Sea ice melt pond bathymetry reconstructed from aerial photographs using photogrammetry: A new method applied to MOSAiC data.

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Abstract.

Melt ponds are a core component of the summer sea ice system in the Arctic, increasing the uptake of solar energy and impacting the ice-associated ecosystem. They were thus one of the key topics during the one-year drift campaign MOSAiC in the Transpolar Drift 2019/2020. Pond depth is a dominating factor in the description of the surface meltwater volume, necessary to estimate budgets, and used in model parametrization to simulate pond coverage evolution. However, observational data on pond depth is spatially and temporally strongly limited to a few in situ measurements. Pond bathymetry, which is pond depth spatially fully resolved, remains entirely unexplored. Here, we present a newly developed method to derive pond bathymetry from aerial images. We determine it from a photogrammetric multi-view reconstruction of the summer ice surface topography. Based on images recorded on dedicated grid flights and facilitated assumptions, we were able to obtain pond depth with a mean deviation of 3.5 cm compared to manual in situ observations. The method is independent of pond color and sky conditions, which is an advantage over recently developed radiometric airborne retrieval methods. It can furthermore be implemented in any typical photogrammetry workflow. We present the retrieval algorithm, including requirements for the data recording and survey planning, and a correction method for refraction at the air—pond interface. In addition, we show how the retrieved surface topography model synergizes with the initial image data to retrieve the water level of individual ponds from the visually determined pond margins.

We use the method to give a profound overview of the pond coverage on the MOSAiC floe, on which we found unexpected steady pond coverage and volume. We were able to derive individual pond properties of more than 1600 ponds on the floe, including their size, bathymetry, volume, surface elevation above sea level, and temporal evolution. We present a scaling factor for single in situ depth measurements, discuss the representativeness of in situ pond measurements, and show indications for non-rigid pond bottoms. The study points out the great potential to derive geometric properties of the summer sea-ice surface emerging from the increasingly available visual image data recorded from UAVs or aircraft, allowing for an integrated understanding and improved formulation of the thermodynamic and hydrological pond system in models.
1 Introduction

Melt ponds are a key driver of the summer energy budget on the sea-ice surface. Their tremendous impact on the surface albedo and related self-reinforcing feedbacks lead to increased uptake of solar radiation (Fetterer and Untersteiner, 1998). However, the effects of melt ponds used to be parameterized rather simplified in global climate models due to limited reference data, coarse resolution, and computing power (e.g., Pedersen et al., 2009a). Observational reference data that allow an integrated understanding of the thermodynamic and hydrological pond system are still rare (Wright and Polashenski, 2018). In particular, most melt pond depth observations used so far for model developments have been collected manually on the ice and were published in Morassutti and Ledrew (1996). They report greater pond depths on multi-year ice (MYI) (27.4 cm) and land-fast ice (LFI) (31.0 cm) in comparison to first-year ice (FYI) (13.0 cm). However, high variances of depths occurred between ice types and across spatial scales due to the inconsistent morphological nature of the different ice types. During the one-year Multidisciplinary drifting Observatory for the Study of Arctic Climate (MOSAiC) from 2019 to 2020, Webster et al. (2022) found average depths of 22±13 cm along transect lines. The actual pond bathymetry, which fully resolves the pond depth profile in all directions and therefore also yields the actual average pond depth, however, remains mainly undiscussed in literature.

Pond depth as a bulk property is used as a parameter in melt pond schemes in the Community Climate System Model, version 4 (CCSM4) (Holland et al., 2012) and the Los Alamos sea ice model CICE (Flocco et al., 2012). Holland et al. (2012) directly relate the use of different optical properties parameterizations of the sea ice surface to pond depth and retrieve pond fraction from the available meltwater volume by formulating a linear relationship between pond fraction and pond depth, which gives them the filled pond volume. Pedersen et al. (2009b) developed a summer sea ice albedo scheme for the ECHAM5 general circulation model in which they derive pond fraction from pond depths given by surface melt rates. The link between fraction and depth was developed based on a small-scale pond model by Lüthje et al. (2006).

A broader, more solid database of pond depths is still missing, yet crucial for parameterizations in sea-ice models building upon a deeper understanding of pond evolution and interactions. Promising new methods like the study by König et al. (2020) reveal that optical remote sensing of the full pond bathymetry is possible on larger scales. They used the increased absorbance of radiation in liquid water at a wavelength of 720 nm to determine the thickness of the liquid water column independently of the pond bottom appearance from hyperspectral data. With this passive radiometric method, a spacious area could be covered by high-resolution optical data in the respective spectral band. However, the spectral method is restricted to observations under clear sky conditions and, therefore, is still rather limited in application. Tilling et al. (2020) and Farrell et al. (2020) evaluated photon backscatter signals measured by IceSAT-2 over sea ice and showed that the depth of particularly large and deep ponds could be retrieved from the satellite along its flight track lines. Another active technique to determine shallow water bathymetry on a large scale is using airborne laser scanner (ALS) systems with water penetrating wavelengths in the green spectrum as airborne laser bathymetry (ALB) systems. To our knowledge, however, there has not been any closer operation of ALB from aircraft over sea ice until now.

Aerial RGB imaging platforms are numerously available and have been deployed in the Arctic for decades. They are already widely used to retrieve properties of bare surfaces in all different fields of geodetic studies. If the flight pattern is suitable,
photogrammetric multi-view reconstruction can derive digital elevation models (DEMs) from aerial images. Sufficient forward
and lateral overlap between images (about 80% and 60%, respectively), results in ground points being recorded from more than
fifteen different azimuth and elevation angles. This is used to achieve a triangulation-based reconstruction with a monocular
camera system. A few studies could already show that the reconstruction method can be applied in mix-phased areas to retrieve
bottom topography of shallow river beds (Westaway et al., 2001), coral reefs (Casella et al., 2017) and in laboratory sea bed
studies (González-Vera et al., 2020). From the nature of the method, the underlying ice or seafloor surface and some structure
on it must be visible to get reconstructed. This limits the method to clear waters and shallow depths. Furthermore, appropriate
correction methods for the light refraction at the water–air interface are needed. Although melt ponds probably closely conform
to these requirements, there was not yet a detailed developed method for deriving pond depth from aerial photographs.

Only one experimental study was carried out above sea ice before by Divine et al. (2016). They used a complex stereo-
vision camera system on a helicopter to detect the sea-ice surface morphology and melt pond depths north of Svalbard in 2012.
Comparing their results of photogrammetrically derived ice freeboard with terrestrial laser scanner data, they retrieved high
agreement (BIAS of 0.03 m) and low deviation (RMS of 0.04 m). Remarkably, they also retrieved the same accuracy when
comparing melt pond depths with manually measured in situ data, although no physical correction was applied, which considers
the different optical properties of water and air, that make subsurface areas appear shallower. Potentially, the measured depths
(<0.3 m) were too small to detect these effects. In contrast, Casella et al. (2017) measured significantly greater depths down to
1.8 m in coral reefs, also neglecting differences in optical properties, arguing that almost nadir measurements do not require
corrections. Other studies on shallow water bathymetry set up entirely new sets of equations to correct for light bending at
the air–water interface directly in the photogrammetric reconstruction, requiring extensive efforts to solve the complex sets of
equations in a reasonable time.

Given that photogrammetric methods for surface reconstruction from aerial images are well developed, reaching a user-
friendly status, and the increasing availability of aerial images (also from drones) collected from monocular camera systems, we
investigate here whether corrections can be incorporated into a feasible workflow based on a commonly used photogrammetry
suite to reconstruct entire melt pond bathymetry. Subsequently, we investigate with the newly developed method how pond
bathymetry evolved on the MOSAiC floe of leg 4, how representative transect lines described the pond evolution on the entire
floe and discuss possible upscaling factors for in situ point measurements.

## 2 Overview of data and ice conditions

### 2.1 Images and field data used in the method development from PASCAL 2017

We developed and initially tested the method on data from RV *Polarstern* Cruise PS106/1 (PASCAL) that took place in June
2017, due to coordinated manual ground-truth measurements. It was subsequently confirmed for deeper ponds (>0.4 m) with
data from the MOSAiC expedition. During PASCAL (Macke and Flores, 2018), we measured pond depths as a reference for
the development of remote sensing-based pond depth retrievals (including: König and Oppelt, 2020; König et al., 2020) and
as part of a geodetic survey of ponds, including their depth and bottom ice thickness. Matching airborne data to study the
photogrammetrical pond depth retrieval was available from two days: 10 June 2017 and 14 June 2017. On both days, RGB images were acquired above the in situ measurement area in a flight pattern that allows for the photogrammetrical retrieval of surface topography. In addition to a high overlap of images in the forward direction which was given in nearly all images captured during the campaign, a crucial lateral offset of the acquisition positions was given on both days. The ice floe to which RV *Polarstern* was anchored during the campaign was located north of Svalbard at 81°50' North and 10°20' East. Given the location, zone 32N in the Universal Transverse Mercator system (UTM32N, EPSG:32632) was used as a projected coordinate system for all geometric evaluation of the data.

The study area was located approximately one kilometer behind the stern of RV *Polarstern* in a young, first and second-year ice region that was, before our visit in June 2017, subject to strong deformation (König et al., 2020). Between rafted ice floes along a ridge, several depressions had been formed and were flooded with sea water. At the time of our arrival, the PASCAL floe was already subject to melting, but visible melt ponds on level ice had not yet formed. The studied depressions were thus most probably initially formed by flooding and provided, at the time of our stay at the floe, a sink for incoming solar radiation, which then led to a catalyzed melt pond formation in the particular region. Due to the very diverse appearance of the underlying ice from bright blue to almost black, this was nonetheless an ideal study area (Fig. 1), even though these ponds cannot be designated strictly as melt ponds.
Images on 10 June (Fig. 1a) were acquired from RV Polarstern helicopter D-HARK with the implemented CANON EOS 1D Mark III 14mm lens nadir camera system during the measurement flight 20170610-2, which took advantage of the thoroughly clear sky conditions and aimed at an up-scaling of ground measurements. Therefore several flight legs were flown in different flight levels (60 m to 3000 m) above the study area. For this method development study, relying on high-resolution data, all images were used that have been captured below 200 m flight altitude and therefore provide a ground sampling distance (GSD) more precise than 10 cm, which is at least one order of magnitude smaller than typical pond extents at the study site.

Weather conditions on 14 June (Fig. 1b) were exactly the opposite and much more common for the Arctic summers. The entire sky was covered by a stratiform cloud cover. No solar disc was visible, meaning incident light can largely be assumed to be diffuse at that time. Images from that day were captured during measurement flight 20170614-1. Due to the sky conditions, flight altitude was limited to 300 ft (≈100 m), so no further altitude filtering was needed.

The measured ponds were assigned numbers #1 to #9 (Fig. 1). Ponds #1_2 and #4_2 merged with two larger ponds #1 and #4 over the course of four days. The selection of ponds for the analysis depended solely on the availability of in situ depth measurements carried out on-site as part of the measurement program and their location in the center of the flight pattern. Due to their position outside the photographed area, some ponds examined in König et al. (2020) had to be left out of this study.

Manual pond depth measurements were collected with a meterstick, and the locations of the measurements used here were determined relative to reference points beside the ponds or marked manually in aerial images from the previous day. We assume a horizontal accuracy of the measurement location of 0.3 m, which should not strongly impact the depth measurement accuracy in the center of ponds.

Pond depth in the study area on PS106 reached from 7 cm to 26 cm on June 10 and 5 cm to 37.5 cm on June 14 (Table 1). We separated ponds by their either bright-blueish or dark-greyish appearance to prove the independence of our approach from the optical properties of the pond bottom. Manual depth measurements show that there were no systematic differences in depth between these groups. Drilling through the pond bottom after completing all other measurements revealed that all ponds were in an equilibrium state with sea level. Ponds #1,#3,#4 were measured on both days, while ponds #5 to #9 were only measured on the first day. Ponds #1_2 and #4_2 had merged with #1 and #4 in the ongoing melt process. Pond #2 was measured only on the second day. Pond coverage increased notably in the study area during the four days.

### 2.2 Aerial image data collected during MOSAiC 2020

Aerial image collection was part of helicopter grid surveys being part of the regular measurement program executed during the year-long drift campaign MOSAiC onboard the RV Polarstern from 2019 to 2020 (Nicolaus et al., 2022). During the drift, RV Polarstern had to be re-positioned several times, with a prolonged break in data during the initial pond formation period between 16 May 2020 and 19 June 2020 because of a pandemic-related crew exchange on Svalbard. At the time of RV Polarstern’s return during leg 4, a distinct floe had emerged, round-shaped and with a diameter of 1 km. It became the new location of the central observatory (called in Webster et al. (2022): Central Observatory 2, CO2). This new floe of leg 4 formed from a former ice formation called the Fortress (von Albedyll et al., 2022); strongly compressed and deformed ice adjacent to the previous legs’ Central Observatory area.
Table 1. In situ pond depth measurement statistics and pond color type bright-blueish (bb) or dark-greyish (dg) from the PS106/1 pond study site.

<table>
<thead>
<tr>
<th># pond</th>
<th>number of measurements</th>
<th>mean depth [cm]</th>
<th>standard deviation [cm]</th>
<th>min. [cm]</th>
<th>max. [cm]</th>
<th>kind</th>
</tr>
</thead>
<tbody>
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<tr>
<td>10 June 2017</td>
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<td></td>
<td></td>
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<tr>
<td>1</td>
<td>1</td>
<td>20.5</td>
<td>4.9</td>
<td>9.5</td>
<td>25.0</td>
<td>bb</td>
</tr>
<tr>
<td>3</td>
<td>2</td>
<td>8.5</td>
<td>-</td>
<td>7.0</td>
<td>10.0</td>
<td>dg</td>
</tr>
<tr>
<td>4</td>
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<td>17.7</td>
<td>1.6</td>
<td>16.0</td>
<td>21.0</td>
<td>dg</td>
</tr>
<tr>
<td>5</td>
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<td>12.0</td>
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<tr>
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<td>7.5</td>
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<tr>
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<td>14.4</td>
<td>2.3</td>
<td>10.0</td>
<td>17.0</td>
<td>dg</td>
</tr>
<tr>
<td>14 June 2017</td>
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<td>5.0</td>
<td>31.0</td>
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<td>4</td>
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<td>19.5</td>
<td>6.8</td>
<td>8.0</td>
<td>25.0</td>
<td>dg</td>
</tr>
</tbody>
</table>

Orthomosaic and DEMs of the entire MOSAiC leg 4 floe are available from 30 June 2020, 17 July 2020 and 22 July 2020 (Neckel et al., 2022). They were compiled using the methods described in Neckel et al. (2023) and Fuchs (2023c) and cropped here to the extent of 2 km² x 2 km² around the floe. The floe edge was retraced manually in QGIS (QGIS Development Team, 2020) to eventually retrieve statistical data only within the floe area. Classification into three main surface types (ice/snow, ponds and open water) was derived applying the sea ice image classification tool PASTA-ice (Fuchs, 2023c) on the brightness corrected orthomosaics (l2 data) on 17 July 2020 and 22 July 2020 and on the brightness corrected orthomosaic with cloud correction (l2b data) on 30 June 2020.

Photogrammetrically reconstructed DEMs from 30 June 2020 and 22 July 2020 were leveled to zero water level using a flat plane fitted trough all lateral snow/ice–open water boundaries positions in the DEM within the cropped extent of 2 km² x 2 km². For 17 July 2020, this processing was not possible, as the DEM shows strong deviations outside of the floe area because of the non-uniform drift of smaller floes around during the grid survey, which made it impossible to extract the water level from the DEM. However, manual inspection of level ice areas and single well-reconstructed water–ice boundaries confirmed that no further correction was required on this day in the area of the floe itself.
3 Method development

The method development was performed with the PASCAL data, due to the availability of ground truth measurements. Flight patterns not yet adapted for depth determination also made it possible to develop a series of corrective measures which, depending on the quality of the data, can also be used in future campaigns.

3.1 Photogrammetric surface reconstruction

We use the commercial photogrammetry suite Agisoft Metashape to solve the complex aerial triangulation equations to calculate orthomosaics and DEM as georeferenced raster data. The continuous drift of the ice during the measurement is thereby automatically corrected in the bundle-block-adjustment by recalculating acquisition positions relative to the ice floe. Each surface point in the area of the studied ponds was captured on both days with more than nine different images. The ground sampling distance of both raster maps, orthomosaic and DEM, on both days, is 10 cm per pixel in the horizontal plane. The vertical resolution of the calculated DEM is $10 \times 10^{-6}$ m. Camera positions determined by aerial triangulation led to a reprojection error of images of 0.96 pixels (10 June 2017) and 1.03 pixels (14 June 2017). The ice drift was, therefore, successfully corrected by the determination of artificial image recording positions, relative to the ice, moved with the drift in a Lagrangian approach. Since ground control points (GCPs) with well-known position data were not available for a further accuracy assessment, a 2.00 m $\times$ 2.00 m black reference target located at the ice surface close to the ponds (Fig. 1) was used as scaling reference. Length scale accuracy of the raster data was thereby determined to $\pm$2 %. DEMs were smoothed using the moderate depth map filter in Agisoft Metashape to avoid unnatural spikes in the model due to incorrect triangulation of single points.

3.2 Light refraction at the water–air interface

The photogrammetrical determination of the DEM relies on collinearity. Hence, optical beam paths between the observed ground surface and the lens are assumed to be straight. They are defined by the external orientation of the camera and the ground elevation. Distortions of the linear beam path are only considered in the camera optics and are corrected using the constant intrinsic camera parameters and the Brown camera model directly integrated into the workflow. However, this basic assumption, valid for typical one-medium, low-level airborne observations, is invalidated in the case of underwater pond bottom observations by light refraction at the water–air interface. Due to the reduced speed of light in water compared to air, the electromagnetic wave, respectively light beam, is refracted more strongly away from the normal as it exits the water. The change from the angle of incidence $\beta$ to the angle of emergence $\alpha$ at the interface between water and air is described by Snell’s law:

$$n_{\text{air}} \cdot \sin(\alpha) = n_{\text{water}} \cdot \sin(\beta)$$  \hspace{1cm} (1)

With $n$ representing the refractive indices of air and water. Both are assumed constant in this work with $n_{\text{air}} = 1$ and $n_{\text{water}} = 1.335$ (Millard and Seaver, 1990) (value for freshwater at 0 °C increased by 0.001 to account for salt remnants in the pond water). We found that dispersion, the wavelength dependency of the refractive index, does not have to be taken into account here.
in the wavelength range of the camera between 300 nm to 700 nm as it leads to deviations below the measurement resolution and accuracy. Further assumptions to describe the recorded beam paths from the pond bottom to the camera are:

1. no reflection or scattering of incident light at the pond surface or in the water column

2. reflection of incident light at the pond bottom can be approximated by Lambert’s law

These assumptions go along with those made in Malinka et al. (2018) for the optical properties of pond bottoms with slight modifications. To match assumption 1, in clear sky conditions, all images with sun glint on the pond surface need to be removed from the analysis. However, given the typically low solar elevations in the high latitudes, there was no sun glint on pond in the observations used here due to (i) mostly wave-free pond surfaces and (ii) almost nadir measurements. The reflection of diffuse light at the pond surfaces in overcast conditions does not affect the structure recognition. It therefore does not pose a problem as it does in the pure optical retrieval algorithm of König et al. (2020).

Refraction at the pond–air interface may result in an underestimation of pond depth in photogrammetric measurements. In the following, we follow an idealized sketch of optical paths given in Fig. 2 to describe correction factors retrieved to cope with the impact of refraction. The overarching goal of the method was to preserve or restore colinearity in the multi-view surface reconstruction so that an integrated evaluation with Agisoft Metashape is still feasible. This approach, therefore, differs strongly from previous studies, which were set up on a completely new and complex set of equations (e.g., Westaway et al., 2001), which then take into account the refraction of light, but do not rely on highly specialized programs to solve it efficiently, or merely neglected the impact of optical effects (e.g., Casella et al., 2017; Divine et al., 2016).

Figure 2 shows the virtual and actual intersection of beamlines in a pond from two opposite and monocular observational positions. The actual intersection point $AP$ represents the true pond bottom, while the virtual point $TP$ is located at the depth where the beamlines would intersect without refraction. The latter is the one determined by Agisoft Metashape.

To better understand the approximations derived from it, we retrace the optical path from the pond bottom to the camera in three steps: (I) A recognizable pattern allows a point on the pond bottom to be clearly identified on different images captured from different positions. We call this key point at its actual position $AP$ and assign the Cartesian coordinates $AP(X_{AP}, Y_{AP}, Z_{AP})$. (II) As we consider $AP$ a Lambertian reflector, identical beams radiate from the point in all unobscured directions. Two of them reach the monocular observation points camera 1 and camera 2, which symbolize two pixels in different aerial images taken along the flight track. These beamlines are not straight but bent at the water–ice interface. The angle of emergence $\alpha$ is larger than the angle of incidence $\beta$ and defined by Snell’s Law: $\alpha = \arcsin(n_{water} \cdot \sin(\beta))$. (III) The coordinate of the origin of $AP$ is determined by aerial triangulation from all available camera positions. Since this is based on the assumption of colinearity, the obtained virtual position of the point in the reconstruction is located in $TP(X_{TP}, Y_{TP}, Z_{TP})$. $TP$ deviates in height from the original position $Z_{AP}$ by $\Delta z$ and since camera positions usually do not all have exactly the same elevation angle also in its horizontal position $X_{TP}$ and $Y_{TP}$ by $\Delta x$.

This results in two deviations in the colinearity approximation caused by the pond water that must be corrected or avoided, a vertical and a horizontal one. Both deviations are discussed separately in the following two paragraphs.
3.2.1 Horizontal deviation

The horizontal deviation $\Delta x$ potentially causes a mismatch of point detections and should therefore be avoided in an integrated scheme. We consider it sufficiently suppressed when $\Delta x$ is smaller than the ground sampling distance. $\Delta x$ is directly dependent on both angles of emergence and the measured pond depth $Z_{TP}$. We define the ratio between horizontal deviation and measured pond depth as deviation factor $\kappa$, with:

$$\kappa = \frac{\Delta x}{Z_{TP}}$$

(2)

Figure 3 shows how $\kappa$ changes with both incident angles. In a flight altitude of 300 ft, which is a good choice for highly resolved pond studies, the ground sampling distance of the CANON camera system is approximately 0.05 m. This means, for all measured pond depths $Z_{TP}$ up to 1.5 m, the maximal horizontal deviation $\Delta x = \kappa \cdot Z_{TP} = 0.042$ m caused by refraction remains below the measurement resolution and the photogrammetric projection error when we restrict incident angles to $\alpha_{max} = 40^\circ$. We see it as a good compromise between moderate horizontal deviation and enough field-of-view to preserve sufficient overlap of images. All image pixels at larger opening angles relative to the nadir are therefore neglected in the reconstruction. This is done by creating masks individually for every single image depending on the orientation angle of the camera derived from the camera alignment process in Metashape.
3.2.2 Vertical correction

After examining how horizontal deviations can be avoided, this section concerns the underestimation of the measured pond depth $Z_{TP}$ owing to refraction. We discuss how it can be corrected with a correction factor $\gamma$ defined by $Z_{AP} = \gamma \cdot Z_{TP}$. $\gamma(\alpha)$ is given by:

$$\gamma(\alpha) = \cos(\alpha) \cdot \sqrt{n_{\text{water}}^2 - \sin^2(\alpha)}$$

(3)

It can be shown that the correction factor $\gamma$ converges towards the refractive index of water $n_{\text{water}}$ for arbitrarily small $\alpha$ and eventually becomes equal to $n_{\text{water}}$ at exactly $\alpha = 0$ (see supplementary material for the equation solutions).

$$\lim_{\alpha \to 0} \gamma(\alpha) = n_{\text{water}}$$

(4)

This contradicts the statement in Casella et al. (2017) that refraction does not influence underwater depths retrieved from almost nadir images. Rather, our mathematical and geometrical evaluation shows that almost nadir depth measurements must be multiplied with the refraction index to achieve correct depth values. When $\alpha$ increases, $\gamma$ rises slowly at first and eventually very strongly (Fig. 4a). In the previously defined range of maximal 40° incident angle, $\gamma$ reaches a maximum value of $\gamma_{\text{max}} = 1.527$. However, since derived depths result from averaging numerous intersection rays with mostly small angles of incidence, the small increase of $\gamma$ is ignored, and $\gamma$ is kept constant and equal to the refractive index of water $n_{\text{water}}$ in our method for the correction of all underwater pixels.
An additional conclusion can be drawn for the horizontal deviation from this analysis. Figure 4 shows that water depths are systematically underestimated with the measured pond depth, which means that the previously obtained maximum opening angle $\alpha_{\text{max}}$ in fact allows for greater actual pond depths than assumed in section 3.2.1, in which we limited the virtual pond depth $Z_{\text{TP}}$ to 1.5 m.

### 3.3 Pond depth determination

Pond depth $d$ is the vertical extent of the water column in ponds. It is composed of the vertical position of the pond bottom $h_{\text{bot}}$ and the height of the pond water surface $h_{\text{surf}}$ (Fig. 5). Large altitude inaccuracies of aircraft positioning systems, especially in high latitudes, make it impossible to use the GPS aircraft altitude and the reconstructed distance to the ground as an absolute height reference above sea level. That is why studies of ice topography with, for example, ALS, usually use areas of very thin ice or open water to be referenced to water level (Hutter et al., 2023). For ponds, the reference is even more complex since pond depth is, as previously mentioned, not only prescribed by the topography of the pond bottom but also by the individual height of the water level in the pond. This water level is typically above sea level, partially caused by impermeable sea ice or later in the season, when ice is typically permeable, by the density difference between freshwater in the pond and underlying seawater. The pond water level is individual for every single pond, especially during the early stages of melt pond formation, i.e. the

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**Figure 4.** Geometrical evaluation of depth correction factor $\gamma$ for equal measuring angles (a) and differing measuring angles (b).

**Figure 5.** Illustration of different elevation and depth levels relevant for the pond depth determination as described in the text.
time in melt season before the ice gets permeable enough to allow for pond drainage (cf. stage I, Eicken et al., 2002). Hence, we calculated relative pond depth without an absolute reference. To this end, the water level in each pond was determined by its height in the DEM at the edge of the pond. The method, therefore, highly benefits from the optical aerial images enabling high-resolution surface type classification with PASTA-ice (described in the next section) on exactly the same raster as the reconstructed topography data. We derived the pond margins as vectors (linestrings) from the classified images and overlaid the photogrammetrically retrieved DEM raster data $T(X,Y)$ with the pond margins. Then, we extracted the relative height of the pond surface $h_{surf}$ at the pond margin from the DEM. This was done using the Python libraries geopandas, rasterio, and rasterstats (Jordahl et al., 2020; Perry, 2015; Gillies, 2013). The two-dimensional bathymetric map $B(X,Y)_i$ of each individual pond $i$, with $X$ and $Y$ as geographic North and East coordinates in the projected coordinate system, was subsequently retrieved from:

$$B(X,Y)_i = -(h_{surf}_i - T(X,Y)) \cdot n_{water}$$  

(5)

where $n_{water}$ is the refractive index of water as depth correction factor as discussed in the previous section 3.2.2. Depth is specified positive down. Last, we compiled a pond-depth corrected topography map $T_{pond}(X,Y)$ from the individual pond bathymetries.

### 3.4 Pond classification with PASTA-ice

For the automatic detection of ponds in aerial images, we used the Proportional Analysis tool for Surface Types in Arctic sea Ice images (PASTA-ice, Fuchs (2023a), previously used in Thielke et al., 2023; Niehaus et al., 2023). In the following, we shortly summarize the algorithm due its importance for the workflow automation. Details are found in Fuchs (2023c).

PASTA-ice is tailored to the aerial images captured with the AWI imaging system. Besides focusing on the semantic separation into surface type classes, the algorithm aimed at retracing pond outlines used to extract pond levels and for the compilation of statistics on individual ponds. Image classification is done pixel-wise in brightness-corrected orthomosaics (e.g., Neckel et al., 2023) based on absolute R, G, B values and ratios thereof (Table 2).

Classification is performed with the random forest classifier implementation in Scikit-learn (Pedregosa et al., 2011). The classifier was trained and tested with data from manually selected areas in very diverse sea ice surface appearances recorded during PS106. Pixels in orthomosaics are classified into nine different sea ice surface sub-classes that belong to four main classes (Table 3). Adjacent pixels of similar main classes are subsequently combined into main class objects if these consist of, at minimum, 100 pixels (similar to Huang et al., 2016). This threshold is applied as a minimum area requirement to match the baseline of high-resolution data that objects are resolved from various pixels (e.g., Wright and Polashenski, 2018). The chosen threshold corresponds in the orthomosaics of this study to an area of approximately 1 m$^2$. Smaller objects are considered noise and are added to the largest adjacent object.

For spatial analysis, main class objects are converted to polygon geometries defining the outer and, if present, inner edges of the object. They also include an attribute table, that contains information on the sub-class proportions and a classification confidence proxy from the prediction probability output of the classifier (Fuchs, 2023c). Classification recall and precision are
Table 2. Pixelwise input features to classification scheme

<table>
<thead>
<tr>
<th>Feature</th>
<th>Equation</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Red</td>
<td>R_8bit</td>
<td>Standard</td>
</tr>
<tr>
<td>Green</td>
<td>G_8bit</td>
<td>Standard</td>
</tr>
<tr>
<td>Blue</td>
<td>B_8bit</td>
<td>Standard</td>
</tr>
<tr>
<td>BR1</td>
<td>G−R/G+R</td>
<td>(Wright and Polashenski, 2018)</td>
</tr>
<tr>
<td>BR2</td>
<td>B−R/B+R</td>
<td>(Miao et al., 2015)</td>
</tr>
<tr>
<td>BR3</td>
<td>B−G/B+G</td>
<td>(Miao et al., 2015)</td>
</tr>
<tr>
<td>BR4</td>
<td>G−R/2B−G−R</td>
<td>(Miao et al., 2015)</td>
</tr>
<tr>
<td>BR5</td>
<td>B + G − 2R</td>
<td>New</td>
</tr>
</tbody>
</table>

Table 3. Sea ice surface type classes used in the classification tool PASTA-ice to semantically segment orthomosaics.

<table>
<thead>
<tr>
<th>Main surface type class</th>
<th>sub-classes</th>
<th>notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>snow/ice</td>
<td>snow / white ice</td>
<td></td>
</tr>
<tr>
<td></td>
<td>bare/wet ice (greyish)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>bare/wet ice (blueish)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>shadow on snow/ice</td>
<td></td>
</tr>
<tr>
<td>ponds</td>
<td>bright blue ponds</td>
<td></td>
</tr>
<tr>
<td></td>
<td>dark/grey ponds</td>
<td></td>
</tr>
<tr>
<td></td>
<td>shadow in pond</td>
<td></td>
</tr>
<tr>
<td></td>
<td>submerged ice</td>
<td>pure optical classification, not location dependent</td>
</tr>
<tr>
<td>open water</td>
<td>open water</td>
<td></td>
</tr>
<tr>
<td>submerged ice</td>
<td>all pond subclasses</td>
<td>pond objects located between snow/ice and large open water areas (post processing)</td>
</tr>
</tbody>
</table>

rather limited for the very specific sea-ice surface subclasses listed in Table 3 due to overlaps in appearance, but high for the combined main classes (Fig. 6). High accuracy values are a result of large sample sizes, resulting in large numbers of true negative pixels. All pond objects are reclassified to submerged ice, if they are located spatially between a snow/ice and open water object and if the open water object is larger than the pond object.

The polygons of ponds, i.e., their outlines defined by vertices and connecting edges that resemble the snow/ice to pond interface, are used to extract the pond level from the DEM. The very high accuracy in the classification of the main classes indicates a sufficient detection of the transition areas from pond to ice and thus of the pond polygons.
Pond margins in the PS106 study area were traced manually in orthomosaics using QGIS 3.4 (QGIS Development Team, 2020) to better assess the depth correction algorithm without the impact of any classification inaccuracies expected in this particular study area (traced polygons shown in the study site overview, Fig. 1). Due to the deformed ice surrounding this specific location, shadows tended to impact the automatic classification scheme in PASTA-ice on this small scale, which eventually could strongly falsify the pond exterior detection needed to derive $h_{\text{surf}}$. Especially since misclassified shadows that stretch from ponds into adjacent ridges can be partially far above the water level. In larger sample sizes and more even ice areas, where most ponds usually form during summer melt, automatic surface classification with pond margins detection is easily possible, as shown in Section 5 with the MOSAiC data.

Missing GCPs and slightly arbitrary camera optics caused by a bubble-shaped protection window in front of the moveable mounted camera - for shock protection - furthermore led to large-scale deviations like curved and tilted surfaces in the Agisoft DEM retrieval of the PS106 data (Fig. 7). These deviations were approximated as a linear slope on the length scales of ponds. As a correction, we fitted a two-dimensional plane through each pond outline in the DEM. This regressed plane is assumed to represent the water level $h_{\text{surf},i}$ in equation 5.

$$h_{\text{surf},i}(X,Y) = a \cdot X + b \cdot Y + Z$$

$Z$ is the absolute height correction resulting from the mean vertical deviation of the retrieved surface from sea level. This mean vertical deviation is mainly caused by the inaccurate GPS altitude in higher latitudes. Height levels along the corrected pond edge deviate only slightly from zero (mostly less than $\pm 0.05$ m) as shown in the box-and-whisker plots in Fig. 8. In bending-free DEMs (e.g., the ones from MOSAiC presented below), the reference height can be derived solely from the mean elevation of the pond outline $h_{\text{surf},i}$.
Figure 7. Photogrammetrically reconstructed DEM of the study site on 14 June 2017 with marked ponds. Missing GCPs led to a strong tilt of the surface. Inaccurate GPS heights and reconstruction in the WGS84 ellipsoid cause an absolute offset from 0 m.

Figure 8. Deviation of the pond outline topography to the fitted pond surface plane on 10 June 2017 (a) and 14 June 2017 (b).

4 Results of the method development

4.1 Photogrammetrically derived pond depth on PS106 compared to manual measurements

Bathymetric charts of ponds in the study area were calculated from aerial images for all manually sampled ponds as previously described (Fig. 9). To account for the location inaccuracy of the in situ data, photogrammetrically derived pond depth data were averaged in a circle with radius 0.3 m around the point measurements (Fig. 9).

In situ and photogrammetry yielded almost identical pond depths (Fig. 10). The original pond color (see Fig. 1) indicated by the color of the dots (blueish, bright, or greyish, dark ponds) in Fig. 10 does not affect the reconstruction. However, pond
Figure 9. Photogrammetrically derived pond bathymetry charts of all ponds in the study area, for which in situ data (dots) were available. The radius of the gray circles shows the area used for averaging the photogrammetrically derived depths before comparing them to the in situ data.

size shown by the size of the dots in Fig. 10 seems to have one specific influence on the reconstruction: small ponds (<1 m in diameter), indicated by tiny dots, are underestimated in their pond depth. As bias of the measurement method, we retrieve $\text{BIAS} = -1.2 \times 10^{-3}$ m with a root mean square error of $\text{RMSE} = 3.84 \times 10^{-2}$ m and mean absolute error of $\text{MAE} = 2.65 \times 10^{-2}$ m.

4.2 Photogrammetrically derived pond depth on MOSAiC compared to echosounding data

It was noted above that ridge structures directly adjacent to the ponds at the PS106 study site required a manual tracing of pond polygons to get a precise reference water level. Improved flight patterns during the MOSAiC expedition (mowing-the-lawn pattern) with regular lateral and forward overlap in images together with well classifiable surface conditions increased the capability of the algorithm to work entirely autonomously. We evaluate the photogrammetrically derived pond depths with the newly developed autonomous pond investigation system Böötle, equipped with a downward-facing echo sounder (Oppelt and Linhardt, 2023). We compare pond depths of a lake-like pond Mystery lake which reached depths of more than 2.5 m. It was regularly mapped during helicopter survey flights and with the Böötle. We chose the two datasets collected closest in time on 7 July 2020 (helicopter survey) and 9 July 2020 (echosounder measurements). However, the temporal difference of two days restricts us from retrieving precise errors and corrections while we can still use it to confirm the overall method. The comparison is particularly interesting because the pond exceeded the maximum depths assumed in the method development, and due to smaller lateral image overlap, the opening angle in the acquired images could not be limited to 40°. Figure 11 displays the comparison of the photogrammetrically derived and echosounding pond depths. Overall, both methods agree in
Figure 10. Pond depth comparison between ground truth data and photogrammetrically derived bathymetry. Colors of the dots indicate the original color of the ponds (blueish, bright, or greyish, dark ponds), see Fig. 1. Size of the dots indicate melt pond size ranging from 0.5 m$^2$ to 116.9 m$^2$.

pond depths for Mystery lake. Yet, the data show a divergence at greater depths (>1 m) that can be attributed to either the further deepening of the pond within the two days or a systematic underestimation of the reconstructed depth, or both. This can be attributed to the unrestricted opening angle which would require a larger correction factor than applied. The percentage deviation was -11.5% at depths below 1 m and raised to -24.2% in greater depths.

4.3 Impact of flight pattern

Since mowing-the-lawn is among the most time-consuming flight patterns, we further determined to what extent other flight patterns, for example, straight flight legs with sufficient forward overlap, also lead to reasonable results. We investigated based on pond #1 (10 June 2017), how the measurement accuracy depended on the overlap of images and the lateral offset of the flight lines. Figure 12 shows bathymetric charts of pond #1 retrieved from (a) a few measurement positions along a straight line (4 images), (b) more measurement positions along a straight line (10 images), (c) similar measurement positions with lateral offset (9 images), (d) many measurement positions with lateral offset respectively all available measurement positions as used for the comparison with in situ observations before (31 images). The camera matrix and image recording positions were optimized before and kept constant during this study to not impact the error. The accuracy strongly increases with an increasing amount of measurement positions, larger incident angles, and especially, lateral offset of the measurement positions when comparing
measurement positions on one straight line or isotropically distributed over the pond (Fig. 13). A reconstruction from 10 images recorded along a straight line yield a higher error of 7.90 cm compared to 9 images with both, lateral and forward overlap (6.98 cm). The quantitative differences are still small, while subjectively, the differences in Fig. 13 even exceed these error estimates. Lateral offset can best be achieved with a mowing-the-lawn flight pattern.

5 Melt ponds on the MOSAiC floe

Regularly flown floe grids during MOSAiC (with mowing-the-lawn flight pattern) in combination with the newly developed pond bathymetry retrieval enable an unprecedented three-dimensional analysis of melt ponds. Given that with the flight pattern, lateral and forward overlap in images was achieved, and owing to open water areas around the major floe and the DEM correction with ALS data by Neckel et al. (2023), a leveling of all data to sea level was possible. To do so, we fitted a flat plane through all snow/ice–open water edge positions in the DEM around the floe and subtracted it from the DEM. For the first time, we could thus retrieve pond level to sea surface height and track pond level changes from flight to flight with aerial imaging.

5.1 Evolution of pond coverage, bathymetry, level and volume

The first pond formation on the MOSAiC floe happened already in May 2020 as observed from satellite images (Webster et al., 2022), at the time of the pandemic-related absence of RV Polarstern from the MOSAiC floe for crew exchange. After
Figure 12. Photogrammetric pond bathymetries of pond #1 (10 June 2017) derived from different subsets of image recording positions used in the reconstruction. (a) reconstructed from 4 images along a straight line with almost nadir measurements. (b) reconstructed from 10 images along a straight line. (c) reconstructed from 9 images scattered above the pond, almost nadir measurements. (d) reconstructed from 31 images scattered all around the pond. Shown RMSEs are given in centimeters.

Figure 13. RMSE of pond nr.1 depths (10 June 2017) derived from the comparison of in situ measurement points to derived pond depths with the same logic as in Fig. 10. Shown are RMSEs for different subsets of image recording positions used as input to the reconstruction. Differentiation is made between points along a single line and points scattered isotropically above the pond. The smaller the smallest measurement angle, the farther away the most distant recording point is and the larger the offset.
Table 4. Pond coverage on the MOSAiC leg 4 floe retrieved from helicopter aerial imaging and PASTA-ice classification on three different days. Numbers in brackets depict the confidence range obtained from a newly developed confidence evaluation (section 3.4).

<table>
<thead>
<tr>
<th>Day</th>
<th>Pond coverage</th>
</tr>
</thead>
<tbody>
<tr>
<td>30 June 2020</td>
<td>22.3% [21.3%, 26.0%]</td>
</tr>
<tr>
<td>17 July 2020</td>
<td>22.0% [20.9%, 24.3%]</td>
</tr>
<tr>
<td>22 July 2020</td>
<td>23.7% [22.9%, 27.6%]</td>
</tr>
</tbody>
</table>

The return in mid-June, continuous pond formation was observed. Pond coverage on the MOSAiC floe between end of June and late July varied between 22.0% to 23.7% (Table 4). End of June, the pond cover was well developed and amounted to 22.3% (Fig. 14). Mid-July (11-13), most ponds drained (Webster et al., 2022). Having orthomosaics of the entire floe from 30 June 2020, 17 July 2020 and 22 July 2020 (Fig. 14), we thus lack comprehensive aerial data directly before drainage. However, already on 30 June, large ponds in the center of the floe were exceptionally deep with partially more than 2 m (Fig. 14). After drainage, the pond cover was more fragmented and braided-like, with more shallower ponds (<1 m) in the center of the floe. A direct comparison of the conditions before and after the drainage event shows that individual ponds in the strongly deformed center of the floe and smaller ponds have remained unchanged in their shape or have even grown. All prominent large ponds on the floe underwent major changes during drainage and show bare patches of ice that were formerly submerged under pond water. Nevertheless, total pond coverage was relatively constant at 22 % at the time of the three measurement flights (Table 4). A possible underestimation of the pond coverage from the PASTA-ice classification was relatively high on 30 June 2020 and 22 July 2020 with 3.7 % and 3.9 %, respectively. This possible underestimation was presumably caused by small pond objects in the classification output that were below the 100 pixels minimum threshold for objects to be resolved as described in the method section.

Previous studies found that pond surfaces before drainage were vertically elevated forming a hydrostatic head (e.g., Perovich et al., 2021, based on SHEBA data). On the MOSAiC floe, on 30-June, two weeks before the main vertical drainage event, we find, in contrast, that 90.1% of the total pond area was already close to sea level (less than 0.2 m above sea level). Only a few small ponds (7.1% of the total pond area) in the strongly deformed center of the floe were well above sea level (more than 0.3 m above sea level). The 50 largest ponds (covering 64.7% of the total pond area) were closer to sea level and therefore had a low hydrostatic head.

The partitioning of melt water has raised particular interest on MOSAiC, since distinct freshwater lenses were observed around and below the floe, strongly impacting the physical and biological sea-ice system (Smith et al., 2023). Melt ponds form a reservoir in the melt water budget. Their bulk volume is therefore of great interest to better assess and understand the total budget. Having derived pond bathymetry maps of the entire floe, we can for the first time derive the overall volume of this meltwater reservoir directly, in contrast to extrapolating it from single transect lines, which was the only available method before (Perovich et al., 2021; Webster et al., 2022). The bulk volume of melt water in ponds on the floe results from the pond bathymetry and the area covered by ponds. Deriving it as area-specific value, we find that pond volume on the entire floe was...
Figure 14. Pond bathymetry (a) and pond level above sea surface height (b) reconstructed from airborne survey flight MOSAiC floe grid, PS122-4_45-36 on 30 June 2020, and pond bathymetries from flights 17 July 2020 and 22 July 2020 (orthomosaics and DEM from Neckel et al. (2022)). The background shows the orthomosaic (UTM31N projection) of the respective day. Pond edges were detected automatically using the PASTA-ice surface type classification.

The mean pond depth has not changed much either, which was driven by a large-scale deepening of ponds after the drainage, which compensated for the disappearance of the particularly deep ponds.
5.2 Comparison to other in situ and satellite observations

Measurements on MOSAiC were carried out using many different methods and may therefore lead to different results. In the following we compare the aerial derived data to available results from high-resolution satellite observations classified with OSSP (Wright and Polashenski, 2018) and in situ transect lines (both Webster et al., 2022) to assess the accuracy of our results and the representativeness of observed areas. Transect lines were repeatedly revisited paths on which extensive in situ measurements of ice thickness, snow and ponds were carried out. The transect considered here was the longest and surrounded the entire floe (Webster et al., 2022, Fig. 2). To compare to this transects, we derived pond properties additionally within a 10 m buffer zone around retraced transect footpaths in the aerial images. Satellite and aerial derived pond coverage of the floe is temporally sparse, but very similar. Also along the transect lines, helicopter-derived pond coverage resembles the in situ observed coverage well (Fig. 15a). Small under- and overestimations occur, probably caused by collocation inaccuracies. However, it becomes apparent that along the floe edge pond coverage increased from 10 % in the end of June to 20 % in mid July and thus acted differently from the relatively constant pond coverage of the entire floe.

Pond depth along the transect line was observed about 2.5 cm higher (≈15 % to 20 %) than the mean derived pond depth for the same area from the aerial derived bathymetric maps (Fig. 15b). The (very variable) pond depth on the entire floe is underestimated by the transect area in June and matches well in July after drainage, probably because the extraordinary deep ponds in the floe center flattened making the pond cover more uniform. Both methods were able to resolve a slight increase in pond depth at the floe edge. Before harmonization through the drainage event, the very deep ponds in the middle of the floe, a region not covered by the transect studies, cause a more constant pond volume than extrapolated by Webster et al. (2022) from the transect area (Fig. 15c). Good agreement between both methods along the transect lines suggests that differences occur mainly due to different observed areas instead of methodical differences.

5.3 Upscaling factor for in situ depth measurements

In situ measurements in ponds are often restricted to very few, single points. We investigate whether and how mean pond depth of entire ponds can be extrapolated from single in situ point measurements by subsampling our high-resolution photogrammetric pond bathymetry reconstruction. To this end, we benefit from the unprecendented data set, both in resolution within ponds and in the total number of ponds.

We subsampled pond depths from survey flights on 30 June 2020 (pre-drainage) and 22 July 2020 (post-drainage). For each pond, we extracted the point which is furthest away from the pond edge as the pond center, the so-called pole of inaccessibility (PIA). We assumed that in situ depth measurements are normally performed at this point, expecting the most representative depth in the center. All pond objects on the major floe classified with PASTA-ice were considered. Except to prevent errors caused by smoothing of the DEM in small ponds, ponds with a maximum distance between center and pond edge of <1 m were neglected. In total, the evaluation was based on 1.6×10⁶ pixels in 1621 aerially observed ponds. A selection between older and younger ice was based on personal testimonies reporting a young ice area in the south of the floe (orientation of the floe in June/July 2020) and older ice in the center.
Comparing mean pond depth $d_{\text{mean}}$ derived from the entire pond bathymetries with single pond depth measurements in the center $d_{\text{center}}$ reveals that a single measurement in the center of the pond strongly overestimates the mean depth. On average, $d_{\text{mean}}$ is only 52\% of $d_{\text{center}}$ (Fig. 16). Hence, the mean pond depth, and with it also pond volume, is much smaller than assumed based on single measurements from the center of the pond. A descriptive form factor $\kappa$, which we define as

$$\kappa = \frac{d_{\text{mean}}}{d_{\text{center}}} = 0.52$$

and retrieve from

$$\kappa = \frac{1}{n} \sum_{i=1}^{n} \left( \frac{d_{\text{mean}}}{d_{\text{center}}} \right)_i$$

including all $n = 1621$ ponds, shows strong statistical significance in the large data set. Residuals of the linear fit and thus deviations from this generalization are normally distributed (Fig. 17), independently if all ponds are considered (Fig. 17b), or if
subsets are taken for ponds in pre- and post-drainage state (Fig. 17f) or on younger, less deformed (FYI) or older, strongly deformed (MYI) ice (Fig. 17d). Furthermore, residuals neither correlate with the pond area (Fig. 17a), nor the maximum disk area from which the single depth measurements are taken (Fig. 17c), nor the pond roundness (defined here as \( \frac{\text{max. disk area}}{\text{pond area}} \)) (Fig. 17e), nor the single depth measurement (Fig. 17b), nor the drainage state (Fig. 17f). Only ponds on young ice seem to develop a slight dependency of the form factor fit residuals from the pond depth with a Pearson correlation coefficient of -0.41 (Fig. 17d). From this robust relationship between \( d_{\text{center}} \) and \( d_{\text{mean}} \) independent of the pond type, we conclude that the descriptive form factor \( \kappa=0.52 \) can be used to upscale single point measurements from the center of the pond (pole of inaccessibility) to mean pond depth.

The introduced form factor describes the average relationship between center depth and mean depth. For individual ponds, deviations may occur as indicated by the residuals of the fit. We explore at which number of sampled ponds, the form factor becomes a valid estimator for the mean pond depth of multiple ponds. We calculated the form factor for 100 randomly chosen subsamples of different sizes \( n \) from the 1621 ponds, similar to bootstrapping. The defined goal was that 99.3 % of the retrieved form factors within the 100 random samples are located within the range of ±10 % of the form factor \( \kappa=0.52 \). Figure 18 shows the box-and-whisker plots for different pond sample sizes \( n \), retrieved from the 100 random samples per size \( n \). The upper and lower whiskers define the 99.3 % range. It can be seen that from 64 ponds on, the requirement is reached. Thus, at least 64 ponds are needed to yield a valid approximation of the mean pond depths from single point measurements in the center of the ponds applying the form factor \( \kappa \).
Figure 17. Residual analysis of the linear fit given in Fig. 16. Residuals of all ponds are shown in respect to their area (a), center depth (b), PIA disk area (c), center depth and ice age (d), pond circularity (e), and center depth together with drainage stage (f). Histograms on the right side show the distribution function of the residuals (b) of all data, (d) separated by the ice age, and (f) separated by drainage stage. Pond circularity is the ratio between the max. PIA disk area and pond area, indicating the shape complexity of the pond.

6 Discussion

6.1 Photogrammetric reconstruction workflow for melt pond bathymetries

Photogrammetry can be used to reconstruct the sea ice surface topography from aerial images (Neckel et al., 2023; Divine et al., 2016). In the first part of this study, we investigated the ability to also reconstruct the full melt pond bathymetry. In particular, we have developed methods to consider water in the light paths used for reconstruction, in addition to air. We developed the methods for PS106 data. More extensive processing was necessary, including corrections due to curved DEMs and the manual digitization of the pond edges. The evaluation of MOSAiC showed that these were no longer required with better data quality through adapted flight patterns and also better classifiable images. We thus present an algorithm that can be adapted depending on the quality and method of the recorded data. In the following, we discuss more specifically the results obtained for the bathymetry reconstruction.
6.1.1 Impact of sky conditions, pond color, size, and shape

Within the presented dataset, no difference in the accuracy of the depth retrieval could be traced back to sky conditions or pond colors. However, we identified potentially larger uncertainties for very small and large ponds. Ponds smaller than 1 m in the horizontal expansion (equalling <10 times the ground sampling distance) were not properly reconstructable. We hypothesize that the essential smoothing of the image depth maps flattens the topography in such small ponds. Further, on very large ponds, we assume that wind fetch causing ripples to form on the water surface can lead to disturbing reflections. In a weak form, this effect was observed on the above-mentioned Mystery Lake (diameter approx. 80 m) on the MOSAiC floe, but it was not strong enough to degrade the quality of the retrieval.

In addition, unavoidable smoothing of the topography in the photogrammetric calculations also may lead to larger uncertainties for steep pond bottom slopes at the outer edges of ponds. Too little measurements were available to evaluate this quantitatively. However, comparing the results visually to data presented in König et al. (2020), we observed such effects. Since their method relies on spectral differences, it does not smooth the bathymetry toward the pond edges.

6.1.2 Accuracy of the in situ data and suggestions for future field campaigns

The accuracy of photogrammetrically derived pond depths was obtained in comparison to in situ measurements as ground truth. As discussed in König et al. (2020), those measurements also contain substantial sources for errors, namely metersticks that slip into cavities and the complex retracing of in situ measurement points in the airborne data. To compensate for the latter, we averaged above a circular area with radius 0.3 m around the in situ points. For future campaigns, we nevertheless strongly recommend a sophisticated system to allow for a direct georeferencing link between in situ and airborne data. A pure GPS-based method proved to be insufficient on the constantly drifting ice. Therefore, we recommend a system consisting of
GPS base stations that are recognizable in images and both record the geographic position in the earth system and act as optical (and topographical) GCPs. These reference stations must encompass the measurement area so that in situ measurements within the study area can be efficiently and accurately triangulated between these points. The best choice of tools, e.g., 360° cameras, theodolites, or low-range indoor positioning systems like Bluetooth beacons needs to be tested. To reduce the error from meterstick point measurements, caused by rippled or porous ice, we recommend the usage of a flat plate at the bottom of the depth gauge on future campaigns. This could, however, possibly lead to photogrammetric measurements slightly overestimating the pond depth since the optical transition layer is probably located somewhat deeper than the upper haptic transition between pond water and ice. This requires further testing. It has also been shown on MOSAiC that measurements with echo sounders from remote-controlled boats can be used as a reference. Yet, even acoustic systems, especially in the high-frequency range of 500 kHz as implemented on the Böötle on MOSAiC, do not always detect the exact transition from water to ice as shown under laboratory test conditions (Werner, 2022). In general, we assume that in situ reference depths, both from manual and acoustic measurements, are slightly overestimated by a few centimeters, if at all and are therefore a good means of testing the algorithm for simultaneous flights. The acoustic measurements in this study, however, could only be used to confirm the great depths in the observed ponds and derive trends, but no exact error could be derived due to the time lag of two days.

6.1.3 Required flight pattern

Our results suggest that pond depth studies require flight grids with great overlap of adjacent images. The more lateral offset is achieved in addition to forward overlap in the flight direction, the higher the accuracy of the pond depth measurements. However, simultaneously we showed, that small measuring angles, i.e., large aperture angles should be avoided, as they lead to a greater underestimation of depths due to light refraction. This effect is most likely responsible for the observed discrepancies between the in situ (echosounder) and aerial pond depths in the deep parts of Mystery lake on MOSAiC, besides ongoing melting between the observing times. To achieve a high overlap and lateral offset at small measuring angles, aerial images need to be captured with a high measurement frequency or at a low flight speed. To give an example for flight planning, the system we used on MOSAiC is limited to a measurement frequency of 0.25 Hz. To obtain a reasonable ground sampling distance of 5 cm, the camera resolution limits flight altitude to 100 m (300 ft). A circle with the maximum angle of incidence of the measurement of 40° that we defined to prevent errors in the photogrammetric reconstruction from light refraction then has a ground radius of 84 m. It is commonly recommended for photogrammetric measurements, to use 80% forward and 60% lateral overlap in images for optimal reconstruction. Maximum flight speed would thus be limited to 4.2 m/s (8 kts) and the lateral offset of flight lines to 33.6 m. Fortunately, state-of-the-art aerial imaging systems can provide sufficiently higher temporal and therefore also spatial measurement frequencies to facilitate measurements.

6.2 MOSAiC melt pond bathymetry

The second part of the study applies the developed method on data from the MOSAiC campaign. Here, we discuss the major results from that unprecedented insight into temporal and spatial pond evolution and compare it to conventional measurement methods.
6.2.1 Pond bottom and level evolution

The large scale and high-resolution observation of ponds on the MOSAiC floe points to several previously unconsidered melt-season processes. Firstly, large ponds on level ice in the deformed center of the MOSAiC floe were extraordinarily deep (>2 m) before the drainage event. Most interestingly, they were thus as deep as the level ice on which they formed was thick (e.g., Itkin et al., 2023; Thielke et al., 2023; von Albedyll et al., 2022), while the pond bottoms themselves still consisted of 1 m and thicker ice, as anecdotal reports from the field showed. After drainage, pond bottoms even of previously deep ponds surfaced, although pond level was close to sea level before. Both these observations are indications for a flexible ice cover (as shown in Fuchs, 2023c) and contradict the traditional assumption of a rigid ice cover on which ponds only reduce to their lowest points during the drainage event (e.g., Popović et al., 2020).

Secondly, it was mostly assumed or observed so far, that pond surfaces are well above sea level before drainage (e.g., Polashenski et al., 2017; Perovich et al., 2021). This was the case only for a few small ponds in the deformed center of the floe. Only their bottom ice seemed to be impermeable and rigid enough on MOSAiC to resist the hydrostatic head that forms when ponds are above sea level. Even before the drainage event, the largest pond with water level >0.2 m higher than sea level had an exposed water surface of 13.4 m meters in diameter (disk size around the pole of inaccessibility). 46 ponds on the MOSAiC floe were larger but their pond level was closer to sea level on 30 June. This indicates that especially large ponds have little possibility of being far above sea level and that blockage processes reducing permeability (Polashenski et al., 2017) are not able to fully sustain impermeability of the underlying ice. Rather, we speculate that a balance of water inflow and outflow to ponds is established (lateral, vertical and melting), allowing a pond level only minimally above sea level. Or, alternatively, that especially in large ponds the bottom ice can bend downwards under the load of accumulated meltwater and thus reduce the surface elevation, while the hydrostatic head, causing the bending, is still higher (as discussed in Fuchs, 2023c). However, more detailed investigations of the mechanical properties of the melting ice are required in order to break down the individual contributions of the processes to the observed results.

The here presented observations of the temporal and spatial pond bathymetry evolution indicate that the pond bottoms can bend downwards under the weight of the accumulated meltwater and, after drainage, when the ice is very permeable, bend upwards due to the buoyancy of the ice. This flexibility must be considered when observing hydrostatic heads in the fields and parameterizing the pond development in models.

6.2.2 Representativeness of in situ studies

In situ transect studies are among the most common methods to collect representative in situ data during sea ice physical field campaigns. The entire sea ice column, including snow depth, pond depth, and ice thickness, can be probed on walked transect lines, providing comprehensive data on the properties of the atmosphere, snow, ice and ocean, as well as transition zones between. However, already Perovich et al. (2003) noted that pond coverage along their transect line on the SHEBA campaign (Uttal et al., 2002) with a peak coverage of 40 % was not representative for the entire SHEBA site, for which they retrieved a comparable smaller and more constant pond coverage of less than 24 % from aerial imaging (Perovich et al., 2002). Also, on
MOSAiC, differences were found in the derived pond coverage between the walked transect line and high-resolution satellite imagery covering the entire floe (Webster et al., 2022). Webster and colleagues attributed a comparably smaller pond coverage along the transect line to its location close to the floe edge, where lateral runoff of meltwater is known to reduce pond coverage (e.g., Wright et al., 2020). Collocated transect and airborne measurements are rare, as they are only possible with enormous effort on large-scale field campaigns or require high-resolution satellite imagery in clear sky conditions, which has become available only in recent years. For this reason, combinations of both, such as those listed previously, are rare, and we know of no study in which both methods have been combined with a focus on comparing them instead of broadening the data source. Owing to the data available from Webster et al. (2022), we could, therefore, for the first time include a systematic comparison of derived geometric pond properties between both measuring methods. The presented results have shown that in situ transect measurements show slightly higher average pond depths in comparison to airborne derived and were not representative for the entire floe before drainage. Slightly greater depths can be expected from manual in situ measurements due to uneven pond bottoms mentioned above. However, we noticed that mean pond depths are apparently commonly derived by averaging depth profiles along single lines through ponds. We would like to point out that the use of a single line to infer the average pond depth is mostly geometrically incorrect due to the rather round shape of the ponds and possibly overestimates the mean pond depth. Shallower areas at the pond edges are underrepresented in such an extrapolation process.

Because of the possible overestimation of mean pond depth by in situ studies, we investigated the possibility of extrapolating mean pond depths of a large number of ponds from single in situ measurements at their center point. On average, the introduced form factor $\kappa=0.52$ indicated a strong correlation between pond depth at the center and mean pond depth. In the center, ponds were about twice as deep as on average, largely independent of other factors such as shape, depth, ice deformation, or stage of evolution. This result, collected from a sample size of 1621 ponds, could help to improve mean pond depth estimations in the field where a complete manual assessment of the pond bathymetry is not feasible due to the limited workload, especially for a larger amount of individual ponds. Measuring only one depth per each of these ponds at the relatively easy findable spot pole of inaccessibility and estimating the mean pond depth using the pond form factor could massively increase the representativeness of the measurement for the mean pond depth.

## Conclusions

We proved that pond bathymetry can be accurately derived from a photogrammetrical reconstruction of the ice surface. Aerial images from a monocular airborne camera in motion are sufficient, provided that strong overlap is given between single images. A simple multiplication of the derived water column depth with the refraction index of water ($n=1.335$) sufficiently corrects measured pond depths for light bending at the water–air interface. This factor naturally varies depending on the angle of incidence of the measurement. Still, here it has been shown that a constant factor is sufficient to be used subsequently to the complex bundle-block-adjustment in Agisoft Metashape, which favors nadir measurements. Incident angles at the surface were restricted to smaller than 40° to avoid horizontal alignment errors becoming greater than the ground sampling distance. Deviating from this limitation possibly contributed to a slight underestimation of large depths in the MOSAiC data.
With the newly developed method, we could reconstruct the evolution of pond coverage, depth and volume on the MOSAiC leg 4 floe. The pond volume of the entire floe was more constant than found by Webster et al. (2022), who extrapolated it from a transect line around the floe. This difference was mainly caused by very deep ponds in the floe center that increased the mean area specific pond volume of the floe before drainage, when coverage was still slightly lower. Harmonization of the pond cover after drainage increased representativeness of the transect area. Furthermore, we could detect clear indicators for a flexible ice cover below the ponds and derive a scaling factor to retrieve mean pond depths from single pond depth measurements in the field.

The study showcases unexploited possibilities of aerial imaging of melt ponds. The developed methods and procedures allow pond bathymetry reconstruction solely from one optical camera deployed on a helicopter or airplane. The resulting availability and exact alignment of optical and morphological data provide a unique database that requires only relatively inexpensive instrumentation and evaluation software to be compiled. Although we used the commercial software Agisoft Metashape for the most complex processing steps, we would like to point out that there are open-source projects like MicMac (Rupnik et al., 2017) available which could further reduce the cost for such systems. Pre- and postprocessing is completely based on freely available Python and QGIS packages. The only change to previous campaigns, which eventually allows for the pond depth retrieval, is the appropriate design of the flight tracks. This approach is probably directly transferable to unmanned aerial vehicles (UAVs). Such a transformation from airplane-based observation to UAVs holds great potential for reduced emissions and an economically more friendly collection of sea ice observations. The data acquired during MOSAiC shows that the method enables multidimensional studies tackling questions far beyond the current scope.

**Code and data availability.** Code and files are made freely available for further use:

- The surface classification tool PASTA-ice is accessible under https://github.com/nielsfuchs/pasta_ice and https://doi.org/10.5281/zenodo.7548469 (Fuchs, 2023c, a).
- Training data for PASTA-ice are available under DOI: https://doi.org/10.5281/zenodo.7513631 (Fuchs, 2023b).
- MOSAiC DEMs and Orthomosaics used for the pond depth retrieval are available under DOI: https://doi.org/10.1594/PANGAEA.949433 (Neckel et al., 2022, 2023).
- Example code for depth determination from a DEM raster and a classification Shapefile is available in the above-mentioned PASTA-ice repository under helpful/PondDepth_retrieval/XX_process_ponds.py (Fuchs, 2023a).
- The compiled pond bathymetry maps are in the upload process to PANGAEA. The DOI will be included here before final publication.

**Video supplement.** For the EGU 2021 online meeting, we prepared an interactive online tour through the PS106 study site, on which one can learn about the pond bathymetry determination (Fuchs et al., 2021). The tour is available under https://nielsfuchs.github.io/egu2021_pond_bathymetry_tour/.
Appendix A: Calculations

The following geometric approaches were used to derive the horizontal and vertical mismatch caused by refraction in the photogrammetric depth calculations.

A1 Horizontal mismatch

From Fig. 2, one can geometrically derive a set of equations describing the different sections of $X$:

\[ X_{\beta_1} = \Delta X + X_{\alpha_1} = Z_{AP} \cdot \tan \beta_1 \quad (A1) \]
\[ X_{\beta_2} = X_{\alpha_2} - \Delta X = Z_{AP} \cdot \tan \beta_2 \quad (A2) \]
\[ X_{\alpha_1} = Z_{TP} \cdot \tan \alpha_1 \quad (A3) \]
\[ X_{\alpha_2} = Z_{TP} \cdot \tan \alpha_2 \quad (A4) \]

Equating these with $Z_{AP}$ results in:

\[ \Delta X = \frac{X_{\alpha_2} \cdot \tan \beta_1 - X_{\alpha_1}}{1 + \frac{\tan \beta_1}{\tan \beta_2}} \quad (A5) \]

By substituting $X_{\alpha_i}$ and applying Snell’s Law to replace $\beta$ by the known angle of emergence $\alpha$, equation A5 becomes:

\[ \Delta X = Z_{TP} \frac{\tan (\alpha_2) \cdot \frac{\tan (\arcsin \left( \frac{\sin \alpha_1}{n_{water}} \right))}{\tan (\arcsin \left( \frac{\sin \alpha_2}{n_{water}} \right))} - \tan (\alpha_1)}{1 + \frac{\tan (\arcsin \left( \frac{\sin \alpha_1}{n_{water}} \right))}{\tan (\arcsin \left( \frac{\sin \alpha_2}{n_{water}} \right))}} \quad (A6) \]

For this, we use the simplified image of opposite measuring points and two different angles of emergence on the pond surface.

A2 Vertical mismatch

The deviation in depth between measured and true depth is derived from geometric analysis of Fig. 2:

\[ X_2 - X_1 = Z_{AP} \cdot \tan \beta_2 + Z_{AP} \cdot \tan \beta_1 \quad (A7) \]
\[ X_2 - X_1 = Z_{TP} \cdot \tan \alpha_2 + Z_{TP} \cdot \tan \alpha_1 \quad (A8) \]

Equating both and including Snell’s Law leads to:

\[ \gamma = \frac{Z_{AP}}{Z_{TP}} = \frac{\tan \alpha_1 + \tan \alpha_2}{\tan \beta_1 + \tan \beta_2} \quad (A9) \]
\[ \gamma = \frac{\tan \left( \arcsin \left( \frac{\sin \alpha_1}{n_{water}} \right) \right) + \tan \left( \arcsin \left( \frac{\sin \alpha_2}{n_{water}} \right) \right)}{\tan \beta_1 + \tan \beta_2} \quad (A10) \]
We apply a limit value analysis for small incident angles. To do so, we first equate both measuring angles $\alpha_1 = \alpha_2$. This results in a simplified form of equation A10:

$$\gamma = \frac{\tan(\alpha)}{\tan\left(\arcsin\left(\frac{\sin(\alpha)}{n_{\text{water}}}\right)\right)}$$

(A11)

In this form, the equation is undefined at zero since $\tan(0) = 0$ and $\arcsin(0) = 0$. However, with a couple of rearranging tricks, one gets an evaluable formula form.

Inserting:

$$\tan(\arcsin(x)) = \frac{x}{\sqrt{1-x^2}}$$

(A12)

into equation A11 leads to:

$$\gamma = \frac{\tan(x)}{\left(\frac{\sin(\alpha)}{n_{\text{water}}}\right)\sqrt{1 - \left(\frac{\sin(\alpha)}{n_{\text{water}}}\right)^2}}$$

(A13)

by rearranging and the definition of the tangent we obtain:

$$\gamma(\alpha) = \cos(\alpha) \cdot \sqrt{n_{\text{water}}^2 - \sin^2(\alpha)}$$

(A14)

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