 23, 25–44, https://doi.org/10.1016/s0921-8181(99)00049-1, 1999.
 - Blank, B., Barletta, V., Hu, H., Pappa, F., and van der Wal, W.: Effect of Lateral and Stress-Dependent Viscosity Variations on GIA Induced Uplift Rates in the Amundsen Sea Embayment, Geochemistry, Geophysics, Geosystems, 22, e2021GC009807, https://doi.org/10.1029/2021gc009807, 2021.
- Book, C., Hoffman, M. J., Kachuck, S. B., Hillebrand, T. R., Price, S. F., Perego, M., and Bassis, J. N.: Stabilizing effect of bedrock uplift on retreat of Thwaites Glacier, Antarctica, at centennial timescales, Earth and Planetary Science Letters, 597, 117798, https://doi.org/10.1016/j.epsl.2022.117798, 2022.
 - Braddock, S., Hall, B. L., Johnson, J. S., Balco, G., Spoth, M., Whitehouse, P. L., Campbell, S., Goehring, B. M., Rood, D. H., and Woodward, J.: Relative sea-level data preclude major late Holocene ice-mass change in Pine Island Bay, Nature Geoscience, pp. 1–5, https://doi.org/10.1038/s41561-022-00961-y, 2022.
 - Bredow, E., Steinberger, B., Gassmöller, R., and Dannberg, J.: Mantle convection and possible mantle plumes beneath Antarctica insights from geodynamic models and implications for topography, in: The Geochemistry and Geophysics of the Antarctic Mantle, Geological Society of London, https://doi.org/10.1144/M56-2020-2, 2023.
- Briggs, R. D. and Tarasov, L.: How to evaluate model-derived deglaciation chronologies: a case study using Antarctica, Quaternary Science Reviews, 63, 109–127, https://doi.org/10.1016/j.quascirev.2012.11.021, 2013.
 - Brotchie, J. F. and Silvester, R.: On crustal flexure, Journal of Geophysical Research, 74, 5240–5252, https://doi.org//10.1029/jb074i022p05240, 1969.
 - Bueler, E. and Brown, J.: Shallow shelf approximation as a "sliding law" in a thermomechanically coupled ice sheet model, Journal of Geophysical Research: Earth Surface, 114, https://doi.org/10.1029/2008JF001179, 2009.
- Bueler, E. and van Pelt, W.: Mass-conserving subglacial hydrology in the Parallel Ice Sheet Model version 0.6, Geoscientific Model Development, 8, 1613, https://doi.org/10.5194/gmd-8-1613-2015, 2015.
 - Bueler, E., Lingle, C. S., and Brown, J.: Fast computation of a viscoelastic deformable Earth model for ice-sheet simulations, Annals of Glaciology, 46, 97–105, https://doi.org/10.3189/172756407782871567, 2007.
- Coulon, V., Bulthuis, K., Whitehouse, P. L., Sun, S., Haubner, K., Zipf, L., and Pattyn, F.: Contrasting response of West and East Antarctic ice sheets to glacial isostatic adjustment, Journal of Geophysical Research: Earth Surface, 126, e2020JF006003, https://doi.org/10.1029/2020jf006003, 2021.
 - Coulson, S., Lubeck, M., Mitrovica, J. X., Powell, E., Davis, J. L., and Hoggard, M. J.: The Global Fingerprint of Modern Ice-Mass Loss on 3-D Crustal Motion, Geophysical Research Letters, 48, e2021GL095 477, https://doi.org/10.1029/2021gl095477, 2021.
- Crawford, A. J., Benn, D. I., Todd, J., Åström, J. A., Bassis, J. N., and Zwinger, T.: Marine ice-cliff instability modeling shows mixed-mode ice-cliff failure and yields calving rate parameterization, Nature communications, 12, 2701, https://doi.org/10.1038/s41467-021-23070-7, 2021.
 - de Boer, B., Stocchi, P., and Van De Wal, R. S. W.: A fully coupled 3-D ice-sheet–sea-level model: algorithm and applications, Geoscientific Model Development, 7, 2141–2156, https://doi.org/10.5194/gmd-7-2141-2014, 2014.
- de Boer, B., Stocchi, P., Whitehouse, P. L., and van de Wal, R. S. W.: Current state and future perspectives on coupled ice-sheet–sea-level modelling, Quaternary Science Reviews, 169, 13–28, https://doi.org//10.1016/j.quascirev.2017.05.013, 2017.
 - DeConto, R. M. and Pollard, D.: Contribution of Antarctica to past and future sea-level rise, Nature, 531, 591–597, https://doi.org/10.1038/nature17145, 2016.





- Dziadek, R., Ferraccioli, F., and Gohl, K.: High geothermal heat flow beneath Thwaites Glacier in West Antarctica inferred from aeromagnetic data, Communications Earth & Environment, 2, 1–6, https://doi.org/10.1038/s43247-021-00242-3, 2021.
- Dziewonski, A. M. and Anderson, D. L.: Preliminary reference Earth model, Physics of the earth and planetary interiors, 25, 297–356, https://doi.org/10.1016/0031-9201(81)90046-7, 1981.
 - Farrell, W. E. and Clark, J. A.: On postglacial sea level, Geophysical Journal International, 46, 647–667, https://doi.org/10.1111/j.1365-246X.1976.tb01252.x, 1976.
 - Feldmann, J. and Levermann, A.: From cyclic ice streaming to Heinrich-like events: the grow-and-surge instability in the Parallel Ice Sheet Model, The Cryosphere, 11, 1913–1932, https://doi.org//10.5194/tc-11-1913-2017, 2017.
 - Feldmann, J., Albrecht, T., Khroulev, C., Pattyn, F., and Levermann, A.: Resolution-dependent performance of grounding line motion in a shallow model compared with a full-Stokes model according to the MISMIP3d intercomparison, Journal of Glaciology, 60, 353–360, https://doi.org/10.3189/2014JoG13J093, 2014.
- Fretwell, P., Pritchard, H. D., Vaughan, D. G., Bamber, J. L., Barrand, N. E., Bell, R., Bianchi, C., Bingham, R. G., Blankenship, D. D.,
 Casassa, G., Catania, G., Callens, D., Conway, H., Cook, A. J., Corr, H. F. J., Damaske, D., Damm, V., Ferraccioli, F., Forsberg, R., Fujita, S., Gim, Y., Gogineni, P., Griggs, J. A., Hindmarsh, R. C. A., Holmlund, P., Holt, J. W., Jacobel, R. W., Jenkins, A., Jokat, W., Jordan, T., King, E. C., Kohler, J., Krabill, W., Riger-Kusk, M., Langley, K. A., Leitchenkov, G., Leuschen, C., Luyendyk, B. P., Matsuoka, K., Mouginot, J., Nitsche, F. O., Nogi, Y., Nost, O. A., Popov, S. V., Rignot, E., Rippin, D. M., Rivera, A., Roberts, J., Ross, N., Siegert, M. J., Smith, A. M., Steinhage, D., Studinger, M., Sun, B., Tinto, B. K., Welch, B. C., Wilson, D., Young, D. A., Xiangbin, C., and Zirizzotti, A.: Bedmap2: improved ice bed, surface and thickness datasets for Antarctica, The Cryosphere, 7, 375–393, https://doi.org/10.5194/tc-7-375-2013, 2013.
 - Gladstone, R. M., Payne, A. J., and Cornford, S. L.: Parameterising the grounding line in flow-line ice sheet models, The Cryosphere, 4, 605–619, https://doi.org/10.5194/tc-4-605-2010, 2010.
- Goelzer, H., Coulon, V., Pattyn, F., De Boer, B., and Van De Wal, R.: Brief communication: On calculating the sea-level contribution in marine ice-sheet models, The Cryosphere, 14, 833–840, https://doi.org/10.5194/tc-14-833-2020, 2020.
 - Golledge, N. R., Menviel, L., Carter, L., Fogwill, C. J., England, M. H., Cortese, G., and Levy, R. H.: Antarctic contribution to meltwater pulse 1A from reduced Southern Ocean overturning, Nature communications, 5, 5107, https://doi.org/10.1038/ncomms6107, 2014.
 - Gomez, N., Mitrovica, J. X., Huybers, P., and Clark, P. U.: Sea level as a stabilizing factor for marine-ice-sheet grounding lines, Nature Geoscience, 3, 850–853, https://doi.org/10.1038/ngeo1012, 2010.
- Gomez, N., Pollard, D., Mitrovica, J. X., Huybers, P., and Clark, P. U.: Evolution of a coupled marine ice sheet–sea level model, Journal of Geophysical Research: Earth Surface, 117, https://doi.org/10.1029/2011JF002128, 2012.
 - Gomez, N., Pollard, D., and Mitrovica, J. X.: A 3-D coupled ice sheet–sea level model applied to Antarctica through the last 40 ky, Earth and Planetary Science Letters, 384, 88–99, https://doi.org/10.1016/j.epsl.2013.09.042, 2013.
- Gomez, N., Pollard, D., and Holland, D.: Sea-level feedback lowers projections of future Antarctic Ice-Sheet mass loss, Nature communications, 6, 8798, https://doi.org/10.1038/ncomms9798, 2015.
 - Gomez, N., Latychev, K., and Pollard, D.: A coupled ice sheet–sea level model incorporating 3D earth structure: variations in Antarctica during the last deglacial retreat, Journal of Climate, 31, 4041–4054, https://doi.org/10.1175/JCLI-D-17-0352.1, 2018.
 - Gomez, N., Weber, M. E., Clark, P. U., Mitrovica, J. X., and Han, H. K.: Antarctic ice dynamics amplified by Northern Hemisphere sea-level forcing, Nature, 587, 600–604, https://doi.org/10.1038/s41586-020-2916-2, 2020.





- 610 Gregory, J. M., Griffies, S. M., Hughes, C. W., Lowe, J. A., Church, J. A., Fukimori, I., Gomez, N., Kopp, R. E., Landerer, F., Cozannet, G. L., Ponte, R. M., Stammer, D., Tamisiea, M. E., and van de Wal, R. S. W.: Concepts and Terminology for Sea Level: Mean, Variability and Change, Both Local and Global, Surveys in Geophysics, 40, 1251–1289, https://doi.org/10.1007/s10712-019-09525-z, 2019.
 - Gudmundsson, G. H.: Ice-shelf buttressing and the stability of marine ice sheets, The Cryosphere, 7, 647–655, https://doi.org/10.5194/tc-7-647-2013, 2013.
- Hagedoorn, J. M., Wolf, D., and Martinec, Z.: An estimate of global mean sea-level rise inferred from tide-gauge measurements using glacial-isostatic models consistent with the relative sea-level record, Pure and Applied Geophysics, 164, 791–818, https://doi.org/10.1007/s00024-007-0186-7, 2007.
 - Han, H. K., Gomez, N., and Wan, J. X. W.: Capturing the interactions between ice sheets, sea level and the solid Earth on a range of timescales: a new "time window" algorithm, Geoscientific Model Development, 15, 1355–1373, https://doi.org/10.5194/gmd-15-1355-2022, 2022.
- Haseloff, M. and Sergienko, O. V.: The effect of buttressing on grounding line dynamics, Journal of Glaciology, 64, 417–431, https://doi.org/10.1017/jog.2018.30, 2018.
 - Heeszel, D. S., Wiens, D. A., Anandakrishnan, S., Aster, R. C., Dalziel, I. W., Huerta, A. D., Nyblade, A. A., Wilson, T. J., and Winberry, J. P.: Upper mantle structure of central and West Antarctica from array analysis of Rayleigh wave phase velocities, Journal of Geophysical Research: Solid Earth, 121, 1758–1775, https://doi.org/10.1002/2015jb012616, 2016.
- Hewitt, I. and Bradley, A.: Tipping point behaviour of submarine melting in ice-sheet grounding zones, Preprint at Research Square, https://doi.org/https://doi.org/10.21203/rs.3.rs-2924707/v1, 2023.
 - Hindmarsh, R. C. A.: A numerical comparison of approximations to the Stokes equations used in ice sheet and glacier modeling, Journal of Geophysical Research: Earth Surface, 109, https://doi.org//10.1029/2003jf000065, 2004.
- IPCC: Summary for Policymakers, in: Climate Change 2021: The Physical Science Basis. Contribution of Working Group I to the Sixth

 Assessment Report of the Intergovernmental Panel on Climate Change, edited by Masson-Delmotte, V., Zhai, P., Pirani, A., Connors,

 S. L., Péan, C., Berger, S., Caud, N., Chen, Y., Goldfarb, L., Gomis, M. I., Huang, M., Leitzell, K., Lonnoy, E., Matthews, J. B. R.,

 Maycock, T. K., Waterfield, T., Yelekçi, O., Yu, R., and Zhou, B., pp. 3–32, Cambridge University Press, Cambridge, United Kingdom
 and New York, NY, USA, https://www.ipcc.ch/report/ar6/wg1/downloads/report/IPCC_AR6_WGI_SPM.pdf, 2021.
- Ivins, E. R., van der Wal, W., Wiens, D. A., Lloyd, A. J., and Caron, L.: Antarctic upper mantle rheology, in: The Geochemistry and Geophysics of the Antarctic Mantle, edited by Martin, A. P. and van der Wal, W., pp. 267–294, Geological Society of London, https://doi.org/10.1144/M56-2020-19, 2023.
 - Johnson, J. S., Venturelli, R. A., Balco, G., Allen, C. S., Braddock, S., Campbell, S., Goehring, B. M., Hall, B. L., Neff, P. D., Nichols, K. A., et al.: Existing and potential evidence for Holocene grounding line retreat and readvance in Antarctica, The Cryosphere, 16, 1543–1562, https://doi.org/10.5194/tc-16-1543-2022, 2022.
- Jones, R. S., Johnson, J. S., Lin, Y., Mackintosh, A. N., Sefton, J. P., Smith, J. A., Thomas, E. R., and Whitehouse, P. L.: Stability of the Antarctic Ice Sheet during the pre-industrial Holocene, Nature Reviews Earth & Environment, 3, 500–515, https://doi.org/10.1038/s43017-022-00309-5, 2022.
 - Joughin, I. and Alley, R. B.: Stability of the West Antarctic ice sheet in a warming world, Nature Geoscience, 4, 506–513, https://doi.org/10.1038/ngeo1194, 2011.
- Joughin, I., Smith, B. E., and Medley, B.: Marine Ice Sheet Collapse Potentially Underway for the Thwaites Glacier Basin, West Antarctica, Science, 12, 49 055, https://doi.org/10.1126/science.1249055, 2014.





- Kendall, R. A., Mitrovica, J. X., and Milne, G. A.: On post-glacial sea level–II. Numerical formulation and comparative results on spherically symmetric models, Geophysical Journal International, 161, 679–706, https://doi.org/10.1111/j.1365-246X.2005.02553.x, 2005.
- Kendall, R. A., Latychev, K., Mitrovica, J. X., Davis, J. E., and Tamisiea, M. E.: Decontaminating tide gauge records for the influence of glacial isostatic adjustment: The potential impact of 3-D Earth structure, Geophysical Research Letters, 33, https://doi.org/https://doi.org/10.1029/2006GL028448, 2006.
 - Kingslake, J., Scherer, R. P., Albrecht, T., Coenen, J., Powell, R. D., Reese, R., Stansell, N. D., Tulaczyk, S., Wearing, M. G., and Whitehouse, P. L.: Extensive retreat and re-advance of the West Antarctic ice sheet during the Holocene, Nature, 558, 430, https://doi.org/10.1038/s41586-018-0208-x, 2018.
- 655 Klemann, V., Martinec, Z., and Ivins, E. R.: Glacial isostasy and plate motion, Journal of Geodynamics, 46, 95–103, https://doi.org/https://doi.org/10.1016/j.jog.2008.04.005, 2008.
 - Konrad, H., Thoma, M., Sasgen, I., Klemann, V., Grosfeld, K., Barbi, D., and Martinec, Z.: The deformational response of a viscoelastic solid earth model coupled to a thermomechanical ice sheet model, Surveys in Geophysics, 35, 1441–1458, https://doi.org/10.1007/s10712-013-9257-8, 2014.
- Konrad, H., Sasgen, I., Pollard, D., and Klemann, V.: Potential of the solid-Earth response for limiting long-term West Antarctic Ice Sheet retreat in a warming climate, Earth and Planetary Science Letters, 432, 254–264, 2015.
 - Kreuzer, M., Reese, R., Huiskamp, W. N., Petri, S., Albrecht, T., Feulner, G., and Winkelmann, R.: Coupling framework (1.0) for the PISM (1.1.4) ice sheet model and the MOM5 (5.1.0) ocean model via the PICO ice shelf cavity model in an Antarctic domain, Geoscientific Model Development, 14, 3697–3714, https://doi.org/10.5194/gmd-14-3697-2021, 2021.
- Larour, E., Seroussi, H., Adhikari, S., Ivins, E., Caron, L., Morlighem, M., and Schlegel, N.: Slowdown in Antarctic mass loss from solid Earth and sea-level feedbacks, Science, 364, eaav7908, https://doi.org/0.1126/science.aav7908, 2019.
 - Le Meur, E. and Huybrechts, P.: A comparison of different ways of dealing with isostasy: examples from modelling the Antarctic ice sheet during the last glacial cycle, Annals of Glaciology, 23, 309–317, https://doi.org/10.1017/s0260305500013586, 1996.
- Lenton, T. M., Armstrong McKay, D. I., Loriani, S., Abrams, J., Lade, S., Donges, J., Milkoreit, M., Powell, T., Smith, S., Zimm, C., Buxton,
 J., Bailey, E., Laybourn, L., Ghadiali, A., and Dyke (eds), J.: The Global Tipping Points Report 2023, Tech. rep., University of Exeter,
 Exeter, UK, https://global-tipping-points.org, 2023.
 - Levermann, A., Albrecht, T., Winkelmann, R., Martin, M., Haseloff, M., and Joughin, I.: Kinematic first-order calving law implies potential for abrupt ice-shelf retreat, The Cryosphere, 6, 273–286, https://doi.org/10.5194/tc-6-273-2012, 2012.
- Li, D.: Physical processes and feedbacks obscuring the future of the Antarctic Ice Sheet, Geosystems and Geoenvironment, 1, 100 084, https://doi.org/j.geogeo.2022.100084, 2022.
 - Lingle, C. S. and Clark, J. A.: A numerical model of interactions between a marine ice sheet and the solid earth: Application to a West Antarctic ice stream, Journal of Geophysical Research: Oceans, 90, 1100–1114, https://doi.org/10.1029/jc090ic01p01100, 1985.
 - Lloyd, A. J., Wiens, D. A., Zhu, H., Tromp, J., Nyblade, A. A., Aster, R. C., Hansen, S. E., Dalziel, I. W., Wilson, T. J., Ivins, E. R., et al.: Seismic structure of the Antarctic upper mantle imaged with adjoint tomography, Journal of Geophysical Research: Solid Earth, 125, https://doi.org/10.1029/2019JB017823, 2020.
 - Lough, A. C., Wiens, D. A., Grace Barcheck, C., Anandakrishnan, S., Aster, R. C., Blankenship, D. D., Huerta, A. D., Nyblade, A., Young, D. A., and Wilson, T. J.: Seismic detection of an active subglacial magmatic complex in Marie Byrd Land, Antarctica, Nature Geoscience, 6, 1031–1035, https://doi.org/10.1038/ngeo1992, 2013.



690



- Martinec, Z.: Spectral–finite element approach to three-dimensional viscoelastic relaxation in a spherical earth, Geophysical Journal International, 142, 117–141, https://doi.org/10.1046/j.1365-246x.2000.00138.x, 2000.
 - Martinec, Z. and Hagedoorn, J.: The rotational feedback on linear-momentum balance in glacial isostatic adjustment, Geophysical Journal International, 199, 1823–1846, https://doi.org/10.1093/gji/ggu369, 2014.
 - Martinec, Z., Klemann, V., van der Wal, W., Riva, R. E. M., Spada, G., Sun, Y., Melini, D., Kachuck, S. B., Barletta, V., Simon, K., A, G., and James, T. S.: A benchmark study of numerical implementations of the sea level equation in GIA modelling, Geophysical Journal International, 215, 389–414, https://doi.org/10.1093/gji/ggy280, 2018.
 - Mercer, J. H.: West Antarctic ice sheet and CO2 greenhouse effect: a threat of disaster, Nature, 271, 321, https://doi.org/10.1038/271321a0, 1978.
 - Milne, G. A. and Mitrovica, J. X.: Postglacial sea-level change on a rotating Earth: first results from a gravitationally self-consistent sea-level equation, Geophysical Journal International, 126, F13–F20, https://doi.org/10.1111/j.1365-246x.1996.tb04691.x, 1996.
- Mitrovica, J. X. and Milne, G. A.: On post-glacial sea level: I. General theory, Geophysical Journal International, 154, 253–267, https://doi.org/10.1046/j.1365-246X.2003.01942.x, 2003.
 - Mitrovica, J. X., Tamisiea, M. E., Davis, J. L., and Milne, G. A.: Recent mass balance of polar ice sheets inferred from patterns of global sea-level change, Nature, 409, 1026–1029, https://doi.org//10.1038/35059054, 2001.
- Morelli, A. and Danesi, S.: Seismological imaging of the Antarctic continental lithosphere: a review, Global and Planetary Change, 42, 155–165, https://doi.org/10.1016/j.gloplacha.2003.12.005, 2004.
 - Morlighem, M., Rignot, E., Binder, T., Blankenship, D., Drews, R., Eagles, G., Eisen, O., Ferraccioli, F., Forsberg, R., Fretwell, P., et al.: Deep glacial troughs and stabilizing ridges unveiled beneath the margins of the Antarctic ice sheet, Nature Geoscience, 13, 132–137, https://doi.org/10.1038/s41561-019-0510-8, 2020.
- Neuhaus, S. U., Tulaczyk, S. M., Stansell, N. D., Coenen, J. J., Scherer, R. P., Mikucki, J. A., and Powell, R. D.: Did Holocene climate changes drive West Antarctic grounding line retreat and readvance?, The Cryosphere, 15, 4655–4673, https://doi.org/10.5194/tc-15-4655-2021, 2021.
 - Nield, G. A., Whitehouse, P. L., van der Wal, W., Blank, B., O'Donnell, J. P., and Stuart, G. W.: The impact of lateral variations in lithospheric thickness on glacial isostatic adjustment in West Antarctica, Geophysical Journal International, 214, 811–824, https://doi.org/10.1093/gji/ggy158, 2018.
- Nowicki, S., Goelzer, H., Seroussi, H., Payne, A. J., Lipscomb, W. H., Abe-Ouchi, A., Agosta, C., Alexander, P., Asay-Davis, X. S., Barthel, A., et al.: Experimental protocol for sea level projections from ISMIP6 stand-alone ice sheet models, The Cryosphere, 14, 2331–2368, https://doi.org/10.5194/tc-14-2331-2020, 2020.
 - Nowicki, S. M. J., Payne, A., Larour, E., Seroussi, H., Goelzer, H., Lipscomb, W., Gregory, J., Abe-Ouchi, A., and Shepherd, A.: Ice Sheet Model Intercomparison Project (ISMIP6) contribution to CMIP6, Geoscientific Model Development, 9, 4521, https://doi.org/10.5194/gmd-9-4521-2016, 2016.
 - Otosaka, I. N., Horwath, M., Mottram, R., and Nowicki, S.: Mass Balances of the Antarctic and Greenland Ice Sheets Monitored from Space, Surveys in Geophysics, 44, 1615–1652, https://doi.org/10.1007/s10712-023-09795-8, 2023.
 - Pattyn, F.: Sea-level response to melting of Antarctic ice shelves on multi-centennial timescales with the fast Elementary Thermomechanical Ice Sheet model (f. ETISh v1. 0), The Cryosphere, 11, 1851–1878, https://doi.org/0.5194/tc-11-1851-2017, 2017.
- 720 Pattyn, F. and Morlighem, M.: The uncertain future of the Antarctic Ice Sheet, Science, 367, 1331–1335, https://doi.org/10.1126/science.aaz5487, 2020.



735



- Pattyn, F., Perichon, L., Durand, G., Favier, L., Gagliardini, O., Hindmarsh, R. C., Zwinger, T., Albrecht, T., Cornford, S., Docquier, D., et al.: Grounding-line migration in plan-view marine ice-sheet models: results of the ice2sea MISMIP3d intercomparison, Journal of Glaciology, 59, 410–422, https://doi.org/10.3189/2013jog12j129, 2013.
- Pegler, S. S.: Marine ice sheet dynamics: the impacts of ice-shelf buttressing, Journal of Fluid Mechanics, 857, 605–647, https://doi.org/10.1017/jfm.2018.741, 2018.
 - Peltier, W.: On the hemispheric origins of meltwater pulse 1a, Quaternary Science Reviews, 24, 1655–1671, 2005.
 - Peltier, W., Argus, D., and Drummond, R.: Space geodesy constrains ice age terminal deglaciation: The global ICE-6G_C (VM5a) model, Journal of Geophysical Research: Solid Earth, 120, 450–487, https://doi.org/10.1002/2014JB011176, 2015.
- Peltier, W. R.: The impulse response of a Maxwell Earth, Reviews of Geophysics, 12, 649–669, https://doi.org/10.1029/rg012i004p00649, 1974.
 - Pollard, D. and DeConto, R.: Description of a hybrid ice sheet-shelf model, and application to Antarctica, Geoscientific Model Development, 5, 1273–1295, https://doi.org/10.5194/gmd-5-1273-2012, 2012.
 - Pollard, D., DeConto, R. M., and Alley, R. B.: Potential Antarctic Ice Sheet retreat driven by hydrofracturing and ice cliff failure, Earth and Planetary Science Letters, 412, 112–121, https://doi.org/10.1016/j.epsl.2014.12.035, 2015.
 - Pollard, D., Gomez, N., and Deconto, R. M.: Variations of the Antarctic Ice Sheet in a Coupled Ice Sheet-Earth-Sea Level Model: Sensitivity to Viscoelastic Earth Properties, Journal of Geophysical Research: Earth Surface, 122, 2124–2138, https://doi.org/10.1002/2017JF004371, 2017.
- Powell, E., Gomez, N., Hay, C., Latychev, K., and Mitrovica, J.: Viscous effects in the solid Earth response to modern Antarctic ice mass flux: Implications for geodetic studies of WAIS stability in a warming world, Journal of Climate, 33, 443–459, https://doi.org/10.1175/jcli-d-19-0479.1, 2020.
 - Powell, E. M., Pan, L., Hoggard, M. J., Latychev, K., Gomez, N., Austermann, J., and Mitrovica, J. X.: The impact of 3-D Earth structure on far-field sea level following interglacial West Antarctic Ice Sheet collapse, Quaternary Science Reviews, 273, 107256, https://doi.org/10.1016/j.quascirev.2021.107256, 2021.
- Quiquet, A., Dumas, C., Ritz, C., Peyaud, V., and Roche, D. M.: The GRISLI ice sheet model (version 2.0): calibration and validation for multi-millennial changes of the Antarctic ice sheet, Geoscientific Model Development, 11, 5003–5025, https://doi.org//10.5194/gmd-11-5003-2018, 2018.
 - Ramirez, C., Nyblade, A., Hansen, S., Wiens, D. A., Anandakrishnan, S., Aster, R. C., Huerta, A. D., Shore, P., and Wilson, T.: Crustal and upper-mantle structure beneath ice-covered regions in Antarctica from S-wave receiver functions and implications for heat flow, Geophysical Journal International, 204, 1636–1648, https://doi.org/10.1093/gji/ggv542, 2016.
 - Reed, B., Green, J., Jenkins, A., and Gudmundsson, G. H.: Recent irreversible retreat phase of Pine Island Glacier, Nature Climate Change, https://doi.org/10.1038/s41558-023-01887-y, 2023.
 - Reese, R., Albrecht, T., Mengel, M., Asay-Davis, X., and Winkelmann, R.: Antarctic sub-shelf melt rates via PICO, The Cryosphere, 12, 1969, https://doi.org/10.5194/tc-12-1969-2018, 2018a.
- Reese, R., Gudmundsson, G. H., Levermann, A., and Winkelmann, R.: The far reach of ice-shelf thinning in Antarctica, Nature Climate Change, 8, 53–57, https://doi.org/10.1038/s41558-017-0020-x, 2018b.
 - Reese, R., Winkelmann, R., and Gudmundsson, G. H.: Grounding-line flux formula applied as a flux condition in numerical simulations fails for buttressed Antarctic ice streams, The Cryosphere, 12, 3229–3242, https://doi.org/10.5194/tc-12-3229-2018, 2018c.





- Rignot, E., Mouginot, J., Morlighem, M., Seroussi, H., and Scheuchl, B.: Widespread, rapid grounding line retreat of Pine Island, Thwaites, Smith, and Kohler glaciers, West Antarctica, from 1992 to 2011, Geophysical Research Letters, 41, 3502–3509, https://doi.org/10.1002/2014GL060140, 2014.
 - Rignot, E., Mouginot, J., Scheuchl, B., Van Den Broeke, M., Van Wessem, M. J., and Morlighem, M.: Four decades of Antarctic Ice Sheet mass balance from 1979–2017, Proceedings of the National Academy of Sciences, 116, 1095–1103, https://doi.org/10.1073/pnas.1812883116, 2019.
- Schannwell, C., Mikolajewicz, U., Ziemen, F., and Kapsch, M.-L.: Sensitivity of Heinrich-type ice-sheet surge characteristics to boundary forcing perturbations, Climate of the Past, 19, 179–198, https://doi.org/10.5194/cp-19-179-2023, 2023.
 - Schoof, C.: Ice sheet grounding line dynamics: Steady states, stability, and hysteresis, Journal of Geophysical Research, 112, https://doi.org/10.1029/2006JF000664, 2007.
- Seroussi, H. and Morlighem, M.: Representation of basal melting at the grounding line in ice flow models, The Cryosphere, 12, 3085–3096, https://doi.org/10.5194/tc-12-3085-2018, 2018.
 - Seroussi, H., Nowicki, S., Payne, A. J., Goelzer, H., Lipscomb, W. H., Abe-Ouchi, A., Agosta, C., Albrecht, T., Asay-Davis, X., Barthel, A., et al.: ISMIP6 Antarctica: a multi-model ensemble of the Antarctic ice sheet evolution over the 21st century, The Cryosphere, 14, 3033–3070, https://doi.org/10.5194/egusphere-egu2020-6309, 2020.
- Spada, G., Barletta, V. R., Klemann, V., Riva, R. E. M., Martinec, Z., Gasperini, P., Lund, B., Wolf, D., Vermeersen, L. L. A., and King, M. A.: A benchmark study for glacial isostatic adjustment codes, Geophysical Journal International, 185, 106–132, https://doi.org/https://doi.org/10.1111/j.1365-246X.2011.04952.x, 2011.
 - Spada, G., Bamber, J. L., and Hurkmans, R. T. W. L.: The gravitationally consistent sea-level fingerprint of future terrestrial ice loss, Geophysical Research Letters, 40, 482–486, https://doi.org/10.1029/2012gl053000, 2013.
- Steinberger, B.: Topography caused by mantle density variations: observation-based estimates and models derived from tomography and lithosphere thickness, Geophysical Journal International, 205, 604–621, https://doi.org/10.1093/gji/ggw040, 2016.
 - Sutter, J., Fischer, H., Grosfeld, K., Karlsson, N. B., Kleiner, T., Van Liefferinge, B., and Eisen, O.: Modelling the Antarctic Ice Sheet across the mid-Pleistocene transition implications for Oldest Ice, The Cryosphere, 13, 2023–2041, https://doi.org/10.5194/tc-13-2023-2019, 2019.
 - The PISM authors: PISM, a Parallel Ice Sheet Model: User's Manual, https://www.pism.io/docs/, based on stable v.2.1 edn., 2023.
- Thomas, R. H. and Bentley, C. R.: A model for Holocene retreat of the West Antarctic ice sheet, Quaternary Research, 10, 150–170, https://doi.org/10.1016/0033-5894(78)90098-4, 1978.
 - Van Calcar, C. J., Van De Wal, R. S., Blank, B., De Boer, B., and Van Der Wal, W.: Simulation of a fully coupled 3D glacial isostatic adjustment–ice sheet model for the Antarctic ice sheet over a glacial cycle, Geoscientific Model Development, 16, 5473–5492, https://doi.org/10.5194/gmd-16-5473-2023, 2023.
- Van den Berg, J., Van de Wal, R., Milne, G., and Oerlemans, J.: Effect of isostasy on dynamical ice sheet modeling: A case study for Eurasia, Journal of Geophysical Research: Solid Earth, 113, https://doi.org/10.1029/2007JB004994, 2008.
 - van der Wal, W., Whitehouse, P. L., and Schrama, E. J.: Effect of GIA models with 3D composite mantle viscosity on GRACE mass balance estimates for Antarctica, Earth and Planetary Science Letters, 414, 134–143, https://doi.org/10.1016/j.epsl.2015.01.001, 2015.
- Wan, J. X. W., Gomez, N., Latychev, K., and Han, H. K.: Resolving glacial isostatic adjustment (GIA) in response to modern and future ice loss at marine grounding lines in West Antarctica, The Cryosphere, 16, 2203–2223, https://doi.org/10.5194/tc-16-2203-2022, 2022.



805



- Weber, M. E., Clark, P. U., Kuhn, G., Timmermann, A., Sprenk, D., Gladstone, R., Zhang, X., Lohmann, G., Menviel, L., Chikamoto, M. O., Friedrich, T., and Ohlwein, C.: Millennial-scale variability in Antarctic ice-sheet discharge during the last deglaciation, Nature, 510, 134–138, https://doi.org/10.1038/nature13397, 00002, 2014.
- Weertman, J.: Stability of the junction of an ice sheet and an ice shelf, Journal of Glaciology, 13, 3–11, https://doi.org/10.1017/s0022143000023327, 1974.
 - Whitehouse, P. L.: Glacial isostatic adjustment modelling: historical perspectives, recent advances, and future directions, Earth Surface Dynamics, 6, 401–429, https://doi.org/10.5194/esurf-6-401-2018, 2018.
 - Whitehouse, P. L., Bentley, M. J., Milne, G. A., King, M. A., and Thomas, I. D.: A new glacial isostatic adjustment model for Antarctica: calibrated and tested using observations of relative sea-level change and present-day uplift rates, Geophysical Journal International, 190, 1464–1482, https://doi.org/10.1111/j.1365-246X.2012.05557.x, 2012.
 - Whitehouse, P. L., Gomez, N., King, M. A., and Wiens, D. A.: Solid Earth change and the evolution of the Antarctic Ice Sheet, Nature communications, 10, 503, https://doi.org/10.1038/s41467-018-08068-y, 2019.
 - Winkelmann, R., Martin, M. A., Haseloff, M., Albrecht, T., Bueler, E., Khroulev, C., and Levermann, A.: The Potsdam Parallel Ice Sheet Model (PISM-PIK) Part 1: Model description, The Cryosphere, 5, 715–726, https://doi.org/10.5194/tc-5-715-2011, 2011.
- 810 Yang, H., Krebs-Kanzow, U., Kleiner, T., Sidorenko, D., Rodehacke, C. B., Shi, X., Gierz, P., Niu, L., Gowan, E. J., Hinck, S., et al.: Impact of paleoclimate on present and future evolution of the Greenland Ice Sheet, Plos one, 17, e0259816, https://doi.org/10.1371/journal.pone.0259816, 2022.
 - Zeitz, M., Haacker, J. M., Donges, J. F., Albrecht, T., and Winkelmann, R.: Dynamic regimes of the Greenland Ice Sheet emerging from interacting melt–elevation and glacial isostatic adjustment feedbacks, Earth System Dynamics, 13, 1077–1096, https://doi.org//10.5194/esd-13-1077-2022, 2022.
 - Ziemen, F. A., Kapsch, M.-L., Klockmann, M., and Mikolajewicz, U.: Heinrich events show two-stage climate response in transient glacial simulations, Climate of the Past, 15, 153–168, https://doi.org/10.5194/cp-15-153-2019, 2019.
 - Zwally, H. J., Giovinetto, M. B., Beckley, M. A., and Saba, J. L.: Antarctic and Greenland drainage systems, GSFC cryospheric sciences laboratory, http://imbie.org/imbie-2016/drainage-basins/, 2012.